Running Head: Allopolyploid networks with phased sequences

Benefits and Limits of Phasing Alleles for Network Inference of Allopolyploid Complexes

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Abstract

Accurately reconstructing the reticulate histories of polyploids remains a central
challenge for understanding plant evolution. Although phylogenetic networks can provide
insights into relationships among polyploid lineages, inferring networks may be hindered by the
complexities of homology determination in polyploid taxa. We use simulations to show that
phasing alleles from allopolyploid individuals can improve inference of phylogenetic networks
under the multispecies coalescent. Phased allelic data can also improve divergence time
estimates for networks, which is helpful for evaluating allopolyploid speciation hypotheses and
proposing mechanisms of speciation. To achieve these outcomes in empirical data, we present
a novel pipeline that leverages a recently developed phasing algorithm to reliably phase alleles
from polyploids. This pipeline is especially appropriate for target enrichment data, where depth
of coverage is typically high enough to phase entire loci. We provide an empirical example in
the North American *Dryopteris* fern complex that demonstrates insights from phased data as
well as the challenges of network inference. We establish that our pipeline (PATÉ: Phased
Alleles from Target Enrichment data) is capable of recovering a high proportion of phased loci
from both diploids and polyploids. These data may improve network estimates compared to
using haplotype consensus assemblies by accurately inferring the direction of gene flow, but
statistical identifiability of phylogenetic networks poses a barrier to inferring the evolutionary
history of reticulate complexes.

Key words: Introgression; Hybridization; Phylogenetic Networks; Statistical Identifiability;
Multispecies Coalescent; Divergence Time Estimation; Polyploidy; Target Enrichment

INTRODUCTION

Polyploidy, or whole-genome duplication, occurs throughout the eukaryotic tree of life. However, its evolutionary significance is especially evident in plants, with recent estimates suggesting up to 35% of vascular plant species are of recent polyploid origin (Wood et al. 2009; Barker et al. 2016). Despite advances in genomic data generation and numerous studies investigating the role of whole-genome duplication in plant speciation and local adaptation (reviewed in Soltis et al. 2014), polyploidy remain a central challenge for the field of phylogenetics. One persistent problem when analyzing sequence data from polyploid taxa, and especially allopolyploids, is identifying the alleles and divergent homeolog copies from parental lineages. Most bioinformatic tools for processing next generation sequence data were developed with diploids, or specifically humans, in mind. These approaches often collapse variable homeolog sequences into a single consensus sequence for *de novo* assemblies or assume the organism is diploid when performing genotyping and phasing for reference-based assembly. For polyploids, this creates chimeric sequences that may interfere with phylogenetic reconstruction and obscure evidence of polyploidy and its origins. Using allelic data that more accurately capture the complex genomic histories of polyploids should enable analyses to incorporate of divergent signals from polyploid loci into phylogenomic inference, distinguish allopolyploidy from autopolyploidy, and identify parental taxa. However, few studies have examined the potential benefits of using phased versus unphased data to reconstruct polyploid histories, and there are few formal methods and little guidance for phasing alleles from polyploid taxa. Here we explore the value of using phased data to reconstruct polyploid networks, leveraging fast polyploid phasing algorithms (Xie et al. 2016) to develop a bioinformatic pipeline that can phase alleles from polyploids using target enrichment sequence data.

Previous studies have suggested phasing alleles is crucial for accurate evolutionary reconstruction of reticulate complexes, at least when sampling relatively few loci (e.g., 4 to 10; Rothfels et al. 2017; Eriksson et al. 2018). However, it remains challenging to genotype and

phase next generation sequencing data from polyploids. Methods exist to genotype consensus

loci from target enrichment data, but these have been either limited to diploids (Kates et al.

2018; Andermann et al. 2019) or used manual curation of variants with polyploids where both

parental populations are available (Eriksson et al. 2018). Otherwise, obtaining phased sequence

data for polyploids has largely depended on long-read sequencing to recover complete

haplotype sequences (e.g., Rothfels et al. 2017) or cloning PCR products (e.g., Sessa et al.

2012; Oberprieler et al. 2017).

Target enrichment (or HybSeq), where specific regions of the genome are isolated and

sequenced (Albert et al. 2007; Gnirke et al. 2009; Faircloth et al. 2012; Lemmon et al. 2012), is

an increasingly common method for collecting large-scale phylogenomic datasets, and these

data can provide insights into the evolutionary history of reticulate complexes (e.g., Crowl et al.

2017; Karimi et al. 2020) and sources of gene tree discordance (e.g., Morales-Briones et al.

2018; Stull et al. 2020). Probe kits for target enrichment have been developed in many land

plant lineages (Wolf et al. 2018; Johnson et al. 2019; Liu et al. 2019; Breinholt et al. 2021), and

there are bioinformatic pipelines available for custom probe design (e.g., Jantzen et al. 2020).

The most common approach to assemble phylogenetic datasets from target enrichment data

has been to use haplotype consensus assemblies from various pipelines (e.g. Faircloth 2016;

Johnson et al. 2016; Andermann et al. 2018; Breinholt et al. 2018). The *de novo* assembly

algorithms within these pipelines typically consider only the most frequent nucleotide sequence

and discard the alternatives (Bankevich et al. 2012; Iqbal et al. 2012; Luo et al. 2012). This

results in loci in which variable positions are collapsed to a single base call (haplotype

consensus loci), losing information related to heterozygosity. While this may be appropriate, or

at least benign, for phylogenetic analyses of diploid taxa (Kates et al. 2018), it may pose

substantial problems when attempting to investigate the evolutionary history of polyploid taxa or

reticulate lineages. Some of the before mentioned pipelines can recover the heterozygosity

information and phase sequences by mapping reads back to their haplotype consensus

sequences (Andermann et al. 2018), but this utility is, at the time of writing, limited to diploids.

While phylogenetic studies in plants usually infer strictly bifurcating trees, the

complexities of allopolyploid evolution can be represented more accurately using networks.

Simulations and empirical analyses have suggested that phylogenetic networks can recover the

reticulate histories of polyploid lineages with few loci, at least when gene tree discordance due

to incomplete lineage sorting (ILS; Hudson et al. 1983; Pamilo and Nei 1988) is low (Oberprieler

et al. 2017) using parsimony methods (Huber et al. 2006; Lott et al. 2009), or with moderate ILS

when it is explicitly modeled (Jones et al. 2013). Contemporary phylogenetic network models

and software packages jointly consider gene tree variation due to allele sampling error as

described by the multispecies coalescent (MSC; Rannala and Yang 2003) and gene flow

modeled as episodic introgression events (Solis-Lemus and Ané 2016; Wen et al. 2016; Zhang,

Ogilvie et al. 2018, Flouri et al. 2020). Depending on the complexity and goals of the research

question, these methods can search for networks with a constrained number of reticulation

events using quartet-based maximum pseudolikelihood (Solis-Lemus and Ané 2016; Wen et al.

2018) or a full-likelihood Bayesian model where the number of reticulations is a parameter (Wen

et al. 2018; Zhang et al. 2018). Also, it is possible to estimate model parameters (divergence

times, population sizes, and the fraction of introgressed genes) on a fixed species network using

a full-likelihood Bayesian model that allows efficient computation with large numbers of loci

(Flouri et al. 2020). We refer to these network models from here on as the multispecies

coalescent with introgression (MSci), consistent with Flouri et al. (2020); although, other names

have been used, such as the network multispecies coalescent (NMSC; Zhu and Degnan 2017)

and multispecies network coalescent (MSNC; Wen et al. 2016). We emphasize that using

network approaches to investigate polyploid complexes is not novel (e.g., Huber et al. 2006; Lott

et al. 2009; Jones et al. 2013), but the difficulty of collecting appropriate genomic data from

polyploids for such analyses has limited their use.

