Implications of (co)evolution of agriculture and resource foraging for the maintenance of species diversity and community structure

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Keywords: niche construction, evolution of specialization, indirect effects, agriculture, functional specialization, coevolution

Abstract: Agriculture is found in numerous taxa such as humans, ants, beetles, fishes and even bacteria. This type of niche construction has evolved independently from hunting, though many species remain primarily predators. When a consumer has a positive effect on its resource, we can expect an allocative cost of agriculture, as the agricultural care diverts time and energy from other activities. Defending the resource against predators may divert time from its consumption (exploitation cost). The cost may also occur on the foraging of alternative resources, for instance if the consumer spends more time nearby the farmed resource and underexploiting resources elsewhere (opportunity cost). We here investigate transitions from predation to agriculture in a simple three-species model of a farmer that consumes two resources and has a positive effect on one. We study the conditions for the (co)evolution of the investment into agriculture and specialization on the two resources, and its consequences on the ecological dynamics of the community. Eco-evolutionary dynamics generate a feedback between the evolution of agriculture and specialization on the helped resource, that can lead to varying selected intensity of agriculture, from generalist strategies with no agriculture, to specialist farmers, with possible coexistence between these two extreme strategies.

Introduction

Some of the species that display the greatest ecological success perform agriculture, that we here define as the cultivation of plants, algae, fungi and the herding of animal. Agriculture is a type of niche construction, an active modification of its environment by an organism, that potentially feed backs on the selective pressures acting upon it (Odling-Smee et al. 2013). A typical example is the impact of agriculture on the evolutionary history of humans and species affected by agriculture (Boivin et al. 2016). Humans have been causing both ecological and evolutionary change through their practice of agriculture, from direct effects such as artificial selection and domestication, to indirect effects such as climate change or introduction of invasive species, and causing the evolution of resistance to use of herbicides or pesticides (Thrall et al. 2011; Loeuille et al. 2013). The consequences of domestication, for instance, are important not only for the selected species (that can display drastic modifications of their phenotypic traits compared to the ancestral, undomesticated species (Thrall et al. 2011)) but also for other species within agricultural landscapes, as the domesticated species may become a dominant species exerting a strong selective force. Humans are not the only species to practice agriculture. Many ant species can use other insects, such as aphids, as cattle, or cultivate fungi (Mueller et al. 2005). Numerous taxa benefit from actively managing their resources: agriculture is also found in termites, beetles, fishes, nematodes and even microorganisms (Hata and Kato 2006; Boomsma 2011; Thutupalli et al. 2017; Brooker et al. 2020). The benefits associated with agriculture are easily understandable in changing, unpredictable and competitive environments: it potentially increases the resource availability, limits competition if the cattle or exploitation is privatized, and allows a greater predictability of resource abundance compared to foraging.

From a consumer-resource theory perspective, agriculture can be envisioned as a modification of a purely trophic interaction between a consumer and a resource. This interaction is then not only

consisting of consumption or predation, but contains an additional positive effect of the consumer

on the resource, which has been described in various contexts (Abrams 1992; Brown et al. 2004;

Terry et al. 2017). The ecological and evolutionary consequences of including positive effects into

trophic networks have recently received increasing attention (Fontaine et al. 2011; Kéfi et al. 2012;

Mougi and Kondoh 2012). Accounting for such non trophic interactions alters the stability of

networks and coexistence of species. Positive effects associated with agriculture can emerge from

different consumer behaviours (protection against predators, helped reproduction or dispersal, for

instance). It can impact the resource demography in various ways (increase of the carrying

capacity, increase of the growth rate) that are expected to increase the resource profitability for the

farmer species, compared to alternative foraged resources. The evolution of agriculture has been

envisioned in the niche construction perspective, particularly in the human context (Rowley-Conwy

and Layton 2011; Boivin et al. 2016; Zeder 2016) A classical example of the consequences of niche

construction through agriculture is the evolution of lactose tolerance in humans (Laland and

O'Brien 2011).

Jointly to the niche construction perspective, the ecological and evolutionary consequences of

agriculture can be conceived in the light of foraging theories (optimal foraging, (Charnov 1976;

Pyke et al. 1977), adaptive foraging, (Loeuille 2010)). This can help understand the question of the

potential transition between foraging strategies such as hunting, gathering, to agricultural strategies.

The evolution of agriculture can lead to full specialization and reciprocal dependency of the

agricultural partners, as in fungus-growing ants (Mueller et al. 2005). To understand those two

questions (transition to settled agriculture, extreme specialization), we can use the evolution of

specialization framework (Egas et al. 2004; Abrams 2006). Optimal foraging theory predicts that

the specialization of a consumer will evolve depending on the resources profitabilities. Agriculture

practice can then modify the resource profitability through the modification of its abundance.

Hence we expect that increasing agriculture selects for higher specialization on the cultivated

resource that becomes more profitable, in turn selecting for more agriculture, leading to a positive

feedback loop between agriculture and specialization on the cultivated resource. As a consequence,

we expect reciprocal evolutionary consequences (or coevolution) between the evolution of

specialization (*sensu* consumption, predation) on the resources, and the evolution of agriculture.

From this perspective, we can understand the evolution of agriculture as the addition of another

dimension to the classic evolution of specialization: an organism allocates energy or time between

the consumption of different resources, and the cultivation of one or several resources. Two types

of evolutionary outcomes are expected: either a high level of agriculture with a high specialization

on the managed resource, or no agriculture and generalism or a specialist on another resource

depending on the trade-off associated with the foraging activities.

This simple prediction can be modified by accounting for the cost of agriculture: the niche

constructing phenotype can first be threatened by cheaters, if niche construction benefits are shared

by all the population (potentially leading to a tragedy of commons, (Hardin 1968)). Farming can

then be considered a public good (Thutupalli et al. 2017). Although privatization might overcome

the threat of freerider invasion (through pleiotropy, (Chisholm et al. 2018), monopolization of the

niche (Krakauer et al. 2009) or benefits going to the closest relatives (Scheiner et al. 2021)), trade-

offs can still mitigate the evolution of agriculture by altering the profitabilities of the resources. If

the cultivated resource is initially much less profitable than an alternative resource, we predict that

agriculture may be counter-selected despite potential benefits. A cost to agricultural behaviour

could emerge because of a high presence of competitors, predators or pathogens of the resource

that needs to be actively protected (Hübner and Völkl 1996; Stadler and Dixon 2005; Adams et al.

