Cooperative multivalent receptor binding promotes exposure of the SARS-CoV-2 fusion machinery core

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Abstract

The molecular events that permit the spike glycoprotein of severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2) to bind, fuse, and enter cells are important to understand for both fundamental and therapeutic reasons. Spike proteins consist of S1 and S2 domains, which recognize angiotensin-converting enzyme 2 (ACE2) receptors and contain the viral fusion machinery, respectively. Ostensibly, the binding of spike trimers to ACE2 receptors promotes the preparation of the fusion machinery by dissociation of the S1 domains. We report the development of bottom-up coarse-grained (CG) models validated with cryo-electron tomography (cryo-ET) data, and the use of CG molecular dynamics simulations to investigate the dynamical mechanisms involved in viral binding and exposure of the S2 trimeric core. We show that spike trimers cooperatively bind to multiple ACE2 dimers at virion-cell interfaces. The multivalent interaction cyclically and processively induces S1 dissociation, thereby exposing the S2 core containing the fusion machinery. Our simulations thus reveal an important concerted interaction between spike trimers and ACE2 dimers that primes the virus for membrane fusion and entry.

Introduction

Infection by severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2) begins with binding of viral particles to angiotensin-converting enzyme 2 (ACE2) cell-surface receptors, followed by viral-host cell membrane fusion, and entry of the viral genetic cargo (Shang et al., 2020). These events are orchestrated by spike glycoproteins – trimeric class I fusion proteins – that decorate the exterior of SARS-CoV-2 particles. Each spike protein consists of S1 and S2 domains, which are post-translationally cleaved by furin and remain non-covalently associated in a metastable prefusion state (Walls et al., 2020; Wrapp et al., 2020). The S1 domain contains the receptor binding domain (RBD) that is responsible for ACE2 recognition, while the S2 domain contains the fusion machinery. The S2 domains interact as a trimeric core with a characteristic helical stalk that is partially covered by the three S1 domains; the RBDs interact as a trimeric cap around the S2 trimeric core (Cai et al., 2020; Ke et al., 2020). A hinge-like conformational change exposes the RBD interfaces that are amenable to ACE2 association. Receptor binding is believed to result in S1 shedding, thereby exposing the S2 core. For fusion to occur, the second proteolytic site S2' is cleaved, thereby releasing the fusion peptide, after which the S2 core undergoes a dramatic conformational change into an extended helical stalk, i.e., the postfusion state, in a process similar to prior coronaviruses (Walls et al., 2017).

As spike proteins are indispensable to SARS-CoV-2 infectivity, inhibiting their function is a natural target for therapeutic design. Understanding how spike proteins bind to ACE2 and how binding primes exposure of the S2 trimeric core is therefore essential to viral activity. Structures resolved using cryo-electron microscopy (cryo-EM) combined with docking have shown that ACE2-RBD binding requires spike trimers to be open, and that two spike trimers can be accommodated on one ACE2 dimer (Yan et al., 2020). Additional cryo-EM structures have shown that up to three soluble ACE2 monomers can bind to the same spike trimer, which may result in exposure of the S2 trimeric core (Benton et al., 2020); indeed, soluble ACE2 trimers were recently demonstrated as an effective inhibitor of SARS-CoV-2 (Xiao et al., 2021). Both modalities are potentially important for viral avidity, and furthermore, likely dependent upon the flexibility exhibited by both the spike trimer stalk (Turoňová et al., 2020) and ACE2 domain (Barros et al.), as well as the stochastic nature of RBD opening observed throughout the spike trimer (Cai et al.,

2020; Ke et al., 2020). It has also been suggested that ACE2 binding to spike trimers induces

allosteric effects that heighten (dampen) conformational motions near proteolytic cleavage sites

and the fusion peptide (near the central helix and stalk) (Raghuvamsi et al., 2021) or

conformational motions that promote subsequent RBD opening (Xu et al., 2021).

Characterization of three circulating variant strains (B.1.1.7, B.1.351, and P.1) has shown that

increased infectivity is, in part, due to mutations in the RBD that increase ACE2 binding affinity

(Supasa et al., 2021; D. Zhou et al., 2021). Clearly, viral binding, fusion, and entry rely on a

complex dynamical process that likely leverages the concerted interactions between spike

trimers and ACE2 receptors.

To elucidate the molecular events that lead to binding and priming of the spike protein

for membrane fusion, we use molecular dynamics simulations. We first use atomistic molecular

dynamics (MD) simulations to systematically derive from "bottom-up" effective coarse-grained

(CG) models of spike trimers and ACE2 dimers, which are then validated against conformational

state statistics observed from experimental cryo-electron tomography (cryo-ET) data. We then

use CG MD simulations at the larger scale of multi-protein arrays on membranes to investigate

the binding between membrane-bound spike trimers and membrane-bound ACE2 receptors, and

associated shedding of the S1 domains that expose the S2 trimeric cores. Our simulations show

that multiple ACE2 dimers bind to spike trimers, consistent with prior cryo-EM models using

soluble ACE2 (Benton et al., 2020). Our analysis indicates that binding between spike trimers and

ACE2 dimers is positively cooperative, and furthermore, shows that this multivalent interaction

is necessary to productively prime the virus for membrane fusion. At present, such insights are

difficult to obtain experimentally.

