

1 **Computational Design and Analysis of**
2 **Modular Cells for Large Libraries of**
3 **Exchangeable Product Synthesis Modules**

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Abstract

Microbial metabolism can be harnessed to produce a large library of useful chemicals from renewable resources such as plant biomass. However, it is laborious and expensive to create microbial biocatalysts to produce each new product. To tackle this challenge, we have recently developed modular cell (ModCell) design principles that enable rapid generation of production strains by assembling a modular (chassis) cell with exchangeable production modules to achieve overproduction of target molecules. Previous computational ModCell design methods are limited to analyze small libraries of around 20 products. In this study, we developed a new computational method, named ModCell-HPC, capable of designing modular cells for large libraries with hundredths of products with a highly-parallel and multi-objective evolutionary algorithm. We demonstrated ModCell-HPC to design *Escherichia coli* modular cells towards a library of 161 endogenous production modules. From these simulations, we identified *E. coli* modular cells with few genetic manipulations that can produce dozens of molecules in a growth-coupled manner under different carbon sources. These designs revealed key genetic manipulations at the chassis and module levels to accomplish versatile modular cells. Furthermore, we used ModCell-HPC to identify design features that allow an existing modular cell to be re-purposed towards production of new molecules. Overall, ModCell-HPC is a useful tool towards more efficient and generalizable design of modular cells to help reduce research and development cost in biocatalysis.

Keywords: Modular cell design; Modular (chassis) cell; Production Modules; Compatibility; ModCell; ModCell-HPC; Multiobjective optimization; Multiobjective evolutionary algorithm; Master-slave parallelization; Island parallelization; High performance computing.

38 1 Introduction

39 Modular design has gained recent interest as an effective approach to understand and re-
40 design cellular systems.¹ In the fields of metabolic engineering and synthetic biology, var-
41 ious modularization strategies²⁻⁷ have been proposed to address the slow and expensive
42 design-build-test cycles of developing microbial catalysts for renewable chemical synthesis.⁸
43 A promising system-level modularization⁹ approach is ModCell,⁴ that aims to design a mod-
44 ular (chassis) cell compatible with exchangeable production modules that enable metabolite
45 overproduction. ModCell could be used as an effective tool to design modular cells capable
46 of efficiently producing a vast number of molecules offered by nature with minimal strain
47 optimization requirements,^{10,11} but it remains unexplored for large product libraries.

48 Previous efforts in computational modular cell design are limited to analyze small libraries
49 of around 20 products.^{4,6} However, the design of modular cells for larger product libraries
50 is both of practical and theoretical interest. Theoretically, using large libraries can lead to
51 more general modular cell design rules, which might help to explain the naturally existing
52 modularity of metabolic networks.¹ Practically, such modular cells could be implemented
53 with genetic engineering techniques that enable rapid pathway generation, such as combina-
54 torial ester pathways,¹² and where the modular cell could serve as a versatile platform for
55 pathway selection and optimization using adaptive laboratory evolution.¹³

56 Modular cell design was formulated as a multi-objective optimization problem (MOP),
57 named ModCell2, where each target phenotype activated by a module is an independent ob-
58 jective.⁴ ModCell2 was solved with multi-objective evolutionary algorithms (MOEAs) that
59 used a master-slave parallelization scheme, where the objective functions are evaluated in
60 parallel by slave processes, but every other step in the algorithm is performed serially (Fig-
61 ure 1 a).^{4,5} This approach contains many serial steps, and hence limits the scalability of
62 the algorithm with the number processes according to Ahmdal's law.¹⁴ In particular, large
63 population sizes, an effective strategy to deal with many objectives,^{5,15} can dramatically slow
64 down serial algorithm operations such as non-dominated sorting in NSGA-II,¹⁶ one of the

65 best performing MOEAs to solve ModCell2.⁵ Furthermore, increasing the product library size
66 for ModCell leads to very large multi-objective optimization problems, which are notoriously
67 difficult to solve.^{17,18} Therefore, the master-slave approach used in ModCell2 is not suitable
68 to analyze large problems that contain hundredths of exchangeable production modules. A
69 new parallelization approach that uses high-performance computing (HPC) more effectively
70 is needed to advance ModCell.

71 In recent years, multiple approaches to harness HPC have been developed to solve single-
72 objective evolutionary algorithms (EA).¹⁹ In particular, the island-parallelization approach
73 has been proposed, where multiple instances of the EA are run independently but communi-
74 cate with each other to enhance overall convergence towards optimal solutions (Figure 1 b).
75 This new approach helps address the serial bottlenecks of the master-slave approach by sep-
76 arating the algorithm into highly independent processes that directly map to the computing
77 hardware. While this approach has not been thoroughly examined in MOEA, there are a few
78 successful applications to specific design problems.^{20–22}

79 In this study, we developed ModCell-HPC, a highly parallel MOEA that uses the island
80 parallelization approach to solve modular cell design problems with hundredths of objectives.
81 We demonstrated ModCell-HPC to design *Escherichia coli* modular cells with a large pro-
82 duction module library of metabolically and biochemically diverse endogenous compounds.
83 Analysis of these designs revealed key genetic manipulations both at the chassis and module
84 levels required for highly compatible modular cells. Furthermore, we designed modular cells
85 for conversion of various hexoses and pentoses, since these sugars are the main components
86 of biomass feedstocks.²³ Finally, we used ModCell-HPC to identify the features of a modular
87 cell that makes it compatible towards new production modules.

88 2 Methods

89 2.1 Multi-objective optimization formulation of modular cell de- 90 sign problem

The modular (chassis) cell is built in a top-down manner by removing metabolic functions from a parent strain, and then inserting exchangeable modules into the chassis to create production strains that optimally display the target phenotypes. Due to the conflicting biochemical and metabolic requirements of different product synthesis pathways, the modular cell design problem is formulated as the following MOP known as ModCell2:⁴

$$\max_{y_j, z_{jk}} (f_1, f_2, \dots, f_{|\mathcal{K}|})^T \quad \text{s.t.} \quad (1)$$

$$f_k \in \arg \max \left\{ \frac{1}{f_k^{max}} \sum_{j \in \mathcal{J}_k} c_{jk} v_{jk} \quad \text{s.t.} \right. \quad (2)$$

$$\left. \sum_{j \in \mathcal{J}_k} S_{ijk} v_{jk} = 0 \quad \text{for all } i \in \mathcal{I}_k \right. \quad (3)$$

$$l_{jk} \leq v_{jk} \leq u_{jk} \quad \text{for all } j \in \mathcal{J}_k \quad (4)$$

$$l_{jk} d_{jk} \leq v_{jk} \leq u_{jk} d_{jk} \quad \text{for all } j \in \mathcal{C} \quad (5)$$

$$\left. d_{jk} = y_j \vee z_{jk} \right\} \quad \text{for all } k \in \mathcal{K} \quad (6)$$

$$z_{jk} \leq (1 - y_j) \quad \text{for all } j \in \mathcal{C}, k \in \mathcal{K} \quad (7)$$

$$\sum_{j \in \mathcal{C}} z_{jk} \leq \beta \quad \text{for all } k \in \mathcal{K} \quad (8)$$

$$\sum_{j \in \mathcal{C}} (1 - y_j) \leq \alpha \quad (9)$$

91 This MOP simultaneously maximizes all objectives f_k (1), where k belongs to the set of
92 production networks \mathcal{K} . Each production network represents the combination of the chassis
93 with a specific production module, and it is simulated through a stoichiometric model²⁴ (2-6)
94 with a set of metabolites \mathcal{I}_k and a set of reactions \mathcal{J}_k . The stoichiometric model predicts

95 metabolic fluxes according to the following constraints: (i) mass-balance (3), where S_{ijk}
96 represents the stoichiometric coefficient of metabolite i in reaction j of production network
97 k , (ii) flux bounds (4) that determine reaction reversibility and available substrates, where
98 l_{jk} and u_{jk} are lower and upper bounds respectively, and (iii) genetic manipulation (5), i.e.,
99 deletion of a reaction j in the chassis through the binary indicator y_j , or insertion of a
100 reaction j in a specific production network k through the binary indicator z_{jk} . Only a subset
101 of all metabolic reactions, \mathcal{C} , are considered as candidates for deletion, since many of the
102 reactions in the metabolic model cannot be manipulated to enhance the target phenotype.

