1 **Antagonistic inhibitory subnetworks control cooperation and competition across cortical**
2 **space**
3

Daniel P. Mossing[1,2], Julia Veit[2,3], Agostina Palmigiano[4], Kenneth D. Miller[4,5] and Hillel Adesnik[2,6]
[1]Biophysics Graduate Group, University of California, Berkeley
[2]Dept. of Molecular and Cell Biology, University of California, Berkeley
[3]Present address: Institute of Physiology I, University of Freiburg
[4]Center for Theoretical Neuroscience, College of Physicians and Surgeons and Mortimer B.
Zuckerman Mind Brain Behavior Institute, Columbia University
[5]Dept. of Neuroscience, Swartz Program in Theoretical Neuroscience, Kavli Institute for Brain
Science, College of Physicians and Surgeons and Mortimer B. Zuckerman Mind Brain Behavior
Institute, Columbia University
[6]The Helen Wills Neuroscience Institute, University of California, Berkeley

14
15 **Abstract**
16

The cortical microcircuit can dynamically adjust to dramatic changes in the strength, scale, and
complexity of its input. In the primary visual cortex (V1), pyramidal cells (PCs) integrate widely
across space when signals are weak, but integrate narrowly when signals are strong, a
phenomenon known as contrast-dependent surround suppression. Theoretical work has
proposed that local interneurons could mediate a shift from cooperation to competition of PCs
across cortical space, underlying this computation. We combine calcium imaging and
electrophysiology to constrain a stabilized superlinear network model that explains how the
four principal cell types in layer 2/3 (L2/3) of mouse V1– somatostatin (SST), parvalbumin (PV),
and vasoactive intestinal peptide (VIP) interneurons, and PCs transform inputs from layer 4 (L4)
PCs to encode drifting gratings of varying size and contrast. Using bidirectional optogenetic
perturbations, we confirm key predictions of the model. Our data and modeling show that
network nonlinearities set up by recurrent amplification mediate a shift from a positive PC-VIP
feedback loop at small size and low contrast to a negative PC-SST feedback loop at large size
and high contrast to support this flexible computation. This may represent a widespread
mechanism for gating competition across cortical space to optimally meet task demands.

32
33 **Introduction**
34
The brain must process sensory inputs across a wide range of sensory environments and
perceptual goals. When sensory signals are weak, adding of activity in ensembles encoding
congruent evidence across space ("corroboration") could optimize detection; when signals are
strong, subtraction of congruent signals ("explaining away") could optimize discrimination or
localization (Sceniak, et al. 1999, Hawken, et al. 2001, Nauhaus, et al. 2009). For a sensory code
to capture this flexible functional interaction, neural ensembles encoding distinct elements of
sensory evidence must be able to rapidly change the nature of their interaction, competing or
cooperating depending on sensory inputs.
Causal and correlative evidence suggests that with increasing contrast, interactions
across cortical space become less cooperative and more competitive (Nauhaus, et al. 2009,

Sato, Häusser and Carandini 2014). However, the network mechanisms underlying this shift are
incompletely understood. Theoretical work has proposed that local inhibition mediates the
transition from cooperative to competitive spatial interactions (Angelucci et al., 2017; Schwabe
et al., 2010); yet whether distinct interneuron subtypes play dissociable roles is unknown
(Rubin et al., 2015). In this study, we determine how a cortical microcircuit of genetically
defined interneuron subtypes underlies this shift from cooperation to competition across
cortical space.
Three interneuron subtypes, parvalbumin- (PV), somatostatin- (SST) and vasoactive
intestinal peptide- (VIP) expressing, comprise 80-85% of cortical interneurons. All three
subtypes have been found to shape the sensory coding properties of pyramidal cells, the
primary output neurons of cortex, in distinct ways to facilitate cortical encoding of sensory
features (Adesnik et al., 2012; Ayzenshtat et al., 2016; Lee et al., 2012; Rudy et al., 2011; Wilson
et al., 2012). VIP cells specialize in inhibition of other interneurons (Pi, et al. 2013, Lee, et al.
2013, Pfeffer, et al. 2013) and may thus play a crucial role in gating cortical competition. VIP
cells receive feedback excitation from higher areas (Zhang, et al. 2014) and strong
neuromodulatory input from the midbrain (Fu, et al. 2014) which positions them to mediate
top-down control of flexible functional interactions in the cortex (Wang & Yang, 2018; Yang et
al., 2016). Recent work has shown that VIP cells, like PCs and PV cells, are highly surround
suppressed (Dipoppa et al., 2018), are sensitive to low contrasts (Millman et al., 2019), and
prefer spatially heterogeneous as opposed to homogeneous textures (Keller, Roth, Caudill, et
al., 2020). Because VIP cells preferentially innervate SST cells (Pfeffer et al., 2013), which are
known to control spatial summation in the cortex (Adesnik, et al. 2012), we hypothesized a
novel role for VIP cells, in contributing to the contrast dependence of cooperation and
competition across cortical space.
Because cortical neurons' firing rate depends superlinearly on their input current
(Anderson, et al. 2000, Miller and Troyer 2002), effective monosynaptic connection strength
depends on the activity level of the postsynaptic neuron. A relatively inactive neuron, whose
average membrane potential is far from its spike threshold, is insensitive to changes in its input.
On the other hand, a highly active neuron, depolarized close to action potential threshold, will
sensitively transduce changes in its synaptic inputs to changes in its spike rate. Because
postsynaptic neurons' activity is tuned to stimulus features, effective monosynaptic connection
strength can itself show stimulus tuning. Because polysynaptic effects depend on the activity of
all intervening cell types, the stimulus tuning of total functional connectivity can be
combinatorially complex. Tuned functional connectivity via polysynaptic effects in a superlinear
network could represent a computationally powerful mechanism for shaping interactions
between ensembles encoding distinct features of the sensory environment (Ahmadian et al.,
2013; Del Molino et al., 2017; Rubin et al., 2015).
We hypothesized that cortical VIP-SST inhibitory microcircuitry in combination with cell-
intrinsic firing rate nonlinearities underlies contrast dependent surround suppression. We
combined experiment and theory to test whether firing rate nonlinearities dynamically set
effective monosynaptic connection strengths, and via polysynaptic effects the total functional
connectivity, between the four principal cortical subtypes to flexibly support cooperation or
competition of PCs across space. To achieve this, we first recorded from the major cell types of
the upper cortical layers in V1 with two photon imaging and electrophysiology while stimulating

V1 with drifting gratings of varying size and contrast. We then used these comprehensive
observational data to fit a circuit model that could explain contrast-dependent shifts from
cooperation to competition across space in terms of shifting effective connection strength
between genetically defined populations of neurons with superlinear responses to input
current. Finally, we tested core predictions of this model with targeted optogenetic
perturbations of VIP cells while measuring the impact on all other cell types. The insight that
superlinearity *per se* could powerfully shape network responses was critical to interpreting
optogenetic effects: at steep points in their superlinearities, neurons were more sensitive to
perturbations. Residual effects, those not explained by activity level in the unperturbed
condition, sensitively reflected the underlying functional connectivity of the network.
We find that VIP and SST activity outline contrasting regimes of sensory coding in PCs. In
the VIP-dominated regime, when the network is weakly activated by stimuli of low contrast and
small size, increasing PC activity drives VIP cells, which in turn disinhibit PCs, closing a positive
PC-VIP feedback loop. PCs show surround facilitation and are highly sensitive to changes in
contrast. Conversely, in the SST-dominated regime, when the network is strongly activated by
stimuli of high contrast and large size, increasing PC activity instead drives SST cells, which in
turn inhibit PCs, closing a negative feedback loop. PCs show surround suppression and are
weakly sensitive to changes in contrast. Thus, the VIP-dominated regime optimizes the dynamic
range of contrast encoding at the expense of the coding of space, while the SST-dominated
regime optimizes dynamic range of size encoding at the expense of the coding of contrast. Our
model explains that high spontaneous drive to VIP cells competes with spatially broad PC→SST
drive to establish these disparate regimes of cortical operation. With increasing size and
contrast, positive PC-VIP feedback, promoting cooperation of PCs across space, is gradually
replaced by negative PC-SST feedback, promoting competition across space. We test key
predictions of this model by showing that optogenetically enhancing the spontaneous drive to
VIP cells powerfully drives activity in the positive feedback-dominated small and low contrast
regime, and more weakly in the negative feedback-dominated large and high contrast regime.
Finally, we show that contrast-dependent recurrent amplification within the PC-PV subnetwork
enhances the difference between these two regimes of circuit operation. This work provides a
detailed explanation for flexible cooperation and competition across cortical space by virtue of
cortical microcircuitry and the intrinsic superlinearity of neurons. Furthermore, it establishes a
generalizable approach for predicting and explaining how physiological or optogenetic
perturbations propagate through a highly recurrent network.
122
123   **Results**
124
125   **Cell-type specific encoding of size and contrast in the mouse primary visual cortex**
126
To study a paradigmatic example of flexible cooperation and competition across cortical space,
we first probed the logic of contrast-dependent surround suppression in layer 2/3 pyramidal
cells (L2/3 PCs) of the primary visual cortex (V1). We recorded neural activity in awake, head-
fixed mice (fig. 1a) using cell type-specific calcium imaging (fig. 1b). After mapping each
neuron's receptive field, we independently varied the size, contrast, and direction of drifting
gratings while keeping their location constant. We measured responses using deconvolved

Figure 1. Cell type-specific responses to stimulus size and contrast in mouse V1. A) Mice were head-fixed and free to run on a circular treadmill, while passively viewing a monitor showing drifting gratings of varying size, contrast, and direction. B) Transgenic mouse lines were used to express gCaMP6s in defined subsets of neurons. C) Event rate deconvolved from gCaMP fluorescence was used to estimate neural activity. D) Averaged deconvolved event rates in L2/3 PCs are plotted against drifting grating patch size, with different contrasts plotted separately. Event rates are normalized to the mean across all stimuli and all neurons within each imaging session. In all size tuning plots, darker color corresponds to higher contrast. E) Surround modulation index (SMI) is defined as the response to 60° gratings divided by the response to the preferred size for each contrast. Each transparent line corresponds to an imaging session, and the solid line corresponds to the average across sessions. F) To quantify the contrast dependence of surround suppression, the SMI at the lowest contrast (6%) is subtracted from the SMI at the highest contrast (100%). This difference of SMI corresponds to the magnitude of contrast dependence of surround suppression. G) The same tuning curves as in D) are plotted, separated by size, with contrast varying along the x-axis. In all contrast tuning plots, darker color corresponds to larger size. H) Naka-Rushton functions were fit to contrast tuning curves for each L2/3 PC experiment. Plotted is C_{50}, the contrast evoking a half-maximal response for the fit Naka-Rushton function, as a function of size, for each experiment (transparent lines) and averaged (bold lines). I) As a global metric of size-dependent contrast sensitivity, we compute the difference in C_{50} between the 5° and 36° size. J-Q) Same as D), G), for L4 PCs, L2/3 PV cells, L2/3 SST cells, and L2/3 VIP cells, respectively. ** significantly different from zero, $p < 0.01$, Wilcoxon signed rank test. Error bars represent bootstrap SEM equivalent.

event rate (fig. 1c, see Methods), and first restricted our analysis to neurons within 10 degrees
of retinotopic space of the center of the stimulus representation, and trials on which the animal
was not locomoting (see Methods). To specifically examine tuning for size and contrast, we
averaged responses across the directions sampled. We first asked how size tuning varied as a
function of contrast. Prior electrical recordings from unidentified cell types in monkeys
(Cavanaugh et al., 2002; Kapadia et al., 1999; Levitt & Lund, 1997; Sceniak et al., 1999), cats
(Polat et al., 1998; Sengpiel et al., 1997; Toth et al., 1996), and mice (Ayaz et al., 2013; Nienborg
et al., 2013; Vaiceliunaite et al., 2013) have established that surround suppression in V1
increases with increasing contrast. Consistent with these findings, we found that at high
contrast, L2/3 PC responses showed strong bandpass size tuning, peaking sharply at small sizes,
while at low contrast, responses peaked more broadly, and at larger size (fig. 1d). Because
stimuli of increasing size drive activity in distal (surrounding) regions of cortical space, this is
consistent with a picture in which surround PCs cooperate with center PCs at low contrast
(supporting broad size tuning) and compete with center PCs at high contrast (supporting sharp
tuning for small sizes).
In order to quantify the degree of surround suppression as a function of contrast, we
computed a surround modulation index (SMI) defined as the response to 60° gratings (the
largest shown) at a given contrast, divided by the response to the preferred size at the same
contrast. We computed these metrics on the population-averaged tuning curves for each
imaging session. SMI decreased monotonically, corresponding to strengthening surround
suppression, with increasing contrast (fig. 1e). As a global metric for the contrast dependence
of surround suppression, we computed the difference of SMI at 6% contrast and 100% contrast.
We found that this difference was significantly positive (fig. 1f—Wilcoxon signed rank test,
p<0.05), indicating that surround suppression increased in strength with increasing contrast.
Enhanced surround facilitation at low contrast has been theorized to enhance
detectability of large textures. If this were the case, we would expect to see sensitivity to low
contrast stimuli increase with size. We measured this change in sensitivity directly by taking a
complementary view of the same data, examining contrast tuning at each size (fig. 1g). The C_{50},
or contrast evoking half-maximal response, increased monotonically with size up to 36° (fig.
1h). As a global metric for the size dependence of contrast sensitivity, we computed the
difference in C_{50} between 5° and 60° size; this difference was significantly positive (fig. 1i—
Wilcoxon signed rank test, p<0.05). Thus, contrast sensitivity was enhanced at large sizes,
consistent with spatial integration enhancing stimulus detectability.
We next asked whether these properties were robust across behavioral states and
recording modalities. We found qualitatively similar results between the locomoting and non-
locomoting conditions (fig. S1). To validate these measurements with electrical recordings, we
performed analogous experiments in which we sampled V1 activity using multi-electrode arrays
rather than calcium imaging. Regular spiking (RS) units could be compared with PCs in our
calcium imaging data. Importantly, tuning measured with electrophysiology and calcium
imaging closely agreed (fig. S2; non-locomoting, RS units, R=0.82, p=2×10^{-8}, Wald test).
To address the network mechanisms that might contribute to PC size and contrast
tuning, we next probed the tuning of other cell types in the circuit. First, we asked whether
similar tuning properties were present in the primary input layer of cortex, layer 4 (L4). Indeed,
L4 PCs on average showed similar tuning (fig. 1j,k), suggesting tuning of feedforward inputs