2013; Fernández-Marín et al. 2013; Thutupalli et al. 2017). Here, we investigate the cost of

agriculture in the foraging theory perspective: increasing the niche construction activity occurs at a

cost on the consumption of resources, because of a limited energy or time budget available to the

farmer species. Agriculture can, as a type of resource exploitation, decrease the consumption of an

alternative resource ("opportunity cost", described in Picot et al. (2019)). It can as well decrease the

consumption of the managed resource, e.g. if defending it against predators or competitors implies

moving away from the resource site, or allocating more time to defense rather than consumption

("exploitation cost" scenario, Picot et al. (2019)).

Because of the previously stated feedback loop, understanding the (co)evolution of

agriculture and specialization requires to investigate its ecological consequences in terms of

variations in resource abundances. Explicitly accounting for niche construction in models and

theory leads to patterns that would not be predictable otherwise (Kylafis and Loreau 2011). In

humans, agriculture is known to have drastic effects on the community and ecosystem level

properties: for instance, by introducing invasive species that engage in apparent competition with

native ones (David et al. 2017; Geslin et al. 2017), so that agricultural has pervasive consequences

for the maintenance of species diversity and ecosystem functioning (Emmerson et al. 2016). The

study of indirect effects may give insights on the community consequences of the evolution of

agriculture. Indirect effects are effects of one species on another, transmitted by another species

(Wootton 1994), here the consumer species. When a consumer consumes two resources, those

resources engage in apparent competition (Holt 1977): an increase in density of one resource may

decrease the other resource growth rate through their interaction with the consumer. Agricultural

aspects modify this view. In an ecological analysis of a consumer-resource model with niche

construction, Picot et al. (2019) show that cultivated and non-cultivated resources may then engage

in various types of indirect interactions through the consumer. Without considering any cost,

increasing niche construction has a positive effect on the managed resource density, which

translates in a bottom-up positive effect on the consumer density, and a negative effect on the

alternative density, because of apparent competition. Considering costs of niche construction

mitigates this result. If the cost of niche construction is high enough in terms of resource

consumption, an increase in niche construction of the cultivated resource may lead to counter-

intuitive increase in the alternative resource density, because of a decrease in its consumption rate

("opportunity cost" scenario) and/or a decrease of the consumer density ("exploitation cost"

scenario and "opportunity cost").

In this study, we use adaptive dynamics and numerical simulations to study the evolution

and coevolution of a consumer niche constructing trait and its specialization on two resources

(Geritz et al. 1998). We address the following questions: (1) How does a fixed foraging strategy

impact the selected investment into agriculture? We predict that a high specialization on the

managed resource favours the evolution of agriculture, while a high specialization on the

alternative resource prevents it. (2) How does the profitability of the different resources impact the

coevolution of the niche construction trait and the specialization on the resources? We predict a

positive correlation between the evolution of agriculture and specialization on the cultivated

resource. (3) How do the evolution of niche construction and its coevolution with specialization

impact the coexistence of the resources and the functioning of the system? We then predict that a

high selected level of agriculture leads to the exclusion of the alternative resource because of

increased apparent competition, while counter-selection of niche construction should lead to

coexistence of the resources.

Model presentation

Ecological dynamics

Our model is based on ordinary differential equations describing the ecological dynamics of the

consumer and two resource species. In this simple model (eq (1) and Fig 1 *A*), the consumer

species C interacts with the two resources R_1 and R_2. The resource R_1 is managed through

agriculture: we assume it receives a positive effect that increases its growth rate, but it is also

consumed. The alternative resource R_2 is only consumed:

$$\begin{cases} \dfrac{dC}{dt} = C\left(e_1(x)\,s_1(x)\,R_1 + e_2\,s_2(x)\,R_2 - m\right) & (a) \\[2mm] \dfrac{dR_1}{dt} = R_1\left(b_1 - g_1 R_1 - s_1(x)C + w\,x\,C\right) & (b) \\[2mm] \dfrac{dR_2}{dt} = R_2\left(b_2 - g_2 R_2 - s_2(x)C\right) & (c) \end{cases} \qquad (1)$$

The consumer *per capita* growth rate depends on its consumption of resources (modelled by

specialization on resource R_i, s_i, and consumption efficiency of resource R_i, e_i) and on its death rate

m. In the absence of the consumer, the two resources grow logistically (allowing for their

coexistence in such situations): b_i is the birth rate and g_i is the intraspecific competition rate for

resource R_i. Only apparent competition through the interactions with the consumer is considered

here: we do not consider any direct competition between resources, which allows us to single out

the impacts of the consumer. Finally, note that resource R_1 receives a positive effect from

agriculture, proportional to the investment into niche construction x and niche construction

efficiency w. We assume that all parameters e_i, s_i, b_i, g_i, x are positive. Niche construction is then

facultative for the maintenance of R_1, as both resources have positive intrinsic growth rates.

158 Trade-offs: costs and benefits of niche construction

159   As stated above, we assume that agriculture occurs at a cost for foraging on the resources. We

160   consider two trade-off scenarios that rely on a time or energy constraint: increasing the agricultural

161   intensity can decrease the consumption of the managed resource ("exploitation cost", $s_1{'}(x) < 0$) or

162   the consumption of the alternative resource ("opportunity cost", $s_2{'}(x) < 0$). We consider that the

163   three traits are linked through the following formula:

$$x^k + s_1^k + s_2^k = L \qquad (2)$$

L represents the total amount of time or energy that the consumer allocates between niche

construction and the consumption of the two resources. In the opportunity cost scenario, s_1 is fixed

while in the exploitation cost scenario, s_2 is fixed. In the coevolution scenario, the three traits may

evolve jointly along the trade-off surface (Fig 1 *B*). The exponent *k* shapes the trade-off

(accelerating for a convex trade-off, *k > 1* or saturating for a concave trade-off, *k < 1*).

We also assume that niche construction provides a direct benefit for the organisms performing it:

for instance, agriculture can provide a more direct access to the managed resource and increase its

consumption efficiency, because of proximity, or through another adaptation. We positively link the

consumption efficiency to the agricultural trait through the following expression

$$e_1(x) = (1+x)^u \tag{3}$$

173 where *u<1* indicates saturating efficiency increase (diminishing returns, for instance if the

174 efficiency consumption is constrained by other factors, such as physiological ones) while *u>1*

175 indicates an accelerating response.

