Sexual selection for males with beneficial mutations

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Abstract

Sexual selection is the process by which traits providing a mating advantage are favoured.

Theoretical treatments of the evolution of sex by sexual selection propose that it operates by

reducing the load of deleterious mutations. Here, we postulate instead that sexual selection

primarily acts through females preferentially mating with males carrying beneficial mutations.

We used simulation and analytical modelling to investigate the evolutionary dynamics of

beneficial mutations in the presence of sexual selection. We found that female choice for

males with beneficial mutations had a much greater impact on genetic quality than choice for

males with low mutational load. We also relaxed the typical assumption of a fixed mutation

rate. For deleterious mutations, mutation rate should always be minimized, but when rare

beneficial mutations can occur, female choice for males with those rare beneficial mutations

could overcome a decline in average fitness and allow an increase in mutation rate. We

propose that sexual selection for beneficial mutations could overcome the 'two-fold cost of

sex' much more readily than choice for males with low mutational load and may therefore be

a more powerful explanation for the prevalence of sexual reproduction than the existing

theory. If sexual selection results in higher fitness at higher mutation rates and if the

variability produced by mutation itself promotes sexual selection, then a feedback loop

between these two factors could have had a decisive role in driving adaptation.

1. Introduction

Mutation is the source of variation and the overwhelming majority of mutations are deleterious (i.e they have a negative impact on fitness) [1]. Because of this, most models have ignored beneficial mutations (i.e. those with a positive impact on fitness), deeming them too rare to be of interest (see [2] for an exception). Nevertheless, adaptation depends upon those rare occasions when mutations have a beneficial impact on fitness, especially in changing environments [3, 4]. Here, we investigate the role of sexual selection in favouring beneficial mutations. Sexual selection can be a powerful process resulting in strongly biased mating success [5]. This can even allow modifiers of the mutation rate ('mutator genes', such as factors controlling DNA repair [6, 7]) to persist, because female choice selects for those males with beneficial mutations [8, 9]. We postulate here that female choice can be so potent that it not only promotes the maintenance of genetic variation, but it allows beneficial mutations, despite their comparative rarity, to have a marked impact on fitness. This means that the two-fold cost of sex may be overcome not just by the lower reduction in fitness caused by deleterious mutation load [10, 11], but by the increase in fitness resulting from fixation of new beneficial mutations. Our focus in this paper is therefore on how sexual selection has a more important effect than has previously been considered in favouring beneficial mutations and driving adaptation, as opposed to the widely considered effect of decreasing deleterious mutational load. We further postulate that female choice can result in higher fitness at higher mutation rates, despite the decline expected from the predominance of deleterious mutations, because female choice is effective in selecting those males with an increased number of beneficial mutations.

Any explanation for the evolution of sexual reproduction within groups must show how the production of males, even when they do not care for offspring, increases the genetic quality of sexually produced offspring, to overcome the numerical reduction of reproducing offspring, the 'two-fold cost of sex' [12, 13]. Sexual reproduction can entail variance in

mating success, especially where females can choose between males of varying quality and

where a male can mate with more than one female [14, 15]. This differential mating success

is integral to the process of sexual selection and it has previously been suggested that this

process could contribute to the maintenance of sex by the selective removal of low quality

males from the breeding population [10, 11]. Sexual selection could thereby reduce the risk

of population extinction [2], as has been demonstrated in flour beetles *Tribolium castaneum*

[16]. According to this theory, females can pick those males with the lowest load of

deleterious mutations and those males that do not contribute to the breeding population are

effectively a sink for deleterious mutations.

