6   Motion extrapolation in the flash-lag effect depends on perceived, rather than physical speed
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20   **Acknowledgements**
21   This study was supported by an Australian Research Council (ARC) Discovery Projects Grant
22   awarded to H.H. (DP180102268).
23   Commercial relationships: none.
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29   Abstract

In the flash-lag effect (FLE), a flash in spatiotemporal alignment with a moving object is

misperceived as lagging behind the moving object. One proposed explanation for this illusion is

based on predictive motion extrapolation of trajectories. In this interpretation, the diverging effects

of velocity on the perceived position of the moving object suggest that FLE might be based on the

neural representation of perceived, rather than physical velocity. By contrast, alternative

explanations based on differential latency or temporal averaging would predict that the FLE does

not rely on such a representation of perceived velocity. Here we examined whether the FLE is

sensitive to illusory changes in perceived speed that result in changes to perceived velocity, while

physical speed is constant. The perceived speed of the moving object was manipulated using

revolving wedge stimuli with variable pattern textures (Experiment 1) and luminance contrast

(Experiment 2). The motion extrapolation interpretation would predict that the changes in the FLE

magnitude should correspond to the changes in the perceived speed of the moving object. In the

current study, two experiments demonstrated that the perceived speed and FLE magnitude

increased in dynamic relative to static pattern conditions, and that the same effect was found in

low contrast compared to high contrast conditions. These results showed that manipulations of

texture and contrast that are known to alter judgments of perceived speed also modulate perceived

position. We interpret this as a consequence of motion extrapolation mechanisms and discuss

possible explanations for why we observed no cross-effect correlation.

Keywords: flash-lag effect, perceived speed, perceived position, motion extrapolation, dynamic

pattern, luminance contrast

1. Introduction

In the process of visual perception, delays are incurred as information encoded by the retina is transmitted to the visual cortex (Schmolesky et al., 1998). Neural processing subsequently takes time, so for a time-varying stimulus such as a moving object, its position information would be outdated when it is available in visual cortical areas (De Valois & De Valois, 1991). Because the object would continue moving in the physical world, a lag between its perceived and veridical position would be inevitable at any given time (Maunsell & Gibson, 1992). Intuitively, the impact of such delays should be significant when localizing moving objects, but despite this, we seem to be able to accurately pursue and interact with even fast-moving objects (Smeets & Brenner, 1995b). One proposed explanation is that neural delays are partly compensated perceptually by a process of motion extrapolation (Nijhawan, 1994, 2002; motor compensation is also observed in Kerzel & Gegenfutner (2003) and outlined in Nijhawan & Wu (2009)). The motion extrapolation hypothesis proposes that the brain continuously extrapolates the trajectory of a moving object to predict where it is now, as closely as possible to its veridical positions (Cavanagh, 1997; Nijhawan & Wu, 2009).

A strong case for visual motion extrapolation has been made on the basis of motion-induced position shifts, many of which indicate a strong coupling between motion and position signals. For example, the Fröhlich effect describes an illusory forward shift in the starting point of the motion trajectory (Fröhlich, 1924), and the representational momentum phenomenon involves a forward displacement in the stopping point of a moving object (Freyd & Finke, 1984; Hubbard, 1995, 2005, 2018). Similarly, when an object moves into a blindspot, the final position of the occluded object is extrapolated in the direction of motion beyond its vanishing point (Maus & Nijhawan, 2008); or if a moving object contains a moving texture, the perceived position of the object appears shifted toward the direction of its internal motion (Arnold, Thompson, & Johnston, 2007; De Valois & De Valois, 1991; Roach, McGraw, & Johnston, 2011). Of these illusions, this paper is concerned with the related flash-lag effect (FLE). The FLE has received extensive attention since Nijhawan (1994) reported that a flashed object is misperceived as lagging behind a physically aligned, continuously moving object. Explanations based on motion extrapolation mechanisms propose that the perceived position of the moving object is extrapolated, evoking an apparent spatial offset

even though the two objects are always physically aligned (Nijhawan, 1994, 2002). Although

different possible causes have been proposed for the FLE (see Hubbard, 2014; Nijhawan, 2002;

Maus, Khurana, & Nijhawan, 2010 for reviews), convergent evidence from neural, behavioral, and

computational studies demonstrate how extrapolation could be implemented in the visual system

– and that this could compensate for neural delays and potentially explain the above illusions

(Hogendoorn, 2020). Were these mechanisms to underlie the FLE, then such a shift should be

expected, indeed, for the moving object but not the flash (Nijhawan, 2002; Maus & Nijhawan,

2006).

