Characterization of peptide-protein relationships in protein ambiguity groups via bipartite graphs

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Abstract

In bottom-up proteomics, proteins are enzymatically digested into peptides before measurement with mass spectrometry. The relationship between proteins and their corresponding peptides can be represented by bipartite graphs. We conduct a comprehensive analysis of bipartite graphs using quantified peptides from measured data sets as well as theoretical peptides from an *in silico* digestion of the corresponding complete taxonomic protein sequence databases. The aim of this study is to characterize and structure the different types of graphs that occur and to compare them between data sets. We observed a large influence of the accepted minimum peptide length during *in silico* digestion. When changing from theoretical peptides to measured ones, the graph structures are subject to two opposite effects. On the one hand, the graphs based on measured peptides are on average smaller and less complex compared to graphs using theoretical peptides. On the other hand, the proportion of protein nodes without unique peptides, which are a complicated case for protein inference and quantification, is considerably larger for measured data. Additionally, the proportion of graphs containing at least one protein node without unique peptides rises when going from database to quantitative level. The fraction of shared peptides and proteins without unique peptides as well as the complexity and size of the graphs highly depends on the data set and organism. Large differences between the structures of bipartite peptide-protein graphs have been observed between database and quantitative level as well as between analyzed species. In the analyzed measured data sets, the proportion of protein nodes without unique peptides ranged from 6.4% to 55.0%. This highlights the need for novel methods that can quantify proteins without unique peptides. The knowledge about the structure of the bipartite peptide-protein graphs gained in this study will be useful for the development of such algorithms.

Introduction

The digestion of intact proteins to peptides via enzymes like trypsin is a requirement for high-throughput bottom-up proteomics based on mass spectrometry (MS) [1–3]. Because of this, peptides are identified and quantified directly from the MS measurements instead of proteins. The protein ambiguity problem describes the challenge to build a list of proteins for which evidence exists that they are present in the respective sample using protein inference methods [4, 5]. Many identified peptides cannot unambiguously be assigned to a single protein, as the respective peptide sequence is part of multiple protein sequences in the underlying database. Because of shared peptides there is the need to form protein ambiguity groups, which consist of proteins whose presence in a sample cannot be completely decided using the peptides identified in the sample. Beyond this, for protein quantification peptide quantities need to be summarized to protein quantities. This is often done by using only unique peptides, although including shared peptides would be desirable to exploit the full potential of the data and to avoid inaccuracies [6–8]. The worst case, a valid quantification of proteins without any quantified unique peptide, is very challenging and not solved yet despite the large variety of different protein quantification methods available [9, 10].

To illustrate and facilitate the protein inference and quantification steps, bipartite graph representations of the protein-peptide relationships have been used [11–15]. A bipartite graph is an undirected graph G (with node set $N(G)$ and edge set $E(G)$) whose nodes are grouped into two sets $N_1(G)$ and $N_2(G)$, so that each edge connects a node of the first set with a node of the second set. In the context of protein-peptide-relationships, proteins are represented by nodes from $N_1(G)$ and peptides by nodes from $N_2(G)$. One straightforward approach would be to add an edge if and only if the considered peptide sequence is part of the protein sequence based on database knowledge. Another possibility is to draw an edge only if the corresponding peptide was quantified in a specific data set (see section *Construction of bipartite graphs*). As not all proteins are connected to each other via chains of shared peptides, the bipartite graph for the whole data set can be divided into smaller connected components. These components can be analyzed and handled separately during protein inference or quantification.

The structure of the connected components is determined by the underlying protein sequence database and contains valuable information on how difficult the protein inference or quantification problem is in this specific case. The M-shaped example in Fig 1A has two protein nodes that each have one unique peptide node and there is a shared peptide node connecting both protein nodes. In this case, the protein inference step is quite simple, as both proteins are likely to be present in the underlying samples because unique peptides exists. For protein quantification however, the shared peptides contain valuable information that should not be discarded but could also lead to contradictions, if the shared peptides' quantities do not fit to the quantities from the unique peptides. In the second example (N-shape, Fig 1B), protein B does not have a unique peptide and it is unclear, if it exists in the sample. Even if it does, it is not straightforward to quantify this protein, as it only has shared peptides whose quantities are also influenced by protein node A. Although bipartite graphs have been used to display the relationships between proteins and peptides and to assist protein inference or quantification [12–15], a comprehensive analysis and characterization of the occurring graph types has yet not been conducted. In this paper, we generate bipartite graphs of peptide-protein relationships using peptides quantified by mass spectrometry based proteomics in three different data sets as well as theoretical peptides from an *in silico* digestion of the related protein databases used for peptide identification. We characterize common types of graphs as well as aggregated metrics over all graphs of a data set and compare results for theoretical and quantified peptides. This approach