103 The desirable phenotype f_k for production module k is determined based on key metabolic
104 fluxes v_{jk} (mmol/gDCW/h) predicted by the model (2-5). For this study, we selected the
105 weak growth coupled to product formation (*wGCP*) design objective that requires a high
106 minimum product synthesis rate at the maximum growth rate, enabling growth selection of
107 optimal production strains. Hence, in *wGCP* design, the inner optimization problem seeks
108 to maximize growth rate while calculating the minimum product synthesis rate through the
109 linear objective function (2). Here c_{jk} is 1 and -0.0001 for j corresponding to the biomass
110 and product reactions across all networks k , respectively, and 0 otherwise. In general, the
111 definition of f_k needs not be linear and other design phenotypes can be defined.⁴

112 Finally, design constraints (7-9) define the limitations of the design variables representing
113 genetic manipulations, y_j and z_{jk} . As part of modular cell design, reactions can be removed
114 from the chassis but inserted back to specific production modules, enabling the chassis to be
115 compatible with a broader number of modules (7). The total numbers of module reaction
116 additions and reaction deletions in the chassis are limited by parameters β (8) and α (9),
117 respectively.

To define the solutions of ModCell2 (1-9), the general multi-objective optimization prob-
lem with design variables x from a set \mathcal{X} and objective functions $f_i(x)$ is expressed as follows:

$$\max_x F(x) = (f_1(x), f_2(x), \dots)^T \forall x \in \mathcal{X}$$

The solution of such an optimization problem is denoted as a Pareto set:

$$\mathcal{PS} := \{x \in \mathcal{X} : \nexists x' \in \mathcal{X}, F(x') \prec F(x)\}$$

Here $F(x') \prec F(x)$ indicates that the objective vector $F(x')$ *dominates* $F(x)$, defined as $f_i(x') \geq f_i(x)$ for all objectives i , and $f_i(x') \neq f_i(x)$ for at least one i . Hence, the Pareto set contains all non-dominated solutions to the optimization problem; that is, when comparing any two non-dominated solutions, the value of a certain objective must be diminished in order to increase the value of a different objective. The projection of the Pareto set on the objective space is denoted as a Pareto front:

$$\mathcal{PF} := \{F(x) : x \in \mathcal{PS}\}$$

118 2.2 Implementation of many-objective evolutionary algorithm with 119 high-performance computing

120 To overcome the issues of the master-slave approach (Figure 1 a) used in ModCell2,⁴ we
121 implemented an island parallelization scheme,¹⁹ where each computing process is an instance
122 of the MOEA (Figure 1 b). These instances exchange individuals (i.e., potential solutions) in
123 a process called migration, hence enhancing overall convergence towards optimal solutions
124 (Figure 1 c). The migration operation can be performed in different modes, depending
125 on which individuals from the local population are exchanged, and also how often such
126 exchanges happen. These options are captured by the migration type and migration interval
127 parameters, respectively (Table 1). To enhance performance and scalability, the migration
128 process was implemented asynchronously, i.e., the population within each island can continue
129 to evolve without a need to wait for sent individuals to arrive at their destination island or
130 for incoming individuals to be received.

131 To improve the quality of the MOEA solutions, we implemented two post-processing steps

132 specific to ModCell (Figure S1): First, we eliminate *futile module reactions*. These module
133 reactions once removed do not diminish the objective value of the associated production
134 network. Second, we coalesce multiple designs with the same deletions but different module
135 reactions. This combination helps obtain a superior solution.

136 The software implementation of the proposed island-MOEA, denoted *ModCell-HPC*, is
137 written in the C programming language and available at [https://github.com/TrinhLab/
138 modcell-hpc](https://github.com/TrinhLab/modcell-hpc).

139 **2.3 Computation hardware**

140 We conducted all ModCell-HPC computations in *beacon* nodes from the Advanced Comput-
141 ing Facility at the Joint Institute for Computational Science, The University of Tennessee
142 and Oak Ridge National Laboratory. Each node contains a 16 core Intel Xeon E5-2670 cen-
143 tral processing unit (CPU) and 256 GB of random access memory (RAM). The results were
144 analyzed in a desktop computer with an Intel Core i7-3770 CPU and 32 GB of RAM.

145 **2.4 Target product identification**

146 The target products are endogenous *E. coli* metabolites that meet the following requirements:
147 i) their maximum theoretical yields are above 0.1 (mol product/mol of substrate); ii) they
148 are organic; and iii) they could be produced anaerobically in a growth coupled manner with
149 a yield above 50%, a property determined in a previous study.²⁵ If a given metabolite meets
150 all these conditions but appears in multiple compartments, only one location is chosen.
151 Implementation of these selection criteria resulted in 161 target metabolites. Metabolites
152 that did not have a secretion mechanism originally present in the model required an exchange
153 pseudo-reaction that represents metabolite secretion to the growth medium or intracellular
154 accumulation at steady-state. The products in the selected library have diverse molecular
155 weights and are overall highly reduced (Figure S2).

156 **2.5 Model configuration**

157 We used the iML1515 *E. coli* model²⁶ for all simulations. To configure the model, glucose
158 uptake was set to 15 (mmol/gCDW/h); the default ATP maintenance value in iML1515 was
159 used; 20% of the maximum anaerobic growth rate was used as the minimum growth rate,
160 corresponding to 0.0532 (1/h); and only commonly observed fermentation products were
161 allowed for secretion. This model configuration is equivalent to the previous modular cell
162 design studies⁴ except for the higher glucose uptake rate. This rate was increased to match
163 the study of Kamp and Klamt²⁵ which was partially used here to identify target products.

164 **2.6 Design characterization**

165 **2.6.1 Compatibility**

166 An important qualitative feature of a designed modular (chassis) cell is module compatibility.
167 The chassis is *compatible* with a module if the performance of the resulting production strain
168 is above a defined threshold of design objective value. In this study, we used the *wGCP* design
169 objective that corresponds to the minimum product yield at the maximum growth rate,⁴ and
170 selected a threshold of 0.5 to establish compatibility. Under these conditions, we expect a
171 module compatible with the chassis can lead to a product yield above 50% of the theoretical
172 maximum during the growth phase. The *compatibility* of a modular cell is defined as the
173 number of modules that are compatible with it.

174 **2.6.2 Minimal covers**

175 A *minimal cover* is the smallest group of modular cells needed to ensure all potentially
176 compatible products in a library are compatible with at least one of the modular cells.
177 To identify minimal (set) covers computationally, we use the classical integer programming
178 formulation:

$$\min_{x_h \in \{0,1\}} \sum_{h \in \mathcal{H}} (\gamma_h x_h) \quad (10)$$

subject to:

$$\sum_{h \in \mathcal{H}} a_{hk} x_h \geq 1 \quad \forall k \in \mathcal{K}' \quad (11)$$

179 This optimization problem minimizes the number of designs in the set cover, where \mathcal{H} is
180 the set of strain designs, h , produced by ModCell-HPC (10). The binary indicator variable
181 x_h takes a value of 1 if design h is selected as part of the set cover and 0 otherwise. Certain
182 designs can be prioritized (e.g., they contain preferable genetic manipulations) using the
183 weighting parameter γ_h . However, we set $\gamma_h = 1$ in all our simulations. All compatible
184 products k must be included in at least one of the selected designs (11). The parameter a_{hk}
185 takes a value of 1 if product k is compatible with design h and 0 otherwise. There must exist
186 at least one $h \in \mathcal{H}$ for which $a_{hk} = 1$ to ensure a feasible solution exists; therefore, \mathcal{K}' is the
187 subset of products compatible in at least one design of \mathcal{H} .