contributes to contrast-dependent surround suppression. We then examined the principal
inhibitory inputs to L2/3 PCs, local interneurons. Prior theoretical studies have proposed that
local interneurons could support a contrast-adaptive code in PCs; one specific model predicts
the existence of an inhibitory cell type that is selectively driven at high contrasts, driving
surround suppression only under these conditions (Angelucci, et al. 2017). We first asked
whether L2/3 PV cells, which share inputs with and strongly inhibit L2/3 PCs, might show
enhanced selectivity for high contrast relative to L2/3 PCs. However, we found that in keeping
with their high degree of shared inputs, tuning of PV cells closely matched that of PCs (fig.
1l,m). Fast spiking (FS) units measured using extracellular electrophysiology closely agreed with
PV cell measurements (fig. S2; non-locomoting, FS units, R=0.84, p=7x10^{-9}, Wald test).
Therefore, we next examined a second major L2/3 interneuron subtype, SST cells.
Previous work has implicated SST cells in contributing to surround suppression of PCs at high
contrast (Adesnik, et al. 2012, Nienborg, et al. 2013). Although SST cells are known to prefer
larger sizes than the other cortical cell types, how this depends on stimulus contrast is not
known. In fact, SST tuning diverged sharply from that of PCs and PV cells. SST cells responded
best at large size and high contrast, and weakly or not at all at small size and low contrast (fig.
1n). Examining SST contrast tuning at varying size showed that at small size, they were
insensitive to all but the highest contrast; stimuli that drove nearly maximal activity in PCs and
PV cells only weakly drove SST cells (fig. 1o). Since SST cells receive strong excitation from L2/3
PCs (Adesnik, et al. 2012, Hakim, Shamardani and Adesnik 2018, Kapfer, et al. 2007, Karnani, et
al. 2016), this difference in tuning was surprising.
This raised the possibility that strong inhibition from L2/3 VIP cells to SST cells
counteracts PC→SST excitation to explain SST cells' remarkable insensitivity to contrast. If this
were true, VIP cells might show size and contrast tuning opposite to that of SST cells. VIP cells,
which powerfully and preferentially inhibit SST cells (Pfeffer et al., 2013), exhibit the strongest
surround suppression of all cell types at high contrast (Dipoppa, et al. 2018), and are highly
sensitive to contrast at large size (Millman et al., 2019). Whether and how VIP contrast
responses vary as a function of stimulus size, however, is not known. In line with our prediction,
as a population VIP cells were selectively responsive at small size and low contrast, and strongly
suppressed at large size and high contrast (fig. 1p; at a single neuron level, this population
average reflected a mixture of behaviors, from strict contrast suppression, to bandpass size and
contrast tuning (fig. S3)). Examining the same data as contrast tuning at varying size showed
further stark differences between SST and VIP cells. Unlike SST cells' monotonic contrast tuning,
VIP cells on average showed bandpass contrast tuning, with the preferred contrast decreasing
with increasing size (fig. 1q). These data demonstrated that SST and VIP cells differentially
encode stimulus size and contrast, and demarcate disparate regimes of visually-evoked
inhibitory circuit activity – one in which VIP is active but SST is largely silent, and one in which
SST is active and VIP activity is strongly suppressed. Thus, average VIP and SST responses were
strongly anti-correlated across sizes and contrasts (fig. S4a, p=5x10^{-5}, Wald test).
Next, we asked how SST and VIP activity might relate to functional interactions of PCs
across space. To address this, we first computed a local metric for PC spatial integration at each
size and contrast: the slope of PC size tuning curves (fig. S4b). This metric was positive where PC
responses were increasing with increasing size (surround facilitating), and negative where PC
responses were decreasing with increasing size (surround suppressing). We then plotted this

metric against the difference between SST and VIP activity (which we termed the SST – VIP axis)
for each stimulus condition. Indeed, we found that surround facilitation was strongly anti-
correlated with movement along the SST – VIP axis (fig. S4c, R=-0.36, p=0.03, Wald test). We
next asked whether the slope of PC contrast responses could likewise be explained by the
differential activity of VIP and SST cells; as a metric for contrast sensitivity, we measured the
local slope of PC contrast responses in a similar way (fig. S4d). Indeed, movement along the SST
– VIP axis was strongly anti-correlated with PC contrast tuning slope (fig. S4e, R=0.44, p=7x10^{-3}).
Thus, in the VIP-dominated regime, PCs sensitively encoded contrast, and in the SST-dominated
regime, PCs sensitively encoded spatial features.
230
231 **A recurrent network model explains size and contrast tuning of the four cell-type circuit**
232
The data presented above show that VIP and SST activity demarcate disparate regimes of
inhibitory circuit operation in V1 L2/3. To understand mechanistically how these regimes might
arise, and how they could give rise to contrast-dependent cooperation and competition of PCs
across space, we developed a data-driven recurrent network model. The goal of this model was
to explain how feedforward drive from L4, recurrent connectivity, and cell-intrinsic
superlinearities interact to dynamically shift PC functional connectivity across space from
cooperative to competitive with increasing stimulus size and contrast.
Using the comprehensive physiological data presented above, along with the responses
of neurons of each cell type located in the surround of the stimulus representation (fig. S5), we
fit a superlinear stabilized network model (see Methods). This model simulated two spatial
domains (center and surround) each containing five cell types (fig. 2a): L4 PCs, which serve as
feedforward inputs, and the four L2/3 cell types. In the model, each L2/3 cell type received a
linear combination of inputs from each other population, transformed through a static
nonlinearity to determine its firing rate (Miller and Troyer 2002) whose dynamics were
described by:

$$\frac{d\boldsymbol{r}}{dt} = -\boldsymbol{r} + f(W\boldsymbol{r} + \boldsymbol{h}). (1)$$

Here, $\boldsymbol{r}$ is a vector representing the firing rate of each cell type, W is the matrix of synaptic
connection strengths, $\boldsymbol{h}$ is a vector of external inputs and bias currents, and f represents the
static nonlinearity. Importantly, the network was constrained to be in an inhibitory stabilized
regime across all stimulus conditions (Sanzeni et al., 2020). Importantly, many model fits were
able to recapitulate key tuning features for each cell type (fig. 2b), including the contrast
dependence of surround suppression of PCs and PV cells, the low contrast sensitivity and high
size sensitivity of SST cells, and bandpass contrast tuning of VIP cells. We next analyzed the
behavior of the best fitting models, starting from randomly initialized model parameters (see
Methods) to identify robust features of network parameters explaining the calcium imaging
data. The synaptic weight matrix averaged across successful model fits is presented in fig. 2b.
Notably, many of the connection weights in these fits correspond well to known connections
from prior studies, including the strong connections among PCs and PV cells, and the strong
reciprocal inhibition between SST cells and VIP cells (Pfeffer et al., 2013). Distributions of model
parameters across successful model fits are shown in fig. S6.

Figure 2. A network model explains tuning properties of layer 2/3 cell types. A) The rate-based network model consisted of five cell types, spread across two spatial domains. Using gradient descent on a loss function defined based on the calcium imaging data, we optimized a set of weights describing connection strengths among these cell types. Connections between two cell types across spatial domains were attenuated by a cross-space weight that was allowed to vary based on the postsynaptic cell type. B) Synaptic weight matrix between cell types averaged across model fits, and size tuning of all five modeled cell types, by contrast. C) Violin plots of bias currents to each cell type. D) Schematic depicting stimulus-dependent effective connections between PCs, and SST and VIP cells. Effective connection strengths are given by the

product of synaptic weight and firing rate nonlinearity slope. For small and low contrast stimuli, VIP cells sit at a steep point in their firing rate nonlinearity, and SST cells at a shallow point. Thus, effective PC→VIP connection strength is stronger than PC→SST. At large size and high contrast, the opposite is true. E) Effective connection strength between PC and SSTs (orange) or VIP (magenta) is plotted as a function of contrast, at 22° size, F) Modeled responses of SST or VIP to weak activation of PCs in both layers and spatial pixels are plotted as a function of contrast, at 22° size. G) Violin plots of cross-space weights for each cell type. H) Schematic depicting stimulus-dependent cooperation and competition between PCs across space. At small size and low contrast, surround PCs more effectively drive VIP cells, disinhibiting center PCs by inhibiting SST cells. At large size and high contrast, surround PCs more effectively drive SST cells, inhibiting center PCs. I) Top: schematic of the modeled perturbations, eliminating either PC→SST or PC→VIP connections. Bottom: Modeled responses of center PCs to weak activation of surround PCs are plotted as a function of contrast, at 22° size. Orange: same but deleting the PC→SST connection. Magenta: deleting the PC→VIP connection. J) The difference between center PC responses to surround PC activation at 100% contrast, and 0% contrast, at 22° size, for the intact network, and after deleting the PC→SST and PC→VIP connections. In the intact network, the difference is significantly larger across successful model fits ($p < 10^{-3}$, $p < 10^{-6}$, Wilcoxon signed-rank test). Error bars represent 16th to 84th percentile of model fits.

Our first goal was to understand the opposing contrast sensitivity of VIP and SST cells.
Starting from spontaneous (0° size, or 0% contrast) activity, increasing PC activity seemed to
first drive VIP activity and not SST activity, at small size and low contrast, and subsequently to
suppress VIP activity while driving SST activity, at large size and high contrast. We first asked
how a single set of synaptic weights could support these seemingly opposite effects depending
on stimulus. We reasoned that a key ingredient might be the superlinear increase of firing rate
with increasing input current. With this superlinearity, active neural populations would be
sensitive to subsequent changes in their input, while inactive populations would be insensitive.
Thus, the importance of a given connection in shaping network activity would increase with the
activity level of the postsynaptic cell type.
First, we asked why at small size and low contrast, increasing PC activity drove VIP cells
but not SST cells. We reasoned that high spontaneous drive to VIP cells could play a role. If
spontaneous drive to VIP ("bias current" in the model) outweighed spontaneous drive to SST,
then the slope of the VIP firing rate nonlinearity should be steep for low levels of sensory
activity, while the slope of the SST firing rate nonlinearity should be shallow. Thus initially,
starting from spontaneous activity, increasing PC activity could robustly drive VIP cells, but not
SST cells. Consistent with this notion, in our physiological data VIP cells exhibited nearly half
maximal activity during spontaneous activity, while SST cells exhibited only 10% of their
maximal activity (fig. S4f). In keeping with this empirical result, across successful model fits, the
bias current to VIP cells was more positive than the bias current to SST cells (fig. 2c, fig. S7a). In
the model, this differential bias current supported the VIP-dominated regime at small size and
low contrast.
Next, we aimed to understand what shifts the network to an SST-dominated regime in
response to large and high contrast gratings. With increasing size and contrast, we
hypothesized that growing levels of PC activity could allow SST cells to overcome VIP cells'
initial advantage in spontaneous input current and ultimately outcompete them (fig. 2d). This
would be possible if SST cells could more effectively convert increases in PC activity to
inhibitory SST→VIP current, than VIP could convert PC activity to inhibitory VIP→SST current.
One possible mechanism would be if SST→VIP weights were larger than VIP→SST weights.
Indeed, across successful model fits, SST→VIP weights were on average 110% stronger than
VIP→SST weights (fig. S7b). Thus, in the model, powerful SST→VIP inhibition supported the
SST-dominated regime at large size and high contrast.
We next asked how the network transitioned from the VIP-dominated to the SST-
dominated regime. First, we expected that with increasing contrast, monosynaptic excitation
from PCs should more strongly drive SST cells, and more weakly drive VIP cells. To test this
hypothesis in the model, we computed "effective monosynaptic connection strengths" for each
pair of cell types and for each stimulus condition. We defined effective monosynaptic
connection strengths from the presynaptic population I to the postsynaptic population j as the
synaptic weight matrix elements $w_{i \to j}$ multiplied by the slope of the postsynaptic firing rate
nonlinearity φ_j. We examined effective connection strength at 22°, a size at which we observed
surround suppression at the highest contrast and nearly flat size tuning at low contrast.
Consistent with the conceptual explanations presented above, we found that during
spontaneous activity, PC→VIP effective connection strength outweighed that of PC→SST (fig.
2e). PC→VIP effective connection strength then gradually decreased with increasing contrast,