here serves as a model to describe the protein inference and quantification problem in more detail and assess its difficulty for a given data set. Especially the quantification of proteins without unique peptides is difficult or even not possible with most methods. We can show the extend of this problem with the help of the bipartite graphs, which differs between different data sets/organisms as well as between measured data sets and theoretical considerations of an *in silico* digestion of the corresponding databases. Results of this analysis will be helpful for development of new protein inference and quantification methods, especially for proteins without unique peptides.

Fig 1. Examples of bipartite graphs depicting protein-peptide relationships.
Protein nodes are shown as green circles and peptide nodes as red diamonds (unique to a protein node) or blue squares (shared between protein nodes). Each node may represent multiple protein accessions or peptide sequences. Unique peptide nodes are defined as nodes belonging to only one protein node, which may contain several protein accessions. Shared peptide nodes belong to at least two distinct protein nodes.

Materials and methods

Data sets and corresponding protein databases

For building and analyzing the bipartite peptide-protein graphs, three different quantitative peptide-level data sets were used together with the corresponding protein databases. A summary of the search engine parameters for each data set can be found in S1 Table. The samples of the first data set (D1) consist of 13 non-mouse proteins that were spiked into a mouse cell background (C2C12 cell lysate) in different concentrations leading to five different states [16]. Each state was measured in three replicates leading to 15 samples in total. The raw files and the protein database were taken from the PRIDE repository [17], identifier PXD012986. Data were re-analyzed using a KNIME [18] workflow employing the search engines Mascot 2.7 [19], MS-GF+ [20] and X!Tandem [21]. Peptide identifications were combined using PIA [22, 23]. The workflow was similar to the original publication [16], except for a peptide identification filter directly after the spectrum identification leaving only peptides which are strictly tryptic (i.e. cutting after arginine (R) and lysine (K), if not followed by proline (P)). The resulting peptide quantities were used for further analysis (quantified_peptides-featureFinderCentroided.csv, which can be found in the PRIDE upload with the identifier PXD024684). The corresponding protein sequence database (in total 52,824 entries) consists of 52,548 entries from the UniProt reference mouse proteome (UP000000589, version 2017_12, only canonical sequences), the 13 spike-in proteins, 147 spike-in contaminants and 115 contaminants from the cRAP database.

For the second data set (D2) the UPS1 standard (containing 48 human proteins of equal molarity) were spiked into a yeast background in 10 different concentrations [24]. Raw files were taken from PRIDE, identifier PXD001819, and re-analyzed with MaxQuant version 1.6.17.0 [25, 26] and Andromeda [27]. Settings were taken from Workflow 7 of the corresponding publication [24], except that "Trypsin" (no cutting after proline) was used instead of "Trypsin/P". The peptide output table from MaxQuant (peptides.txt file) was used for further processing of the quantitative peptide-level data. The corresponding database (in total 6,342 entries) consists of the UniProt yeast proteome (UP000002311, version 2019_11, 6,049 entries, only canonical sequences), the UPS1 fasta file [28] (48 entries), as well as the contaminants database [29] provided by Andromeda (245 entries).

Data set D3 is a re-analysis of a published ground-truth data set with two experimental groups. 60 μg of HeLa cell lysate was mixed with either 10 μg or 30 μg of *E. coli* lysate, each measured in three technical replicates [26]. Raw files were taken from the PRIDE repository, identifier PXD000279, and re-analyzed with MaxQuant version 1.6.17.0 and Andromeda. The peptides.txt file was used for further processing of the quantitative peptide-level data. The database contains in total 81,709 canonical sequences and consists of the UniProt human reference proteome (UP000005640, version 2021_02, 77,027 entries), the *E. coli* reference proteome (UP000000625, version 2021_02, 4,437 entries) and the Andromeda contaminants database (245 entries). Additionally, we repeated this analysis including isoforms. The reference proteomes with isoforms contain 99,012 entries for human and 4,449 entries for *E. coli*. Together with the contaminant sequences, 103,706 sequences are included. This allows an analysis of the impact of including isoforms on the bipartite peptide-protein graphs.

