Luminosity thresholds of colored surfaces are determined by their heuristic upper-limit luminances in the visual system

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Abstract

Some objects in the real world themselves emit a light, and we typically have a fairly good idea as to whether a given object is self-luminous or illuminated by a light source. However, it is not well understood how our visual system makes this judgement. This study aimed to identify determinants of luminosity threshold, a luminance level at which the surface begins to appear self-luminous. We specifically tested a hypothesis that our visual system knows a maximum luminance level that a surface can reach under the physical constraint that surface cannot reflect more lights that incident lights and apply this prior to determine the luminosity thresholds. Observers were presented a 2-degree circular test field surrounded by numerous overlapping color circles, and luminosity thresholds were measured as a function of (i) the chromaticity of the test field, (ii) the shape of surrounding color distribution and (iii) the color of illuminant lighting surrounding colors. We found that the luminosity thresholds strongly depended on test chromaticity

and peaked around the chromaticity of test illuminants and decreased as the purity of

the test chromaticity increased. However, the locus of luminosity thresholds over

chromaticities were nearly invariant regardless of the shape of surrounding color

distribution and generally well resembled the locus drawn from theoretical upper-limit

luminance but also the locus drawn from the upper boundary of real objects. These

trends were particularly evident for test illuminants on blue-yellow axis and curiously did

not hold under atypical illuminants such as magenta or green. Based on these results,

we propose a theory that our visual system empirically internalizes the gamut of surface

colors under illuminants typically found in natural environments and a given surface

appears self-luminous when its luminance exceeds this heuristic upper-limit luminance.

1. Introduction

Most objects in the real world are visible because they reflect a light. Some objects

however themselves emit a light and such self-luminous objects typically have a distinct

appearance (e.g. traffic lights visually stand out in a scene). However, any light reaching

our retina is indiscriminately encoded by three classes of cone signals regardless of

whether the light is reflected from a surface or directly emitted from a light source. Thus,

judging whether a given object is self-luminous presents an mathematically

underdetermined problem to the visual system. The goal of this study is to reveal how

our visual system overcomes this computational challenge and generates the luminous

percept.

Self-luminous objects normally have a glowing appearance which is distinct from the

appearance of an illuminated surfaces. This qualitative difference was formally

introduced as a mode of color appearance (Katz, 1935). The original description finely

discriminates various categories, but this study concerns two modes: surface-color mode

and aperture-color mode, which respectively correspond to the qualities of color

appearance for an illuminated surface and a self-luminous object. The color appearance

was mostly studied in the surface-color mode, and only a limited number of studies

investigated the nature of the aperture-color mode (e.g. Uchikawa, Uchikawa & Boynton,

1989).

One common approach is to measure the transition luminance between the surface-

color mode and the aperture-color mode which is known as *luminosity threshold.* Past

studies investigated what factors might govern the threshold. In early study, Ullman

(1976) extensively discussed potential determinants of luminosity thresholds: highest

intensity in a scene, absolute intensity of stimulus, local or global contrast, intensity

comparison with the average intensity in the scene, and lightness computation. It was

concluded that although each factor plays a role, none of these factors are sufficient to

predict the luminosity thresholds. Bonato & Gilchrist (1994) reported quantitative

observation that an achromatic surface appears luminous when it has roughly 1.7 times

luminance of a surface that would be perceived as white. In later years they reported that

a surface with a smaller area appears to emit a light at lower luminance level (Bonato &

Gilchrist, 1999). For chromatic stimuli, it was repeatedly shown that luminosity thresholds

were negatively correlated with stimulus purity in a series of studies (Evans, 1959; Evans

& Swenholt, 1967; Evans & Swenholt, 1968; Evans & Swenholt, 1969). They further

pointed out the loci of luminosity thresholds over chromaticities are related to the upper-

limit luminance of surface colors, known as MacAdam limit (MacAdam 1935a; MacAdam

1935b). Spiegle & Brainard (1996) measured luminosity thresholds using colored real

objects placed under illuminants of different color temperatures. They supported Evans'

consistent observation about chromaticity-dependent nature of luminosity thresholds

and showed that the color of the illuminant also affects luminosity thresholds. They

further suggested that the locus of luminosity thresholds can be explained by the

physically realizable luminance level with real pigments under an estimated illuminant by

a participant. This is an interesting conceptualization linking the luminous percept to

illuminant lighting a scene. More recently, Uchikawa et al. (2001) pointed out that the

brightness of colored surfaces rather than a physical luminance is highly correlated with

luminosity thresholds of colored surfaces. Some studies revealed relation between

luminous percept and other perceptual dimensions. For instance, surround stimuli at the

same depth as a test field primarily affects the luminosity thresholds (e.g. Yamauchi &

Uchikawa, 2005).

These studies well characterized the properties of a test stimulus and of surrounding

contexts that have an impact on luminosity thresholds. One implicit assumption here is

that visual system bases luminous judgement on external factors available in a scene.

Such strategy is prevalent in many other visual judgements. For example, a famous

anchoring theory determines a reference based on simple statistics in a given scene (e.g.

highest luminance in a scene) which has been successful in explaining empirical results

involving lightness judgement (Gilchrist & Bonato, 1995; Gilchrist et al. 1999).

Alternatively, visual system might internally hold more absolute criterion for luminous

judgement. For instance, it was shown that our visual system might use statistical

regularities about possible range of surface color and illuminant color (Judd et al., 1964)

to solve an ill-posed problem such as color constancy (Maloney & Wandell, 1986). Also

there are suggestions that color contrast and assimilation arise simply from learning of

statistical regularities in external environments (Lotto & Purves, 2000; Long & Purves,

2003). The success of these prior-based approaches implies a possibility that humans

might take a similar strategy to make self-luminous judgement.

