SIA: Selection Inference Using the Ancestral Recombination Graph

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1 Abstract

Detecting signals of selection from genomic data is a central problem in population genetics. Coupling the rich information in the ancestral recombination graph (ARG) with a powerful and scalable deep learning framework, we developed a novel method to detect and quantify positive selection: **S**election **I**nference using the **A**ncestral recombination graph (SIA). Built on a Long Short-Term Memory (LSTM) architecture, a particular type of a Recurrent Neural Network (RNN), SIA can be trained to explicitly infer a full range of selection coefficients, as well as the allele frequency trajectory and time of selection onset. We benchmarked SIA extensively on simulations under a European human demographic model, and found that it performs as well or better as some of the best available methods, including state-of-the-art machine-learning and ARG-based methods. In addition, we used SIA to estimate selection coefficients at several loci associated with human phenotypes of interest. SIA detected novel signals of selection particular to the European (CEU) population at the *MC1R* and *ABCC11* loci. In addition, it recapitulated signals of selection at the *LCT* locus and several pigmentation-related genes. Finally, we reanalyzed polymorphism data of a collection of recently radiated southern capuchino seedeater taxa in the genus *Sporophila* to quantify the strength of selection and improved the power of our previous methods to detect partial soft sweeps. Overall, SIA uses deep learning to leverage the ARG and thereby provides new insight into how selective sweeps shape genomic diversity.

Introduction

The ability to accurately detect and quantify the influence of selection from genomic sequence data enables a wide variety of insights, ranging from understanding historical evolutionary events to characterizing the functional and disease relevance of observed or potential genetic variants. Adaptive evolution is driven by increases in frequency of alleles that enhance reproductive fitness. In addition, alleles experiencing such positive selection often provide insights into the functional or mechanistic basis of phenotypes of interest. Examples of genetic determinants of important phenotypic traits under selection in human populations include a family of mutations in the hemoglobin-β cluster, which confer resistance to malaria and are at high frequencies in many populations [1,2], loci controlling growth factor signaling pathways that contribute to short stature in Western Central African hunter-gatherer populations [3,4], as well as mutations in several genes involved in immunity, hair follicle development, and skin pigmentation [5] (reviewed in refs. [6–9]).

Population genetic methods predominantly identify positive selection through the detection of selective sweeps. As the frequency of an advantageous allele increases, linked variants in the vicinity can "hitchhike" to high frequency, leading to local reductions in genetic diversity. Previous approaches to detecting selective sweeps (such as traditional summary statistics [10], approximate likelihood and Approximate Bayesian Computation (ABC) methods [11], or supervised machine learning (ML) methods [12,13]) exploit the effect of genetic hitchhiking on the spatial haplotype structure and site frequency spectrum (SFS). Summary statistics have the advantage of being fast and easy to compute, but may confound the effects of selection on genetic diversity with the effects of complex demographic histories including bottlenecks, population expansions and structured populations. Besides, they cannot easily be used to estimate the value of the selection coefficient. Approximate likelihood and ABC methods, on the other hand, can

provide an estimate of the strength of selection by aggregating multiple summary statistics [11],

but can be prohibitively computationally expensive when applied at a large scale. ML methods for

inferring selection can be more scalable, and can capture complex nonlinear relationships among

features. With the exception of a handful of recently developed methods that operate on the

multiple sequence alignment itself [14,15], however, the majority of ML approaches to selection

inference solely make use of traditional summary statistics as features for prediction. In short,

previous methods (including ABC and most ML methods) predominantly rely on low-dimensional

summary statistics, which, even in combination, capture only a small portion of the information in

the sequence data.

Recently, a new generation of inference methods have made it possible to go beyond summary

statistics and estimate or sample a full ancestral recombination graph (ARG) [16–18] for a

collection of sequences of interest. The ARG is a complex data structure that summarizes the

shared evolutionary history and recombination events that have occurred in a collection of DNA

sequences, and therefore contains highly informative features that can potentially be leveraged

to make accurate inferences about selection. The ARG representation is interchangeable with a

sequence of local genealogies along the genome and the recombination events that transform

each genealogy to the next. The influence of selection on each allele can be characterized from

the ARG, based on departures from the patterns of coalescence and recombination expected

under neutrality as reflected in the local genealogies. Traditional ARG inference methods [19–23]

were restricted in accuracy and scalability, limiting the practical application of ARGs. Recent

advances [24], however, have enabled scalable yet statistically rigorous genome-wide ARG

inference with dozens of genomes. Moreover, methods such as Relate [25] and tsinfer [26] have

further dramatically improved the scalability of ARG inference to accommodate thousands or even

hundreds of thousands of genomes. The latest progress in genealogical inference has paved the

way for ARG-based methods to address many different questions in population genetics [24–27].

One natural way to exploit the richness of the ARG representation in inference of selection would

be to extract features from inferred ARGs and feed them into a modern supervised machine-

learning framework. Deep-learning methods, in particular, have recently achieved unprecedented

success on a variety of challenging problems, including image recognition, machine translation,

and game-play [28]. Deep learning is also highly flexible, providing many opportunities for the

design of novel model architectures motivated by biological knowledge. An ARG-guided deep-

learning model could potentially provide new insight into how natural selection impacts the human

genome, human diseases and other phenotypes, and human evolution.

With these goals in mind, we developed a new method, called SIA (**S**election **I**nference using the

Ancestral recombination graph), that uses a Recurrent Neural Network (RNN) [29,30] to infer the

selection coefficient and allele frequency trajectory of a variant that maps to a gene tree

embedded in an ARG. Rather than relying on traditional sequence-based summary statistics, SIA

makes use of features based on the local genealogies extracted from the ARG. Based on these

local topological features, SIA learns to infer the selection coefficient and allele frequency

trajectory of a beneficial variant (see **Figure 1**). As described below, SIA performs well on

benchmarks and is reasonably robust to model misspecification. Applying SIA to data from the

1000 Genomes Northern and Western European (CEU) population, we identified new and known

loci under positive selection that are associated with a variety of phenotypes and estimated

selection coefficients at these loci. In addition, using SIA, we built on our previous work [31] on a

bird species-complex in the genus *Sporophila* by elucidating the strength and targets of selection

at specific loci tied to a collection of rapid speciation events. Overall, SIA is the first method that

couples ARG-based features with a machine-learning approach for population genetic inference.