For each of the protein databases, all protein sequences were digested *in silico* using the digestion rules for trypsin (cut after R and K, if not followed by P) to obtain all theoretical tryptic peptides. All peptides with a maximum of two missed cleavage sites were allowed. Only peptides with a length between five and 50 amino acids (AA) were considered further, as longer or shorter peptides are unlikely to be found via bottom-up MS [30]. Different values for the lower bound for the peptide length (five, six, seven and nine) were evaluated (see section *General overview and impact of minimal peptide length*).

Processing of quantitative peptide-level data

For data set D1, peptides exclusively originating from decoy proteins were filtered out. Intensities for the same peptide sequence but with different post-translational modifications (PTMs) were summed up. Peptide sequences with a length larger than 50 AA or lower than the chosen minimal peptide length (see Section *General overview and impact of minimal peptide length* in the *Results* chapter) were removed, to be directly comparable with the theoretical peptides. The remaining sequences were mapped to the proteins in the corresponding database. The three replicates for each state were combined by averaging the peptide intensities, while zero values were treated as missing values (NA). If two or more of the three values were NA, the combined peptide intensity for this peptide was set to NA. For each possible comparison of the five different states, these aggregated values were used to calculate peptide ratios, which were set to NA if one of the corresponding values was NA. For each comparison, only peptides with a valid ratio (different from NA) were considered in the construction of the bipartite graphs (see Section *Construction of bipartite graphs*). For data sets D2 and D3, peptide LFQ values were extracted from the respective peptides.txt tables and zero values were re-assigned by NA. Further processing was the same as explained for data set D1, except that aggregation of peptides with different PTMs was not necessary here. An overview of the different quantitative peptide-level data sets can be found in S2 Table.

Construction of bipartite graphs

For every data set, the bipartite protein-peptide graphs are constructed using two different sets of peptides. First, all theoretical peptides obtained from *in silico* digestion of the corresponding protein database are used (D1_fasta, D2_fasta, D3_fasta). Second, for each comparison of two states only those peptides with a valid ratio are used (D1_quant, D2_quant and D3_quant). The connected components that arise from the pairwise comparisons of the different states within one data set are put together and analyzed jointly.

To construct the bipartite graphs, a matrix with peptides in rows and all corresponding proteins in columns is created, with entries of 1 if the peptide belongs to the respective protein and 0 otherwise. This matrix is used as a biadjacency matrix [11] to build the bipartite graph of the relationship between proteins and peptides. Proteins that have the same set of peptides are indistinguishable and are therefore collapsed to a single node, i.e. a protein group. Similarly, all peptides sequences that belong to exactly the same set of proteins are collapsed to one single node to further simplify the graph structure. Accordingly, in Fig 1, one node may stand for multiple protein accessions or peptide sequences. This also means that here uniqueness is defined on the level of nodes. A peptide node (which may contain multiple peptide sequences) is defined as unique if it belongs to only one single protein node (which may contain multiple protein accessions), and it is defined as shared if it belongs to at least two protein nodes. In the resulting bipartite graph, protein nodes can be connected to each other via chains of shared peptide nodes. As not all protein nodes are connected this way, the graph can be decomposed into connected components, where all nodes are connected to each other, but not to any other node outside of it. The connected components (called "graphs" in the following for simplicity) can be treated separately for protein inference or protein quantification provided that each MS2 spectrum was assigned to only one peptide sequence or the data have been filtered accordingly.

Two graphs G and H are called isomorphic if there exists a bijective function $f : N(G) \to N(H)$ that maps the node set of G to the one of H, so that the edge structure remains the same: $(u, v) \in E(G) \Leftrightarrow (f(u), f(v)) \in E(H) \ \forall \ u, v \in N(G)$ [31]. Additionally, we require that the function f preserves the node type, i.e. that protein and peptide nodes are distinguished in terms of isomorphisms. Groups of isomorphic graphs reflect identical structures of protein-peptide relationships and contain the same information needed for inference or quantification, except the specific quantities of the peptides. Sets of isomorphic bipartite graphs (isomorphism classes) are built for the data sets, based on theoretical peptides from the *in silico* digestion of the database and quantified peptides with a valid ratio.