One primary focus in this study is to reveal whether determinants of luminosity thresholds

are externally defined from one scene to another or internally held by visual system

regardless of what are present in a scene. We specifically built a hypothesis based on

the latter view: visual system internalizes the physical gamut of surface colors under

various illuminants and refers to this knowledge when judging whether a given surface

is self-luminous. This physical gamut can be visualized by hypothetical surface called

optimal colors (MacAdam 1935a, MacAdam 1935b) which will be detailed in General

Method section. This hypothesis was specifically led up based on the observation made

in a series of color constancy experiments (Uchikawa et al, 2012; Fukuda & Uchikawa

2014; Morimoto et al, 2016; Morimoto et al, 2021). In these studies, we developed a

model for illuminant estimation that operated on the assumption that visual system

internalizes the gamut of surface colors under various illuminants (i.e. distribution of

optimal colors) and the model accounted for observers' estimation of illuminants

reasonably well in a variety of conditions. One interpretation of luminosity thresholds is

that we visualize the luminance level which visual system assumes as an upper-limit

boundary of surface color. Thus, we speculated that loci of luminosity thresholds

measured under different illuminants might resemble the locus of optimal colors.

We conducted three experiments to test our hypothesis. In each experiment, we

presented a 2-degree circular colored test field surrounded by many overlapping colored

circles. We measured luminosity thresholds as a function of test chromaticities.

Experiment 1 was designed to test the degree to which luminosity thresholds were

influenced by the color statists of surrounding stimuli, in this case the geometry of color

distribution. In Experiment 2, we tested the effect of illuminants as well as the shape of

surrounding color distribution to reveal whether luminosity thresholds loci agree with

optimal color locus under different illuminants (3000K, 6500K and 20000K). In

Experiment 3, we measured the loci of luminosity thresholds under atypical illuminants

(magenta and green) to investigate whether the loci of luminosity thresholds over

chromaticities might differ between chromatically typical and atypical illuminants.

2. General Method

2.1. Computation of physical upper-limit luminance at a given chromaticity

We can compute the theoretical upper-limit luminance at each chromaticity by calculating

the chromaticity and the luminance of optimal colors. Here we provide a basic idea of

optimal color, but more detailed description is available elsewhere (Uchikawa et al., 2012,

Morimoto, 2021). An optimal color is a hypothetical surface having a steep spectral

reflectance function as shown in Figures 1 (a) and (b). There are two types (band-pass

and band-stop types), and they can have only 0% or 100 % reflectances. Changing λ_1

and λ_2 generate numerous optimal colors ($\lambda_1 < \lambda_2$). To give concrete examples we

generated three illuminants of black body radiation (Figure 1 (c)). Then, 102,721 optimal

colors were rendered under these illuminants as shown by small dots in Figures 1 (d)

and (e). Panel (d) shows L/(L+M) in MacLeod-Boynton (MB) chromaticity diagram

(MacLeod & Boynton, 1979) vs luminance distributions. Panel (e) shows $\log_{10}S/(L+M)$

vs. luminance distributions. To calculate cone excitations, we used the Stockman &

Sharpe cone fundamentals (Stockman & Sharpe, 2000).

In the real-world surface reflectance must be less than 1.0 due to a physical constraint,

and thus an optimal color has a higher luminance than any other surface that has the

same chromaticity. Thus, no real surface can exceed this optimal-color distribution. To

show this concretely, we show, in Figures 1(d) and (e), 49,667 objects in the standard

object color spectra database for color reproduction evaluation (SOCS, ISO/TR

16066:2003).

From optimal color distributions we see that the physical upper-limit luminance is

dependent on the chromaticity. The peak of an optimal color distribution always

corresponds to a full-white surface (1.0 reflectance across all wavelengths), which thus

corresponds to the chromaticity and intensity of the illuminant itself (so-called white point

of the illuminant). For this reason, when the color temperature of illuminant changes, the

whole optimal color distribution shift towards the chromaticity of the illuminant without

drastically chaning the overall shape. Optimal colors with a higher purity have lower

luminance, as they have a narrower-band reflectance and consequently the distribution

spreads out as the purity increases. Importantly, once all optimal colors are calculated,

we can look for the physical upper-limit luminance at any chromaticity by looking for the

luminance of the optimal color at the chromaticity. Interestingly it is notable that the

distribution of real objects (SOCS dataset) shows a somewhat similar shape to the

optimal color distribution.

Figure 1: (a), (b) Example optimal colors of band-pass and band-stop types, respectively.

(c) Three illuminants defined based on Planck's radiation law. (d), (e) L/(L+M) vs.

luminance and $\log_{10}$S/(L+M) vs. luminance distributions, respectively, for optimal colors

and SOCS reflectance dataset rendered under 3000K, 6500K and 20000K.

2.2. Estimation of the upper-limit luminance at a given chromaticity for real

surfaces

Theoretical upper-limit luminance can be computed through the calculation of optimal

color, but the upper-limit luminance for real objects needs to be estimated. Thus, we

analyzed 49,672 surface reflectances from SOCS reflectance database (SOCS). This

dataset includes reflectances from a wide range of categories of natural and man-made

objects: photo (2304 samples), graphic (30,624), printer (7856); paints (229); flowers

(148); leaves (92); face (8049); Krinov datasets (370) including natural objects which

were measured in the separate study (Krinov, 1947). We then excluded reflectances that

contained a value higher than 1.0 at any wavelength as they might include fluorescent

substance. As a result, one reflectance from the printer category and 4 reflectances from

the paints category were excluded.

Remaining 49,667 surfaces were then rendered under 6500K, and their chromaticity and

luminance were calculated. The luminance value was normalized by that of the full-white

surface (100% reflectance at any wavelength). As shown in Figure 2 (a), we plotted

chromaticity of all surfaces on the MacLeod-Boynton chromaticity diagram, where

$L/(L+M)$ is the horizontal axis and $\log_{10} S/(L+M)$ is the vertical axis. We defined a grid of

25×25 bins and classified 49,667 colors into corresponding bins. Then, for each bin, the

maximum luminance across all colors that belong to the bin was defined as the upper-

limit luminance of real objects. This procedure was repeated for all 625 bins. The left and

center subpanels in panel (b) show the upper-limit luminance for optimal color (for

comparison purpose) and real objects. As seen here the locus of the upper-limit

luminance for real objects were not smooth. We assumed that this is an artifact due to a

limited availability of reflectance samples in the database rather than a nature of

reflectances of real objects. Thus, we smoothed the upper-limit luminances based on

spatial filtering by 3×3 convolutional filters (each pixel has the value of 1/9). The right

subpanel indicates the smoothed data. Note that this upper-limit luminance heatmap is

dependent on the color of illuminant. Thus we repeated the same procedure for other

black-body illuminants with color temperatures from 3000K to 20000K with 500 K steps.