To enumerate all minimal covers, we iteratively solved the minimal cover problem (10-11) with the addition, in each iteration, of an integer cut inequality (12) that removes a previously found solution \mathcal{S} .

$$\sum_{h \in \mathcal{S}} x_h \leq |\mathcal{S}| - 1 \quad (12)$$

188 2.7 Coverage performance indicator

Algorithm performance is tested against several parameter configurations, each producing a Pareto front approximation (\mathcal{PF}). All resulting Pareto fronts are gathered into a reference Pareto front (\mathcal{PF}^*). Coverage, C , is defined as the fraction of solutions in \mathcal{PF}^* captured by a given approximation \mathcal{PF} :

$$C = \frac{|\mathcal{PF} \cap \mathcal{PF}^*|}{|\mathcal{PF}^*|} \quad (13)$$

189 In our analysis, we only used unique non-dominated points in both \mathcal{PF} and \mathcal{PF}^* to avoid
190 many alternative solutions from biasing the coverage indicator.

191 **3 Results**

192 **3.1 Tuning of ModCell-HPC method parameters**

193 A known challenge of heuristic optimization approaches is their reliance on parameter tun-
194 ing for rapid convergence towards optimal solutions. To identify sensible default parameters
195 for ModCell-HPC, we first scanned parameter combinations with a previous 20-objectives
196 problem⁴ that is fast to solve, then focused on the most relevant parameters for a large-scale
197 problem with 161 objectives corresponding to the current product library. In both cases,
198 we used two performance metrics to identify the best algorithm parameters: i) *Coverage*,
199 that indicates the fraction of Pareto optimal solutions identified by a given parameter con-
200 figuration (Section 2.7). ii) *minimal cover size*, i.e., the smallest number of modular cells
201 needed to ensure all compatible products in the library that are compatible in at least one
202 (Section 2.6.2). Coverage is a general and unbiased quantitative measure which is preferred
203 over other similar metrics based on a previous study,⁵ while minimal cover size is based on
204 practical goals.

205 In our initial benchmark study with the 20-objectives problem, we screened different to-
206 tal run times, migration interval, migration types, and population sizes (Table 1) for best
207 achieving modular cell designs. The design parameters were set to $\alpha = 6$ and $\beta = 1$, which
208 are sufficient to find highly compatible designs.⁶ For 1-hour run time, we observed the small-
209 est population size (100) reached more generations (Figure S3 e,f) and hence achieved better
210 results in both metrics (Figure S3 a,b). However, for a 2-hours run time, both population
211 sizes of 100 and 500 attained similar cover sizes (Figure S3 g), indicating that a minimum of
212 approximately 150 generations (Figure S3 e,f,k,l) is necessary for convergence of this prob-
213 lem, irrespective of the population size. Taken together, the different performance between

214 100 and 500 population sizes in relation to run time indicates that under limited run times
215 an optimal population size could be found to attain sufficient generations for convergence.
216 The migration interval only appeared detrimental at the highest value of 50 with the smallest
217 population size of 100 at 1 hour (Figure S3 a,b,g,h); otherwise this parameter was consid-
218 ered secondary, and hence an intermediate value of 25 was selected for further simulations.
219 Similarly, migration policy also appeared to be a secondary parameter; nonetheless, the “Re-
220 placeBottom” migration policy was selected for further simulations since it is better or equal
221 to the “Random” policy in all cases (Figure S3 c,d,i,j).

222 For the large-scale benchmark with 161 products, we investigated the importance of run
223 time, population size, and the number of computational cores (Table 1). For this benchmark,
224 the design parameters were set to $\alpha = 10$ and $\beta = 2$ to enable successful designs without
225 a large number of genetic modifications that can lead to unrealistic model predictions and
226 implementation requirements. We evaluated 5 and 10 hour run times. For 5-hours run
227 time, a population size of 200 was better in all metrics (Figure 2 a,b,c,e,f,g) and reached
228 50-100 generations (Figure 2 d). For a 10-hours run time, the population sizes of 200 and
229 300 had equivalent performance (Figure 2 e-g), despite the population size of 200 reaching
230 approximately 50 generations more than the 300 population size. The population size of
231 100 underperformed at both run-times (Figure 2 a,b,e,f). Taken together, this large-scale
232 benchmark study indicates that after a given number of generations, larger population sizes
233 are comparable as long as they are above a minimum size. Hence, a population size of 200 is
234 the minimum required for proper convergence and should be used under limited run times.
235 Increasing the number of cores leads to more solutions (Figure 2 c,g), due to a larger meta-
236 population (the total population of all islands). However, additional cores do not necessary
237 find better solutions in terms of minimal cover size and individual product compatibility
238 (Figure 2 b,f). These indicators plateaued at around 48 cores in both cases so this value was
239 used for further simulations. Alternative communication topologies among islands²⁷ may
240 provide better scaling with cores but were not explored here.

241 In summary, the benchmark performed here aims to provide a general guideline to use the
242 ModCell-HPC. Furthermore, this parameter meta-optimization procedure can be repeated
243 to fine-tune the algorithm to specific problem features (e.g., number of objectives) and
244 computational resources available (e.g., run time and computing cores).

245 **3.2 Design of *E. coli* modular cells for large product library**

246 **A small number of genetic manipulations are sufficient for highly compatible**
247 **modular cell** After tuning ModCell-HPC, we used it to design *E. coli* modular cells for our
248 library of 161 products. First, we scanned a broad range of design parameter combinations
249 (α - β : 5-1, 10-2, 20-4, and 40-8) to identify the required genetic manipulations for highly
250 compatible designs (Figure S4 a). Increasing the number of genetic manipulations led to
251 an average increase in design compatibility. However, the maximum compatibility remained
252 around 50% of the library (80 products) for all cases. This result indicates that highly
253 compatible modular cells can be built with a small number of genetic manipulations. We
254 selected the designs with $\alpha = 5$, $\beta = 1$ (Supplementary Material 2) for further analysis,
255 since designs with few genetic manipulations are more accurately simulated and also better
256 to implement in practice.

257 **A few reaction deletions in central metabolism targeting byproducts and branch-**
258 **points are key to build modular cells** We sorted reaction deletions according to how
259 often they appear across designs (Table 2). The top 7 reactions are used $\geq 10\%$ of the de-
260 signs and belong to central metabolism, indicating their importance to accomplish growth-
261 coupled-to-product-formation phenotypes. Overall, the role of these deletions can be classi-
262 fied into two functions: i) to eliminate major byproducts and ii) to alter key branch-points
263 in metabolism that influence the pools of precursor metabolites, including carbon, redox,
264 and energy precursors. The first type of manipulations is generally intuitive and often used
265 in metabolic engineering strategies.²⁸ The second type of manipulations are not commonly

266 identified unless metabolic model simulations are used,^{29–31} even though the importance of
267 targeting metabolic branch-points was noted early.³² An example of this second type observed
268 in our designs is TPI deletion, that activates the methylglyoxal bypass,³³ reducing the overall
269 ATP yield resulting from glucose conversion into pyruvate. Lower ATP yield limits biomass
270 formation hence redirecting carbon flow towards products of interest. While such strategies
271 are not common, TPI deletion predicted by model simulations was successfully used for en-
272 hanced 3-hydroxypropionic acid production,²⁹ and ATP wasting has recently been proposed
273 to enhance production of certain molecules.³⁴ Another example of branch-point manipulation
274 is PPC deletion, that has been shown to lower flux from lower glycolysis towards the TCA
275 cycle,^{35,36} resulting in lower succinate production, and an increased pool of *pep*, pyruvate
276 and acetyl-CoA. Additionally, PPC deletion to increase the *nadph* pool for production of
277 flavonoids was predicted by model simulation and experimentally validated.³¹ In summary,
278 design of highly compatible modular cells requires not only major byproduct removal, but
279 also manipulation of key branch points in central metabolism.