Classes of isomorphic graphs are determined by comparing two graphs using the "isomorphic" function from the igraph package, which uses the BLISS algorithm proposed by Junttila and Kaski [32]. Both graphs are transformed into defined canonical forms which are then directly compared. These canonical forms are also used for graphical representation of the graphs in S2 Fig, S3 Fig, S4 Fig and S5 Fig. As the "isomorphic" function does not take into account the type of nodes in a bipartite graph (e.g. a M-shaped and W-shaped graph would be considered isomorphic), we added a criterion that additionally compares the node types of both graphs. In an iterative procedure, each bipartite graph is compared to the current set of isomorphism classes and added to the corresponding class. If necessary, a new isomorphism class is built.

Software

Calculations were performed and graphics created using R 4.1.2 [33]. The package seqinr 4.2-8 [34] was used to import the fasta files and OrgMassSpecR 0.5-3 [35]

(modified version of the Digest() function) to perform the *in silico* digestion. For dealing with (bipartite) graphs, the igraph package 1.2.9 [36] was used, and for further graphics ggplot2 3.3.5 [37]. Additionally, function from the following R packages were used: reshape2 1.4.4 [38], BBmisc 1.11 [39], pbapply 1.5-0 [40], limma 3.47.16 [41], Matrix 1.3-4 [42], matrixStats 0.61.0 [43], openxlsx 4.2.4 [44], xtable 1.8-4 [45], tidyverse 1.3.1 [46], cowplot 1.1.1 [47], ggpubr 0.4.0 [48].

R code that was used for this work is available at:
https://github.com/mpc-bioinformatics/bipartite-peptide-protein-graphs.

Results

General overview and impact of minimal peptide length

Very small and very large peptides cannot be measured by MS for high-throughput bottom-up proteomics [30]. During peptide identification, the length of peptides is usually restricted by limiting the number of amino acids as a setting for the search engine. Even if small peptides are allowed during database search, often only a few are identified and subsequently quantified in the end (see S1 Fig B, exemplary for D1). However, on database level, many small peptides exist after tryptic digestion. Especially peptides with a length of five amino acids (which are usually not identified nor quantified) show a larger proportion of shared peptides compared to longer peptides (see S1 Fig A, C and D). We analyzed the influence of different minimal peptide lengths on the overall bipartite graph structures (Table 1, S3 Table and S4 Table). We chose six and seven, as common default values for search engines, five as an extreme lower bound, and nine, the required length by the Human Proteome Project of the Human Proteome Organization (HUPO HPP) [49].

Table 1. Influence of different minimal peptide lengths on the bipartite graphs for D1_fasta.

	min 5 AA	min 6 AA	min 7 AA	min 9 AA
protein accessions	52,760	52,752	52,741	52,679
protein nodes	52,405	52,388	52,364	52,250
peptide sequences	2,872,496	2,777,410	2,642,464	2,365,974
peptide nodes	133,137	103,517	96,241	92,346
edges	444,272	277,656	241,601	221,186
graphs	2,916	10,356	15,402	17,114
graphs with 1 protein node	2,004	4,809	6,355	7,147
isomorphism classes	206	1,474	2,583	2,692
largest graph*				
protein nodes	47,525	25,006	1,632	939
peptide nodes	126,315	57,763	3,971	2,415
edges	433,174	185,147	14,093	8,751
second largest graph*				
protein nodes	26	91	1,104	529
peptide nodes	75	177	2,940	1,046
edges	288	486	10,541	2,484

* In terms of number of protein nodes.

For D1_fasta (Table 1), 52,824 protein sequences from the database were *in silico* digested to around 2.87 million peptides, including all peptides with a length between five and 50 amino acids and up to two missed cleavages. 64 protein sequences for which

no tryptic peptide within the desired length was found were excluded from the analysis. The number of protein nodes is only slightly lower than the number of protein accessions (this is expected, as only few database proteins should be indistinguishable considering their tryptic peptides). However, the number of peptide nodes is notably lower than the number of peptide sequences (only about 130,000). The bipartite graph covering all these nodes consists of 2,916 connected components that form 206 different isomorphism classes. The largest class consists of the smallest possible graph with only one protein and one unique peptide node, which is an easy case for protein inference and quantification. This system occurs 2,004 times, making up around 69% of all graphs and covering 3.8% of all protein nodes. The largest graph (in terms of the number of protein nodes) contains over 47,000 protein nodes and therefore around 90% of all protein nodes and almost 95% of all peptide nodes. All these proteins are connected via chains of shared peptides. The second largest graph is much smaller with only 26 protein nodes and 75 peptide nodes.