Both optimal color locus and real objects locus unsurprisingly peak at the chromaticity of

illuminant shown by the red cross symbol. The upper-limit luminance of real objects

decrease as the stimulus purity increases more sharply than that of optimal colors. We

can refer to these look-up-table to find the upper-limit luminance of real objects for an

arbitrary chromaticity under illuminant with a range of color temperatures.

Figure 2: How to estimate the upper-limit luminance for real objects using the SOCS

spectral reflectance dataset. 25 × 25 grid was first drawn on MacLeod-Boynton

chromaticity diagram. For each grid bin, we searched the surface that has the highest

luminance as shown at the right part of panel (a), which was defined as the upper-limit

luminance for the chromaticity bin. (b) From left to right, the locus of upper-limit

luminance for optimal color, real objects (raw), and real objects (smoothed). The

lightness indicates the upper-limit luminance for chromaticity bins. The pale green color

indicates there is no data in that bin.

2.3. Observers

Four observers (KK, MI, TM and YK) participated in Experiment 1. KK and YK were also

recruited to Experiment 2 as well as two new observers (KS and NT). KK, KS and YK

participated in Experiment 3. Observers ages ranged between 22 and 57 (*mean* 31.4,

s.d. 13.2). Observers were all Japanese. All observers had corrected visual acuity and

normal color vision as assessed by Ishihara pseudo-isochromatic plates.

2.4. Stimulus Configuration

The stimulus configuration is shown in Figure 3. The color distribution for surrounding

stimuli and chromaticities used for test field are detailed in each experimental section.

The spatial pattern was shuffled for each trial.

Figure 3: Example of stimulus configuration. The center circle is a test stimulus, and its

luminance was adjusted by observers. Each circle had a diameter of 2 degrees in visual

angle, and the whole image subtended 15 × 15 degrees. The surrounding color

distribution is detailed in each experimental section.

2.5. Apparatus

Data collection was computer-controlled and all experiments were conducted in a dark

room. Stimuli were presented on a cathode ray tube (CRT) monitor (BARCO, Reference

Calibrator V, 21 inches, 1844 × 1300 pixels, frame rate 95Hz) controlled with ViSaGe

(Cambridge Research Systems), which allows 14-bit intensity resolution for each of RGB

phosphors. We conducted gamma correction using a ColorCAL (Cambridge Research

Systems) and spectral calibration was performed with a PR650 SpecrtaScan Colorimeter

(Photo Research inc.). Observers were positioned 114 cm from the CRT monitor and the

viewing distance was maintained with a chin rest. Observers were asked to view the

stimuli binocularly.

2.6. General procedure

Observers first dark-adapted for 2 mins and then adapted to an adaptation field for 30

seconds. The adaptation field was the full uniform screen that had either the chromaticity

of 6500K (Experiments 1 and 3) or the chromaticity of test illuminant (Experiment 2), and

in either case the luminance was equal to mean luminance value across surrounding

stimuli. Then, the first trial began. We drew surrounding stimulus circles so that they had

a specific color distribution as detailed in each experimental section. The 2-degree

circular test field was presented at the center of the screen. The test field was never

occluded by surrounding stimuli. Observer's task was to adjust the luminance of the test

field to the level at which the surface-color mode changed to the aperture-color mode.

The ambiguity regarding the criterion to judge the transition between surface-color mode

and aperture-color mode was reported in a past study (Speigle & Brainard, 1978,

Uchikawa et al., 2001). This is mainly because the transition is not sharp, and there is a

range that a surface can appear the mixture of surface-color mode and aperture color

mode. We took care this issue and instructed observers to set the luminance value to

the halfway between the upper-limit of the surface color mode and the lower-limit of the

aperture color mode. During the experiments, observers were instructed to view whole

stimuli rather than fixating at a specific point to avoid local retinal adaptation. The initial

luminance value for the test field was randomly chosen from 2.0, 5.0, 8.0, 11.0, 14.0,

17.0, 20.0, 23.0, 26.0 and 29.0 cd/m^2. Specific experimental conditions are detailed in

each experimental section.

3. Experiment 1

3.1 Surrounding color distribution, test illuminant and test chromaticity

In a natural scene, the colors of objects tend to cluster around the white point of illuminant

and the density of colors decreases as purity increases. Consequently, the color

distribution tends to form a mountain-like shape as shown in Figure 1 (d). The aim of

Experiment 1 was to investigate how loci of luminosity thresholds change when

thresholds are measured in a scene that has an atypical shape of color distribution. In

an extreme case, where observers purely rely on internal criteria to judge self-luminous

surface, the luminosity thresholds should not change at all regardless of surrounding

color distribution. However, in contrast if observers make a self-luminous judgement

using surrounding colors, for example by estimating the upper luminance boundary from

surrounding distribution, luminosity thresholds should largely change depending on the

shape of surrounding color distribution.

Figure 4 (a) shows the five surrounding color distributions used in Experiment 1. The

6500K illuminant on the black-body locus was chosen as a test illuminant in this

experiment. We first defined *natural* color distribution at upper-left subpanel and then

transformed the distribution to generate 4 atypical color distributions (*reverse*, *flat*, *slope+*

and *slope-*) in following ways. First, to construct the *natural* color distribution, we used

dataset of 574 spectral reflectances of natural objects (Brown, 2003). Out of 574

reflectances, 516 reflectances were inside the chromaticity gamut of the experimental

CRT monitor when rendered under the 6500K test illuminant. All stimuli were presented

via a ViSaGe, which had the technical constraint that only 253 colors can be

simultaneously presented. Thus, we selected 253 reflectances samples out of 516

reflectances so that when rendered under 6500K, 253 colors approximately spatially

uniformly distribute in a three-dimensional color space (L/(L+M), S/(L+M) and L+M).