We simulated the 'genetic quality' of individuals by examining the evolution of deleterious

and beneficial mutations in asexual and in sexual populations, and by varying the degree of

female choice in the latter. Implicit in our model is the assumption that, in addition to

determining survival, the mutations that a male accumulates determine the condition of

some trait, which is used by female subjects in mate choice. Thus, we assume that a male's

genetic quality is revealed in the trait and the female subjects use that information to select

the best male. Choice thereby functions to identify the highest quality mates [3, 17]. This is

supported by the literature on 'good genes' effects in sexual selection [18, 19] and by the

demonstration that sexual traits can reveal genetic quality [20-22]. It is also consistent with

other sexual selection models [23]. We compared sexual and asexual populations in the

presence of varying levels of sexual selection and a modifier of mutation rate. We

hypothesized that increasing mutation rate above a baseline would leverage the effects of

sexual selection making it more likely for sexual types to have higher genetic quality than

asexual types. The rationale for this is that an increase in mutation rate feeds variation in

genetic quality (and hence attractiveness), and that this variation promotes choice between

males [15]. We consider that sexually reproducing individuals will vary in mating success

[11] and that a key driver of this variation is female choice for high quality and attractive

mates that will provide females with high viability and attractive offspring. We propose that

females can actually get 'good genes' rather than 'fewer bad genes' as in the models of how

sexual selection facilitates the evolution of sex [10, 11]. As such, we predicted that variability

in mutation rate should facilitate the effect of sexual selection in overcoming the two-fold cost

of sex.

2. Methods

We simulated the 'genetic quality' of individuals by examining the evolution of deleterious

and beneficial mutations in asexual and in sexual populations, and by varying the degree of

female choice in the latter. A simplified flow diagram of the simulations is given in Figure S6

and a Visual C program is provided as supplementary information. Our simulation methods

were based on models of the evolution of mutation rate [6, 8]. As in those simulations, the

parameters reflected literature estimates where available [24], subject to the constraint that

the model was intended as a simple abstraction of reality and not an attempt to simulate an

entire genome.

The simulations began by setting up a population of P individuals. In simulations of sexual

populations, exactly half were male and half female. Individuals were given a pair of

homologous 'chromosomes' (i.e., we assumed diploidy) each bearing a 'mutator gene' and

an associated string of 10 'viability genes'. We did not assume that these genes constituted

the entire genome; only that there were no interactions between the genes of interest and

those at other sites and that for the purposes of comparison between simulations, all other

things were equal.

Each viability gene was subjected to a mutation process which could introduce deleterious

and/or beneficial mutations. By default, deleterious mutations occurred with probability 10^{-3}

per gene per generation and beneficial mutations at 10^{-6} per gene per generation, so

deleterious mutation occurred at a rate 1000x that of beneficial mutations. This implemented

both the principle that there are many more ways to introduce faults in a complex organism

than there are to improve it; and the empirical finding that beneficial mutations are much

rarer than deleterious ones. We note that estimates of the per nucleotide mutation rate for

sexually reproducing species tend to be around 1×10^{-8} per individual per generation [24-

26]). However, if we were to use literature mutation rates we would also need to use realistic

numbers of genes because selection acts at the level of the individual carrying those genes.

This would then effectively mean we were trying to simulate entire genomes. We cannot do

this, nor is this what the model is for. Instead, what we try to do is provide a 'proof of

concept' by modelling a scenario where individuals are subject to selection based on

differences in numbers of mutations. We assumed that each mutation had a sexually

concordant effect. A mutator gene increased the rates of beneficial and of deleterious

mutation by a factor *M*. We assumed that the mutator gene affected DNA repair only in a

relatively small region of the genome [27], namely the set of viability genes referred to

above; that it was adjacent to the first of the row of viability genes; and that the crossover

rate between the mutator and the first viability gene was the same as between each other

viability gene.

Individuals were subjected to a mortality process, whereby their probability of survival was a

function of their genetic quality. Deleterious mutations were assumed to have larger

phenotypic effects than beneficial mutations: deleterious mutations reduced the wild type

fitness of 1 by 0.005; beneficial mutations increased it by 0.002. The model assumed co-

dominance with additive fitness effects, so the effects of mutations were summed to give

'genetic qualities', which determined individual survivorship in a mortality process.