Almost 100,000 short peptides of length five are included in the above analysis. When these are omitted (minimum peptide length six), the number of graphs more than triples to over 10,000. A major influence on this is the fragmentation of the former largest graph, which splits into over 7,000 graphs. Now, still about half of all protein and peptide nodes are connected within one single graph. The number of different isomorphism classes increases dramatically to almost 1,500. For peptides of length five the proportion of shared peptides is increased compared to longer peptides (S1 Fig), which can explain the breakdown of the largest graph. If the minimal peptide length is further increased to seven, the number of graphs rises further and the size of the largest graph decreases. At this minimal peptide length, the largest graph reaches a size comparable to the second largest graph, without loosing too much information. Increasing the minimal peptide length even further, e.g. to nine, would lead to the loss of about 4,000 peptide nodes and 20,000 edges. We decided to use a minimal peptide length of seven, as a further increase risks losing too many well-quantifiable peptides and therefore complexity of the graph. In conclusion, a minimal peptide length of seven seems to be reasonable, as the largest graph is small enough to handle and not too many peptides are lost.

The second database (D2_fasta, S3 Table) contains 6,371 protein accessions, much less than D1_fasta. When using five AA as minimal length, only six protein accessions did not produce at least one peptide with the given criteria. More than 750,000 peptides are created during the *in silico* digestion. After collapsing of nodes, around 6,300 protein and 13,000 peptide nodes remain. 90.1 % of all graphs contain only one peptide node and protein node. There are only 19 different types of graphs. The largest graph contains 70.5% of all protein nodes and 84.1% of all peptide nodes. Increasing the minimal peptide length has a similar effect as for D1: the largest graph falls apart and the number of graphs rises. In contrast to D1, here the size of the largest graph already drops dramatically for a minimum peptide length of six. The number of protein nodes in the largest and second largest graphs are not influenced by omitting peptides of length seven and eight, however, they now contain fewer peptide nodes and edges.

For D3_fasta (S4 Table), based on human and *E. coli* databases, the behaviour is similar to D1_fasta, although on a higher level, because there are more protein accessions present in the FASTA file. Again, the number of graphs and of different isomorphism classes rises for higher minimum peptide length. Between a limit of seven and nine, again the increase has slowed down compared to lower limits.

In summary, the minimal peptide length has a huge impact on the graph structures and especially on the size of the largest graph. For the following analyses, a minimal peptide length of seven for D1_fasta and D3_fasta and of six amino acids for D2_fasta is used. This ensures that the largest graph is decomposed far enough to yield a

reasonable size comparable to the second largest graph. These thresholds are also applied to the quantitative peptide-level data to ensure direct comparability.

Occurring types of graphs

In the following, common isomorphism classes occurring from theoretical or quantified peptides of D1, D2 and D3 are described. For D1_fasta, 15,402 bipartite graphs are constructed which fall into 2,583 different isomorphism classes. The graphs of the ten largest isomorphism classes are shown in S2 Fig (a). The largest class (6,355 occurrences) consists of the smallest possible graph with only one protein and one peptide node. About 41% of all graphs are of this type, containing in total 12.1% of all protein nodes. The second largest class (almost 3,000 occurrences, i.e. around 19% of the graphs) contains graphs with two protein nodes and three peptide nodes. In these M-shapes graphs there are two peptide nodes that are unique for one of the protein groups each, and a peptide node that is shared by the two protein nodes. As each protein group has at least one unique peptide, both should be reported during protein inference. For quantification, however, it is not clear how to handle shared peptides. They may be omitted (as done in some currently used quantification algorithms), but this would mean to delete valuable information.

Among the ten largest isomorphism classes, there are four (ranks three, four, five and ten) that have three protein nodes that are each connected to a unique peptide node. The graphs differ in number of and connections to shared peptide nodes. From an inference and quantification point of view, they behave similar to M-shaped graphs. The same holds for the eighth most common isomorphism class, which contains four proteins, each connected to a unique peptide node. The sixth, seventh and ninth largest isomorphism classes have in common, that one of the protein nodes is not connected to a unique peptide node. This means that from the identified peptides it is not clear if this protein is in the sample or not. However, the quantities of the shared peptides in combination with the unique peptides can help to estimate a quantity for this protein node. E.g., in case of N-shaped graphs with only two protein nodes and one unique and one shared peptide node, this is possible. The ratio for protein B cannot be given exactly, but a lower or upper limit can be calculated, depending on the values of the two peptide ratios. This opportunity is not exploited by most currently applied protein quantification methods. Of the remaining isomorphism classes, 2,306 only occur once in D1_fasta. These are often relatively large systems that are uniquely found in the data due to their complex combination of protein and peptide nodes and the corresponding edges. However, these graphs contain almost 26,700 protein nodes which corresponds to almost 51% of all protein nodes and should not be neglected.