Ecological dynamics

The ecological dynamics of a similar system has been studied in Picot et al. (2019), assuming a

fixed level of niche construction, and differing only in the trade-off functions that are used. In this

previous work, niche construction intensity linearly decreased with specialization rates s_1 and s_2,

and no direct benefit of niche construction was assumed (this would mean *u=0* in our present

model). However, some general results of the ecological dynamics apply in the present model:

different types of ecological equilibria are obtained: either the coexistence of the two resources,

with or without the consumer, or the maintenance of one resource (still with or without the

consumer) or the extinction of all species. Note that this previous work only tackled ecological

dynamics, while we here focus on the evolution of the different traits.

Evolutionary dynamics

We first study the evolution of the phenotypic trait x using the adaptive dynamics framework (Dieckmann and Law 1996; Geritz et al. 1998), assuming that the consumer diet (s_1, s_2) is fixed. Adaptive dynamics allows to investigate evolutionary dynamics of phenotypic traits while defining the fitness of a given phenotype based on its ecological dynamics. The analytical framework relies on the separation of ecological and evolutionary timescales, while numerical simulations allows us to more freely investigate the limits of this hypothesis. The evolution of a trait is studied through several steps, assuming clonal reproduction, and small and rare mutations:

- the ecological equilibrium is determined, for a monomorphic population of resident trait x_{res} (by nullifying equations 1(a) to 1(c))

- a rare mutant with trait x_{mut} is introduced and replaces the resident trait if its invasion fitness (i.e., its *per capita* growth rate when rare, based on eq1(a)) is positive. Invasion fitness is given by:

$$W(x_{mut}, x_{res}) = e_1(x_{mut}) s_1(x_{mut}) R_1^*(x_{res}) + e_2 s_2(x_{mut}) R_2^*(x_{res}) - m \tag{4}$$

The new ecological equilibrium is established and the process is iterated.

A deterministic approximation of the evolution of the trait is given by the canonical equation of adaptive dynamics (Dieckmann and Law 1996) :

$$\frac{\mathrm{d}x}{\mathrm{d}t} = \frac{1}{2} \mu \sigma^2 N^0(x_{res}) \left. \frac{\partial W(x_{mut}, x_{res})}{\partial x_{mut}} \right|_{x_{mut} \to x_{res}} \tag{5}$$

$\mu \sigma^2 N^0(x_{res})$ is the evolutionary potential, that is total phenotypic variability brought by mutations with μ the *per capita* mutation rate, σ^2 the phenotypic variance associated to these mutations and $N^0(x_{res})$ the resident population equilibrium density. The selection gradient

$\left. \dfrac{\partial W\left(x_{mut},x_{res}\right)}{\partial x_{mut}} \right|_{x_{mut} \to x_{res}}$ is derived from the invasion fitness (eq 4) and corresponds to the slope

of the fitness landscape around the resident population, therefore representing the selective

pressures acting on the phenotypic variability brought by mutations. The traits that nullify this

gradient are called singular strategies (Dieckmann and Law 1996). Dynamics around these singular

strategies are characterized by the second partial derivatives of fitness (Dieckmann and Law 1996;

Geritz et al. 1998). This allows to distinguish two stability-related properties: invasibility and

convergence. A singular strategy x^* is non-invasible (Maynard Smith 1982), or evolutionary stable

if:

$$\left. \frac{\partial^2 W\left(x_{mut},x_{res}\right)}{\partial x_{mut}^2} \right|_{x_{mut} \to x_{res} \to x^*} < 0 \tag{6}$$

212 *i.e.* when the singular strategy is the resident population, no nearby mutant can invade.

213 A singular strategy is convergent or continuously stable (Eshel 1983) if:

$$\left. \frac{\partial^2 W\left(x_{mut},x_{res}\right)}{\partial x_{mut}^2} \right|_{x_{mut} \to x_{res} \to x^*} + \left. \frac{\partial^2 W\left(x_{mut},x_{res}\right)}{\partial x_{mut} \partial x_{res}} \right|_{x_{mut} \to x_{res} \to x^*} < 0 \tag{7}$$

i.e., considering a resident population close to the singular strategy, mutants that are even closer

to it are selected. The two trade-off scenarios lead to different fitness expressions for each scenario,

since in the "exploitation cost" scenario, s_2 is fixed and $s_1(x)=\left(L-s_2^k-x^k\right)^{\frac{1}{k}}$ while in the

opportunity cost scenario s_1 is fixed leading to $s_2(x)=\left(L-s_1^k-x^k\right)^{\frac{1}{k}}$.

We illustrate the evolution of x in the "exploitation cost" and "opportunity cost" scenarios using

numerical simulations. The simulation algorithm was built in C++.

Coevolutionary dynamics

In the coevolution scenario, we let the three traits s_1, s_2, and x vary while accounting for trade-

off constraints (equation (2)). This means we allow the two traits s_1 and x to evolve independently

and derive the trait s_2 from the trade-off. We approach this question both with semi-analytical

calculations, and using our evolutionary algorithm, by introducing mutations of the three traits.

When both x and s_1 jointly evolve, we derive two expressions of the fitness. The fitness $W_x(x_{mut},$

$x_{res}, s_{1res})$ of a mutant of trait x_{mut} and the fitness $W_{s1}(s_{1mut}, s_{1res}, x_{res})$ of a mutant of trait s_{1mut} appearing

in a resident population of traits x_{res} and s_{1res} are:

$$W_x(x_{mut}, x_{res}, s_{1res}) = e_1(x_{mut}) s_{1res} R_1*(x_{res}, s_{1res}) + e_2 s_2(x_{mut}, s_{1res}) R_2*(x_{res}, s_{1res}) - m$$
$$W_{s_1}(s_{1mut}, s_{1res}, x_{res}) = e_1(x_{res}) s_{1mut} R_1*(x_{res}, s_{1res}) + e_2 s_2(x_{res}, s_{1mut}) R_2*(x_{res}, s_{1res}) - m$$

(8)

228   We can then compute the two coupled fitness gradients:

$$\left. \frac{\partial W_x(x_{mut}, x_{res}, s_{1res})}{\partial x_{mut}} \right|_{x_{mut} \to x_{res}} = e_1'(x_{mut}) s_{1res} R_1*(x_{res}, s_{1res}) + e_2 \frac{\partial s_2(x_{mut}, s_{1res})}{\partial x_{mut}} R_2*(x_{res}, s_{1res}) = 0$$

$$\left. \frac{\partial W_{s_1}(s_{1mut}, s_{1res}, x_{res})}{\partial s_{1mut}} \right|_{s_{1mut} \to s_{1res}} = e_1(x_{res}) R_1*(x_{res}, s_{1res}) + e_2 \frac{\partial s_2(x_{res}, s_{1mut})}{\partial s_{1mut}} R_2*(x_{res}, s_{1res}) = 0$$