Surviving individuals reproduced, either by asexual or by sexual reproduction, the latter with

or without female choice. Reproduction replaced the population by selecting females at

random as parents, each such selection producing one offspring, with or without a male,

which was either selected at random or chosen from a set of *n*. Asexual reproduction was

implemented by selecting an individual at random and copying its chromosomes into an

individual in the next generation. Sexual reproduction without female choice involved

selecting a male and a female subject at random. In the case of female choice, a female

subject was selected at random, and a set of F male subjects was selected at random. The

female then bred with the male of highest genetic quality from that set of F males. This 'best

of n' rule is the most widely used rule in modelling female choice [28, 29] and has some

empirical support from lekking species [30]. For each sexual mating, one offspring was

produced by bringing together chromosomes contributed by both parents. This was carried

out by selecting a chromosome at random from each parent and allowing crossover between

each adjacent gene with probability 0.01. The process of selecting parents and producing

offspring was repeated until the population was replaced by a new generation of P

individuals.

Each scenario was simulated 10 times, allowing for uncertainty estimates to be computed

across runs which each produced different results due to the stochastic processes in the

models. Unless otherwise stated, parameters used were as given in Table S1.

3. Results

Considering first the results with the default mutation rates, if we compare Figure 1 a and b,

we can see that female choice had a marked effect in decreasing deleterious mutations

(means and standard errors across 10 simulations at generation 100 were 1.7526+-0.4349

and 0.04200 +- 0.06530 with no female choice and with female choice between two males

respectively) and in increasing beneficial mutations (from 0.0003+-0.0055 to 0.2000 +-

0.1897). We can approximate the relative effects of female choice on beneficial mutations as

increasing them by a factor of 0.2000/0.0003 = 667, as compared to decreasing deleterious

mutations by a factor of 1.7526/0.042 = 42. Figure 1 shows that this difference continued to

increase markedly with the number of generations.

Looking at the relationship between mutation rate and deleterious mutations, we found that

in populations with asexual reproduction and in those with sexual reproduction but no sexual

selection, deleterious mutation load increased dramatically when mutation rate increased

(Figure 2a). However, female choice, even between just two males, reduced deleterious

mutations to very low levels. Female choice was so effective that even with a high mutation

rate, the numbers of deleterious mutations were reduced to substantially below those found

in asexual populations or in sexual populations lacking female choice. Conversely, numbers

of beneficial mutations were low, even with a ten-fold increase in mutation rate in asexual

populations and sexual ones without female choice (Figure 2b). However, with female

choice, beneficial mutations were much more common, increasing from 12.49 ± 1.52 through

15.47 ± 1.57 to 17.19 ± 1.48 with female choice of 1, 2 and 5 males respectively; and an

increase to ten times the mutation rate accentuated this effect (with 3.29x, 5.87x and 6.38x

the numbers of beneficial mutations with female choice of 1, 2 and 5 males respectively).

Summing these effects, overall genetic quality decreased with increasing mutation rate in

asexual populations and sexual ones lacking female choice, yet it increased with increasing

mutation rate in populations with female choice (Figure 2c). Thus, sexual selection was so

powerful that it overcame the 1000-fold disadvantage (see Methods) of the beneficial

mutation rate and allowed an increase in genetic quality with increased mutation rate. This

increase in genetic quality occurred because sexual selection was effective at keeping

numbers of deleterious mutations low despite an increase in mutation rate, yet was also

effective in selecting for beneficial mutations, and could do this most effectively when

mutation rate was high.

We further investigated the interaction between female choice and mutation rate (Figure 3).

Genetic quality increased with mutation rate and female choice to an intermediate maximum

before declining rapidly. High levels of female choice improved genetic quality; but there

came a point where even the highest level of female choice shown was insufficiently

powerful not to be overwhelmed by the surge in deleterious mutations caused by a

substantially increased mutation rate.