Results

Methodological overview. SIA is based on an RNN that is trained to predict selection at a genomic site from genealogical features at that site of interest and nearby sites (see **Methods** for detailed descriptions, see **Figure 1** for a conceptual overview of SIA, and **Figure S1** for an illustration of ARG features and the RNN architecture). Based on the demography of a particular population of interest, training data including genomic regions under various strengths of selection are simulated. The ARG is then inferred from each simulated data set. ARG-level statistics are extracted at the site under selection (or a neutral site) as features to be used as input to the deep-learning model. Specifically, we use lineage counts at a set of discrete time points as a fixed-dimension encoding of a genealogy. The encoding of the genealogy at the focal site as well as similar encodings of flanking genealogies constitute the feature vector for that site. SIA uses a Long Short-Term Memory (LSTM) architecture, designed specifically to handle the temporal nature of the feature set. The LSTM unrolls temporally such that the lineage counts at each time point are fed to the network iteratively. Finally, the model trained on simulations is applied to ARGs inferred from empirical data to identify sweeps, infer selection coefficients, and allele-frequency trajectories.

Classification of sweeps. We first compared SIA with several existing methods, including the Tajima's D [10] and H1 [32] summary statistics, iHS [33], a genealogy-based statistic [25] and a summary-statistic-based machine-learning method [12,13] (see **Methods**), in the classification task of distinguishing hard sweeps from neutrally evolving regions. Our performance comparison was conducted across 16 combinations of selection coefficients and segregating allele frequencies such that the beneficial site was subjected to selection ranging from weak to strong, resulting in low to high derived allele frequencies (DAFs). Since *a priori* we expected sweep sites with lower selection coefficients and lower DAFs to be harder to detect, we performed a stratified

analysis of SIA's performance by selection coefficient and DAF. **Figure 2** reports the Receiver

Operating Characteristic (ROC) curves using simulations based on the CEU demographic model

[34] where inferred genealogies were used as input to SIA to account for gene tree uncertainty.

As expected, all methods tended to perform better in a regime with higher selection coefficients

and DAFs, as indicated by increasing values of the area under the ROC curve (AUROC) statistic

from left to right (increasing selection) and from top to bottom (increasing DAF). SIA outperformed

the other methods across model conditions, with a more pronounced performance advantage for

sites under weaker selection and segregating at lower DAFs (**Figure 2**). For each given selection

coefficient, the AUROC of the Relate tree statistic (shown in red in **Figure 2**), which measures

how unlikely it is that the observed expansion of the derived lineages is purely due to genetic drift,

did not substantially improve as the DAF increased. Alleles at higher frequency tend to be older

and subjected to drift over longer periods, which may lead to reduced power for Relate to

distinguish lineage expansion under selection from the neutral expectation. Consequently, while

the ARG-based methods SIA and Relate both outperformed other methods at low DAFs, SIA was

alone in maintaining this advantage at higher DAFs.

In addition, we validated the ability of SIA to classify genomic regions with additional test sets

simulated under a demographic model for southern capuchinos, a group of songbirds in which we

previously identified and characterized many examples of sweeps [31], finding a predominance

of "soft" rather than "hard" sweeps (meaning that they tend to be based on standing genetic

variation rather than new mutations; see **Methods**). **Figure S2** reports the ROC curves for the

task of distinguishing partial soft sweeps from neutral regions. Despite soft sweeps being harder

to detect, the classifier achieved good performance in the moderate-to-strong selection regimes

($s = 0.005$ and $s = 0.0075$) where the accuracy ranged between 82% and 96%, a substantial

improvement over the previous accuracy of 56% [31]. SIA performed particularly well in identifying

partial soft sweeps when the site under selection was at a high segregating frequency. For

example, at segregating frequencies of 0.75 and 0.9, the performance of SIA ranged between

80% and 96% across a variety of selection regimes (s = 0.0025, 0.005, and 0.0075). The

performance of SIA degraded somewhat for weak selection (s = 0.001) with an accuracy ranging

between 63% and 74%.

Selection coefficient inference using true gene trees. We assessed the performance of SIA in

correctly predicting the selection coefficient and compared it to CLUES [35]. Like SIA, CLUES

uses local genealogies based on the ARG to infer a selection coefficient. However, CLUES

calculates the likelihood of the genealogy analytically using a hidden Markov model (HMM), and

does not rely on simulated training data. In addition, CLUES uses a single genealogy at the focal

site, whereas SIA additionally considers flanking trees.

We began by supplying both methods with true genealogies, in order to later disentangle the error

deriving from the ARG inference step from other sources of error (see **Discussion**). We found

that SIA identified regions under neutrality with approximately no bias (median inferred s = 7.5e-

05; **Figure 3**). Similarly, SIA correctly inferred the selection coefficient for regions under moderate

to strong selection ($s \in$ {0.0025, 0.005, 0.0075, 0.01}) with the median inferred s deviated from

the true s by at most 3%. On the other hand, SIA somewhat underestimated the selection

coefficient (median inferred s = 0.00037) for the weak selection regime (true s = 0.001), likely

owing to limits in the training set within that selection regime (see **Discussion**). We further binned

the results by segregating frequency and selection coefficient and found that, in general, the

variance in estimates of s for SIA (as well as CLUES) tended to decrease as the segregating

frequency of the beneficial allele increased (**Figure S3**).

CLUES performed roughly similarly to SIA in this experiment, but tended to slightly overestimate

s for the neutral regions (i.e., true s = 0) and underestimate s for the moderate to high selection

regimes (i.e., true s = 0.005, 0.0075, and 0.01). Under these conditions, SIA's median predictions

of s were noticeably closer to the true values (**Figure 3A**). At the same time, CLUES performed

slightly better than SIA in weak selection regimes (i.e., true s = 0.001 and 0.0025) (**Figure 3**).

Overall, SIA (RMSE = 9.52e-4) achieved a lower error in estimating s than CLUES (RMSE =

1.44e-3), when true genealogies were used as input to both methods (Wilcoxon signed-rank test

for difference in mean of squared error, p = 1.25e-42). This finding potentially reflects the benefit

of linkage information utilized by SIA through the additional flanking genealogies (see

Discussion).

Selection coefficient inference using inferred gene trees. To account for gene-tree uncertainty,

we next used ARGs inferred with Relate, which is scalable to the size of the training dataset for

SIA (see **Methods**), as input to SIA and CLUES and compared their performance on CEU

simulations. Furthermore, we compared both methods to a supervised machine learning method,

ImaGene (see **Figure S20**), that operates directly on an image of the alignment itself. ImaGene

does not require gene trees as input and instead uses a Convolutional Neural Network (CNN) to

perform dimensionality reduction of the sequence alignment, allowing for accurate and efficient

classification and regression.

Overall, we found that SIA and ImaGene outperformed CLUES in these experiments (**Figure 4**).

CLUES tended to underestimate selection coefficients for the moderate-to-strong selection

regimes, to a greater extent compared to the case where true genealogies were used for inference

(**Figures 3A & 4A**). This decrease in performance of CLUES evidently derives from error at the

ARG reconstruction step. SIA, on the other hand, appeared to be more robust to the same ARG

reconstruction error. ImaGene performed remarkably similarly to SIA, given that it relies solely on

the sequence alignment. SIA exhibited lower error at neutral sites and sites with low-to-moderate

values of s, whereas ImaGene prevailed at sites under strong selection (**Figure 4B**).

