

1 **Behavioural synchronization in a multilevel** 2 **society of feral horses**

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14 **SUMMARY**

15 Behavioural synchrony among individuals is essential for group-living organisms. It is still largely
16 unknown how synchronization functions in a multilevel society, which is a nested assemblage of
17 multiple social levels between many individuals. Our aim was to build a model that explained the
18 synchronization of activity in a multilevel society of feral horses. We used multi-agent based models
19 based on four hypotheses: A) horses do not synchronize, B) horses synchronize with any individual
20 in any unit, C) horses synchronize only within units and D) horses synchronize across and within
21 units, but internal synchronization is stronger. Our empirical data obtained from drone observations
22 best supported hypothesis D. This result suggests that animals in a multilevel society coordinate with
23 other conspecifics not only within a unit but at an inter-unit level. In this case, inter-individual
24 distances are much longer than those in most previous models which only considered local
25 interaction within a few body lengths.

26

27

28 **Introduction**

29 Behavioural synchronization is the phenomena where multiple individuals perform the
30 same behaviours at the same time by mirroring each other, either consciously or unconsciously
31 (Duranton and Gaunet, 2016). The patterns of synchronous activity have been found in many
32 animals and with many different behaviours, from Placozoa to humans (Couzin, 2018). The
33 common property of this collective behaviour is that relatively simple interactions among the
34 members of the group can explain a global pattern of behaviour (Couzin and Krause, 2003). For
35 example, a pattern of fission-fusion in some ungulate species could be simply explained by the
36 dynamic tension between the advantages of aggregation and the disagreement among
37 mainly between female and males, due to the variation in resource demand (Bonenfant et al.,
38 2004; Mooring et al., 2005). Synchronization of behaviour is essential for animals to maintain
39 functions of a group, and thus enhance their fitness and survival (Duranton and Gaunet, 2016).
40 Fundamentally, animals need to synchronize the timing and direction of their movements to
41 an aggregation (Couzin and Krause, 2003). Furthermore, it has been reported that
42 synchronization can increase efficiency in their vigilance and defensive behaviours (like
43 mobbing) to predators (Kastberger et al., 2008), as well as facilitating social interactions and
44 enhancing social bonds (Ancel et al., 2009; McIntosh, 2006).

45 Many studies on synchronization were done on cohesive, single-layered groups, either
46 natural or experimental setup (Bialek et al., 2014; Kastberger et al., 2008; King et al., 2011;
47 Torney et al., 2018). In many social animals, social networks have a considerable effect on the
48 propagation of behaviour (Centola, 2010; Couzin, 2018; King et al., 2008; Papageorgiou and
49 Farine, 2020; C. Sueur et al., 2011; Sueur and Deneubourg, 2011). Socially central individuals
50 can have a greater influence on group behaviour than subordinate individuals (Sueur et al., 2012,
51 2009). Also, it is widely observed that socially affiliated dyads more intensely synchronize their
52 behaviours (Briard et al., 2015; King et al., 2011). However, most of these studies which
53 examine the social network effect were conducted on small, cohesive groups (but see
54 Papageorgiou and Farine, 2020) whilst studies with large groups of individuals were based on
55 anonymous mechanisms because of the difficulty in identifying and following all members.

56 Multilevel societies composed of nested and hierarchical social structures are
57 considered to be among the most complex forms of social organization for animals (Grueter et
58 al., 2020, 2017, 2012). In a multilevel society, the fundamental component is called as a 'unit',
59 and these units gather to form larger groups. It is often reported that the different units also
60 forage and sleep together (Papageorgiou et al., 2019; Swedell and Plummer, 2012). The most

61 famous example of multilevel society is the troop, a third or fourth level social organization, of
62 hamadryas baboons sleeping together in a cliff (Schreier and Swedell, 2009). It is highly likely
63 that synchrony occurs not only among the same units but also in a higher-level of social
64 organization, but studies on their synchronization mechanisms and functions are quite limited
65 (but see Ozogány and Vicsek, 2014).

66 Multilevel society is characterized by a different association pattern in each social level.
67 Usually, members of a unit stay close together, while the extent of cohesion becomes smaller
68 as the social level increases (Grueter et al., 2012; Maeda et al., 2021; Papageorgiou et al.,
69 2019; Qi et al., 2014; Snyder-Mackler et al., 2012). Some studies have found that different
70 units keep an intermediate distance from each other, staying farther apart than the
71 inter-individual distance within units (Bowler et al., 2012), but closer than random distribution
72 (Maeda et al., 2021). It is argued that this differentiation of social relationships has evolved to
73 balance the advantages of being a large-group and the disadvantages of resource competition
74 with other units (Moscovice et al., 2020; Rubenstein and Hack, 2004; Sueur et al., 2011). For
75 example, a study on golden snub-nosed monkeys (*Rhinopithecus roxellana*) suggested that
76 harem unit aggregation could reduce a risk of inbreeding and bachelor threat, but being a large
77 group may cause intense competition for food, so their aggregation pattern changes according
78 to the seasonal prevalence of resources (Qi et al., 2014). We assumed that this fission-fusion
79 patterns which balances competition and cooperation between units could be also applied to
80 behavioural synchronization. Whether multi-level societies show behavioural synchronization
81 remains unclear, but it is important to address this question in order to better understand the
82 collective features of such societies.

83 New technologies enable more wide ranging and accurate data collection in societies
84 with hundreds of individuals (Charpentier et al., 2021; Inoue et al., 2019; Schroeder et al., 2020).
85 For instance, our use of drones succeed in obtaining positional and behavioural data of a
86 multilevel society composed of more than a hundred of feral horses in Portugal and showed a
87 two layered structure of units (combinations of individuals which stayed closer than 15.5m
88 more than 70% of the time) nested within a herd (i.e. observed inter-unit distance was
89 significantly smaller than that of permuted data sets) (Maeda et al., 2021). In the current study,
90 we further apply this data collection to investigate whether horse multilevel society shows
91 synchrony in resting/moving timing, and if so, whether the extent of synchronization changes
92 within and across units.

93 We hypothesize that (1) horses synchronize their behaviour both at an intra- and

94 inter-unit level, and (2) the extent of synchronization in a dyad is correlated to its social
95 relationships. In this current study, we develop different models based on hypotheses ranging
96 from no synchronization between individuals and units to full synchronization, with
97 intermediate mechanisms based on social networks. In this way, we develop a stochastic
98 multi-agent based model where the probability of an individual to change stage (resting versus
99 moving) depends on different hypotheses: (A) Independent: horses do not synchronize and are
100 socially independent. This hypothesis is used as the null model. (B) Anonymous: horses
101 synchronize with any individual in any unit. This hypothesis does not include the importance of
102 stable social relationships in trade-off between group-living advantages and competition. (C)
103 Unit-level social: horses synchronize only within units, not considering the herd-level
104 association and without advantages of large societies. (D) Herd-level social: horses synchronize
105 across and within units, but internal synchronization is stronger (Figure 1). Hypothesis D could
106 achieve the best balance between the intra and inter-unit level associations. Finally, we
107 compared these models to the empirical data in order to assess which models best explain
108 synchronization in our population of feral horses.