Results

Our CG MD simulations consist of three constituents, spike trimers, ACE2 dimers, and lipid

membranes, each depicted in **Fig. 1A**. We extended our previously reported implicit-solvent, CG

spike protein model derived from all-atom molecular dynamics trajectories (Yu et al., 2020),

which were based on the open and closed state atomic models from cryo-EM (Protein Data Bank,

PDB: 6VYB, 6VXX) (Walls et al., 2020). Each spike protomer is modeled as non-covalently

interacting S1 and S2 domains with a CG resolution of around 10-15 amino acids per CG "bead"

or site, and initially prepared as trimers. Briefly, intra-domain interactions are represented by a

heterogeneous effective harmonic bond network while inter-domain interactions are

represented by a combination of excluded volume repulsion, short-range attraction, and

screened electrostatic terms (see *Materials and Methods*). A similar resolution and interaction

model are used to represent each ACE2 monomer, initially prepared as dimers. The lipids are

represented by a phenomenological CG model with a bending rigidity of 30 k_BT to emulate the

mechanical properties of typical membranes (Grime & Madsen, 2019). All CG model details and

parametrization procedures are described in the *Materials and Methods* section.

It is well-known that the RBDs of spike trimers are capable of hinge-like movements,

resulting in combinations of open and closed configurational states throughout the trimer (Cai et

al., 2020; Ke et al., 2020; Walls et al., 2020; Wrapp et al., 2020). Therefore, to validate our

updated CG spike model, we quantified the configurational sampling of the RBD. We first

simulated a single CG spike trimer in membrane (see *Materials and Methods*) for 50×10^6 CG

timesteps (τ_{CG} = 50 fs). To characterize the motions of the RBD, we quantified the distribution of

reciprocal interatomic distances (T. Zhou & Caflisch, 2012) (DRID) for each configuration of the

three RBDs; the DRID method computes the first, second, and third moments of the reciprocal

distances between each CG site and every other CG site, yielding $3N_{CG}$ features. We next

performed dimensional reduction using time-lagged independent component analysis (tICA), a

linear projection technique that aims to maximize representation of auto-correlations (Naritomi

& Fuchigami, 2011). The first 10 tIC dimensions were clustered using *k*-means clustering (Lloyd,

1982), revealing three primary conformational states. These three states can be seen in **Fig. 1B**,

which depicts the probability distribution of each of the three labeled clusters along the first tIC

(tIC_1) dimension. Assessing the root-mean-squared deviation of the configurations from each of

the three states (see **Fig. 1D** and **Fig. 1 – figure supplement 2**) reveals that the green-labeled

distribution represents "closed" RBDs, the red-labeled distribution represents "open" RBDs, and

the blue-labeled distribution represents an intermediate state we denote as "partially closed,"

which we discuss later. The separability of the open- and closed-state distributions (we include

the partially-closed state in the latter) depicted in **Fig. 1B** suggests that tIC_1 can be used as a

classifying metric for the open state ($tIC_1 > 0.4$) and closed or partially-closed states ($tIC_1 < 0.4$).

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Fig. 1. **Schematic overview and characterization of our coarse-grained (CG) models.** (**A**) Representative
depiction of a CG simulation of spike trimers in membrane interacting with an adjacent membrane with
ACE2 dimers. The insets depict the CG model components for the spike trimer (bottom), ACE2 dimer (upper
left), and lipid membrane (upper right). Note that the protein CG sites are colored by monomer while
glycans are represented by grey balls. (**B**) Probability distributions for RBD conformations projected onto
the first time-lagged independent component (tIC_1). The purple, grey, and orange distributions denote the
three clusters identified by k-means clustering with labels indicating their representative conformational
state. (**C**) Comparison of spike trimer conformational state populations (ranging from 0 to 3 open RBDs or
shed RBDs, i.e., exposure of the S2 trimeric core) from CG simulations and cryo-ET classification; the core
exposed state is in the prefusion form in the CG simulations while it is in the postfusion form in the cryo-ET
dataset. (**D**) Representative depiction of the average configuration of CG S1 (brown beads) within the
identified k-means clusters. For reference, CG configurations of experimentally-resolved open and closed
states of S1 are shown as magenta and cyan beads, respectively. Arrows indicate the positions of each
respective RBDs. In all cases, the N-terminal domains of S1 are aligned.

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140   **Fig. 1 - figure supplement 1**. Eigenvector components of the 1st tIC with respect to the 1st through 3rd
141   moments of DRID using the listed CG bead index within S1 as the reference point.

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148  In our prior cryo-ET classification of RBDs within spike trimers along the surface of intact

virions, we found that RBD conformations are stochastic and may range from three closed RBDs

to three open RBDs, with three closed RBDs and one open (two closed) RBDs representing the

two most predominant states (Ke et al., 2020). Given these observations, we assessed the

distribution of open RBDs within spike trimers as predicted by our CG model. We prepared 25

spike trimers in a flat membrane (around 170×170 nm^2) with periodic boundary conditions and

simulated three replicas of the system for 172×10^6 τ_{CG}. The simulated surface density, which is

around 1150 nm^2 per spike trimer, was chosen to reflect virions observed using cryo-ET, which

had 24 ± 9 spike trimers and an average diameter of 91 nm (Ke et al., 2020). Using the final

12.5×10^6 τ_{CG}, we characterized the RBDs throughout each of the trimers and computed the

population of trimers with 0, 1, 2, and 3 open RBDs. In **Fig. 1C**, we compare the distribution of

trimer states from our CG simulations to that of a previously reported cryo-ET dataset (Ke et al.,