To address the issues outlined above, we have developed a pipeline, PATÉ (Phased

Alleles from Target Enrichment data), that can phase genotyping data for individuals of a known

ploidy without the need for sampling their parental lineages. PATÉ was designed with scalability

and population-level sampling in mind for target enrichment projects where deep coverage from

paired-end Illumina data allow calling of high-quality variants. In this study, we first use

simulations to explore the ability of network approaches to reconstruct the history of

allopolyploidy in the presence of ILS, and whether phasing the data affects the accuracy of the

reconstruction. We show that using phased allelic data can improve network estimation and

divergence time estimation compared to using haplotype consensus sequences, but also

highlight scenarios where phasing may not be necessary or beneficial. Next, we describe the

individual steps used by PATÉ to phase target enrichment data. For an empirical example of the

benefits of PATÉ, we compare phased and unphased (haplotype consensus) data to infer the

evolutionary history of the North American *Dryopteris* complex, a model system for reticulate

polyploid evolution (Sessa et al. 2012a; Sessa et al. 2012b), using new targeted enrichment

data. The system includes four diploid species, as well as one extinct diploid, that have formed

five allopolyploids in which there is high confidence in the parent-progeny relationships (Fig. 1),

although numerous sterile allopolyploid species have also been reported within the complex

(Montgomery and Paulton 1981). The allopolyploid species have relatively ancient origins, with

the best estimates placing hybridization events between six and 13 Ma (Sessa et al. 2012b).

PATÉ is largely successful in recovering phased haploid sequences from polyploid individuals;

although, the switch errors among these haplotypes sequences is unknown. Networks inferred

from phased data more accurately represent some relationships within the North American

Dryopteris complex than unphased strategies, but statistical identifiability problems confound all

data types.

MATERIALS & METHODS

Testing the Effects of Phasing on Network Inference through Simulation

Simulating phased and unphased sequence data for an allopolyploid — We simulated

gene trees and their nucleotide sequence data using the MSC model (Rannala and Yang 2003)

with BPP v4.4.0 (Flouri et al. 2020) under a network with five tips, such that one taxon was a

hybrid of the ancestors of two other tip taxa (Fig. 2). All simulations used the HKY85 (Hasegawa

et al 1985) model of sequence evolution with a transition-transversion rate ratio of 3 and

gamma-distributed among-site rate heterogeneity with a shape parameter of 0.6. Equilibrium

frequencies were 0.3, 0.2, 0.3, and 0.2 for nucleotides A, C, G, and T. The allopolyploid species

E was treated as two lineages (*E* sister to *B* and *F* sister to *C*) whose alleles were pooled to

form the hybrid species *E* at time τ_h. This makes species *E* a tetraploid hybrid with the parents

the ancestors of *B* and *C*. The mutation-scaled effective population size (θ) was constant

among lineages and set at 0.01. Assuming a per-generation mutation rate (μ) of 1×10^{-8} and

one year per generation yields an effective population size (N_e) of 250,000 and hybridization

age of 10 Ma (Fig. 2). We also simulated data such that θ was 0.001 (hybridization at 1 Ma) or

0.1 (hybridization at 100 Ma). Investigating such extreme values can generate general

expectations for downstream estimation under a wide range of parameters, but has some

biological salience as there is increasing evidence for reticulate evolution early in the

diversification of plant orders and families (Sun et al. 2015; Stull et al. 2020; Liu et al. 2022)

Because the distance between speciation nodes is 0.01 substitutions per site and $\theta =$

0.01 (Fig. 2), there are two coalescent units between nodes, $T = \frac{\tau}{\left(\frac{\theta}{2}\right)}$ (Yang 2006), which yields a

low probability (0.09) of gene tree discordance due to ILS (Hudson 1983). We incorporated

more ILS into the simulation by keeping the node heights fixed but increasing θ to 0.02, 0.03,

and 0.04. This increased the probability of a non-speciodentric split among all nodes to 0.25,

0.34, and 0.4, respectively. With three different starting values of θ and τ, this gave a total of 12

simulation conditions. While our simulations do not explore the limits of gene tree discordance,

they allow us to learn about some general features of increasing ILS on network inference with

different data types. We simulated 1000 gene trees and their sequences, 500 base pairs (bp) in

length, under the MSC 100 times for each of the 12 conditions. We also explored the effects of

sampling fewer genes on downstream analyses. For each replicate of 1000 gene trees and their

sequences, we randomly sampled 400, 40, and four genes without replacement.

All simulations sampled haploid data. Two haploid sequences were sampled for each

diploid species and four haploid sequences were sampled for the allopolyploid species *E,* where

two sequences came from each parental lineage. We then investigated unphased data in three

ways. First, to generate unphased genotype sequences, the simulated haploid sequences for

each species were collapsed into a single sequence in which heterozygous sites were

represented by IUPAC ambiguity codes (genotype). The allopolyploid species was not restricted

to only biallelic sites. Second, we generated haploid consensus sequences, where for each

variable site, only one base was randomly chosen and retained (consensus). This could

represent a case in which read coverage across a locus is highly uneven such that a haploid

sequence is actually a chimera of two or more alleles. Finally, we simply picked one phased

haploid sequence, which is possible when one parental haplotype has a majority of reads for a

locus (pick one). This scenario where only one parent's sequence would be recovered in the

offspring could be anticipated in real data due to subgenome dominance (e.g., Buggs et al.

2014; Bird et al. 2018). In practice, we expect most *de novo* assemblers to generate output in

between the haploid consensus data and pick one data.

Inferring species networks with phased and unphased simulated data — We estimated

species networks with the SNaQ function (Solís-Lemus and Ané 2016) from PhyloNetworks

v0.12.0 (Solís-Lemus et al. 2017) using Julia v.1.4.1 (Bezanson et al. 2015) from either the true

gene trees used to simulate the data, or gene trees estimated from the phased, pick one,

genotype, and consensus sequence data. For estimated trees, we used IQTREE v1.6.10

(Nguyen et al. 2015) with the same substitution model used to simulate the data. Each SNaQ

analysis used the species tree (A,((B,E),(C,D))) as the starting tree and allowed zero, one, or

two reticulation events. Each analysis included ten independent optimizations of the

pseudolikelihood score. We considered increasing numbers of reticulations if there was a

pseudolikelihood score improvement of two or greater compared to the previous model with one

fewer allowed hybrid edges. Note that pseudolikelihoods violate standard likelihood-based

model selection criteria such as likelihood ratio tests or using AIC weights, and slope heuristics

(Baudry et al. 2012) are often used instead. The choice of a cutoff here was necessary to

streamline processing across thousands of simulations. We compared the estimated networks

with one reticulation to the true network with the *hardwiredClusterDistance* function (Huson et

al. 2010) in PhyloNetworks. This allowed us to score the number of replicates that 1) recovered

the correct number of reticulations and 2) matched the true network when the number of

reticulations was set to one. We estimated networks for samples of four, 40, 400, and 1000

gene trees for each of the 100 replicates from the 12 simulation conditions.