According to the motion extrapolation interpretation, the predictive mechanism that results in the

FLE and related illusions derives from a process of constantly estimating and updating motion

and/or position signals (Kwon, Tadin, & Knill, 2015). Arguably, early extrapolation signals have

been shown to carry an estimate of an object's velocity, in order to gauge the distance for the object

to (have) travel(ed) (Nijhawan, 2008; Nijhawan & Wu, 2009; Rosenbaum, 1975; Crick & Koch,

1995; Pollen, 2003). Importantly in both representational momentum (Freyd & Finke, 1985;

Hubbard & Bharucha, 1988) and the FLE (Nijhawan, 1994; Brenner & Smeets, 2000; Krekelberg

& Lappe, 1999, 2000; Murakami, 2001; Nijhawan, Watanabe, Khurana, & Shimojo, 2004; López-

Moliner & Linares, 2006), the perceived offset increases linearly with the velocity of the moving

object. However, not all FLE studies are consistent. Kanai, Sheth, and Shimojo (2004) observed

that the FLE was unaffected by velocity when the FLE magnitude was measured in spatial units

and, in fact, decreased with increased velocity in units of time. Cantor & Schor (2007) showed that

the FLE can decrease for increasing velocities larger than one degree of visual angle (dva) per

second, while Wojtach, Sung, Truong, and Purves (2008) tested a larger range of 3 dva/s–50 dva/s

and found that the FLE varied as a logarithmic function of velocity, so the linear effects consistent

with previous observations were only shown at the lower velocity ranges. This inconsistent

dependence on velocity led us to question whether these effects on the FLE might be due to

changes in perceived, rather than physical velocity (Finke, Freyd, & Shyi, 1986; Makin, Stewart,

& Poliakoff, 2009). Although physical velocity and perceived velocity are naturally closely

correlated, perceived velocity is modulated by physical properties of the moving object such as

stimulus contrast (Stone & Thompson, 1992), transiency/duration (Treue, Snowden, & Andersen,

1993), and spatial (Smith & Edgar, 1990) as well as temporal frequency (Shen, Shimodaira &

Ohashi, 2003). For this reason, we investigate the nature of the velocity representation that
contributes to the neural computation that generates the perceived flash-lag.

In the present study, we test the hypothesis that the magnitude of the FLE depends on perceived
velocity, resulting from changes in perceived speed, even when the physical velocity of the moving
object is unchanged. Unique among explanations of the FLE, under the motion extrapolation
model, a neural representation of velocity is necessary for an explicit computation that allows us
to correctly perceive objects in their current and future positions despite neural delays. Other
models of the FLE which attribute the FLE to temporal processes (based on differential processing
latency and attentional shifts; Baldo & Klein, 1995; Purushothaman, Patel, Bedell, & Ögmen,
1998; Whitney & Murakami, 1998; Ögmen, Patel, Bedell, & Camuz, 2004, or based on temporal
averaging of positions, sampling, and postdiction; Krekelberg & Lappe, 1999, 2000; Whitney,
Murakami, & Cavanagh, 2000; Brenner & Smeets, 2000; Eagleman & Sejnowski, 2000, 2007)
would also expect the FLE to increase with faster physical speed – but only as a temporal offset
evident as a spatial error (Krekelberg and Lappe, 1999, 2000; Kanai et al., 2004). These models
therefore do not require an explicit representation of velocity, and as such, would not be expected
to depend on perceived speed when physical speed remains constant.
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131   **2. Experiment 1**
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One method of manipulating perceived speed is by dynamically modulating the texture of a
moving object (Treue et al., 1993). When Carlson, Schrater, and He (2006) presented a smaller
square with a static noise texture superimposed on top of a larger square with dynamic noise and
the two objects moved together, the area of static noise was perceived to consistently lag behind
the area of dynamic noise – causing an illusory percept that they called the Floating Square illusion.
Despite having the same physical velocities, observers perceived the dynamic noise object to move
faster and separate from the static noise object. The difference in the perceived speed of the two
patterns was sufficient to generate large perceptual errors when their relative positions were in fact
identical. The results from this experiment are consistent with the idea that motion extrapolation
is influenced by perceived speed. We apply this manipulation to an FLE paradigm, where our
motion stimulus contains either a static or a dynamic pattern.

Participants carried out a two-alternative forced-choice (2AFC) spatial localization task where they

were asked whether a revolving stimulus or a flashed target appeared to lead in the direction of

motion, at the moment of the flash. Hereafter we refer to this as the flash-lag task (Experiment

1A). In a control speed-discrimination task (Experiment 1B), participants were asked to judge if

the patterns differed in perceived speeds. We hypothesized that if the FLEs were sensitive to a

change in perceived speed, then both the perceived speed and perceived offset would be greater

for the dynamic stimulus relative to the static stimulus. Conversely, if the FLE were not dependent

on perceived speed, then we would expect no difference in the FLE magnitude as an addition of a

dynamic pattern.