Nevertheless, SIA showed a slightly smaller overall RMSE (2.75e-3) compared to ImaGene

(2.91e-3) (Wilcoxon signed-rank test, $p = 6.18e-38$), and in particular, SIA produces estimates of

s much closer to 0 for neutral loci. Notably, in this case both SIA and ImaGene were trained with

simulations under the same uniform distribution of *s* values (see **Methods**). A different choice of

training distribution could impact their performance across selection regimes (see **Discussion**).

Furthermore, we binned the results of these methods by both the segregating frequency and the

selection coefficient (see **Figure S4**) and again found that in general they exhibit higher variance

under low segregating frequency of the beneficial allele. As before, we also tested our regression

framework on true and inferred gene trees of test sets simulated under the *S. hypoxantha*

demographic model (see **Figure S5**). We found that SIA was approximately unbiased for the

moderate ($s = 0.005$) and high ($s = 0.01$) selection regimes but appeared to overestimate the

selection coefficient for regions under weak selection ($s = 0.001$ and 0.0025), when both true and

inferred genealogies were used as input. Furthermore, SIA appeared to overestimate the

selection coefficient for neutral regions when inferred gene trees were used as input, whereas it

was approximately unbiased for true gene trees.

Performance on selection coefficient prediction with different sample sizes. To explore the

tradeoffs associated with the use of larger data sets, we examined the performance of SIA under

different sample sizes, assuming a constant-sized demographic model (N_e=10,000). **Figure S6**

shows the error in selection coefficient inference on a held-out test set, stratified by the age of the

allele (panels **A&B**) and present-day derived allele frequency (panels **C&D**) at the site of interest.

We observed that sites with low frequency (AF < 0.33) and more recent (onset < 0.2 x $2N_e$

generations) alleles experience the most significant reduction in error as sample size increases.

Notably, the performance of SIA on more ancient alleles (onset > 0.2 x $2N_e$ generations) had little

to no improvement as the sample size increased from 32 to 254. These observations are in line

with the expectation that having more samples improves the chance of capturing low-frequency

alleles, but provides limited information about more ancient events. The reason for this age-dependency is that, looking backwards in time, most lineages coalesce rapidly and only a few survive to more ancient epochs, in a manner that depends only weakly on the sample size. It may be useful to consider these observations when choosing the sample size for use in studying selection in a particular context (see **Discussion**).

Inference of allele frequency trajectory. We further adapted the deep-learning architecture of SIA to model the allele frequency (AF) trajectory at a site by retaining the output of the LSTM at each time point (**Figure S1**, see **Methods**). We then evaluated the performance of SIA in the inference of the AF trajectory using simulations under the CEU demography across a range of selection coefficients and current DAFs. SIA was largely able to capture the expected trend of more rapidly increasing AF under stronger selection (**Figure S7** and **S9**). In addition, AF estimates by SIA using both true and inferred genealogies were generally unbiased, although AF at more recent time points tended to be slightly underestimated when data was simulated under weaker selection. AF estimates also appeared to be more accurate in terms of variance for alleles under stronger selection (**Figure S8** and **S10**). As expected, the variance of AF estimates tended to increase going further back in time (**Figure S8** and **S10**).

Model performance on simulations with misspecified demographic models. To evaluate the robustness of SIA to mismatches between the demographic parameters used for simulating training data and the true underlying demography of real data, we tested the method on the selection-coefficient inference task with datasets simulated under a range of alternative parameters. Each aspect of this model misspecification was assessed independently of the others. In particular, the misspecified datasets contained simulations under (*i*) combinations of population mutation (θ) and recombination (ρ) rates sampled beyond the range used for the training data (**Figures S11** and **S14**), (*ii*) various alternative demographic scenarios (**Figures S12**,

S15, and **S17**), and (*iii*) various effective population sizes (**Figures S13** and **S16**). We compared

the performance of SIA on these misspecified datasets to that of CLUES [35], supplying both

methods with the true genealogies. We consider CLUES the "silver standard" when it comes to

robustness because it is unsupervised and therefore should not be susceptible to misspecified

training data compared to supervised learning methods such as SIA. Overall, we found that both

CLUES and SIA were reasonably robust to model misspecification (**Figures S11-13**), although

the performance of both methods inevitably declined when tested on severely misspecified data

(**Figure S13**). Interestingly, SIA tended to overestimate selection coefficient when the true N_e was

much smaller than that used for training, and underestimate it when the true N_e was much larger,

whereas CLUES did the opposite (**Figure S13**). Since the CLUES likelihood model of allele

frequency transition is parameterized by the population-scaled selection coefficient ($\alpha = 2Ns$), a

larger N_e likely appears to CLUES as equivalent to a higher s. On the other hand, features used

by SIA capture broad information of coalescence and linkage in the ARG, and therefore can be

distorted by misspecified N_e in more subtle ways (see **Discussion**). Using the same misspecified

dataset, we also ran SIA with Relate-inferred genealogies and compared its performance to that

of the genotyped-based deep-learning model ImaGene [14,15]. In general, SIA appeared to be

more robust to model misspecifications, achieving an overall RMSE of 0.00362, 0.00318 and

0.00374 in the misspecified θ/ρ, demography, and N_e experiments, respectively, compared to

ImaGene, whose RMSE was 0.00416, 0.00330 and 0.00462 in the corresponding experiments

(**Figures S14-16**). The advantage of SIA was particularly noticeable in cases of misspecified

demographic parameters (**Figures S15 & S16**). Notably, SIA exhibited reduced bias when

working with inferred genealogies compared to true genealogies, under conditions of extremely

mismatched N_e (compare **Figures S13 & S16**).

Model prediction at genomic loci of interest in CEU population. We then applied the SIA model to

identify selective sweeps and infer selection coefficients at selected genomic loci in the 1000

Genomes CEU population. These loci included the canonical example of selection at the *MCM6*

gene, which regulates the neighboring *LCT* gene and contributes to the lactase persistence trait

[36], the *ABCC11* gene regulating earwax production, several pigmentation-related genes, as well

as genes associated with obesity, diabetes and addiction (**Table 1**).

For *LCT*, SIA detected a strong signal of selection at the nearby SNP that has been associated

with the lactase persistence trait (rs4988235). At this SNP, SIA inferred a sweep probability close

to 1 and a selection coefficient greater than 0.01, making this one of the strongest signals of

selection in the human genome. A close examination of the local genealogy at this site reveals a

clear pattern indicative of a selective sweep — a burst of recent coalescence among the derived

lineages (orange taxa are the lineages carrying the derived allele) is clearly visible from the tree

(**Figure 5**).