Effect of phasing on divergence time estimation — We also used our simulated phased

and unphased data to estimate divergence times under the MSci model (Flouri et al. 2020)

using BPP v4.4.0. Here, we estimate divergence times (τ), population sizes (θ), and the

introgression probability, or proportion of immigrant loci in the receiving population, (φ) on the

correct fixed species network. φ was originally represented by γ (Meng and Kubatko 2009) and

referred to as an inheritance probability (Yu et al. 2011), but we use φ and the term

introgression probability to be consistent with BPP (Flouri et al. 2020). Our MSci analyses used

diffuse priors on τ_r and θ, with a mean on their simulated values and $\varphi \sim \beta(1,1)$. Phased, pick

one, and consensus sequences were treated as haploids while genotype sequences were

treated as unphased diploids and used for analytical integration over phases (Gronau et al.

2011) implemented in BPP. Although this is not correct for the tetraploid, it is arguably more

appropriate than treating all of the genotype sequences as haploids with ambiguous states.

Each Markov chain Monte Carlo (MCMC) analysis collected 10,000 posterior samples, saving

every 100 generations, while discarding the first 100,000 generations (i.e., 10% of the total run)

as burnin. Scripts for simulation and subsequent analyses of simulated data are available in

Dryad (http://dx.doi.org/10.5061/dryad.[NNNN]).

A Phasing Pipeline for Polyploids

Target enrichment data — The success of empirical studies in which phasing was

informative about hybridization or introgression events (e.g., Kamneva et al. 2017; Oberprieler

et al. 2017; Eriksson et al. 2018) motivated us to use phased data to infer reticulate evolutionary

histories of polyploids. We were aware of few instances of phasing genomic or phylogenomic

data in polyploids, except in cases where chromosome-level whole-genome assemblies have

characterized subgenomes in allopolyploid crops (Yang et al. 2017; Colle et al. 2019) or tree-

based methods that are dependent on the sampling of parental lineages (Freyman et al. 2020;

Nauheimer et al. 2020). We designed PATÉ for target enrichment data because of the

availability of such data for many taxa, but it is applicable to other types of data with paired-end

Illumina reads.

The end product of a *de novo* target enrichment assembly pipeline (such as HybPiper;

Johnson et al. 2016) generally is a single consensus sequence for each locus for each

individual. Allelic variation may be represented by ambiguous nucleotide codes within the single

consensus sequence or lost when the pipeline outputs the haplotype consensus sequence

where the majority vote from a collection of reads is used. We use these existing *de novo*

assembly pipelines as a starting point to provide the reference sequence for each locus for each

individual and leverage a recent phasing algorithm with high-quality variant calls to recover

phased haplotype sequences for taxa with known ploidy levels. Ploidy levels were characterized

for individuals in our *Dryopteris* analyses, but for unknown systems there are existing methods

to estimate ploidy directly from target enrichment data (Weiss et al. 2018; Viruel et al. 2019) in

the absence of other sources, such as flow cytometry (Farhat et al. 2019). PATÉ implements a

test for ploidy based on allele balance distributions for biallelic sites (Tiley et al. 2023a), but we

implore heavy caution with these tests.

Phasing alleles within loci — PATÉ (Supplementary Fig. S1) starts with assembled

target enrichment loci, such as the supercontig files output from HybPiper (Johnson et al. 2016),

that contain a single haplotype consensus sequence from each individual per locus. Reads for

each individual are then realigned to their consensus locus using BWA v0.7.17 (Li and Durbin

2009). PCR duplicates are flagged with MarkDuplicates in Picard v2.9.2

(http://broadinstitute.github.io/picard), and variant calls are computed with HaplotypeCaller in

GATK v.4.1.4 (McKenna et al. 2010). We applied the following hard filters with VariantFiltration

in GATK: (1) QD < 2.0, (2) FS > 60.0, (3) MQ < 40.0, (4) ReadPosRankSum < −8.0, (5) AF <

0.05 || AF > 0.95. These loosely follow community recommendations on filters for germline

variant discovery (DePristo et al. 2011). Notably, we do not perform quality score recalibration

or filter on the mapping quality rank sum, as we anticipate allopolyploids could have a lower

mapping quality associated with an alternate allele due to sequence divergence or structural

variation among homeologous chromosomes. We also consider a very narrow window for

filtering on allele frequency. Because increasing ploidy levels will generate smaller anticipated

ratios of alternate to reference alleles, coupled with sequencing error and read stochasticity, we

only aim to remove the most extreme cases. For example, if almost all reads support the

alternate allele at a site, it is difficult to diagnose if the error lies in the consensus assembly or

the read alignment. In these cases, only the reference site is retained, and the variant does not

pass the allele frequency filter. However, the allele frequency filter could be removed if

investigators are focused on organisms with higher ploidy levels. Additional options for pipeline

configuration are available on GitHub (https://github.com/gtiley/Phasing).

Biallelic SNPs that pass filters are then phased with H-PoPG v.0.2.0 (Xie et al. 2016). H-

PopG solves a heuristic phasing problem efficiently using dynamic programming. Although not

guaranteed to be an optimal solution, H-PoPG has been shown to have high accuracy while

also being fast (Xie et al. 2016; He et al. 2018; Moeinzadeh et al. 2020). Phasing variants in

polyploids is difficult because for *n* variants and *k* ploidy, there are $2^{n-1}(k-1)^n$ possible ways

to link the sites together. H-PoPG evaluates possible solutions efficiently by grouping reads into

k groups in such a way that differences within the groups are minimized. Focusing on target

enrichment data also constrains the complexity of the phasing problem compared to whole-

genome alignments (i.e., haplotype blocks are constrained to about 1000 bp). We then used the

phased variants to create individual allele sequences, where invariable sites are filled in based

on the reference sequence. In cases where there is no linkage information to phase across the

entire locus, we retain the phasing only for the longest block. The variants for the shorter

haplotype blocks can be collapsed into IUPAC ambiguity codes or treated as missing data

based on the investigator's preferences. PATÉ outputs analysis-ready fasta files with multiple

alleles per species. Variants are only phased within loci; we do not attempt to assign loci to

parental subgenomes. While this may complicate analyses of concatenated multi-locus

datasets, it is ideal for the MSC that assumes free recombination between loci and can leverage

multiple alleles per species for estimating θ. Assigning alleles to parental subgenomes should

be possible with PATÉ outputs where both parental lineages are sampled and there is sufficient

divergence for gene tree estimation.

Analyses of a Species Complex with Allopolyploidy

The North American wood fern complex (Dryopteris) — We tested PATÉ using new

target enrichment data from nine North American *Dryopteris* species, including both

allotetraploid and allohexaploid taxa, with well-studied reticulate relationships (Sessa et al.

2012a, b), as well as two outgroup taxa from the sister genus *Polystichum*. All putative parental

lineages are represented in our dataset, with the exception of a hypothesized extinct lineage (*D.*

semicristata; Sessa et al. 2012b). We sampled two or three individuals for each *Dryopteris*

taxon (Table S1). The target enrichment data were generated from the GoFlag 408 flagellate

land plant probe set (Breinholt et al. 2021) at RAPID Genomics (Gainesville, FL). The target

regions for this probe set are 408 exons found in 229 single or low-copy nuclear genes. We

generated haplotype consensus assemblies for each with HybPiper (Johnson et al. 2016). The

resulting supercontig sequences, which includes the exon region targeted by probes for

enrichment and flanking intron regions, became our reference sequences for genotyping and

phasing with PATÉ. We aligned both phased and haplotype consensus (i.e., the reference

supercontig) sequences with MUSCLE v.3.8.31 with default settings (Edgar 2004). For

comparison with simulation results, we generated a "pick one" dataset where only one phased

haplotype per locus was randomly selected from each individual. A "genotype" dataset was

generated by collapsing allelic variation into IUPAC codes for each individual as a locus.

