Luminosity thresholds of colored surfaces are determined by their heuristic upper-limit luminances in the visual system

Takuma Morimoto[1]*, Ai Numata[2], Kazuho Fukuda[3] and Keiji Uchikawa[4]

1: Department of Experimental Psychology, University of Oxford, Oxford, UK

2: Department of Information Processing, Tokyo Institute of Technology, Yokohama, Japan

3: Department of Information Design, Kogakuin University, Tokyo, Japan

4: Human Media Research Center, Kanagawa Institute of Technology, Atsugi, Japan

*Corresponding author: takuma.morimoto@psy.ox.ac.uk

Address: New Radcliffe House, Radcliffe Observatory Quarter, Woodstock Road, Oxford OX2 6GG

Keywords: Luminosity threshold, Color vision, Optimal color

Abstract

We typically have a fairly good idea whether a given object is self-luminous or illuminated, but it is not fully understood how we make this judgement. This study aimed to identify determinants of the luminosity threshold, a luminance level at which a surface begins to appear self-luminous. We specifically tested a hypothesis that our visual system knows the maximum luminance level that a surface can reach under the physical constraint that a surface cannot reflect more light than any incident light and applies this prior to determine the luminosity thresholds. Observers were presented with a 2-degree circular test field surrounded by numerous overlapping colored circles and luminosity thresholds were measured as a function of (i) the chromaticity of the test field, (ii) the shape of surrounding color distribution and (iii) the color of the illuminant of the surrounding colors. We found that the luminosity thresholds peaked around the chromaticity of test illuminants and decreased as the purity of the test chromaticity increased. However, the

loci of luminosity thresholds across chromaticities were nearly invariant to the shape of

the surrounding color distribution and generally resembled the loci drawn from theoretical

upper-limit luminances and upper-limit luminance boundaries of real objects. These

trends were particularly evident for illuminants on the black-body locus and did not hold

well under atypical illuminants such as magenta or green. These results support the idea

that our visual system empirically internalizes the gamut of surface colors under natural

illuminants and a given object appears self-luminous when its luminance exceeds this

heuristic upper-limit luminance.

1. Introduction

Most objects in the real world are visible because they reflect light. Some objects

however emit light themselves; such self-luminous objects typically have a distinct

appearance (e.g., traffic lights visually stand out in a scene). However, any light reaching

our retina is indiscriminately encoded by three classes of cone signals regardless of

whether the light is reflected from a surface or directly emitted from a light source. Thus,

judging whether a given object is self-luminous presents a mathematically

underdetermined problem to the visual system. The goal of this study is to reveal how

our visual system overcomes this computational challenge and generates a luminous

percept.

Self-luminous objects normally have a glowing appearance distinct from the appearance

of illuminated surfaces. This qualitative difference was formally introduced as a mode of

color appearance (Katz, 1935). The original description finely discriminates various

categories, but this study concerns two modes: surface-color mode and aperture-color

mode, which respectively correspond to the qualities of color appearance for an illuminated surface and a self-luminous object. Color appearance has mostly been studied in the surface-color mode; only a limited number of studies have investigated the nature of the aperture-color mode (e.g., Uchikawa, Uchikawa & Boynton, 1989).

One common approach is to measure the transition luminance between surface-color mode and aperture-color mode, which is known as the *luminosity threshold.* Past studies have investigated what factors might govern this threshold. In an early study, Ullman (1976) extensively discussed potential determinants of luminosity thresholds: highest intensity in a scene, absolute intensity of the stimulus, local or global contrast, intensity comparison with the average intensity of the scene, and lightness computation that emphasizes a transient intensity change over space while ignoring a gradual intensity change. It was concluded that although each factor plays a role, none of these factors are sufficient to predict luminosity thresholds. Bonato & Gilchrist (1994) reported quantitative observations that an achromatic surface appears luminous when it has roughly 1.7 times the luminance of a surface that would be perceived as white. For chromatic stimuli, it was repeatedly shown that luminosity thresholds were negatively correlated with stimulus purity in a series of studies (Evans, 1959; Evans & Swenholt, 1967; Evans & Swenholt, 1968; Evans & Swenholt, 1969). Speigle & Brainard (1996) measured luminosity thresholds using real colored objects placed under illuminants of different color temperatures. They supported Evans's consistent observation about the chromaticity-dependent nature of luminosity thresholds and showed that the color of the illuminant also affects luminosity thresholds. More recently, Uchikawa et al. (2001) pointed out that the brightness of colored surfaces rather than their physical luminance

is highly correlated with the luminosity thresholds of colored surfaces. These studies well

characterized the properties of a test stimulus and of surrounding contexts that have an

impact on luminosity thresholds.

One important open question in the field is whether our visual system bases self-

luminous judgements purely on heuristics that extract statistics from the external world.

Such a strategy is prevalent in many other visual judgements. For example, the famous

anchoring theory determines a reference based on simple statistics in a given scene (i.e.,

the highest luminance in a scene is defined as white) which has been successful in

explaining empirical results involving lightness judgements (Gilchrist & Bonato, 1995;

Gilchrist et al. 1999). If our visual system takes a heuristic-based strategy, luminosity

thresholds should be susceptible to scene content – for example a combination of

surface reflectances that happen to be present in a scene. Alternatively, the visual

system might additionally use an internal reference for luminosity judgements that is

more robust to the variety of available scene contents. For instance, it was shown that

our visual system might use statistical regularities about the possible range of surface

colors and illuminant colors (Judd et al., 1964) as a prior to solve an ill-posed problem

such as color constancy (Maloney & Wandell, 1986). Also, there are suggestions that

color contrast and assimilation arise simply from learning statistical regularities in

external environments (Lotto & Purves, 2000; Long & Purves, 2003). The success of

these prior-based approaches implies a possibility that humans might take a similar

strategy when making self-luminosity judgements.

Thus, one primary focus in this study is to reveal whether luminosity thresholds are

determined purely based on rigid heuristics that rely on the statistics of external stimuli

or whether the visual system additionally uses internal references to make a luminosity

judgement. We specifically built a hypothesis based on the latter view: the visual system

internalizes the physical gamut of surface colors under various illuminants (i.e., optimal

colors introduced in MacAdam (1935a, 1935b), detailed in the General Method section)

and refers to this knowledge when judging whether a given surface is self-luminous. It is

assumed that the visual system estimates the illuminant color and chooses the gamut

under the estimated illuminant. In a more general sense, this hypothesis could be treated

as a Bayesian framework where the visual system monitors the scene illuminant and

selects which prior to use based on the estimated illuminant. This hypothesis was

specifically designed based on observations made in a series of color constancy

experiments (Uchikawa et al, 2012; Fukuda & Uchikawa 2014; Morimoto et al, 2016;

Morimoto et al, 2021). In these studies, we developed a model for illuminant estimation

that operated on the assumption that the visual system internalizes the gamut of surface

colors under various illuminants (i.e., distribution of optimal colors) and the model

accounted for observers' estimations of illuminants reasonably well in a variety of

conditions. One interpretation of luminosity thresholds is that the visual system takes the

upper-limit boundary of surface colors as the point beyond which objects are self-

luminous. Thus, we speculated that the loci of luminosity thresholds measured under

different illuminants might resemble the locus of optimal colors.

We note that this study is also built on previous efforts made by Evans (1958) and Speigle

and Brainard (1996) for the following reasons. Evans (1958) in part of his analyses first

made a comparison between luminosity thresholds and the optimal color locus, which is

the primary purpose of this study. Though it was concluded that luminosity thresholds do

not well align with optimal color locus, the research used a simple stimulus configuration

where a colored surface was presented with a uniform background. Thus, we believe it

is worth testing the accountability of the optimal color model under a wider variety of

conditions where richer cues to the illuminant are provided. Speigle and Brainard (1996)

was the first study to directly suggest that luminosity thresholds are strongly influenced

by illuminant color. They further modeled observers' luminosity thresholds using the

upper-limit luminance of physically plausible surfaces in the real world estimated by a

linear model that uses basis reflectance functions obtained via a principal component

analysis of Munsell papers. The locus obtained via their method corresponds to a

practical upper-limit luminance in the real world as opposed to a theoretical upper-limit

luminance defined by optimal colors. Nevertheless, we believe that their suggestion

shows conceptual similarity to our hypothesis.

In this study, we conducted three experiments to test our hypothesis. In each experiment,

we presented a 2-degree circular colored test field surrounded by many overlapping

colored circles. We measured luminosity thresholds as a function of test chromaticities.