2.1 Participants

A total of 99 observers participated in one or both parts of Experiment 1: 30 observers participated

in Experiment 1A, and 20 observers participated in Experiment 1B. To investigate possible

correlations between the FLE measure obtained in Experiment 1A and the perceived speed

measure obtained in Experiment 1B, a further 49 observers participated in both tasks. Two

observers were excluded from Experiment 1A because their results significantly violated normality

(Shapiro-Wilk: $p < 0.001$; Kolmogorov-Smirnov: $p < 0.001$). One observer was excluded from

both tasks for incorrectly performing the tasks. Together, this yielded a total of 76 observers in

Experiment 1A (23 males, mean age 24.2 years and SD 6 years) and 68 observers in Experiment

1B (23 males, mean age 24.2 years and SD 5.6 years), with 48 of these observers having completed

both tasks.

All observers were naïve to the purpose of the experiment, were right-handed, and reported normal

or corrected-to-normal vision. Observers gave informed consent and were reimbursed 10 AUD per

hour for their participation in the experiment. The study was conducted in accordance with the

Declaration of Helsinki and approved by the University of Melbourne Human Research Ethics

Committee of the Melbourne School of Psychological Sciences (Ethics ID 1954146.2).

2.2 Stimuli

All stimuli were presented on a 24.5-inch ASUS ROG PG258 monitor (ASUS, Taipei, Taiwan)

with a resolution of 1920×1080 running at 200 Hz, controlled by an HP EliteDesk 800 G3 TWR

running MATLAB R2017b (Mathworks, Natick, NA) with PsychToolbox 3.04.14 extensions

(Kleiner et al., 2007). Participants sat in a light-attenuated room and viewed the stimuli from a

headrest at 60 cm from the screen.

The primary stimulus consisted of a revolving wedge segment and a static annulus around a white

fixation point, displayed on a uniform 50% gray background (Figure 1A). Its inner and outer edges

were 4.05° and 6.75° of visual angle away from the fixation point and subtended 45° of polar angle

along the radial axis. The wedge moved in a randomly interweaved clockwise or counter-

clockwise direction (second-order motion) at a fixed speed of 200° of polar angle/s.

Stimuli contained one of two texture types. Filtered noise was created by applying a low-pass filter

on white noise at 0.5cycles/deg, and pixelated noise was created using an array of 5x5 pixel blocks

with random luminance. The dynamic pattern was added by replacing the textures with a new

random set of pixels, of no correlation with the previous set, at every frame. This configuration

resulted in a flickering appearance of the texture. The background of the annulus always contained

the static pattern, otherwise the wedge would be indistinguishable from the background if both

textures were dynamic.

Figure 1. Schematic depiction of the stimuli and flash-lag sequence. (A) For filtered noise (top)

and pixelated noise (bottom) texture conditions, the primary stimulus consisted of a revolving

wedge segment superimposed on a static annulus of the same texture (see also <u>videos</u> of the stimuli

used in this experiment). (B) A single flash-lag trial began with the primary stimulus (illustrated

using a pixelated noise texture and outlined in red). The target stimulus flashed near the midpoint

of the sequence, and after a delay, observers were asked to respond using a keypress. A complete

trial lasted up to 7s, with the presentation sequence lasting 2s.

In Experiment 1A, observers compared the position of the primary stimulus to a flashed target

stimulus. The target had the same static texture as the primary stimulus and was briefly presented

along the inner circumference of the annulus (Figure 1B). Its inner and outer edges corresponded

to 2.43° and 3.78° of visual angle from fixation and subtended 45° of polar angle along the radial

axis.

In Experiment 1B, observers compared the speed of the primary stimulus to a previously presented

comparison stimulus. The primary stimulus was identical to that of Experiment 1A, and the

comparison stimulus was a solid black wedge of the same eccentricity as the primary stimulus,

without the background of the annulus. The speed of the primary stimulus was constant at 200°/s,

but the speed of the comparison stimulus varied across trials using a staircase procedure (see *2.3*

Procedure below). Both stimuli always revolved in the same direction, which was randomly

chosen at the start of each trial.

2.3 Procedure

2.3.1 Experiment 1A: Flash-lag task

On each trial, the primary stimulus was presented from a random starting position of the annulus

and revolved for one of three possible durations (850, 1000, or 1150ms chosen at random). The

target stimulus was presented for 15ms next to the primary stimulus, after which the primary

stimulus continued its trajectory for the remaining 1150, 1000, or 850ms (cumulative presentation

duration of 2s). After the sequence ended, observers were instructed to report whether the

revolving primary stimulus or the target stimulus was spatially ahead of the other when the flash

appeared (2AFC). Keypress responses were recorded in the next 5s – 'i' as in inner (target stimulus) or 'o' as in outer (primary stimulus) – and prompted the next trial.