Three species tests — We first explored the value of phasing data when estimating

reticulate relationships among three species, where we sampled two extant parental lineages

and their putative hybrid. We examined the three such extant relationships in the North

American *Dryopteris* complex:

1) Two diploid parental lineages (*D. ludoviciana* and *D. goldiana*) and their putative

314   allotetraploid descendent (*D. celsa*).

315   2) Two diploid parental lineages (*D. expansa* and *D. intermedia*) and their putative

316   allotetraploid descendent (*D. campyloptera*).

317   3) One tetraploid parent (*D. cristata*), one diploid parent (*D. goldiana*), and their putative

318   allohexaploid descendent (*D. clintoniana*).

These three scenarios represent different ages of parental divergence, with a common ancestor

near 10 Ma for *D. ludoviciana* and *D. goldiana*, 15 Ma for *D. expansa* and *D. intermedia*, and 30

Ma for *D. cristata* and *D. goldiana* (Sessa et al. 2012b). We used both a full-likelihood Bayesian

approach and a topology-based pseudolikelihood approach to estimate the correct species

relationships from the different data types. First, using BPP v.4.4.0 (Flouri et al. 2020), we

estimated log-marginal likelihoods (ln *mL*) with stepping-stone sampling (Xie et al. 2011) for the

three possible rooted 3-taxon trees and network models that imply differences in the timing and

direction of gene flow among species (Supplementary Fig. S2). Each ln *mL* estimate used 24

steps, and each step had a posterior sample of 10,000, saving every 30 generations after a

30,000 generation burnin (10% of the total run). The ln *mL* values were then used to calculate

the six model probabilities following equation 1 using the bppr v.0.6.3 R package

(https://github.com/dosreislab/bppr). A percentile-based 95% confidence interval was generated

for each model probability by bootstrapping posterior disributions 1,000 times to investigate

uncertainty in model selection.

$$P(model) = \frac{exp(ln\ mL_{model} - ln\ mL_{max})}{\Sigma_i[exp(ln\ mL_i - ln\ mL_{max})]} \quad Equation\ 1$$

We performed four independent runs for each model for each data type prior to marginal

likelihood estimation to ensure convergence and the appropriateness of the MCMC settings.

The combined posteriors from the correct model were also used estimate all τ and θ for

comparison across data types. Notably, BPP can analytically integrate over possible phases of

sequence data when given IUPAC codes representing heterozygous sites (Gronea et al. 2011),

which is as accurate as perfectly phased data for diploids (Huang et al. 2022). In comparison,

standard gene tree estimation under the Felsenstein likelihood (Felsenstein 1981) treat IUPAC

codes as uncertainty and integrate over the possible tip states at sites independently.

For our topology-based method, we used the SNaQ function (Solís-Lemus and Ané 2016) from

PhyloNetworks v0.12.0 (Solís-Lemus et al. 2017) to test the presence and placement of gene

flow between the three species, while also including the two *Polystichum* outgroups. Gene trees

were estimated for each data type across the three cases with IQ-TREE v1.6.10 (Nguyen et al.

2015), using ModelFinder (Kalyaanamoorthy et al. 2017) for model selection on the

unpartitioned alignments. The starting tree was obtained with ASTRAL III v5.6.3 (Zhang et al.

2018) from the collection of ML gene trees. We tested the presence of zero, one, or two

reticulations based on a two pseudolikelihood point cutoff for accepting an additional

reticulation. Each analysis used ten independent optimizations.

Nine species tests — We investigated the differences in networks from SNaQ across

data types for the nine-species complex. This complex involves multiple reticulation events on

an edge, and thus the true network is not identifiable with topology-based methods (Solis-

Lemus and Ané 2016). Although full-likelihood methods should not suffer from the some of the

identifiability issues (Yu and Nakhleh 2015), they are not computationally feasible for the North

American *Dryopteris* complex. Despite the inherent identifiability issues, it is worthwhile to

examine the performance of scalable topology-based methods in such contexts to see if they

will identify some of the correct reticulate relationships or if they also will identify erroneous

relationships. Thus, we performed analyses of the nine-species complex and two outgroups

across the four data types with SNaQ as described above, but we allowed up to six reticulation

events. We used ASTRAL III v5.6.3 (Zhang et al. 2018) to generate the starting species tree for

network estimation using gene trees inferred from IQ-TREE v1.6.10 (Nguyen et al. 2015) with

the best model selected by ModelFinder (Kalyaanamoorthy et al. 2017). 100 standard bootstrap

replicates were performed for each gene tree, which were used to evaluate gene tree

incongruence and informativeness with respect to the ASTRAL species tree from phased data

for the consensus, genotype, and pick one gene trees with phyparts (Smith et al. 2015). To

assess node support for SNaQ, we performed 100 non-parametric bootstrap replicates, in which

both loci and bootstrap trees per locus were sampled with replacement. Each bootstrap

replicate was distributed independently to hasten the computation using a Perl script that

accommodates multiple alleles available on GitHub (https://github.com/gtiley/bootSNaQ-MA).

RESULTS

Simulation Shows Benefits of Phased Data

Network inference — In our simulation results, all data types performed well estimating the

correct number of reticulations (Supplementary Fig. S3). The analyses typically converged to

the true number of reticulations with 40 or more gene trees, except when using gene trees

estimated from genotype data with a 25% ($\theta = 2 \times \tau_h$) chance of a discordance gene tree.

However, using phased data provided more accurate estimates of the placement of the

reticulation edge in comparison to the genotype, consensus, and pick one data (Fig. 3). When

the true gene trees were used, which have information about the allopolyploid's hybridization

event (i.e., the allele sequences are sister to their respective parents in every tree), the correct

network can be inferred with 40 loci regardless of the age of hybridization or degree of ILS. The

gene trees estimated from phased data perform equally well, aside from requiring a few more

gene trees for recent hybridization events with high ILS ($\theta = 4 \times \tau_h$). Analyses based on

genotype, consensus, and pick one data almost always recover the true network when sampling

400 or more loci, but can miss the true network over half the time with 40 or fewer loci.

However, the genotype data failed to converge to the true network with increasing loci for a

hybridization age of 10 Ma with low to moderate amounts of ILS. Otherwise, varying degrees of

ILS had a negligible effect on network estimation among data types, and estimated gene trees,

aside from those from phased data, were less efficient when the hybridization age was more

recent.

394  *Divergence times* — Using phased data, whether using all alleles or only one, typically

395 resulted in accurate estimation of the hybridization age (Fig. 4). When divergence was low,

396 there was a small amount of estimation error, such that the phased data underestimated and

397 the pick one data overestimated the hybridization age, but the pattern suggests estimates could

398 converge to the true values with more loci. Interestingly, convergence towards the true value

399 appeared more efficient with higher ILS (Fig. 4). The phased and pick one data could otherwise

400 accurately estimate the hybridization time with 40 or fewer loci across all other divergence and

401 ILS scenarios. For analyses with genotype and consensus data, as the number of loci increased

402 and uncertainty in the posterior was reduced, the posterior mean did not converge to the true

403 estimate, and the simulated value was not within the highest posterior density (HPD) interval.