At a number of pigmentation genes [37–41], SIA detected signals of moderate selection, including

MC1R (rs1805007, P(sweep) = 0.95, $s \approx 0.0037$), *KITLG* (rs12821256, P(sweep) = 0.87, $s \approx$

0.0019), *ASIP* (rs619865, P(sweep)= 0.78, $s \approx 0.0019$), *OCA2* (rs12913832, P(sweep) = 0.75, s

≈ 0.0056) and *TYR* (rs1393350, P(sweep) = 0.62, $s \approx 0.0011$). In addition, SIA identified a weak

signal of selection at a SNP in the *ABCC11* gene (rs17822931), which influences earwax and

sweat production [42], with a selection coefficient of around 0.00035. There are few other

estimates for these genes available for comparison, but, notably, our estimate for *LCT* of $s \approx 0.01$

is consistent with a previous estimate on the order of 0.01-0.1 [36], and with recent studies of

ancient DNA samples [43,44] suggesting a value closer to 0.01. Our estimates suggest that

selection at the pigmentation loci is considerably weaker than at *LCT*, in contrast to previous

estimates for these loci, which covered a wide range but were generally considerably larger

(ranging from 0.02-0.1) [45]. Interestingly, CLUES estimated *s* at the *OCA2* locus to be on the

order of 0.001 (roughly similar to SIA's estimate of 0.0056), but *s* at the *KITLG*, *ASIP*, *TYR* loci to

be greater than 0.01 (in comparison to SIA's considerably smaller estimates of 0.0019, 0.0019,

and 0.0011) [35]. The apparent discrepancy between the estimates may be partially due to the

fact that the two methods used samples from two different populations (CEU for SIA and

GBR/British for CLUES).

On the other hand, SIA did not detect significant evidence of positive selection at several disease-

associated loci (rs7903146/*TCF7L2*, rs1800497/*ANKK1*, and rs9939609/*FTO*) or at several other

pigmentation loci (rs13289810/*TYRP1*, rs1003719/*TTC3*, and rs7495174/*OCA2*) (**Table 1**).

Notably, allele frequencies at these six loci tend to be similar in African and European populations

[46], suggesting that they are not likely to be under strong environment-dependent positive

selection, although it is possible that they have experienced very recent selective pressure that

SIA lacks the power to detect (see **Discussion**). Notably, *TYRP1* and *TTC3* also lacked signals

of selection in the CLUES analysis. Compared to the genealogies at sweep sites (**Figure 5**), the

trees at these putatively neutral loci lack the distinctive signature of recent bursts of coalescence

among derived lineages (**Figure 6**).

Southern capuchino species analysis. Our previous study of southern capuchino seedeaters

made use of the full ARG and machine learning to detect and characterize selective sweeps, and

suggested that soft sweeps are the dominant mode of adaptation in these species (see **Methods**

for more details). To further characterize the targets and strengths of positive selection in these

species, we applied SIA to polymorphism data [47] for *S. hypoxantha,* and adopted a conservative

approach by reporting only sites with DAF ≥ 0.5, SIA-inferred $s \geq 0.0025$, and SIA-inferred sweep

probability ≥ 0.99 (see **Methods**). In addition to loci near top F_{ST} peaks and known pigmentation-

related genes (**Table 2**), we identified many more sites under positive selection located outside

the previously scanned F_{ST} peaks, amounting to a total of 15,551 putative partial soft sweep sites

across the 333 scanned scaffolds for *S. hypoxantha*. These sites can be prioritized for further

evaluation and downstream analysis. Notably, SIA enabled us to distinguish between selection at

regulatory and coding sequences, and we found that sweep loci near F_{ST} peaks and pigmentation

genes fall mostly in non-coding regions (**Table 2**). We additionally surveyed all putative sweep

sites identified by SIA and found that they are indeed enriched in non-coding regions (Fisher's

exact test, $p = 6.80 \times 10^{-5}$), particularly noticeable in the "near-coding" regions (**Figure S21**).

Consistent with the observation that the most highly differentiated SNPs among taxa are non-

coding [47,48] our finding suggests that positive selection may act on *cis*-regulatory regions to

drive differentiation and the subsequent speciation process. Furthermore, we examined many

individual predictions in detail, considering the local trees inferred by Relate at these high-

confidence predictions (**Figure 7**). We found, in numerous cases, that these sweeps had distinct

genealogical features, displaying evidence of a burst of coalescence events, corresponding to

unusually large and young clades. Prominent examples include predictions near pigmentation-

related genes *ASIP*, *KITL*, *SLC45A2*, and *TYRP1*.

Discussion

The ARG is useful for addressing a wide variety of biological questions ranging from inferring

demographic parameters to estimating allele ages. SIA exploits the particular utility of the ARG

for accurate inference of positive selection in a way that makes use of the full dataset, as opposed

to traditional summary statistics, which necessarily discard substantial information. Direct use of

the ARG improves upon traditional summary statistics in two key ways. First, it enables

consideration of the temporal distribution of coalescence and recombination events in the history

of the analyzed sequences, in contrast to traditional summary statistics that simply average over

these coalescence and/or recombination events. In addition, ARG-based methods provide better

spatial resolution by separately examining individual genealogies and the recombination

breakpoints between them, rather than averaging across windows containing unknown numbers

of genealogies. These detailed patterns of coalescences and linkage enable the ARG-based

approaches to capture a more localized and fine-grained picture of selection (e.g. infer selection

coefficient and allele frequency trajectory) as well as to achieve a better classification

performance. This performance advantage is particularly noticeable at lower DAFs and when

selection is weak, a regime where previous methods for selection inference fall short (**Figure 2**).

At the same time, the supervised machine-learning approach sets SIA apart from another ARG-

based method, CLUES, which approximates a full likelihood function for ARGs in the presence of

selection using importance sampling and a HMM. Although the accuracy of both SIA and CLUES

degraded when using inferred genealogies compared to true genealogies, reflecting the error and

uncertainty at the ARG inference step, SIA appeared to be more robust to gene tree uncertainty

(**Figures 3** and **4**). One possible reason for this observation is that CLUES effectively assumes

that the selection coefficient at the focal site is conditionally independent of the flanking trees

given the focal tree. This assumption should hold in the presence of fully specified genealogies,

but it may make CLUES more sensitive to errors in the inferred genealogies. In other words,

through its use of supervised learning, SIA may be able to compensate for the effects of

genealogy inference error on its estimation of the selection coefficient by also directly considering

the flanking trees and LD-related patterns among them. Still, the drop in accuracy observed

across methods underscores the dependency of ARG-based approaches on the ARG inference

method. For this reason, we anticipate that SIA may benefit substantially from further

improvement in ARG inference tools (see ref. [9]).