The physical alignment between the primary stimulus and the target stimulus was driven by a one-up, one-down staircase procedure, and trials were randomly drawn from two interleaved staircases. One staircase started at a large difference of +20° of polar angle (moving ahead of flash). A –20° starting point was omitted in this procedure as a reversing, flash-lead presentation would be redundant for the purpose of our hypothesized flash-lag illusion. Instead, the second staircase started at a smaller difference of 0° (physically aligned) during the central presentation frame. Depending on the response, the angle difference was adjusted by ±2° in the following trial drawn from that staircase. Observers completed 120 trials from each staircase, and the final 60 points of each staircase were averaged to estimate the point of subjective equality (PSE): the displacement at which the moving and flashed wedges were perceived as aligned.

Trials were blocked into 4 conditions. Each condition consisted of 120 trials (each lasting up to 7s), for a total of 480 trials over 4 blocks. The conditions were determined based on a combination of *pattern type* (static or dynamic) and *texture type* (filtered noise or pixelated noise). The order of condition was randomized for observers who completed only Experiment 1A and counterbalanced if they completed both Experiment 1A and 1B. All observers completed 12 trials as practice before each experimental block, followed by a self-paced break. This resulted in a total testing duration of approximately 30 minutes.

2.3.2 Experiment 1B: Speed-discrimination task

In each trial, the comparison stimulus started revolving from a random position against a 50% gray background, for either 1500, 1750, or 2000ms randomly chosen (Figure 2). The comparison stimulus then disappeared, after which the primary stimulus was presented from a random position of the annulus and revolved for 1500, 1750, or 2000ms also randomly chosen. The presentation duration was varied so that observers could not reliably base their responses on the difference between the distance traveled by each wedge. After the sequence ended, observers were instructed to report whether the comparison stimulus or the primary stimulus appeared faster (2AFC).

Keypress responses were recorded in the next 5s – '1' for first (comparison stimulus) or '2' for

second (primary stimulus) – and prompted the next trial.

Figure 2. Schematic illustration of Experiment 1B. In a single speed-discrimination trial, the

comparison stimulus and the primary stimulus (illustrated using a pixelated noise texture and

outlined in blue) were presented sequentially, and after a delay, observers were asked to respond

using a keypress. A complete trial lasted up to 9s, with the presentation sequence lasting up to 4s.

While the speed of the primary stimulus was fixed, the speed of the comparison stimulus was

determined using a similar staircase procedure using the ratio of these two stimulus speeds. Trials

were drawn from one of two interleaved staircases. Because velocity is represented logarithmically

in perception (Priebe & Lisberger, 2004; Nover, Anderson, & DeAngelis, 2005), the steps were

adjusted by means of multiplying and dividing, rather than adding and subtracting. The first

staircase was initialized at 1.075^7, and the second started at 1.075^{-7}, with a step size set to 1.075

for both. The staircase value of a given trial was proportionate to the relative speed of the

comparison stimulus relative to the primary stimulus. For example, 1.075^7 (~1.66) indicated that

the comparison stimulus revolved at 166% of the speed of the primary stimulus (166% of 200°/s).

Depending on the response, the speed of the comparison stimulus was adjusted by 1.075 for the

next trial drawn from that staircase. Observers completed 72 trials from each staircase, and the last

36 points of each staircase were averaged to estimate the PSE: the speed at which the comparison

and primary wedges were perceived to match.

Trials were blocked into the same 4 conditions of Experiment 1A: *pattern type* (static or dynamic)

and *texture type* (filtered noise or pixelated noise). All observers completed a total of 4 blocks.

Observers who completed only Experiment 1B completed 72 trials per block (for a total of 288

trials), and observers who completed both Experiment 1A and 1B completed 144 trials per block

(for a total of 576 trials). The total testing duration was 25 and 50 minutes, respectively.

2.4 Results

We tested for differences in the magnitude of the FLE and perceived speed in each condition using

a two-way repeated measures ANOVA with factors of *pattern type* (static or dynamic) and *texture*

type (filtered noise or pixelated noise). Post hoc paired-samples *t*-tests (two-tailed) with Bonferroni

corrections estimated these differences.

2.4.1 Experiment 1A: Effect of dynamic pattern on perceived flash-lag

A repeated measures ANOVA revealed a significant main effect of pattern type ($F_{1,75} = 5.14$, $p =$

0.026), with greater FLE magnitudes observed for dynamic than for static stimuli (Figure 3A).

There was no significant main effect of texture type ($F_{1,75} = 1.61$, $p = 0.209$) and no interaction

effect between the two factors ($F_{1,75} = 0.81$, $p = 0.37$). The mean PSE was significantly larger for

dynamic compared to static stimuli for the filtered noise texture ($t_{75} = 2.49$, $p = 0.015$), but the

difference did not reach significance for the pixelated noise texture ($t_{75} = 1.03$, $p = 0.309$).