404 There was always a small degree of estimation error with the genotype data despite using

405 analytical phasing, and the consensus data overestimated the hybridization age between 1.5x

406 and 2x when using 400 loci across all simulation scenarios. These biases from genotype or

407 consensus data were also propagated for the parent nodes of the hybridization event across all

408 levels of ILS for $\tau_h = 0.001$ (Supplementary Figs. S4-S7), $\tau_h = 0.01$ (Supplementary Figs. S8-

409 S11), and $\tau_h = 0.1$ (Supplementary Figs. S12-S15). Nodes from speciation events could always

410 be estimated accurately with high precision by the phased and pick one data types provided

411 enough loci were sampled. The phased data was more efficient, always converging to the true

412 value by 40 loci, while the pick one data required 400 to recover τ_u when the sequence

413 divergence was low at $\tau_h = 0.001$. There was a small degree of estimation error among

414 speciation nodes for the genotype and consensus data, and the patterns suggested they might

415 not converge to the true values with more loci. However, speciation times were overestimated

416 by genotype and consensus data for $\tau_h = 0.001$ (Supplementary Figs. S4-S7) and $\tau_h = 0.01$

417 (Supplementary Figs. S8-S11), but underestimated by the genotype data and overestimated by

418 the consensus data for $\tau_h = 0.1$ (Supplementary Figs. S12-S15). Across all simulations, there

was little effect of increasing ILS aside from increasing HPD intervals, but the uncertainty was

negligible when 400 loci were sampled.

Analyses of target enrichment data from Dryopteris

Recovery of Phased Loci — On average, 62% of loci sequenced for an individual were

phased with eight variants passing filters per locus per individual (Supplementary Table S2).

The ploidy level appears to be strongly associated with the number of phased loci. Among

diploids, only 32% of loci were phased; the other 68% of diploid loci were either homozygous or

had too few linked variants for phasing. For tetraploids and hexaploids, 87% and 94% of loci,

respectively, were phased such that two or more phased haplotype sequences could be

recovered. Among loci where phasing was possible, variants were almost always resolved as a

single haplotype block, as opposed to being split into two or more blocks because not enough

reads were available to physically link variants. For polyploids, the number of unique phased

haplotype sequences most frequently matched the ploidy level, except in the case of a single *D.*

campyloptera individual (B087-D08), which also had relatively few recovered loci. Phasing data

only extended sequence alignment length by about two base pairs relative to the haplotype

consensus sequences (Supplementary Table S3). However, phased data more than tripled the

number of parsimony informative sites per alignment, similar to the increase in number of tips

(Supplementary Table S3).

Placing a single reticulation event — For our three-species full-likelihood analyses with

the MSci model, all data types decisively supported the putative reticulation hypothesis in the

cases of the allotetraploids *D. celsa* or *D. campyloptera* (Table 1). However, only the genotyped

data, coupled with the analytical phasing technique of BPP, chose the putatively correct model

for the allohexaploid *D. clintoniana* (Table 1). The phased and pick one data types selected the

network with the diploid *D. goldiana* as the hybrid descendent of the allohexaploid *D. clintoniana*

and allotetraploid *D. cristata*, while the best model for consensus data was a binary tree with *D.*

clintoniana sister to *D. cristata* (Table 1). However, model probability confidence intervals

suggest a great deal of uncertainty underlies model selection results for the allohexaploid case,

with the upper end of the interval for the putatively correct model at 0.603, 0.582, and 0.996 for

the phased, consensus, and pick one data, respectively (Table 1). Model parameters typically

converged across all analyses with the exception of the phased data for the *D. clintoniana* triplet

(Supplementary Fig. S16), which was due to one MCMC run despite convergence of the lnL

values.

The simulation experiments established some expectations that the phased and pick

one data would provide unbiased estimates of divergence times for nodes involved in the

hybridization events, while the genotyped and consensus data would provide under- and

overestimates, respectively. However, phased data generally produced younger mean τ

estimates for the *D. celsa* triplet with reduced credible intervals relative to other data types, but

much older mean τ estimates with more uncertainty for the *D. campyloptera* and *D. clintoniana*

triplets (Fig. 5; Supplementary Table S4). Similarly, there was inconsistency in θ estimates

observed among data types across triplets, with notably larger credible intervals for phased data

in the *D. celsa* and *D. clintoniana* triplets. Estimates of φ were sensitive to data type across

triplets, such that the mean φ suggested the major contribution to the focal allopolyploid from

phased data was *D. goldiana* into *D. celsa*, *D. intermedia* into *D. campyloptera*, and *D. goldiana*

into *D. clintoniana*, with other data types sometimes disagreeing (Fig. 5). Credible intervals

around φ always spanned $\varphi = 0.5$, but estimates for genotype, consensus, and phased data

suggested some biased gene retention for the *D. celsa* and *D. clintoniana* triplets

(Supplementary Table S4).

When performing a network search based on gene tree distributions with SNaQ, all data

types recovered the putatively correct relationship among *D. celsa* and its diploid parental

lineages (Fig. 6a). For *D. campyloptera*, all data types correctly detected one hybrid edge

(Supplementary Table S5), but they got the direction of gene flow wrong (Fig. 6b). All data types

also detected one hybrid edge for the allohexaploid *D. clintoniana* (Supplementary Table S5),

but there was disagreement over the underlying network. Both the phased and consensus data

invoked a ghost lineage sister to the three sampled *Dryoptersis,* with gene flow into the

allotetraploid *D. cristata*. While not unreasonable given the putatively extinct *D. semiscristata*

and missing *D. ludoviciana* from the sample, the relationship between *D. clintoniana* and its

parental lineages goes undetected (Fig. 6c). The genotype and pick one data recovered the

correct network, but reversed the direction of gene flow from allohexaploid *D. clintoniana* into

allotetraploid *D. cristata* (Fig 6c).

Inferring relationships among a complex with multiple reticulation events — The nine

Dryopteris species SNaQ network analysis with phased data identified two out of five

hypothesized reticulation events correctly along with one incorrect reticulation edge (Fig. 7a;

Supplementary Table S6). The analysis correctly identified the diploid *D. ludoviciana* and *D.*

goldiana as parents to the allotetraploid *D. celsa*, as well as the diploids *D. expansa* and *D.*

intermedia as parents to the allotetraploid *D. campyloptera*. It also detected a moderate level of

gene flow ,with an introgression probability of 0.335 from the common ancestor of *D. celsa*, *D.*

ludoviciana, and *D. goldiana* into the common ancestor of the outgroup *Polystichum*, albeit with

low bootstrap support. The parents of *D. celsa* were also detected by the other data types, but

all had some degree of error. The genotype data found a reticulation edge between the

allotetraploid *D. carthusiana* and diploid parent *D. intermedia*, but reversed the direction of gene

flow (Fig. 7b). A reticulation edge was also detected between *D. cristata* and the common

ancestor of *D. clintoniana*, *D. goldiana*, *D. celsa*, and *D. ludoviciana*, which is not completely

unreasonable given the allotetraploid *D. cristata* is believed to be a parent of *D. clintoniana*. The

consensus data only detected two reticulation edges (Supplementary Table S6), with the

second edge correctly showing gene flow from the diploid parent *D. intermedia* into the

allotetraploid *D. carthusiana*, provided the other parent *D. semicristata* is presumed extinct

obscuring the network interpretation (Fig. 7c). The pick one data, similar to the genotype data,

inferred a reticulation edge between *D. carthusiana* and *D. intermedia* with the wrong direction

of gene flow (Fig. 7d). The pick one data also detected a reticulation edge from *D. cristata* into

the common ancestor of *D. carthusiana D. intermedia*, *D. campyloptera*, and *D. expansa*, which

lakcs a clear interpretation other than invoking missing lineages underlying complexity of the

backbone topology (Fig. 1). In the one case where all data types detected the correct

relationship regarding *D. celsa*, the introgression probability was approximately 0.5 with phased

data while between 0.37 and 0.39 with others (Fig. 7; Supplementary Fig. S17).