109

110 **Method**

111 **(a) Data collection**

112 We conducted observations from June 6th to July 10th, 2018 in Serra D'Arga, Portugal,
113 where approximately 150 feral horses were living without human care (Ringhofer et al., 2017).
114 The field site had two large flat areas, Zone 1 and 2, which were visually separated by rocky
115 hills (see Figure 3 of Maeda et al., 2021). We separated these areas because we rarely observed
116 horses moving between them during daytime. We used drones (Mavic Pro: DJI, China) to
117 accurately measure distances between all individuals in the observation area of two zones
118 covering approximately 1 km² each. The flights were performed under clear sky conditions at an
119 altitude of 30–50 m from the ground and we took successive aerial photographs of the horses
120 present at the site in 30-minute intervals from 9:00–18:00 (for more detailed explanation see
121 Maeda et al., 2021). The average duration of each flight was 4 minutes 24 seconds ± 3 minutes
122 5 seconds.

123 Orthomosaic imaging was conducted using AgiSoft PhotoScan Professional software.
124 The software connected successive photos and created orthophotographs in the GeoTIFF format
125 under the WGS 84 geographic coordinate system. We first identified all horses from the ground
126 and made an identification sheet for all individuals, recording their sex (whether they had testes),

127 estimated age class, and physical characteristics such as colour, body shape, and white markings
128 on the face and feet (Fig. 2). The adults were individuals who experienced dispersal from their
129 natal group, the young were those who were born in or before 2017 and still belonged to their
130 natal group, and the infants were individuals born in 2018. All horses in the orthophotographs
131 were identified accordingly. We positioned the heads of the horses and recorded whether they
132 were resting or not. The horses were considered to be resting if they did not move in the
133 successive photos and showed resting posture, i.e., laying down or standing still with their neck
134 parallel to the ground. Otherwise, we considered them to be moving. All locations were stored
135 in shapefile formats. The coordinate system was converted to a rectangular plain WGS 84 /
136 UTM Zone 29N and we then calculated the distances between all pairs of individuals in the
137 same zone. In total, 243 observations were conducted in 20 days and a total of 23,716 data
138 points of individual positions were obtained (for detailed availability and number of
139 observations each day, see Figure S3). A total of 126 non-infant horses (119 adults: 82 females
140 and 37 males, 7 young individuals: 6 females and 1 male) and 19 infants (11 females and 8
141 males) were successfully identified. They belonged to 23 units (21 harems and 2 AMUs;
142 all-male unit), along with 5 solitary males. One adult female, named Oyama from Kanuma
143 harem, disappeared sometime between the evening of June 15th and morning of June 16th,
144 probably predated by wolves. We eliminated this female and two solitary males which never
145 located within 11m of other individuals from the subsequent analysis. We also eliminated
146 infants because their position was highly dependent on their mothers.

147

148 **b) Herd social network**

149 To create a social network, we first decided the threshold distance which defines the
150 association. We created a histogram of inter-individual distance data under the R environment.
151 The bin width was decided based on the method used in Wand (1999) and using R package
152 ‘KernSmooth’ (Wand, 2015). As shown in Figure 2, the histogram had two peaks – at the 2nd
153 bin (0.9-1.8m) and at the 55th bin (49.7-50.6m) with a bin-width of 0.92m. The minimum
154 frequency, or nadir, between these two peaks was observed at the 12th bin (10.1-11.0m), and we
155 selected this as the threshold distance that divides the intra- and inter-unit association (cf.
156 Maeda et al., 2021).

157 To obtain the social relationships for each dyad a_{ik} , networks were generated for each
158 sampling period (i.e., each flight of drones). Pairs of horses whose inter-individual distance was
159 smaller than 11 meters were assigned an edge weight of 1, based upon the threshold distance

160 defined above. When a pair of individuals were connected with each other indirectly via another
161 individual, they were also considered to be connected (edge weight = 1). All other pairs were
162 assigned an edge weight of 0. In the total number of drone flights, we detected 658 temporarily
163 isolated individuals who had no association with any other individuals. If the distance from the
164 nearest individual was smaller than p_2 (the second peak of the histogram), we presumed that
165 they had an association with the nearest neighbour, otherwise we eliminated them from the
166 analysis. 643 out of 658 isolated points were within 50.6 m (the second peak of histogram) from
167 the nearest individual. A social network was created from this co-membership data using the
168 simple ratio index (Cairns and Schwager, 1987). This calculates the probability that two
169 individuals are observed together given that one has been seen, which is widely used in animal
170 social network analysis. The density of the network was 0.047 ± 0.177 (average \pm SD). The
171 edge weight was normalized so that the sum of a_{ik} ($k=1,2,\dots, N; k \neq i$) became N (in other words,
172 average network weight became 1.0).

173

174

175 **c) Synchronization data scoring and calculation of modelling parameters**

176 *Population synchronization rate:* We scored at each time step (in our case, a scan every
177 30 minutes) the number N of horses and their identities in each state (S_r for resting and S_m for
178 moving). As explained in (a), resting is standing still or laying down, and moving is any other
179 behaviour, mainly grazing. We only used observations when more than 90% (21 out of 23) of
180 units were available in the field. We observed 21–23 units in 8 days out of 19 days during June
181 14th–28th and July 5th. We did not include July 5th data, although 21 units were available, since
182 horses foraged in the edge of the field site, rocky area with many obstacles, which may limit
183 their vision. One AMU was not observed on 15th and 16th, and one harem and one AMU were
184 not observed on the 28th (Figure S3). We defined a synchronization rate of a dyad as a
185 proportion of the observation when two individuals were in the same activity state, i.e., we
186 scored 1 when two individuals were in a same state (e.g., resting or moving respectively) in an
187 observation and 0 when not, and then calculated its average.

188 *Individual synchronization/state phase latency:* We defined a synchronization phase $P_{r,m}$
189 as a ‘resting \rightarrow moving’ event when there was a continuous decrease of resting individuals from
190 the minimal to the maximal, and a phase $P_{m,r}$ ‘moving \rightarrow resting’ event as the opposite (Figure
191 4). We excluded the increase/decrease from the first observation or the last observation of the
192 day. In total, we found 21 moving \rightarrow resting events and 18 resting \rightarrow moving events. We

193 calculated the state phase latency ΔT_{01s} as the time elapsed between the end of one state phase
194 and the beginning of the next one. This phase latency corresponds to the departure latency on an
195 individual to change state in previous works (Bourjade et al., 2009; Sueur et al., 2010, 2009;
196 Sueur and Deneubourg, 2011). ΔT_{01r} corresponds to the resting phase latency and ΔT_{01m} to the
197 moving phase latency (Table 1, Figure S1). For explanations of modelling self-organisation and
198 collectives, see also Sueur and Deneubourg (2011).

199 *Individual refractory period:* Many synchronization processes in animal groups imply a
200 refractory period, which is the short time period after an individual has changed their state and
201 then appears insensitive to its neighbours (Couzin, 2018, 2009). Theoretical studies showed that
202 this period is necessary for animals to not be stuck in a state (Couzin, 2018, 2009), and
203 preliminary works on our model also showed that, to avoid observing agents being stuck in a
204 state, the refractory period is necessary. According to the observed data, the mean refractory
205 period for moving was 50 minutes and 25 minutes for resting (Figs. S3, S4). We used these
206 values as well as lower and higher values of the refractory period to check the fitness of
207 simulations to the empirical data (see supplementary material and section (d)). We then scored
208 the changing state latency $\Delta T_{j-1,j,s}$ of each horse j changing state s corresponding to the time
209 elapsed between the state change of the individual $j - 1$ (i.e., the previous individual changing
210 state s_1 to s_2 , and the state change of the horse j (changing also from s_1 to s_2). The expected
211 value of $\Delta T_{j-1,j,m}$ and $\Delta T_{j-1,j,r}$ were 2.3 and 1.3 minutes respectively (Table 1, Figure S2).