Figure 3. Results of Experiment 1. For illustrative purposes, the bars contain corresponding

textures in this figure. (A) Mean FLE magnitudes of static and dynamic wedges across the texture

conditions in Experiment 1A. (B) Mean perceived speeds of static and dynamic wedges across the

texture conditions in Experiment 1B. Perceived speed was calculated as a ratio of the comparison

speed relative to the primary speed (higher bars mean that objects in that condition were perceived

as faster). Baseline speed is indicated by a horizontal dashed line at y = 1. Mean perceived speeds

were significantly different from zero and between pattern conditions. Error bars represent

standard errors across observers. Asterisks above the bars indicate a statistically significant main

effect of pattern type. * denotes $p < 0.05$. *** denotes $p < 0.001$.

2.4.2 Experiment 1B: Effect of dynamic pattern on perceived speed

A repeated measures ANOVA showed a significant main effect of pattern type on perceived speed

($F_{1,67} = 35.82$, $p < 0.001$), with higher perceived speeds reported for dynamic than for static stimuli

(Figure 3B). This effect was significant for both filtered noise ($t_{67} = 4.08$, $p < 0.001$) and pixelated

noise ($t_{67} = 5.33$, $p < 0.001$) textures. In addition, there was a significant main effect of texture

type ($F_{1,67} = 11.5$, $p = 0.001$) but no significant interaction effect ($F_{1,67} = 2.518$, $p = 0.117$).

2.4.3 Cross-effect correlation

In order to further evaluate the possible relationship between the two measures, we investigated

whether a dynamic pattern affected perceived speed and perceived position (flash-lag) in the same

way. We were interested in the relation between one effect and the other, and if this was consistent

between observers in a cross-effect correlation analysis. Among 48 observers who completed both

tasks, we hypothesized that observers for whom the dynamic textures greatly increased perceived

speed would be expected to report larger changes in the illusion, and conversely, observers with

minimal (or negative) changes in perceived speed would be expected to show corresponding small

or negative effects in the illusion. However, Pearson's correlation (two-tailed) did not reveal a

significant correlation between the two tasks in either filtered noise (r = 0.15, p = 0.3) or pixelated

noise (r = 0.07, p = 0.64) conditions (Figure 4).

Figure 4. [dynamic-static] FLE difference plotted as a function of [dynamic-static] speed difference for (A) filtered noise and (B) pixelated noise textures. Legend for texture type is shown in the top right corner of each panel.

3. Experiment 2

Overall, Experiment 1 demonstrates that the dynamic modulation of a moving object's texture, which is known to influence perceived speed, also influences the perceived position of the moving object – systemically in the same direction in the FLE, as predicted by the motion extrapolation model. To provide confidence that this effect is due to changes in perceived speed rather than unknown low-level factors, we carried out a parallel set of experiments to investigate whether a different, independent manipulation of perceived speed similarly affects the FLE.

The well-known 'Thompson effect' describes how speed is underestimated at low contrasts (Thompson, 1982; Snowden, Stimpson, & Ruddle, 1998; Blakemore & Snowden, 1999; Anstis, 2003). As a natural example, this has been used to explain why drivers frequently drive too fast under foggy conditions, compensating for their incorrect estimates of how fast (or slow) they and other cars are moving (Snowden et al., 1998; Anstis, 2003; but see also Owens, Wood, & Carberry, 2010; Pretto, Bresciani, Rainer, & Bülthoff, 2012). Theoretically, this effect is consistent with the findings of Berry, Brivanlou, Jordan, and Meister (1999), which showed that anticipatory neural responses for the leading edges of a moving object varied based on the contrast of the object. It also resembles the Hess effect (Hess, 1904), a similar illusion to the Floating Squares illusion and the FLE, in which a brighter object is perceived to lead a dimmer object when the two are actually

aligned and have the same physical velocities. However, the effects of contrast on perceived speed depend on properties such as object luminance or physical velocity, and a handful of studies previously demonstrated that the effect can reverse under certain circumstances. For example, perceived speed can be overestimated at higher velocities (>8 dva/s; Thompson, Brooks, & Hammett, 2006; Hawken, Gegenfurtner, & Tang, 1994; Pretto et al., 2012) and low luminance levels (Vaziri-Pashkam & Cavanagh, 2008, 2011).