The ARG-based feature set distinguishes SIA from other supervised machine learning

approaches for characterizing selective sweeps. SIA uses local topological features of the ARG,

which are more informative than the SFS- or LD-based summary statistics employed by machine

learning methods such as S/HIC, SFselect, and evolBoosting. Using simulations, we

demonstrated that the SIA classifier outperformed a deep-learning method that aggregates these

traditional summary statistics (**Figure 2**). We also compared SIA with ImaGene, which represents

another flavor of supervised learning methods, inspired by the recent rise of CNNs for image

recognition. ImaGene encodes sequence alignments as images for powerful population genetic

inferences with CNNs and provides a state-of-the-art benchmark to compare against. We found

that ImaGene performs remarkably well across a wide range of simulations, but SIA does appear

to be somewhat less biased and more robust to model misspecification than ImaGene. The

evolutionary information in the ARG is implicit in the sequence alignment but some of this

information may be difficult for a brute-force machine learning model to discover directly.

We demonstrated that utilizing the ARG granted SIA considerably improved performance over

deep learning models solely employing traditional summary statistics. However, a possible

drawback of an ARG-based model is the potentially prohibitive computational overhead incurred

by ARG inference, especially as sample size grows. Picking a sample size when running SIA

involves a tradeoff between scalability (fewer samples, faster ARG inference) and performance

(more samples, slower ARG inference). We have found that SIA can infer selection coefficients

reasonably well with as few as 16 haplotypes. Including more samples did improve performance

but with a sublinear reduction in error (**Figure S6**). Therefore, a sample size from a few dozen to

a few hundreds — well within the capabilities of most modern ARG inference methods — strikes

a good balance between performance and scalability. Moreover, we found that larger sample

sizes improved prediction performance primarily for alleles at lower frequencies but had little

impact on the performance for more ancient alleles (as most lineages would have already

coalesced going further back in time) (**Figure S6**). This observation suggests that the choice of

the sample size when applying SIA should be guided by the biological question of interest —

ancient selection can be studied with just a handful of samples, whereas a larger sample size is

better suited to detect more recent sweeps.

Like other supervised learning methods, SIA relies on simulations to generate training data, and

therefore could be biased by subjective choices of simulation parameters. For example, SIA and

ImaGene cannot make accurate predictions of selection coefficients outside the range

represented in the training data (**Figure S18**), whereas unsupervised methods such as CLUES

are not limited to a pre-defined range (**Figure S19**). This problem could be circumvented by

training on an extended range of *s*. Similarly, the tendency of SIA to underestimate the selection

coefficient for sites under weak selection (**Figures 3, 4**) could be mitigated by augmenting the

training set with simulations densely sampled from the weak selection regime. A more subtle

issue, however, arises when the underlying generative process of the real data does not match

the assumptions made for the simulations of the training data, potentially compromising the

accuracy of the method when applied to real data. Thus, we tested SIA on simulations with

parameters mismatching those used in the training procedure. In general, we found that SIA was

fairly robust to alternative parameter values, although, as expected, performance did degrade

somewhat under severely misspecified models. Notably, SIA achieved a similar level of

robustness to model parameter misspecification as the unsupervised (i.e. not relying on training

data) likelihood method CLUES, yet outperformed the supervised deep learning method

ImaGene.

Applying SIA to the CEU panel from the 1000 Genomes Project yielded several noteworthy

findings at loci with known ties to phenotypes of interest. In addition to confirming the canonical

signal of selective sweep at the *LCT* locus, SIA detected a novel signal of selection at a GWAS

SNP in the *MC1R* gene associated with red hair color, contrasting a previous study that could not

find evidence of selection at *MC1R* in the European population [49]. The derived allele at this

locus segregates at around 10% in the CEU population but is nearly absent in non-European

populations [46]. In addition, at the *MC1R* locus the Relate test statistic for selection [25], which

tends to perform particularly well at low segregating frequencies (**Figure 2**), falls slightly below

the significance threshold of 0.05, supporting the evidence of positive selection at this locus. SIA

also detected evidence of selection at a SNP in the *ABCC11* gene reported to be the determinant

of wet versus dry earwax as well as sweat production, mirroring the signal of selection previously

found in the East Asian population [50], although selection in the CEU population appeared to be

much weaker. In addition, SIA identified selection at a few other pigmentation-related loci, yet

determined previously identified SNPs in the *TYRP1* and *TTC3* genes to be largely free from

selection (**Table 1**). These results were consistent with a previous study [35], which reported

similar results for these pigmentation-related loci, albeit in a slightly different population (GBR).

SIA notably did not detect positive selection at GWAS loci in the *TCF7L2* gene associated with

type-2 diabetes, the *ANKK1* gene implicated in addictive behaviors, and the *FTO* gene associated

with obesity. Overall, this empirical study with the 1000 Genomes CEU population has illustrated

how SIA can be applied to assess natural selection at the resolution of individual sites, suggesting

that it may be useful in prioritizing GWAS variants for further scrutiny.

In our previous work on southern capuchino seedeaters [31] (see **Methods**), we applied newly

developed statistical methods for ancestral recombination graph inference and machine-learning

for the prediction of selective sweeps. We found evidence suggesting that a substantial fraction

of soft sweeps are partial but had limited power to identify them (i.e. average accuracy of 56%).

SIA considerably improved our characterization of positive selection in the southern capuchino

species in two key ways. The SIA framework performs inference of selection directly from

genealogies instead of traditional summary statistics, and in doing so achieved an accuracy of up

to 96% in detecting partial soft sweeps. Consequently, we found abundant evidence of soft

sweeps beyond the previously scanned F_{ST} peaks, and additionally were able to estimate their

selection coefficients. Importantly, SIA also took the analysis of selection beyond broad genomic

windows containing sweeps to the identification of specific putative causal variants. We took

advantage of this substantial improvement in genomic resolution and analyzed the distribution of

these sweep sites, which revealed that positive selection on regions that likely contain *cis-*

regulatory elements plays a role in driving the differentiation and speciation of southern capuchino

seedeaters.

While we believe SIA represents an important step forward in the use of the ARG for machine-

learning-based selection inference, there remain several possible avenues for improvement. For

example, SIA currently uses a point-estimate of the ARG, rather than a distribution, and therefore

does not explicitly take gene-tree uncertainty into account. We plan to improve SIA by using

strategies for inferring approximate posterior distribution of ARGs (e.g., [24]), as well as designing

better algorithms for ARG reconstruction that balance accuracy with scalability and can handle

thousands of genomes. In addition, the SIA framework was applied in the context of single-locus

selective sweeps, but could be extended to study polygenic selection, by making use of summary

statistics from genome-wide association studies (as in [51]) and adapting the architecture of our

neural network to account for selection acting at multiple sites. Finally, the robustness of SIA to

model misspecifications can be further improved by ensuring the simulated data is generated

under a distribution that is compatible with the real target data set. We anticipate that the continual

advancement in ARG inference methods has the potential to open up many new applications for

this flexible and powerful model of ARG-based deep learning in population genetics.