We investigated the robustness of our results by varying key parameters whilst maintaining a

moderate degree of female choice ($F = 5$). First, we varied the ratio of deleterious to

beneficial mutation around the default ratio of 1000:1 respectively. As intuitively expected,

genetic quality increased as beneficial mutations became relatively more common, and

especially when this factor combined with a higher mutation rate (Figure S1). Looking at the

effect of each beneficial mutation on genetic quality, we can again see that the results are

intuitive (Figure S2): increasing the effect of beneficial mutations increases genetic quality,

especially when mutation rate is high. Varying the cost of female choice within the range

shown has no effect on genetic quality in either mutation rate condition (Figure S3).

Increasing the population size, P, increased the effect size, as expected from the increased

potential for genetic change across more individuals (Figure S4). Varying recombination rate

had a little quantitative effect, with increased recombination allowing an increase in genetic

quality, presumably through allowing favourable genetic combinations (Figure S5). All in all,

varying key parameters suggested that the main effect we describe was robust.

The benefit of simulations is that they can help us predict processes that are difficult to

comprehend intuitively or mathematically; the corollary is that they can be hard to interpret.

To better understand the processes in the model we hypothesized that female choice selects

for a breeding population that results in offspring that are s standard deviations above the

mean of the underlying population. To test whether males that were chosen to breed were

indeed of higher genetic quality than the population from which they were drawn, we

aggregated across the first 1000 generations for all 1000 reproducing pairs and calculated

the mean difference in genetic quality between females and their chosen males. Where

female choice was absent and mutation was at the default rate, the mean difference was

$0.0001 \pm {<}0.00005$ (standard error of the mean); with females choosing the best of 10 males

and mutation rate at 10x the default, the difference was 0.0022 ± <0.00005. Therefore,

females were choosing males that had a genetic quality equivalent to approximately 1

beneficial mutation above the average (where each beneficial mutation had an effect of

0.002 on fitness, as represented by the 10 simulated genes). In this way, sexual selection

appears to be able to exploit increasing variation caused by increased mutation rate and

actually produce an increase in genetic quality out of a background that one would otherwise

expect to be dominated by increased deleterious mutation load.

As a simple analytical approximation, consider that female choice between males results in

offspring that are *s* standard deviations above the mean genetic quality. For these offspring

to be of a quality that overcomes the two-fold cost of sex we need:

$$\bar{x} + s\sigma > 2\bar{x}$$

And therefore:

$$s > \frac{\bar{x}}{\sigma}$$

243   Equation 1

This equation will most readily be satisfied when the standard deviation of genetic quality is

high relative to the mean. That is, there needs to be high variability within the population.

Variability results from mutation, and we can show when an increase in mutation rate can be

favoured. This can occur when the decrease in the mean genetic quality in the population

that necessarily results from an increase in mutation rate (assuming there is a strong

predominance of deleterious over beneficial mutations) is more than compensated for by the

effect of female choice in selecting for males of high genetic quality. If subscripts 1 and 2

indicate the means and standard deviations before and after the change in mutation rate,

then:

$$\bar{x}_2 + s\sigma_2 > \bar{x}_1 + s\sigma_1$$

So:

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$$s > \frac{\bar{x}_1 - \bar{x}_2}{\sigma_2 - \sigma_1}$$

Equation 2

This analytical approach has the benefit that it considers the whole genome, something we

do not attempt in our simulations, which allow us to include stochastic factors at the level of

the gene. As a hypothetical numerical example, consider that increasing the mutation rate

lowers the mean genetic quality from 1 to 0.9 whilst increasing the variance in genetic quality

from 0.2 to 0.4. Consider also that female choice selects for males that produce offspring 1

standard deviation above the mean. Entering these hypothetical values into Equation 2

demonstrates that an increase in mutation rate combined with female choice can indeed

lead to an increase in the genetic quality of offspring. To aid understanding, this example is

illustrated in Figure S6. Whilst simplified, this makes the point that an increase in mutation

rate can be favoured under sexual selection and can thereby contribute to overcoming the

two-fold cost of sex.