280 **Module reaction usage reveals pathway interfaces and unbiased module definition**

281 The modular cell optimization formulation (Section 2.1) not only identifies genetic manipu-
282 lations in the modular cell, but also in the production modules. Module reactions correspond
283 to reactions deleted in the chassis but inserted back in specific production modules to enable
284 compatibility. We examined the module reactions used by all designs (Figure 3). As ex-
285 pected, ALCD2x, ACKr, and LDH_D, are used by ethanol, acetate, and lactate production
286 networks, respectively. More notably, we also observed several reaction modules are used for
287 specific products, for example, MDH and FUM 3-methyl-2-oxobutanotae and 2,3-dihydroxy-
288 3-methylbutanoate, resepectively, that are naturally precursors of valine and artificially of
289 isobutanol^{37,38}. These module reactions likely play a role in both the synthesis of relevant
290 TCA precursors and the secretion of succinate as an electron sink. Interestingly, fatty acids
291 tend to use TPI, which as mentioned earlier, its deletion activates the methylglyoxal bypass

292 lowering the overall ATP yield. The first step in fatty acid biosynthesis, acetyl-CoA carboxy-
293 lase, requires one ATP per mol of malonyl-CoA, explaining the usage of TPI as a module
294 reaction for this family of products. Overall, module reactions enhance the compatibility
295 of a modular cell, leading to more efficient strategies and revealing potential metabolic flux
296 bottlenecks that are not always directly upstream of the target product.

297 **Three modular cells is the smallest set needed to cover all compatible products**

298 We next aimed to identify the smallest set of modular cells that include all compatible prod-
299 ucts in the library (Section 2.6.2). For the Pareto set of designs $\alpha = 5$, $\beta = 1$, we enumerated
300 a total of 12 minimal covers of size 3. These covers are spanned by combinations of 8 unique
301 designs (Figure S5). We selected the cover k that contains designs 82, 121, and 124, which
302 use few deletions and have similar genetic manipulations among them. All designs in this
303 cover have in common the deletion of ALCD2x and LDH_D, disabling production of ethanol
304 and lactate, the major reduced products of anaerobic growth in *E. coli*. Designs 121 and
305 124 have 57 compatible products in common, while design 121 is uniquely compatible with
306 ethanol, formate, and 2,3-dihydroxymethylbutanoate, and design 124 is uniquely compatible
307 with succinate (Figure 4 a). These two designs only differ in that design 121 uses FUM
308 deletion while design 124 uses MDH deletion (Figure 4 b). Different from designs 121 and
309 124, design 82 is the only design that features the deletion of FLDR2 and PPC and is
310 uniquely compatible with 24 modules, all for fatty acids synthesis. FLDR2 is coupled with
311 POR5 to form a pathway for the reduction of pyruvate into acetyl-CoA consuming *nadph*
312 (Figure 4 c), a key redox cofactor in fatty acid biosynthesis. PPC deletion is a metabolic
313 engineering strategy to increase *nadph* available that has been experimentally validated.³¹
314 Overall, these designs can be efficiently built due to their similarity, and are mainly composed
315 of strategies that have been demonstrated in isolation and cover large product families.

316 **3.3 Design of *E. coli* modular cells for conversion of hexoses and** 317 **pentoses**

318 **Non-glucose carbon sources require more genetic manipulations for high compat-**
319 **ibility designs** We designed modular cells to consume other relevant fermentable sugars
320 besides glucose also present in biomass feedstocks, including pentoses (i.e., xylose and arabi-
321 nose) and hexoses (i.e., galactose and mannose) (Figure 5 a). For this case study, everything
322 remained the same except for the substrate uptake reaction in the model which was changed
323 to reflect the sole carbon source in each case. We first scanned the distribution of design com-
324 patibilities resulting from various combinations of α and β for each carbon source (Figure S4
325 b-e). All cases plateaued at maximum compatibilities around 50%; however, galactose, ara-
326 binose and xylose required at least $\alpha = 10$, $\beta = 2$ to reach this level, while glucose and
327 mannose reached it with only $\alpha = 5$, $\beta = 1$. Hence, we selected $\alpha = 10$, $\beta = 2$ for further
328 analysis. Overall, this simulation reveals the possibility of highly compatible modular cells
329 for various hexose and pentose carbon sources, at the expense of an increased number of
330 genetic manipulations for some of the carbon sources.

331 **The effect of pentose uptake in redox metabolism leads to lower compatibility**
332 **than hexoses** For the set of designs in each carbon source, we examined the total com-
333 patible products, i.e., the number of unique products compatible in at least one design from
334 the Pareto front. This analysis revealed a group of 26 products (27% of the total 96 compat-
335 ible products and 16% of the original library size) that are only compatible in designs with
336 hexose carbon sources (Figure 5 b). The incompatibility of these 26 products is likely due
337 to the lower reduction potential and different uptake pathways of pentoses with respect to
338 hexoses (Figure 5 a). More specifically, analysis of the most deleted reactions in each carbon
339 source revealed several differences in deletions between pentoses and hexoses (Figure 5 c).
340 Notably, pentoses do not use TKT2 and MDH reaction deletions, while hexoses make highly
341 frequent use of them. TKT2 is a key component of incorporating pentoses into glycolysis,

342 and hence cannot be deleted by pentose consuming designs. MDH has been observed to be
343 up-regulated under anaerobic conditions when the sole carbon source is pyruvate, galactose,
344 or xylose with respect to glucose.³⁹ Hence, MDH could be an important source of *nadh* for
345 substrates with less reduction potential. Alternatively, MDH could also be important for
346 *nadph* generation as part of a pathway involving NADP-dependent malic enzyme (ME2)
347 that converts malate to pyruvate and generates one mol of *nadph*. Overall, pentose uptake
348 does not use the oxidative branch of the pentose phosphate pathway, the most important
349 source of *nadph* in *E. coli*,⁴⁰ hence limiting the products that can be growth-coupled to
350 these carbon sources. Further study of the reactions that limit pentose compatibility could
351 enable strategies to overcome it in certain cases (e.g., generation of alternative sources of
352 *nadph*^{41,42}).

353 **3.4 Compatibility towards modules unknown at the time of chas-** 354 **sis design**

355 **Highly compatible designs are better suited to be re-purposed towards unknown**
356 **products.** To rapidly explore the large space of potential production modules, existing
357 strains could be re-purposed for production of molecules not considered as part of the orig-
358 inal design. To examine this scenario, we randomly partitioned the product library into
359 two evenly sized groups, and independently used each partition as input for ModCell-HPC.
360 This was done in triplicates, each corresponding correspond to a different random product
361 partition. Hence, in each replicate there is a group of known products at the time of design
362 and a group of unknown products. For the designs produced by ModCell-HPC, we computed
363 their objective value and then compatibility towards unknown products, which we refer to as
364 *unknown compatibility* of a design, a useful metric to understand the potential to re-purpose
365 a given design. In contrast, *known compatibility* is the compatibility towards known prod-
366 ucts at the time of design, simply referred to as compatibility in previous cases study. The
367 analysis of unknown compatibility of a new production module with an existing modular

368 cell design is similar to the concept of degree of coupling that was previously introduced in
369 MODCELL based on a different computation framework.³ The total number of designs for
370 each product group and the unknown compatibility distributions noticeably changed across
371 replicates (Figure 6 a). This result reveals the important effect of known products in the
372 resulting designs, which could be further explored to identify “representative products” that
373 can capture the necessary metabolic phenotypes required for certain product families. Re-
374 markably, there was a high correlation between known and unknown compatibility of a given
375 design (Figure 6 b-d). Hence, highly compatible designs are better suited to be re-purposed
376 towards unknown products.

