Modulation of pulsatile GnRH dynamics across the ovarian cycle: the role of excitability within the arcuate kisspeptin network.

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Abstract

Pulsatile GnRH release is essential for normal reproductive function. Kisspeptin secreting neurons found in the arcuate nucleus, known as KNDy neurons for co-expressing neurokinin B, and dynorphin, drive pulsatile GnRH release. Furthermore, gonadal steroids regulate GnRH pulsatile dynamics across the ovarian cycle by altering KNDy neurons' signalling properties. However, the precise mechanism of regulation remains mostly unknown. Here we investigate these mechanisms using a combination of mathematical and in-vivo approaches. We find that optogenetic stimulation of KNDy neurons stimulates pulsatile GnRH/LH secretion in estrous mice but inhibits it in diestrous mice. Our mathematical modelling suggests that this differential effect is due to well-orchestrated changes in neuropeptide signalling and the excitability of the KNDy population controlled via glutamate signalling. Guided by model predictions, we show that blocking glutamate signalling in the arcuate nucleus in diestrous animals inhibits LH pulses, and that optic stimulation of the KNDy population mitigates this inhibition. In estrous mice, disruption of glutamate signalling inhibits pulses generated via sustained low-frequency optic stimulation of the KNDy population, supporting the idea that the level of network excitability is critical for pulse generation. Our results reconcile previous puzzling findings regarding the estradiol-dependent effect that several neuromodulators have on the GnRH pulse

generator dynamics. Therefore, we anticipate our model to be a cornerstone for a more quantitative understanding of the pathways via which gonadal steroids regulate GnRH secretion dynamics. Finally, our results could inform useful repurposing of drugs targeting the glutamate system in reproductive therapy.

Introduction

The dynamics of gonadotropin-releasing hormone (GnRH) secretion is critical for reproductive health. In female animals, GnRH secretion is tightly regulated across the ovarian cycle. Pulsatile secretion dominates most of the cycle, with frequency and amplitude modulated by the ovarian steroid feedback. Positive feedback from increasing estradiol levels triggers a preovulatory surge of GnRH/LH secretion (Christian and Moenter, 2010). Furthermore, there is ample evidence that ARC kisspeptin neurons are prime mediators of the ovarian steroid feedback on the pulsatile dynamics of GnRH/LH secretion (McQuillan et al., 2019), although the mechanisms remain unclear.

In-vitro studies have shown that gonadal steroids have a dramatic effect on the electrophysiology of ARC kisspeptin neurons. For instance, spontaneous firing activity of ARC kisspeptin neurons from castrated mice appears elevated compared to intact animals (Ruka et al., 2016) and estradiol replacement attenuates ARC kisspeptin neuron activity in gonadectomised animals (Ruka et al., 2016; Wang et al., 2018). Also gonadal steroids modulate the amplitude of LH pulses generated by intermittent optogenetic activation of ARC kisspeptin neurons (Han et al., 2015). More recently, fiber photometry data from female mice show that the ARC kisspeptin neuronal population (KNDy network) pulses at a relatively constant frequency throughout the ovarian cycle apart from the estrous phase where the frequency is dramatically reduced (McQuillan et al., 2019). This silencing effect is thought to be a direct consequence of the increasing progesterone levels in the circulation after ovulation has occurred (McQuillan et al., 2019). Furthermore, studies in the sheep indicate the silencing effect of progesterone is mediated through increased dynorphin signalling (Goodman et al., 2011; Moore et al., 2018), however this is less clear in mice where ovarian steroids have a negative effect on Dyn mRNA levels (Navarro et al., 2009).

Perplexing is also the differential effect of various neuromodulators on LH secretion depending on the gonadal steroid background. For instance, N-methyl-D-aspartate (NMDA) robustly inhibits LH pulses in the ovariectomized monkey whereas in the presence of estradiol this effect is reversed, and NMDA stimulates LH secretion (Reyes et al., 1990; Reyes et al., 1991).

Similar reversal of action on LH dynamics depending on the underlying ovarian steroid milieu
has been also documented for other neurotransmitter and neuropeptides in other species (Kalra
and Kalra, 1983; Brann and Mahesh, 1992; Arias et al., 1993; Bonavera et al., 1994; Scorticati
et al., 2004) and highlights the complex mechanisms underlying the modulation the GnRH
pulse generator by gonadal steroids.

Here, using mathematical modelling along with optogenetic stimulation of ARC kisspeptin
neurons we embark to understand how the dynamics of the pulse generator are modulated
across the ovarian cycle. Our mathematical model suggests that the level of excitability within
the ARC kisspeptin network—the propensity of kisspeptin neurons to singal and activate each
other—is one of the key parameters modulated in different stages of the cycles by gonadal
steroids. Previous studies have shown that ARC kisspeptin neurons synapse on each other (Yip
et al., 2015; Qiu et al., 2016) and because these neurons are mainly glutamatergic (Cravo et al.,
2011; Qiu et al., 2011; Kelly et al., 2013; Wang et al., 2018), we hypothesise that population
excitability should be enabled primarily via glutamatergic transmission. We test our predictions
in-vivo and show that glutamatergic transmission is an important factor for the pulsatile
behaviour of the KNDy network.