(9)

229   The coevolutionary dynamics of the traits are then described by a system of coupled canonical

230   equations (Dieckmann and Law 1996):

$$\frac{dx}{dt} = \frac{1}{2} \mu_x \sigma_x^2 N^0(x_{res}, s_{1res}) \left. \frac{\partial W_x(x_{mut}, x_{res}, s_{1res})}{\partial x_{mut}} \right|_{x_{mut} \to x_{res}}$$

$$\frac{ds_1}{dt} = \frac{1}{2} \mu_{s_1} \sigma_{s_1}^2 N^0(x_{res}, s_{1res}) \left. \frac{\partial W_{s_1}(s_{1mut}, x_{res}, s_{1res})}{\partial s_{1mut}} \right|_{s_{1mut} \to s_{1res}}$$

(10)

The singularities are obtained by solving the system (10), which means finding x and s_1 values

that simultaneously nullify the two fitness gradients, (x^*, s_1^*). This is done by numerically solving

the equations in Mathematica with fixed parameter values. From the equations of the

coevolutionary dynamics, we can derive the Jacobian matrix and evaluate the conditions to obtain a

stable coalition (evolutionary attractor) for the singularity (x^*, s_1^*) (Marrow et al. 1996).

The Jacobian matrix J of the system (10) at the equilibrium (x^*, s_1^*) is:

$$J = \frac{1}{2} N^0 \left[\begin{array}{cc} \mu_x \sigma_x^2 \left(\dfrac{\partial^2 W_x}{\partial^2 x_{mut}} + \dfrac{\partial^2 W_x}{\partial x_{mut} \partial x_{res}} \right) & \mu_x \sigma_x^2 \dfrac{\partial^2 W_x}{\partial x_{mut} \partial s_{1res}} \\[2em] \mu_{s_1} \sigma_{s_1}^2 \dfrac{\partial^2 W_{s_1}}{\partial s_{1mut} \partial x_{res}} & \mu_{s_1} \sigma_{s_1}^2 \left(\dfrac{\partial^2 W_{s_1}}{\partial^2 s_{1mut}} + \dfrac{\partial^2 W_{s_1}}{\partial s_{1mut} \partial s_{1res}} \right) \end{array} \right]_{\substack{x_{mut} \to x_{res} \to x^* \\ s_{1mut} \to s_{1res} \to s_1^*}} \tag{11}$$

237   The condition to have a stable equilibrium (x^*, s_1^*) is that $Tr(J) < 0$ and $Det(J) > 0$. We note that the

238   diagonal terms correspond to the criteria of convergence in the monomorphic evolution, so if these

239   terms are negative, then $Tr(J) < 0$. The second condition is that $Det(J) > 0$ (which is the condition for

240   absolute convergence in Kisdi (2006). This condition can be expressed as:

$$\left[\left(\frac{\partial^2 W_x}{\partial^2 x_{mut}} + \frac{\partial^2 W_x}{\partial x_{mut} \partial x_{res}} \right) \left(\frac{\partial^2 W_{s_1}}{\partial^2 s_{1mut}} + \frac{\partial^2 W_{s_1}}{\partial s_{1mut} \partial s_{1res}} \right) > \frac{\partial^2 W_x}{\partial x_{mut} \partial s_{1res}} \frac{\partial^2 W_{s_1}}{\partial s_{1mut} \partial x_{res}} \right]_{\substack{x_{mut} \to x_{res} \to x^* \\ s_{1mut} \to s_{1res} \to s_1^*}} \tag{12}$$

241   We then numerically check that the two conditions are met at the singularities. We also adapt our

242   evolutionary algorithm in C++ to take account for the coevolution of the three traits and check that

243   the algorithm converges to the analytically obtained singularity values.

244 Results

245 1) Evolutionary dynamics of agriculture in the two trade-off scenarios

"Exploitation cost" scenario: managing the resource or consuming it.

In this scenario, increasing the intensity of niche construction negatively impacts the

consumption of the helped resource. We first study the general possible evolutionary dynamics

depending on the trade-off shape, then focus on the linear trade-off scenario to get a more thorough

mathematical investigation. As a first step, we do not specify the various functions implied in the

biological trade-off, in order to have a general analysis of possible evolutionary dynamics: we

ignore equations 2 and 3 and simply assume that s_1 decreases with x while e_1 increases with x.

Considering these assumptions in the fitness function definition (eq (4)) allows us to compute

the fitness gradient (eq (13)):

$$G(x_{mut}, x_{res}) = \frac{\partial W(x_{mut}, x_{res})}{\partial x_{mut}} = \left(e_1'(x_{mut}) s_1(x_{mut}) + e_1(x_{mut}) s_1'(x_{mut}) \right) R_1*(x_{res}) \qquad (13)$$

From this equation, we immediately note that if we do not consider a direct benefit to niche

construction ($e_1'(x_{mut})=0$), the fitness gradient becomes negative (as $s_1'(x_{mut})<0$). This leads to

gradual decrease of the trait and counter-selection of niche construction. This is consistent with the

result of Chisholm et al. (2018): considering a direct benefit (from pleiotropy or pseudo-

spatialization) is necessary to avoid a tragedy of the commons. That is inevitable given that our

completely mixed model implicitly assumes that all consumers have access to the farmed resource

(i.e., interaction is modeled by a mass action function). Variation in spatial access is a well-known

way to avoid this situation (Lion et al. 2011). To keep the model simple and tractable, we thus

consider an easier access to the constructed ressource, i.e.that $e_1'(x_{mut})>0$.

Assuming that the helped resource is not extinct ($R_1^*(x^*) > 0$), the position of singular strategies

x^* can be obtained from eq (14).

$$(e_1 s_1)'(x^*) = e_1'(x^*) s_1(x^*) + e_1(x^*) s_1'(x^*) = 0 \qquad (14)$$

This mathematical condition means that the singular strategies correspond to an optimum of the

realized consumption of the managed resource: if this strategy is an evolutionary endpoint,

evolution optimize total effective consumption of the managed resource, since the consumption

efficiency and specialization rate vary oppositely with agriculture trait x. We then expect

intermediate levels of agriculture to be selected for. In the scenario, we also note that the value of

the singular strategy only depends on this consumption-efficiency optimization: the densities of the

resources do not matter.