2020). Our CG spike trimers undergo a slow yet reversible transition between open and closed

states, with around 50% of the total population having 1 open RBD, around 40% having 0 open

RBDs (i.e., 3 closed), and diminishing populations of 2 and 3 open RBD trimers. The relative

populations of these states are consistent with the cryo-ET classification of RBDs in virions. Note

that complete S2 trimeric core exposure (i.e., the precursor to the postfusion state) was not

observed throughout these simulations. However, we observed partial exposure in rare cases,

i.e., single S1 domains from spike trimers spontaneously dissociated due to thermal fluctuations,

which we discuss further later. In contrast, a minority population of postfusion trimers was

observed by cryo-ET. At this point, it is unclear whether this discrepancy is due to limitations of

the CG model, due to fixation by formaldehyde which may shift the open/closed equilibrium, or

both. Nonetheless, our analysis provides qualitative validation that the conformational variability

of the RBD in our CG spike trimer is consistent with experimental observations.

172  Next, to investigate the spike-ACE2 binding process, we simulated spike trimers

interfacing with ACE2 dimers. We prepared triplicate simulations of spike trimers in one

membrane adjacent to another containing ACE2 dimers (see **Fig. 1A**). The density of spike trimers

and ACE2 dimers was fixed such that the relative ratio of ACE2 dimer to spike trimer

([ACE2$_{dimer}$]/[S$_{trimer}$]) was 2.56, i.e., 64 ACE2 dimers and 25 spike trimers, sufficient to allow

multivalent ACE2 binding to each spike trimer. The two membranes (and their constituents) were

initially shifted along their normal directions until the closest distance between spike trimers and

ACE2 dimers was around 2 nm. The simulations were run for $172 \times 10^6\ \tau_{CG}$.

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Fig. 2. **Dissociation of S1 facilitated by multivalent ACE2 binding.** (**Top**) Snapshots of one representative S1
dissociation process upon binding of two ACE2 dimers. Each monomer in the ACE2 dimer is represented by
red and blue beads, respectively, while each S1 protomer in the spike trimer is represented by cyan, pink,
and green beads, respectively. The grey and silver beads denote glycans and S2 protomers, respectively.
The depicted process is also shown in **Video 1**. (**Bottom**) Time series profile depicting tIC$_1$ evaluated for the
RBD of each protomer (sharing the same color) for the spike trimer depicted above, i.e., spike trimer
protomers are labeled cyan to pink to green (back to cyan) in counter-clockwise order when viewing from
the top-down. To the right of the panel, the double-ended arrows represent the extent of the tIC$_1$
distributions for each state from **Fig. 1B**, while the rectangle shows the peak of each distribution.

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191   **Fig. 2 - figure supplement 1**. Additional time-series profiles of tIC$_1$ during ACE2-mediated S1 dissociation
192   from spike trimers. Each of the three panels is an independent spike trimer. The colors are the same as **Fig.**
193   **2**. Note that the spike trimer protomers are labeled cyan to pink to green to cyan in counter-clockwise order
194   when viewing from the top-down. These time series profiles indicate that the counter-clockwise protomer
195   from the initially ACE2-bound protomer is bound next then dissociated.

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197   **Video 1. Dissociation of S1 induced by multivalent ACE2 binding during coarse-grained molecular**
198   **dynamics simulations**. The two protomers within ACE2 dimers are depicted as red and blue beads,
199   respectively, while the three S1 protomers within the spike trimer are depicted as cyan, pink, and green
200   beads. All glycans and S2 protomers are represented by grey and silver beads, respectively. Lipids are not
201   shown for clarity.

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Throughout our simulations, we observed spike trimers fluctuating between the open and
closed state, with the former preceding ACE2 binding, as expected. Interestingly, we observed
spike trimers that were capable of binding to multiple ACE2 dimers, which required additional
opening of RBDs. However, we did not see multiple spike trimers binding to the same ACE2 dimer,
suggesting that any multivalent interactions between spike and ACE2 are due to an excess of
accessible ACE2 receptors.

Our simulations predict two modalities for ACE2-facilitated dissociation of S1. First, S1
dissociation appears to occur due to thermal fluctuations, which may happen both in the absence
and presence of binding between an open RBD and a single ACE2 dimer. The remaining two S1
monomers persist on the spike trimer, although in some cases, complete S1 shedding occurs after
secondary RBD opening and binding to a new ACE2 receptor. The second modality was observed
more frequently and involves the sequential binding of two ACE2 receptors to the same spike
trimer. Consequently, dissociation of all three S1 domains is accelerated and results in the
exposure of the S2 trimeric core (**Video 1**).