Deletion reactions that remove major fermentation byproducts and alter redox metabolism have the highest contribution towards unknown compatibility

To identify the specific genetic intervention strategies that contribute to the unknown compatibility of a design, we defined the unknown compatibility contribution of deletion reaction j (ucc_j) as follows:

$$ucc_j = \frac{\sum_{h \in \mathcal{H}_j} u_h}{|\mathcal{H}|} \quad (14)$$

377 where \mathcal{H}_j is the subset of designs from a ModCell-HPC solution (Pareto set \mathcal{H}) containing
378 deletion reaction j , and u_h is the unknown compatibility of design h . We computed ucc for
379 all 3 replicates and examined the top 10 sorted by mean value (Table 3). The main contribu-
380 tors towards unknown compatibility were removal of major fermentative byproducts (lac-
381 tate, ethanol, and acetate) followed by manipulation of redox pathways (THD2pp, FLDR2,
382 MDH) and metabolic branch points (TKT2, PPC). Indeed byproduct removal strategies are
383 the most common across the metabolic engineering literature.²⁸ Strain re-purposing could
384 be further explored with algorithms specialized for this task, e.g., by identifying module
385 reactions in the unknown modules or using the existing strain as a starting point to iden-
386 tify genetic manipulations instead of a wild-type strain. In our analysis, we have identified
387 that high modular cell compatibility and certain reaction deletions are positive indicators of

388 compatibility towards unknown products.

389 4 Conclusions

390 In this study, we developed ModCell-HPC, a computational method to design modular cells
391 compatible with hundredths of product synthesis modules. We applied ModCell-HPC to
392 design *E. coli* modular cells with a product library of 161 endogenous metabolites. This
393 resulted in many Pareto optimal designs for the production of these molecules, from which
394 we identified three modular cells that include all compatible products. The designs feature
395 strategies consistent with previous experimental studies aimed at optimizing production of
396 a single product, reinforcing our confidence in the value of our simulations. Remarkably,
397 the strategies not only include removal of major byproducts, but also modification of key
398 metabolic branch-points. The modular cells were designed for growth-coupled production,
399 which not only is expected to result in high product yields but also enables high-throughput
400 pathway engineering approaches. Specifically, the modular cell can be simultaneously trans-
401 formed with a module library to rapidly identify good candidates through adaptive laboratory
402 evolution.^{13,43} We also used ModCell-HPC to design modular cells that utilize different hex-
403 oses and pentoses carbon sources. This revealed the limitations of pentoses towards coupling
404 with certain products which might be addressed by redox cofactor engineering. Finally, we
405 identified that high compatibility and certain reaction deletion are important features to
406 re-purpose an existing modular cell towards new modules. Overall, ModCell-HPC is an ef-
407 fective tool towards more efficient and generalizable design of modular cells and platform
408 strains that have recently captured the interest of metabolic engineers.⁸

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416 Tables

Table 1: Island-MOEA parameters evaluated in ModCell-HPC.

Name	Description
Population size	Number of individuals per island.
Migration type	“ReplaceBottom”: After non-dominated sorting of the Pareto front ¹⁶ (survivor selection), top individuals are sent and bottom individuals replaced. “Random”: Random individuals are sent and replaced.
Migration interval	Number of generations between migration events.
Run time	Wall-clock time for which the MOEA runs. It determines the total number of generations.
Cores	Each island is a computing core at the hardware level.

Table 2: Top 20 reaction deletions for design parameters $\alpha = 5$, $\beta = 1$ with 162 designs. Counts indicate the percentage of designs where the deletion is used. All reaction and metabolite abbreviations used in this study correspond to BiGG identifiers (<http://bigg.ucsd.edu>).

ID	Name	Formula	Counts (%)
ALCD2x	Alcohol dehydrogenase (ethanol)	etoh_c + nad_c \leftrightarrow acald_c + h_c + nadh_c	57.4
TPI	Triose-phosphate isomerase	dhap_c \leftrightarrow g3p_c	45.1
ACALD	Acetaldehyde dehydrogenase (acetylating)	acald_c + coa_c + nad_c \leftrightarrow accoa_c + h_c + nadh_c	40.7
FLDR2	Flavodoxin reductase (NADPH)	2.0 flxso_c + nadph_c \rightarrow 2.0 flxr_c + h_c + nadp_c	24.1
PPC	Phosphoenolpyruvate carboxylase	co2_c + h2o_c + pep_c \rightarrow h_c + oaa_c + pi_c	21.6
TKT2	Transketolase	e4p_c + xu5p_D_c \leftrightarrow f6p_c + g3p_c	15.4
LDH_D	D-lactate dehydrogenase	lac_D_c + nad_c \leftrightarrow h_c + nadh_c + pyr_c	13
G3PD2	Glycerol-3-phosphate dehydrogenase (NADP)	glyc3p_c + nadp_c \leftrightarrow dhap_c + h_c + nadph_c	7.4
POR5	Pyruvate synthase	coa_c + 2.0 flxso_c + pyr_c \leftrightarrow accoa_c + co2_c + 2.0 flxr_c + h_c	7.4
ACKr	Acetate kinase	ac_c + atp_c \leftrightarrow actp_c + adp_c	6.8
THD2pp	NAD(P) transhydrogenase (periplasm)	2.0 h_p + nadh_c + nadp_c \rightarrow 2.0 h_c + nad_c + nadph_c	6.2
GLUDy	Glutamate dehydrogenase (NADP)	glu_L_c + h2o_c + nadp_c \leftrightarrow akg_c + h_c + nadph_c + nh4_c	5.6
ASPT	L-aspartase	asp_L_c \rightarrow fum_c + nh4_c	5.6
ASNS2	Asparagine synthetase	asp_L_c + atp_c + nh4_c \rightarrow amp_c + asn_L_c + h_c + ppi_c	4.9
CBMKr	Carbamate kinase	atp_c + co2_c + nh4_c \leftrightarrow adp_c + cbp_c + 2.0 h_c	4.3
RNDR4	Ribonucleoside-diphosphate reductase (UDP)	trdrd_c + udp_c \rightarrow dudp_c + h2o_c + trdox_c	3.7
RPE	Ribulose 5-phosphate 3-epimerase	ru5p_D_c \leftrightarrow xu5p_D_c	3.1
SERD_L	L-serine deaminase	ser_L_c \rightarrow nh4_c + pyr_c	3.1
LCARS	Lactaldehyde reductase (S-propane-1,2-diol forming)	h_c + lald_L_c + nadh_c \leftrightarrow 12ppd_S_c + nad_c	2.5
FUM	Fumarase	fum_c + h2o_c \leftrightarrow mal_L_c	2.5

Table 3: Top 10 reactions sorted by mean unknown compatibility contribution (*ucc*) among replicates (i.e., R.1, R.2, and R.3).