To generate the other color distributions (*reverse*, *flat*, *slope+* and *slope-*), we

independently scaled each of 253 reflectances by a scalar value to manipulate the

luminance while keeping the chromaticity constant. The inserted image in each subpanel

shows an example of surrounding stimuli that has a corresponding color distribution.

Note that the spatial layout of surrounding stimuli was shuffled for each trial. For all

distributions, the intensity of test illuminant was determined so that a full-white surface

(i.e. 100% reflectance across all visible wavelengths) had the luminance of 35.0 cd/m^2

under the test illuminant.

For the center test field, we chose 9 reflectances from the 253 reflectances so that they

fall closely on the black-body locus when placed under 6500K illuminant. The panel (b)

in Figure 4 shows these 9 test chromaticities at which luminosity thresholds were

measured.

Figure 4: (a) 5 color distribution sets for surrounding stimuli. An inserted image at top

part shows an example stimulus configuration for each color distribution. The vertical

dashed black line indicates L/(L+M) value of 6500K test illuminant. Black cross symbols

indicate mean cone response across all 253 surrounding stimuli. (b) 9 test chromaticities

at which the luminosity thresholds were measured.

3.3 Procedure

One block consisted of 9 settings to measure thresholds at all 9 test chromaticities in a

random order. There were 5 blocks in each session to test all 5 distribution shapes. The

order of distribution condition was randomized. All observers completed 20 sessions in

total (i.e. 20 repetitions for each data point). They completed 10 sessions per day and

thus experiments were conducted in two days.

3.3 Results

Figure 5 shows results in Experiment 1. Colored symbols with error bars indicate each

observer's setting. Each data point is the average across 20 repetitions. The average

across 4 observers is shown by black circles. There were some variations across

individuals. Furthermore, the experimental design was to try to collect reliable data from

a small number of participants. Thus, we argue results individually. The magenta circles

show luminances of optimal colors at test chromaticities when rendered under the test

6500K illuminant (the optimal color locus). In other words, if the visual system uses the

optimal color to judge whether a surface emits a light, the observers setting should match

the magenta line. The blue line shows a smoothed upper-limit luminance locus of real

objects, estimated from SOCS reflectance dataset as shown in Figure 2, which more

rapidly decreases as it gets away from the white point than the optimal color locus does.

For simplicity, we hereafter refer to the magenta and blue lines as predictions of the

optimal color model and the real object model, respectively.

First, all observers showed that loci of luminosity thresholds show the mountain-like

shape regardless of surrounding color distribution. The loci generally peaked around the

chromaticity of a test illuminant (the vertical black dashed line) and the luminosity

threshold decreases as the test chromaticity gets away from the white point. Although

there are some individual differences, especially in the overall setting level (e.g. KK

generally has higher thresholds than others) and in the peak chromaticity, the luminosity

thresholds generally seem to be more resemble the prediction of the optimal color model

than that of the real object model in this experiment. This is consistent with the

hypothesis that the visual system knows the upper boundary of the optimal color

distribution and judges that a given surface is self-luminous when its luminance exceeds

the luminance of optimal colors.

Figure 5: Colored square symbols indicate averaged settings across 20 repetitions for

each observer. The error bar indicates ± S.E across 20 repetitions. The black circle

symbols indicate average observer settings (n = 4). The magenta circle symbols

denote the luminance of the optimal color at test chromaticities and thus indicate the

physical upper-limit luminance. The blue line shows the upper-limit luminance of real

objects estimated from the SOCS reflectance dataset. The vertical dashed line shows

the chromaticity of the test illuminant (6500K). The black cross symbol indicates mean

LMS value across surrounding stimuli.

To quantify the similarity between observers and models, we calculated Pearson's

correlation coefficient between observer settings and model predictions over 9 test

chromaticities. The Figure 6 shows summary matrices of correlation coefficient. We

calculated correlation coefficients for each observer and discuss them on an individual

basis.

The magenta and blue symbols indicate the optimal color model and the real object

model, respectively. In addition, we evaluated a model to judge the self-luminous

surface when its luminance exceeds the surrounding color distribution. The luminosity

thresholds estimated from such model should show the similarity to the shape of

surrounding color distribution. For example, in the reverse condition, the luminosity

threshold should be lowest at white point and increase as the saturation of the test

stimulus increases. This model is labelled as "surrounding color" in the Figure 6. Note

that this is a simplified model, and it is unlikely that visual system takes such strategy.

Instead, our goal here was to build a framework in which we quantitatively predict an

observer's behaviour if she/he judges the luminosity thresholds solely based on what's

externally presented in each trial without using any prior about statistics in the real

world.

The cyan star symbols in some cells indicate the highest correlation-coefficient value

across 3 tested models. The cyan arrows below each subpanel indicates the model

that received the highest number of cyan stars across 4 observers.

Overall, since the observer settings are stable across all distribution conditions, the

correlation coefficient patterns are also similar between the optimal color and the real

object models whose prediction are both not affected by surrounding colors. However,

the correlation coefficients for the surrounding color model strongly depend on

distribution condition as predicted. Specific trends are as follows. For observers KK

and MI, the loci of luminosity thresholds showed highest correlation with the optimal

color model for all distributions. For TM, the real object model was the best predictor in

all distributions except for the Flat condition. For YK, the optimal color model showed

the highest correlation for *reverse*, *flat* and *slope+* conditions while the real object

model showed the highest correlation for *natural* and *slope-* conditions. If we

summaries these trends based on the number of cyan arrows each model received,

the optimal color model is the best predictor in Experiment 1.