Replacing the fitness gradient with the chosen functions of equations 2 and 3 (in equation (14))

leads to:

$$\left(L - s_2^k - x^{*k}\right)^{\frac{1-k}{k}} \left(x^{*k} - \left(L - s_2^k\right) u\, x^{*u} + (1 + u) x^{*k+u}\right) = 0 \qquad (15)$$

275   The condition for non-invasibility and convergence (that are equivalent here, see Supplementary

276   Information for details) is:

$$(u-1) u\, x^{*u} \;-\; \frac{2u\, x^{*k+u}}{L - s_2^k - x^{*k}} \;-\; \frac{(k-1)\left(L - s_2^k\right) x^{*k}\left(1 + x^{*u}\right)}{\left(L - s_2^k - x^{*k}\right)^2} < 0 \qquad (16)$$

In the linear case ($u=k=1$), the equation (15) becomes $\left(x^* - (L - s_2) x^* + 2 x^{*2}\right) = 0$. We obtain

two possible singularities: $x^* = 0$ (which is a neutral case in the sense that the second derivative is

null) or $x* = \dfrac{(L - s_2 - 1)}{2}$ which is always convergent and non-invasible (CSS) (the second

derivative expressed in (16) is $\dfrac{-2 x*^2}{L - s_2 - x*}$ and is negative), it is an evolutionary endpoint.

While a completely general study using non-linear trade-offs is not possible, note that a

sufficient condition to obtain a CSS is that $u < 1$ and $k > 1$ (see equation (16)), in other terms

having diminishing returns of niche construction on resource consumption efficiency and a concave

trade-off between specialization and niche construction. If $u > 1$ and $k < 1$ (accelerating efficiency

and convex trade-off) the strategy may be characterized as a repellor (an unstable evolutionary

point) depending of the sign of our expression. In this case, directional selection brings the trait to

either zero niche construction (and total consumption), or total niche construction (and zero

consumption), the latter case being less likely biologically. We show the possible evolutionary

dynamics for different trade-off shapes in Supplementary Figure S1.

"Opportunity cost" scenario: managing one resource or foraging on another resource

When increasing agriculture occurs at a cost of the consumption of the alternative resource, the

invasion fitness of a mutant of trait x_{mut} appearing in a resident population of consumer with trait

x_{res} is derived:

$$W(x_{mut}, x_{res}) = e_1(x_{mut}) s_1 R_1*(x_{res}) + e_2 s_2(x_{mut}) R_2*(x_{res}) - m \qquad (17)$$

294 To obtain the fitness gradient $G(x_{mut}, x_{res})$ we consider the derivation of the fitness with respect to the

295 mutant trait x_{mut}:

$$G(x_{mut}, x_{res}) = \frac{\partial W(x_{mut}, x_{res})}{\partial x_{mut}} = e_1{}'(x_{mut}) s_1 R_1*(x_{res}) + e_2 s_2{}'(x_{mut}) R_2*(x_{res}) \qquad (18)$$

296 Singularities x^* are obtained through nulling $G(x^*,x^*)$. The position of the singularity depends on

297 optimizing both the consumption efficiency and the cost on the alternative resource consumption.

298 Contrary to the previous scenario, the resident agricultural trait x_{res} matters for the position of the

299 singularity. The non-invasibility condition is given for a general trade-off and for our chosen trade-

300 off functions in equation (18):

$$e_1''(x^*)s_1 R_1^*(x^*) + e_2 s_2''(x^*) R_2^*(x^*) < 0$$
$$e_1(u-1)u\,x^{u-2} s_1 R_1^*(x^*) + e_2(1-k)(L-s_1^k)\,x^{k-2}(L-x^{*k}-s_1^k)^{\frac{1}{k}-2} R_2^*(x^*) < 0 \tag{19}$$

In the linear case ($u = k = 1$), the invasibility criteria is null, but not necessarily the convergence

criteria. This can lead us to identify parameters set for which the strategy is convergent, and

invasible.

As in the previous scenario, we can get partial information in the non-linear cases. We obtain a

sufficient condition for non-invasibility of the singular strategy (equation (19)) (i.e. if this level of

agriculture is reached, it is an ESS): $u < 1$ and $k > 1$. A sufficient condition for the invasibility of

the point is that if $u > 1$ and $k < 1$. Those invasibility conditions are the same as for the

"exploitation cost" scenario invasibility condition. Conditions for evolutionary convergence are

however not tractable in the general case, and we only study numerically (see Supplementary

Information for the convergence condition).

2) Effect of specialization patterns on the evolutionary dynamics of

agriculture and feedbacks on the ecological dynamics

In the "exploitation cost" scenario, when we consider linear functions, we obtain a continuously

stable strategy (CSS) that is both convergent and non-invasible. The value of this selected level of

agriculture is expressed in eq 20:

$$x* = \frac{(L - s_2 - 1)}{2} \qquad\qquad (20)$$

316 This singular strategy is positive if $s_2 < L - 1$. If $s_2 > L - 1$, the value of the singularity becomes

317 negative and the niche constructing trait evolves to 0. From the expression of the singularity (eq

318 20) we show that the selected level of niche construction is is negatively correlated to

319 specialization on resource R_2, consistent with our predictions.

320 The consumption of the managed resource at the evolutionary equilibrium ($s_1(x*)$) is

$$s_1(x*) = L - s_2 - \frac{(L - s_2 - 1)}{2} = \frac{(L - s_2 + 1)}{2} \qquad\qquad (21)$$

We plot the value of the selected agriculture level and consequent consumption of the managed

resource, as a function of specialization on resource 2 in Figure 2 *A*. We represent the area of stable

coexistence of the species when resource 2 specialization s_2 and x vary (ecologically). We show

that the selected value of agriculture, $x*$ (represented as a black line) falls in the resource

coexistence area (the black arrows indicated the direction of evolution, meaning that starting from a

high value of agriculture, evolution brings the trait back into a coexistence area. The corresponding

equilibrium densities are shown on Figure 2 *B*. Increasing the consumption of the alternative

resource leads to a decrease in its evolutionary equilibrium density. The highest consumer

equilibrium density is obtained when the specialization on the alternative resource is intermediate

(and when the cultivated resource density is the lowest).