Experiment 1 was designed to test the degree to which luminosity thresholds were

influenced by the color statistics of surrounding stimuli, in this case the geometry of the

color distribution. In Experiment 2, we tested the effect of the illuminant as well as the

shape of the surrounding color distribution to reveal whether the luminosity threshold loci

agree with the optimal color locus under different illuminants (3000K, 6500K and

20000K). In Experiment 3, we measured the loci of luminosity thresholds under atypical

illuminants (magenta and green) to investigate whether the loci of luminosity thresholds

over chromaticities might differ between chromatically typical and atypical illuminants.

2. General Method

2.1. Computation of physical upper-limit luminance at a given chromaticity

We can compute the theoretical upper-limit luminance at each chromaticity by calculating

the chromaticity and the luminance of its optimal colors. Here we provide a basic idea of

optimal color, but a more detailed description is available elsewhere (e.g., Uchikawa et

al., 2012, Morimoto, et al., 2021). An optimal color is a hypothetical surface having a

steep spectral reflectance function as shown in Figures 1 (a) and (b). There are two types

(band-pass and band-stop) and they can have only 0% or 100% reflectances. Changing

λ_1 and λ_2 generates numerous optimal colors ($\lambda_1 < \lambda_2$). To give concrete examples we

generated three illuminants of black body radiation (Figure 1 (c)). Then 102,721 optimal

colors were rendered under these illuminants as shown by small dots in Figures 1 (d)

and (e). Panel (d) shows L/(L+M) in MacLeod-Boynton (MB) chromaticity diagram

(MacLeod & Boynton, 1979) vs luminance distributions. Panel (e) shows $\log_{10}$S/(L+M)

vs. luminance distributions. To calculate cone excitations, we used the Stockman &

Sharpe cone fundamentals (Stockman & Sharpe, 2000).

In the real world surface reflectances must be less than 1.0 at any wavelength due to

physical constraints, and thus an optimal color has a higher luminance than any other

surface that has the same chromaticity. Thus, no real surface can exceed this optimal-

color distribution. To show this concretely, in Figures 1(d) and (e) are 49,667 objects from

the standard object color spectra database for color reproduction evaluation (SOCS,

ISO/TR 16066:2003).

From optimal color distributions we see that the physical upper-limit luminance is dependent on the chromaticity. The peak of an optimal color distribution always corresponds to a full-white surface (1.0 reflectance across all wavelengths), which thus corresponds to the chromaticity and intensity of the illuminant itself (so-called white point of the illuminant). For this reason, when the color temperature of the illuminant changes, the whole optimal color distribution shifts towards the chromaticity of the illuminant without drastically changing its overall shape. Optimal colors with a higher purity have lower luminance, as they have a narrower-band reflectance, and consequently the distribution spreads out as the purity increases. Importantly, once all optimal colors are calculated, we can look for the physical upper-limit luminance at any chromaticity by looking for the luminance of the optimal color at that chromaticity. Interestingly it is notable that the distribution of real objects (SOCS dataset) shows a somewhat similar shape to the optimal color distribution.

Figure 1: (a), (b) Example optimal colors of band-pass and band-stop types, respectively. (c) Three illuminants defined based on Planck's radiation law. (d), (e) L/(L+M) vs. luminance and $\log_{10}$S/(L+M) vs. luminance distributions, respectively, for optimal colors and the SOCS reflectance dataset rendered under 3000K, 6500K and 20000K.

2.2. Estimation of the upper-limit luminance at a given chromaticity for real surfaces

The theoretical upper-limit luminance can be computed through the calculation of optimal colors, but the upper-limit luminance for real objects needs to be estimated. Thus, we analyzed 49,672 surface reflectances from the SOCS reflectance database. This dataset includes reflectances from a wide range of categories of natural and man-made objects: "photo" (2304 samples), "graphic" (30,624), "printer" (7856); "paints" (229); "flowers" (148); "leaves" (92); "faces" (8049); and "Krinov datasets" (370) including natural objects

which were measured in a separate study (Krinov, 1947). We then excluded reflectances

that contained a value higher than 1.0 at any wavelength as they might include

fluorescent substances. As a result, one reflectance from the printer category and 4

reflectances from the paints category were excluded.

The remaining 49,667 surfaces were then rendered under 6500K and their chromaticity

and luminance were calculated. The luminance value was normalized by that of a full-

white surface (100% reflectance at any wavelength). As shown in Figure 2 (a), we plotted

the chromaticity of all surfaces on the MacLeod-Boynton chromaticity diagram, where

$L/(L+M)$ is the horizontal axis and $\log_{10} S/(L+M)$ is the vertical axis. We defined a grid of

25×25 bins and classified 49,667 colors into corresponding bins. Then, for each bin, the

maximum luminance across all colors that belong to the bin was defined as the upper-

limit luminance of real objects. This procedure was repeated for all 625 bins. The left and

center subpanels in panel (b) show the upper-limit luminance for optimal colors (for

comparison purposes) and for real objects. As seen here the loci of the upper-limit

luminance for real objects were not smooth. We assumed that this is an artifact due to

the limited availability of reflectance samples in the database rather than the nature of

reflectances of real objects. Thus, we smoothed the upper-limit luminances by spatial

filtering with 3×3 convolutional filters (each pixel has the value of 1/9). The right subpanel

depicts the smoothed data. Note that this upper-limit luminance heatmap is dependent

on the color of the illuminant. Thus we repeated the same procedure for other black-body

illuminants with color temperatures from 3000K to 20000K with 500 K steps. Both the

optimal color locus and real object locus unsurprisingly peak at the chromaticity of the

illuminant shown by the red cross symbol. The upper-limit luminance of real objects

decreases more sharply as the stimulus purity increases than that of optimal colors. We

can refer to these look-up-tables to find the upper-limit luminance of real objects for an

arbitrary chromaticity under illuminants of a range of color temperatures. Note that this

model corresponds to the proposed model by Speigle and Brainard (1996) at a

conceptual level though they estimated the boundary using a linear model rather than

the 'big data' approach taken here.

Figure 2: How to estimate the upper-limit luminance for real objects using the SOCS

spectral reflectance dataset. A 25×25 grid was first drawn on the MacLeod-Boynton

chromaticity diagram. For each grid bin, we searched for the surface that has the highest

luminance as shown in the right part of panel (a), which was defined as the upper-limit

luminance for that chromaticity bin. (b) From left to right, the locus of upper-limit

luminance for optimal color, real objects (raw), and real objects (smoothed) under 6500K

illuminant. The lightness indicates the upper-limit luminance for the chromaticity bins.

The pale green color indicates that there is no data in that bin.

2.3. Observers

Four observers (KK, MI, TM and YK) participated in Experiment 1. KK and YK were also

recruited for Experiment 2 as well as two new observers (KS and NT). KK, KS and YK

participated in Experiment 3. Observers except for KS were naïve to the purpose of all

experiments. Observers' ages ranged between 22 and 57 (*mean* 31.4, *s.d.* 13.2).

Observers were all Japanese. All observers had corrected visual acuity and normal color

vision as assessed by Ishihara pseudo-isochromatic plates.

2.4. Stimulus Configuration

The stimulus configuration is shown in Figure 3. The color distribution of the surrounding

stimuli and the chromaticities used for the test field are detailed in each experimental

section. The spatial pattern was shuffled for each trial.

Figure 3: Example of stimulus configuration. The center circle is the test stimulus, and

its luminance was adjusted by observers. Each circle had a diameter of 2 degrees in

visual angle, and the whole image subtended 15×15 degrees. The surrounding color

distribution is detailed in each experimental section.

2.5. Apparatus

Data collection was computer-controlled and all experiments were conducted in a dark room. Stimuli were presented on a cathode ray tube (CRT) monitor (BARCO, Reference Calibrator V, 21 inches, 1844 × 1300 pixels, frame rate 95Hz) controlled with ViSaGe (Cambridge Research Systems), which allows a 14-bit intensity resolution for each of the RGB phosphors. We performed gamma correction using a ColorCAL (Cambridge Research Systems) and spectral calibration was performed with a PR650 spectroradiometer (Photo Research inc.). Observers were positioned 114 cm from the CRT monitor and the viewing distance was maintained with a chin rest. Observers were asked to view the stimuli binocularly.