The effects of contrast have also been specifically investigated in the context of motion extrapolation. In the FLE, Kanai et al. (2004) found increases in the FLE magnitude with decreases in contrast of moving objects with the background. Kanai et al. suggested that the FLE was modulated by positional uncertainty, as visibility is affected when the contrast of a target and background is reduced. Maus and Nijhawan (2006, 2009) also reported that the forward displacement of a moving object increases if the contrast of the target gradually decreased, while Hubbard and Ruppel (2014) reported that representational momentum decreases with low or decreasing contrast of the target and background. Finally, Vaziri-Pashkam and Cavanagh's (2011) FLE paradigm presented a moving patch of random dots against the background containing static random dots. While they found that the perceived speed of moving objects increases at low luminance, caused by motion blurring for faster speeds (Vaziri-Pashkam & Cavanagh, 2008), there were no additional effects on the FLE magnitude due to these changes in perceived speed.

We reexamined the effects of contrast in Experiment 2. In line with Experiment 1, the primary (moving) stimulus revolved at a speed of 200°/s, but presented at either high (100%) or low (10%) contrast. Based on the divergent effects of contrast on perceived speed in the previous literature as briefly discussed above, we had no a priori directional hypothesis about the effect of contrast on perceived speed. Instead, we hypothesized that any effect of contrast on perceived speed would be mirrored in an effect on the FLE magnitude in the same direction. In other words, mean FLE magnitudes would increase in high contrast relative to low contrast conditions if perceived speed increased with high contrast, or in the opposite direction, it would increase for low contrast compared to high contrast conditions if perceived speed increased with low contrast. Conversely, if the FLE were not driven by perceived speed, then we would expect an effect of contrast on perceived speed, but no effect on the FLE magnitude.

3.1 Participants

386 Seven observers (3 males, mean age 25.3 years, SD 3.4 years) participated in the experiment. All
387 were experienced observers and completed both Experiment 2A (Flash-lag) and 2B (Speed-
388 discrimination). All inclusion criteria were identical to Experiment 1.

3.2 Stimuli

Stimuli were similar to those used in Experiment 1 with the following exceptions (see also videos
of the stimuli used in this experiment). The primary stimulus revolved around the fixation point,
identical to Experiment 1, with the exception that the wedge was presented against the uniform
gray background without the annulus that was presented in Experiment 1. In doing so, we aimed
to control for a potential confounding effect as otherwise observers would be required to detect
the contrast of the wedge on top of the background of the annulus against the gray background
while tracking the wedge's motion (Blakemore & Snowden, 2000).

Observers viewed the stimuli from a distance of 50cm. The inner and outer edges of the primary
stimulus were 4.75° and 7.92° of visual angle away from the fixation point and subtended 3.17°
of polar angle along the radial axis. The inner and outer edges of the target stimulus in Experiment
2A were 3.46° and 4.44° from fixation, subtending 1.58° of polar angle along the radial axis.
Stimuli textures were filtered noise or pixelated noise and always presented as a static pattern. The
main experimental manipulation of Experiment 2 was that on each trial, the primary stimulus was
presented at high (100%) or low (10%) contrast relative to the gray background.

3.3 Procedure

Due to the COVID-19 pandemic, observers participated from their own homes. All observers
completed the experiment using identical-speed ASUS ROG PG258Q monitors (1920 x 1080
resolution, 200Hz) in a dimly lit room. A chinrest was not used for this experiment, but observers
were instructed to sit approximately 50cm from the screen and make sure the fixation point was at
eye level.

The experimental conditions were determined by a combination of *contrast level* (high or low) and

texture type (filtered noise or pixelated noise). All observers completed a total of 4 blocks: 120

trials per block (for a total of 480 trials) in Experiment 2A and 144 trials per block (for a total of

576 trials) in Experiment 2B. The total testing duration was approximately 80 minutes.

3.4 Results

As in Experiment 1, we probed the FLE magnitudes for each condition in Experiment 2A and

perceived speed in Experiment 2B. We submitted all data to a two-way repeated measures

ANOVA with factors of *contrast level* (high or low) and *texture type* (filtered noise or pixelated

noise) and *t*-tests. All relevant assumptions were met.

3.4.1 Experiment 2A: Effect of contrast on perceived flash-lag

A repeated measures ANOVA revealed a significant main effect of contrast level ($F_{1,6} = 7.32$, $p =$

0.035), with greater FLE magnitudes observed for low contrast than for high contrast stimuli

(Figure 5A). There was a main effect of texture type ($F_{1,6} = 28.87$, $p = 0.002$), with greater FLE

magnitudes observed for the pixelated noise texture than for the filtered noise texture. There was

no significant interaction effect between the two factors ($F_{1,6} = 0.47$, $p = 0.52$). The mean PSE was

significantly larger for low contrast compared to high contrast stimuli for the filtered noise texture

($t_6 = 3.47$, $p = 0.013$), but the difference did not reach significance for the pixelated noise texture

($t_6 = 2.12$, $p = 0.078$). For individual data, the FLE consistently increased in the low contrast

condition compared to the high contrast condition for all but two observers (P6 for filtered noise

and P3 for pixelated noise; Figure 5B).