ID	Name	<i>ucc</i>			
		R. 1	R. 2	R. 3	Mean
LDH_D	D-lactate dehydrogenase	13.2	10.5	11.9	11.9
ALCD2x	Alcohol dehydrogenase (ethanol)	11.5	10.5	11.8	11.3
PTAr	Phosphotransacetylase	4.0	4.8	6.5	5.1
ACALD	Acetaldehyde dehydrogenase (acetylating)	4.5	2.8	2.9	3.4
THD2pp	NAD(P) transhydrogenase (periplasm)	4.7	2.4	2.2	3.1
ACKr	Acetate kinase	3.8	2.2	1.7	2.6
FLDR2	Flavodoxin reductase (NADPH)	2.0	2.2	2.9	2.4
TKT2	Transketolase	2.6	2.0	2.5	2.4
PPC	Phosphoenolpyruvate carboxylase	2.3	2.2	2.5	2.3
MDH	Malate dehydrogenase	2.7	1.1	2.3	2.0

417 Figures

Figure 1: Parallelization schemes for multi-objective evolutionary algorithms. (a) Master-slave approach used in the original ModCell2 implementation. (b) Island parallelization following ring topology implemented in ModCell-HPC. (c) Key steps in the evolutionary algorithm.

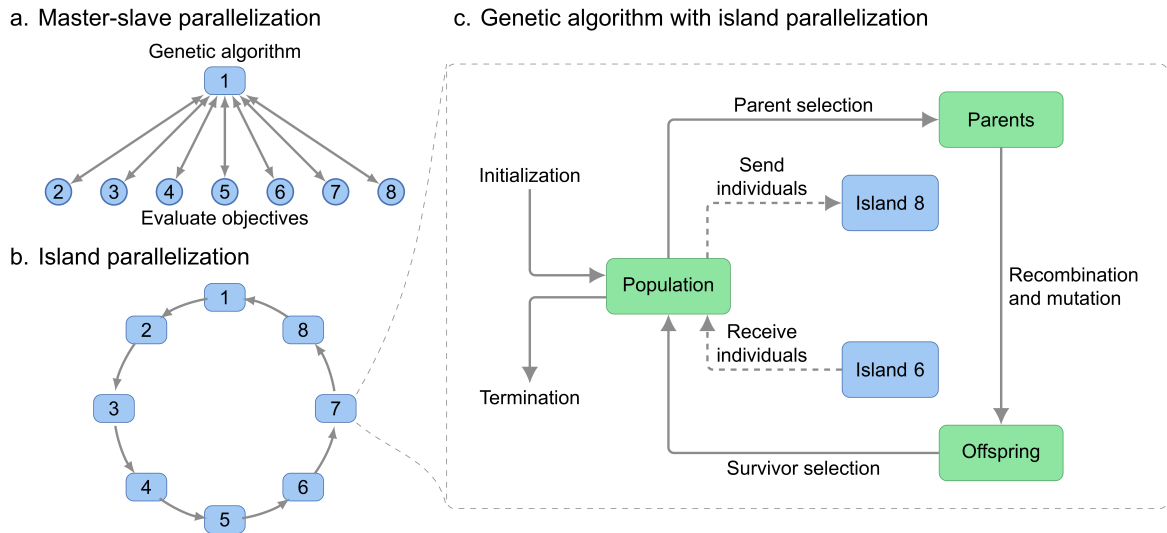


Figure 2: ModCell-HPC benchmark with 161 products. (a) and (e) Coverage is the fraction of Pareto optimal designs captured by a Pareto front approximation (Section 2.7). (b) and (f) Compatible modules indicates the products that appear in at least one design with a design objective above the compatibility threshold, while minimal cover size is the smallest number of designs needed to capture all compatible products (Section 2.6). (c) and (g) Total and unique number of solutions in the Pareto front approximations. (d) and (h) Total number of generations.

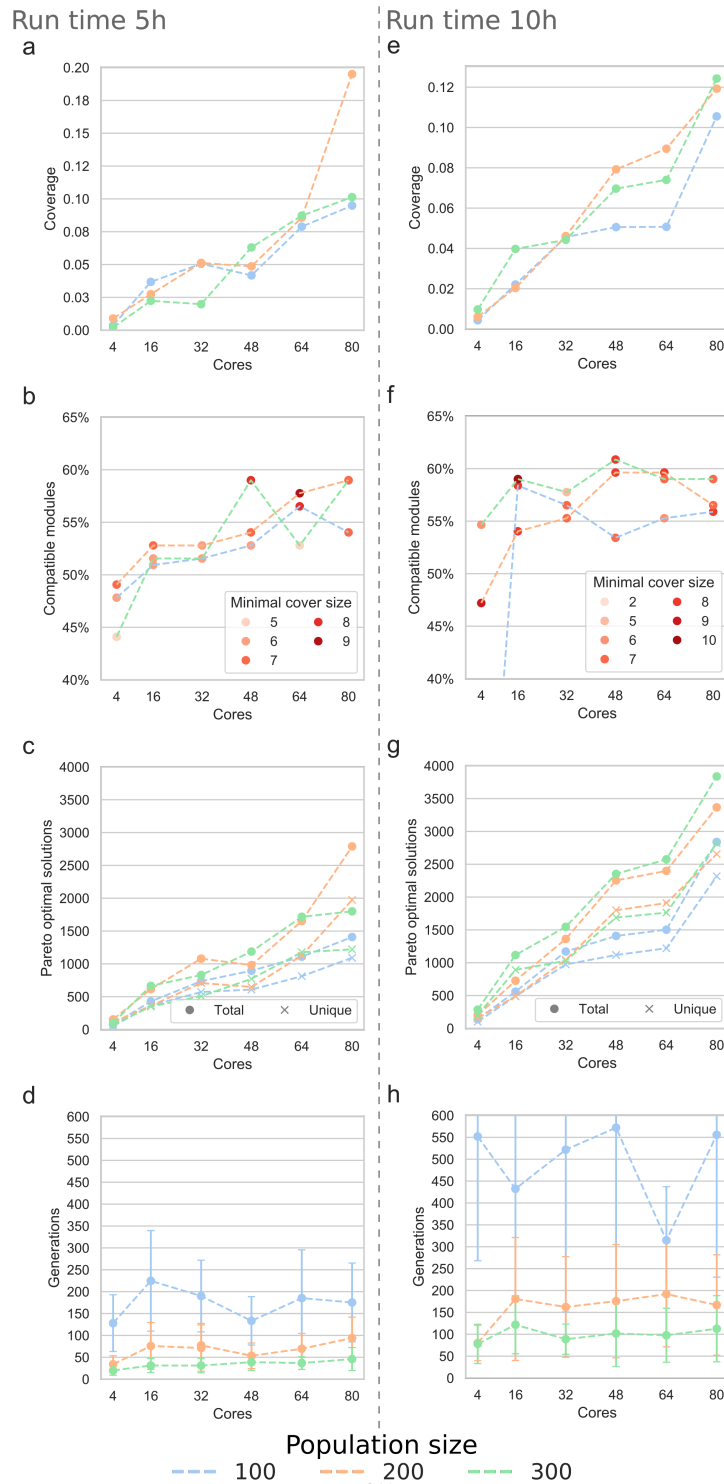


Figure 3: Module reaction usage for design parameters $\alpha = 5$, $\beta = 1$. Only designs compatible with the product are considered in the module usage frequency.