212

213 **(d) The models**

214 Our aims were to understand the synchronization process of horses between two
215 states—moving and resting—throughout the day. We considered that, in multilevel society,
216 individuals synchronize across and within units but their internal synchronization is stronger. In
217 other words, the synchronization should be similar to their spatial association pattern, where
218 intra-unit cohesion is quite strong but the inter-unit cohesion is moderate.

219 According to the preliminary analysis, the horses' resting/moving was independent of
220 the time of day (see Supplementary Appendix for detailed explanation), so we did not consider
221 the effect of time in the following models.

222

223 *Model design:* The overall design of the models is shown in Figure 1. The model is
224 stochastic and individualistic (Couzin, 2009; Sueur and Deneubourg, 2011), meaning that we
225 consider the probability of each individual to change state, and not the collective probability or

226 state. We followed this concept as we introduced the selective mimetism (mimetism based on
227 social relationships) as a hypothesis and this can be done only with calculating probabilities per
228 individuals (Sueur et al., 2009; Sueur and Deneubourg, 2011). This bottom-up approach is also
229 better than the top-down one for understanding individual decision processes. We obtained the
230 probability of individuals to change states, mimetic-coefficient and refractory time period of
231 resting/moving and social relationships from the data set (Table 1, details about calculations are
232 given below). The probability $\Psi_1 (N\lambda)$, mimetic coefficient C, and refractory time period ΔT_{01}
233 ($=1/\Psi_1$) of moving were calculated as 0.04, 0.796 and 25 minutes, and those of resting were
234 0.02, 0.426 and 50 minutes, respectively (Table 1, Figure S1 and S2). We ran a simulation (one
235 day) extending 9 hours (540 minutes) with 18 observations, and we repeated the simulations
236 100 times for each hypothesis. We also tested the model with different parameter sets to
237 investigate its robustness (Supplementary Appendix “Comparisons of models under various
238 parameters”).

239

240

241 *Individual probability of changing state:* As the distribution of the state latencies
242 corresponded to an exponential distribution (figure S3), the probability of an individual
243 changing its state was the log gradient of this exponential distribution, that is, the inverse of the
244 mean state latency (Sueur et al., 2009):

$$\Psi_{1,s} = \sum_{i=1}^N \lambda_{i,s}$$

245 We assumed that all individuals may have the same mean latency while their probability of
246 changing their state might differ. The mean latencies to start event are equal irrespective of the
247 individual:

$$\Delta T_{01,s} = \frac{1}{\Psi_{01,s}}$$

248 as explained above, we also defined ΔT_{01} as a refractory time period in the simulations.

249 *Mimetic coefficient:* In a mimetic process where the probability of changing state is
250 proportional to the number of individuals already in this state, the probability per unit time that
251 individual i changes state is:

$$\psi_{i,s} = \lambda_s + C n_s$$

252 where C was the mimetic coefficient per individual and j_s is the number of individuals in the
253 state s, either R for resting or M for moving. As ψ_i is same for all the individuals in the herd,

254 the mimetic coefficient C could be obtained from the inverse of the average T_{jj-1} , $1/E[\Delta T_{jj-1}]$
255 ($j=2,3,\dots$). We calculated the parameters C and ΔT_{01} using survival analysis (figures S3 and S4
256 respectively) and quadratic functions (see results and figures 5 and 6 respectively).

257

258 *Models based on the different hypotheses:* We tested different sub-models (figure 1)
259 based on each hypothesis, presented here for i to iii. Overall, we tested seven models: (A)
260 independent, (Ba) absolute anonymous, (Bb) proportional anonymous, (Ca) unit-level absolute
261 social, (Cb) unit-level proportional social, (Da) herd-level absolute social, and (Db) herd-level
262 proportional social model.

263

264 (i) Independent hypothesis (model A)

265 The first hypothesis assumed that horses were independent: the probability of an
266 individual changing their state is not influenced by the state of any other members. Under this
267 hypothesis, the probability that one of the agents (e.g., individual i) changes state per unit time
268 was $\lambda_{i,s}$. Considering the refractory period, the probability ψ_i is equal to $\lambda = \Psi_{01}/N$ when Δt_i
269 $< \Delta T_{01,s}$ and is equal to 1 when $\Delta t_i = \Delta T_{01,s}$.

270 This model corresponds to a null model.

271

272 (□) Anonymous hypotheses (model Ba and Bb)

273 The second hypothesis specified that horses synchronize with all the herd members
274 anonymously. In the absolute anonymous model (model Ba), individuals will change state s
275 according to the absolute (i.e., not proportional) number of herd members in this state s
276 (respectively number R for state r and number M for state m). To test this hypothesis, we added
277 a mimetic coefficient C in the independent model, which indicated the strength of the collective
278 process.

279 Considering the refractory time period, the n resting agents became the joiner $j+1$ under
280 the model Ba was obtained from equation:

$$\psi_{i,s} = \min \left\{ \frac{1}{\Delta T_{01,s} - \Delta t_i}, \lambda_s + C n_s \right\}$$

281 when $\Delta t_i < \Delta T_{01,s}$. It is equal to 1 when $\Delta t_i = \Delta T_{01,s}$ (this is same for all the models, so we only
282 refer to the probability when $\Delta t_i < \Delta T_{01,s}$). The equation shows that when Δt_i is small, that is,
283 soon after an individual changed its state (beginning of a refractory period), it is less likely to be
284 influenced by other individuals' states.

285 We created another model based on the proportional number of individuals in state s ,
 286 where the probability of changing state $s1$ depends on the number of individuals in state $s1$
 287 divided by the number of individuals in state $s2$ (model Bb). The probability of individuals in $s2$
 288 to go in state $s1$ is:

$$\psi_{i,s1} = \min \left\{ \frac{1}{\Delta T_{01,s1} - \Delta t_i}, \lambda_{s1} + C \frac{n_{s1}}{n_{s2}} \right\}$$

289 As $n_{s1} = N - n_{s2}$, the response of individuals become reciprocal, not linear like the anonymous
 290 model.

291

292 (iii) Social hypothesis (model Ca, Cb, Da and Db)

293 In these hypotheses, we tested the influence of the social relationships between units or
 294 herd members on the decision to join. Unit-level social hypothesis (model Ca and Cb) assumed
 295 the synchrony happened only among unit members, while herd-level social hypothesis (models
 296 Da and Db) considered both intra- and inter-unit sociality. Within these two social hypotheses,
 297 we tested two models: one taking the absolute numbers of individuals in each state (model Ca
 298 and Da), another one taking the proportion as described for the anonymous mimetic models (Cb
 299 and Db).

300 Models Ca and Da considered the individual identities and the social relationships of
 301 each dyad. Each observed social relationship of the study herd was implemented in the model,
 302 allowing us to consider differences in social relationships between dyads. The probability per
 303 unit time that one of the n_{s2} individuals would change state to n_{s1} differed inversely between the
 304 resting agents with respect to their social relationships with agents already in $s1$. The probability
 305 of an individual i to change state under the social hypothesis was:

$$\psi_{i,s} = \min \left\{ \frac{1}{\Delta T_{01,s} - \Delta t_i}, \lambda_s + C \sum_{k \in s, k \neq i} a_{ik} \right\}$$

306 where $k \in s$ means that individual k is in state s . We simulated two types of the social index
 307 a_{ik} ; ‘unit-level’ (only intra-unit) in model Ca, and ‘herd-level’ (both intra- and inter-unit)
 308 association network in the model Da to investigate whether individuals made decisions based
 309 only on the members of the same unit or on all herd individuals.