Materials and methods

Animals

Adult Kiss-Cre heterozygous transgenic female mice aged between 8-14 weeks, 25-30 g, were
used for experiments (Yeo et al., 2016). Breeding pairs were obtained from the Department of
Physiology, Development and Neuroscience, University of Cambridge, UK and mated in house
at King's College London. Genotyping was performed using a multiplex PCR protocol for
detection of heterozygosity for the Kiss-Cre or wild-type allele as previously described (Lass
et al., 2020). Only mice with normal estrous cycles were used. Daily vaginal smears were
performed for the detection of the estrous and diestrous stages of the ovarian cycle. Mice were
singularly housed and provided with food (standard maintenance diet; Special Dietary
Services, Wittam, UK) and water ad libitum while being kept under a 12:12 h light/dark cycle
(lights on 0700 h) at $23 \pm 2°C$. All animal procedures performed were approved by the Animal
Welfare and Ethical Review Body Committee at King's College London and conducted in
accordance with the UK Home Office Regulations.

Surgical procedures

Stereotaxic injection of AAV9-EF1-dflox-hChR2-(H134R)-mCherry-WPRE-hGH (4.35 x 1013 GC/ml; Penn Vector Core; University of Pennsylvania, PA, USA) for targeted expression of channelrhodopsin (ChR2) in ARC kisspeptin neurons was done under aseptic conditions. The mice were anaesthetised using ketamine (Vetalar, 100 mg/kg, i.p.; Pfizer, New York City, NY, USA) and xylazine (Rompun, 10 mg/kg, i.p.; Bayer, Leverkusen, Germany). Kiss-Cre female mice (n = 12) or wilt-type (n = 3) were secured in a Kopf Instruments motorized stereotaxic frame (Kopf Instruments, Tujunga, CA, USA) and surgical procedures on the brain were performed using a Robot Stereotaxy system (Neurostar, Tubingen, Germany). Stereotaxic injection coordinates used to target the ARC were obtained from the mouse brain atlas of Paxinos and Franklin (Paxinos and Franklin, 2004) (0.25 mm lateral, 1.94 mm posterior to bregma and at a depth of 5.8 mm). A skin incision was made and a small hole was drilled in the skull above the location of the ARC. A 2-μl Hamilton micro-syringe (Esslab, Essex, UK) was attached to the robot stereotaxy and used to inject 0.3μl of the AAV-construct into the ARC, unilaterally, at a rate of 100 nl/min. After the injection, the needle was left in position for 5 min and then slowly lifted over 1 min. The same coordinates as the injection site were then used to insert a fiber-optic cannula (200 μm, 0.39 NA, 1.25 mm ceramic ferrule; Thorlabs, LTD, Ely, UK), however a depth of 5.78 mm was reached to ensure the fiber-optic cannula was situated immediately above the injection site. Additionally, an intracerebroventricular (ICV) fluid guide cannulae (26 gauge; Plastics One) targeting the lateral ventricle (coordinates: 1.1 mm lateral, 1.0 mm posterior to bregma and at a depth of 3.0 mm) was chronically implanted. Dental cement (Superbond C&B kit Prestige Dental Products, Bradford UK) was used to fix the cannulae in place and the skin incision was sutured. A one week recovery period was given post-surgery. After this period, the mice were handled daily to acclimatize them to the tail-tip blood sampling procedure (Steyn et al., 2013). Mice were left for 4 weeks to achieve effective opsin expression before experimentation.

Validation of AAV injection site and fibre optic and ICV cannula position

Once experiments were completed, mice were given a lethal dose of ketamine and transcardially perfused for 5 min with heparinized saline, followed by 10 min of ice-cold 4% paraformaldehyde (PFA) in phosphate buffer, pH 7.4, for 15 min using a pump (Minipuls; Gilson). Brain were collected immediately and post fixed at 4°C in 15% sucrose in 4% PFA and left to sink. They were then transferred to 30% sucrose in PBS until they sank. The brains were then snap-frozen on dry ice and stored at -80°C. Using a cryostat, every third coronal brain section (30 μm) was collected between -1.34 mm to -2.70 mm from bregma and sections

129 were mounted on microscope slides, left to air-dry and cover slipped with ProLong Antifade

130 mounting medium (Molecular Probes, Inc, OR, USA). Verification and evaluation of the

131 injection site was performed using an Axioskop 2 Plus microscope equipped with axiovision

132 4.7 (Zeiss). One of 12 Kiss-Cre mice failed to show mCherry fluorescence in the ARC and was

133 excluded from the analysis.

Experimental design and blood sampling for LH measurement.