Differences in the network estimates among data types may be explained by their

underlying spectra of quartet concordance factors (Supplementary Fig. S18). While spectra

were overall similar among data types, some deviations from expectations under ILS alone were

stronger in the phased data versus others (Supplementary Fig. S18). Analyses of gene tree

incongruence among the consensus (Supplementary Fig. S19), genotype (Supplementary Fig.

S20), and pick one (Supplementary Fig. S21) data showed similar levels of conflict among the

different data types with respect to a species tree estimated from the phased data (such

analyses with multiple alleles per species is not possible). The frequency of conflicting splits

with high bootstrap support was similar across datatypes for all nodes (Supplementary Fig.

S22), and low-support conflicts represented on average 56% of splits within *Dryopteris*.

DISCUSSION

New phylogenetic network methods offer the promise of elucidating the often complex

reticulate histories of polyploid lineages, even in the presence of ILS. Our results demonstrate

that under some conditions phasing polyploid target enrichment data can improve the accuracy

of such network inferences as well as divergence time estimates for the networks, and we

describe a novel pipeline (PATÉ) to address the difficult problem of phasing polyploid data.

Although PATÉ could handle different types of genomic data, such as transcriptomes and whole

genomes, target enrichment data are ideal for computational phasing because they can yield

high (i.e. greater than 100x) and even coverage within a locus. This was demonstrated by

almost all loci under investigation here being recovered as single haplotype blocks

(Supplementary Table S2). Because MSC methods treat loci independently and assume free

recombination between loci, it is not necessary to assign individual loci to parental subgenomes

for network analyses. However, the allele sequences output by PATÉ can also be used as input

for other tools such as *Homologizer* (Freyman et al. 2023) or *HybPhaser* (Nauheimer et al.

2020), which attempt to phase across loci and assign parental subgenomes. Our methods also

enable population genomic studies of polyploids (Tiley et al. 2023) where accurate estimation of

site frequency spectra can be used for demographic analyses otherwise complicated by

polyploidy (e.g., Excoffier et al. 2013; Liu and Fu 2020) or SNP-based network inference in the

absence of variation suitable for gene tree estimation (Blischak et al. 2018; Olave and Meyer

2020).

Promises and Limits of Phasing

The prospect of using alleles from phased genomic data presents an exciting step

towards revealing the evolutionary history of polyploids, which remains a critical impediment

within the plant evolution community (McKain et al. 2018). New strategies for explicitly

addressing this challenge are emerging (Freyman et al. 2023; Nauheimer et al. 2020; Mendez-

Reneau et al. 2023), and PATÉ can be a useful tool by phasing variants for many individuals

while leveraging genotype quality information. Our simulations demonstrated that phasing can

improve estimates of reticulate evolutionary relationships using network methods. In

simulations, phased data with all alleles represented in gene trees could more efficiently recover

the placement and directionality of hybrid edges than the genotyped, haplotype consensus, or

single haplotype sequences (Fig. 3). The advantages of using phased data for network

estimation diminished in simulations as the number of loci increased (Fig. 3), and this was

evident from our empirical analyses of *Dryopteris* triplets which produced similar results across

data types with 330 or 328 loci (Table 1; Fig. 6), except for the correct inference of allopolyploid

and parent relationships with genotyped data in the case of *D. clintoniana* (Table 1).

Both our simulations (Fig. 4; Supplementary Figs. S4-S15) and previous investigations

(Anderman et al. 2019). Our empirical analyses also demonstrated how the timing of

introgression τ_h and other parameters can be greatly affected by the data type used (Fig. 5). In

our *Dryopteris* analyses, τ_h for *D. celsa* was at least in the same order-of-magnitude among

data types, which had partially overlapping credible intervals, while phased τ_h estimate *for D.*

campyloptera was nearly four times older than the other data types (Fig. 5; Supplementary

Table S4). The *D. clintoniana* τ_h estimate from phased data was also much older than other

data types; albeit, with a 95% HPD interval. There were noticeable mixing problems in our *D.*

clintoniana full-likelihood analyses, which makes it difficult to evaluate whether the uncertainty

was due to extreme differences in θ among phased alleles within *D. clintoniana* and/or the

computational difficulty of the Bayesian methods with increasing sequence data. In all cases,

the differences between τ_h among data types is not consistent with results from the simulation

experiements, which suggested the consensus data should overestimate age compared to

phased or pick one data, with genotyped data having slightly younger estimates than phased

data. This highlights the difficulties of simulating data that capture the complexities of empirical

data and makes deciding which estimate is more reliable somewhat difficult. For example the

uncertainty of τ_h with phased data for *D. celsa* and *D. campyloptera* triplets was reduced

compared to the consensus and pick one estimates, but greater uncertainty was observed for τ

and θ at other nodes (Fig. 5). A potential compromise from simulations and empirical analyses

is the use of analytical phasing of polyploid data, as done with our genotyped data for BPP

analyses. Analytical phasing (Gronau et al. 2011; Flouri et al. 2020) has been shown to perform

well in diploids (Huang et al. 2022), and any potential biases from ignoring ploidy seem

outweighed by getting the *D. clintoniana* model correct (Table 1) as well as seemingly

reasonable parameter estimates under the MSci model with tight credible intervals (Fig. 5).

Our analyses also suggest that phasing may be problematic when the parental lineages

are deeply diverged. Although the phased data were able to accurately estimate the age of

older speciation nodes in simulations (Supplementary Figs. S4-S15), as phylogenetic

information is lost from multiple hits, the influence of the prior in full likelihood analyses should

become stronger. Deeper divergences will likely generate more switch errors among phased

haplotype sequences generated by PATÉ (Xie et al. 2016), as there will be more opportunities

for paralogy, structural variants, and sequence divergence to confound the read mapping,

genotyping, and phasing processes. When enough reads are available to call high-confidence

variants, we suggest that phasing with PATÉ can improve network estimation based on the

correct identification of the allotetraploids *D, celsa* and *D. campyloptera* and their parental

lineages in the analyses of the North American *Dryopteris* complex (Fig. 7a); however, phasing

alone cannot overcome some inherent challenges of network estimation.