The slopes of the selected $x*$ and $s_1(x*)$ are the same (the lines are parallel), meaning that a higher

specialization on resource 2 equally impact niche constructing activities and exploitation of the

managed resource. This comes directly from our trade-off expression: mathematically, we assume

that the total amount of energy or time L is a linear combination of all the traits and here they all

have the same coefficient (i.e., 1). Were we to weight the different traits through different

coefficients, so that the variation of each trait does not have the same impact on the energy

allocation, then at the evolutionary equilibrium, modifying the specialization on resource 2 would

lead to weighted cost on agriculture investment and the resource 1 consumption (see

Supplementary Figure S2). In the non-linear CSS cases as well, the intensity of alternative resource

consumption is negatively correlated with the evolved level of agriculture (figure not shown). This

result is qualitatively the same when the strategy is a repellor. The singular strategy value is

positively related to the specialization on R_2, so that a higher specialization s_2 on the alternative

resource creates a larger basin of attraction for the zero niche construction state, i.e., niche

construction is more often counter-selected.(see Supplementary Figure S3).

In the "opportunity cost" scenario, we do not obtain an analytical value of the expected selected

level of agriculture: it is obtained by numerically nullifying the fitness gradient (equ. (18)), and

then computing convergence and invasibility criteria. We do this for a range of s_1 values in order to

investigate our prediction that higher specialization on the managed resource should select for

higher investment in agriculture. On Figure 3, we show the selected investment into agriculture in

CSS cases (evolutionary endpoint), as well as the resulting specialization on the alternative

resource, and the densities of the species at the evolutionary equilibrium.

When specialization on the managed resource s_1 is relatively low (left part of Fig 3 *A*), as predicted,

increasing s_1 leads to an increase in the selected agriculture intensity x^*. The level of foraging on

resource 2, $s_2(x^*)$ consequently decreases due to trade-off constraints. However, when s_1 is higher

(right part of Fig 3 *A*), the pattern is reversed: increasing s_1 selects for less agriculture. We can

explain this by considering the evolutionary equilibrium densities (Fig 3 *B*): because an increase in

s_1 decreases the foraging on resource 2 (blue line, Fig 3 *A*), the alternative resource suffers less

from the indirect effects. In the second part of the graph, it increases in density (green line). This

increases its profitability which selects for less niche construction.

As in the "exploitation cost" scenario, the selected agriculture level (x^*, purple line) falls in the

coexistence area represented in gray for all specialization values. Evolution of agriculture therefore

again favors the persistence of the system. This however depends on the trade-off shapes, and on

the effect of niche construction on the helped resource, that mediates apparent competition and

hence coexistence. We can obtain insight from how evolution could reduce coexistence from Fig 3

B: at low s_1, increasing specialization on the helped resource decreases the alternative resource

density at the evolutionary equilibrium. The evolution selects for more niche construction

(advantaging its competitor) and higher consumer densities at the equilibrium, then the alternative

resource suffers from a higher apparent competition. A even stronger pattern can lead to the

extinction the alternative resource. When the helped resource obtains even higher benefits from

niche construction (high conversion efficiency *w*), apparent competition is strong enough that for

intermediate R_1 specializations, R_2 may become extinct (see Supplementary Figure S4). In this case,

evolution kills the alternative resource but also destabilizes the community since it increases the

agricultural trait to levels where the consumer and the helped resource are involved in a very strong

positive feedback that produce an ever increasing dynamics.

Can evolution increase the diversity of the system?

We have seen that even though evolution mostly maintains the diversity in CSS scenarios (since

the selected trait *x** falls in the coexistence area) it can also disrupt it if apparent competition is too

strong. We now investigate whether the diversity in the system can be increased, in particular

through dimorphism in the consumer population.

In the "exploitation cost" scenario, because the non-invasibility and convergence criteria are

equivalent, the two only types of evolutionary dynamics are evolutionary endpoints (CSS) that

select for intermediate agriculture levels, or repellors leading to runaway evolution towards either

no niche construction or full niche construction (potentially destabilizing for the community) or to

intermediate levels of niche construction (see supplementary figure S1).

In the "opportunity cost", all types of singular strategies can be potentially obtained, combining

convergence and non-convergence, invasibility and non-invasibility. In particular, it is possible to

obtain convergent points that are invasible: evolutionary branching points. In such conditions, the

traits evolve towards the singularity value where disruptive selection is experienced. Dimorphism

can then be maintained in the consumer population. We illustrate these dynamics in Figure 4. If the

initial level of niche construction is high enough (that is, higher than the repellor value of the

singularity, around 0.4 in the example), it evolves towards the singularity (around 1.2) where it

experiences disruptive selection. We then observe the coexistence of two consumers in the

population, a "farmer" strategy with a high value of niche construction investment and a "predator"

strategy, not investing at all into niche construction. If initial niche construction investment is too

low, it is then counter-selected and evolves towards zero (which is consistent with the positive

nature of the feedbacks, we can expect threshold-dependent dynamics). This evolution leads to the

coexistence of the two resources. The farmer strategy is a full specialist on the helped resource. The

predator strategy consumes both preys, and is a relative generalist (here we have a higher

specialization on the alternative resource, which is a property of our parameters: we fixed s_1 to 0.5,

so evolution towards zero niche construction automatically brings s_2 to 1.5). The evolutionary

branching point that we obtain here is not linked to the trade-off between specialization and niche

construction shape ($k=1$) but to the niche "privatization" effect, that is the accelerating positive

effect of agriculture intensity on the consumption efficiency on the resource ($u=2$). This is intuitive:

providing diminishing returns to the farmer should favor generalism, while providing increasing

returns favors specialization and more niche construction.

3) Coevolution of the specialization and the agriculture investment traits.

Until now we have fixed one trait and considered two trade-off scenarios, namely the

opportunity cost and exploitation cost scenarios. We now assume that the three traits evolve

simultaneously while still respecting the trade-off constraint, which means that we are looking at

the coevolution of two traits, for instance x and s_1, and with s_2 being deduced from the two first and

trade-off (eq (2)).