310 In models Cb and Db, the proportion of the joiner to the non-joiner mattered. The
 311 probability of an individual i becoming a joiner $j+1$ under the social hypothesis was:

$$\psi_{i,s1} = \min \left\{ \frac{1}{\Delta T_{01,s1} - \Delta t_i}, \lambda_{s1} + C \frac{\sum_{k \in s1, k \neq i} a_{ik}}{\sum_{k \in s2, k \neq i} a_{ik}} \right\}$$

312

313 *Model setup:* At the group level, the collective state $S(t)$ can be described at time t by
314 the number n_m of individuals which are moving at that time (for a given group size N , the
315 number n_r of resting individuals is always $N - n_m$).

316 The number of individuals, individual identities, and social relationships of the
317 observed herd were included in the model. Thus, the number of agents N was fixed to 123. The
318 model is time-dependent with each time-step representing one minute. At the start of simulation,
319 30% of the agents were resting ($n_r = 37$). This 30% came from the average percentage of resting
320 horses through observation. This value was consistent with the other studies of feral horses
321 (Boyd and Keiper, 2005). We implemented the probability of changing state λ_i of each agent.
322 We did not implement any ecological barriers in the model, as usually the horses foraged in a
323 flat area with almost no obstacles (i.e., trees or rocks).

324

325

326 **(e) Statistical analyses**

327 To evaluate the model fit, we compared the number of horses changing states and
328 synchronization rate of simulated data to those of observed data.

329 For both $P_{m,r}$ and $P_{r,m}$, we plotted how many individuals changed state after the
330 synchronization phase started in each 30-minute window (e.g. 0–30, 30–60, 60–90 min...). We
331 refer to this number as Δn_s (Δn_r is for $P_{m,r}$ and Δn_s for $P_{r,m}$). We fitted the observed data to a
332 quadratic function that crosses (0,0), i.e., ax^2+bx , using linear regression in the R environment.
333 We evaluated the models by comparing the simulated data to observed data using the
334 Kolmogorov-Smirnov (K-S) test.

335 We calculated the correlation between the synchronization rate per dyad of simulated
336 data and that of observed data and tested its significance using the Mantel and K-S tests. We
337 evaluated the similarity of the intra-unit synchronization rate distribution to that of the observed
338 data using the K-S test. We used the Mantel test to evaluate the similarity of the synchronization
339 rate matrix as a whole, especially the ratio of intra- and inter-unit synchronization rate. Indeed,
340 the synchronization rate across units were mostly the same among models and never became
341 better than independent, so we eliminated it from the evaluation. A Mantel test was performed
342 using the R package ‘vegan’ (Oksanen et al., 2019) and K-S tests were performed using the
343 function ‘ks.test’ in the R environment.

344 Horses live in a multilevel society and are therefore expected to show social cohesion

345 and behavioural synchronization. We therefore expected the mimetic model, either anonymous
346 or social, to do better than the independent model (model Aa). Thus, we defined the model Aa
347 as a null model and compared other models to it. We calculated a score for each model, defined
348 as the proportion of the model showing better results than the independent one, i.e., when the
349 model had lower D in K-S tests, and higher r in Mantel tests than those of independent model.
350 As we have four tests, the score takes a value, 0, 0.25, 0.5, 0.75, or 1.0, where 1.0 is the best.

351

352 **Results**

353 **(a) Empirical data**

354 The average number of individuals changing states are shown in figures 4 ($P_{m,r}$) and 5
355 ($P_{r,m}$) (in blue, repeated in all graphs for comparison). Both showed a positive correlation with
356 the quadratic function (adjusted $R^2 = 0.79$ in $P_{m,r}$, $R^2 = 0.81$ in $P_{r,m}$, see table S5 for the detailed
357 results), indicating a mimetic or synchronization process with an increase of the number of
358 horses in a state followed by a decrease (Sueur et al., 2009; Sueur and Deneubourg, 2011).

359 The average \pm SD synchronization rate of each pair was 0.93 ± 0.03 within unit and
360 0.63 ± 0.06 across units in observed data, which showed a strong synchronization based on the
361 social network of horses. The correlation of the social network and synchronization rate of
362 observed data was 0.69 (Mantel test, permutation: 9999, $p < 0.001$), indicating a synchronization
363 process based on social relationships but a part of the process (at least 31%) was not based on
364 these relationships.

365 The average \pm SD weight within units and across units was 19.4 ± 9.9 and 0.26 ± 0.85
366 respectively. This means that we assumed that the same unit members had around 75.9 times
367 stronger effects on the behaviour than horses from different units in the herd-level hypothesis,
368 and as units are mixed (different ages, sex and personality), other hypotheses (sex, age and
369 personality tested separately from the network) are not relevant compared to the social network
370 which embed all these sociodemographic variables.

371

372 **(b) Simulations**

373 Concerning the states' synchronization, four models showed parabolic shape correlated
374 to observed data (table 2) in moving to resting phase (absolute anonymous: Figure 5Ba,
375 proportional anonymous: 5Bb, herd level absolute social: 5Da, and herd-level proportional
376 social: 5Db) and resting to moving phase (absolute anonymous: Figure 6Ba, proportional
377 anonymous: 6Bb, herd level absolute social: 6Da, and herd-level proportional social: 6Db).

378 Agents merely changed their states in the other three models (independent: Figure 5A and 6A,
379 unit-level absolute social: 5Ca and 6Ca, and unit-level proportional social: 5Cb and 6Cb).

380 Figure 7 shows the comparison between model-generated synchronization scores and
381 synchronization scores from the empirical data. The model simulations that did not consider
382 social relationships (i.e., independent, absolute anonymous, and proportional anonymous
383 models) showed a lot of overlap in the histograms of intra-unit and inter-unit synchronization
384 scores, unlike the observed data which show clear separation between intra and inter-unit
385 synchronization scores (figure 7).

386 Overall, the herd-level social (model Da) and the herd-level proportional social (model
387 Db) always had better scores than the independent (null) model, while the others did not. K-S
388 tests for Δn_m and Δn_r were better in the herd-level social model, and the K-S test and the
389 Mantel test were better in the herd-level proportional social model (table 2).

390

391

392 **Discussion**

393 We compared seven models to find which one best explained the dynamics of
394 behavioural states, specifically the synchronization of resting versus movement, in horses'
395 multilevel society. Among the models tested, only the herd-level absolute social model (model
396 Da) and the herd-level proportional social model (model Db) matched the empirical data better
397 than the null model (model A). Considering the simplicity of the model, which does not contain
398 any environmental effect and temporal changes of agents' positions, and the fact that the model
399 is based on temporally sparse data with 30 minutes intervals, we argue that these two models
400 were quite fitted to the empirical data. These models indicate that synchronization in a
401 multilevel society of horses can be largely explained by their internal rhythm plus the social
402 network. Model Da (herd-level absolute) was better at explaining the number of horses
403 changing states, while model Db (herd-level proportional) more successfully explained the
404 synchronization rate distribution, thus the mechanism most likely lies somewhere between them
405 (for instance, these two mechanisms switch at a certain threshold). It is also possible that we
406 could not evaluate the fitness of two models accurately enough because of the sparse observed
407 data. Although a multilevel society is considered among the most complex social structures in
408 animals (Grueter et al., 2017), our study suggested that the collective behavioural pattern could
409 be represented by simple mathematical models.