while PC→SST effective connection strength gradually increased (fig. 2e), ultimately overtaking
it at 50-100% contrast. This suggested that as contrast increases, PCs more effectively recruit
SST cells compared with VIP cells, helping to explain the contrast-dependent shift from a VIP- to
an SST-dominated regime.
Having characterized the effective monosynaptic connection strength from PCs to SST
cells and VIP cells, we then asked how the full polysynaptic effect of PCs on these cell types, or
functional connectivity, changed with increasing contrast to shape their tuning. We simulated
the impact of small excitatory current injections to L2/3 PCs, propagating through the full
recurrently connected network, on VIP and SST firing rates (fig. 2f—see Methods). Indeed, as
contrast increased, driving PC activity increasingly drove SST cells, but increasingly suppressed
VIP cells. In fact, by simulating current injections of increasing, finite magnitude to PCs starting
from spontaneous activity, we were able to reconstitute opposing tuning of SST and VIP cells,
with SST cells showing superlinear responses to increasing PC activity, and VIP cells showing
bandpass responses, peaking at intermediate levels of PC activity (fig. S7c). Deleting either the
VIP bias current (fig. S7d) or the SST→VIP weight from the model (fig. S7e) abolished this
behavior, tipping the competition in favor of SST and VIP cells, respectively, across contrasts.
This supported the idea that a large stimulus-independent current to VIP cells competes with
strong stimulus-dependent SST→VIP inhibition to support opposing regimes of VIP and SST
activity depending on stimulus size and contrast.
To understand the significance of these opposing regimes of VIP and SST activity, we
then examined the monosynaptic connectivity of the VIP-SST subnetwork across cortical space.
Above, we proposed that SST activity should support surround suppression by participating in
disynaptic inhibition across space. If this were true, we would expect that SST cells should
strongly integrate inputs across the two modeled spatial domains. Indeed, across successful
model fits, SST cells had substantially higher cross-space weight than the other three L2/3 cell
types (fig. 2g). Next, we expected that PC-SST feedback could be important for promoting
competition between PCs across space. In turn, we reasoned that PC-VIP feedback might
suppress competition by controlling tuning of SST cells (fig. 2h).
To measure cooperation and competition between PCs across cortical space in the
model, we simulated the effect of excitatory current injections to L2/3 PCs in the surround, on
L2/3 PCs in the center. The model predicted surround PCs should increasingly suppress center
PCs with increasing contrast (fig. 2i). To test the importance of PC-SST feedback for this
contrast-dependent competition, we deleted PC→SST connections, allowed the rest of the
network to settle to a new steady state, and then repeated the activation of surround L2/3 PCs
as before. Eliminating this connection promoted cooperation at all contrasts, and weakened the
contrast dependence of this competition overall (fig. 2i,j), demonstrating that in the model, PC-
SST negative feedback is critical for contrast-dependent competition across space. Deleting
PC→VIP connections in a similar way promoted competition across all contrasts, and weakened
the contrast dependence of this competition overall (fig. 2i,j). This demonstrated that in the
model, a balance of negative PC-SST feedback and positive PC-VIP feedback is necessary for the
contrast dependence of cooperation and competition between PCs across space.
348
Optogenetic dissection of the VIP-SST subnetwork's role in contrast dependent surround
suppression

The computational model explained that PC-SST feedback supports competition between PCs
across space, while PC-VIP feedback supports cooperation. This implies that VIP cells might
directly shape the tuning of SST cells. Indeed, the model predicted that suppressing VIP cells
would significantly alter the response properties of SST cells (fig. 3a). To empirically test this, we
examined the impact of optogenetically silencing VIP cells on SST responses using simultaneous
one photon optogenetics and two photon calcium imaging. We simultaneously measured
neural activity in VIP cells, SST cells, and PCs (see Methods and fig. S8) while silencing VIP cells
using Cre-dependent eNpHR3.0. We first confirmed the efficacy of optogenetic silencing of VIP
cells (fig. S9b). Red illumination through the microscope objective robustly suppressed activity
in eNpHR3.0-expressing VIP cells approximately linearly across stimuli by about 67% (fig. S9c-h,
R=0.91, p=1×10^{-9}).
Consistent with model predictions, silencing VIP cells potently facilitated SST cells across
all sizes and contrasts (fig. 3b). This demonstrated that VIP cells crucially regulate visually driven
SST-activity. More importantly, we next asked whether the remarkable insensitivity of SST cells
to low contrast stimuli could be explained by inhibition from VIP cells. If VIP activity is necessary
for tuning the contrast sensitivity of SST cells, silencing VIP cells should preferentially facilitate
SST responses to low contrast. Indeed, we found that silencing VIP cells preferentially
potentiated SST cells' responses to low contrast (fig. 3c), and only more weakly facilitated SST
responses to high contrast (fig. 3d). This was true across sizes (fig. 3e,f). As a result, the
sensitivity of SST cells to contrast increased significantly, measured as a decrease in the C_{50} of
their contrast tuning across sizes (fig. 3g, $p < 0.05$, Wilcoxon signed-rank test). This
demonstrates that VIP cells shape the contrast sensitivity of SST cells by strongly suppressing
their responses to low contrast.
Having established that VIP activity was necessary for suppressing SST responses to low
contrast, we next asked how this effect would propagate through the network polysynaptically
to PCs, which only receive weak or sparse monosynaptic inhibition from VIP cells (Pfeffer et al.,
2013). Because intrinsic firing rate nonlinearities in L2/3 PCs have been found to give rise to
non-intuitive asymmetries in optogenetic perturbations (Phillips & Hasenstaub 2016), we
measured the impact on PCs of both activation and silencing of VIP cells. A previous model of
this microcircuit predicted that disconnecting VIP cells from the network (equivalent to
completely silencing them) would suppress PC responses selectively to low contrast, while
leaving responses to high contrast unaffected (Millman et al., 2019). However, because
superlinearity was a key driver of tuning properties in our network model, one might predict
the opposite: that silencing of VIP cells could more strongly suppress PCs at high contrast, when
PCs are at a more sensitive point in their firing rate nonlinearity (see schematic, fig. 4a). We
conceived a purely phenomenological simple superlinear model, in which the effect of
bidirectional (silencing or activating) optogenetic perturbations on response to a given stimulus
linearly increases with increasing network activity in the control (light off) condition (fig. 4b). By
contrast, in a simple linear model, the effect of optogenetic perturbations would be constant
with respect to control activity level. This phenomenological model allowed us to partition
optogenetic effects into two components: a component that could be explained purely by the
activity level in control conditions for a specific visual stimulus (fig. 4c), and a residual
component that could not (fig. 4d). We reasoned that this residual component, not explained

Figure 3. VIP suppression enhances responses of SST cells to low contrast. A) Model: predictions for the impact of inhibitory current injection to VIP on the responses of SST cells to gratings of various contrasts and sizes. Shown is a scatter plot of SST event rate with light off, vs. difference between light on and light off, for stimuli of varying size (dot size) and contrast (dot color—increasing from cold to warm colors). B) Same as A), but for experimental VIP silencing. C) SST event rate as a function of size, at 6% contrast, in the light off (black) and light on (yellow) condition. D) Same as C), for 100% contrast. E) SST event rate as a function of contrast, at 5° size. F) Same as E), for 60° size. G) C_{50} as a function of size. C_{50} is significantly reduced by VIP silencing at the 11° size, and across sizes. Error bars represent bootstrap SEM equivalent.

a

b

c

d

Simulated:

VIP silencing

VIP activation

Experimental:

VIP silencing

VIP activation

e

f

g

h

i

j

k

l

m

n

o

p

Figure 4. Network superlinearity explains experimental and simulated effects of bidirectional VIP manipulations, in simulation and experiment. A) Schematic model for predicting the effects of VIP perturbations. PC activity is intrinsically superlinear, with both network suppression and network facilitation increasing in strength with increasing network activity. B) If the effect of optogenetic perturbation is entirely described by a superlinear curve, as in A), the light on – light off activity (Δ activity) given light off (control) activity will fall along a monotonically increasing (decreasing) curve for facilitating (suppressing) perturbations. If the curve in A) is an exponential, the curve describing changes in activity is a straight line. C) Schematic scatter plot of Δ activity, vs. control activity, with best fit line in yellow. "Residual" effects are defined as the difference between the actual change in activity, and best fit line. D) Schematic plot of residual effects vs. contrast. E) Scatter plot of PC Δ firing rate vs. control firing rate for simulated inhibitory current injection to VIP, with L4 activity held constant. In yellow is the least squares linear fit, with shading indicating bootstrap 68% confidence intervals. Dot size and color are as in fig. 3A. F) Same as A), for simulated excitatory current injection to VIP. In red is the least squares linear fit, with shading indicating bootstrapped 68% confidence intervals. G) Experimentally measured Δ PC event rate in response to VIP silencing, vs. control event rate. Linear fit is plotted as in C). H) Same as G), but for VIP activation.. I) Residual effect of simulated VIP inhibitory current injection in E) not captured by the best fit line. J) Same as I), but for simulated VIP excitatory current injection in F. K,L) Same as I), J), but for experimental VIP silencing and activation, respectively, in G),H). M-P) Residual effect at 100% - 0% contrast, for 5º and 60º size, for data in I-L), respectively. Error bars indicate bootstrap SEM equivalent. Shading on fit lines indicates 68 percent confidence interval of linear fits.

simply by network superlinearity, might be informative of recurrent network mechanisms.
Using our network model, we could then separately probe the roles of modeled synaptic
connections in generating each component.
First, we sought to distinguish whether our network model was operating in the regime
exemplified in (Millman et al., 2019), or in a regime where superlinearity dominated responses
to optogenetic perturbations. If the latter were true, the simple superlinear model should
capture much of the optogenetic effects. Because our network model took L4 PC activity as
feedforward input, it was first necessary to measure the direct effects of bidirectional VIP
manipulations on L4 PCs (see fig. S10a,b and Methods). We then simulated bidirectional current
injections to VIP cells, combined with the empirically measured bidirectional effects on L4 PCs.
Across a range of simulated current injection magnitudes, the full recurrent network model
predictions were broadly in line with the simple superlinear model, with higher control firing
rates predicting stronger suppressive effects of VIP silencing (fig. 4e, R=-0.72, p=0.0, Wald test)
and stronger facilitating effects of VIP activation (fig. 4f, R=0.16, p=2x10^{-13}, Wald test). This
agreed with the simple superlinear model prediction, and contrasted with the prediction of
(Millman et al., 2019). This was true also when excluding the effect of VIP manipulations on L4
PCs in the model (fig. S11). Our network model predicted that despite VIP cells' low activity
level at high contrast, perturbations to VIP cells would be differentially amplified by the
network depending on the strength of PC activity in control conditions, thus increasing with
contrast overall.
To test this model prediction experimentally, we virally expressed Cre-dependent
eNphR3.0-mRuby3 or ChrimsonR-tdTomato in VIP cells in separate mice, and gCaMP6s in all
L2/3 neurons using the hSynapsin promoter (see Methods). As with VIP silencing, we confirmed
the efficacy of optogenetic activation of VIP cells. Red illumination through the microscope
objective drove robust activity in ChrimsonR-expressing VIP cells across stimulus conditions (fig.
S12a,b), although optogenetic facilitation was somewhat stronger for small and low contrast
stimuli (fig. S12c-h). Importantly, in control mice expressing no opsin, the optogenetic
stimulation light alone produced no systematic facilitation or suppression of visual responses
(fig. S13). This confirmed that the observed effects were due to the optogenetic perturbation
per se. Next, we analyzed the impact of perturbing VIP cells on the activity of all gCaMP6s-
expressing neurons not labeled with a red fluorophore (primarily PCs). In both VIP silencing and
VIP activation experiments, PC responses with the optogenetic light off agreed well with
responses we measured previously using calcium imaging in transgenic gCaMP-expressing mice
(fig. S14; VIP silencing, R=0.95, p=3x10^{-12}, Wald test; VIP activation, R=0.84, p=3x10^{-7}, Wald
test). As predicted by the full recurrent network model, across stimulus conditions, high PC
activity in control conditions predicted stronger suppressing effects of VIP silencing (fig. 4g, R=-
0.64, p=2x10^{-12}, Wald test), and stronger facilitating effects of VIP activation (fig. 4h, R=0.45,
p=2x10^{-8}, Wald test).
Importantly, the simple superlinear model, in which control activity levels completely
determined the effect of optogenetic perturbations, could explain much but not all of the effect
of bidirectional VIP manipulations on PC activity. We next examined the residual effects of
optogenetic perturbations that were not captured by the simple superlinear model: specifically,
the difference between the actual change in activity and the best fit line prediction of change in
activity from control activity. We reasoned that these residuals might shed light on the

Figure 5. VIP activation unidirectionally enhances contrast-dependent surround suppression.
A) Size is plotted on the x-axis, and PC event rate on the y-axis, for 6% contrast, the lowest tested, in the light off condition (black) and light on condition (yellow). B) Same as A) for 100% contrast. C) Surround modulation index is plotted as a function of contrast, in the light on and light off conditions. D) Change in SMI between the light off and light on condition, with each line an experiment. E) Same as A), B), but responses to increasing contrast are plotted for fixed 5° size, in the light off and light on condition. F) Same as E), but for 60° size. G) C_{50} is plotted as a function of size, for the light off and light on conditions. H) Bar plot of change in C_{50} between 5° and 60° size, for the light off and light on conditions, with lines indicating individual imaging sessions. I-P) Same as A-H), but for optogenetic activation of VIP cells. * significant difference, $p < 0.05$ (Wilcoxon signed-rank test). Error bars indicate bootstrap SEM equivalent.