For measurement of LH pulsatility during optogenetic stimulation, the tip of the mouse's tail

was removed with a sterile scalpel for tail-tip blood sampling (Czieselsky et al., 2016). The

chronically implanted fiber-optic cannula was attached to a multimode fiber-optic rotary joint

patch cables (Thorlabs) via a ceramic mating sleeve. This allows for freedom of movement and

blue light delivery (473 nm wavelength) using a Grass SD9B stimulator controlled DPSS laser

(Laserglow Technologies) during optogenetic stimulation.

The experimental protocol involved an hour long acclimatisation period, followed by 2.5 h of

blood sampling, where 5 µl of blood was collected every 5 min. For estrous and diestrous mice,

optic stimulation was initiated after 1 h of control blood sampling and was sustained for 1.5 h

h. Optic stimulation was delivered as 5ms pulses of light at 5Hz with the laser intensity

measured at the tip of the fiber-optic patch cable set to 5mW. Additionally, in separate

experiments, diestrous mice were optically stimulated at 5 or 15 Hz for 2.5 h, that is entire

blood sampling period. Control mice (in estrus or diestrus) received no optic stimulation in, to

control for the effects of viral injections and surgical procedures. Wild-type mice

(estrus/disetrus???) received 5 Hz optic stimulation to verify that our optic stimulation protocol

had no undesirable effects on LH secretion.

Neuropharmacological manipulation of glutamatergic signalling was performed using a

combination of NMDA (AP5, Tocris, Abingdon, UK) and AMPA (CNQX, Alpha Aesar,

Heysham, UK) receptor antagonist treatment with or without simultaneous optogenetic

stimulation. The animals were prepared for optogenetic experimentation as described above

with additional preparation of the ICV injection cannula. Immediately after connection of the

fiber-optic cannula, the ICV injection cannula with extension tubing, preloaded with drug

solution (AP5 and CNQX dissolved in artificial CSF) or artificial CSF alone as control, was

inserted into the guide cannula. The extension tubing, reaching outside of the cage, was

connected to a 10 µl Hamilton syringe mounted in an automated pump (Harvard Apparatus) to

allow for remote micro-infusion without disturbing the animals during experimentation. After

a 55 min control blood sampling period, as described above, and 5 min before the onset of optic

stimulation, a bolus ICV injection of drug solution (12 nmol AP5 and 5 nmol CNQX in 2.3 μl)

was given over 5 min, followed by a continuous infusion (20 nmol AP5 and 10 nmol CNQX

in 5.6 μl) for the remaining 90 min of experimentation. Artificial CSF controls, with or without

optic stimulation, received the same ICV fluid regime. When no optic stimulation was applied

the same ICV administration and blood sampling regimen described was applied. Stimulation

and non-stimulation protocols were implemented in random order for Kiss-Cre mice.

The blood samples were snap-frozen on dry ice and stored at -80°C until processed. In-house

LH enzyme-linked immunosorbent assay (LH ELISA) similar to that described by Steyn et al.

was used for processing of the mouse blood samples (Steyn et al., 2013). The mouse LH

standard (AFP- 5306A; NIDDK-NHPP) was purchased from Harbor-UCLA along with the

primary antibody (polyclonal antibody, rabbit LH antiserum, AFP240580Rb; NIDDK-NHPP).

The secondary antibody (donkey anti-rabbit IgG polyclonal antibody [horseradish peroxidase];

NA934) was from VWR International. Validation of the LH ELISA was done in accordance

with the procedure described in Steyn et al. (Steyn et al., 2013) derived from protocols defined

by the International Union of Pure and Applied Chemistry. Serially diluted mLH standard

replicates were used to determine the linear detection range. Nonlinear regression analysis was

performed using serially diluted mLH standards of known concentration to create a standard

curve for interpolate the LH concentration in whole blood samples, as described in Voliotis et

al. (Voliotis et al., 2019). The intraassay and interassay variations were 4.6% and 10.2%,

respectively.

LH pulse detection and statistical analysis.

Dynpeak algorithm was used for the detection of LH pulses (Vidal et al., 2012). The differential

effect of optogenetic stimulation on LH pulsatility in estrus and diestrus was determined by

looking at the frequency of LH pulses. For mice in estrus and for the neuropharmacological

experiments, the mean ± SEM of LH pulses per hour were compared between the 60 min pre-

stimulation/drug delivery control period and subsequent 90 min stimulation period. For mice

in diestrus, the mean ± SEM of LH pulses per hour were compared between controls, 5 Hz and

15 Hz treatment groups, as optic stimulation was applied from the beginning of blood sample

period. No optic stimulation was applied to control animals, however the same time points

were compared. The frequency of LH pulses in the 90-min optic stimulation/drug delivery

period was also compared between treatment groups. One-way ANOVA followed by Dunnett's

test, $p < 0.05$, was used to determine statistical significance.

Mathematical model of the KNDy network.