Figure 5. Results of Experiment 2A. For illustrative purposes, the bars contain corresponding
textures and contrasts in this figure. (A) Mean FLE magnitudes of high and low contrast wedges
across texture conditions, pooled over all seven observers. (B) Individual observers. Error bars
represent standard errors across observers. The asterisk above the bars indicates a statistically
significant main effect of contrast level at $p < 0.05$.

3.4.2 Experiment 2B: Effect of contrast on perceived speed

A repeated measures ANOVA revealed a significant main effect of contrast level on perceived
speed ($F_{1,6} = 52.85$, $p < 0.001$), with low contrast perceived to move faster than high contrast
stimuli with an identical physical velocity (Figure 6A). There was no significant main effect of
texture type ($F_{1,6} = 0.086$, $p = 0.779$) or an interaction effect ($F_{1,6} = 4.68$, $p = 0.074$). The mean
PSE was significantly larger for low contrast compared to high contrast stimuli in both filtered
noise ($t_6 = 5.72$, $p = 0.001$) and pixelated noise ($t_6 = 7.31$, $p < 0.001$) texture conditions. The effect
was highly consistent across individual observers (Figure 6B).

Figure 6. Results of Experiment 2B. For illustrative purposes, the bars contain corresponding textures and contrasts in this figure. (A) Mean perceived speeds of high and low contrast wedges across texture conditions, pooled over all seven observers. (B) Individual observers. Perceived speed was calculated as a ratio of the comparison speed relative to the primary speed, and the baseline speed is indicated as y = 1. Error bars represent standard errors across observers. Asterisks above the bars indicate a statistically significant main effect of contrast level. *** denotes *p* < 0.001.

4. Discussion

The flash-lag effect (FLE) is a classic illusion that has been argued to result from motion extrapolation mechanisms that might be implemented in the visual system to contribute to overcoming its time delays. Although many alternative explanations for the FLE have been presented, the motion extrapolation account is unique in that it posits a neural computation that requires a representation of velocity. We hypothesized that under this motion extrapolation interpretation, experimental manipulations that affect perceived velocity might similarly influence the magnitude of the FLE. Here, we investigated this hypothesis by examining how illusions of perceived speed altered the perceived flash-lag in two experiments. We show that dynamically modulating a texture causes an illusory percept of increased speed as well as increased FLE

magnitude compared to a static texture. Similarly, when objects were presented at low contrast as

compared to high contrast, both perceived speed and FLE magnitude increased. These findings are

consistent with the motion extrapolation account of the FLE.

Experiment 1 shows robust differences between dynamic and static patterns for both perceived

speed and magnitude of the FLE. These differences were qualitatively similar across different

textures. Overall, these results closely reproduce the previously reported effects on the perceived

speed of gratings, Gabor patches, and in the Floating Square illusion (De Valois & De Valois,

1991; Treue et al., 1993; Shen et al., 2003; Carlson et al., 2006), and are also consistent with the

effects of speed on motion extrapolation (Freyd & Finke, 1985; Hubbard & Bharucha, 1988;

Nijhawan, 1994; Brenner & Smeets, 2000; Krekelberg & Lappe, 1999, 2000; Murakami, 2001;

Nijhawan et al., 2004; López-Moliner & Linares, 2006).

Experiment 2 likewise shows subjective increases in both perceived speed and the FLE magnitude

in the low contrast relative to high contrast conditions. These results diverge from the findings of

some previous studies that investigated the effects of contrast on motion extrapolation (e.g., Maus

& Nijhawan, 2006, 2009; Hubbard & Ruppel, 2014), in that our wedge stimuli were perceived as

faster at low contrast than high contrast. The discrepancy with the Thompson effect is likely due

to methodological differences because our primary stimulus revolved at approximately 28.15

dva/s, which is significantly faster than in the literature we outlined here (approximately 3-17

dva/s; Stone & Thompson, 1992; Blakemore & Snowden, 1999; Thompson et al., 2006; Hubbard

& Ruppel, 2014; Maus & Nijhawan, 2006, 2009). Consistent with this interpretation, Vaziri-

Pashkam and Cavanagh (2011) found that only their highest velocity of 27.36 dva/s was

overestimated.