recurrent network mechanisms that mediate the contrast dependent shift from cooperation to
competition via the VIP-SST network. If competition between PCs across space increased with
increasing contrast, as predicted by the recurrent network model, we might expect this to
support a strong negative feedback loop at high contrast, limiting the network's response to VIP
activation at high contrast but permitting it at low contrast. We optimized the magnitude of
excitatory and inhibitory current injected to VIP cells for each model fit, to maximize dynamic
range of PC competition across space (see Methods and fig. S17). Although modeled residual
effects of VIP silencing were small (fig. 4i), modeled residual effects of VIP activation were in
keeping with this prediction (fig. 4j). PC facilitation in response to VIP activation was stronger
than expected by the simple superlinear model at low contrast, and weaker than expected at
large size and high contrast. Experimental results of VIP silencing (fig. 4k) and activation (fig. 4l)
showed a similar asymmetry. Across all conditions, VIP activation at 60° size showed the
strongest contrast dependence of residuals, defined as the residual effect at 100% contrast –
0% contrast (fig. 4m-p).
We then asked how this asymmetric contrast-dependent residual effect of bidirectional
VIP manipulation affected contrast-dependent surround suppression in the experimental data.
Although VIP silencing significantly suppressed visual responses across most stimuli (Fig. 5a,b),
it did not significantly affect the surround modulation index (SMI) at any contrast (fig. 5c), and
thus there was no significant change in ΔSMI between 6% and 100% contrast (fig. 5d). Similarly,
there was no significant change in contrast sensitivity at any size (fig. 5e-h). We corroborated
these calcium imaging results by recording neural activity using extracellular electrophysiology
in a separate cohort of mice. In these electrophysiological experiments, we also compared the
optogenetic effects between the non-locomoting an the locomoting condition (fig. S15), and as
above, saw no brain-state dependent difference. We also found similar effects in RS and FS
units (fig. S15). These measurements confirmed that VIP silencing did not substantially alter the
contrast dependence of surround suppression.
On the other hand, VIP activation enhanced visual responses across all conditions. For
the same control activity level, activating VIP cells disproportionally facilitated PCs in response
to large, low contrast stimuli (fig. 5i), but less so for large, high contrast stimuli (fig. 5j). As a
consequence, VIP activation enhanced the contrast dependence of surround suppression
overall, evident as an increase in SMI specifically at low contrast (fig. 5k,l) and an increase in
ΔSMI between 6% and 100% contrast. This change in contrast-dependent surround suppression
could not be explained by the simple superlinear model alone (fig. S16), and therefore was a
result of the asymmetric contrast-dependent residual effects of VIP activation. Similarly, VIP
activation increased size dependence of contrast sensitivity (fig. 5m-p).
We next returned to our recurrent network model to ask whether this asymmetric
contrast-dependent residual effect of VIP activation was tied directly to contrast dependent
spatial competition between PCs. If this were the case, we would expect manipulations that
suppressed the contrast dependence of PC spatial competition to suppress the contrast
dependence of residual effects of VIP activation. Previously, we found that the contrast
dependence of PC spatial competition in the model depended on an interplay between two
feedback loops: a PC-VIP feedback loop, primarily active at low contrast, and promoting
cooperation, and a PC-SST feedback loop, primarily active at high contrast, and promoting
competition. Having established that these feedback loops supported the contrast dependence

of PC spatial competition, we next asked whether they also supported the contrast-dependent
residual effect of VIP activation on PC responses that was evident in our previous simulations.
While deleting PC→VIP weights or PC→SST weights only weakly affected simulated responses
to VIP silencing (fig. 6a,b respectively), the same manipulation dramatically reduced simulated
responses to VIP activation (fig. 6c,d respectively). Similarly, these manipulations significantly
and asymmetrically reduced residual effects of VIP activation, and not silencing (fig. 6d-g), as
well as the contrast dependence of these residuals (fig. 6h-k). This suggested that the
asymmetric contrast-dependent residual effect of VIP activation, which was necessary for
enhancement of contrast-dependent surround suppression, was a result of contrast-dependent
spatial cooperation and competition between PCs. The model predicted that this asymmetric
residual effect at low contrast was a generic result of facilitating feedforward drive to the L2/3
network, not only via manipulation of VIP activity (fig. S10c,d). Further, the asymmetry could be
explained by enhanced contrast dependence of positive PC-VIP feedback specific to moderate
increases in PC and VIP activity, with decreases in activity, and large increases in activity,
causing a much weaker reduction in this contrast dependence (fig. S17). Thus, modeling results
supported the idea that residual effects of VIP activation we observed were signatures of
contrast-dependent competition between PCs across space, mediated by the VIP-SST
subnetwork.
501
502   **Recurrent amplification drives the network superlinearity that enforces contrast dependent**
503   **surround suppression**
504
Our modeling and optogenetic results suggested that network superlinearity critically shapes
cooperative and competitive interactions across space, and thus the sensory code. To address
the origin of this superlinearity, we considered two possibilities: it could be generated purely by
the cell-intrinsic firing rate nonlinearity, or also steepened by PC-PC recurrent excitation. To
distinguish between these two possibilities, we simulated the effect of direct current injection
to PCs in several conditions. First, to isolate the cell-intrinsic response, we deleted all synaptic
connections in the network and compared this to the intact condition. Deleting all connections
made network nonlinearity much more shallow (fig. 7a, black solid black versus dashed black
line). This suggested that recurrent circuits contributed substantially to network superlinearity.
Next, we selectively deleted PC-PC weights while leaving all other connections intact. This
yielded a substantially shallower response to current injection than the full network response,
and shallower even than the cell-intrinsic firing rate nonlinearity alone (Fig. 7a, gray solid line).
This suggested that PC-PC recurrent excitation is critical to this superlinearity, and in its
absence, powerful feedback inhibition from PV cells may suppress network superlinearity even
below the cell-intrinsic nonlinearity. To test this, we deleted all recurrent connections among
the PC-PV subnetwork (PC-PC, PC-PV, and PV-PV), while leaving all other connections intact. In
this scenario, current injections to PCs yielded a superlinear response similar to the cell-intrinsic
firing rate nonlinearity alone (Fig. 7a, blue line). Notably, deleting PC-PV connections alone
drove the network to instability (data not shown). Thus, within the network model, recurrent
amplification by the PC-PV subnetwork generated a second and more powerful network
nonlinearity, building on the cell-intrinsic firing rate nonlinearity.

Figure 6. Asymmetric residual effect of VIP perturbation reflects contrast-dependence of PC-VIP and PC-SST feedback loops in simulation. A) Scatter plot of modeled change in firing rate, vs. control firing rate, both normalized to mean across stimuli, in response to inhibitory current injection to VIP cells, after deleting PC→VIP connections. Transparent dots and lines in all panels correspond to the baseline condition, without deleting any connections. Dot size and color are as in fig. 3A. B) Same as A), after deleting PC→SST connections, respectively. C,D) Same as A), B), but for modeled excitatory current injection to VIP cells. E-H) Residual effect of VIP silencing and activation in A-D), respectively, defined as effect minus expectation based on linear fit to control (light off) firing rate. I-L) Residual effect at 100% - 0% contrast, for 5° and 60° size, for data in E-H), respectively. Error bars indicate bootstrap SEM equivalent. Shading on fit lines indicates 68 percent confidence interval of linear fits.

Figure 7. A positive PC-PV feedback loop enhances contrast-dependent surround suppression in simulation. A) Schematic of modeled perturbations. We measure the response of simulated neurons for (1) no network connections (cell-intrinsic response), (2) the baseline

condition (all connections intact), (3) PC-PC connections selectively deleted, and (4) PC-PC, PC-PV, and PV-PV connections deleted. Plotted at right is the simulated L2/3 PC firing rate in response to direct current injections to L2/3 PCs, vs. the current injected, for the four conditions considered, at the 0% contrast condition. Shading indicates 16th to 84th percentile. B) Simulated response of L2/3 center PCs to excitatory current injection to L2/3 surround PCs, for 22° size, at increasing contrast. Also plotted are the same responses for PC-PC connections deleted, or all recurrent connections among PCs and PV cells deleted. C) The difference between center PC responses to surround PC activation at 100% contrast, and 0% contrast, at 22° size, for the baseline case, and after deleting PC-PV connections, or all connections among PCs and PV cells. At baseline, the difference is significantly larger across successful model fits (p < 10^-7, p < 10^-7, Wilcoxon signed-rank test). D) Scatter plot of simulated change in L2/3 PC activity vs. baseline activity in response to inhibitory current injection to VIP cells, plus empirically measured suppression of L4 PCs, after deleting all recurrent connections among PCs and PV cells. Transparent dots and lines in all panels correspond to the baseline condition, without deleting any connections. Dot size and color are as in fig. 3A. E) Same as D), but for simulated excitatory current injection to VIP cells, plus empirically measured facilitation of L4 PCs (same as 4F), after deleting all recurrent connections among PCs and PV cells. F,G) Residual effect of VIP perturbation in D), E), respectively, defined as effect minus expectation based on linear fit to baseline firing rate. H, I) Residual effect at 100% - 0% contrast, for 5° and 60° size, for data in F), G), respectively. J) Schematic summarizing primary findings. At low contrast and small size, VIP cells are highly active, enhancing the effective weight of the PC-VIP connection. This results in a disinhibitory positive feedback loop, facilitating PC responses and promoting cooperation among PCs. At high contrast and large size, SST cells are highly active, enhancing the effective weight of the PC-SST connection. This results in a negative feedback loop, suppressing PC responses and promoting competition among PCs. Recurrent amplification within the PC-PV subnetwork strengthens both the positive PC-VIP and negative PC-SST feedback loops. Error bars in B), C) indicate 16th to 84th percentile of model fits. Error bars in D-G) indicate bootstrap SEM equivalent. Shading on fit lines indicates 68 percent confidence interval of linear fits.

We next asked what role intrinsic connections within the PC-PV subnetwork played in
shaping contrast-dependent cooperation and competition of PCs across space. Consistent with
recurrent PC-PV connections amplifying the effect of contrast-dependent PC-VIP and PC-SST
feedback loops, we found that in the absence of connections among PCs, or among PCs and PV
cells, PC competition across space depended much more shallowly on contrast (fig. 7b,c).
Because superlinearity could explain the control activity dependence of VIP optogenetic effects,
we reasoned that the PC-PV network could powerfully shape this dependence, via the
steepness of the network nonlinearity. We next asked how the network nonlinearity generated
by recurrent PC-PV connections shaped the impacts of VIP perturbations on PCs. To this end,
we simulated optogenetic VIP activation as before with the full network intact, or when
deleting recurrent weights among PCs and PV cells. Based on the enhancement of network
superlinearity by recurrent weights among PCs and PV cells, we first expected that the activity
dependence of PC responses to VIP perturbations (as captured by the simple superlinear model
above) would be strongly affected. Indeed, while effects of simulated VIP silencing were only
modestly affected by deleting weights in the PC-PV subnetwork (fig. 7d), across stimuli, the
same manipulation substantially reduced the effects of simulated VIP activation (fig. 7e).
Previously, we found that this contrast-dependent spatial competition had signatures in
the residual effects of bidirectional VIP perturbations, compared to the predictions of a purely
superlinear prediction. In principle, we reasoned that positive feedback loops within this
subnetwork could shape the residual effects we observed above, by amplifying the strength of
the PC-VIP and PC-SST feedback loops shaping PC competition across cortical space. Based on
our simulations of deleting PC-VIP and PC-SST connections, we predicted that the reduced
contrast dependence of spatial competition we observed after deleting connections in the PC-
PV subnetwork would result in a dramatic reduction in residual effects of VIP activation on PC
responses at low contrast. As shown above, for the intact network, VIP silencing generated
small residual effects on PCs; deleting recurrent PC-PV weights dampened even these small
residual effects. For the intact network, VIP activation generated a large contrast-dependent
residual effect on PCs (fig. 7i) and deleting recurrent PC-PV weights severely dampened these
residual effects (fig. 7j). This suggested that, within our simulations, the small and low contrast-
selective effect of VIP activation, depends critically on positive feedback loops within the PC-PV
subnetwork. Thus, the model explains that PC-PV recurrent amplification sets up a steep
network superlinearity that synergizes with a PC-VIP positive feedback loop at small size and
low contrast to favor cooperation across space, and with a PC-SST negative feedback loop at
large size and high contrast to favor competition (fig. 7k).
560
561   **Discussion**
562
We combined experiments and computational modeling to address the circuit mechanisms that
gate cooperation and competition across cortical space. We studied contrast-dependent
surround suppression in the primary visual cortex as a paradigmatic example of such flexible
cooperation and competition. Although discovered more than two decades ago, a circuit
mechanism for how the same cortical circuit dynamically shifts between a cooperative and
competitive operating regime based on the size and contrast of the visual stimulus has been
lacking. As the same cell types and circuits exist throughout cortical areas, the findings of this