4. Discussion

We have shown here that sexual selection is a potent force not just in reducing deleterious

mutation load but in leveraging the spread of beneficial mutations. Several empirical studies

have found that sexual selection over relatively short periods of time (typically under 100

generations) resulted in increased average fitness or reduced extinction [31]. Intuitively, it

seems more plausible that these results are observed because sexual selection is acting on

the already present standing variation, which largely comprises deleterious alleles. However,

our result shows that sexual selection for beneficial mutations can actually be the more

important effect, even over moderate numbers of generations and even when beneficial

mutations were 1000 times rarer than deleterious ones and when they each had only 40% of

the impact on fitness. We suggest that rather than males being effectively a sink for bad

genes [10, 11] they can be a vehicle for good genes.

The power of sexual selection was also apparent when we allowed for an increase in

mutation rate. We found that sexual selection for beneficial mutations could result in an

increase in genetic quality with increased mutation rate. This is counterintuitive given that

any increase in mutation rate brings 1000 times as many deleterious as beneficial mutations

in our model. An increase in mutation rate can never be adaptive in a model that considers

only deleterious mutations; it is only by allowing for rare beneficial mutations that we can

discern this effect. The result highlights just how powerful the effect of female choice can be,

even when just choosing between 2 males. Not only can sexual selection combined with

increased mutation rate provide a solution to the paradox of how variation can be maintained

[8, 32], but it can also lead to an increase in genetic quality.

We believe this is the first time that this effect has been reported. Its significance is that if

mutation rate is elevated above a typically postulated minimum level then this would

increase the benefits of sex relative to asexual reproduction, helping to overcome what has

been termed the 'two-fold cost of sex' [12, 13]. It therefore seems that the role of sexual

selection in the promotion of heritable genetic variation is key to understanding the

predominance of sexual reproduction.

Our model employs 'best of n' female choice as a convenient way of modelling sexual

selection. However, this is just one way of implementing variance in mating success in which

some individuals take a disproportionate share of mating opportunities. Active choice by

females is clearly something that must have evolved after sexual reproduction itself, but in

line with theoretical treatments that have focussed on deleterious rather than beneficial

mutations [10, 11], we posit that some variance in mating success is inevitable and that this

could have contributed to the invasion of sexual reproduction in an asexual population in the

first instance. Current thinking suggests that anisogamy has evolved from isogamy [33, 34].

The evolution of anisogamy needs to be accompanied by an effect on mating success. Only

when an increase in mating success of smaller male gametes overcomes the cost of loss of

a male resource contribution to the zygote will this system be evolutionarily stable. Where

mating success is determined by the level of indirect genetic benefits, the male phenotype

will evolve to reveal their underlying genetic quality and only when the genetic quality

differences are large and constantly maintained by mutation will this system be evolutionarily

stable [8, 15, 35]. Signalling of genetic quality by males must therefore have evolved either

concurrently or very early on in the evolution of anisogamy.

Our model assumes that mutation can be controlled genetically. One mechanism for this is

through selection on those genes that are responsible for DNA repair [6], but there are other

possible genetic mechanisms [36]. We predict a greater mutation rate in genes that influence

sexually selected phenotypes and in more sexually selected species. Across non-human

species, particularly in birds, which differ in within population variance in mating success

[37], and thus the level of sexual selection, there is some evidence of a positive correlation

with the rate of mutation, measured by variance in minisatellite mutation rate [38, 39]. Given

that sexual selection can often result in greater variance in mating success in males, our

results are also consistent with male-biased mutation rates [40]. Our results may also be

consistent with the findings of experimental work on seed beetles [41]: interestingly, an

experiment reported that not only did sexually selected males pass on a lower mutation load

but that they had fewer *de novo* mutations suggesting that that sexual selection interacts

with mutation rates.