Figure 6: The matrices of Pearson's correlation coefficient calculated between observer

settings and model predictions over 9 test chromaticities. Each subpanel indicates

each distribution condition (*natural*, *reverse*, *flat*, *slope+* and *slope-*). The color of

individual cell indicates the correlation coefficient as denoted by the color bar. The cyan

star symbol indicates the highest correlation coefficient across 3 models. The cyan

arrows at the bottom of each subpanel show the model that received the highest

number of cyan star marks, indicating a good candidate model of human observers'

strategy to judge the self-luminous surface.

The major finding in this experiment is that the loci of luminosity thresholds are nearly

invariant regardless of the shape of surrounding color distribution. This result supports

the idea that observers use an optimal color distribution as an internal reference to

determine the luminosity thresholds rather than what is presented in a scene. In

Experiment 2, we tested whether this observation holds under different illuminants which

changes the shape of optimal color distribution as shown in Figure 1. If the visual system

indeed uses the optimal color, the luminosity thresholds should also follow the change in

a consistent way that optimal color distribution changes.

4. Experiment 2

4.1 Surrounding color distribution, test illuminant and test chromaticity

We employed *natural*, *reverse* and *flat* distributions of surrounding colors. For test

illuminants, we used 3000K, 6500K and 20000K on the black-body locus whose spectral

distributions are shown in panel (c) of Figure 1. For surrounding stimuli, we sampled 180

out of 253 reflectances used in Experiment 1 that were inside the chromaticity gamut of

the experimental CRT monitor under all test illuminants. The panel (a) in Figure 7 shows

all 9 test surrounding conditions (3 distributions × 3 test illuminants).

We then selected 15 surface reflectances from the 180 reflectances. The panel (b) shows

the 15 test chromaticities when rendered under each test illuminant at which the

luminosity threshold was measured.

Figure 7: (a) 9 color distributions for surrounding stimuli (3 test illuminants × 3 distributions). Inserted image shows an example stimulus configuration. The vertical dashed black line indicates the L/(L+M) value of each test illuminant. Black cross symbols indicate mean cone response values across 180 surrounding stimuli. (b) 15 test chromaticities at which the luminosity threshold was measured.

4.2 Procedure

One block consisted of 15 consecutive settings to measure thresholds for all test

chromaticities presented in a random order. There were 9 blocks in one session to test

all conditions (3 illuminants × 3 distributions). The order of condition was randomized. All

observers completed 10 sessions in total. The experiment was conducted in three days.

4.3 Results

The black line in Figure 8 shows the mean setting across 4 observers. The rest of the

data presentation follows the result in Experiment 1. For the clarity, only the averaged

setting is shown here, but the individual observers' data is presented in Figure S1 in

Supplementary material.

First, the mean settings showed that the locus of luminosity thresholds were again

mountain-like shape, and the influence of the shape of surrounding color distribution was

almost absent, supporting the finding in Experiment 1. It is also noticeable that the peak

chromaticity of the mean setting in each panel shifted towards the illuminant chromaticity

shown by vertical dashed lines.

Figure 8: The black circle symbols indicate average observer settings (n = 4). The error

bar indicates ± S.E across 4 observers. The magenta circle symbols denote the optimal

color locus. The blue line shows the upper-limit luminance of real objects. The red,

black and blue vertical dashed lines show the chromaticities of test illuminants of

3000K, 6500K and 20000K, respectively. The black cross symbol indicates mean LMS

value across surrounding stimuli. The individual observer data is shown in

supplementary material. A region surround by a rectangle in 20000K condition are

further discussed in Figure 9.

It should be noted that the peak chromaticity of luminosity threshold loci for 20000K was slightly shifted to higher L/(L+M) direction from the chromaticity of the test illuminant. This trend was generally consistent across observers as shown in Figure S1. One potential reason would be that observers misestimated the illuminant color from the surrounding colors. Human color constancy is often imperfect, and thus we speculated that observers' luminance settings might better agree with the optimal color or real objects rendered under an illuminant estimated by each observer instead of a ground-truth illuminant (20000K). In fact allowing misestimate of illuminant color was also reported be an important factor in predicting luminosity thresholds by Spiegle and Brainard (1990). The estimated illuminant is normally measured using a technique such as achromatic setting (Brainard, 1998), but these data were not collected in this study. Thus, we assumed the peak chromaticity of observer settings as the observer's estimated illuminant.

We first calculated the chromaticities of illuminants from 3000K to 20000K in 500K steps. Then, for each observer and for each condition independently, we searched the color temperature that has the closest chromaticity to the peak chromaticity of the luminosity thresholds. Table 1 summarizes color temperatures of the estimated illuminants in each condition. In 3000K condition, estimated illuminants matched ground-truth color temperature for most observers. For 6500K, there was a slight variation across observers. It is notable that in 20000K condition that observers estimated color temperatures substantially lower than those of the ground-truth.

492 Table1: Estimated illuminant by each observer judged from the chromaticity at which

493 luminosity thresholds peaked. The top row shows the color temperatures of ground-

494 truth illuminants and the numbers in other cells indicate the color temperature of

495 estimated illuminants.

		3000K	6500K	20000K
Natural	KK	3000	5500	10500
	KS	3000	7000	8500
	NT	3000	5000	10500
	YK	3000	5500	12000
Reverse	KK	3000	6500	7500
	KS	4000	7000	7500
	NT	3000	5500	12000
	YK	3500	5000	10500
Flat	KK	3000	7000	8500
	KS	3000	5000	8500
	NT	3000	5500	12000
	YK	3000	6500	12000

Then, we drew optimal color loci under these estimated color temperatures. This concept

is depicted in Figure 9. Intuitively speaking this procedure allows us to equate the peak

between the optimal color locus and the measured luminosity thresholds locus. The pale

magenta curve shows the optimal colors under the estimated illuminant and seems to

predict mean observer settings better than the optimal color locus under the ground-truth

illuminant (20000K).