2.6. General procedure

Observers first dark-adapted for 2 mins and then adapted to an adaptation field for 30 seconds. The adaptation field was the full uniform screen that had either a chromaticity of 6500K (Experiments 1 and 3) or the chromaticity of the test illuminant (Experiment 2), and in either case the luminance was equal to the mean luminance value across surrounding stimuli. Then, the first trial began. We drew surrounding stimulus circles so that they had a specific color distribution as detailed in each experimental section. The 2-degree circular test field was presented at the center of the screen. The test field was never occluded by surrounding stimuli. The observers' task was to adjust the luminance of the test field to the level at which the surface-color mode changed to the aperture-color mode using a keyboard with three possible luminance steps (± 0.5, ± 1.0, or ± 5.0 cd/m^2). The ambiguity regarding the criterion to judge the transition between surface-color mode and aperture-color mode was reported in a past study (Speigle & Brainard,

1996, Uchikawa et al., 2001). This is mainly because the transition is not sharp, and

there is a range that a surface can appear a mixture of surface-color mode and aperture

color mode. Considering this reported ambiguity, we instructed observers as follows:

"Your task is to adjust the luminance of the center test field so that the test field appears

to be at the midpoint between the upper-limit of the surface color mode and the lower-

limit of the aperture color mode." The upper-limit of the surface color mode and the lower-

limit of the aperture color mode were described to observers as the limit at which the test

field completely appears as an illuminated surface and the limit at which the test field

completely appears as a light source, respectively. All observers agreed that this was a

reasonable judgment. Also, we note that our criterion is analogous to criteria used in past

studies (Bonato & Gilchrist,1994; Evans, 1959; Evans & Swenholt, 1967, 1968, 1969;

Speigle & Brainard, 1996; Ullman, 1976). During the experiments, observers were

instructed to view the whole stimulus rather than fixate at a specific point to avoid local

retinal adaptation. The initial luminance value for the test field was randomly chosen from

2.0, 5.0, 8.0, 11.0, 14.0, 17.0, 20.0, 23.0, 26.0 and 29.0 cd/m^2. Specific experimental

conditions are detailed in each experimental section.

3. Experiment 1

3.1 Surrounding color distribution, test illuminant and test chromaticity

In a natural scene, the colors of objects tend to cluster around the white point of the

illuminant and the density of colors decreases as purity increases. Consequently, the

color distribution tends to form a mountain-like shape as shown in Figure 1 (d). The aim

of Experiment 1 was to investigate how the loci of luminosity thresholds change when

thresholds are measured in a scene that has an atypical color distribution shape. In an

extreme case where observers rely purely on internal criteria to judge the self-luminosity

of a surface, luminosity thresholds should not change at all regardless of the surrounding

color distribution. However, in contrast if observers make a self-luminous judgement

using surrounding colors, for example by estimating the upper luminance boundary from

the surrounding distribution, luminosity thresholds should largely change depending on

the shape of the surrounding color distribution.

Figure 4 (a) shows the five surrounding color distributions used in Experiment 1. The

6500K illuminant on the black-body locus was chosen as the test illuminant in this

experiment. We first defined the *natural* color distribution in the upper-left subpanel and

then transformed the distribution to generate 4 atypical color distributions (*reverse*, *flat*,

slope+ and *slope-*) in the following ways. First, to construct the *natural* color distribution,

we started with a dataset of 574 spectral reflectances of natural objects (Brown, 2003).

Out of the 574 reflectances, 516 reflectances were inside the chromaticity gamut of the

experimental CRT monitor when rendered under the 6500K test illuminant. All stimuli

were presented via a ViSaGe, which had the technical constraint that only 253 colors

could be simultaneously presented. Thus, we selected 253 reflectance samples out of

516 reflectances. The reflectance spectra in the Brown dataset were clustered around a

white point in a chromaticity diagram; therefore, if we randomly sample from those

spectra, it generates a biased distribution with more data points around the white point.

Thus the 253 reflectances were selected such that, when rendered under 6500K, they

were approximately spatially and uniformly distributed across a chromaticity diagram:

$L/(L+M)$ and $S/(L+M)$.

To generate the other color distributions (*reverse*, *flat*, *slope+* and *slope-*), we

independently scaled each of the 253 reflectances by a scalar value to manipulate the

luminance while keeping the chromaticity constant. The inserted image in each subpanel

shows an example of surrounding stimuli that has the corresponding color distribution.

Note that the spatial layout of the surrounding stimuli was shuffled for each trial. For all

distributions, the intensity of the test illuminant was determined so that a full-white

surface (i.e., 100% reflectance across all visible wavelengths) had a luminance of 35.0

cd/m^2 under the test illuminant. We note that surrounding colors had relatively low

luminance values. For the test field to appear self-luminous, the test field needs to have

a substantially higher luminance than the surrounding colors. Thus, the choice of

surround luminances was unavoidable in order to ensure that observers could make a

satisfactory adjustment at any tested chromaticities within the luminance range allowed

by our experimental monitor.

For the center test field, we chose 9 reflectances out of the 253 so that they fell closely

along the black-body locus when placed under a 6500K illuminant. The panel (b) in

Figure 4 shows these 9 test chromaticities at which luminosity thresholds were measured.

The chromaticity of two reflectances are slightly off from the black-body locus. This is

because we could not find reflectance samples that exactly fall on the locus.

Figure 4: (a) 5 color distribution sets for surrounding stimuli. An inserted image at the top

shows an example stimulus configuration for each color distribution. The vertical dashed

black line indicates the L/(L+M) value of 6500K test illuminant. Black cross symbols

indicate mean cone response across all 253 surrounding stimuli. (b) 9 test chromaticities

at which the luminosity thresholds were measured.

3.3 Procedure

One block consisted of 9 settings to measure thresholds at all 9 test chromaticities in

random order. There were 5 blocks in each session to test all 5 distribution shapes. The

order of distribution condition was randomized. All observers completed 20 sessions in

total (i.e., 20 repetitions for each data point). They completed 10 sessions per day and

thus the experiment was conducted in two days.

3.3 Results

Figure 5 shows the results for Experiment 1. Colored symbols with error bars indicate

each observer's setting. Each data point is the average across 20 repetitions. The

average across 4 observers is shown as black circles. There was some variation across

individuals. Furthermore, the experimental design was to try to collect reliable data from

a small number of participants. Thus, we discuss results individually. The magenta circles

and the line show luminances of optimal colors at test chromaticities when rendered

under the test 6500K illuminant (the optimal color locus). In other words, if the visual

system uses the optimal color to judge whether a surface emits a light, the observer's

settings should match the magenta line. The blue circles and the line show a smoothed

upper-limit luminance locus of real objects, estimated from the SOCS reflectance dataset

as shown in Figure 2, which more rapidly decreases as it gets away from the white point

than the optimal color locus does. For simplicity, we hereafter refer to the magenta and

blue lines as predictions of the optimal color model and the real object model,

respectively.

First, the loci of luminosity thresholds for all observers had a mountain-like shape

regardless of surrounding color distribution. The loci generally peaked around the

chromaticity of the test illuminant (the vertical black dashed line) and the luminosity

thresholds decreased as the test chromaticity moved away from the white point. Although

there were some individual differences, especially in the overall setting level (e.g., KK

generally had higher thresholds than others) and in the peak chromaticity, the luminosity

thresholds generally seem to more resemble the prediction of the optimal color model

than that of the real object model in this experiment. This is consistent with the hypothesis

that the visual system knows the upper boundary of the optimal color distribution and

judges that a given surface is self-luminous when its luminance exceeds the luminance

of optimal colors.

Figure 5: Colored square symbols indicate averaged settings across 20 repetitions for

each observer. The error bars represent ±1 S.E. across 20 repetitions. The black

circles represent settings averaged across observers (n = 4). The magenta circles

denote the luminance of the optimal color at the test chromaticities and thus indicate

the physical upper-limit luminance. The blue line shows the upper-limit luminance of

real objects estimated from the SOCS reflectance dataset. The vertical dashed line

shows the chromaticity of the test illuminant (6500K). The black cross symbol indicates

the mean LMS value across surrounding stimuli.

To quantify the similarity between observers and models, we calculated Pearson's

correlation coefficient between observer settings and model predictions over the 9 test

chromaticities. Figure 6 shows summary matrices of the correlation coefficients. We

calculated correlation coefficients for each observer and discuss them on an individual

basis.

The magenta and blue symbols represent the optimal color model and the real object

model, respectively. In addition, we evaluated a model which judges the surface as

self-luminous when its luminance exceeds that of the surrounding color distribution.