We used a modified version of a mathematical model of the KNDy network previously presented in (Voliotis et al., 2019). Briefly, the model describes the ARC kisspeptin population in terms of three variables: $\bar{D}$, the average concentration of Dyn secreted by the population; $\bar{N}$, the average concentration of NKB secreted by the population; and $\bar{v}$, the average firing activity of the population, measured in spikes/min. The variables obey the following set of coupled ordinary differential equations (ODEs):

$$\frac{d\bar{D}}{dt} = f_D(\bar{v}) - d_D\bar{D}; \tag{1}$$

$$\frac{d\bar{N}}{dt} = f_N(\bar{v}, \bar{D}) - d_N\bar{N}; \tag{2}$$

$$\frac{d\bar{v}}{dt} = f_v(\bar{v}, \bar{N}) - d_v\bar{v}. \tag{3}$$

Parameters d_D, d_N and d_v control the characteristic timescale of each variable. The secretion rate of Dyn and NKB are given by:

$$f_D(\bar{v}) = k_{D,0} \frac{\bar{v}^{n_1}}{\bar{v}^{n_1} + K_{v,1}^{n_1}};$$

$$f_N(\bar{v}, \bar{D}) = k_N \frac{\bar{v}^{n_2}}{\bar{v}^{n_2} + K_{v,2}^{n_2}} \frac{K_D^{n_3}}{\bar{D}^{n_3} + K_D^{n_3}}.$$

In the equations above neuronal activity ($\bar{v}$) stimulates secretion of both neuropeptides, and Dyn represses NKB secretion. The maximum secretion rate for the two neuropeptides is controlled by parameters k_D and k_N and we refer to these parameters as the strength of Dyn and NKB singalling respectively. The effector levels at which saturation occurs are controlled via parameters $K_{v,1}$, $K_{v,2}$ and K_D. Here, we are interested in investigating the effect of network excitability on the dynamics therefore we modify the equation for the neuronal activity, $\bar{v}$, by setting:

$$f_v(\bar{v}, \bar{N}) = v_0 \frac{1 - \exp(-I)}{1 + \exp(-I)}; I = I_0 + k_v \left(\frac{N^{n_4}}{N^{n_4} + K_N^{n_4}} \bar{v} \right),$$

where we have introduced parameter k_v capturing the strength of the synaptic connections between KNDy neurons in the ARC and which we will use a proxy for intrinsic network excitability. Furthermore, v_0 is the maximum rate at which the firing rate increases in response to synaptic inputs I. Note the stimulatory effect of NKB (which is secreted at the presynaptic terminal) on neuronal (Qiu et al., 2016) activity. Finally, parameter I_0 controls the basal

neuronal activity in the population, which could stem from synaptic noise or external inputs.

Table 1 give the full list of model parameters.

Parameter inference

We used Approximate Bayesian Computation (ABC) based on sequential Monte Carlo (SMC)

(Toni et al., 2009) to infer four key model parameters (Dyn signalling strength, k_D; NKB

signalling strength, k_N; network excitability k_v; and basal activity, I_0) in the estrous and

diestrous phase of the ovarian cycle. For this inference we used the average LH pulse frequency

observed in four different settings: estrous animals without optic stimulation (F_E) and with 5Hz

optic stimulation (F_{E+5Hz}); diestrus animals without optic stimulation (F_D) and with 5Hz optic

stimulation (F_{D+5Hz}). Model simulations were generated in Matlab using function ode45 under

the four different settings for 6000min and by calculating the frequencies after discarding the

initial 1000min. The following discrepancy function was used to compare simulated data,

$D^* = (F_E^*, F_{E+5Hz}^*, F_D^*, F_{D+5Hz}^*)$ to experimental data, $D = (F_E, F_{E+5Hz}, F_D, F_{D+5z})$:

$$d(D, D^*) = \max(abs(D - D^*))$$

Furthermore, for the ABC SMC algorithm the size of the particle population was set to 500

and the algorithm was run for $T = 4$ populations with corresponding tolerance levels $\varepsilon_i =$

$10^{2-i}, i = 1, ..., T$. The following prior distributions were used: $\log_{10}(k_D) \sim Uniform(-3,3)$,

$\log_{10}(k_N) \sim Uniform(-3,3)$, $\log_{10}(k_v) \sim Uniform(-3,3)$., $\log_{10}(I_0) \sim Uniform(-3,3)$

All remaining parameters were fixed to values found in the literature (see Table 1). For each

parameter an independent $\log_{10}$-normal perturbation kernel with variance 0.05 was used.