Challenges of Network Estimation

Our analyses highlight the difficulty of estimating the evolutionary histories of reticulate

complexes, regardless of data type. The full-likelihood implementation of the MSci model

appears to be useful when the number of tips and plausible models for investigation are low, but

these methods may not be practical for generating hypotheses and exploring unknown

relationships for large numbers of taxa (e.g., Zhang et al. 2018). Quartet-based methods are

much faster and accurate when model assumptions are met (Solis-Lemus and Ané 2016) and

show similar accuracy to full-likelihood methods for estimating introgression probabilities (Flouri

et al. 2020). However, there are scenarios the true networks are non-identifiable (Yu and

Nakhleh 2015; Solís-Lemus and Ané 2016). For example, when multiple introgression events

affect the same lineage, such that there are overlapping cycles in a network (Solís-Lemus and

Ané 2016), the expected quartet distribution under the MSci model becomes a poor fit for the

empirical data (Cai and Ané 2020) and the network estimated may be incorrect. These effects

were evident in our empirical analyses where the relationship between *D. campyloptera*, *D.*

expansa, and *D. intermedia* was missing in the nine-species analysis (Fig. 7), which we expect

is due to a reticulation edge present between *D. intermedia* and *D. carthusiana*. Phasing

sequence data adds information that can improve estimates (Supplementary Table S3), but

unsampled or extinct lineages, such as the hypothesized *D. semicristata,* can create significant

barriers to recovering the true evolutionary history of reticulate complexes, regardless of how

many loci or individuals are available. Another identifiability problem is getting the direction of

gene flow correct (Yu and Nakhleh 2015; Thawornwattana et al. 2023), and these scenarios

were evident in our quartet-based analyses of a triplet that reversed gene flow from the

allotetraploid *D. campyloptera* into the diploid *D. expansa* (Fig. 6d) or in the analyses of the full

complex that reversed gene flow from the allotetraploid *D. carthusiana* into the diploid *D.*

intermedia (Fig. 7b and 7d).

Insights into Dryopteris Evolution

The North American *Dryopteris* complex has been well-characterized through the study

of multi-locus nuclear and chloroplast phylogenies, morphology, cytological observations,

chromatography, and isozyme analyses (reviewed in Sessa et al. 2012b). This makes it a useful

system for testing our phasing pipeline, and our analyses add nuance to our understanding of

some of the relationships among *Dryopteris* species. For example, our results with phased data

indicated *D. campyloptera* has received more loci from *D. intermedia* than *D. expansa* (Fig. 7a),

and *D. intermedia* is likely the maternal progenitor of *D. campyloptera* (Sessa et al. 2012b).

Following the allopolyploidy event, the *D. intermedia* subgenome may have been dominant,

providing a selective advantage for *D. campyloptera* in its distribution at the time (Bird et al.

2018). The phased nine-taxon analyses also supported the hypothesis of the unsampled diploid

lineage *D. semicristata*, based on the placement of *D. carthusiana* as sister to the rest of

Dryopteris, and the general sensitivity of *D. carthusiana* and *D. cristata* in the phylogenetic

backbone across data types (Fig. 7). Additional insights may be gained by a more complete

sampling of the genus, as the North American *Dryopteris* complex is not a clade (Sessa et al.

2012b), which should alleviate some of the identifiability problems. Analyses of the North

American *Dryopteris* complex alone highlight the need for caution when interpreting networks,

that are increasingly prominent plant evolutionary research.

Does Phasing Matter?

Combining phased data with recent network methods can help confront a major

challenge of plant phylogenetics: resolving the complex histories of polyploids. While our

analyses showed haplotype consensus sequences can be adequate for resolving single

reticulation events where both parental lineages are sampled, phased sequences may provide

more information with few loci sequence divergence is not too high or improve divergence time

estimates (see also Huang et al. 2022). Sequencing hundreds to thousands of loci is becoming

easier, but large studies with degraded herbarium material can have low returns in target

enrichment studies. Analytical phasing approaches (Gronau et al. 2011; Flouri et al. 2020)

provide a way forward available for full-likelihood methods while avoiding the potential for switch

errors from read-based phasing as done in PATÉ, but these will become difficult with many tips.

This highlights the need for continued development of models that explicitly consider

polyploidization mechanisms (Jones et al. 2013) while addressing scalability and limiting

assumptions for contemporary genomic data (Yan et al. 2022). Some reticulate complexes will

be difficult to disentangle with any data when confronted with statistical identifiability problems,

such as networks with multiple reticulations on a single edge (Solís-Lemus et al. 2016) when

using quartet-based methods, and our *Dryopteris* analyses demonstrate that caution is needed

when interpreting biological processes from phylogenetic networks in the absence of

corroborating evidence. As haplotype-phased genomes from long-read data become

increasingly available, the discussion of phase resolution will become trivial, but progress on

models that leverage such data and improve interpretation of processes, especially in polyploids

that maintain distinct subgenomes, from networks is still needed.

DATA AVAILABILITY

PATÉ is available through GitHub (https://github.com/gtiley/Phasing) and can be run on any

UNIX environment after installing basic genotyping software and H-PoPG.

(https://github.com/gtiley/Phasing). Simulated and empirical data supporting findings and files

for replicating analyses are available from the Dryad Digital Repository:

http://dx.doi.org/10.5061/dryad.[NNNN]. Raw Fastq reads for *Dryopteris* individuals are

available through the NCBI SRA database and are associated with BioProject PRJNA725004.

Individual SRA Identifiers are available in Supplementary Table S1.

SUPPLEMENTARY MATERIAL

Data available from the Dryad Digital Repository: http://dx.doi.org/10.5061/dryad.[NNNN]

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 FIGURES

 Figure 1 — Hypothesized Relationships among North American *Dryopteris*. Synthesis of

 results from Sessa et al. 2012a and Sessa et al. 2012b. A) Links between shapes show the

 putative parents and their allopolyploid derivatives. Black circles are diploids, squares are

 tetraploids, and the hexagon is the one hexaploid species in the group. *Dryopteris semicristata*

 is presumed extinct. B) Placement of allopolyploids in the context of the backbone relationships

 among diploids. Tetraploids are indicated with solid orange lines and the hexaploid with dotted

 lines. The grey line denoting a sister relationship between *D. semicristata* and *D. expansa*

 reflects one possible placement for the extinct taxon based on previous analyses (Sessa et al.,

 2012b).

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Figure 2 — Species network used for simulation. The divergence times in expected

substitutions per site are given for each node, and *h* is the hybrid node where two alleles enter

from both *t* and *v*. E is an allotetraploid while other species are diploid. Absolute divergence

times were changed by using values of θ at 0.001, 0.01, and 0.1. ILS was increased by

multiplying θ by a factor of 2, 3, or 4 while keeping all τ_u fixed to their initial values.

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Figure 3 — Proportion of simulation replicates that correctly identify the allopolyploid lineage using the SNaQ function of Phylonetworks. The x-axes are the number of loci sampled for each simulation. The y-axes are the proportions of correct networks. Results are based on networks estimated with a single reticulation, even if that network was considered less optimal than networks with zero or two reticulations. We saved the true gene trees from the simulations, while we estimated gene trees with the phased, genotype, consensus, and pick one data types.

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Figure 4 — Estimating the Timing of Hybridization with the MSci Model. Divergence times

are for node *h* in Figure 2. Divergence times are measured as the expected number of

substitutions per site. The dashed line represents the true simulated values. Points are posterior

means, and error bars are 95% HPD intervals, averaged across 100 replicates. Results are not

shown for the genotype data when $\tau_h = 0.1$ and $\theta = 4\tau_h$ because posterior means went towards

infinity and numerically unstable values that cannot be displayed.

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D. celsa   _D. campyloptera_   _D. clintoniana_

Figure 5 — _Dryopteris_ Divergence Times, Population Sizes, and Introgression

Probabilities under the MSci Model. Divergence times are measured as the expected number

of substitutions per site. The x-axis shows estimates from phased data and the y-axis shows

estimates from unphased (haplotype consensus) data for the inset network (equivalent to model

1085   7 from Supplementary Fig. S1). The dashed one-to-one line shows where older age estimates

1086   are consistently obtained from phased data. Error bars on points show the 95% HPD intervals

1087   for phased and unphased data.