Figure 9: Optimal color models based on ground-truth illuminant (magenta) and based

on estimated illuminants for averaged observer setting (pale magenta). It is shown that

observers' settings are better explained by the optimal color model that allows

misestimation of illuminants by observers.

Figure 10 indicates correlation coefficient matrices for all conditions. We compare

correlations from 5 models: (i) optimal color model and (ii) real object model under

ground-truth illuminant, (iii) optimal color model and (iv) real object model under

estimated illuminant, and (v) surrounding color model. Again, the cyan star symbol in

cells indicates the highest correlation across 5 models for that participant. The cyan

arrows below each subpanel indicates the model that has the highest number of cyan

stars indicating the overall best model for that condition.

Figure 10: The matrices of Pearson's correlation coefficient calculated between

observer settings and model prediction over 15 test chromaticities. The cyan star

symbol indicates the highest correlation coefficient across 5 models. The cyan arrows

at the bottom of each subpanel show the model that received the highest number of

cyan star mark.

Overall, the surrounding color model does not show high correlation with observer

settings in any condition, agreeing with the trends in Experiment 1. The optimal color

model and the real object model seem to show high correlation, and it depends on the

condition whether which model shows a higher correlation. For 3000K, *natural*

condition shows highest correlation was found for the real object model, consistently

across all observers. For *reverse* condition, all observers except NT showed highest

correlations with the optimal color model under estimated illuminant while for *flat*

condition the votes were split between optimal color and real object models. For

natural-6500K, KS and NT were well predicted by the optimal color model under

ground-truth illuminant, but other two observers were better correlated with the real

objects model. For *reverse* condition, the optimal color and the real object model both

show high correlation. The real object model under estimated illuminant predicted best

in *flat* distribution condition. It is notable that for 20000K condition, the optimal color

model under the estimated illuminant was consistently the best predictor. It is also

shown that the optimal color model under the ground-truth illuminant shows much

lower correlations, suggesting that considering observers' misestimate of illuminants

plays a role in predicting luminosity thresholds. In summary both the optimal color

model and the real object model both showed a fairly good agreement with human

observers' settings.

Experiments 1 and 2 collectively suggested that both optimal color locus and real

object locus seemed to be a good candidate determinant of luminosity thresholds. One

noteworthy feature in Experiments 1 and 2 is that we used illuminants on blue-yellow

axis that are typically found in natural environments. We also used chromaticities on

black-body locus for the test field. If we assume that visual system learns the locus of

optimal color distribution or real objects distribution through observing colors in natural

environments, luminosity thresholds under atypical illuminants may not well agree with

prediction of the optimal color model or the real object model. We directly tested this

hypothesis in Experiment 3.

5. Experiment 3

Experiment 3 tested whether luminosity thresholds resembled optimal color locus

under atypical illuminants. We also chose a wider range of test chromaticities from the

black-body locus and a locus that is orthogonal to the black-body locus.

5.1 Surrounding color distribution, test illuminant and test chromaticity

We employed *natural*, *reverse* and *flat* for surrounding distributions. For test illuminants,

we used magenta and green illuminants. We chose two color filters (Rosco, R44 "Middle

Rose" and R4460 "Calcolor 60 Green") and 6500K illuminant was passed through these

filters to obtain the spectra shown Figure 11 (a). The chromaticities of these illuminants

largely deviate from black-body locus as shown in panel (b). Out of the 574 spectral

reflectances of natural objects collected by Brown, 251 reflectance were inside the

chromaticity gamut of the CRT monitor under both illuminants. For surrounding stimuli,

we sampled 180 reflectances out of the 251 reflectances and created each distribution

following the manipulation used in Experiments 1 and 2.

Panel (a) in Figure 12 shows surrounding distributions for all 6 test conditions (3

distributions × 2 test illuminants). The intensities of test illuminants were determined so

that average luminance across 180 colors matches 2.5 cd/m^2.

Figure 11: (a) Spectra for magenta and green illuminants used in Experiment 3. (b)

Chromaticities of both illuminants. The black-body locus and the chromaticity of 6500K

illuminant are shown for the comparison purpose.

For the test field, 8 reflectances were selected from the 180 reflectances and they were

used under both illuminant conditions. Then, we sampled different 5 reflectances

separately for each illuminant condition. The panel (b) shows 13 chromaticities when

rendered under each test illuminant. The 5 data points surrounded by a red edge

indicates the 5 reflectances that were not shared between illuminant conditions. In this

experiment, the test chromaticities were chosen so that their chromaticities vary along

two directions: (i) the black-body locus (shown by circles symbols) and (ii) an axis

approximately orthogonal to the black-body locus (shown by triangle symbols). There

were 7 chromaticities for each direction, but there was one chromaticity used for both

directions (shown by the black square symbol). The chromaticities of natural objects tend

to spread along black-body locus, and the purpose of this design was to test whether

luminosity thresholds measured at atypical chromaticities would deviate from the

prediction of optimal color model or real object model.

Figure 12: (a) 6 color distributions for surrounding stimuli (2 test illuminants × 3

distributions). Inserted image shows an example stimulus configuration. The vertical

dashed black line indicates the L/(L+M) value of test illuminant. Black cross symbols

indicate mean cone response values across 180 surrounding stimuli. (b) 13 test

chromaticities at which the luminosity threshold was measured. Symbols with a red

edge indicates reflectances that were not shared between magenta and green

illuminants.

5.2 Procedure

One block consisted of 13 consecutive settings and thresholds were measured for all test chromaticities in a random order. Each session comprised 6 blocks to test all distribution × illuminant conditions. The order of condition was randomized. All observers completed 10 sessions in total. Experiments were conducted in two days, and observers completed 5 sessions per day.

5.3 Results

Figure 13 shows results. Left 6 panels show luminosity thresholds measured at chromaticities on black-body locus (black circles and the square in panel (b), Figure 12) while right 6 panels indicate thresholds at chromaticities on the orthogonal locus (black triangles and the square in panel (b), Figure 12).