The luminosity thresholds estimated from such a model should show much similarity to

the shape of the surrounding color distribution. For example, in the *reverse* condition,

the luminosity threshold should be lowest at the white point and increase as the

saturation of the test stimulus increases. This model is labelled as the "surrounding

color" model in Figure 6. Note that this is a simplistic model and we are not trying to

claim that the visual system takes such a strategy. Instead, our goal here is to build a

framework in which we quantitatively predict an observer's behavior if she/he judges

the luminosity thresholds solely based on surrounding stimuli presented in each trial

without using any prior about the statistics of the real world.

The cyan star symbols in some cells indicate the highest correlation-coefficient value

across the 3 tested models. The cyan arrows below each subpanel indicate the model

that received the highest number of cyan stars across the 4 observers.

Overall, since the observer settings are stable across all distribution conditions, the

correlation coefficient patterns are also similar between the optimal color and real

object models whose predictions are both not affected by surrounding colors. However,

the correlation coefficients for the surrounding color model strongly depend on

distribution condition as predicted. Specific trends are as follows. For observers KK and

MI, the loci of the luminosity thresholds showed the highest correlation with the optimal

color model for all distributions. For TM, the real object model was the best predictor in

all distributions except for the *flat* condition. For YK, the optimal color model showed

the highest correlation for *reverse*, *flat* and *slope+* conditions while the real object

model showed the highest correlation for *natural* and *slope-* conditions. If we

summaries these trends based on the number of cyan arrows each model received, the

optimal color model is the best predictor in Experiment 1.

Figure 6: The matrices of Pearson's correlation coefficients calculated between

observer settings and model predictions over 9 test chromaticities. Each subpanel

represents each distribution condition (*natural*, *reverse*, *flat*, *slope+* and *slope-*). The

color of each individual cell indicates the correlation coefficient as denoted by the color

bar. The cyan star symbol indicates the highest correlation coefficient across the 3

models. The cyan arrows at the bottom of each subpanel show the model that received

the highest number of cyan star marks, indicating a good candidate model of human

observers' strategy to judge the self-luminosity of a surface.

The major finding in this experiment is that the loci of luminosity thresholds are nearly

invariant regardless of the shape of the surrounding color distribution. This result

supports the idea that observers use an optimal color distribution as an internal reference

to determine the luminosity thresholds. In the Appendix, we also provide two other

alternative models that predicts luminosity thresholds based on post-receptoral signals

or cone signals of the test field alone, but it was shown that these models did not predict

the luminosity threshold well in Experiment 1. In Experiment 2, we tested whether this

observation holds under different illuminants which shift the peak of the optimal color

distribution as shown in Figure 1. If the visual system indeed uses optimal colors,

changes in luminosity thresholds should reflect changes in the optimal color distribution.

4. Experiment 2

4.1 Surrounding color distribution, test illuminant and test chromaticity

We employed *natural*, *reverse* and *flat* distributions of surrounding colors. For test

illuminants, we used 3000K, 6500K and 20000K on the black-body locus whose spectral

distributions are shown in panel (c) of Figure 1. Out of the 253 reflectances we used in

Experiment 1, only 180 samples were inside the chromaticity gamut of the experimental

CRT monitor under all test illuminants and those 180 samples were used as surrounding

stimuli in Experiment 2. Panel (a) in Figure 7 shows all 9 test surrounding conditions (3

distributions × 3 test illuminants). Though we found that surrounding color distribution

has no systematic effects on luminosity thresholds in Experiment 1, we again

manipulated the distribution shapes in Experiment 2 to investigate if this finding held

under different illuminants.

We then selected 15 surface reflectances from the 180 reflectances. Panel (b) shows

the 15 test chromaticities when rendered under each test illuminant at which the

luminosity threshold was measured.

Figure 7: (a) 9 color distributions for surrounding stimuli (3 test illuminants × 3

distributions). Inserted image shows an example stimulus configuration. The vertical

dashed black line indicates the L/(L+M) value of each test illuminant. Black cross

symbols indicate mean cone response values across the 180 surrounding stimuli. (b)

15 test chromaticities at which the luminosity threshold was measured.

4.2 Procedure

One block consisted of 15 consecutive settings to measure thresholds for all test

chromaticities presented in random order. There were 9 blocks in one session to test all

conditions (3 illuminants × 3 distributions). The order of conditions was randomized. All

observers completed 10 sessions in total. The experiment was conducted in three days.

4.3 Results

The black line in Figure 8 shows the mean setting across 4 observers. The rest of the

data presentation follows the results in Experiment 1. For clarity, only the averaged

setting is shown here, but the individual observers' data is presented in Figure A1 in the

Appendix.

First, the mean settings showed that the loci of luminosity thresholds were again

mountain-like in shape, and the influence of the shape of the surrounding color

distribution was almost absent, supporting the findings in Experiment 1. It is also

noticeable that the peak chromaticity of the mean setting in each panel shifted towards

the illuminant chromaticity shown as vertical dashed lines.

Figure 8: The black circle symbols represent averaged observer settings (n = 4). The

error bars represent ±1 S.E. across the 4 observers. The optimal color loci are plotted

as magenta circles. The blue circles show the upper-limit luminance of real objects.

The red, black and blue vertical dashed lines show the chromaticities of the 3000K,

6500K and 20000K test illuminants, respectively. The black cross symbol indicates the

mean LMS value across surrounding stimuli. Individual observer data is shown in the

Appendix. The region surrounded by a rectangle in the 20000K condition is further

discussed in Figure 9.

It should be noted that the peak chromaticity of the luminosity threshold loci for 20000K

was slightly shifted to the right along the L/(L+M) dimension from the chromaticity of the

test illuminant. This trend was generally consistent across observers as shown in Figure

A1 (Appendix). One potential reason could be that observers misestimated the illuminant

color from the surrounding colors. Human color constancy is often imperfect, and thus

we speculated that observers' luminance settings might better agree with the optimal

color or real object model rendered under an illuminant estimated by each observer

instead of a ground-truth illuminant (20000K). In fact, misestimates of illuminant color

was also reported be an important factor in predicting luminosity thresholds by Speigle

and Brainard (1996). The estimated illuminant is typically measured using a technique

such as achromatic adjustment (Brainard, 1998), but these data were not collected in

this study. Thus, we assumed that the peak chromaticity of observer settings indicated

the observer's estimated illuminant.

We first calculated the chromaticities of illuminants from 3000K to 20000K in 500K steps.

Then, for each observer and for each condition independently, we searched for the color

temperature that had the closest chromaticity to the peak chromaticity of the luminosity

thresholds. Table 1 summarizes the color temperatures of the estimated illuminants in

each condition. In the 3000K condition, estimated illuminants matched the ground-truth

color temperature for most observers. For 6500K, there was a slight variation across

observers. It is notable that in the 20000K condition observers estimated color

temperatures substantially lower than those of the ground-truth, meaning illuminant color

was estimated to be less blue. This could be because perceptual differences between

stimuli rendered under 20000K and under 6500K is smaller than the difference between

3000K and 6500K, as perceptual sensitivities are reported to be worse for bluish

illuminants and surfaces (Pearce et al., 2014; Winkler et al., 2015).

Table1: Estimated illuminant by each observer judged from the chromaticity at which

luminosity thresholds peaked. The top row shows the color temperatures of ground-

truth illuminants, and the other numbers indicate the color temperature of estimated

illuminants.

		3000K	6500K	20000K
Natural	KK	3000	5500	10500
	KS	3000	7000	8500
	NT	3000	5000	10500
	YK	3000	5500	12000
Reverse	KK	3000	6500	7500
	KS	4000	7000	7500
	NT	3000	5500	12000
	YK	3500	5000	10500
Flat	KK	3000	7000	8500
	KS	3000	5000	8500
	NT	3000	5500	12000
	YK	3000	6500	12000

Then, we drew optimal color loci under these estimated color temperatures. This concept

is depicted in Figure 9. Intuitively speaking this procedure allows us to estimate an

optimal color locus that the observer presumably used during the task, so that the peak

of this new optimal color locus coincides with the peak of the measured locus of

luminosity thresholds. The pale magenta curve shows the optimal colors under the

estimated illuminant and seems to predict mean observer settings better than the optimal

color locus under the ground-truth illuminant (20000K).

Figure 9: Optimal color models based on the ground-truth illuminant (magenta) and

based on estimated illuminants for the averaged observer setting (pale magenta). It is

shown that observers' settings are better explained by the optimal color model that

allows misestimation of illuminants by observers.