No	Parameter	Description	Value	Ref.
1	d_D	Dyn degradation rate	0.25 min^{-1}	(Voliotis et al., 2019)
2	d_N	NKB degradation rate	0.25 min^{-1}	(Voliotis et al., 2019)
3	d_v	Firing rate reset rate	10 min^{-1}	(Qiu et al., 2016)
4	k_D	Dyn singalling strength	inferred	
5	k_N	NKB signalling strength	inferred	(Ruka et al., 2016)
6	k_v	Network excitability	inferred	
7	v_0	Maximum rate of neuronal activity increase	30000 spikes min^{-2}	(Qiu et al., 2016)
8	K_D	Dyn IC$_{50}$	0.3 nM	(Yasuda et al., 1993)
9	K_N	NKB EC$_{50}$	32 nM	(Seabrook et al., 1995)
10	$K_{v,1}$	Firing rate for half-maximal Dyn secretion	1200 spikes min^{-1}	(Dutton and Dyball, 1979)
11	$K_{v,2}$	Firing rate for half-maximal NKB secretion	1200 spikes min^{-1}	(Dutton and Dyball, 1979)
12	I_0	Basal activity	inferred	
13	n_1, n_2, n_3, n_4	Hill coeffcients	2 (dimensionless)	fixed

243 **Table 1. Model parameters values**

Results

The dynamic response of the KNDy network to sustained, low-frequency optic stimulation is estrous cycle dependent.

To test whether and how sex steroids modulate the dynamical response of the KNDy network to sustained stimulation, ARC kisspeptin-expressing neurons were transduced with a Cre-dependent adeno-associated virus (AAV9-EF1-dflox-hChR2-(H134R)-mCherryWPRE-hGH) to express ChR2 (Fig. 1; see Materials and Methods) and were optogenetically stimulated at the estrous and the diestrous phase of the cycle, measuring LH pulse frequency as a readout of the system's dynamic response. Sustained, low-frequency optic stimulation was used to emulate elevated basal activity in ARC kisspeptin neurons or persistent stimulatory signals to the kisspepting population from other neuronal populations.

Figure 1. **Expression of arcuate nucleus (ARC) kisspeptin neurones with ChR2-mCherry in Kiss-Cre mouse.** Coronal section showing red mCherry fluorescence positive neurons in the ARC which indicates ChR2 receptor expressing kisspeptin neurones, following unilateral injection of AAV9.EF1.dflox.hChR2(H134R)-mCherry.WPRE.hGH into the ARC of Kiss-Cre mouse. The blue arrow shows the location of the injection site. Note the absence of mCherry fluorescence in the other side of ARC. 3V, Third ventricle.

In estrous mice, we find that sustained optogenetic stimulation of ARC kisspeptin neurons at 5Hz immediately triggers robust LH pulses at a frequency of 2.10 ± 0.24 pulses/hour (Fig. 2 A,C&E), which is in agreement with our previous findings (Voliotis et al., 2019) and highlights how pulsatile dynanics can emerge as a population phenomemon without the need of an intermittent activation signal (Strogatz, 2018). In diestrous mice, on the other hand, optogenetic stimulation of ARC kisspeptin neurons at 5Hz leads to an apparent slowdown of LH pulse frequency towards the end of the 1.5 h stimulation period (data not shown). To investigate the response in diestrous mice in greater detail we revised our experimental protocol, removing the control period and extending the stimulation period to 2.5 h. The revised protocol reveals a decrease in LH pulse frequency to 0.64 ± 0.09 and 0.40 ± 0.13 pulses/hour for 5Hz and 15 Hz optic stimulation respectively. albeit with a characteristic delay with 5 and 15 Hz optic stimulation, respectively (Fig. 2 B,D&F).

Our data illustrate how natural variation of ovarian steroids across the cycle leads to qualitative changes in the dynamical response of ARC kisspeptin neurons to optical stimulation. These changes are most probably driven by the effect that gonadal steroids have on the intrinsic electrophysiological properties of ARC kisspeptin neurons (Ruka et al., 2016) and the neuromodulator signalling capacity within the KNDy network (Vanacker et al., 2017).

Figure 2. Differential effect of optic stimulation of ARC kisspeptin neurons in estrous and diestrous Kiss-

Cre mice. (A-B) Representative examples showing LH secretion in response to no stimulation (grey bar) or

sustained blue light (473 nm, 5-ms pulse width, black bar) activation of kisspeptin neurons at 5 Hz in estrous (C)

and diestrous D) mice. (E) Summary showing mean ± SEM LH pulse frequency over the 60min control period

(white bars) and over the subsequent stimulation period (black bar) in estrous mice. (F) Summary showing mean

± SEM LH pulse frequency in the control (grey bar) and stimulated (black bars) diestrous mice. *Denote LH

pulses. [#]P < 0.05 vs control; [†]P < 0.05 vs pre-stimulation; n = 5-6 per group.

A mathematical model predicts key mechanisms modulating the behaviour of the KNDy

pulse generator across the estrous cycle.

To understand the origin of the differential effect that optic stimulation of ARC kisspeptin

neurons has across the ovarian cycle, we use our mathematical model of the KNDy network

(Voliotis et al., 2019). The model describes the dynamical behaviour of ARC kisspeptin

neurons using three dynamical variables: representing the levels of Dyn, NKB and neuronal

activity (Fig. 3 A). We postulate that gonadal steroids could potentially modulate the behaviour

of the KNDy system across the cycle via acting on four key model parameters capturing the (i)

level of Dyn signalling, (ii) level of NKB signalling, (iii) network excitability (i.e., propensity

of neurons in the population to transmit signals to one another), and (iv) basal neuronal activity.