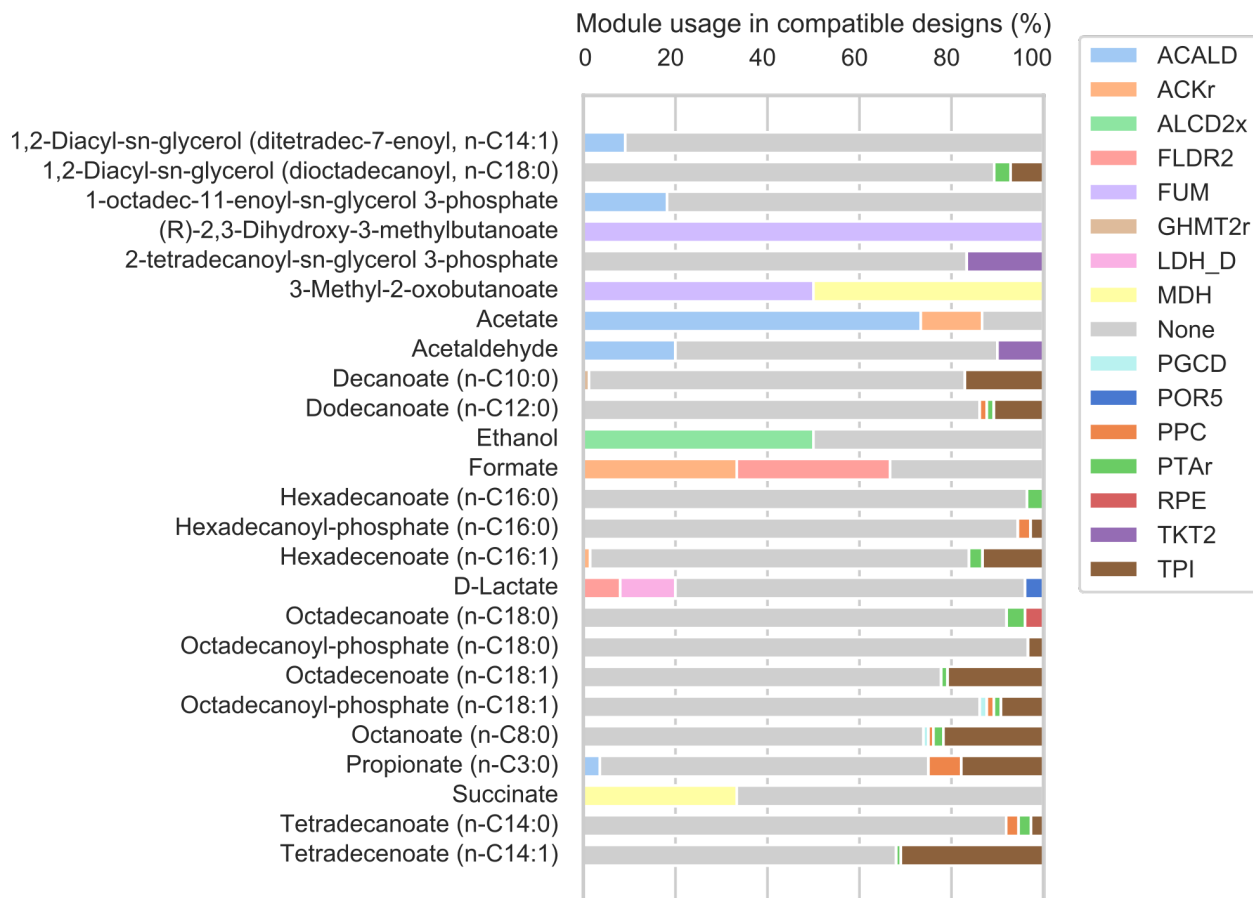
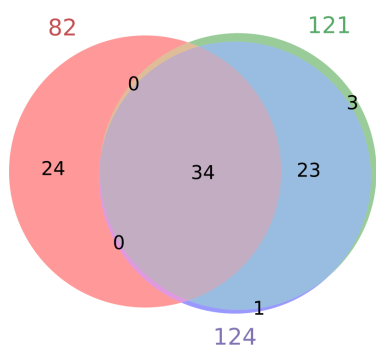
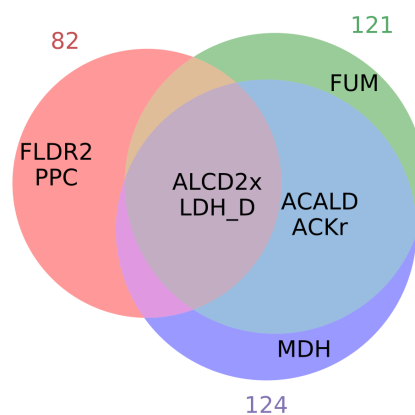


Figure 4: Comparison of the designs in the selected minimal cover. (a) Venn diagram of products compatible with each design. The products uniquely compatible with specific designs are (see <http://bigg.ucsd.edu> for abbreviation descriptions): Design 121: *etoh*, *for*, *23dhmb*; Design 124: *succ*; Design 82: *pg140*, *2hdecg3p*, *2odec11eg3p*, *1agpg180*, *pe140*, *pg161*, *pg141*, *2hdec9eg3p*, *pgp161*, *2agpg180*, *1ddecg3p*, *pg120*, *pgp141*, *pgp140*, *pe141*, *ps140*, *apg120*, *ps120*, *pgp120*, *pe120*, *lipidX*, *2tdecg3p*, *2odecg3p*, *ps141*. (b) Venn diagram of reaction deletions that constitute each design. (c) Metabolic map with reaction deletions colored in red.