Figure 10 depicts the correlation coefficient matrices for all conditions. We compared

correlations from 5 models: (i) the optimal color model and (ii) the real object model

under the ground-truth illuminant, (iii) the optimal color model and (iv) the real object

model under the estimated illuminant, and (v) the surrounding color model. Again, the

cyan star symbol in some cells denotes the highest correlation across the 5 models for

that participant. The cyan arrows below each subpanel point to the model that has the

highest number of cyan stars – the overall best model for that condition.

Figure 10: The matrices of Pearson's correlation coefficient calculated between

observer settings and model predictions over 15 test chromaticities. The cyan star

symbol indicates the highest correlation coefficient across the 5 models. The cyan

arrows at the bottom of each subpanel show the model that received the highest

number of cyan star symbols.

Overall, the surrounding color model does not show high correlation with observer

settings in any condition, agreeing with the trends in Experiment 1. The optimal color

model and the real object model seem to show high correlation, and it depends on the

condition which model correlates better. For the *natural*-3000K condition, the highest

correlation was found for the real object model, consistently across all observers. For

the *reverse*-3000K condition, all observers except NT were best correlated with the

optimal color model under the estimated illuminant while for the *flat*-3000K condition

the votes were split between the optimal color and real object models. For *natural*-

6500K, KS and NT were well predicted by the optimal color model under the ground-

truth illuminant, but the other two observers were better correlated with the real object

model. For the *reverse*-6500K condition, the optimal color and the real object model

both showed high correlations. The real object model, when used with the estimated

illuminant, predicted observer settings best for the *flat*-6500K condition. It is notable

that for the 20000K condition, the optimal color model under the estimated illuminant

was consistently the best predictor. The optimal color model under the ground-truth

illuminant also shows much lower correlations, suggesting that considering observers'

misestimates of the illuminant plays a role in predicting luminosity thresholds. In

summary both the optimal color model and the real object model showed fairly good

agreement with human observers' settings.

Experiments 1 and 2 collectively suggested that both the optimal color locus and the

real object locus seemed to be good candidate determinants of luminosity thresholds.

We also note that two other alternative simplistic models again did not predict

luminosity thresholds well in Experiment 2 (shown in Appendix). One noteworthy

feature in Experiments 1 and 2 is that we used illuminants on the blue-yellow axis that

are typically found in natural environments. We also used chromaticities on the black-

body locus for the test field. If we assume that the visual system learns the locus of

optimal color distribution or real object distribution by observing colors in natural

environments, the luminosity thresholds under atypical illuminants may not agree well

with the prediction of the optimal color model or the real object model. We directly

tested this hypothesis in Experiment 3.

5. Experiment 3

Experiment 3 tested whether luminosity thresholds resembled the optimal color locus

under atypical illuminants. We also chose a wider range of test chromaticities from the

black-body locus and a locus that is orthogonal to the black-body locus.

5.1 Surrounding color distribution, test illuminant and test chromaticity

We employed *natural*, *reverse* and *flat* distributions for the surrounding stimuli. For test

illuminants, we used magenta and green illuminants. We chose two color filters (Rosco,

R44 "Middle Rose" and R4460 "Calcolor 60 Green") through which the 6500K illuminant

was passed to obtain the spectra shown in Figure 11 (a). The chromaticities of these

illuminants largely deviate from black-body locus as shown in panel (b). Out of the 574

spectral reflectances of natural objects collected by Brown, 251 reflectances were inside

the chromaticity gamut of the CRT monitor under both illuminants. For the surrounding

stimuli, we sampled 180 reflectances out of the 251 reflectances and created each

distribution following the manipulation used in Experiments 1 and 2. Experiments 1 and

2 showed no effect of surrounding color distribution but Experiment 3 also included this

manipulation to confirm that the findings also held under atypical illuminants.

Figure 11: (a) Spectra for magenta and green illuminants used in Experiment 3. (b)

Chromaticities of both illuminants. The black-body locus and the chromaticity of 6500K

illuminant are shown for comparison purposes.

Panel (a) in Figure 12 shows surrounding distributions for all 6 test conditions (3

distributions $\times$ 2 test illuminants). The intensities of the test illuminants were determined

so that the average luminance across the 180 colors matched 2.5 cd/m^2.

In this experiment, the test chromaticities were chosen so that they varied along two

directions: (i) the black-body locus (shown as circles) and (ii) an axis approximately

orthogonal to the black-body locus (shown as triangles) depicted in panel (b). First, 8

reflectances were selected from the 180 and were used under both illuminant conditions.

Then, we sampled different 5 reflectances separately for each illuminant condition from

the 323 reflectances that can be presented only under either magenta or green illuminant.

Thus, these reflectance samples are not shared between illuminant conditions. This

choice was made to choose test chromaticities on the locus orthogonal to black-body

locus as widely as possible. In panel (b), the 5 data points surrounded by a red edge

represent the 5 reflectances that were not shared between illuminant conditions. There

were 7 chromaticities for each axis, but one chromaticity was used for both axes (plotted

as a black square). The chromaticities of natural objects tend to spread along the black-

body locus, and the purpose of this design was to test whether luminosity thresholds

measured at atypical chromaticities would deviate from the prediction of the optimal color

model or the real object model.

Figure 12: (a) 6 color distributions for surrounding stimuli (2 test illuminants × 3 distributions). Inserted image shows an example stimulus configuration. The vertical dashed black line indicates the L/(L+M) value of test illuminant. Black cross symbols indicate mean cone response values across 180 surrounding stimuli. (b) 13 test chromaticities at which the luminosity threshold was measured. Symbols with a red edge indicates reflectances that were not shared between magenta and green illuminants.

5.2 Procedure

One block consisted of 13 consecutive settings and thresholds were measured for all test chromaticities in random order. Each session comprised 6 blocks to test all distribution × illuminant conditions. The order of condition was randomized. All observers completed 10 sessions in total. Observers conducted 5 sessions per day and thus the experiment were completed in two days.

5.3 Results

Figure 13 shows the results. The left 6 panels depict luminosity thresholds measured at chromaticities along the black-body locus (black circles and square in panel (b), Figure 12) while the right 6 panels indicate thresholds at chromaticities along the orthogonal locus (black triangles and square in panel (b), Figure 12).

We first look at the left two columns. For the magenta illuminant condition, observers' settings again show a mountain-like shape. Also, one can see that settings are not dependent on the surrounding color distribution. However, in this condition the optimal color model and the real object model show a relatively flat locus. For the green illuminant, observer settings appear flat. However luminosity thresholds for subject KS show a fairly different trend from the other observers, and the locus is not well predicted by the optimal color locus nor the real object locus, which was not observed in Experiments 1 and 2.

Figure 13: Observer settings in Experiment 3. The left two columns plot luminosity

thresholds measured at test chromaticities on the black-body locus (circle and square

symbols in panel (b), Figure 12). The right two columns show results for test

chromaticities on the locus orthogonal to black-body locus (triangle and square

symbols in panel (b), Figure 12). Colored square symbols indicate averaged settings

across 10 repetitions for each observer. The error bar plots ±1 S.E across 10

repetitions. The black circle symbols plot average observer settings (n = 3). The

magenta circle symbols denote the optimal color locus and the blue circles show the

real object locus. The vertical dashed line represents the chromaticity of the test

illuminant. The black cross symbol indicates the mean LMS value across surrounding

stimuli.

When the test chromaticities are on the axis orthogonal to the black-body locus (right

two columns), for the magenta condition all observers' settings might appear to resemble

the optimal color locus. However, for the green illuminant condition, KS again shows a

different trend from the other observers and observers do not all agree with either model

prediction.

Figure 14 allows us to compare the correlation coefficient across models and conditions.

For the leftmost column, the optimal color model overall showed good correlations for

the *natural* condition, while the real object model showed good correlations for the

reverse and *flat* conditions. For the *natural* condition, one observer (KS, not naïve) had

the highest correlation with the surrounding color model, which was not observed in

Experiments 1 and 2 in which illuminants on the black-body locus were used as test

illuminants. For the second leftmost column, in most cells correlation coefficients

appeared considerably low. Although the optimal color model consistently had the

highest correlation for all distribution conditions (average coefficient across 9 cells is

0.58), the correlation coefficient is not so high if we consider that the correlation for the

optimal color model was 0.901 in Experiment 1 (averaged across 5 distributions $\times$ 4

observers). Also, in Experiment 2, correlations were 0.746 for the optimal color model of

the ground-truth illuminant and 0.837 for the estimated illuminant (average across 9

conditions $\times$ 4 observers in both cases).