We first look at left two columns. For magenta illuminant condition, observers' settings again show a mountain-like shape. Also, it is shown that settings are not dependent on surrounding color distribution. However, in this condition optimal color model and real object model show relatively flat locus. For green illuminant, observer settings appear flat. Also luminosity thresholds for subject KS show a fairly different trends from the other observers, and the locus is not well predicted by optimal color locus nor real object locus, which was not observed in Experiments 1 and 2.

Figure 13: Observer settings in in Experiment 3. Left two columns indicates luminosity

thresholds measured at test chromaticities on black-body locus (circle and square

symbols in panel (b), Figure 12). Right two columns show test chromaticities on the

locus orthogonal to black-body locus (triangle and square symbols in panel (b), Figure

12). Colored square symbols indicate averaged setting across 10 repetitions for each

observer. The error bar indicates $\pm$ S.E across 10 repetitions. The black circle symbols

indicate average observer settings (n = 3). The magenta circle symbols denote the

optimal color locus and the blue line shows the real objects locus. The vertical dashed

line shows the chromaticity of the test illuminant. The black cross symbol indicates

mean LMS value across surrounding stimuli.

When the test chromaticities are on the axis orthogonal to the black-body locus (right

two columns), for magenta condition all observers' settings might appear to resemble the

optimal color locus at a first glance. However for green illuminant condition, KS again

shows different trend from other observers and all observers do not agree with the

prediction of the optimal color model nor the real object model.

Figure 14 allows us to compare the correlation coefficient across models and conditions.

For the leftmost column, the optimal color model showed overall good correlation for

natural condition, while the real object model showed good correlation for *reverse* and

flat conditions. For *natural* condition, KS shows highest correlation with surrounding color

model, which was not observed in Experiments 1 and 2 in which illuminants on black-

body locus were used as test illuminants. For the second leftmost column, in most cells

correlation coefficients appear considerably low. Although the optimal color model

consistently showed highest correlation for all distribution conditions (average coefficient

across 9 cells is 0.58), the correlation coefficient is not so high if we consider that the

correlation for the optimal color model was 0.901 in Experiment 1 (average across 5

distributions × 4 observers). Also, in Experiment 2, correlations were 0.746 for the optimal

color model of ground-truth illuminant and 0.837 for estimated illuminant (average across

9 conditions × 4 observers in both cases).

For right two columns, for magenta illuminant condition, the trend seems to be close to

that of test chromaticities on black-body locus (leftmost column), but correlation

coefficient overall seems to be lower. For green-natural condition, the closest color

shows a high correlation with observers KK and KS. It is notable that the optimal color

model shows nearly zero or even negative correlations. For reverse condition, real

objects showed the best correlation, but their values are not high (0.577, average across

3 observers). For flat condition, we did not find a consistently good model.

Figure 14: The matrices of Pearson's correlation coefficient calculated between

observer settings and model prediction over 7 test chromaticities in Experiment 3. The

cyan star symbol indicates the highest correlation coefficient across 3 models. The

cyan arrows at the bottom of each subpanel show the model that received the highest

number of cyan star mark.

In summary these results suggested that although the optimal color model and real

object models can account for observer settings to some extent, overall coefficient values

were substantially lower than those observed in Experiments 1 and 2. Also the

surrounding color model showed good correlation in some cases. These results might

imply that visual system does not have a rigid internal reference about upper-limit

luminance under atypical illuminant and sometimes relies on external cues such as the

color in surrounding stimuli. This trend was particularly true when the test chromaticities

are sampled from the locus orthogonal to black-body locus.

Finally, we summarize correlation coefficient from three experiments to test whether

correlation coefficient of optimal color model is higher for typical illuminants (Experiments

1 and 2) than atypical illuminants (Experiment 3). For each observer, we averaged

correlation coefficient of optimal color model for all conditions in Experiment 1 and 2 (14

conditions), which serves as a summary statistic for a typical illuminant. For 20000K

condition in Experiment 2, we used correlation coefficient value of the optimal color

model under estimated illuminant as it predicted observer settings substantially better

than the model under the ground-truth illuminant. We also calculated average correlation

coefficient for all conditions in Experiment 3 (8 conditions). Then, the averaged

correlation coefficients across all observers were 0.879 ± 0.0114 (average ± S.D.) for

typical illuminant and 0.525 ± 0.155 for atypical illuminant. Welch's t-test (one-tailed, no

assumption about equal variance) showed that optimal color model has a significantly

higher correlation for typical illuminant than atypical illuminant ($t(2.01) = 3.94$, $p = 0.0290$).

Also we performed the same analysis using correlation coefficient for the real object

model which showed the same trend ($t(2.84) = 2.93$, $p = 0.0326$).

These results are consistent with the idea that human observers empirically learn the

upper-limit luminance through observing colors in natural environments and use the

criterion to judge whether a given surface is self-luminous or not. Since magenta and

green illuminants are uncommon in natural environments, the visual system does not

know the upper limit of surface colors under those illuminants. This interpretation may

explain why prediction from optimal color model and real objects model did not well

explain observers' luminosity thresholds in Experiment 3.

5. General Discussion

This study investigated potential determinants of luminosity thresholds. Three

experiments showed that loci of luminosity thresholds are mountain-like shape peaking

around the illuminant color and decreases as stimulus purity increases, which showed a

strikingly similarity to the optimal color and real object loci. A simple alternative strategy

which bases a judgement on a surrounding color distribution did not explain observers'

settings well. Rather observers seem to hold an internal representation about at what

luminance a surface should reach self-luminous. Moreover, such similarity between

luminosity threshold and optimal-color/real-object loci was higher when surfaces are

placed under illuminants along blue-yellow direction than magenta and green illuminants

that are atypical in natural environments. These support an idea that visual system

empirically internalizes the heuristic gamut of surface colors through an observation of

colors in a daily life. Going back to the original question whether visual system relies on

external or internal reference for luminous judgement, the present study strongly

supports an internal reference hypothesis. However, in Experiment 2, the peak of the loci

of luminosity thresholds were strongly influence by the color temperature of illuminant

lighting surrounding stimuli. Thus, though the surrounding color model implemented in

this study did not explain observers' settings well, it should be noted that properties of

external stimuli are also likely to influence luminosity thresholds.