478   Methods

Simulated datasets used for training and testing the selective sweep model. Training and testing

data sets were generated using discoal [52] by simulating 1,000,000 regions of length 100 kb for

each model we considered (i.e., "neutral" or "hard sweep"). Aside from these regions, 2,000 were

simulated for validation and 5,000 were simulated for testing. The number of sampled sequences

was selected to match the number of individuals in the CEU population in the 1000 Genomes

dataset. Thus, a total of 198 haploid sequences were sampled. Simulations used a demographic

model based on European demography [34]. In non-neutral simulations, selection was applied to

a single focal site located in the middle of the simulated region. We sampled each of the main

demographic and selection parameters from a uniform distribution: (1) mutation rate $\mu \sim U$(1.25e-

08, 2.5e-08), (2) recombination rate $\rho \sim U$(1.25e-08, 2.5e-08), (3) selection coefficient $s \sim$

U(0.0001, 0.02), and (4) segregating frequency of the site under selection $f \sim U$(0.01, 0.99).

ARG Feature Extraction. For each target variant, we extracted the corresponding gene tree from

the ARG, then overlaid it with 100 discrete timepoints. These timepoints were fixed across all

trees in an approximately log-uniform manner that resulted in finer discretization of more recent

time scales (as in [24]). We considered biallelic sites only and assumed no recurrent mutations;

thus each mutation was assumed to occur on the branch of the tree where the ancestral allele

switches to the derived. For each timepoint, we calculated the number of active ancestral and

derived lineages. Furthermore, we computed the number of all active lineages (not distinguishing

between ancestral and derived) at the same set of predefined timepoints in the two left and right

flanking gene trees to account for linkage disequilibrium. Together, these features were

summarized in a 600-dimensional feature vector, which was then used as input to an RNN. The

feature of a simulated sweep region was extracted from the sweep site (by default at the center

in all simulations) whereas the feature of a simulated neutral region was extracted from a variant

site (randomly chosen) with a pre-defined matched derived allele frequency. The features for each

genomic locus of interest in the CEU population were extracted from all variant sites at that locus

having a derived allele frequency of >0.05.

Training an RNN to predict different modes of selection. An RNN was applied to the simulated

training data sets to learn a classification or regression model for the task at hand. We used a

Long Short-Term Memory (LSTM), a particular form of RNN, to accommodate the temporal nature

of our features and account for long-term dependencies and the vanishing gradient problem

observed in traditional RNNs. Our model had 100 timepoints with the final target output depending

on the use of classification or regression. For the classification task, the final target output is a

label for a binary classification problem predicting whether a region is under selection or neutrality.

For the regression task, the final target output is a continuous value, representing the selection

coefficient or the time of selection onset. We also took a many-to-many approach to model the

allele-frequency trajectory for the site under selection. The *Keras* software was used to train and

test the model. We used a two-stacked LSTM to account for greater model complexity where the

number of units in each stack was set to 100 and the hyperbolic tangent (*tanh*) was used as an

activation function. The *Adam* optimization method with its default operating parameters was used

to update the network weights. For the classification task, the *Softmax* activation function was

applied on the final dense layer and the *binary_crossentropy* was used to compute the cross-

entropy loss between true labels and predicted labels. For the regression task, the *linear*

activation function was applied on the final dense layer and the *mean_squared_error* function was

used.

Estimation of Confidence Intervals. To turn our single-valued regression model into one capable

of returning a distribution of predictions of *s*, we reused the dropout technique that is typically

used during training. Dropout enables a fraction of nodes to be randomly "turned off" in a certain

layer, which assists in the regularization of the model and helps prevent overfitting. We applied

dropout during inference, enabling us to sample a "thinned" network to generate a sample

prediction. By repeatedly sampling thinned networks, we generated a distribution of predictions

and then computed confidence intervals based on this distribution [53].

ARG Inference. Relate [25] (v1.0.17) was used for inferring ARGs underlying simulated genomic

samples as well as the CEU population in the 1000 Genomes dataset. For simulations under the

Tennessen *et al.* demography [34], Relate was run with the true simulation parameters (μ, ρ and

N_e) specified; whereas for genomic loci of the CEU population, Relate was run with a mutation

rate of 2.5×10^{-8} /base/generation (-m 2.5e-8), a constant recombination map of 1.25×10^{-8}

/base/generation and a diploid effective population size of 188,088 (-N 376176). The choice of

mutation rate follows [35] based on estimates from [54]. Although some more recent estimates

have been lower [55], these differences in mutation rate are unlikely to have a major effect on our

selection inference since SIA appears to be fairly robust to misspecification of mutation rate

(**Figures S11 & S14**). For simulations and genomic loci of the *S. hypoxantha* population, Relate

was run with $\mu=\rho=1\times10^{-9}$ /base/generation and a diploid N_e of 130,000. The branch lengths of

Relate-inferred genealogies were estimated iteratively with the `*EstimatePopulationSize.sh*` script

in the Relate package. Specifically, population size history was inferred from the ARG, the branch

lengths are then updated for the estimated population size history and these steps are repeated

until convergence. This was done for a default of 5 iterations (--num_iter 5).

Alternative methods for selection inference. To benchmark the performance of SIA for

classification of sites under neutrality versus selective sweep, we ran the following methods:

Tajima's D [10], H1 [32], iHS [33], a summary statistics-based deep learning model, and a tree-

based statistic that is part of the Relate [25] program. Tajima's D, H1 and iHS were calculated

with the *scikit-allel* package. Haplotypes of the entire 100kb simulated genomic segment were

used for Tajima's D and H1 calculations. The unstandardized iHS was computed at every site

with minor allele frequency > 5%, with respect to all other sites in the genomic segment

(min_maf=0.05, include_edges=True). iHS scores of all sites were then standardized in 50 allele-

frequency bins. Finally, the iHS score of a genomic region was taken to be the mean of the iHS

scores of all of its variant sites. For the summary statistics-based deep learning model, we made

use of the summary statistics used by S/HIC [12,13] as features for our deep learning architecture.

These included 11 sequence-based summary statistics (see **Figure 3** in [56]) which were used

as features for our deep learning model to distinguish among the two classes at hand (selective

sweep versus neutral drift). All statistics were collected along five consecutive 20-kb windows with

the objective of identifying possible sweeps induced by a positively selected mutation in the third

(middle) window. Some of these summary statistics corresponded to standard measures of

diversity, such as ss (the number of segregating sites), π [57], Tajima's D [10], θ_W [58], θ_H [59],

the number of distinct haplotypes [60], H1, H12, H2/H1 [32], Z_{nS} [61], and maximum value of ω

[62]. For each of these statistics, we computed an average value for each of the five 20 kb

windows for the simulated population. Finally, each summary statistic was normalized by dividing

the value recorded for a given window by the sum of values across all five windows. The Relate

tree-based selection test was performed with an add-on module (*DetectSelection.sh*) using the

inferred genealogy with calibrated branch lengths at a site of interest, yielding a $\log_{10}$ p-value for

each site. We also compared the performance of SIA for selection coefficient inference to that of

CLUES [35] and a genotype-based convolutional neural network (CNN) framework [14,15].