We have shown here that sexual selection can cause fitness to be higher when mutation

rate is higher; but we have not shown that this can dynamically drive an increase in mutation

rate through individual level selection. To do this would require an understanding of how

much individuals gain themselves from having a high mutation rate and how much they gain

from others having a high mutation rate. These fitness benefits depend in turn on with whom

individuals interact, which means considering population size and structure. Hence to limit

the complexity of the analysis presented we have here confined ourselves to considering

fitness benefits at the population level from fixed mutation rates.

Our results suggest a positive feedback effect whereby a high mutation rate could favour

sexual reproduction over asexual reproduction, while sexual reproduction with sexual

selection could favour a high mutation rate. We speculate that this could create a ratchet

effect in that once sexual reproduction is established, it would become harder to switch back

to asexual reproduction. We predict that the transition from sexual reproduction to asexuality

should be particularly rare in populations with strong sexual selection and that

parthenogenetic females could only invade a population of sexually reproducing females

when there is little or no genetic variation in male genetic quality. This could occur in small,

isolated inbred populations that become genetically depauperate. There is some evidence

that parthenogenetic populations can occur on islands [42]. Interestingly, some island

populations of birds are also known to lose the sexually selected signals that are

characteristic of mainland populations [43].

Natural selection will tend to favour a low mutation rate [1], yet adaptation requires mutation.

Our model shows how a faster rate of adaptation can occur with sexual selection. This is

consistent with the finding that sexual selection (measured as the degree of polygyny)

interacts with the rate of molecular evolution and with body mass to predict species richness

at the genus level [44]. We suggest that evolvability itself is under selection [45], and that

through sexual reproduction with sexual selection, evolution can lead to greater evolvability.

 Figures

a

b

Figure 1

Simulated evolutionary dynamics of the numbers of deleterious and beneficial mutations with

(a) no female choice and (b) female choice between two males. Plotted are the means

across 10 simulations. Parameters were: population size N=1000, equally divided between

males and females; Rate of deleterious and of beneficial mutations per gene per generation

= 10^{-3} and 10^{-6} respectively; effect of deleterious and beneficial mutations on default fitness

of 1 = 0.005 and 0.002 respectively; cost of female choice = 0.02*female choice.

 Figure 2

a

b

c

The figure shows how the numbers of mutations per individual vary with mode of

reproduction and strength of female choice where "Asex" is asexual reproduction; "Sex" is

sexual reproduction without female choice; and where "2", "5" and "10" are sexual

reproduction with female choice between the given number of males. Figures a and b show

the numbers of mutations per individual; c shows 'genetic quality' calculated as baseline

fitness (1) minus the number of deleterious mutations per individual multiplied by the effect

of each (0.005); plus the number of beneficial mutations multiplied by the effect of each

(0.002). The rate of deleterious mutations per gene per individual per generation was 1000x

that of beneficial mutations. Plotted are the means and standard errors computed across 10

simulations for each set of parameters, taken at generation 1000. Plotted in red are the

results where the mutator gene $M = 1$; blue is where $M = 10$, i.e. the rates of both deleterious

and beneficial mutations are at 10x the baseline mutation rates, which were 10^{-3} and 10^{-6}

respectively. Other parameters: population size N=1000, equally divided between males and

females in simulations with sexual reproduction; cost of female choice = 0.02*female choice.

Figure 3

The figure shows how 'genetic quality' varies with a 'Mutator' and with sexual selection by

female choice. Genetic quality was calculated as given in Fig. 2. The mutator was a

multiplier of the default mutation rates. Female choice was between 2, 5 and 10 males.

Plotted are the means and standard errors computed across 10 simulations for each set of

parameters, taken at generation 1000. Other parameters were as in Fig. 2.

Author contributions: GR devised the computer simulations and analysis and wrote the

first draft of the paper. MP conceived the original idea of relating sexual selection and

mutation rate and contributed to the theoretical background.

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