a. Compatible modules



b. Reaction deletions



c. Metabolic location of reaction deletions

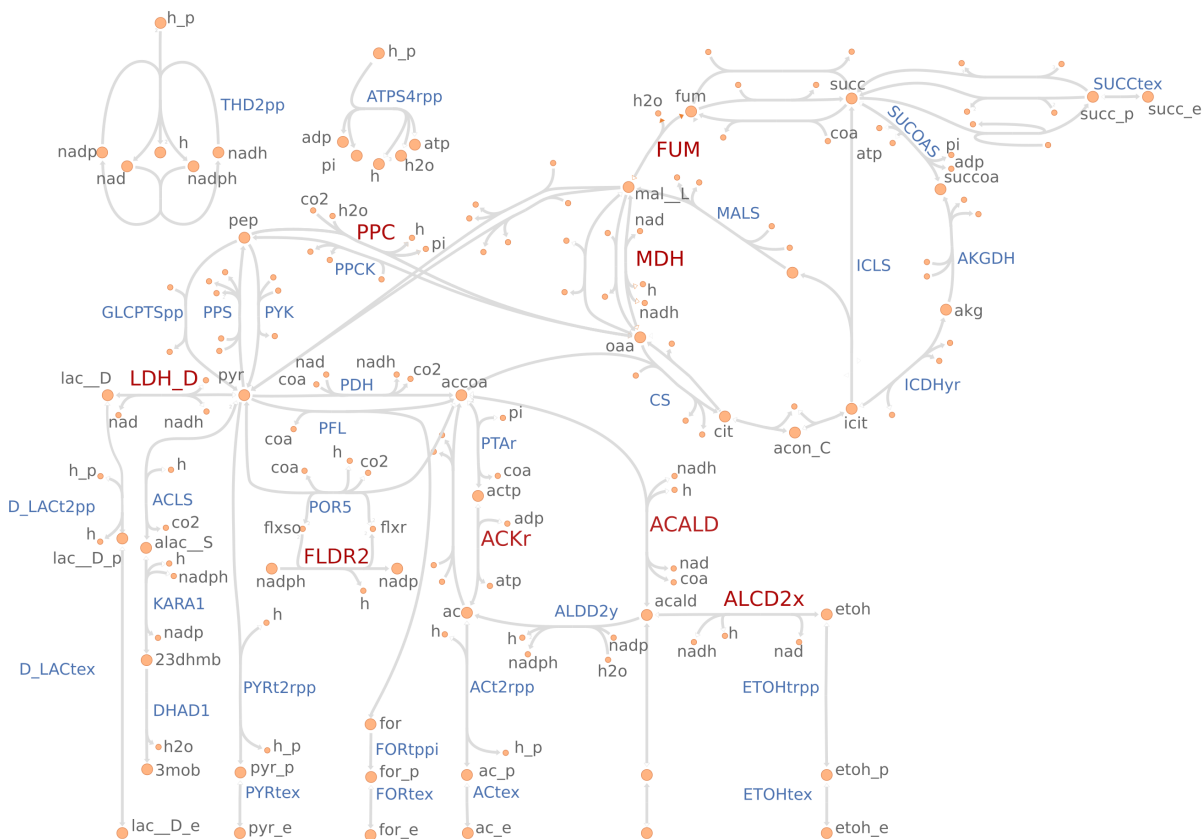


Figure 5: Design of modular cells for different carbon sources with design parameters $\alpha = 10$, $\beta = 2$. (a) Sugar uptake, pentose phosphate, Entner-Doudoroff, and upper glycolysis pathways. (b) Venn diagram of total products compatible with designs using pentoses and hexoses. The 26 products uniquely compatible with hexoses are: *1agpg180*, *2tdecg3p*, *2agpg181*, *3c3hmp*, *3mob*, *2hdecg3p*, *pe141*, *ps120*, *1agpg160*, *2agpg160*, *23dhmb*, *ps141*, *1agpe180*, *2agpg180*, *apg120*, *2agpe180*, *pe120*, *2odec11eg3p*, *4mop*, *lipidX*, *3c2hmp*, *2ippm*, *2hdec9eg3p*, *1agpg181*, *dha*, *2odecg3p*. (c) Top 20 reaction deletions according to deletion frequencies average across carbon sources. The counts for each carbon source correspond to the percentage of designs containing that reaction deletion.

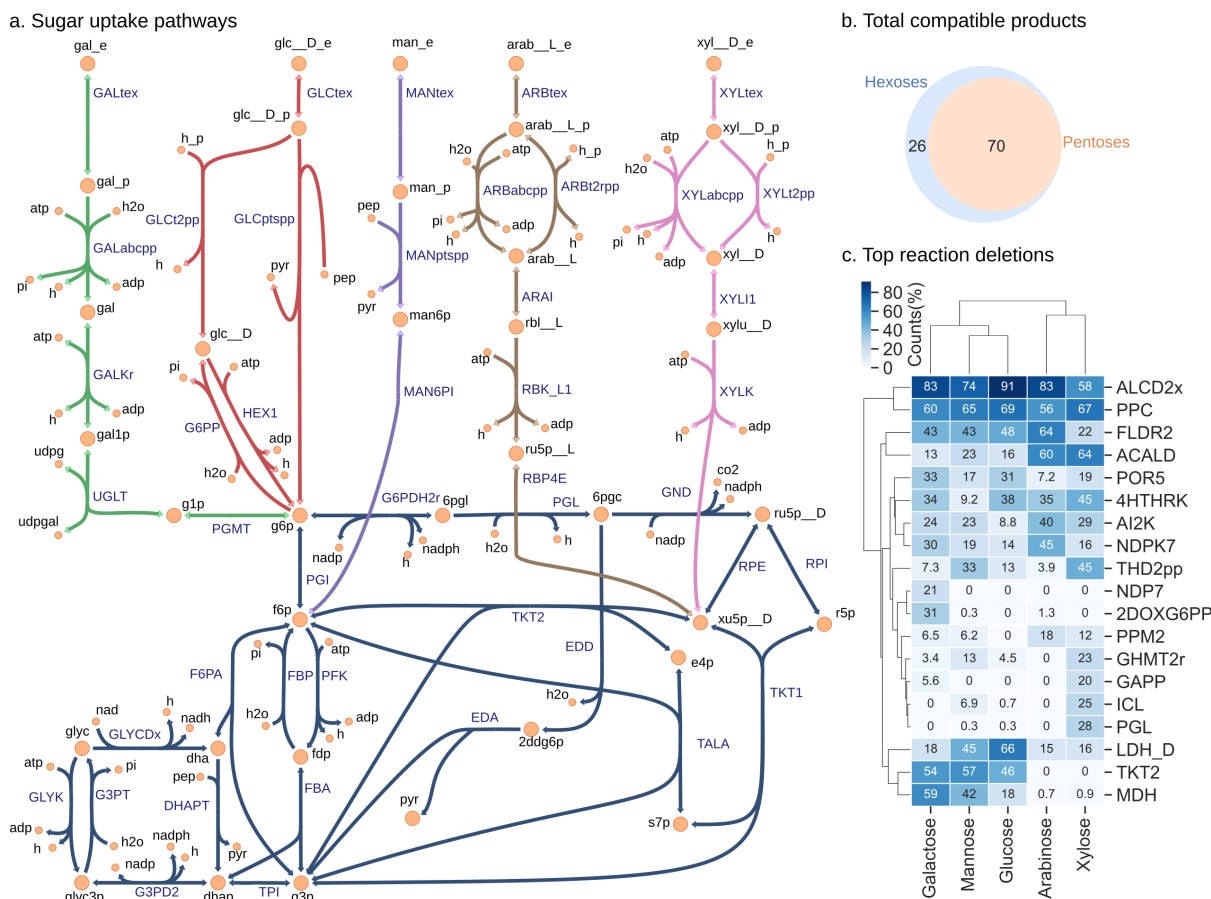
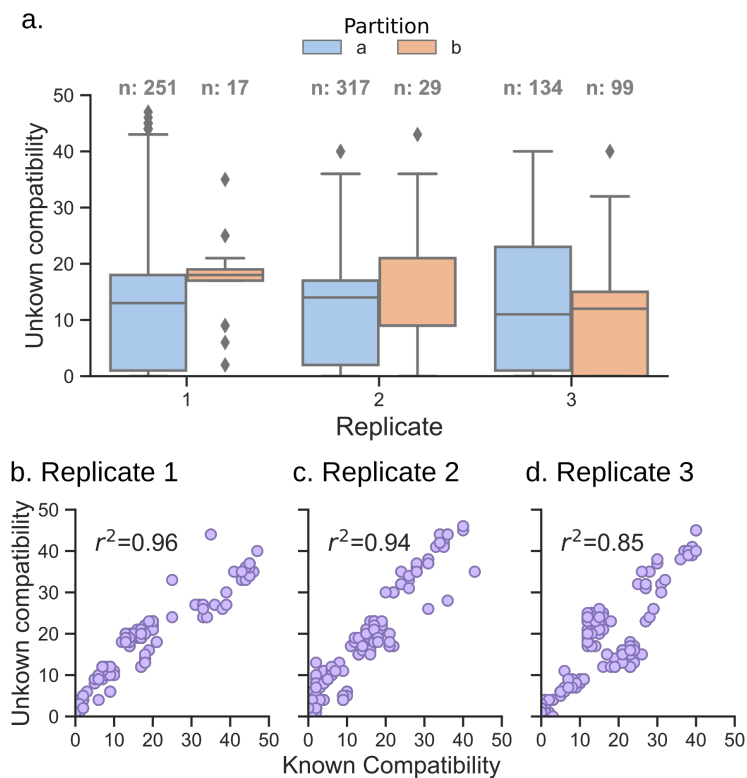


Figure 6: Compatibility towards unknown products in 3 random even partitions of the product library. (a) Distribution of unknown compatibility, n corresponds to the number of designs in each case. (b-d) Comparison between unknown and known compatibilities of each design for each replicate, where r^2 is the Pearson correlation coefficient.



418 **Supplementary Materials**

- 419 1. Supplementary Material 1 (SM1): Supplementary figures.
- 420 2. Supplementary Material 2 (SM2): Designs for selected parameters $\alpha = 5$, $\beta = 1$.

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