For the column second-from-the-right (the magenta illuminant condition), the trend

seemed to be close to that of the test chromaticities on the black-body locus (leftmost

column), but the correlation coefficients overall seemed to be lower. For the green-

natural condition, the surrounding color model shows a high correlation with observers

KK and KS. It is notable that the optimal color model shows nearly zero or even negative

correlations. For the *reverse* condition, the real object model showed the best correlation,

but their values were not high (0.577, average across 3 observers). For the *flat* condition,

we did not find a consistently good model. It may be worth noting that for the green

illuminant condition, correlation coefficients for test chromaticities sampled from the locus

orthogonal to black-body locus are overall lower than those for test chromaticities

sampled from black-body locus.

Figure 14: The matrices of Pearson's correlation coefficient calculated between

observer settings and model predictions over 7 test chromaticities in Experiment 3. The

cyan star symbols indicate the highest correlation coefficient across the 3 models. The

cyan arrows at the bottom of each subpanel indicate the model that received the

highest number of cyan stars.

In summary these results suggested that although the optimal color and real object

models can account for observer settings to some extent, overall coefficient values were

substantially lower than those observed in Experiments 1 and 2. Also the surrounding

color model showed good correlations in some cases. These results might imply that the

visual system does not have a rigid internal reference about upper-limit luminance under

atypical illuminants and sometimes relies on external cues such as the color of the

surrounding stimuli. Also, for green illuminant condition, we found a trend that the

predictions of optimal color model were particularly worse when test chromaticities were

sampled from the axis orthogonal to the black body locus.

Finally, we summarize results from the three experiments to test whether correlation

coefficients of the optimal color model are higher for typical illuminants (Experiments 1

and 2) than atypical illuminants (Experiment 3). For each observer, we averaged the

correlation coefficient of the optimal color model across all condition in Experiments 1

and 2 (14 conditions), which served as a summary statistic for typical illuminants. For the

20000K condition in Experiment 2, we used the correlation coefficient value of the

optimal color model under the estimated illuminant as it predicted observer settings

substantially better than the model under the ground-truth illuminant. We also calculated

averaged correlation coefficients across all conditions in Experiment 3 (8 conditions) per

observer. The averaged correlation coefficients across all observers were 0.879 ± 0.0114

(average ±1 S.D.) for typical illuminants and 0.525 ± 0.155 for atypical illuminants.

Welch's t-test (one-tailed, no assumption about equal variance) showed that the optimal

color model has a significantly higher correlation for typical illuminants than atypical

illuminants ($t(2.01) = 3.94$, $p = 0.0290$). Also we performed the same analysis using

correlation coefficients for the real object model which showed the same trend ($t(2.84) =$

2.93, $p = 0.0326$).

These results are consistent with the idea that human observers empirically learn the

upper-limit luminance through observing colors in natural environments and use the

criterion to judge whether a given surface is self-luminous or not. Since magenta and

green illuminants are uncommon in natural environments, the visual system does not

know the upper limit of surface colors under those illuminants. This interpretation may

explain why predictions from the optimal color model and the real object model did not

well explain observers' luminosity thresholds for atypical illuminants. Moreover, in the

Appendix, we show that a simplistic model predicts the luminosity threshold in

Experiment 3 as well as the optimal color model. A potential interpretation would be that

when the scene illuminant has an atypical color such as magenta or green, the visual

system makes a self-luminous judgement based on simple statistics because visual

system does not internalize the optimal color locus for unfamiliar illuminants.

5. General Discussion

This study investigated potential determinants of luminosity thresholds. Our three

experiments showed that the loci of luminosity thresholds have a mountain-like shape

that peaks around the illuminant color and decreases as stimulus purity increases,

showing a striking similarity to optimal color and real object loci. A simple alternative

strategy which bases judgements on the surrounding color distribution did not explain

observers' settings well. Rather observers seem to hold an internal representation about

what luminance a surface should reach self-luminosity. Moreover, such similarity

between luminosity threshold and optimal color or real object loci was higher when

surfaces were placed under illuminants along the blue-yellow direction than magenta

and green illuminants that are atypical in natural environments. These support an idea

that the visual system empirically internalizes the heuristic gamut of surface colors

through an observation of colors in daily life. Going back to the original question of

whether the visual system relies on a heuristic or Bayesian framework for luminosity

judgements, the present study generally supports the Bayesian hypothesis.

We also note that some properties of the test field we did not consider in the present

study are known to affect luminosity judgement. For instance, it was reported that

surfaces with smaller areas appeared to emit light at lower luminance levels (Bonato &

Gilchrist, 1999). It has also been reported that surround stimuli are more likely to affect

luminosity threshold if the surround stimuli are presented at the same depth as the test

field (e.g., Yamauchi & Uchikawa, 2005). Thus, in future studies, it would be desired to

expand our model to modify the prediction of luminosity thresholds based on factors such

as stimulus size and relative depth in a way that agrees with human luminosity

judgements.

One consistent trend across the three experiments was that observer settings were

above the physical limit (i.e., prediction of the optimal color model) in most cases. We

suspect that there are at least two reasons for this. First, observers' criterion to judge the

luminosity threshold in this study was the midpoint between the upper-limit of the surface

color mode where a test field purely appears as an illuminated surface and the lower-

limit of the aperture color mode where a test field purely appears as a light source. If we

instead used a different criterion, for example to set the luminance so that the test field

appears simply as the upper-limit of the surface color mode, we would have seen a

smaller discrepancy. Second, it is possible that observers overestimated the intensity of

the test illuminant. Just as humans cannot directly access the chromaticity of test

illuminant, the intensity is also not directly known to observers. In fact, in other color

constancy studies (Morimoto, Fukuda & Uchikawa 2016; Morimoto et al., 2021), we have

repeatedly found that observers tend to overestimate illuminant intensities and the

degree of overestimation substantially varied across individuals. When the illuminant

intensity is overestimated, the observers' internal upper-limit luminance should

accordingly increase, which could account for an observed discrepancy between model

predictions and observer settings. Moreover, we also note that the limit drawn by optimal-

color or real-object model corresponds to the upper-boundary as a surface color, but the

models are not designed to exactly predict how the test field should appear when the

luminance of the test field exceeds the predicted value by the models. Thus, it is

inherently difficult to directly compare the model prediction and observers' settings, and

we think that they rather need to be compared relatively (for example, using correlation

coefficient). We also found that individual differences in this study were mainly found in

gain rather than the shape of the observer settings (though for some conditions in

Experiment 3 shape differences were also evident). This individual variation in gain could

also be due to the variability in estimating illuminant intensity. We also suspect that

individuals might have used different criteria to judge the luminosity threshold in the

current task.

Color constancy is often described as a visual ability to identify a surface under different

illuminants. A surface reflects a light, and that reflected light enters our eyes. Because

the reflected light is a product of surface and illuminant components, color constancy is

often framed as a process in which our visual system estimates the influence of the

illuminant. The "brightest is white" heuristic, which assumes that a surface with the

highest luminance provides the closest information about the illuminant color, has been

known as an influential approach in estimating illuminant color (Land, 1977). However,

self-luminous objects do not carry information about the scene illuminant, which might

cause a misestimation of the illuminant if included in a scene. In general, when we

received an intense light from a surface, there are two ways to interpret this. One is that

the surface is placed under an intense illuminant and the other is that the surface is self-

luminous. This example highlights the need for luminous percepts to be incorporated into

the process of color constancy. In fact, Fukuda & Uchikawa (2014) showed that a surface

appearing in aperture-color mode does not have a strong influence on observers'

estimates of the illuminant.

We chose a set of colored circles as experimental stimuli to directly test our hypothesis

while excluding any other cues. However, it is reported that changing a material property

could affect the mode of color appearance (Kuriki, 2015). Also, our experimental stimuli

were simulated to be uniformly illuminated by a single illuminant, but in natural

environments the spectra hitting an object surface changes from one direction to another

(Morimoto et al., 2019). The presence of multiple illuminants means that we need to

consider multiple optimal color distributions, and thus the loci of luminosity thresholds

measured under such an environment might also change. Despite a growing amount of

research on material perception (Fleming, 2013), luminosity perception is little studied in

the field. While our choice of stimuli was necessary for experimental control, it will be

interesting whether our finding can be applied to a wider range of stimuli that have

complex material properties and are illuminated in non-uniform ways.