Using the mean frequency data we observed experimentally in estrus and diestrus (with and

without 5Hz optic stimulation; Fig. 2 E&F) and employing Bayesian inference techniques (see

material and methods), we sample a population of estimates for these four parameters

corresponding to diestrus and estrus. Inspection of the dynamical behaviour of the model, using

the identified diestrous parameter values, reveals that in response to optic stimulation in

diestrus pulsatile dynamics could die out gradually (i.e, there is a transient period before

activity completely shuts down; see Fig. 3 B for an illustrative example), which is consistent

with the delayed inhibition of LH pulses we observed experimentally in diestrous mice.

Next, we focus on how the four key parameters change between diestrus and estrus. We

measure the change in each parameter using the log-ratio of its estrous to diestrous value, and

calculate the covariance matrix of these log-ratios from our set of inferred parameter values.

We find a positive (linear) correlation between changes in Dyn and NKB signalling strength,

and negative (linear) correlation between changes in NKB signalling strength and network

excitability (Fig. 3 C). That is, the model predicts that NKB signalling strength and network

excitability are characterised by opposite (in direction) correlations during the transition from

diestrus to estrus (one decreasing the other increasing; we note the model predicts that both

combinations are possible), whereas NKB and Dyn signalling remain correlated in the same

direction (ether increasing or decreasing; we note the model predicts that both combinations

are possible). Finally, we apply Principal Component Analysis (PCA) to study the sensitivity

of the system with respect to changes in the four parameters (Toni et al., 2009). We calculate

the principal components in dataset with the inferred parameter changes. Principal components

explaining small portions of the variance in the dataset (i.e., principal component with the

smallest eigenvalue) correspond to parameter combinations to which the system dynamics are

most sensitive (stiff parameter combinations). These combinations are the most critical in terms

of regulation as small changes in the combined parameters result in significant shifts in the

system's dynamics. Interestingly, the principal component capturing the smallest share of the

variance is comprised of the parameters controlling NKB signalling, Dyn signalling and

network excitability in approximately equal portions, and therefore the model predicts that co-

ordinated changes in these three parameters should be critical for the observed changes in

system dynamics between diestrus and estrus.

Taken together our theoretical findings suggest that network excitability in the KNDy network,

along with Dyn and NKB signalling, are crucial parameters of the GnRH pulse generator and

are tightly co-regulated across the reproductive cycle by the gonadal steroid milieu.

Figure 3. Model predictions on the key mechanisms modulating the behaviour of the KNDy pulse generator

across the ovarian cycle. (A) Schematic illustration of the coarse-grained model of the ARC KNDy population.

The model comprises three dynamical variables representing the average levels of Dyn and NKB secreted by the

population, and its average firing activity. We hypothesise that four key parameters modulate the behaviour of the

system across the ovarian cycle: (i) Dyn signalling strength; (ii) NKB signalling strength; (iii) network excitability

and (iv) basal neuronal activity. Estimates for the four parameters in estrus and diestrus are inferred from LH

pulse frequency data in estrus and diestrus animals; with or without 5Hz optic stimulation (Fig. 2 E&F) (B) System

response to low frequency stimulation during estrus and diestrus, using the maximum a-posteriori estimate of the

parameter values inferred from the frequency data. (C) Analysis of parameter changes across the cycle. For each

of the four parameter ($\theta^i; i = 1,2,3,4$) the diestrus-to-estrus change is defined as the log-ratio between the

corresponding parameter values, i.e., $\log_{10} \theta^i_{\text{estrus}} / \theta^i_{\text{diestrus}}$. Normalised covariance (correlation) matrix of

parameter changes reveals a strong negative correlation between changes in NKB signalling strength and network

excitability, and strong positive correlation between Dyn signalling strength and both NKB signalling and network

345   excitability. Principal component analysis produces a set of linearly uncorrelated eigen-parameters explaining the

346   variance of the inferred parameter values (posterior distribution). These eigen-parameters are linear weighted

347   combinations of the initial parameters and are visualised as pie charts. The eigen-parameter explaining the least

348   of the variance in the posterior distribution corresponds to the stiffest parameter combination to which the system

349   is most sensitive.

Glutamatergic transmission in the KNDy population is critical for LH pulsatility

The model predicts that excitability in the KNDy network (i.e., the efficacy of ARC kisspeptin

neurons to signal and excite each other) is one of the critical parameters controlling the dynamic

behaviour of the system across the ovarian cycle. As ARC kisspeptin neurons are mainly

glutamatergic (Cravo et al., 2011), we hypothesise that network excitability should be enabled

primarily via glutamatergic transmission. We therefore set out to test how disrupting signalling

via glutamate receptors impacts LH pulsatility.