We depict the representative elements of the multivalent ACE2-binding process in **Fig. 2**,
in addition to tIC_1 time-series profiles for each RBD (additional examples are shown in **Fig. 2 –**
figure supplement 1). Here, the observed effect on the bound spike trimer is one of processive
release of S1 domains in a cyclical fashion. The process generally adheres to the following
sequential steps. First, RBDs conformationally vary between the open and closed state, as seen
for $\tau < 5\times10^6\ \tau_{CG}$ (note the variation of the cyan and pink lines/protomers in **Fig. 2**). One ACE2
dimer successfully binds to the open RBD, pulling the RBD and enforcing the open state, as seen
for $\tau = 12\times10^6$ CG (the cyan protomer adopts $tIC_1 = 1.0$ with reduced variance). The cleft formed
between the upraised RBD and the N-terminal arm of S1 provides a stabilizing pocket for the
clockwise RBD (from a top-down view), or the green protomer as depicted in **Fig. 2** ($tIC_1 = -0.6$),
thereby "tightening" the adhesion of this S1 domain. Conversely, the counter-clockwise RBD, or
the pink protomer as depicted in **Fig. 2**, appears to "loosen" its adhesion to the same cleft
provided by the green S1 domain. Due to the weakened interactions, the pink protomer
dynamically adopts the partially-closed state, as seen between $15\times10^6 < \tau < 20\times10^6\ \tau_{CG}$ (pink
line/protomer in **Fig. 2** with $tIC_1 = -0.25$). Thermal fluctuations allow the pink protomer to

spontaneously adopt the open state ($\tau = 26 \times 10^6\ \tau_{CG}$). A second ACE2 dimer binds to the newly

exposed RBD and "pulls" this S1 domain away from the spike, thereby promoting dissociation (τ

$= 30 \times 10^6\ \tau_{CG}$). The remaining S1 dimer complex, which remains bound to the first ACE2 dimer,

subsequently "loosens" and eventually dissociates due to thermal fluctuations ($\tau = 45 \times 10^6\ \tau_{CG}$).

Finally, the S1-bound ACE2 dimers diffuse away from the spike trimer, which now consists of the

exposed S2 trimeric core ($\tau > 50 \times 10^6\ \tau_{CG}$).

Prior experimental binding assays using soluble ACE2 have demonstrated positive

cooperativity when binding to SARS-CoV-2 spike trimers (Anand et al., 2020). Our simulations

show that multivalent ACE2 interactions induce productive S1 dissociation, and further suggest

that exposure of the postfusion machinery may be cooperatively correlated with ACE2

expression. To test this hypothesis, we prepared additional triplicate simulations with the same

spike trimer density but varied the ACE2 density. Here, we tested stoichiometric ratios of

[ACE2$_{dimer}$]/[S$_{trimer}$] between 0 and 4, the latter representing 100 ACE2 dimers and 25 spike

trimers, and performed simulations for $172 \times 10^6\ \tau_{CG}$. The final $12.5 \times 10^6\ \tau_{CG}$ were used for analysis.

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Fig. 3. **Cooperative enhancement of S2 trimeric core exposure by ACE2.** (**A**) Summary statistics for the
fraction of S1 monomers bound to ACE2 (blue), S1 monomers dissociated from the spike trimer (red), and
spike trimers with complete exposure of the S2 trimeric core (green) as the stoichiometric ratio of ACE2
dimers to spike trimers, [ACE2$_{dimer}$]/[S$_{trimer}$], is varied. (**B**) Hill plot comparing the natural log of the surface
density of ACE2 (in #/nm^2) to the natural log of the fraction of S1 monomers bound to ACE2 or the fraction
of completely exposed S2 trimeric cores (Θ). The black and grey lines are fits to the Hill equation with Hill
coefficients (n_H) equal to 1.45 and 2.02. All data points report the mean and standard error from triplicate
simulations.
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We summarize statistics on the extent of ACE2 binding, S1 dissociation, and S2 trimeric

core exposure as [ACE2$_{dimer}$]/[S$_{trimer}$] is varied in **Fig. 3A**. We used a distance-based metric

(described in *Materials and Methods*) to determine both binding and dissociation events. First,

we find that S1 monomers are capable of spontaneous dissociation due to thermal fluctuations

in the absence of ACE2, as noted above. Within our simulated timescales, however, none of these

dissociation events resulted in complete S2 trimeric core exposure. As S1 dissociation was not

observed in our atomistic MD simulations, nor during training of the CG model, we speculate that

the collective membrane fluctuations, further induced by the spike trimer inclusions, promote S1

dissociation as bound S1 should be considered a metastable state.

The presence of ACE2 has intriguing effects on binding, dissociation, and exposure

statistics. To measure the degree of cooperativity, we fit our binding data to the Hill equation:

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$$\ln \frac{\Theta}{1 - \Theta} = n_H \ln[A] + c$$

where Θ is the fraction of S1 monomers bound to ACE2, $[A]$ is the surface density of ACE2, n_H is

the Hill coefficient, and c is a constant. As seen in **Fig. 3B**, we find that $n_H > 1$ (= 1.45) for the

binding curve, indicating that S1 binding to ACE2 is positively cooperative. In **Fig. 3A**, both the

extent of S1 dissociation and S2 trimeric core exposure appear to monotonically increase with

$[ACE2_{dimer}]/[S_{trimer}]$. Note that the relative ratio between S1 dissociation and S2 core exposure

significantly decreases when $[ACE2_{dimer}]/[S_{trimer}]$ ratios exceed 2. In fact, as seen in **Fig. 3B**, the

propensity for S2 core exposure when $[ACE2_{dimer}]/[S_{trimer}] > 2$ also exhibits positive cooperativity

with $n_H = 2.02$. Together, these results suggest that multivalent ACE2 binding promotes S1

dissociation events that productively expose the S2 trimeric core, and eventually, the postfusion

machinery.