Color constancy is often described as a visual ability to identify a surface under different

illuminants. A surface reflects a light, and the reflected light enters our eyes. Because

the reflected light is a product of surface and illuminant components, color constancy is

often framed as a process in which our visual system estimates the influence of illuminant.

The "brightest is white" heuristics, which assumes that a surface with the highest

luminance provides the closest information about the illuminant color, has been known

as an influential approach to estimate an illuminant color (Land, 1977). However, self-

luminous objects do not carry information about scene illuminant, which might cause an

misestimation of illuminant if included in a scene. In general, when we received an

intense light from a surface, there are two ways to interpret this. One is that the surface

is placed under an intense illuminant and the other is that the surface is self-luminous.

This example highlights that generation of luminous percept needs to be incorporated

into a process of color constancy. In fact, Fukuda & Uchikawa (2014) showed that a

surface appearing in aperture-color mode does not have a strong influence on observers'

estimates of illuminant.

We chose a set of colored circles as experimental stimuli to directly test our hypothesis

while excluding any other cues. However, it is reported that changing a material property

could affect the mode of color appearance (Kuriki, 2015). Also, our experimental stimuli

were simulated to be uniformly illuminated by a single illuminant, but in natural

environments the spectra hitting an object surface changes from one direction to another

(Morimoto et al., 2019). The presence of multiple illuminants means that we need to

consider multiple optimal color distributions, and thus loci of luminosity thresholds

measured under such environment might also change. Despite a growing amount of

research on material perception (Fleming, 2013), luminous perception is little studied in

the field. While our choice of stimuli was necessary for experimental control, it will be

interesting whether our finding applied a wider range of stimuli that have complex

material properties and are illuminated in non-uniform ways.

One closely related phenomenon to self-luminous perception would be brightness

perception of colored objects. The Helmholtz-Kohlrausch effect describes that stimuli

with high purity appear to have high brightness even if luminance was kept the same.

There are reports that the effect is observed under a variety of viewing conditions

(Nayatani et al., 1991; Donoforio, 2011). However it has been uncertain why a color with

high purity needs to appear brighter. Curiously, as observed in the present study the

same trends hold for luminosity thresholds, a surface with high purity reaches the limit

of surface color mode at lower luminance level. Thus, if we take a strategy to determine

the brightness of colored stimuli in comparison to the theoretical upper-limit luminance

at the chromaticity we could account for why the Helmholtz-Kohlrausch effect exists.

Uchikawa et al. (2001) directly focused on this relationship and argued that saturated

colors appear brighter because visual system knows that it has a lower limit and

brightness might be determined in proportion to the theoretical upper-limit luminance.

Identifying the range of natural colors has been one major focus especially in the field of

color science (Pointer, 1980). While the limit of chromaticity has been well characterized,

little is known regarding the luminance limit. In this study, we used SOCS reflectance

dataset as a reference to draw an upper-luminance boundary for real objects. The

database covers a wide range of color space as it includes man-made materials such as

ink which can have narrow-band reflectances. We do not intend to claim that SOCS

dataset in any sense represents all plausible natural reflectance spectra. Yet, our

separate analysis based on 16 hyperspectral images (Nascimento, 2002, Foster 2006)

showed that colors in those images were mostly covered in the gamut of SOCS dataset.

Also, to our knowledge we have not encountered other dataset that has a larger color

gamut than SOCS dataset. We also found that if we restrict samples to natural objects,

the color gamut largely shrinks (see Figure 2 (b) in Morimoto 2016) and upper-limit

luminance estimated from such sample would not predict obtained luminosity thresholds

in this study. Also, in this study, we used a smoothed upper-limit luminance. If we instead

use a raw unsmoothed data, the correlation coefficient lowered in almost all tested

conditions. These results show that a precise evaluation of the abundance of reflectance

samples in real world seems to play a key role in understanding the luminosity percept.

When more reflectance datasets become available in future, the gamut of real objects

should be re-evaluated.

In summary, our results suggested that there is a mysterious relationship between

luminosity threshold and optimal colors. Yet it is difficult to make a conclusive statement

as to whether the optimal color model is better in accounting for luminosity thresholds

than real object model. This is partially because the optimal color locus well resembles

the locus of real objects, leading to high correlation between predictions from two models.

Furthermore, an intrinsically more challenging question would be that how our visual

system learns the optimal color locus even though optimal colors do not exist in the real

world. Considering this point, one plausible theory would be that our visual system

empirically learns natural color distributions through seeing colors in a daily life and

develops the heuristic gamut of surface colors. Then, a given surface appears self-

luminous when its luminance exceeds this heuristic upper-limit luminance. As argued

above, SOCS dataset does not fully represent all real reflectance that can exist, and it is

possible that the real gamut is larger than our estimation. As we have more surfaces, the

gamut of surface color expands, and in theory it will eventually converge to the optimal

color distribution. There is a report that Japanese monkeys (Macaca fuscata) raised only

under monochromatic light do not develop color constancy (Sugita, 2004). Our current

study also presents a potential link between our perceptual judgment and importance of

learning natural scene statistics available in the real world.

Supplementary Material

Figure S1 shows individual observer settings in Experiment 2. There are some individual

variations but overall trend was similar across individuals.

808
Figure S1: Individual observer settings in Experiment 2. Colored square symbols indicate
averaged setting across 10 repetitions for each observer. The error bar indicates ± S.E
across 10 repetitions. The magenta circle symbols denote the optimal color locus and
the blue line shows the real objects locus. The vertical dashed line shows the
chromaticity of the test illuminant. The black cross symbol indicates mean LMS value
across surrounding stimuli. Notice that the horizontal range differs across panels.
815

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Data access

823   The raw experimental data will be available at a data repository. Codes to reproduce

824   figures will be available at https://github.com/takuma929 at the time of publication.

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