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 Figure 6 — Network search results for three-taxon *Dryopteris* cases with SNaQ. The major

topology edge is indicated in blue and the minor edge (direction of introgression) is shown in

gold. The introgression probability (φ) is shown for each data type. In cases where a) *D. celsa*

or b) *D. campyloptera* were the allotetraploids under investigation, all data types recovered the

same species network. When c) *D. clintoniana* was the allohexaploid lineage from the

allotetraploid *D. cristata* and diploid *D. goldiana* progenitors, different networks were recovered

by the phased or consensus versus genotype or pick one data types.

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Figure 7 — Networks for all North American *Dryopteris* inferred from SNaQ. The major

topology edge is blue and the minor (reticulation) edges are shown in gold, with the direction of

introgression flowing into the major edge. Introgression probabilities for each reticulation edge

are shown in gold. Numbers on branches subtending nodes are bootstrap support values.

Results are shown separately for a) phased data where all haplotype sequences are included in

gene trees, b) genotyped data with a single sequence for individual with IUPAC ambiguity

codes, c) haplotype consensus sequences, and d) a single haplotype sequence representing

each individual among gene trees.

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1108 **TABLES**

Hybrid	Topology	Phased Model Probability	Genotype Model Probability	Consensus Model Probability	Pick One Model Probability
D. celsa	1	8.02×10^{-142} (3.62×10^{-146}, 3.31×10^{-137})	1.95×10^{-173} (1.03×10^{-177}, 2.78×10^{-169})	5.79×10^{-168} (3.15×10^{-172}, 8.7×10^{-164})	4.32×10^{-105} (1.99×10^{-109}, 2.27×10^{-101})
	2	3.18×10^{-126} (4.89×10^{-131}, 1.34×10^{-121})	5.44×10^{-136} (2.17×10^{-140}, 7.99×10^{-132})	1.66×10^{-113} (9.18×10^{-118}, 2.83×10^{-109})	2.78×10^{-84} (1.24×10^{-88}, 2.14×10^{-80})
	3	3.33×10^{-124} (5.19×10^{-129}, 1.66×10^{-119})	5.77×10^{-149} (1.63×10^{-153}, 1.31×10^{-144})	5.66×10^{-162} (6.09×10^{-166}, 9.31×10^{-158})	1.44×10^{-109} (6.87×10^{-114}, 2.06×10^{-105})
	4	1.36×10^{-146} (5.71×10^{-151}, 5.14×10^{-142})	6.98×10^{-149} (2.24×10^{-153}, 1.62×10^{-144})	2.89×10^{-152} (1.19×10^{-156}, 4.33×10^{-148})	1.44×10^{-109} (8.54×10^{-114}, 8.43×10^{-106})
	5†	**1 (1, 1)**	**1 (1, 1)**	**1 (1, 1)**	**1 (1, 1)**
	6	3.69×10^{-113} (1.31×10^{-117}, 1.45×10^{-108})	1.59×10^{-143} (7.07×10^{-148}, 3.22×10^{-139})	1.97×10^{-118} (1.83×10^{-122}, 4.43×10^{-114})	1.46×10^{-92} (1.12×10^{-96}, 8.06×10^{-89})
D. campyloptera	1	1.42×10^{-251} (1.6×10^{-256}, 5.32×10^{-247})	3.77×10^{-251} (2.11×10^{-255}, 6.16×10^{-247})	3.15×10^{-154} (3.78×10^{-158}, 5.25×10^{-150})	1.52×10^{-130} (5.8×10^{-135}, 3.11×10^{-126})
	2	1.03×10^{-210} (1.12×10^{-215}, 8.01×10^{-206})	2.54×10^{-226} (1.33×10^{-230}, 2.41×10^{-222})	1.69×10^{-110} (9.98×10^{-115}, 1.72×10^{-106})	1.11×10^{-90} (5.02×10^{-95}, 2.23×10^{-86})
	3	2.16×10^{-242} (2.64×10^{-247}, 6.06×10^{-238})	1.53×10^{-184} (7.18×10^{-189}, 5.03×10^{-180})	1.24×10^{-129} (6.49×10^{-134}, 2.39×10^{-125})	5.72×10^{-123} (5.18×10^{-127}, 1.1×10^{-118})
	4	1.22×10^{-133} (7.33×10^{-139}, 7.63×10^{-129})	1.87×10^{-193} (6.47×10^{-198}, 2.12×10^{-189})	2.8×10^{-134} (1.98×10^{-138}, 7.92×10^{-130})	4.19×10^{-114} (2.78×10^{-118}, 6.67×10^{-110})
	5†	**1 (1, 1)**	**1 (1, 1)**	**1 (1, 1)**	**1 (1, 1)**
	6	4.96×10^{-173} (6.57×10^{-178}, 3.7×10^{-168})	1.88×10^{-189} (9.15×10^{-194}, 1.93×10^{-185})	5.11×10^{-103} (2.49×10^{-107}, 4.81×10^{-99})	5.44×10^{-86} (3.65×10^{-90}, 1.32×10^{-81})
D. clintoniana	1	3.44×10^{-110} (5.27×10^{-115}, 1.25×10^{-105})	6.01×10^{-65} (2.21×10^{-69}, 1.99×10^{-60})	2.62×10^{-12} (8.24×10^{-17}, 1.82×10^{-8})	1.52×10^{-13} (3.47×10^{-18}, 4.54×10^{-10})
	2	1.44×10^{-04} (1.46×10^{-9}, 0.826)	1.91×10^{-47} (4.69×10^{-52}, 3×10^{-43})	4.49×10^{-9} (1.83×10^{-13}, 4.18×10^{-5})	5.84×10^{-6} (9.84×10^{-11}, 7.03×10^{-2})
	3	4.6×10^{-134} (6.97×10^{-139}, 5.65×10^{-130})	2.31×10^{-55} (5.51×10^{-60}, 5.35×10^{-51})	**1 (4.84×10^{-2}, 1)**	2.23×10^{-12} (5.82×10^{-17}, 1.38×10^{-8})
	4	1.23×10^{-115} (3.09×10^{-120}, 2.69×10^{-111})	2.18×10^{-27} (3.04×10^{-32}, 3.68×10^{-23})	*1.88×10^{-4} (1.05×10^{-8}, 0.728)*	2.02×10^{-27} (3.5×10^{-32}, 1.34×10^{-23})
	5†	*4.23×10^{-5} (7.74×10^{-10}, 0.603)*	**1 (1, 1)**	*1.73×10^{-4} (6.85×10^{-09}, 0.582)*	*5.7×10^{-3} (1.31×10^{-7}, 0.996)*
	6	**1 (3.81×10^{-2}, 1)**	2.48×10^{-31} (6.11×10^{-36}, 5.76×10^{-27})	1.04×10^{-15} (6.71×10^{-20}, 6.87×10^{-12})	**0.994 (3.6×10^{-3}, 1)**

1109 †The *a priori* allopolyploid hypothesis is always number five.

1110 **Table 1 — Model Probabilities for Possible Topological Hypotheses Using the MSci model.** Topologies of six models that

1111 enumerate the possible binary and reticulate evolutionary histories are displayed in Figure S2. The best model for each data type

1112 and triplet is shown in bold. A percentile-based 95% confidence interval is given for each probability by bootstrapping the posteriors.

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