One closely related phenomenon to self-luminous perception would be brightness

perception of colored objects. The Helmholtz-Kohlrausch effect is that stimuli with high

purity appear to have high brightness even if luminance is kept the same. The effect was

reported under a variety of viewing conditions (Nayatani et al., 1991; Donoforio, 2011).

However, it is unclear why a color with high purity appears brighter. Curiously, as

observed in the present study, the same trend holds for luminosity thresholds: a surface

with high purity reaches the limit of surface color mode at a lower luminance level. Thus,

if we take a strategy to determine the brightness of colored stimuli in comparison to the

theoretical upper-limit luminance at the chromaticity we could account for the Helmholtz-

Kohlrausch effect. Uchikawa et al. (2001) directly focused on this relationship and argued

that saturated colors appear brighter because the visual system knows that it has a lower

limit and brightness might be determined in proportion to the theoretical upper-limit

luminance.

Identifying the range of natural colors has been a major focus especially in the field of

color science (e.g. Pointer, 1980). While the limit of chromaticity has been well

characterized, little is known regarding the luminance limit. In this study, we used the

SOCS reflectance dataset as a reference to draw an upper-luminance boundary for real

objects. The database covers a wide range of color space as it includes man-made

materials such as ink which can have narrow-band reflectances. We do not intend to

claim that the SOCS dataset in any sense represents all plausible natural reflectance

spectra. Yet, our separate analysis based on 16 hyperspectral images (Nascimento,

2002; Foster, 2006) showed that colors in those images were mostly covered in the

gamut of the SOCS dataset. Also, to our knowledge we have not encountered another

dataset that has a larger color gamut than the SOCS dataset. We also found that if we

restrict samples to natural objects, the color gamut largely shrinks (see Figure 2 (b) in

Morimoto et al., 2016), and upper-limit luminance estimated only from natural samples

would not predict obtained luminosity thresholds in this study. Also, in this study, we used

a smoothed upper-limit luminance. We confirmed that if we instead used raw

unsmoothed data, the correlation coefficient was lower in almost all tested conditions.

These results show that a precise evaluation of the abundance of reflectance samples

in real world seems to play a key role in understanding the luminosity percept. When

more reflectance datasets become available in the future, the gamut of real objects may

need to be re-evaluated.

In summary, our results showed a mysterious similarity between luminosity thresholds

and optimal colors. Yet it is difficult to make a conclusive statement as to whether the

optimal color model is better in accounting for luminosity thresholds than the real object

model. This is partially because the optimal color locus well resembles the locus of real

objects, leading to high correlation between predictions from two models. Furthermore,

an intrinsically more challenging question would be how our visual system learns the

optimal color locus because optimal colors do not exist in the real world. Considering this

point, one plausible theory would be that our visual system empirically learns natural

color distributions by seeing colors in daily life and develops a heuristic gamut of surface

colors. Then, a given surface appears self-luminous when its luminance exceeds this

heuristic upper-limit luminance. As argued above, the SOCS dataset does not fully

represent all real reflectances that can exist, and the real gamut could be larger than our

estimation. As we include more surfaces, the gamut of surface color expands, and in

theory it will eventually converge to the optimal color distribution. There is a report that

Japanese monkeys (*Macaca fuscata*) raised only under monochromatic light do not

develop color constancy (Sugita, 2004). Our current study also presents a potential link

between our perceptual judgment and scene statistics in the real world.

Acknowledgement

All authors thank Laysa Hedjar for her careful edit of the language throughout the
manuscript. This work was supported by JSPS KAKENHI Grant Number JP19K22881,
JP17K04503 and 26780413. TM is supported by a Sir Henry Wellcome Postdoctoral
Fellowship awarded from the Wellcome Trust (218657/Z/19/Z) and the Junior Research
Fellowship from Pembroke College, University of Oxford.

Data access

The raw experimental data will be available in a data repository. Codes to reproduce

figures in the main manuscript are available at https://github.com/takuma929.

Reference

Bonato F., & Gilchrist, A. L. (1994). The Perception of Luminosity on Different
Backgrounds and in Different Illuminations. Perception. 23, 9, 991-1006.

Bonato, F., & Gilchrist, A. L. (1999). Perceived area and the luminosity threshold.
Perception & Psychophysics, 61, 786–797.

Brainard. D. H. (1998). Color constancy in the nearly natural image 2 Achromatic loci.
Journal of the Optical Society of America A, 15, 2, 307–325.

Brown, R. Background and illuminants: the yin and yang of colour constancy. in Colour
Perception: Mind and the Physical World, R. Mausfeld and D. Heyer, eds. (Oxford
University, 2003), 247–272.

Buchsbaum, G. (1980). A spatial processor model for object colour perception. Journal
of the Franklin Institute, 310, 1, 1–26.

Donofrio, R.L. (2011). Review Paper: The Helmholtz-Kohlrausch effect. Journal of the
Society for Information Display, 19, 658-664.

Evans, R. M. (1959). Fluorescence and Gray Content of Surface Colors. J. Opt. Soc. Am.
49, 1049-1059

Evans, R. M. & Swenholt, B. K. (1967). Chromatic strength of colors: dominant
wavelength and purity. J. Opt. Soc. Am. 58, 580-584. J. Opt. Soc. Am. 58, 580-584.

Evans, R. M. & Swenholt, B. K. (1968). Chromatic Strengths of Colors, Part II. The

Munsell System. J. Opt. Soc. Am. 58, 580-584.

Evans, R. M. & Swenholt, B. K. (1969). Chromatic Strength of Colors, III. Chromatic

Surrounds and Discussion. J. Opt. Soc. Am. 59, 628-634.

Fleming, R. W. (2013). Material Perception. Annual Review of Vision Science, 3, 365–

388.

Fukuda, K. & Uchikawa, K. (2014). Color constancy in a scene with bright colors that do

not have a fully natural surface appearance. Journal of the Optical Society of America

A, 31, 4, A239–A246.

Gilchrist, A. & Bonato, F. (1995). Anchoring of lightness values in center-surround

displays. Journal of Experimental Psychology: Human Perception and Performance,

21, 6, 1427-1440.

Gilchrist, A., Kossyfidis, C., Bonato, F., Agostini, T., Cataliotti, J., Li, X., Spehar, B., Annan,

V. & Economou, E. (1999). An anchoring theory of lightness perception. Psychological

Review, 106, 795–834.

Judd, D. B., MacAdam, D. L. Wyszecki, G., Budde, H. W., Condit, H. R., Henderson S.

T., and Simonds J. L. (1964) "Spectral distribution of typical daylight as a function of

correlated color temperature," J. Opt. Soc. Am. 54(8), 1031–1040

Kuriki, I. (2015) Effect of material perception on mode of color appearance. Journal of

Vision, 15(8), 4.

Krinov, E. (1947) Spectral reflectance properties of natural formations. Tech. rep.,

National Research Council of Canada. Technical Translation: TT-439.

Land, E. H. (1977). The Retinex Theory of Color Vision, Scientific American, 237, 6, 108

-128.

Long, F., & Purves, D. (2003) Natural scene statistics as the universal basis of color

context effects. Proceedings of the National Academy of Sciences, 100, 25, 15190-

15193.

Lotto, R. B. & Purves, D. (2000) An empirical explanation of color contrast. Proceedings

of the National Academy of Sciences, 97, 23, 12834-12839.

MacAdam, D. (1935a). The theory of the maximum visual efficiency of colored materials.

Journal of the Optical Society of America A, 25, 249–252.

MacAdam, D. (1935b). Maximum visual efficiency of colored materials. Journal of the

Optical Society of America A, 25, 361–367.

MacLeod, D. I. A., & Boynton, R. M. (1979) Chromaticity diagram showing cone

excitation by stimuli of equal luminance. Journal of the Optical Society of America A,

69, 1183–1186.

Maloney, L. T. & Wandell, B. A. (1986) Color constancy: a method for recovering surface

spectral reflectance Journal of the Optical Society of America A, 3, 1, 29–33.

Morimoto, T., Fukuda, K., & Uchikawa, K. (2016) "Effects of surrounding stimulus
properties on color constancy based on luminance balance", Journal of the Optical
Society of America A, 33, 3, A214–A227.

Morimoto, T., Kishigami, S., Linhares, J. M. M., Nascimento, S. M. C., & Smithson, H. E.
(2019). Hyperspectral environmental illumination maps: characterizing directional
spectral variation in natural environments. Optics Express, 27, 32277-32293.