study may generalize beyond the visual cortex to more broadly explain how cortical circuits
adjust functional interactions across cortical space to meet task demands.
Through a combination of calcium imaging, electrophysiology, optogenetic
perturbations, and network modeling, we show that a transition from positive PC-VIP feedback
at low contrast, to negative PC-SST feedback at high contrast, explains the contrast dependence
of surround suppression. Because SST cells strongly integrate PC inputs across space, these
positive and negative feedback loops couple PCs across space. The PC-PV subnetwork amplifies
the strength of both feedback loops. We tested core predictions of this model experimentally
by optogenetically perturbing VIP cells. First, as predicted by the superlinearity of the network,
both VIP silencing and activation have the strongest effects when PC activity is highest, namely
at small size and high contrast. On top of this activity-dependent effect, VIP activation had a
large, asymmetric residual effect that was unexplained by PC activity level, positive at low
contrast and negative at high contrast. Our network model explains that this residual effect is a
consequence of contrast-dependent PC competition across space. Further, due to network
superlinearity, building on the cell-intrinsic superlinearity, the contrast dependent
enhancement of PC-VIP positive feedback by VIP activation is stronger than the contrast-
dependent suppression of PC-VIP positive feedback by VIP silencing, contributing to the
asymmetry. We found the partitioning of optogenetic effects into an activity-dependent
component and a residual component to be important to our interpretation of the optogenetic
results. The asymmetric effects of VIP activation and inactivation on pyramidal cell tuning are
reminiscent of a recent study examining activation and inactivation of PV and SST cells in A1
(Phillips & Hasenstaub, 2016). Bidirectional perturbations, generally, are likely to provide
rigorous tests of a predictive understanding of network dynamics.
The data and modeling presented above highlight that understanding strongly
recurrently connected networks (within and beyond the cortex), requires a combination of
causal perturbations and computational modeling. Without causal perturbations,
computational models may be underconstrained. In contrast to the theoretical predictions of a
recent study (Millman et al., 2019), we found that the effect of removing VIP activity from the
network was not selective for low contrast stimuli, despite the fact that VIP activity was highest
for those stimuli in control conditions. On the other hand, inferring recurrent network
mechanisms from causal perturbations is likely to be difficult when unsupported by a
computational model. The contrast dependence of PC coupling to the VIP and SST subnetworks,
which our perturbations revealed, challenges the simplest linear intuitions of how the network
might operate. Iteratively developing new intuitions instructed by recurrent network models,
such as feedback loops and stabilization, may be crucial for developing a predictive
understanding of neural function. Because one study cannot explore all possible causal
perturbations, constraining models based on the results of multiple studies will likely become
increasingly important. Incorporating the constraint that our modeled network occupy an
inhibitory stabilized regime, established by causal perturbations in previous studies, was crucial
to our understanding of the mechanism of network superlinearity.
In this study we considered PCs, PV cells, SST cells, and VIP cells as homogenous
populations, and restricted most of our analysis to population averages. However, it is already
well appreciated that each of the cell types breaks down into distinct sub-classes with unique
physiological properties, anatomy, and circuit connectivity. Future work may uncover

subpopulations of the interneurons we studied playing dissociable roles. For example, VIP cells
are transcriptionally diverse, and molecular markers such as cholecystokinin and calretinin (He,
et al. 2016), could define functional subclasses of VIP cells. Tuning diversity of VIP cells, like
transcriptional diversity, has also been found to correlate with cortical depth (Dipoppa, et al.
2018). Diversity in tuning properties may align with diversity of functional roles in the cortical
microcircuit. A recent study in the somatosensory barrel cortex found that a subpopulation of
VIP cells co-expressing ChAT exert an inhibitory influence on PCs specifically in response to
weak stimuli (Dudai, et al. 2020). A combination of intersectional genetic techniques and
optogenetics, or two photon optogenetics, could yield further insight in the functional roles of
distinct VIP populations in sensory coding. Furthermore, other 5-HT3aR+ interneurons not
expressing VIP, particularly in layer 1, have been shown to have similar tuning for sensory
signals as VIP cells (Abs et al., 2018; Mesik et al., 2015). Future work could clarify the extent to
which these cell types act in concert with VIP cells or play disparate roles to control sensory
coding. In addition to discrete variability between sub-classes of each cell type, continuous
variability could be important, both in synaptic connections and in tuning properties. Future
work could seek to model this variability, which might generate further hypotheses to be tested
with more sophisticated optogenetic perturbations.
Translaminar inhibitory as well as excitatory connections are also likely to be important,
particularly as VIP manipulations affect L4 as well as L2/3 activity. Future work expanding the
scope of these experiments could clarify the extent to which translaminar feedforward and
feedback connections shape the response properties of these cell types. Further, these cell
types might differentially integrate feedback signals from higher areas (Keller, Roth, &
Scanziani, 2020; Zhang et al., 2014), which could be important for their encoding of
homogeneous textures as well as richer stimuli.
Furthermore, although we argue that the influence of VIP cells is likely to be important
for network regimes optimizing detection, this study has examined only passively viewing mice,
not animals motivated to detect weak signals. Behavioral context and salience of sensory inputs
has been found to powerfully shape the tuning properties of these interneuron types, possibly
to enhance coding properties of pyramidal cells. Future work combining two photon imaging of
these cell types with behavior and network modeling could suggest possible dynamical
mechanisms for this enhancement.
Despite these limitations, there is growing evidence that the circuit motifs examined in
this study may generalize to other areas of the brain. In particular, in auditory cortex, a series of
recent studies have uncovered analogous tuning properties and functional roles of the same
interneuron types. VIP cells show bandpass tuning for sound amplitude (analogous to contrast)
(Mesik, et al. 2015), while SST cells are insensitive to all but high amplitude tones (Li, Xiong, et
al. 2015). Whereas PCs commonly prefer narrow spectral bandwidth (analogous to size) (Li et
al. 2019), SST cells prefer broader spectral bandwidth (Lakunina et al., 2020). Silencing SST cells
results in a reduction of lateral inhibition (Kato, Asinof and Isaacson 2017) and a facilitation of
PC responses to broad spectral bandwidth sounds (Lakunina et al., 2020). Future work could
examine the extent to which the L2/3 microcircuit in V1 and A1 occupies a similar dynamical
regimes, and examine tuning properties of interneurons in S1 for space and intensity. How
these insights extend to non-sensory cortices is an exciting area for future study.

Supplementary Figures

Figure S1. Similar cell-type specific responses to stimulus size and contrast during locomotion.
A) Size tuning curves of L2/3 PCs in the locomoting condition, averaged across experiments. B) Surround modulation index (SMI; response to 60° size / response to preferred size) of L2/3 PCs as a function of contrast in the locomoting condition. C) Change in SMI between 6% and 100% contrast for all three cell types. **, significantly greater than 0, p < 0.01. D-G) Same as A), but for L4 PCs, L2/3 PV cells, L2/3 SST cells, and L2/3 VIP cells, respectively. Error bars indicate bootstrap SEM equivalent.

Figure S2. Extracellular electrophysiology reveals similar tuning properties as calcium imaging. A) Scatter plot of firing rate of regular spiking (RS) units recorded using extracellular electrophysiology, vs. PC event rate/mean across stimuli measured using calcium imaging for the equivalent stimuli, in the non-locomoting condition. Dot size and color are as in fig. 3A. B) Same as A), but for fast spiking (FS) units recorded using extracellular electrophysiology, vs. PV event rate/mean measured using calcium imaging. C) Size tuning curves, separated by contrast, for RS units plotted in A). D) Same as C) for FS units plotted in B). E) Surround modulation index

(SMI), defined as the response to $60°$ gratings divided by response to the preferred size gratings, as a function of contrast, for L2/3 RS units. Each line is a single recording session, and the bold line corresponds to average across recording sessions. F) same as E) for L2/3 FS units. G) Difference of SMI between 6% and 100% contrast. Each dot corresponds to one recording session. H-N) Same as A-G), for the locomoting condition. ** significantly positive, $p < 0.01$; ***, $p < 0.001$. Error bars indicate bootstrap SEM equivalent.

Figure S3. Example tuning curves show diversity of VIP cell size-contrast tuning. A) Receptive field of an example SST cell (see Methods). Mapped using 10º drifting gratings of time-varying direction, shown for 1.5 seconds each. B) ΔF/F time course of size-contrast responses for the neuron shown in A; each curve represents the response to gratings of a given contrast, averaged across sizes and orientations. C) Size tuning of the same cell, split up by contrast. D-F) Same as A-C), for an example contrast-suppressed VIP cell. G-I) Same as A-C), for an example contrast-facilitated VIP cell. Error bars indicate bootstrap SEM equivalent.

Figure S4. SST and VIP activity outline contrasting regimes of PC spatial integration. A) Average event rate of SST cells, normalized to the mean across stimuli, is plotted on the x axis, with VIP responses plotted on the y-axis, likewise normalized to the mean across stimuli. Dot size and color are as in fig. 3A. On the basis of their negative correlation, we define an axis based on the difference between SST and VIP activity. B) On the x axis is plotted size, and on the y axis is plotted the local slope of PC size tuning curves. Where the slope is positive, cells undergo surround facilitation on average, and where the slope is negative, cells experience surround suppression. C) PC size tuning slope is plotted against the difference of SST and VIP event rate. D) Same as B), but for the local slope of PC contrast tuning curves. E) Same as C), but with PC contrast tuning slope rather than size tuning slope. F) Spontaneous activity of SST and VIP cells, as a fraction of maximal sensory-evoked activity. ** significantly different, p < 0.01, Wilcoxon signed rank test. Error bars indicate bootstrap SEM equivalent.

Figure S5. Neurons with receptive fields not aligned with the stimulus center show preference for larger sizes. A) Size tuning of L4 PCs, including only those located within 10 visual degrees of retinotopic space of the center of the stimulus representation (left). Beyond 10 visual degrees (right). B-E) Same as A), for L2/3 PCs, PV cells, SST cells, and VIP cells, respectively. Error bars indicate bootstrap SEM equivalent.

Figure S6. Well performing model fits show variability in fit parameters. A) Violin plots showing variability in synaptic input weights among model fits for each of the four L2/3 cell types modeled. B) Variance of intrinsic input noise for each cell type.

Figure S7. Network parameters support PC activity-dependent competition between VIP and SST cells. A) VIP bias current is plotted against SST bias current, for all successful model fits. VIP bias currents are significantly larger than SST bias currents, p=8x10^{-16}, Wilcoxon signed-rank test. B) VIP→SST weight is plotted against SST→VIP weight, across successful model fits. SST→VIP weights are significantly stronger (more negative) than VIP→SST weights, p=4x10^{-15}, Wilcoxon signed-rank test. C) Starting from the network steady state for 0% contrast (dashed line), positive or negative current injections to PCs are modeled, and the resulting steady state firing rates of SST and VIP cells are plotted as a function of injected current to PCs. D) Same as C), but after deleting (setting to 0) VIP bias current. E) Same as C), but after deleting SST→VIP weight. Shading indicates 16th to 84th percentile of model fits.

Experimental:

a   Putative VIP   b   Putative SST

c   Putative PC   Putative VIP   Putative SST

d

e

Figure S8. SST-tdTomato and VIP-mRuby3 cells can be distinguished by brightness and spatial profile. A) Outlines of putative VIP (membrane-bound mRuby3 expressing) cells, with red channel images. B) Analogous for putative SST (cytosolic tdTomato expressing) cells. C) Average red channel images for putative PCs (left), VIP cells (middle), and SST cells (right), aligned to the center of each cell. D) Red intensity (a.u.) as a function of radial distance from the center of the ROI. Each transparent line is one cell, and the bold line is the average. On the left, in magenta, are putative VIP cells, and on the right, in orange, are putative SST cells. E) Same plots as D), but normalized to the maximum value.

Figure S9. Optogenetic silencing of VIP cells. A) eNpHR3.0-mRuby3-labeled VIP cell from a VIP silencing experiment. B) ΔF/F averaged across all VIP cells, for gray screen trials following gray screen trials with no optogenetic stimulation. In yellow is the average trace for trials where the optogenetic stimulation light was on, and in black is the average trace for trials where the optogenetic stimulation light was off. C) Response of a VIP cell to gratings of varying size, at 6% contrast. In black is the light off response, and in yellow is the light on response. D) Same as B), for 100% contrast. E,F) Same as C), D), but for varying contrast, at 5° and 60° size, respectively. G) Scatter plot of light on vs. light off event rate for putative VIP cells at varying size and contrast. In yellow is the best fit line, with the intercept constrained to be 0. Dot size and color are as in fig. 3A. H) Residual effect of optogenetic manipulation not captured by the best fit line in G), for varying contrast, and at varying sizes. Shading and error bars represent bootstrap SEM equivalent.

Figure S10. VIP manipulation modulates feedforward inputs to L2/3. A) Effect of VIP silencing on L4 regular spiking units measured using extracellular electrophysiology. Change in measured firing rate, normalized to mean light off firing rate, is plotted against light off firing rate, normalized to its mean, averaged across mice. Dot size and color are as in fig. 3A. B) Effect of VIP activation on L4 PCs measured using calcium imaging. Change in measured event rate, normalized to mean light off firing rate, is plotted against light off firing rate, normalized to its mean, averaged across mice. C) Response of L2/3 PCs to a modeled DC decrease in L4 PC firing rate across stimulus conditions. Change in firing rate, normalized to mean, is plotted against baseline firing rate. D) Same as C), but for a DC increase in L4 PC firing rate, across stimulus conditions. Error bars represent bootstrap SEM equivalent.

Figure S11. Modeled effect of bidirectional VIP manipulations depend on baseline activity, even without change to layer 4 activity. A) Scatter plot of modeled change in firing rate, vs. baseline firing rate, both normalized to mean across stimuli, in response to inhibitory current injection to VIP cells, without perturbing L4 PC activity. Dot size and color are as in fig. 3A. **B)** Same as A), but for excitatory current injection to VIP cells. Error bars represent bootstrap SEM equivalent.