We investigate whether our prediction of a correlation between the profitability of the cultivated

resource and the coevolution of specialization and agriculture on this resource. To do this, we vary

the intrinsic growth rates of the two resources (b_1 and b_2) which can represent a proxy for their

profitabilities, and explore how the values of the three traits at the coevolutionary equilibrium are

impacted. We present these results in Figure 5. In Fig 5 A, b_1 is varied and the values of the traits is

plotted. We show that as the profitability of R_1 increases, both x^* and s_1^* increase, which means an

increase in the consumer specialization on R_1 and the investment in its cultivation. Inversely, when

b_2 is increased (Fig 5 B), the profitability of resource R_2 increases, thus decreasing the evolution

towards specialization and agriculture on R_1. We then explore how the joint variation of the two

profitabilities determine the ecological state at the coevolutionary equilibrium. We show how the

selected agriculture investment (Fig 5 C) and relative preference on R_1 (Fig 5 D) increase with

increased relative profitability of R_1 compared to R_2. In Fig 5 E, we summarize the different

possible states of the system with three areas. When b_2 is high and b_1 is low (area 1), the consumer

is mostly specialized on the non cultivating resource at the equilibrium and investing less in

constructing R_1. When b_1 is intermediate and b_2 is high (area 2), the consumer is a generalist that

cultivates R_1 and consumes R_1 and R_2. When b_1 is high, the consumer evolves to predominantly

agricultural strategies with high investment into the cultivation and consumption of R_1.

Discussion

In this work, we have studied the evolution of niche constructing agriculture in a consumer-

resource perspective. Our initial prediction is that intuitively, cultivating a resource that the

consumer is not consuming (so, a resource that is not profitable) is not adaptive and is counter-

selected. We show a positive correlation between the evolution of agriculture and specialization on

the cultivated resource, both in the two trade-off scenarios (although the cost of agriculture

mitigates this result) and in the coevolution study.

In the "exploitation cost" scenario, we predicted that increasing the (fixed) specialization on the

alternative resource should decrease the investment into agriculture. In the "opportunity cost"

scenario, increasing the (fixed) specialization on the cultivated resource should increase the

investment into agriculture. These predictions are partly confirmed by our results. Indeed,

increasing the profitability of the alternative resource (via increased specialization) decreases the

investment for agriculture in the "exploitation cost" scenario. Conversely, increasing the

specialization on the cultivated resource increases the selected level of agriculture in the

"opportunity cost" scenario, although a further increase mitigate the profitability of the cultivated

resource through indirect effects, leading to a decrease in the selected level of agriculture.

The joint evolution of specialization and agriculture is analyzed in the coevolution scenarios,

where an increase in the profitability of the cultivated resource leads to an increase in the level of

investment into both specialization of this resource and cultivation of the resource, via the

emergence of an eco-evolutionary feedback between these two traits. This gives important insights

on the transitions from foraging-only to agriculture-only strategies, that may be observed in the

model, as well as on transitions from foraging-only to facultative farmers (or facultative foragers).

This question that we here investigated here from a niche construction/agriculture perspective is

well suited to understand the evolution of mutualism or symbiosis. For instance, some ants perform

facultative agriculture (on aphids or fungi) and usually remain generalist, while other taxa are

obligate farmers of fungi (Chapela et al. 1994; Stadler and Dixon 2005) or aphids (Ivens et al.

2016) in which cases many specialized traits are observed. We here show that such dynamics may

emerge from foraging theory constraints (that may be linked to physiology, but also to resource

densities, dynamics). In our model, we do not investigate whether the net interaction is mutualistic

for the helped resource, because this has been proven difficult to measure experimentally (context-

dependency of interactions (Chamberlain et al. 2014), multiple components of fitness) but we

implement both a positive and a negative aspect of the interaction. For instance, in the ant-aphid

interaction, it is unclear whether this can be qualified as mutualism or exploitation (Offenberg

2001; Stadler and Dixon 2005; Billick et al. 2007).

One of the two questions that stimulated our study was to improve our understanding of the

conditions under which agriculture may evolve. The other one, is the effect of this evolution on the

ecological dynamics and in particular the coexistence of cultivated and non-cultivated resources.

This aspect is here mediated by the indirect interactions occurring in the system, particularly

apparent competition. Apparent competition has been experimentally described in agricultural

systems where a predator has a positive effect of one of its preys, notably in aphid-tending ant

increasing the predation on other arthropods (Warrington and Whittaker 1985; Wimp and Whitham

2001). In our model, we note that evolution does not optimize densities: this result that could seem

counter-intuitive is rather well known when considering adaptive dynamics studies (Metz et al.

2008; Boudsocq et al. 2011). Second, we show that evolution of agriculture may favor coexistence

in the system. In the "exploitation cost" scenario, without evolution, we expect that increasing

specialization on the alternative resource should reduce coexistence, as it increases predation

pressure on the resource which does not benefit from niche construction. When we consider

evolution though, the decreased selected level of niche construction compensates for this effect and

rescues the alternative resource, thus favoring coexistence. We can observe similar patterns in the

"opportunity cost" scenario. Adaptive foraging is also known to improve coexistence of resources

by mitigating apparent competition in purely trophic systems (Abrams 2010). We note however

that this evolutionary facilitation of coexistence is dependent on costs and benefits. Especially, in

cases where the efficiency of niche construction is very high, even if the evolution mitigates the

stronger apparent competition that the alternative resource suffers from, it might not be enough to

rescue it. Such effects may be linked to natural observations. In devil's gardens, ants kill

competitors of their host plant species thereby actively limiting coexistence at a local scale (Frederickson et al. 2005). In our model, runaway evolution toward high niche construction may yield large positive feedbacks, potentially destabilizing the system and leading to the exponential growth of the consumer and helped resource. Such infinite increases could be avoided if we considered diminishing returns of niche construction, for instance, if niche construction is limited by other parameters. This addition to the model has been shown to stabilize the ecological dynamics within this module (Picot et al. 2019).

Evolution of agriculture in our model assumed two main hypotheses. First, that agriculture occurs at a cost, here constraining the foraging of resources (either the cultivated one or the alternative one) ; second, that agriculture provides a direct benefit to the organism that performs it. This direct benefit can also be interpreted as a trade-off between the consumption efficiency of resource 1 and its non-cultivation, and allows the evolution of agriculture because it limits the invasion of cheaters that would not pay the cost of agriculture investment. Such a scenario has been described in a model of niche construction in which pleiotropy allows the maintenance of niche construction (Chisholm et al. 2018). If there is a positive correlation between the investment and the returns, costly niche construction may evolve. If the direct benefits of niche construction are accelerating with increasing niche construction intensity, evolution can lead to dimorphism in the consumer population. We then observe the coalition of a highly specialized farmer, that invests a lot in niche construction and only preys on the helped resource, and of a generalist predator strategy that performs no or very low agriculture. This latter could be considered a cheater in the evolution of cooperation terminology: it consumes the resource that is maintained by niche construction, without paying the cost of agriculture (but see Ghoul et al. (2013). Because of the direct benefit that the farmer obtains from the exploitation of the helped resource ("privatization" or "monopoly" (Krakauer et al. 2009; Chisholm et al. 2018; Scheiner et al. 2021), the invasion of the cheater is avoided and the two phenotypes coexist.