Discussion

We developed and applied CG simulation models of SARS-CoV-2 spike trimers and

receptor ACE2 dimers to study the dynamical mechanisms involved in viral avidity and

dissociation, the latter being a necessary step prior to membrane fusion. Our simulations

recapitulate the metastability of the S1 domains, which remain bound to spike trimers after furin

cleavage. Although rare, we observed spontaneous dissociation of S1 even in the absence of ACE2

binding, consistent with cryo-EM characterization of postfusion trimers on mature virions (Cai et

al., 2020; Ke et al., 2020). It has been shown that the D614G mutation is more infectious and

stabilizes interactions between S1 and S2 that prevent dissociation (L. Zhang et al., 2020),

promotes RBD opening (Benton et al., 2021; Mansbach et al., 2021), and increases ACE2 affinity

(Ozono et al., 2021). Ostensibly, the D614G mutation prevents premature S1 dissociation and

facilitates productive RBD-ACE2 binding, while ACE2-mediated S1 dissociation remains

unimpeded. It would be valuable for future atomistic and CG simulations to ascertain how D614G

and related mutations (e.g. the B.1.1.7, B.1.351, B.1.617.2, and P.1 variants) affect spike trimer

stability before, during, and after ACE2 binding.

One of our key findings is that the primary binding modality between spike trimers and

ACE2 dimers involves multiple ACE2 dimers binding to single spike trimers, rather than multiple

spike trimers binding to the same ACE2 dimer, an observation that is consistent with split

reporter assays of soluble spike trimers incubated with ACE2 dimers (Lui et al., 2020). We found

that spike trimer binding exhibits positive cooperativity with ACE2 dimer density due to the

multivalent nature of ACE2 binding. Soluble ACE2 has also been observed to cooperatively bind

to SARS-CoV-2 spike trimers, yet interestingly, not for SARS-CoV-1 spike trimers (Anand et al.,

2020). Finally, our simulations suggest that the multivalency of the ACE2 to spike trimer

interaction is necessary to facilitate complete dissociation of the S1 monomers that occlude the

S2 trimeric core, which contains the viral fusion machinery. Binding to ACE2 induces a cyclical

tightening and loosening process that processively weakens S1 interactions, both to adjacent S1

monomers and to the underlying S2 core, which leads to S1 dissociation. On the basis of cryo-EM

maps of soluble spike trimers bound to soluble ACE2, it was recently proposed that the three

RBDs throughout the spike trimer open and bind to ACE2 in a processive fashion, eventually

resulting in simultaneous dissociation of the three S1 monomers due to reduced contacts

between neighboring monomers (Benton et al., 2020). The process we observe in our simulations

is conceptually similar, although we propose that only two ACE2 dimers are minimally necessary

for productive uncoating of S1, and the counter-clockwise S1 (from a top-down view) from the

initial ACE2-bound S1 tends to open, bind to a second ACE2, and dissociate first.

One notable difference between the conditions of our simulations and the experiments

discussed above is that both our spike trimers and ACE2 dimers are tethered to their respective

membranes in a more realistic system than solubilized proteins. The tethers inherently restrict

the diffusion and conformational motions available to both spike and ACE2 proteins. One

potential consequence is that the relative populations of different spike/ACE2 complexes for

solubilized proteins may not reflect populations at the interface between virions and host cells.

Likewise, these populations are likely dependent upon the relative stoichiometry of spike trimers

and ACE2 dimers, as our simulations indicate. We suggest that the use of fluid membrane-bound

spike trimers and ACE2 receptors in biochemical and structural characterization of viral avidity,

e.g., as seen in the work of Yang et al. and Lu et al. (Lu et al., 2020; Yang et al., 2020), compared

to assays using soluble components, may prove to be characteristically different. For example,

single-molecule Förster resonance energy transfer analysis suggests that spike trimers bound to

one or two ACE2 receptors exhibit asymmetry throughout the three spike protomers (Lu et al.,

2020), which is consistent with the dynamical behavior observed in our CG simulations.

Our analysis also motivates several directions for future simulations. While researchers

have explored the free energy surface of single RBD open-close transitions (Casalino et al., 2021;

Gur et al., 2020), the thermodynamics of secondary and tertiary RBD opening, as well as the role

of multivalent ACE2 binding, should be thoroughly investigated. We note that our current CG

model will also likely require additional features to holistically probe SARS-CoV-2 virion binding,

fusion, and entry. Here, we investigated spike trimer and ACE2 dimer association at the interface

of two planar membranes. However, it will be important to elucidate the effects of virion

curvature (between 70-120 nm diameters (Ke et al., 2020)), which likely impose additional

restrictions to spike trimer conformational sampling while seeking ACE2 receptors. Sophisticated

modeling approaches to incorporate large-scale conformational changes, such as the extension

of the heptad repeat coiled coil in the postfusion state (Walls et al., 2017), will also be necessary.

In this work, we linearly mixed two model Hamiltonians that represent different configurational

states (open and closed RBDs). Several additional approaches, including plastic network models

(Maragakis & Karplus, 2005) and multi-configurational coarse-graining (Sharp, Vázquez, Wagner,

Dannenhoffer-Lafage, & Voth, 2019), may prove useful to construct CG models capable of state

transitions with increased accuracy for state populations and transition rates. These efforts will

expand the capabilities of CG modeling, which in turn will provide valuable insight into collective

molecular phenomena during SARS-CoV-2 infection, such as the role of cooperative multivalent

ACE2 binding to induce spike trimer uncoating reported herein.