Figure S12. Optogenetic activation of VIP cells. A) ChrimsonR-tdTomato-labeled VIP cell from a VIP activation experiment. B) ΔF/F averaged across all VIP cells, for gray screen trials following gray screen trials with no optogenetic stimulation. In red is the average trace for trials where the optogenetic stimulation light was on, and in black is the average trace for trials where the optogenetic stimulation light was off. C) Response of VIP cells to gratings of varying size, at 6% contrast. In black is the light off response, and in red is the light on response. D) Same as B, for 100% contrast. E,F) Same as C), D), but for varying contrast, at 5° and 60° size, respectively. G) Scatter plot of light on vs. light off event rate for putative VIP cells at varying size and contrast. In red is the best fit line, with the intercept constrained to be 0. Dot size and color are as in fig. 3A. H) Residual effect of optogenetic manipulation not captured by the best fit line in G), for varying contrast, and at varying sizes. Shading and error bars represent bootstrap SEM equivalent.

Figure S13. VIP perturbations bidirectionally control responses of VIP and non-VIP cells. A) Scatter plot of size-contrast tuning responses for an example neuron from a VIP-eNpHR3.0 expressing mouse. On the x-axis are plotted light-off responses, and on the y-axis, light-on responses. In yellow is the best-fit slope transforming light-off to light-on responses, and in black is the unity line (slope = 1). Dot size and color are as in fig. 3A. B) Histogram of best-fit slopes for optogenetic experiments (yellow) and control experiments (black) in which identical illumination parameters were used. Each line corresponds to one imaging session. C,D) Analogous to A), B) for VIP-ChrimsonR experiments, with optogenetic experiments represented in red, and control experiments in black.

Figure S14. Measured baseline activity in calcium imaging and optogenetic experiments matches activity measured in only-calcium imaging experiments. A) Scatter plot of event rate, normalized to mean, for synapsin-GCaMP6s responses in VIP silencing experiments, with the optogenetic stimulation light off, vs. transgenic GCaMP6s responses of pyramidal cells in non-optogenetic experiments, for the analogous stimuli. Dot size and color are as in fig. 3A. B) Same as A), but for responses in VIP activation, rather than silencing, experiments. Error bars represent bootstrap SEM equivalent.

Figure S15. Extracellular electrophysiology confirms VIP silencing does not affect contrast dependence of surround suppression. A) Response of regular spiking (RS) units recorded using electrophysiology to drifting gratings of varying size, at 5% contrast, in the non-locomoting condition. B) Same as A, but at 80% contrast. C) Surround modulation index is plotted as a function of contrast, in the light on and light off case. D) Change in SMI between 6% and 100% contrast is plotted, for the light on and light off cases. Each line represents the average of units recorded over one experiment. E-H) Same as A-D), but for fast-spiking (FS) units. I-P) Same as A-

H), but for the locomoting condition. The light on and light off conditions are not significantly different in D), H), L), or P), p > 0.05. Error bars represent bootstrap SEM equivalent.

Figure S16. Linear firing rate transformations do not explain enhancement of contrast dependence of surround suppression. A,B) Fig. 5C,K are reproduced here for clarity. C) As in A), surround modulation index is plotted as a function of contrast, for the VIP silencing data. In black is the light off condition. In red is plotted, rather than the true light on condition, the prediction of a linear fit to the light on condition, based on the light off condition. D) Same as C), for the VIP silencing case. Error bars represent bootstrap SEM equivalent.

Figure S17. Positive PC-VIP feedback loop at low contrast is enhanced by intermediate levels of VIP activation, underlying asymmetric residual effects of VIP activation. A) Simulated response of VIP cells to small excitatory perturbations to PCs, as a function of contrast, at 22° size. Black curve corresponds to non-optogenetic condition. Yellow curve corresponds to simulated finite inhibitory current injection to VIP cells, along with empirically measured VIP silencing-dependent perturbation to L4 PCs. Red curve corresponds to simulated finite excitatory current injection to VIP cells, along with empirically measured VIP activation-dependent perturbation to L4 PCs. Current injection magnitudes are chosen to maximize average magnitude of residual effects of current injection. B) Same as A), but for PC responses

to small excitatory perturbations to VIP cells. C) Slope and average magnitude of residual of best fit line between baseline activity level and effect of optogenetic perturbation on PCs, for simulated finite inhibitory current injections to VIP cells of varying magnitude, along with (fixed) empirically measured VIP silencing-dependent perturbations to L4 PCs. D) Same as C), but for simulated finite excitatory current injections, along with (fixed) empirically measured VIP activation-dependent perturbations to L4 PCs. E,F) Same as C), D), but after deleting modeled PC→VIP weights. G,H) Same as C), D), but after deleting modeled PC→SST weights. I,J) Same as A), B), but with current injection magnitudes corresponding to the maximal injection magnitude plotted in C), D). Error bars represent 16th to 84th percentile of model fits.

Figure S18. Example fields of view, and deconvolution analysis controls. A) An example imaging plane of a Camk2a-tTA; tetO-GCaMP6s animal, used for recording L2/3 PCs. Computed by averaging motion corrected frames across an experiment. B-D) Same as A), for PV-Cre; TITL2-GCaMP6s, SST-Cre; TITL2-GCaMP6s, and VIP-Cre; TITL2-GCaMP6s, respectively. E) Example

fluorescence (ΔF/F) trace with deconvolved event rate, from a L2/3 PC. Reproduced from fig. 1C. F) In a subset of control experiments, a longer inter-stimulus interval was used, so that evoked calcium transients did not overlap between successive trials. Orientation tuning in nine neurons with reliably estimated ΔF/F tuning curves (Pearson's *r* > 0.5 between halves of the data, see Methods) is plotted, as measured using ΔF/F and deconvolved event rate. Values are normalized for each to lie between 0 and 1. Error bars represent bootstrap SEM equivalents. G) Cumulative distribution of Pearson's *r* between ΔF/F and deconvolved tuning curves for two experiments (analyzing only neurons with reliably estimated ΔF/F tuning curves, n = 488/1131, 466/1060, respectively).

Methods

Experimental model details

All experiments were performed on mice between 1.5 to 14 months of age. CaMKII-tTA mice
(RRID:IMSR_JAX:003010) crossed to tetO-GCaMP6s mice (RRID:IMSR_JAX:024742) were used
when imaging L2/3 pyramidal cells. Both lines had been outcrossed to the ICR line (Charles
River) for several generations. These mice were on a mixed background between outcrossed
tetO-GCaMP and camk2-tTA on the C57/B6 background. For L4 PC experiments (resp. L2/3 SST,
L2/3 VIP, and L2/3 PV experiments), Scnn1a-Tg3-Cre (resp. Sst-IRES-Cre, Vip-IRES-Cre, and Pv-
IRES-Cre) mice were crossed to Ai162(TIT2L-GC6s-ICL-tTA2)-D mice (RRID:IMSR_JAX:031562).
For VIP optogenetic and calcium imaging experiments, Vip-IRES-Cre or Vip-IRES-Cre crossed to
Sst-IRES-Flp were used. For optogenetic and electrophysiology experiments, Vip-IRES-Cre or Sst-
IRES-Cre animals were used. Both female and male animals were used, and maintained on a
12:12 reversed light:dark cycle. All procedures were approved by the Animal Care and Use
Committee of UC Berkeley.

Preparation for *in vivo* two photon imaging

Headplate attachment, habituation to running on a circular treadmill, and cranial window
installation were performed as described previously (Lyall et al. 2020). Briefly, anesthesia was
induced with 5% isoflurane and maintained at 1-3% during surgery. Respiratory rate and
response to toe/tail pinching was monitored throughout surgery to ensure adequate anesthetic
depth. 0.05 mg/kg of buprenorphine was administered subcutaneously for post-operative
analgesia, and 2 mg/kg of dexamethasone as an anti-inflammatory. The scalp was disinfected
with 70% alcohol and 5% iodine. The skin and fascia above the sensory cortices were removed
and Vetbond (3M) was applied to the skull surface and wound margins. A custom titanium
headplate was fixed to the skull with dental cement (Metabond). A cranial window was
installed to provide for optical access to the cortex. A biopsy punch was used to create a 3.5mm
diameter craniotomy over the left primary visual cortex. A window plug consisting of two 3 mm
diameter coverslips glued to the bottom of a single 5 mm diameter coverslip using Norland
Optical Adhesive #71 was placed over the craniotomy and sealed permanently using dental
cement (Orthojet or Metabond). The dental cement was coated in a layer of black oxide to
mitigate light leakage during subsequent experiments. Mice were provided at least two days to
recover.
For VIP silencing experiments, neonatal Vip-IRES-Cre; Sst-IRES-Flp (P4–6) were briefly
cryo-anesthetized and placed in a head mold. Transcranial injection of ~45nl of undiluted AAV9-
CAG-DIO-eNpHR3.0-mRuby3 (UPenn Vector Core) was performed using a Drummond Nanoject
injector at three locations in left V1 using a glass pipette beveled to fine tip (~30–60μm). With
respect to the lambda suture coordinates for V1 were 0.0 mm AP, 2.2 mm L and injection was
as superficial as possible under the skull.
For VIP activation experiments, Vip-IRES-Cre mice were injected with AAV9-syn-
GCaMP6s (UPenn Vector Core) and rAAV9-syn-DIO-ChrimsonR-tdT (UNC Vector Core) virus in

left V1. For VIP silencing experiments, Vip-IRES-Cre; Sst-IRES-Flp mice were injected with AAV9-
syn-GCaMP6s (UPenn Vector Core) virus in left V1. Briefly, they were anesthetized and
administered buprenorphine as described above. A dental drill (Foredom) was used to create a
small burr hole 2.75 mm lateral to bregma. Then a WPI UltraMicroPump3 injector was used to
inject 300-400 nL of the virus at a rate of 50 nL/min. Post-injection, the needle was left in the
brain for 5 minutes to allow the viral solution to absorb into the tissue. Injected mice were
provided 2-3 weeks with intermittent head-fixation over the circular treadmill to allow the
infected neurons to ramp up expression of GCaMP6s.
708
709 **Visual stimulus presentation, *in vivo* imaging, and pupil tracking**
710
For visual stimulus presentation, the monitor was placed 13-15 cm from the eye. Animals were
habituated to visual stimulation on the setup for at least two sessions prior to imaging. Before
and/or after each experiment, receptive fields were mapped using 10° drifting grating patches.
These patches had spatial frequency of 0.08 cycles per degree, and a temporal frequency of 1
Hz, with direction cycling through 0-360° over the course of 1.5 seconds. They appeared at
randomly interleaved locations tiling a 40 x 40 visual degree grid, sampled at 5° intervals, with
1.5 second inter-stimulus intervals. In subsequent size-contrast experiments, the visual stimulus
consisted of square wave drifting gratings, with directions tiling 0-360 degrees at 45° intervals,
with a spatial frequency of 0.08 cycles per degree, and a temporal frequency of 1 Hz (calcium
imaging experiments without optogenetics) or 2 Hz (calcium imaging and optogenetic
experiments). Visual stimulus presentation lasted one second, followed by a one second inter-
stimulus interval. Patch configurations, orientations, and sizes were pseudorandomly
interleaved, and stimuli were generated and presented using the Psychophysics Toolbox
(Brainard, 1997). Each distinct visual stimulus was displayed for 5-10 repetitions.
Mice were head-fixed on a freely spinning running wheel under a Nixon 16x-
magnification water immersion objective and imaged with a two-photon resonant scanning
microscope (Neurolabware) within a light tight box. The imaging FOV was 430 by 670 um, with
four planes spaced 37.5 μm apart imaged sequentially using an electrotunable lens (Optotune),
sampling each plane at an effective frame rate of 7.72 Hz. For L2/3 imaging, imaging depth was
100 – 300 μm, and for L4 imaging, depth was 350 – 500 μm deep. Electrical tape was applied
between the objective and the mouse's headplate to block monitor light from entering the
microscope.
Locomotion was monitored using a rotary encoder, with trials where mean absolute run
velocity > 1 cm/sec classified as "locomoting" and < 1 cm/sec classified as "non-locomoting".
Eye movements were imaged using a Basler Ace aCA1300-200um camera, with a hot mirror
(Edmund Optics) placed between the eye and the monitor reflecting infrared light for eye
imaging while transmitting visible light for visual stimulation. Infrared illumination was provided
by the two photon imaging laser, transmitted through the pupils, as well as a panel of 850nm
LEDs (CMVision). Pupil location and diameter were tracked using custom MATLAB code.
740
741 **Imaging and optogenetic stimulation**
742