First, using Kiss-Cre estrous mice we test whether glutamatergic transmission is necessary for

the optogentic induction of LH pulses. We drive the ARC kisspeptin population using

sustained, low-frequency optic stimulation (5 Hz) in the presence of the combined NMDA and

AMPA receptor antagonists (AP5 and CNQX, respectively). We find that blocking signalling

via glutamate receptors inhibits the capacity of optic stimulation to generate and sustain

pulsatile LH secretion (Fig. 4 A,B&D). The combined AP5 and CNQX in the absence of optic

stimulation had no effect (Fig. 4 C&D).

Next, we test whether glutamatergic transmission is critical for the endogenous LH pulses

observed in diestrus. Treatment of diestrous mice with the combined NMDA and AMPA

receptor antagonists resulted in a significant reduction of LH pulse frequency from 2.50 ± 0.29

to 0.45 ± 0.15 pulses/hour (Fig. 5 B&D), confirming that the glutamatergic transmission is

indeed critical for pulsatility. Moreover, combining NMDA and AMPA receptor antagonist

treatment with low frequency optic stimulation (5 Hz) partially restored LH pulsatility to 1.58

± 0.17 pulses/hour (Fig. 5 C&D), suggesting low network excitability could be offset by

exogenous inputs or elevated basal activity and highlighting the complex regulatory

interactions that are underpinning pulsatile GnRH secretion.

Figure 4. Effect of NMDA+AMPA receptor antagonists on pulsatile LH secretion in estrus. Representative examples showing LH secretion in estrous mice in response to optic stimulation (5Hz blue light, 473 nm, 5-ms pulse width) (A) and optic stimulation combined with the NMDA+AMPA receptor antagonist (bolus ICV injection [12 nmol AP5 + 5 nmol CNQX] over 5 min, followed by a continuous infusion [20 nmol AP5 and 10 nmol CNQX] for the remaining 90 min) treatment (B). NMDA+AMPA receptor antagonist alone had no effect (C). (D) Summary showing mean ± SEM LH pulse frequency over the 60min non-stimulatory period (white bars) and over the subsequent 90 min stimulation period or appropriate non-stimulatory period in presence of. NMDA+AMPA receptor antagonist alone (black bar) in diestrous mice. *Denote LH pulses. †P < 0.05 vs pre-stimulation. #P < 0.05 compared to antagonist treatment groups; n = 5-6 per group.

Figure 5. Effect of NMDA+AMPA receptor antagonists on pulsatile LH secretion in diestrus. Representative

examples showing pulsatile LH secretion in response to ICV administration of aCSF as control (A), treatment

with NMDA+AMPA receptor antagonists (AP5+CNQX: bolus ICV injection [12 nmol AP5 + 5 nmol CNQX]

over 5 min, followed by a continuous infusion [20 nmol AP5 and 10 nmol CNQX] for the remaining 90 min) (B)

and combined NMDA/AMPA receptor antagonist treatment and sustained optic stimulation (blue light 473 nm,

5-ms pulse width) at 5Hz (C). (D) Summary showing mean ± SEM LH pulse frequency over the 60min non-

stimulatory period (white bars) and over the subsequent 90 min stimulation period in control mice (grey bar) and

mice receiving treatment (black bar). *Denote LH pulses. [†]P < 0.05 vs pre-stimulation. [#]P < 0.05 compared to 5

Hz stimulation plus antagonist treatment and aCSF control groups; n = 5-6 per group.

Discussion

Using optogenetics we probed the dynamic response of the GnRH pulse generator at different

stages of the ovarian cycle. Previous studies have shown how the pulsatile activity generated

by the kisspeptin neuronal network is modulated across the estrous cycle (Han et al., 2015;

McQuillan et al., 2019). Our data show that the stage of the cycle has also a profound effect on

the dynamical response of the kisspeptin population to sustained, low frequency optic

stimulation: with stimulation during estrus accelerating LH pulses, while stimulation during

the diestrus phase slowing them down. This is suggestive of a critical role of the gonadal state

in modulating the dynamical response of the KNDy network to small changes in basal activity

of ARC kisspeptin neurons or in how the population processes external neuronal inputs.

Using our mathematical model of the system we gained insight into possible mechanisms via

which gonadal steroids modulate the dynamic behaviour of the GnRH pulse generator. Based

on the LH pulse frequency observed in estrous and diestrous animals under no optic stimulation

or with 5Hz optic stimulations, the model predicted that network excitability is an important

parameter of the system, which could be modulated at different stages of the ovarian cycle.

Importantly, KNDy network excitability is most probably co-regulated with parameters

controlling the strength of Dyn and NKB signalling as the system transitions between the

different phases of the ovarian cycle. In particular, our analysis suggests strong negative

correlation between changes in NKB signalling strength and changes in network excitability

and strong positive correlation in changes between NKB and Dyn signalling. Interestingly

these finding are in line with recent transcriptomic data showing that treatment of

ovariectomised mice with estradiol reduced expression of NKB and Dyn but increased

expression of glutamate transporters (vGlut2) leading to increased glutamate

neurotransmission and neuronal excitability (Qiu et al., 2018).