Materials and Methods

Atomistic MD simulations. Trajectories from prior atomistic MD simulations of the spike trimer

in membrane were used to derive effective CG Hamiltonians (Casalino et al., 2020; Yu et al.,

2020). Statistics for the open and closed state of the spike trimer were supplemented with

additional triplicate simulations of the spike ectodomain using PDB 6VYB and 6VXX as initial

structures, respectively (Walls et al., 2020). Triplicate simulations of the ACE2 dimer interacting

with bound RBDs were also prepared using an initial structure from PDB 6M17 (Yan et al., 2020).

All simulations were prepared using CHARMM-GUI (Jo, Kim, Iyer, & Im, 2008) and the

CHARMM36m (Huang et al., 2016) force field. Each system was solvated with 2 nm of TIP3P water

from the protein edge to the simulation domain boundary and with 150 mM NaCl. All simulations

were performed using GROMACS 2020 (Abraham et al., 2015). Minimization was performed

using steepest descent until the maximum force was reduced to 1,000 kJ/mol/nm^2. Then,

equilibration was performed in several phases. First, 10 ns were integrated in the constant *NVT*

ensemble using the stochastic velocity rescaling thermostat (Bussi, Zykova-Timan, & Parrinello,

2009) with a damping time of 0.2 ps and a timestep of 1 fs. During this phase, the Cα backbone

of the protein was harmonically restrained with a force constant of 1,000 kJ/mol/nm^2. An

additional 40 ns were integrated in the constant *NPT* ensemble using the stochastic velocity

rescaling thermostat (Bussi et al., 2009) (2 ps damping time) and the Parrinello-Rahman barostat

(Parrinello & Rahman, 1980) (10 ps damping time) and a timestep of 2 fs. Finally, an additional

1650 ns were integrated in the constant *NVT* ensemble using the Nose-Hoover chain thermostat

(Martyna, Klein, & Tuckerman, 1992) (2 ps damping time) and a timestep of 2 fs. Throughout this

procedure, H-containing bonds were constrained using the LINCS algorithm (Hess, Bekker,

Berendsen, & Fraaije, 1997). Statistics were gathered every 100 ps and the final 1,200 ns of each

trajectory was used for CG model generation.

CG modeling. CG model generation for the protein constituents proceeded in three phases. The first phase determined the mapping between atomistic and CG sites. Mapping was performed using the essential dynamics coarse-graining (EDCG) method (Z. Zhang et al., 2008), which was designed to preserve the principal modes of motion sampled during atomistic simulations (Z. Zhang et al., 2008). In EDCG, the CG mapping operator, $M_R^N: \mathbf{r}^n \to \mathbf{R}^N$, which relates the configurations of the atomistic trajectory ($\mathbf{r}^n$) to that of the CG model ($\mathbf{R}^N$), is variationally optimized using simulated annealing. Here, each CG site is constructed using the center of mass of residues within contiguous segments of the protein's amino acid sequence. For N CG beads, $N - 1$ segment boundaries throughout the amino acid sequence are adjusted to minimize the target residual:

$$\chi^2 = \frac{1}{3N} \sum_{I=1}^{N} \langle \sum_{i,j} |\mathbf{r}_i - \mathbf{r}_j|^2 \rangle_t \quad : i, j \in I, j \geq i$$

where $I = 1, \dots, N$ is the CG site index, the brackets $\langle \cdot \rangle_t$ denote a time-averaged quantity, the sum over i, j is a sum over all unique pairs in the set of atoms belonging to the CG site I, and $\mathbf{r}_i = \mathbf{x}_i - \langle \mathbf{x}_i \rangle_t$ is the displacement of atom i from its mean position $\langle \mathbf{x}_i \rangle_t$. Note that the residual is small when the displacements $\mathbf{r}_i$ and $\mathbf{r}_j$ are similar, i.e. the motions of atoms in the same CG site are correlated. We chose N using an "elbow" heuristic to identify when increasing N yielded diminishing returns in χ^2. The "elbow" region when comparing a range of N values with corresponding residual (i.e., χ^2) values, as depicted in **Fig. 4**, yields a CG mapping resolution that balances computational expense and least-squared error in the represented principal component subspace. Following this protocol, we used 60, 50, and 70 CG beads for the S1, S2, and ACE2 protein mappings, respectively. The N-linked glycans (Watanabe, Allen, Wrapp, McLellan, & Crispin, 2020) were removed prior to this procedure. Each glycan was mapped to its center of mass and appended to their corresponding EDCG-mapped protein, totaling 13, 9, and 7 sites, respectively.

The second phase determined the effective CG Hamiltonian for each protein. We systematically determined parameters for S1/S2 in the open state, S1/S2 in the closed state, and ACE2 in the bound state, as well as their inter-domain interactions. The Hamiltonian (E_{tot}) was decomposed into four terms: intra-domain fluctuations (E_{intra}), inter-domain exclusion (E_{excl}), inter-domain attraction (E_{attr}), and screened electrostatics (E_{yukawa}):

$$E_{tot} = E_{intra} + E_{excl} + E_{attr} + E_{yukawa}$$

We used a hetero-elastic network model (hENM), in which harmonic bonds are assigned to all pairs of CG particles within a tunable distance cutoff r_{cut} (Lyman, Pfaendtner, & Voth, 2008), to represent E_{intra}; bond energies are equal to $k(r - r_0)^2$ where k is the spring constant of a particular bond and r_0 is the equilibrium bond length. The harmonic force constants k are

413 iteratively adjusted until the fluctuations in the CG model converge to that of the atomistic data,