Optogenetic stimulation through the objective was performed with a 617 nm LED (Thorlabs),
filtered through a 632/22 nm single-band bandpass filter (Semrock), at an amplitude through
the objective of either 6 mW (VIP silencing experiments) or 1.5 mW (VIP activation
experiments). Electrical tape between the mouse's head and the objective served to mitigate
direct visual stimulation by the optogenetic light. The PMT was not gated, but protected by a
strict shortpass filter. Optogenetic illumination began 0.25 seconds prior to visual stimulus
delivery, and ended 0.25 seconds after. Small square wave optogenetic artifacts visible on the
PMT were subtracted in post-processing.
751
752 **Calcium imaging analysis**
753
754 Motion correction and ROI segmentation was performed using Suite2p (Pachitariu et al. 2017).
755 Neuropil subtraction was applied as described in (Lyall et al., 2020). ΔF/F traces were
756 calculated as

$$\Delta F/F = \frac{F(t) - F_0}{F_0}$$

with baseline F_0 computed over a sliding 20th percentile filter of width 3000 frames. Because
the inter-stimulus interval was reduced in V1 recordings to permit more stimuli to be displayed,
calcium transients overlapped between successive trials. Therefore, we deconvolved calcium
traces for this data using OASIS with L1 sparsity penalty (Friedrich et. al., 2017), using ΔF/F
traces as input.
To confirm that the deconvolution procedure did not distort tuning curve
measurements, we performed two experiments with longer inter-stimulus intervals (3 seconds
rather than 1 second), varying only stimulus direction, at fixed 15° size and 100% contrast, for
20-30 trials per condition. Because evoked calcium transients did not overlap between
successive trials in this condition, tuning curves computed using ΔF/F and deconvolved event
rate should agree quantitatively (Fig. S18f). To restrict our analysis to neurons for which our
estimate of the tuning curve with ΔF/F was robust (e.g. neurons that were visually responsive
and orientation-tuned) we randomly split trials into two halves, computed tuning curves for
each half, and computed Pearson's correlation coefficients between the two independent
tuning curve estimates. We determined that a neuron's tuning curve measurement was robust
if the two estimates were correlated with r > 0.5 (n = 488/1131, 466/1060 for the two
experiments). For these neurons, we then computed tuning curves based on all trials, using
ΔF/F and deconvolved event rates. Indeed, we found that for both mice, ΔF/F and deconvolved
estimates of tuning curves were correlated with r > 0.9 in ~80% of neurons.
777
778 **Retinotopic map estimation**
779
Responses to receptive field mapping stimuli were fit using 2D gaussians. The underlying
retinotopic map was estimated using linear regression of cell centers (in microns of cortical
space) vs. receptive field centers (in degrees of visual space). For subsequent analyses, neurons
were separated based on either their receptive field center relative to the center of the size-
contrast stimulus, or based on their location on the estimated retinotopic map, relative to the
center of the stimulus representation, as indicated in the text. For each FOV, the retinotopic

map orientation relative to the rostral-caudal and medial-lateral axes, and cortical
magnification, was confirmed to be consistent with V1.
788
789   **Simultaneous imaging of VIP and SST activity using Cre-Flp**
790
We used VIP-Cre SST-Flp mice, injected with GCaMP6s expressed in all neurons. SST cells
expressed cytosolic tdTomato in a Flp-dependent manner, while VIP cells expressed Cre-
dependent mRuby3 fused to eNpHR3.0. Using calcium imaging, we identified SST cells using
their bright, cytosolic red signal, compared with the dimmer, membrane bound mRuby3 in VIP
cells; they could be distinguished both by membrane localization and brightness of the red
fluorophore (fig. S8).
797
798   **Recurrent network model**
799
For a detailed expanation, see Supplementary Note. Briefly, we modeled cortical space using
two spatial domains. The first represented neurons within ten visual degrees of retinotopic
space of the stimulus representation's center; the second, neurons beyond 10 degrees. Activity
in layer 4 pyramidal cells (L4 PCs) in each spatial domain was treated as input to the four
recurrently connected layer 2/3 (L2/3) populations in each pixel. The full weight matrix
describing synaptic connections between the four L2/3 cell types in each of the two spatial
domains was modeled as the product of a cell type-dependent term, describing the connection
strength of cell type I onto cell type j, multiplied by a term describing the integration across
space, and a term describing integration across orientations, of the postsynaptic population j.
Thus, the full 8x8 matrix of recurrent synaptic connections was described by a 4x4 matrix, plus a
4-dimensional vector. A similar procedure was used to generate the full 2x8 matrix of
feedforward synaptic connections from L4 PCs. A four-dimensional vector gave the bias current
for each L2/3 population. The linear combination representing synaptic input currents was then
passed through a distinct static nonlinearity for each cell type. The shape of this nonlinearity
was determined by the intrinsic variability in a given cell type's input current, which was fit for
each cell type.
816   Because r appears on both the left and right sides of equation (1), we say that solutions
for r must in general be "self-consistent." For each cell population and each stimulus condition,
a stimulus-dependent residual current parameter was introduced, added to the synaptic input
and bias currents, so that perfect self-consistency was not required at each step of the
optimization. However, squared error penalties on these residual currents ensured that the
final network parameters achieved nearly perfect self-consistency. The model fits were
randomly initialized, and optimized using L-BFGS. The cost function incorporated both the
calcium imaging data for all cell types, and the optogenetic silencing data (combining both
calcium imaging and electrophysiology results). The optogenetic data were fit by linearizing the
model around the firing rates in the unperturbed condition. Several synaptic weights (L4
PC→SST, SST→SST, and VIP→PC) were constrained to be 0, and the PC→PC weight was
constrained to be large, in the sense that the product $w_{PC\text{->}PC}\,\varphi_{PC} > 1$, in units where the synaptic
leak current is 1, for every stimulus condition (with φ_{PC} as defined below).

For steady state solutions to equation (1), the change in firing rate r expected from a
small change in input current I can be computed as the product
831 $$\Delta r \approx \varphi \Delta I, (2)$$
832   where φ is the slope of the firing rate nonlinearity around the steady state solution $\boldsymbol{r}$. Because I
833   is itself a function of $\boldsymbol{r}$, we were able to simulate the response of a cell population j to small
834   current injections to population j by computing a "response matrix" R as in (Del Molino et al.,
835   2017):
836                              $$\Delta r = (1 - \Phi W)^{-1} \Phi \Delta h = R \Delta h. (3)$$
This amounts to linearizing $\boldsymbol{r}$ about a steady state solution to equation (1). Here, $\boldsymbol{\Delta h}$ is a vector
of optogenetically induced currents, and Φ is a diagonal matrix whose entries are the values of
φ for each cell type. The matrix R yields the theoretical prediction for the effect of small current
injections to a given cell population j, on any cell population i. This matrix changes as a function
of stimulus via changes in $\boldsymbol{r}$, and thus φ for each cell type.
We leveraged these recurrent network model fits to predict the effects of manipulations
on network activity, some experimentally realizable with current technology, and some not.
First, we simulated the deletion of certain synaptic connections. For these simulations, we
allowed the network to evolve to a new steady state according to equation (1), after setting
certain elements of the 4x4 L2/3 synaptic weight matrix to 0, with all other parameters held
constant. Second, we simulated the injection of inhibitory (negative) or excitatory (positive)
current to specific cell types, modeled as a stimulus-dependent DC offset to the synaptic input
current for that cell type. Again, we allowed the network to evolve to a new steady state
according to equation (1). In both of these cases, we computed both the perturbed steady state
firing rates $\boldsymbol{r}$, as well as the perturbed response matrix R, resulting from the perturbed values
for Φ and W.
For simulations of optogenetic silencing and activation of VIP cells, we tuned the
magnitude of current injection for each model fit based on the computed response matrix. In
particular, for both silencing and activation simulations, we chose current magnitude to
maximize the dynamic range of the term corresponding to PC cooperation or competition
across space ($R_{near\ PC,\ far\ PC}$), defined as the absolute difference between the maximum and
minimum values of $R_{near\ PC,\ far\ PC}$ across stimuli.
859
860   **Quantification and statistical analysis**
861
Statistically significant differences between conditions were determined using standard
nonparametric tests in the SciPy library, including the Wilcoxon signed-rank test and Mann-
Whitney U test. Analyses were performed on each ROI's deconvolved event rate for each trial.
A single trial's response was calculated as the average deconvolved event rate during the entire
1 second of stimulation. 95% confidence intervals and SEM equivalents (68% confidence
intervals) were generated via bootstrap. For validation of the deconvolution procedure, trials
were split randomly into two halves, and tuning curves were computed on each half of trials.
Neurons whose tuning curves computed on both halves of the data using ΔF/F agreed with
Pearson's $r > 0.5$ were retained. For these neurons, tuning curves were computed across all trials
using both ΔF/F and deconvolved event rate (fig. S18f,g).
872

Data Availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Contributions

D.P.M., J.V., A.P., K.D.M., and H.A. conceived the study. D.P.M. performed the calcium imaging experiments. J.V. performed the extracellular electrophysiology experiments. D.P.M. designed and built the recurrent network model, and designed and carried out *in silico* experiments. D.P.M. and H.A. wrote the paper, with input from all other authors.

Acknowledgements

The authors acknowledge the GENIE Project, Janelia Farm Research Campus, and the Howard Hughes Medical Institute for the GCaMP6 viruses. Thanks to the members of the Adesnik Lab, particularly Hayley Bounds, Mora Ogando, and Hyeyoung Shin for helpful comments. Thanks also to Charles G. Frye, Sang Min Han, and Benjamin E. Smith. D.P.M. was supported by an NSF Graduate Research Fellowship. A.P. would like to acknowledge the support of the Swartz Foundation Fellowship for Theory in Neuroscience 2019-4 and 2020-6. H.A. is a New York Stem Cell Foundation-Robertson Investigator. This work was supported by The New York Stem Cell Foundation. This work was supported by NEI grant R01EY023756-01 and U19NS97613.

BIBLIOGRAPHY

Abs, Elisabeth, Rogier B. Poorthuis, Daniella Apelblat, Karzan Muhammad, M. Belen Pardi, Leona Enke, Dahlia Kushinsky, et al. 2018. "Learning-related plasticity in dendrite-targeting layer 1 interneurons." *Neuron* (Elsevier) 100: 684–699.

Adesnik, Hillel, William Bruns, Hiroki Taniguchi, Z. Josh Huang, and Massimo Scanziani. 2012. "A neural circuit for spatial summation in visual cortex." *Nature* (Nature Publishing Group) 490: 226–231.

Ahmadian, Yashar, Daniel B. Rubin, and Kenneth D. Miller. 2013. "Analysis of the stabilized supralinear network." *Neural computation* (MIT Press) 25: 1994–2037.

Anderson, Jeffrey S., Ilan Lampl, Deda C. Gillespie, and David Ferster. 2000. "The contribution of noise to contrast invariance of orientation tuning in cat visual cortex." *Science* (American Association for the Advancement of Science) 290: 1968–1972.

Angelucci, Alessandra, Maryam Bijanzadeh, Lauri Nurminen, Frederick Federer, Sam Merlin, and Paul C. Bressloff. 2017. "Circuits and mechanisms for surround modulation in visual cortex." *Annual review of neuroscience* (Annual Reviews) 40: 425–451.

Atallah, Bassam V., William Bruns, Matteo Carandini, and Massimo Scanziani. 2012. "Parvalbumin-expressing interneurons linearly transform cortical responses to visual stimuli." *Neuron* (Elsevier) 73: 159–170.

Cavanaugh, James R., Wyeth Bair, and J. Anthony Movshon. 2002. "Nature and interaction of signals from the receptive field center and surround in macaque V1 neurons." *Journal of neurophysiology* (American Physiological Society Bethesda, MD) 88: 2530–2546.

Chen, Gang, Yang Dan, and Chao-Yi Li. 2005. "Stimulation of non-classical receptive field enhances orientation selectivity in the cat." *The Journal of physiology* (Wiley Online Library) 564: 233–243.

Coen-Cagli, Ruben, Adam Kohn, and Odelia Schwartz. 2015. "Flexible gating of contextual influences in natural vision." *Nature neuroscience* (Nature Publishing Group) 18: 1648–1655.

Del Molino, Luis Carlos Garcia, Guangyu Robert Yang, Jorge F. Mejias, and Xiao-Jing Wang. 2017. "Paradoxical response reversal of top-down modulation in cortical circuits with three interneuron types." *Elife* (eLife Sciences Publications Limited) 6: e29742.

Dipoppa, Mario, Adam Ranson, Michael Krumin, Marius Pachitariu, Matteo Carandini, and Kenneth D. Harris. 2018. "Vision and locomotion shape the interactions between neuron types in mouse visual cortex." *Neuron* (Elsevier) 98: 602–615.

Douglas, Rodney J., Christof Koch, Misha Mahowald, K. A. Martin, and Humbert H. Suarez. 1995. "Recurrent excitation in neocortical circuits." *Science* (American Association for the Advancement of Science) 269: 981–985.

Dudai, Amir, Nadav Yayon, Vitaly Lerner, Gen-ichi Tasaka, Yair Deitcher, Karin Gorfine, Naomi Niederhoffer, Adi Mizrahi, Hermona Soreq, and Michael London. 2020. "Barrel cortex VIP/ChAT interneurons suppress sensory responses in vivo." *PLoS biology* (Public Library of Science San Francisco, CA USA) 18: e3000613.

Fu, Yu, Jason M. Tucciarone, J. Sebastian Espinosa, Nengyin Sheng, Daniel P. Darcy, Roger A. Nicoll, Z. Josh Huang, and Michael P. Stryker. 2014. "A cortical circuit for gain control by behavioral state." *Cell* (Elsevier) 156: 1139–1152.

Hakim, Richard, Kiarash Shamardani, and Hillel Adesnik. 2018. "A neural circuit for gamma-band coherence across the retinotopic map in mouse visual cortex." *Elife* (eLife Sciences Publications Limited) 7: e28569.

Hawken, Michael J., Robert M. Shapley, Michael P. Sceniak, Dario L. Ringach, and Elizabeth N. Johnson. 2001. "Contrast gain, area summation and temporal tuning in primate visual cortex." In *Vision and attention*, 41–62. Springer.

He, Miao, Jason Tucciarone, SooHyun Lee, Maximiliano José Nigro, Yongsoo Kim, Jesse Maurica Levine, Sean Michael Kelly, et al. 2016. "Strategies and tools for combinatorial targeting of GABAergic neurons in mouse cerebral cortex." *Neuron* (Elsevier) 91: 1228–1243.