The effect of cycle stage on the LH response to sustained optogenetic stimulation is reminiscent

of the well documented effect that gonadal steroids have on LH response to various excitatory

neurotransmitters and neuropeptides (e.g., NMDA). For instance, investigations in the female

monkey revealed an unexplained inhibition of LH in OVX animals following treatment with

NMDA, in contrast with the excitatory action of NMDA on LH secretion in the presence of

ovarian steroids (Reyes et al., 1990; Reyes et al., 1991). Similar reversal of action on LH

dynamics depending on the underlying ovarian steroid milieu has been documented for various

other neurotransmitters and NKB receptor agonists (Kalra and Kalra, 1983; Scorticati et al.,

2004). Our mathematical model supports that ovarian steroids change key parameters of the

KNDy network, which control the dynamic behaviour of the system and its response to

perturbations. As an illustration, Fig. 6 shows how the dynamic behaviour of the model

depends on network excitability and NKB signalling. Since these parameters are governed by

gonadal steroids (Qiu et al., 2018; Wang et al., 2018), it is expected that the underlying steroid

milieu will also modulate the effect of perturbations on the dynamics of the system. For

instance, the effect of stimulating NKB signalling (e.g., via administration of NK3 receptor

agonists) or network excitability (e.g., via NMDA administration) could result in inhibition of

the pulse generator if the system is already located closer to the right boundary of the pulsatile dynamics region (e.g., point B in Fig. 6). Such points correspond to states with high pulse generator activity similar to pulse generator dynamics observed in many animal models after gonadectomy (Reyes et al., 1990; Kinsey-Jones et al., 2012). In contrast, similar perturbations but from a different point in the parameter space, lying closer to the left edge of the pulsatile region (e.g., point A in Fig. 6), could result in stimulation of the pulse generator (higher frequency). This illustrative example also highlights that it is the actual continuous levels of the gonadal steroids modulating the response of the pulse generator to perturbations rather than their mere presence or absence. Therefore, the underlying steroid levels could explain seemingly incompatible findings regarding the effect of NKB receptor agonism on LH secretion: ranging from stimulation (Navarro et al., 2011) or inhibition (Sandoval-Guzman and Rance, 2004; Kinsey-Jones et al., 2012) to no effects (Navarro et al., 2009) in rodents.

Figure 6. Differential effect of perturbations on the dynamics of the pulse generator. Two-parameter (NKB signalling and Network excit ability) bifurcation diagram showing the region in the parameter space for which the system exhibits pulsatile dynamics (grey area). Two points (denoted by A and B) illustrate how an increase in NKB signalling or network excitability could have a differential effect on the dynamics of the system. For point A an increase in network excitability or NKB signalling could lead to an increase in the frequency and width of pulses. However, for point B a similar increase leads to pulse inhibition and steady state system dynamics.

Based on our model predictions regarding the importance of network excitability, we set out to uncover the role of this parameter on the dynamic response of the network in-vivo. We hypothesised that network excitability should critically depend on the levels of glutamate signalling as ARC kisspeptin neurons are known to synapse one another (Yip et al., 2015; Qiu et al., 2016) and are primarily glutamatergic (Cravo et al., 2011; Qiu et al., 2011; Kelly et al., 2013; Wang et al., 2018). Therefore, we used glutamate receptor (NMDA and AMPA) antagonists to inhibit excitability in the KNDy network. ICV delivery of these antagonists

leaves open the possibility of interfering with the glutamatergic transmission of other neuronal

population to the KNDY population. Nevertheless, the effect of blocking these exogenous

inputs should be secondary to the effect of blocking signalling between kisspeptin neurons.

Indeed, our results suggested a critical role for glutamate in enabling the population to

synchronise and pulse in unison. In diestrus animals blocking glutamate receptors (NMDA and

AMPA) inhibited LH pulses that were then rescued via low frequency optogenetic stimulation

of kisspeptin neurons. Furthermore, in estrus animals, NMDA and AMPA receptor antagonism

inhibited the induction of LH pulses via optic stimulation. These experimental findings

highlight the complex fine-balanced mechanisms underlying pulse generation by the KNDy

network. In particular, limited glutamatergic signalling within the KNDy population blocks LH

pulsatility but this can be mitigated by elevated basal neuronal activity. Similarly, increased

basal neuronal activity can induce pulse generation but this effect can be negated by decreased

glutamatergic signalling within the neuronal population. Pulse generation is therefore an

emergent property of the KNDy network depending both on intrinsic, single neuron properties

such as basal activity but also on how the neurons signal and communicate with each other.

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476 **Acknowledgments:** The authors gratefully acknowledge the financial support of the EPSRC
477 via grant EP/N014391/1 (KTA and MV), and BBSRCH via grants BB/S000550/1 and
478 BB/S001255/1 (KTA, KOB, MV, XFL).

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