Selection coefficient inference from true genealogies was performed with *clues-v0*

(https://github.com/35ajstern/clues-v0). Transition probability matrices were built on a range of

selection coefficients [0, 0.05] at increments of 0.0001 and present-day allele frequencies [0.01,

0.99] at increments of 0.01. Selection-coefficient inference from Relate inferred genealogies was

performed with CLUES (https://github.com/35ajstern/clues). Branch lengths of the genealogy at

the site of interest were resampled with Relate for 600 MCMC iterations, and CLUES was run

with the following arguments: `--tCutoff 10000 --burnin 100 --thin 5`. For the genotype-based CNN

model, each simulated genomic segment was preprocessed by first sorting the haplotypes and

then converting the segment to a fixed-size genotype matrix. Haplotype sorting was performed

by *1)* calculating the pairwise manhattan distances between haplotypes, *2)* setting the haplotype

with the smallest total distance to all other haplotypes as the first haplotype, and *3)* sorting the

remaining haplotypes in increasing distance to the first haplotype. To convert the sorted

haplotypes to a fixed-size genotype matrix, centered on the middle variant of a simulated region,

up to 180 variants on each side were retained. Variants beyond 180 were discarded and if there

were fewer than 180, the missing variants were padded with zeros. Ancestral and derived alleles

were coded with 0's and 1's, respectively. Consequently, each simulated genomic region was

encoded as a (198 x 360) binary matrix, along with a real-valued vector encoding the genomic

positions of the variants in the matrix. The CNN model had a branched architecture — one branch

with five 1D convolution layers taking the genotype matrix as input and another branch with a fully

connected layer taking the vector of variant positions as input. The output of the two branches

was flattened, concatenated and fed into 3 fully connected layers, followed by a linear output layer

to predict selection coefficient (**Figure S20**).

Evaluation metrics. To evaluate the performance of SIA's classification model and alternative

methods, we computed a receiver operating characteristic (ROC) curve for the binary class at

hand ("neutral" or "sweep"), to provide a more complete summary of the behavior of different

types of errors. We further assessed the performance of SIA and alternative methods in terms

of correctly predicting the selection coefficient numerically using mean absolute error (mae),

root mean square error (rmse), coefficient of determination (r^2), and visually using a box plot that

compares the simulated ground truth against the predictions by the method at hand.

Robustness study. We carried out an extensive analysis of the robustness of our approach,

considering not only alternative demographic parameters (such as population size), but also

alternative parameters for recombination rate, mutation rate, time of selection onset, and selection

coefficients. In all cases, we took care to test our prediction methods under parameters well

outside the range used in training.

Analysis of CEU population in 1000 Genomes data. We applied SIA to infer selection coefficients

and allele frequency trajectories in the 1000 Genomes [63] CEU population at 13 genomic loci

with known association to phenotypes, some of which were previously identified as likely targets

of positive selection (**Table 1**). For each gene of interest, the ARG was inferred with Relate from

SNPs within a 2Mb window centered at the gene. Once the ARG was inferred, only SNPs with

valid ancestral allele (`AA` INFO field in the vcf file) were retained for downstream analysis.

Following the aforementioned protocol (see *ARG feature extraction*), features at all variant sites

in the 2Mb window above a derived allele frequency threshold of 0.05 were extracted. Lastly, the

SIA model was applied to classify neutrality versus selection, and infer selection coefficient and

allele frequency trajectory at each site.

Localizing sweeps in southern capuchino seedeaters. We recently applied a combination of ARG

inference and machine-learning methods for identifying selective sweeps to study previously

identified "islands of differentiation" in southern capuchino seedeaters and distinguish among

possible evolutionary scenarios leading to their formation [31]. Taking advantage of its improved

power and genomic resolution, we applied SIA to sequence data for the species for which we

have the most samples, *Sporophila hypoxantha*. We simulated training (250,000 neutral; 250,000

soft sweeps), validation (1000 neutral; 1000 soft sweeps), and testing (2,500 neutral; 2,500 soft

sweeps) data sets for SIA under a demographic model inferred by G-PhoCS [64]. Simulations

were performed using discoal with the following parameters: (1) mutation rate μ = 1e-9, (2)

recombination rate ρ = 1e-9, (3) derived N_e = 130,000, (4) root divergence time = 1,850,000

generations ago, (5) root N_e = 1,450,000, (6) ancestral divergence time = 44,000 generations ago,

(7) ancestral N_e = 14,380,000, (8) selection coefficient $s \sim U(0.001, 0.02)$, (9) initial frequency at

which selection starts acting on the allele $f_{init} \sim U(0.01, 0.05)$, and (10) segregating frequency of

the site under selection $f \sim U(0.25, 0.99)$. A total of 56 haploid sequences were sampled from

each simulation, matching the number of *S. hypoxantha* individuals (28) in the real data. The SIA

model for *S. hypoxantha* was built, trained and evaluated in an otherwise similar fashion to that

for the CEU population as outlined above.

Using a subset of polymorphism data from [47] of 28 *S. hypoxantha* and 2 *S. minuta* individuals,

we applied our trained model to localize selective sweeps in *S. hypoxantha* on 19 scaffolds that

contain top F_{ST} peaks in at least one pairwise species comparison [48] and/or harbor known

pigmentation-related genes such as *ASIP* (located on scaffold 252; induces melanocytes to

synthesize pheomelanin instead of eumelanin), *KITL* (located on scaffold 412; stimulates

melanocyte proliferation), *SLC45A2* (located on scaffold 404; transports substances needed for

melanin synthesis), and CAMK2D (located on scaffold 1717; cell communication), as well as 316

scaffolds that i) are longer than 100kb, ii) contain more than 1,000 variants, and iii) where more

than 95% of sites have a consensus ancestral allele, as determined by four identical haplotypes

for two individuals from the outgroup species *S. minuta*. The ARG was inferred with Relate for

each scaffold independently. Once the ARG was inferred, the SIA model was applied to sites with

consensus ancestral allele for classification and selection coefficient inference.

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Availability of data and materials

664   The scripts used for analyses in this study are available at [github.com/CshlSiepelLab/arg-](https://github.com/CshlSiepelLab/arg-selection)

665   [selection](https://github.com/CshlSiepelLab/arg-selection) under a GNU GPLv3 license.

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Figures

Figure 1: A high-level framework for automating the detection of selective sweeps. We
first estimate the demographic history for the population of interest, then based on the estimated
demographic history, we simulate neutral regions and sweeps using the discoal simulator [52].
We proceed with ARG inference and then extract ARG-level statistics from each simulated
region. The ARG-level statistics were used as features for a deep-learning Recurrent Neural
Network (RNN) model. Finally, the learned model was applied to the empirical data to infer
sweeps, selection coefficients, and allele-frequency trajectories.