410 The observation data had higher intra- and inter-unit synchronization rate, and the

411 number of individuals that change state after the synchronization phase started (Δn_s and Δn_m)
412 had a higher peak than those of the herd-level hypothesis (models Da and Db) in most of the
413 parameter sets. Δn_s represents the speed of the behaviour spread, and synchronization rate
414 corresponds to the stability of the state (for example, whether horses keep resting when many
415 individuals are resting), suggesting that both are stronger in the observed data than those in
416 simulation. According to the models with different parameter sets, the fitness to Δn_s value and to
417 synchronization rate was negatively correlated with each other, suggesting the trade-off between
418 them (Figure S2). Indeed, the higher the speed of synchronization, the lower the stability. To
419 further improve the fitness of the model, we may need to consider a parameter sets and/or
420 equations which establish compatibility between the speed and the stability. For example, in the
421 current model, shorter refractory time period could enhance the speed but lower the stability,
422 because agents will definitely wake up after the refractory time passes. We may need to either
423 change the equation of the refractory time period or enhance the speed without changing the
424 refractory time period.

425 Most previous studies of non-multilevel societies suggested local interaction within a
426 few body lengths or the several nearest neighbours (Couzin and Krause, 2003). However, our
427 result showed that inter-individual interaction also occurred among spatially separated
428 individuals. According to Maeda et al., (2021), the average nearest unit distance was 39.3 m
429 (around 26.2 times a horse's body length) and the nearest individual within the same unit was
430 3.2 m. It is still not sure whether horses have a global view, or if they just respond to the several
431 nearest units, but either way this is a notably large distance compared to other studies. Horses
432 usually did not create any significant cue (e.g., vocalization) when they start moving/resting,
433 thus it is likely that horses have an ability to recognize the behaviour of both horses of the same
434 units and other units simultaneously. In a multilevel society, it is important to keep the inter-unit
435 distance moderate. This avoids competition between units while keeping the cohesion of the
436 higher-level group to obtain the benefits of being in a large group, such as protection from
437 bachelors or predators (Swedell and Plummer, 2012), and may have led to the evolution of such
438 cognitive ability.

439 Besides the temporal positions of units, another factor which may be important is
440 individual and unit attributes. The integration of the network in the model already considered
441 individual differences in network connectedness and centrality caused from such variations in
442 attributes. In the intra-unit level, some individual characteristics could affect the leaderships of
443 collective departure in a multilevel society (lactation: Fischhoff et al., 2007; personality: Briard

444 et al., 2015; intra-unit dominance rank: Krueger et al., 2014; Papageorgiou and Farine, 2020),
445 but it is unclear that those factors affect the behavioural propagation in herd-level (but see
446 Fischhoff et al., 2007). We presume most of these individual level attributes would become less
447 effective in inter-unit level synchronization because each unit has individuals with different
448 status, and the synchronization inside units are far stronger than those across units. In herd level
449 synchronization, we may be able to assume that all individuals in the same units always perform
450 the same behaviour (all resting or all moving), so individual differences should be largely
451 diluted. However, it is still possible that unit-level social status exists and effects the
452 synchronization pattern. In this horse population, our previous study found that large harems
453 tend to occupy the centre and had higher strength centrality (the sum of the edge that connects
454 to a node), while small harems and AMUs stayed on the periphery, suggesting the existence of
455 inter-unit level dominance rank (Maeda et al., 2021). It may therefore be possible that such
456 dominant units are more influential. Our data was too sparse in time scale to observe how
457 behaviour propagated across units and include horses' positional dynamics in a model, which is
458 needed to investigate horses' recognizable distance and the effect of the attributes. Finer-scaled
459 observation will be needed for the further investigation on the underlying mechanism in
460 herd-level synchronization.

461 Because of the simplicity of our model, our methodology is highly applicable to other
462 species. The spatial structure of multilevel societies is still poorly understood, but it may vary
463 among species, habitat environments and contexts. For example, a migrating herd of
464 Przewalski's horses (*Equus ferus przewalskii*) was relatively aggregated (Ozogany and Vicsek,
465 2014), but a higher level group of Peruvian red uakari (*Cacajao calvus*) was much more
466 sparsely distributed, like the horses in our study (the nearest unit distance was 10–15 m or
467 more) (Bowler et al., 2012). It is also highly possible that other species forming multilevel
468 societies show an ability to recognize the behaviour of other units which are located far away,
469 (especially in species that live in open fields, like equines and cetaceans). Horses do not have
470 specific timing for resting and it is unlikely that all individuals sleep at the same time, thus to
471 test whether agents only perceive units nearby, we needed to add a formula representing
472 collective movement in the current model. However, some animals that form multilevel
473 societies, such as primates, often sleep together at the same location during the night (Grueter et
474 al., 2012). In that case, we do not need to consider the movement, making it easier to test the
475 range of their perception. It is important to discover whether the association index could also
476 explain the behavioural decisions of other multilevel social animals with various special

477 structures to generalize our knowledge of behavioural synchronization in multilevel societies.

478 Overall, our study provides new insights into the behavioural synchronization process
479 and contributes to the understanding of collective behaviours in complex animal societies. The
480 organization of multilevel societies has become a topic of great interest recently, but studies
481 have so far tended to focus on social relationships and many questions are still unresolved. We
482 hope that our study on collective synchronization will contribute to an understanding of the
483 evolution and functional significance of multi-level animal societies.

484

485 **Limitations of the study**

486 Our model could not consider the temporal changes in position of horses including concurrent
487 inter-individual and inter-group distances, although it is highly likely that the behaviour of units
488 is more affected by closer units. While horses are in the moving state, their movement is likely
489 to be synchronized with each other, so we may need to consider movement synchronization in a
490 model as well as behavioural state synchronization. Developing inter-individual and intergroup
491 distances in the model can be done indirectly through giving variance using stochasticity to
492 relationships implemented in the model. For calculating the parameter on stochasticity, more
493 temporally fine scaled data may be needed. Orthomosaic data has the advantage of obtaining the
494 accurate and identified positions of individuals in a wide-ranged group, but it could obtain only
495 temporally sparse data. Optimizing the data collection method, such as combination of the video
496 recording from drones and orthomosaics, should be needed to further develop the model. In
497 addition, the variations of parameter sets we tested were limited, making it difficult to hold a
498 detailed discussion on the function of the parameters.

499

500

501 **Author Contributions**

502 SH and SY managed the project. TM collected data. CS designed the models and TM and CS conducted the analysis
503 and interpreted the results. TM wrote the manuscript with help from CS, SH, and SY. All authors have approved the
504 final version of the manuscript and agree to be accountable for all aspects of the work related to the accuracy and
505 integrity of any part of the work.

506

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514

515 **Data availability**

516 The relevant data and models are available at the following link: <https://doi.org/10.5061/dryad.c866t1g3b>

517

518 **Declaration of Interests**

519 The authors declare no competing interests.

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664 **Figure and Tables Legends**

665 **Figure 1.** A graphic representation of synchronisation models. The dots represent individual
666 agents and the cluster of dots represent units. When agents/units were connected with lines, it
667 means that their states were affected by each other. The width of the lines represents the strength
668 of synchronisation.