Increasing the number of consumers also stabilizes the system: similar to exploitative

competition where two consumers may coexist when consuming two shared resources (according

to the R^* rule, (Tilman 1980)), in apparent competition, resources are more likely to coexist if they

are consumed by n consumers because it balances apparent competition (similarly to the P^* rule,

(Holt et al. 1994)). If the consumer population is considered as a whole comprised of two

subpopulations, we can then interpret this coalition as division of labor, or functional

specialization, between farmers and foragers. This type of division of labour has been investigated

in theoretical works which stress the importance of considering high benefits to specialization or

accelerating returns (Rueffler et al. 2012; Cooper and West 2018). This is consistent with our

model, and recalls the importance of trade-off geometries in evolutionary dynamics of

specialization (de Mazancourt and Dieckmann 2004; Egas et al. 2004; Ravigné et al. 2009; Kisdi

2014). From an evolution of specialization perspective, the coalition between niche-constructors

and non-constructors is also a coalition between a specialist and a generalist. The question of the

coexistence of specialists and generalists have often been frequently investigated from a purely

trophic context (Egas et al. 2004; Abrams 2006; Rueffler et al. 2006). Our model provides various

dynamics that emerge from simple assumptions, and these results can be understood both in the

evolution of cooperation and evolution of specialization framework. The coevolution analysis

allows to describe situations where if a potentially cultivable resource is profitable enough, it might

be advantageous to switch from a generalist forager to a specialized farmer, which can explain

evolutionary transitions from foraging-only to settled agriculture behaviours.

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 Figures

Figure 1: A) The module: the consumer C (in brown) consumes resources R_1 (in orange) and R_2 (in

green) according to respective specialization rates s_1 and s_2. The resource R_1 receives an additional

positive effect through niche construction (agriculture) performed by the consumer. B) Different

trade-off shapes determine the dependency between the three traits. Typically, concave trade-offs

(here $k=2$) and convex trade-offs are considered ($k=0.8$).

Figure 2: Effect of specialization on resource 2 on the evolutionary and ecological dynamics in the

"exploitation cost" scenario. A) effect on the selected level of niche construction x^* (in purple, the

arrows indicate the direction of evolution) and subsequent consumption of resource 1, $s_1(x^*)$ (in

orange). The area of stable ecological coexistence of the three species when varying agriculture and

the specialization on R_2 (i.e., in a (s_2,x) plane) is represented in grey. B) effect on the species

densities at the ecological evolutionary equilibrium (that is at the selected niche construction): the

consumer is in brown, R_1 is in orange, R_2 is in green. $b_1 = b_2 = 2$, $g_1 = g_2 = 0.8$, $e_1 = e_2 = 1$, $L = 2$,

$w = 1$, $m = 0.8$, $k = 1$, $u = 1$

Figure 3: Effect of specialization on resource 1 on the evolutionary and ecological dynamics in the

"opportunity cost" scenario. A) effect on the selected level of niche construction x^* (in purple, the

arrows indicate the direction of evolution) and subsequent consumption of resource 2, $s_2(x^*)$ (in

green). The area of stable ecological coexistence of the three species when varying agriculture and

the specialization on R_1 (i.e., in a (s_1,x) plane) is represented in grey. B) effect on the species

densities at the ecological evolutionary equilibrium (that is at the selected niche construction): the

consumer is in brown, R_1 is in orange, R_2 is in green. $b_1 = b_2 = 2$, $g_1 = g_2 = 2$, $e_1 = e_2 = 2$, $L = 2$, w

$= 0.1$, $m=2$, $k=2$, $u=0.5$

Figure 4: Evolutionary branching leading to dimorphism in agriculture investment, in the

"opportunity cost" scenario. A: Pairwise Invasibility Plot, the sign of the fitness of a mutant of trait

x_{mut} appearing in a population of trait x_{res} is shown (white for negative, black for positive). The pink

arrows indicated the direction of evolution. B: Evolution trajectory of the investment into

agriculture: the trait experiences disruptive selection at the convergent singularity leading to two

coexisting phenotypes. C: final module with traits values (in color) and population densities (in

black): the width of the arrows represents the trait value, not the net interaction (eg, the net per

capita effect of C on R_1 is $s_1 - w\,x = 0.35$). Values are: $s_1=0.5$, $k=1$, $u=2$, $w=0.1$, $b_1=b_2=3$, $g_1=g_2=2$,

$e_1=e_2=2$, $m=2$.

Figure 5: Coevolutionary dynamics. A) Correlation between the profitability of R_1 and the

values of the traits at the coevolutionary equilibrium (attractor, CSS): x^* is shown in purple, s_1^* in

orange, and s_2^* in green. B) Correlation between the profitability of R_2 and the values of the traits

at the coevolutionary equilibrium (attractor, CSS): x^* is shown in purple, s_1^* in orange, and s_2^* in

green. C) Values of the niche construction trait at the coevolutionary equilibrium in the two

resources profitabilities plane. D) Relative resource preference at the coevolutionary equilibrium:

the consumer is more specialized on R_1 in the orange area and more specialized on R_2 in the green

area. E) Module state in the different areas defined by the profitabilities of the resources. When b_2

is high and b_1 is low (area 1), the consumer is mostly specialized on the non cultivating resource at

the equilibrium and investing less in constructing R_1. When b_1 is intermediate and b_2 is high (area

2), the consumer is a generalist that cultivates R_1 and consumes R_1 and R_2. When b_1 is high, the

consumer evolves to predominantly agricultural strategies with high investment into the cultivation

and consumption of R_1.

Values are: $g_1=g_2=2$, $e_1=e_2=2$, $L=3$, $w=0.1$, $k=2$, $u=2$, $m=1$. In panel A, $b_2=1$. In panel B, $b_1 = 1$.