Kamigaki, Tsukasa, and Yang Dan. 2017. "Delay activity of specific prefrontal interneuron subtypes modulates memory-guided behavior." *Nature neuroscience* (Nature Publishing Group) 20: 854.

Kapadia, Mitesh K., Gerald Westheimer, and Charles D. Gilbert. 1999. "Dynamics of spatial summation in primary visual cortex of alert monkeys." *Proceedings of the National Academy of Sciences* (National Acad Sciences) 96: 12073–12078.

Kapfer, Christoph, Lindsey L. Glickfeld, Bassam V. Atallah, and Massimo Scanziani. 2007. "Supralinear increase of recurrent inhibition during sparse activity in the somatosensory cortex." *Nature neuroscience* (Nature Publishing Group) 10: 743–753.

Karnani, Mahesh M., Jesse Jackson, Inbal Ayzenshtat, Jason Tucciarone, Kasra Manoocheri,
William G. Snider, and Rafael Yuste. 2016. "Cooperative subnetworks of molecularly
similar interneurons in mouse neocortex." *Neuron* (Elsevier) 90: 86–100.
Kato, Hiroyuki K., Samuel K. Asinof, and Jeffry S. Isaacson. 2017. "Network-level control of
frequency tuning in auditory cortex." *Neuron* (Elsevier) 95: 412–423.
Keller, Andreas J., Morgane M. Roth, Matthew Caudill, Mario Dipoppa, Kenneth D. Miller, and
Massimo Scanziani. 2020. "A disinhibitory circuit for contextual modulation in primary
visual cortex." *bioRxiv* (Cold Spring Harbor Laboratory).
Kuchibhotla, Kishore V., Jonathan V. Gill, Grace W. Lindsay, Eleni S. Papadoyannis, Rachel E.
Field, Tom A. Hindmarsh Sten, Kenneth D. Miller, and Robert C. Froemke. 2017. "Parallel
processing by cortical inhibition enables context-dependent behavior." *Nature*
neuroscience (Nature Publishing Group) 20: 62–71.
Lee, Seung-Hee, Alex C. Kwan, and Yang Dan. 2014. "Interneuron subtypes and orientation
tuning." *Nature* (Nature Publishing Group) 508: E1–E2.
Lee, Seung-Hee, Alex C. Kwan, Siyu Zhang, Victoria Phoumthipphavong, John G. Flannery, Sotiris
C. Masmanidis, Hiroki Taniguchi, et al. 2012. "Activation of specific interneurons
improves V1 feature selectivity and visual perception." *Nature* (Nature Publishing
Group) 488: 379–383.
Lee, Soohyun, Illya Kruglikov, Z. Josh Huang, Gord Fishell, and Bernardo Rudy. 2013. "A
disinhibitory circuit mediates motor integration in the somatosensory cortex." *Nature*
neuroscience (Nature Publishing Group) 16: 1662–1670.
Letzkus, Johannes J., Steffen B. E. Wolff, Elisabeth M. M. Meyer, Philip Tovote, Julien Courtin,
Cyril Herry, and Andreas Lüthi. 2011. "A disinhibitory microcircuit for associative fear
learning in the auditory cortex." *Nature* (Nature Publishing Group) 480: 331–335.
Levitt, Jonathan B., and Jennifer S. Lund. 1997. "Contrast dependence of contextual effects in
primate visual cortex." *Nature* (Nature Publishing Group) 387: 73–76.
Li, Ling-yun, Xiaorui R. Xiong, Leena A. Ibrahim, Wei Yuan, Huizhong W. Tao, and Li I. Zhang.
2015. "Differential receptive field properties of parvalbumin and somatostatin inhibitory
neurons in mouse auditory cortex." *Cerebral cortex* (Oxford University Press) 25: 1782–
1791.
Li, Ling-yun, Ya-tang Li, Mu Zhou, Huizhong W. Tao, and Li I. Zhang. 2013. "Intracortical
multiplication of thalamocortical signals in mouse auditory cortex." *Nature neuroscience*
(Nature Publishing Group) 16: 1179–1181.
Li, Ya-tang, Leena A. Ibrahim, Bao-hua Liu, Li I. Zhang, and Huizhong Whit Tao. 2013. "Linear
transformation of thalamocortical input by intracortical excitation." *Nature neuroscience*
(Nature Publishing Group) 16: 1324–1330.
Lien, Anthony D., and Massimo Scanziani. 2013. "Tuned thalamic excitation is amplified by
visual cortical circuits." *Nature neuroscience* (Nature Publishing Group) 16: 1315–1323.
Litwin-Kumar, Ashok, Robert Rosenbaum, and Brent Doiron. 2016. "Inhibitory stabilization and
visual coding in cortical circuits with multiple interneuron subtypes." *Journal of*
neurophysiology (American Physiological Society Bethesda, MD) 115: 1399–1409.
Mesik, Lukas, Wen-pei Ma, Ling-yun Li, Leena A. Ibrahim, Z. J. Huang, Li I. Zhang, and Huizhong
W. Tao. 2015. "Functional response properties of VIP-expressing inhibitory neurons in
mouse visual and auditory cortex." *Frontiers in neural circuits* (Frontiers) 9: 22.

Miller, Kenneth D., and Todd W. Troyer. 2002. "Neural noise can explain expansive, power-law nonlinearities in neural response functions." *Journal of neurophysiology* (American Physiological Society Bethesda, MD) 87: 653–659.

Millman, Daniel J., Gabriel Koch Ocker, Shiella Caldejon, Josh D. Larkin, Eric Kenji Lee, Jennifer Luviano, Chelsea Nayan, et al. 2019. "VIP interneurons selectively enhance weak but behaviorally-relevant stimuli." *bioRxiv* (Cold Spring Harbor Laboratory) 858001.

Mineault, Patrick J., Elaine Tring, Joshua T. Trachtenberg, and Dario L. Ringach. 2016. "Enhanced spatial resolution during locomotion and heightened attention in mouse primary visual cortex." *Journal of Neuroscience* (Soc Neuroscience) 36: 6382–6392.

Nauhaus, Ian, Laura Busse, Matteo Carandini, and Dario L. Ringach. 2009. "Stimulus contrast modulates functional connectivity in visual cortex." *Nature neuroscience* (Nature Publishing Group) 12: 70.

Nienborg, Hendrikje, Andrea Hasenstaub, Ian Nauhaus, Hiroki Taniguchi, Z. Josh Huang, and Edward M. Callaway. 2013. "Contrast dependence and differential contributions from somatostatin-and parvalbumin-expressing neurons to spatial integration in mouse V1." *Journal of Neuroscience* (Soc Neuroscience) 33: 11145–11154.

Okamoto, Masahiro, Tomoyuki Naito, Osamu Sadakane, Hironobu Osaki, and Hiromichi Sato. 2009. "Surround suppression sharpens orientation tuning in the cat primary visual cortex." *European Journal of Neuroscience* (Wiley Online Library) 29: 1035–1046.

Orban, G. A., H. Kato, and P. O. Bishop. 1979. "End-zone region in receptive fields of hypercomplex and other striate neurons in the cat." *Journal of Neurophysiology* (American Physiological Society Bethesda, MD) 42: 818–832.

Ozeki, Hirofumi, Ian M. Finn, Evan S. Schaffer, Kenneth D. Miller, and David Ferster. 2009. "Inhibitory stabilization of the cortical network underlies visual surround suppression." *Neuron* (Elsevier) 62: 578–592.

Pfeffer, Carsten K., Mingshan Xue, Miao He, Z. Josh Huang, and Massimo Scanziani. 2013. "Inhibition of inhibition in visual cortex: the logic of connections between molecularly distinct interneurons." *Nature neuroscience* (Nature Publishing Group) 16: 1068–1076.

Phillips, Elizabeth A. K., and Andrea R. Hasenstaub. 2016. "Asymmetric effects of activating and inactivating cortical interneurons." *Elife* (eLife Sciences Publications Limited) 5: e18383.

Pi, Hyun-Jae, Balázs Hangya, Duda Kvitsiani, Joshua I. Sanders, Z. Josh Huang, and Adam Kepecs. 2013. "Cortical interneurons that specialize in disinhibitory control." *Nature* (Nature Publishing Group) 503: 521–524.

Polat, Uri, Keiko Mizobe, Mark W. Pettet, Takuji Kasamatsu, and Anthony M. Norcia. 1998. "Collinear stimuli regulate visual responses depending on cell's contrast threshold." *Nature* (Nature Publishing Group) 391: 580–584.

Reinhold, Kimberly, Anthony D. Lien, and Massimo Scanziani. 2015. "Distinct recurrent versus afferent dynamics in cortical visual processing." *Nature neuroscience* (Nature Publishing Group) 18: 1789–1797.

Rubin, Daniel B., Stephen D. Van Hooser, and Kenneth D. Miller. 2015. "The stabilized supralinear network: a unifying circuit motif underlying multi-input integration in sensory cortex." *Neuron* (Elsevier) 85: 402–417.

Rudy, Bernardo, Gordon Fishell, SooHyun Lee, and Jens Hjerling-Leffler. 2011. "Three groups of
interneurons account for nearly 100% of neocortical GABAergic neurons."
Developmental neurobiology (Wiley Online Library) 71: 45–61.
Sanzeni, Alessandro, Bradley Akitake, Hannah C. Goldbach, Caitlin E. Leedy, Nicolas Brunel, and
Mark H. Histed. 2020. "Inhibition stabilization is a widespread property of cortical
networks." *Elife* (eLife Sciences Publications Limited) 9: e54875.
Sato, Tatsuo K., Michael Häusser, and Matteo Carandini. 2014. "Distal connectivity causes
summation and division across mouse visual cortex." *Nature neuroscience* (Nature
Publishing Group) 17: 30–32.
Sceniak, Michael P., Dario L. Ringach, Michael J. Hawken, and Robert Shapley. 1999. "Contrast's
effect on spatial summation by macaque V1 neurons." *Nature neuroscience* (Nature
Publishing Group) 2: 733–739.
Schwabe, Lars, Jennifer M. Ichida, S. Shushruth, Pradeep Mangapathy, and Alessandra
Angelucci. 2010. "Contrast-dependence of surround suppression in Macaque V1:
experimental testing of a recurrent network model." *Neuroimage* (Elsevier) 52: 777–
792.
Sengpiel, Frank, Arjune Sen, and Colin Blakemore. 1997. "Characteristics of surround inhibition
in cat area 17." *Experimental brain research* (Springer) 116: 216–228.
Tasic, Bosiljka, Zizhen Yao, Lucas T. Graybuck, Kimberly A. Smith, Thuc Nghi Nguyen, Darren
Bertagnolli, Jeff Goldy, et al. 2018. "Shared and distinct transcriptomic cell types across
neocortical areas." *Nature* (Nature Publishing Group) 563: 72–78.
Tosches, Maria Antonietta, Tracy M. Yamawaki, Robert K. Naumann, Ariel A. Jacobi, Georgi
Tushev, and Gilles Laurent. 2018. "Evolution of pallium, hippocampus, and cortical cell
types revealed by single-cell transcriptomics in reptiles." *Science* (American Association
for the Advancement of Science) 360: 881–888.
Toth, Louis J., S. Chenchal Rao, Dae-Shik Kim, David Somers, and Mriganka Sur. 1996.
"Subthreshold facilitation and suppression in primary visual cortex revealed by intrinsic
signal imaging." *Proceedings of the National Academy of Sciences* (National Acad
Sciences) 93: 9869–9874.
Tsodyks, Misha V., William E. Skaggs, Terrence J. Sejnowski, and Bruce L. McNaughton. 1997.
"Paradoxical effects of external modulation of inhibitory interneurons." *Journal of
neuroscience* (Soc Neuroscience) 17: 4382–4388.
Vaiceliunaite, Agne, Sinem Erisken, Florian Franzen, Steffen Katzner, and Laura Busse. 2013.
"Spatial integration in mouse primary visual cortex." *Journal of neurophysiology*
(American Physiological Society Bethesda, MD) 110: 964–972.
Wang, Xiao-Jing, and Guangyu Robert Yang. 2018. "A disinhibitory circuit motif and flexible
information routing in the brain." *Current opinion in neurobiology* (Elsevier) 49: 75–83.
Wilson, Nathan R., Caroline A. Runyan, Forea L. Wang, and Mriganka Sur. 2012. "Division and
subtraction by distinct cortical inhibitory networks in vivo." *Nature* (Nature Publishing
Group) 488: 343–348.
Xing, Dajun, Robert M. Shapley, Michael J. Hawken, and Dario L. Ringach. 2005. "Effect of
stimulus size on the dynamics of orientation selectivity in Macaque V1." *Journal of
Neurophysiology* (American Physiological Society) 94: 799–812.

Yang, Guangyu Robert, John D. Murray, and Xiao-Jing Wang. 2016. "A dendritic disinhibitory
circuit mechanism for pathway-specific gating." *Nature communications* (Nature
Publishing Group) 7: 1–14.
Zhang, Siyu, Min Xu, Tsukasa Kamigaki, Johnny Phong Hoang Do, Wei-Cheng Chang, Sean
Jenvay, Kazunari Miyamichi, Liqun Luo, and Yang Dan. 2014. "Long-range and local
circuits for top-down modulation of visual cortex processing." *Science* (American
Association for the Advancement of Science) 345: 660–665.
1092