669 **Figure 2.** Overall procedure of the research. (a) We took aerial photos of horses using drones.
670 (b) These successive photos were stitched together to create an orthomosaic. (c) Individuals in
671 orthomosaics were identified, and the positional and behavioural data of horses were obtained.
672 We then constructed the social network using inter-individual distance data. The photograph is
673 also used in Maeda et al., (2021) published in Scientific Reports.

674 **Figure 3.** Histogram of inter-individual distances showing clear bimodality. The distance of the
675 first peak and the second peak could be considered as the most frequent value of inter-individual
676 distances within a unit and between units, respectively. The trough between two peaks
677 represents the threshold that divides the intra- and inter-unit association. This figure is reprinted
678 from Figure 2(a) in Maeda et al., (2021).

679 Figure 4. The explanation of $P_{m,r}$ and $P_{r,m}$.

680 **Figure 5.** The change of the number of resting individuals in $P_{m,r}$. The pink points are data
681 obtained from simulation and blue are those from the observation. Data was fitted to quadratic
682 function that cross (0,0), i.e., ax^2+bx . R^2 is the coefficient of determination of the regression for
683 simulated data. Aa: independent, Ba: absolute anonymous, Bb: proportional anonymous, Ca:
684 unit-level absolute social, Cb: unit-level proportional social, Da: herd-level absolute social, and
685 Db: herd-level proportional social models.

686 **Figure 6.** The change of the number of resting individuals in $P_{r,m}$. Same as Figure, 4.

687 **Figure 7.** Histograms of the synchronisation rate. White and grey bars represent the observed
688 value of synchronisation rate across units and within units, respectively. Pink and blue bars
689 represent those of simulated data across units and within units, respectively. Aa: independent,
690 Ba: absolute anonymous, Bb: proportional anonymous, Ca: unit-level absolute social, Cb:
691 unit-level proportional social, Da: herd-level absolute social, and Db: herd-level proportional
692 social models.

693

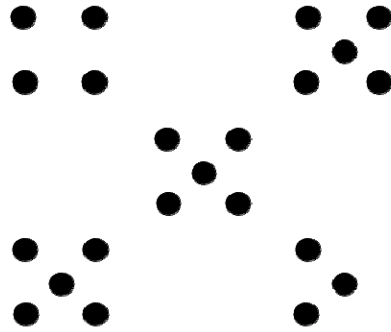
694 Table 1. The explanation and values of parameters. The value of the parameter was written
695 when it is a constant. See also supplementary appendix for the detailed explanation of how to
696 obtain the parameter value. ‘-’ means that the value can change dynamically.

697 Table 2. The result of the evaluation of Δn and the synchronisation rate obtained from the
698 simulations. “Eval” (evaluation) is “+” when the result is better than independent model and “-”
699 when not. The model with smaller D and larger r is considered as the better. Score is the
700 percentage of the tests which showed better results than independent (null) model.