Morimoto, T., Kusuyama T., Fukuda, K. & Uchikawa, K. (2021). Human color constancy
based on the geometry of color distributions. Journal of Vision, 27, 21(3):7. doi:
https://doi.org/10.1167/jov.21.3.7.

Nascimento, S.M.C., Ferreira, F.P., & Foster, D.H. (2002). Statistics of spatial cone-
excitation ratios in natural scenes. Journal of the Optical Society of America A, 19,
1484-1490.

Foster, D.H., Amano, K., Nascimento, S.M.C., & Foster, M.J. (2006). Frequency of
metamerism in natural scenes. Journal of the Optical Society of America A, 23, 2359-
2372.

Nayatani Y., Umemura, Y., Sobagaki, H., Takahama, K. & Hashimoto, K. (1991).
Lightness perception of chromatic object colors. Color research and application, 16, 1.

Pearce B., Crichton S., Mackiewicz M., Finlayson G. D., & Hurlbert A. (2014). Chromatic
Illumination Discrimination Ability Reveals that Human Colour Constancy Is Optimised
for Blue Daylight Illuminations. PLoS ONE 9(2): e87989.

Pointer, M. R. (1980) The gamut of real surface colours. Col. Res. Appl. 5, 145–155.

Speigle, J. M. & Brainard, D. H. (1996). Luminosity thresholds: effects of test chromaticity
and ambient illumination. Journal of the Optical Society of America A, 13, 436-451

Stockman, A. and Sharpe, L. T. (2000) The spectral sensitivities of the middle- and long-
wavelength-sensitive cones derived from measurements in observers of known
genotype. Vision Research, 40, 1711–1737.

Sugita, Y. (2004). Experience in Early Infancy Is Indispensable for Color Perception.
Current Biology, 14, 3, 1267- 1271.

Uchikawa, K., Koida, K., Meguro, T., Yamauchi Y., & Kuriki, I. (2001). Brightness, not
luminance, determines transition from the surface-color to the aperture-color mode for
colored lights. Journal of the Optical Society of America A, 18, 737–746.

Uchikawa, H., Uchikawa, H. & Boynton, R. M. (1989). Influence of achromatic surrounds
on categorical perception of surface colors. Journal of the Optical Society of America
A, 29, 7, 881–890.

Uchikawa, K., Fukuda, K., Kitazawa, Y., & MacLeod, D. I. A. (2012). Estimating illuminant

color based on luminance balance of surfaces. Journal of the Optical Society of
America A, 29, 2, A133–A143.
Ullman, S. (1976) On visual detection of light sources. Biological Cybernetics, 21, 205–
211.
Winkler A. D., Spillmann L., Werner J. S., & Webster M. A. (2015) Asymmetries in blue-
yellow color perception and in the color of 'the dress'. Current Biology, 29, 25(13), R547-
R548.
Yamauchi, Y. & Uchikawa, K. (2005). Depth information affects judgment of the surface-
color mode appearance. Journal of Vision, 5, 515-524.
1016

Appendix

Individual observer settings in Experiment 2

In the main text, we presented mean observer settings for Experiment 2. Figure A1

shows the individual observer settings. There is some individual variation, but overall the

trend was similar across individuals.

Figure A1: Individual observer settings in Experiment 2. Colored square symbols indicate
the averaged setting across 10 repetitions for each observer. The error bar indicates ±1
S.E across 10 repetitions. The magenta circles denote the optimal color locus and the
blue circles show the real object locus. The red, black and blue vertical dashed lines
show the chromaticities of the 3000K, 6500K and 20000K test illuminants, respectively.
The black cross symbol indicates mean LMS value across surrounding stimuli. Note that
the horizontal range differs across panels.

1031

1032 ***Implementation of other past models***

1033 Here, we compare two simplistic models that predict luminosity thresholds based on

1034 post-receptoral signals or cone signals of the test field. Note that these two models were

1035 also implemented as candidate models in Speigle & Brainard (1996).

1036

The first model is a post-receptoral model which assumes that the visual system monitors

the weighted sum of the three types of cone signals of the test field. The test field appears

a self-luminous when $w_L L_T + w_M M_T + w_S S_T >= 1$, where L_T, M_T and S_T denote cone signals

of the test field and w_L, w_M and w_S denote weightings for each class of cone signal ($w_L >$

0, $w_M > 0$, and $w_S > 0$). Then, we optimized weightings w_L, w_M and w_S which produced

the minimum root mean square error between model prediction and mean observers'

setting.

1044

The second model is a generalized Evans's model (Evans, 1959) which assumes that a

test field appears self-luminous when any of L_T, M_T or S_T cone signals exceed a certain

criterion level. Thus, the model predicts that a test field is self-luminous when $L_T >= c_L$,

$M_T >= c_M$ or $S_T >= c_S$. The goal of the optimization here was to find criterion c_L, c_M and c_S

that minimized the root mean square error between model prediction and mean

observers' setting.

1051

1052 For both models, the optimization procedure was performed separately for each

1053 experimental condition. In other words, for example in Experiment 2, we performed

1054 optimization procedures 9 times in total (3 illuminants×3 distributions).

1055

Figures A2, A3 and A4 depict the prediction of the post-receptoral model and the

generalized Evans's model as well as the optimal color model in Experiments 1, 2 and

3. To obtain the prediction of the optimal color model, we used the ground-truth illuminant

for Experiments 1 and 3, but for Experiment 2, we used the estimated illuminant so that

the peak is matched between the prediction of optimal color model and the mean

observer settings (for more details, see the Results section in Experiment 2 in the main

text).

1063

1064 For Experiment 1, we see that the post-receptoral model predicts a linear luminosity

1065 threshold locus over L/(L+M) which did not lead to a high correlation coefficient (shown

1066 at the right upper corner in each panel). The generalized Evans's model came closer to

observer settings, but in all conditions the correlation coefficient was lower than that of the optimal color model. Welch's t-test (one-tailed, no assumption about equal variance) on averaged correlation coefficients across the 5 conditions showed that the optimal color model has a significantly higher correlation than the Evans' model ($t(4.64) = 4.57$, $p = 0.0072$).

A quite similar trend is shown in Experiment 2 though in one condition (*flat* and 20000K), the Evans's model exceeded the optimal color model's correlation coefficient. However, again Welch's t-test on averaged correlation coefficients across the 9 conditions showed a significantly higher correlation coefficient for the optimal color model than the Evans's model ($t(8.95) = 3.72$, $p = 0.0048$).

In contrast, for Experiment 3, we see that the Evans's model showed higher correlations than the optimal color model especially in green illuminant conditions. Welch's t-test on averaged correlation coefficients across the 12 conditions showed that there is no significant difference between the Evans's model and the optimal color model ($t(12.2) = 1.80$, $p = 0.0962$).

In summary, it is evident that for Experiments 1 and 2 the optimal color model predicts human observer settings better than the two alternative models considered here. In Experiment 3, there was no significant difference in correlation coefficients between the Evans's model and the optimal color model. One interpretation would be that when the scene illuminant is atypical, human observers rely on the simple statistics of a test field such as cone signals because the visual system does not know the optimal color locus under the illuminant.

Figure A2: Predictions from the post-receptoral model, the generalized Evans's model and the optimal color model in Experiment 1. Each model prediction was scaled to give the minimum root mean square error between model prediction and mean observer setting to compare their shapes more easily. The correlation coefficients between model prediction and mean observer settings are shown at the top right corner in each panel (in the order of post-receptoral model, generalized Evans's model and optimal color model from top to bottom). We used a ground-truth illuminant (i.e., 6500K) to obtain the prediction from the optimal color model.

1105

Figure A3: Predictions from the post-receptoral model, the generalized Evans's model,
and the optimal color model in Experiment 2. Each model prediction was scaled to give
the minimum root mean square error between model prediction and mean observer
setting. The correlation coefficients between model prediction and mean observer setting
are shown at the right top corner in each panel. For the optimal color model, we used an
estimated illuminant whose peak matched that of the observer settings (see Results
section in Experiment 2 in the main text for more details).

1113

1114

1115

Figure A4: Predictions from the post-receptoral model, the generalized Evans's model, and the optimal color model in Experiment 3. Each model prediction was scaled to give the minimum root mean square error between model prediction and mean observer setting. The correlation coefficient between model prediction and mean observer setting is shown at the top right corner in each panel. We used a ground-truth illuminant (i.e., magenta or green) for the optimal color model.

58