414 i.e.,

415
$$\frac{1}{k_{ij}^{n+1}} = \frac{1}{k_{ij}^{n}} - \alpha\left(\langle r_{ij}^2 \rangle_{\text{CG}} - \langle r_{ij}^2 \rangle_{\text{AA}}\right)$$

where k_{ij}^{n} is the harmonic force constant for each i,j CG pair at iteration n, $\langle r_{ij}^2 \rangle =$

$\langle\left(x_{ij} - \langle x_{ij} \rangle\right)^2\rangle$ is the mean-squared fluctuation for each i,j CG pair, and α is a parameter that

controls the magnitude of the adjustment for each iteration. We chose r_{cut} for each CG model

using the "elbow" heuristic as shown in **Fig. 5**. Here, our residual was $\sum_{i,j}\langle r_{ij}^2 \rangle_{\text{CG}} - \langle r_{ij}^2 \rangle_{\text{AA}}$.

Following this protocol, we used distance cutoffs of 3, 4, and 3 nm for the S1, S2, and ACE2 CG

models, respectively.

422
423 **Fig. 5.** Comparison of hENM residuals to hENM cutoff radii for each of the CG protein models: S1, S2, and
424 ACE2.

426   Inter-protein interactions were composed of excluded volume, attractive, and screened

427   electrostatic terms. For excluded volume interactions (E_{excl}), a soft cosine potential was used:

428
$$A\left[1 + \cos\frac{\pi\, r}{r_c}\right]$$

429   where $A = 25$ kcal/mol and r_c is the onset for excluded volume. For each CG pair, r_c was set to

430   the minimum of two values: the minimum distance with non-zero frequency in the corresponding

431   pairwise distance histogram from CG-mapped atomistic statistics or the default value of $r_c =$

432   3.0 nm. Screened electrostatics (E_{yukawa}) were modeled using Yukawa potentials:

433
$$\frac{q_i q_j}{4\pi\epsilon_r\epsilon_0 r_{ij}}\exp\left(-\kappa\, r_{ij}\right)$$

434   where q_i is the aggregate charge of CG site i, $\kappa = 1.274$ nm^{-1} is the inverse Debye length for

435   0.15 M NaCl, and ϵ_r is the effective dielectric constant of the protein environment, approximated

436   as 17.5 (Li, Li, Zhang, & Alexov, 2013).

437   Attractive non-bonded interactions between inter-protein contacts (E_{attr}) were modeled

438   as the sum of two Gaussian potentials:

439
$$A_1\exp\left[-\frac{(r_{ij}-r_1)^2}{2\sigma_1^2}\right] + A_2\exp\left[-\frac{(r_{ij}-r_2)^2}{2\sigma_2^2}\right]$$

440   where r_1 and σ_1 are the mean and standard deviation determined by a fit to the pair correlation

441   functions (from CG-mapped atomistic statistics) between CG sites i and j through least-squares

442   regression. The constants A_1 and A_2 were optimized using relative-entropy minimization (REM)

443   (Shell, 2008). We used the iterative Newton-Raphson method (Chaimovich & Shell, 2009) to

444   update A_1 and A_2, which we refer to as parameter λ at iteration n:

445
$$\lambda_{n+1} = \lambda_n - \chi\frac{\left(\frac{\partial S}{\partial\lambda}\right)}{\left(\frac{\partial^2 S}{\partial\lambda^2}\right)}$$

where χ is the "mixing ratio" or "learning rate" of the iterative optimization procedure. Each

iteration required a LAMMPS simulation (Plimpton, 1995) of a single copy of the CG protein using

the current CG force field, which was run for 21×10^6 steps using a 100 fs timestep and a Langevin

thermostat (10 ps damping time) at 300 K. Statistics were gathered every 800 steps over the final

20×10^6 steps to calculate the parameter update. To aid convergence during training, a learning

rate schedule for χ was implemented:

452
1. $\chi = 0.5$ during the first 25 iterations
2. $\chi = 0.1$ during the next 75 iterations
3. $\chi = 0.01$ during the next 75 iterations
4. $\chi = 0.001$ during the next 75 iterations
5. $\chi = 0.1$ during the next 50 iterations
6. $\chi = 0.01$ during the final 150 iterations
459

A total of 450 iterations were used to generate each CG model. After this point, changes to λ

were effectively zero, and the optimization was considered complete.

The third phase determined an effective Hamiltonian for the spike trimer that was

capable of continuously transitioning between the open and closed state. Here, we modified

E_{intra}, E_{excl}, and E_{attr} as follows. For E_{intra}, we kept bonds that appeared in both open and closed

states and used the mean k and r_0 constants. For E_{excl}, we used the minimum r_c from both open

and closed states. For E_{attr}, we tested different linear combinations of the Gaussians parametrized

from the open and closed state. We found that an equal mix recapitulated open/closed statistics

the best, i.e., $E_{attr} = 0.5E_{attr,open} + 0.5E_{attr,closed}$. No modification of E_{yukawa} was needed since

this term is not state dependent.