If a neural representation of perceived velocity is used to inform the extrapolation process that

underlies the FLE, then we would expect to see a causal relationship between the effects of

dynamic pattern on perceived speed and the effects on the FLE. However, we did not observe a

correlation between the behavioral responses, similar to Vaziri-Pashkam and Cavanagh (2011),

with a portion of observers showing a decrease in the FLE magnitude despite clear increases in

perceived speed. One possibility is that the experiments in this study illustrate that different

processes are involved in making judgments of speed versus relative position. For example,
de'Sperati and Thornton (2019) showed that varying the contrast of a moving object affected
extrapolation judgments but not interceptive decisions when observers were required to make
saccadic eye movements to avoid colliding with multiple moving targets. Based on these findings,
de' Sperati and Thornton suggested these tasks involve intrinsically different processes. An
important question arising from our findings is therefore whether the representations of velocity
that contribute to explicit reports of motion (i.e. *how fast* an object is perceived to move) differ
from the representations used for implicit processing of position (i.e. *where* an object is; cf.
Brenner & Smeets, 1994; Smeets & Brenner, 1995a) – and involve different cortical areas – or,
alternatively, if a shared velocity representation might cause greater differences in perceived speed
than in the FLE. The latter explanation could reconcile findings of Vaziri-Pashkam and Cavanagh
(2011), as at low luminance the effects of perceived speed did not significantly affect the
magnitude of the FLE any more than the effects of physical speed.

Furthermore, there was a large variability for individual observers in Experiments 1A and 1B. This
could be partly attributed to measurement noise, so we can suspect that the effect of perceived
speed (although robust within individuals) might explain only a small proportion of the variance
in the illusion across individuals in our study. Other factors might also influence responses in the
FLE (thereby contributing to error variance). Kanai et al. (2004) reported FLE biases in the same
direction, but they explain their effects in terms of uncertainty (see also Purushothaman et al.,
1998; Fu, Shen, & Dan, 2001; Maus & Nijhawan, 2006, 2009; Vreven & Verghese, 2005).
According to this interpretation, increases in the FLE magnitude are caused by increases in
positional uncertainty, due to decreased contrast rather than increased perceived speed. This
reasoning is also compatible with Experiment 1 if the dynamic pattern would increase uncertainty;
presumably, dynamic or low contrast objects would be expected to elicit weaker or noisier position
signals for the visual system to work with. In turn, the perceived position might depend more
strongly on predictions originating from extrapolation processes, and be less strongly influenced
by (uncertain) sensory information. This would, in principle, be expected to cause increases in the
FLE magnitude for dynamic texture c.q. low contrast conditions as we observe here. However, the
hypothesized effects of uncertainty have been shown to have little impact on judgments of speed
(Stocker & Simoncelli, 2006), and observers can accurately report the extrapolated positions of

moving objects despite decreases in visibility (Graf, Warren, & Maloney, 2005), making this

interpretation unlikely.

Instead, we might consider if there is an indirect or additional influence of uncertainty. Uncertainty

could predict an increase in error variance, and this would be expected to work against any

systemic biases, rather than cause one. This would be compatible with the absence of a cross-effect

correlation. Another possible influence on our FLE effects is not in terms of uncertainty, but in the

amount of attention allocated to the moving object. We cannot definitely rule out this possibility,

as we did not explicitly control or measure attention in our different conditions. Conceivably, an

object containing a dynamic texture might require more attention to localize than an object

containing a static texture. If this were true, then we might expect a greater FLE, based on studies

showing that the FLE increases when attention is divided (e.g., across concurrent tasks, across

multiple stimuli, or for increased speeds; Sarich, Chappell, & Burgess, 2007; Scocchia, Actis-

Grosso, de'Sperati, Stucchi, & Baud-Bovy, 2009). This explanation also applies if low contrast

requires more attention than high contrast. These alternative interpretations need to be tested by

future experiments.

Overall, the pattern of results is consistent with the notion that the magnitude of the FLE depends

on a neural representation of velocity that is sensitive to (some of) the same experimental

manipulations that also affect over reports of perceived speed. This finding is consistent with an

explanation of the FLE in terms of visual motion extrapolation. It also corroborates a growing

body of evidence supporting the existence of neural mechanisms involved in extrapolation in both

animal models (e.g., Berry et al.,1999; Jancke, Erlhagen, Schöner, & Dinse, 2004; Sunberg, Fallah,

& Reynolds, 2006; Schwartz, Taylor, Fisher, Harris, & Berry, 2007; Palmer, Marre, Berry, &

Bialek, 2015; Subramaniyan et al., 2018; Benvenuti et al., 2020) and human neuroimaging (e.g.,

Ekman, Kok, & de Lange, 2017; Schneider, Marquardt, Sengupta, De Martino, & Goebel, 2019;

Hogendoorn & Burkitt, 2018; Blom, Feuerriegel, Johnson, Bode, & Hogendoorn, 2020), and is

consistent with several decades investigating motion extrapolation in perception (Hubbard, 2005,

2014, 2018; Nijhawan, 2002, 2008; Maus et al., 2010; Hogendoorn, 2020).

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