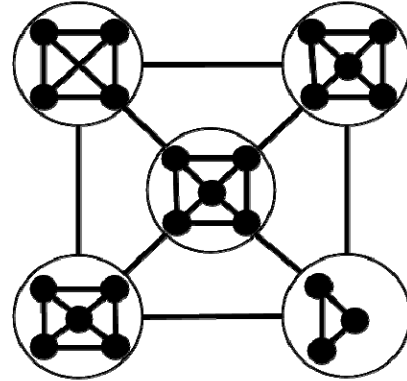
701

702 **Figures and Tables**

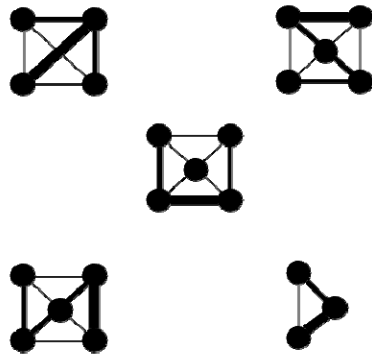
(A) Independent



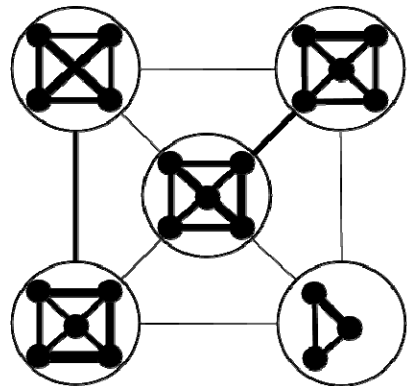
(B) Anonymous



(C) Unit-level social



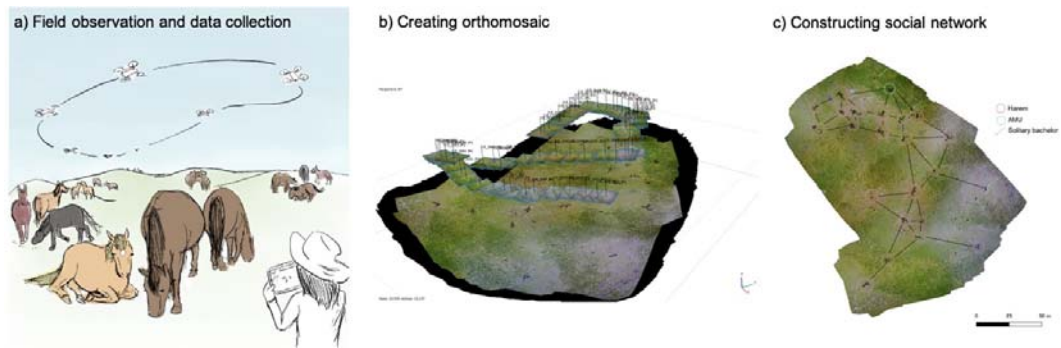
(D) Herd-level social



703

704 **Figure 1**

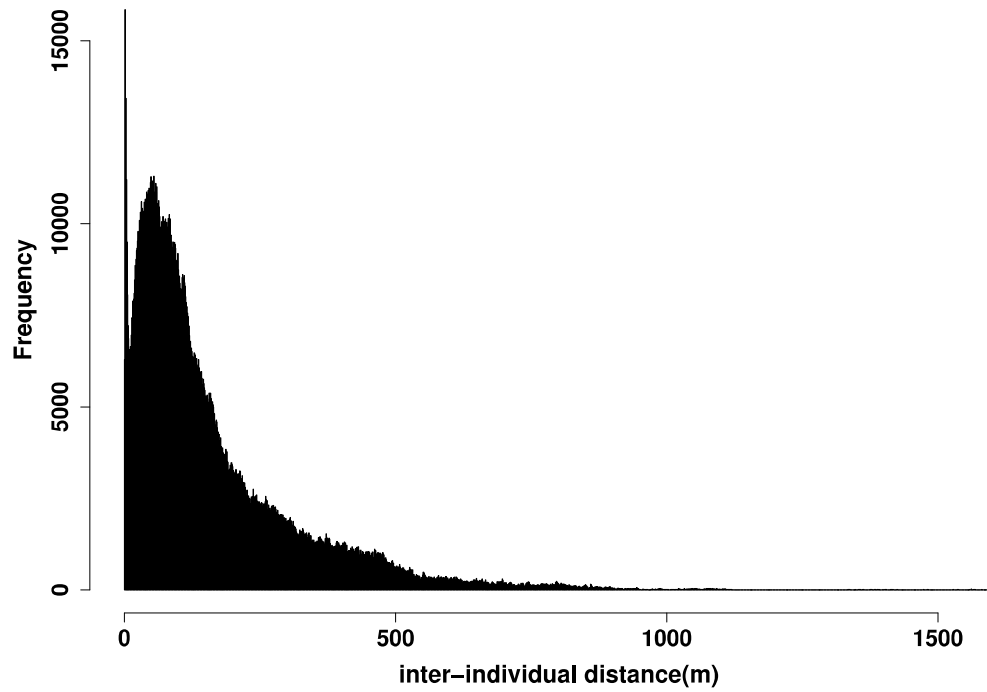
705



706

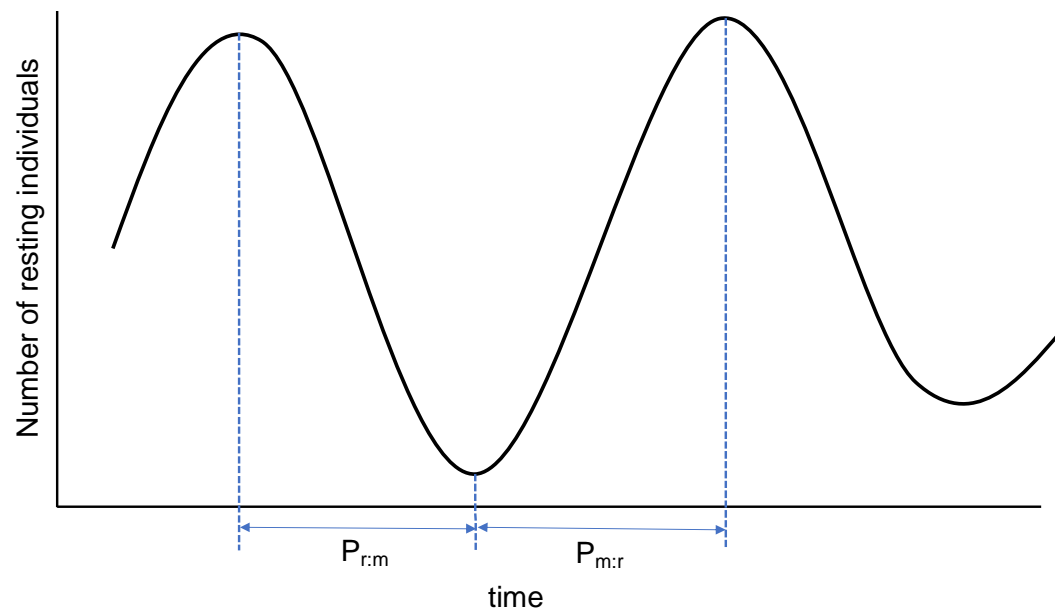
707 **Figure 2**

708

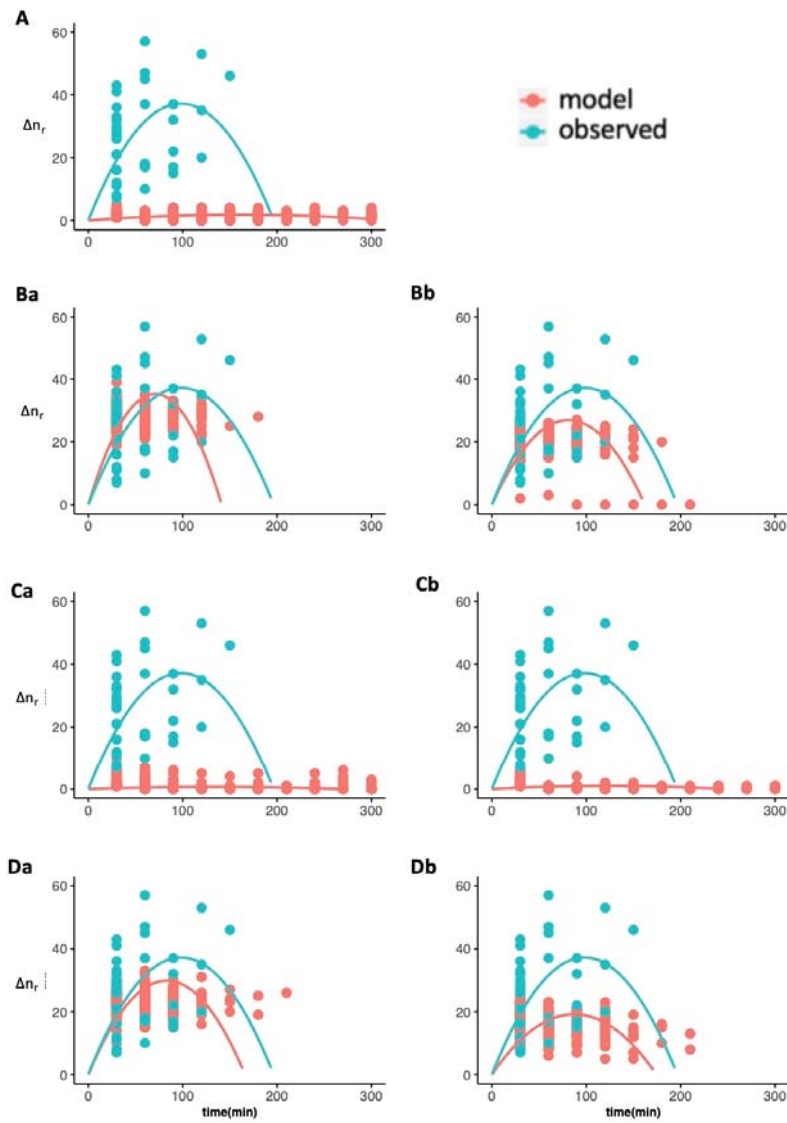


710 **Figure 3**

711



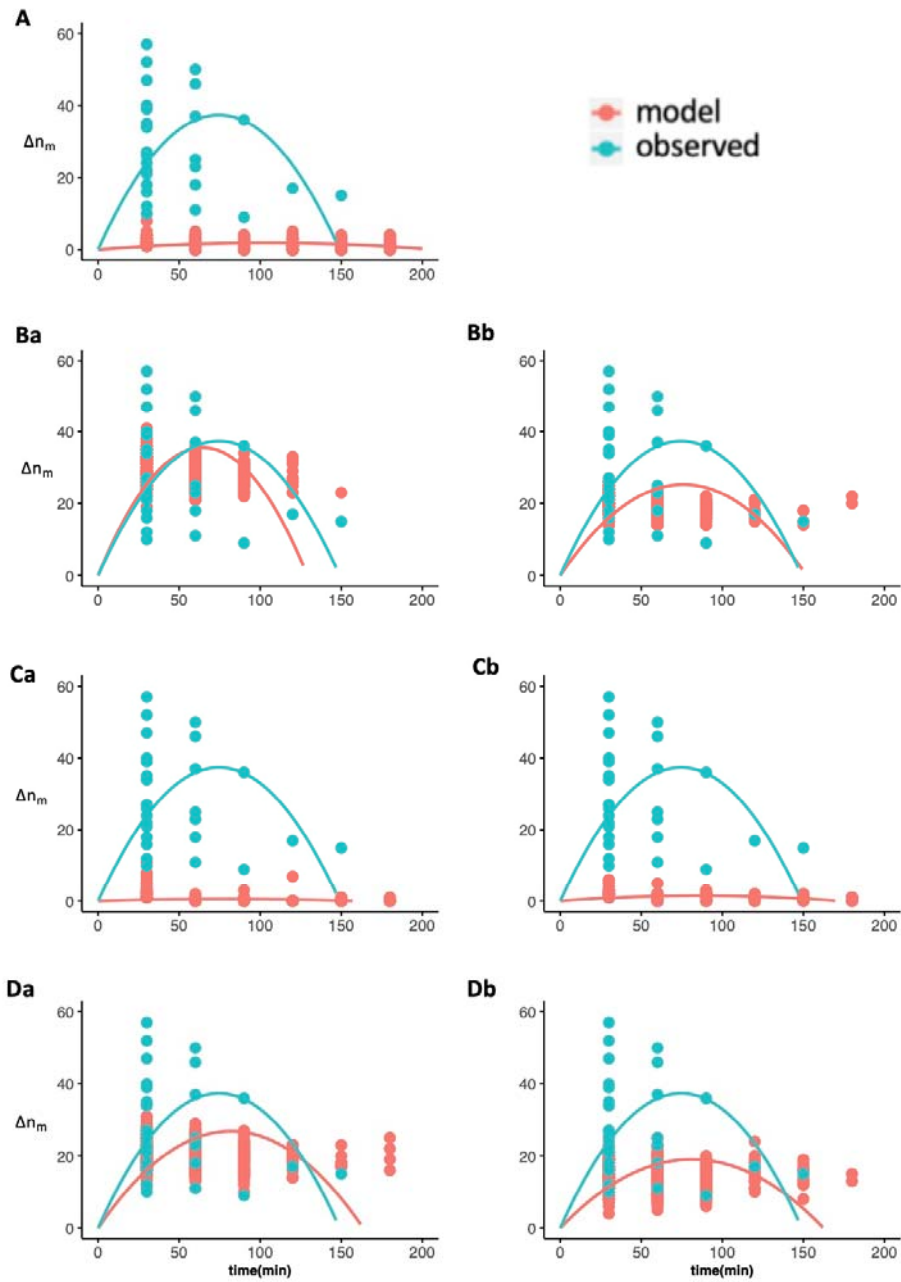
713 **Figure 4**



714

715 **Figure 5**

716

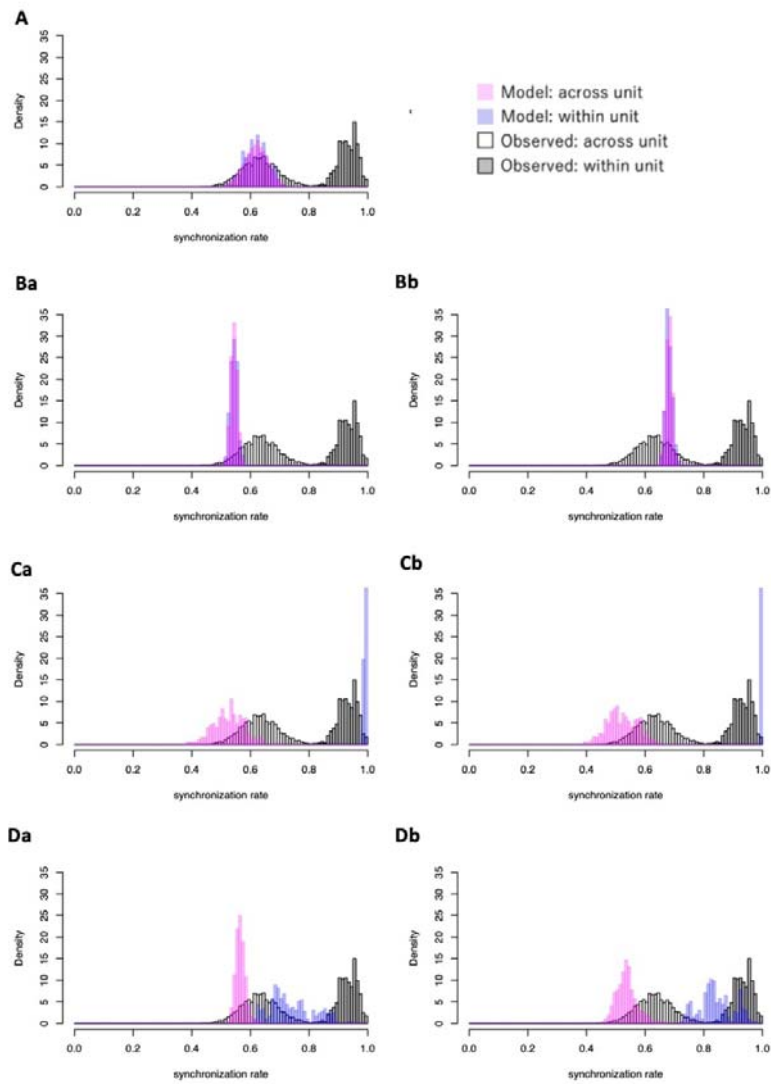


717

718 **Figure 6**

719

parameter	value	value	Definition
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720

721 **Figure 7**

722

	(resting)	(moving)	
a_{ki}	social network		social network weight between individuals k and i .
C	0.426	0.796	mimetic coefficient
Ψ_1	0.030	0.040	A probability of starting resting/moving. Equal to $N\lambda_i$
Ψ_j	-	-	Probability per unit time that one of the n agents became the j th joiner (corresponding to the hypothesis where the identities of individuals are not taken into an account)
$\Psi_{i,s}$	-	-	Probability per unit time of an individual i changing the state s (the refractory time period and the identities of individuals are taken into an account.)