The lipid model used the functional form from (Grime & Madsen, 2019), which we

summarize here. We used a linear four-bead model with 1 head bead, 1 middle bead, and 2 tail

beads. A piecewise potential was used to describe inter-lipid interactions:

473
$$
\begin{cases}
-\left(\dfrac{2Ar_0}{\pi}\right)\sin\dfrac{\pi r}{2r_0}; & r \le r_0 \\[2ex]
-\left(\dfrac{B(r_c - r_0)}{\pi}\right)\sin\dfrac{\pi}{2} + \dfrac{(r - r_c)\pi}{r_c - r_0}; & r_0 < r < r_c \\[2ex]
0; & otherwise
\end{cases}
$$

474   where $r_0 = 1.2$ nm (or $r_0 = 0.9$ nm for the head bead), $r_c = 2.4$ nm, $B = 1.66$ k_BT, and $A = 50$

475   k_BT (20 k_BT for the head bead). Harmonic bonds and angles were used to describe intra-lipid

476   interactions:

477
$$K_b\left(r - r_{0,b}\right)^2$$

478
$$K_a(\theta - \theta_0)^2$$

where $K_b = 5\ k_BT/\text{Å}^2$, $r_{0,b} = 0.6$ nm, $K_a = 5\ k_BT/\text{rad}^2$, and $\theta_0 = \pi$ rad. For the purposes of

modeling the interaction between the transmembrane domains of the spike trimer/ACE2 dimer

and lipids, we effectively considered the transmembrane domain as having the same interaction

as the lipids.

Model parameters and input files are available on Github: https://github.com/uchicago-

voth/MSCG-models/tree/master/Spike_ACE2

CG simulations. All simulations were prepared using PACKMOL and Moltemplate (Jewett,

Zhuang, & Shea, 2013; Martínez, Andrade, Birgin, & Martínez, 2009). Briefly, CG spike trimers

and ACE2 dimers were arranged in a grid using each density described in the main text. Two CG

lipid membranes were randomly packed around the transmembrane domains of each grid of

proteins in a 200×200 nm^2 lateral (*xy*) domain; the *z* dimension of the box was fixed to 160 nm.

The two membranes were then translated along the *z* direction until the minimum *z* distance

between spike trimers and ACE2 dimers was 2 nm. All simulations were performed using

LAMMPS (Plimpton, 1995). Conjugate gradient energy minimization was performed on each

system until the change in force was less than 10^{-6}. Then, proteins were held fixed while lipids

were integrated using a Langevin thermostat at 310 K (0.5 ps damping constant) and a Berendsen

barostat at 1 atm (0.5 ps damping constant, applied over the lateral *xy* dimension) over $2\times10^6\ \tau_{CG}$

(with τ_{CG} = 50 fs). During this process, the *xy* simulation domain compressed to around 170×170

nm^2. We then integrated both proteins and lipids using a Langevin thermostat at 310 K (5 ps

damping constant) over $170\times10^6\ \tau_{CG}$. Trajectory snapshots were saved every $25\times10^3\ \tau_{CG}$.

Analysis. All analysis was performed using a combination of custom Tcl scripts using VMD

(Humphrey, Dalke, & Schulten, 1996) and Python scripts using the MSMBuilder (Beauchamp et

al., 2011) and MDTraj (McGibbon et al., 2015) libraries. The configurational state of each RBD

was featurized using the DRID method (T. Zhou & Caflisch, 2012). Dimensional reduction (via tICA

(Naritomi & Fuchigami, 2011)) of this feature set into 10 tICs was performed using a lag time of

$40\times10^3\ \tau_{CG}$; the values of the first tIC eigenvector are shown in **Fig. 1 – figure supplement 1**. The

data were then clustered into 3 sets using k-means clustering (Lloyd, 1982). We featurized and

projected the configuration of each RBD extracted from our CG simulations onto the first tIC to

classify its state. We also used the following distance metric to classify the bound state of the S1

domain to both its partner S2 domain and ACE2:

512
$$\left| \frac{1}{N_{ii}} \sum_{ii}^{N_{ii}} r_{S1,ii} - \frac{1}{N_{jj}} \sum_{jj}^{N_{jj}} r_{S2(ACE2),jj} \right| = d_{S1-S2(ACE2)}$$

where ii and jj refer to CG site indices out of a set with N_{ii} and N_{jj} total sites, r is the position, d is

the distance, and | | is the norm of the vector. In other words, we compute the distance between

the centers of geometry of sets of CG sites. We chose CG site clusters that were observed to have

close association distances with minimal fluctuation during CG model training. For S1/S2 binding,

these included site indices 31-32 and 54-57 for S1 and 77, 87-89, 98-99, and 102 for S2. For

S1/ACE2 binding, these included site indices 43-49 for S1 and 134-137, 158, and 162 for ACE2

(residue mapping for each site is shown in Supplementary File 1). Using this metric, we

respectively classified S1/S2 and S1/ACE2 as bound states when d_{S1-S2} and $d_{S1-ACE2}$ were less than

4 nm, respectively.

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Competing Interests

544 The authors declare no competing financial and non-financial interests.
545
Supplementary Files

547 **Supplementary File 1** – Tables that summarize the residue mapping to each coarse-grained site
548 type in S1, S2, and ACE2.
549
Figure Supplements

551
552 **Fig. 1 - figure supplement 1**. Eigenvector components of the 1st tIC with respect to the 1st through 3rd
553 moments of DRID using the listed CG bead index within S1 as the reference point.
554

567
568 **Video 1. Dissociation of S1 induced by multivalent ACE2 binding during coarse-grained molecular**
569 **dynamics simulations**. The two protomers within ACE2 dimers are depicted as red and blue beads,
570 respectively, while the three S1 protomers within the spike trimer are depicted as cyan, pink, and green
571 beads. All glycans and S2 protomers are represented by grey and silver beads, respectively. Lipids are not
572 shown for clarity.
573

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