Figure 2: Classification performance of SIA and other methods on simulated data.
Sequence data were simulated under a variety of selection regimes (*s,* shown horizontally) and derived allele frequencies (DAFs) for the beneficial mutation under selection (*f,* shown vertically) (see **Methods** for more details). The prediction task distinguished neutral regions and sweeps. The methods were tested on a set of 200 regions per panel (100 per class), and the receiver operating characteristic (ROC) curve records the true positive rate (TPR) as a function of the false positive rate (FPR). The curve is obtained by varying the prediction threshold from 0 to 1 and recording for each threshold the number of regions correctly assigned (TPs) or misassigned (FPs) as positives (with prediction probability above the threshold). The performance of each method was evaluated based on the area under its ROC curve, or AUROC. We report each method's AUROC as an average across 200 replicate datasets for each model condition. Note that inferred genealogies were used as input to SIA.

Figure 3: Predictions of selection coefficients for simulated regions using SIA and CLUES based on true genealogies. (A) The distribution of inferred selection coefficients for each method under each model condition are reported using a box plot. The box plot for each method reports these five statistics (from bottom to top): minimum, first quartile, median, third quartile, and maximum. The y-axis shows the inferred selection coefficient while the x-axis shows the true selection coefficient. The dashed-black line indicates the true selection coefficient for each model condition. The simulations are based on the CEU demographic model and true genealogies were used as input to both methods. Each model condition (i.e. box plot) represents a set of 400 independent simulations. The mean ranks and variances of the distributions of inferred s were compared using the Wilcoxon signed-rank test (p_W) and the Brown-Forsythe test (p_{BF}), respectively. (B) The root mean square error (RMSE) for each method under each model condition evaluated on 400 independent simulations.

Figure 4: Predictions of selection coefficient on simulated regions using SIA and CLUES based on inferred genealogies, and ImaGene. (A) The distribution of inferred selection coefficients and **(B)** root mean square error (RMSE) for each method under each model condition. The simulations are based on the CEU demographic model where inferred genealogies were used as input to SIA and CLUES, whereas sequence alignments were used as input to ImaGene. Figure layout and description are otherwise similar to **Figure 3**.

LCT
rs4988235
Derived frequency = 0.74
Prob = 0.99
s = [0.01019, 0.01056]

OCA2
rs12913832
Derived frequency = 0.77
Prob = 0.75
s = [0.00539, 0.00575]

MC1R
rs1805007
Derived frequency = 0.12
Prob = 0.949
s = [0.00362, 0.00384]

ABCC11
rs17822931
Derived frequency = 0.13
Prob = 0.620
s = [0.00034, 0.00036]

ASIP
rs619865
Derived frequency = 0.12
Prob = 0.777
s = [0.00172, 0.00197]

TYR
rs1393350
Derived frequency = 0.24
Prob = 0.616
s = [0.00085, 0.00135]

Figure 5: Local genealogies at six loci inferred to be under positive selection in the 1000 Genomes CEU population. Gene name, RefSNP number, derived allele frequency, SIA-inferred sweep probability and SIA-inferred selection coefficient range for each locus are indicated at the top of each panel (see **Table 1** for more details). Taxa carrying the ancestral and derived alleles are colored in blue and orange, respectively.

Figure 6: Local genealogies at six loci lacking signal of positive selection in the 1000 Genomes CEU population. Gene name, RefSNP number, derived allele frequency and probability of neutrality inferred by SIA for each locus are indicated at the top of each panel (see **Table 1** for more details). Taxa carrying the ancestral and derived alleles are colored in blue and orange, respectively.

Figure 7: Local genealogies at five loci inferred to be under positive selection in *S. hypoxantha.* Contig name, position of SNP, derived allele frequency, SIA-inferred selection coefficient range, and the pigmentation gene closest to the locus in question are indicated at the top of each panel. Haploid genomes carrying the ancestral and derived alleles are colored in blue and orange, respectively.

Tables

Table 1: List of genomic loci of interest along with their derived allele frequencies (DAF), sweep probabilities, and selection coefficients inferred by SIA in the 1000 Genomes CEU population.

Gene	SNP ID	Chr	Position*	DAF	P(sweep)	Selection coefficient (95% CI)
LCT [36]	rs4988235	2	136608646	0.74	0.999	[0.01019, 0.01056]
OCA2 [37,38]	rs12913832	15	28365618	0.77	0.750	[0.00539, 0.00575]
MC1R [37,39]	rs1805007	16	89986117	0.12	0.949	[0.00362, 0.00384]
ABCC11 [42]	rs17822931	16	48258198	0.13	0.620	[0.00034, 0.00036]
ASIP [65]	rs619865	20	33867697	0.12	0.777	[0.00172, 0.00197]
TYR [39,65]	rs1393350	11	89011046	0.24	0.616	[0.00085, 0.00135]
KITLG [39]	rs12821256	12	89328335	0.13	0.869	[0.00183, 0.002]
TYRP1 [40]	rs13289810	9	12396731	0.37	0.144	[0.00004, 0.00006]
TTC3 [41]	rs1003719	21	38491095	0.62	0.011	[0, 0]
OCA2	rs7495174	15	28344238	0.94	0.013	[0, 0.00005]
TCF7L2 [66]	rs7903146	10	114758349	0.69	0.035	[0, 0]
ANKK1 [67]	rs1800497	11	113270828	0.80	0.045	[0, 0]
FTO [68]	rs9939609	16	53820527	0.56	0.011	[0, 0]

Note: *Genomic coordinates in GRCh37 (hg19) assembly

Table 2: The top 25 F_{ST} peaks identified in [31] along with the number of partial soft sites in *S. hypoxantha* identified for each scaffold using SIA. To avoid cases with limited power, we focused on sites with segregating frequency ≥ 0.5, SIA-inferred $s > 0.0025$, and SIA-inferred sweep probability ≥ 0.99.

Scaffold	Start position (Mb)	End position (Mb)	Length (kb)	# of partial soft sites*
59	5.74	5.86	120	11
118	7.16	7.22	60	5
252	0.40	0.54	140	3
257.1	21.24	21.78	540	26
257.2	24.40	24.84	440	43
257.3	28.66	28.96	300	10
257.4	31.30	31.38	80	8
257.5	5.78	6.20	420	25 (1)
263	0.00	0.58	580	31
308	0.04	0.20	160	0
404.1	5.04	5.84	800	115 (7)
404.2	10.76	10.96	200	30
412	3.38	3.62	240	15
430	10.98	11.10	120	24
567	2.50	2.80	300	0
637.1	6.00	6.32	320	2
637.2	6.84	6.92	80	4
762	1.65	1.73	80	30
766	1.98	2.10	120	1
791	9.90	9.98	80	15
1717	0.92	0.98	60	7
3622	0.96	1.36	400	8
1635	3.71	3.75	40	4
1954	2.8	2.9	100	17
579	0.1	0.16	60	0

Note: *The number of sweep sites in coding regions is shown in parenthesis.