$\lambda_{i,s}$	0.00016	0.00033	The average probability per unit time of an individual i changing the state s .
$\Delta T_{01,s}$	50 (min)	25 (min)	Refractory time period. time elapsed from the end of the previous event.
$\Delta T_{j,j-1,s}$	2.3 (min)	1.3 (min)	time elapsed between the state change of the joiner $j-1$ and the state change of the joiner j . The inverse of C .
Δt_i	-	-	time elapsed from the previous state change of individual i
N	123		number of individuals in a herd
n_s	-	-	Number of the individuals in the state s (resting/moving).

723 **Table 1**

724

725 **Table 2**

model	K-S test ($\Delta n_m, P_{r,m}$)			K-S test ($\Delta n_r, P_{m,r}$)			K-S test (sync rate of intra-unit)			Mantel test (sync rate)			score	
	D	p	eval	r	p	eval	D	p	eval	r	p	eval		
independent (null model)	A	0.980	0.010		0.980	0.010		1.000	<0.001		0.367	0.010		
absolute anonymous	Ba	0.215	0.989	+	0.306	0.989	+	1.000	<0.001	-	-0.050	0.989	-	0.50
proportional anonymous	Bb	0.564	0.947	+	0.561	0.947	+	1.000	<0.001	-	-0.057	0.947	-	0.50
unit-level absolute social	Ca	0.993	<0.001	-	0.995	<0.001	-	0.973	<0.001	+	0.572	<0.001	+	0.50
unit-level proportional social	Cb	0.980	<0.001	-	0.980	<0.001	-	0.993	<0.001	+	0.627	<0.001	+	0.50
herd-level absolute social	Da	0.537	<0.001	+	0.577	<0.001	+	0.915	<0.001	+	0.601	<0.001	+	1
herd-level proportional social	Db	0.698	<0.001	+	0.714	<0.001	+	0.714	<0.001	+	0.634	<0.001	+	1