The data set D1_quant contains five states of different combinations of concentrations of 13 spike-in proteins, leading to ten possible pairwise comparisons. Over the ten comparisons 28,802 graphs are formed in total, which belong to 354 different isomorphism classes. The largest isomorphism class (S2 Fig (b)) contains again the most simple type with only one protein and peptide node each. The proportion of this graph type increases to almost 61% of all graphs when compared to the database level, containing 32.5% of protein nodes. In comparison to the database level, the N-shaped graph type occurs more often and is the second most common graph type with almost 19% of all graphs. In contrast, the M-shaped graph that was the second most common on the database level is now on position eight with only 0.62%. From the top ten graph types, eight contain at least one protein node without a unique peptide node. The fifth and tenth largest isomorphism classes do not contain any unique peptide node.

For D2_fasta, 4,908 graphs are formed that fall into 64 different isomorphism classes. Again, the most common graph type is the most simple one (S3 Fig (a)). It is more common than in D1_fasta with more than 88.5% of all graphs that cover in total 68.6%

of all protein nodes. This can be explained by the lower complexity of the analyzed yeast compared to the mouse proteome, which leads to fewer connections between proteins via shared peptides. The second largest class also is the same as for in D1_fasta, with 8.54% of all graphs. The remaining classes are each relatively seldom but nevertheless contain around 18% of all protein nodes. In all of the top 10 graph types all proteins nodes are connected to a unique peptide node.

On quantitative level (D2_quant, S3 Fig (b)), the percentage of the most simple graph type only increases slightly compared to the database level. However, the N-shaped graph type (which did not exist at all in D2_fasta) is now the second most common, like for D1_quant, with 4.77%. The M-shaped graph type moves from place two to three and still covers 4.56% of the graph types. Seven of the graph types in the top ten now contain proteins without any unique peptide, which was not seen on database level.

The graphs for data set D3 (S4 Fig (a) and (b)) behave more similarly to D1 than to D2. While the percentage of the most simple graph type is higher for D3_fasta compared to D1_fasta (almost 50% compared to 41%), this value is quite similar for D3_quant and D1_quant (63% and 61%, respectively). Overall, the graph structure and even the order of the ten largest isomorphism classes is nearly the same for D3_fasta and D1_fasta. On the quantitative level it can be noted that nine of the top ten classes contain protein nodes without unique peptides and there are three with only shared peptides. The M-shaped graph is missing from the top ten here.

Aggregated characteristics of graphs

To characterize the graphs that occur in different situations, the distribution of numbers of different node types is shown in Fig 2. The two main node types are protein and peptide nodes, which can be further divided into unique and shared peptide nodes. The most simple graph type is the only one with just one protein node. This is the most frequent class in all six situations (D1, D2 and D3, on database and quantitative level), and therefore the corresponding bar is the highest. Going from the database to the quantitative level, the proportion of this simple graph type increases due to the disappearance of shared peptides that do not fulfill the criteria (see Section *Processing of quantitative peptide-level data*). This increase is less pronounced for data set D2, since the proportion of the simple graph type is already high on database level. In all four cases, the frequency of graph types with higher numbers of protein nodes decreases steadily. This decrease is strongest for D2 and especially for the quantitative level, where the distribution is shifted to smaller numbers, as graphs split up due to disappearing shared peptides. D1 and D3 show a similar pattern, only the bar for larger graphs with ten or more nodes is higher for D3.

For peptide nodes, the first bar again belongs to the most simple graph type with only one peptide node. On database level, graph types with two peptide nodes (N-shaped, like Fig 1B) are very uncommon and much less present than those with three peptide nodes. This graph type forms the second largest class for D1_quant, D2_quant and D3_quant, but almost never appears on the database level. The M-shaped graph type (see Fig 1A) is the second most common for all three data sets on the database level, which causes a higher bar for a peptide number of three. A lot of M-shaped graph types fall apart from database to quantitative level to the most simple or N-shaped graphs or vanish completely. In general, for the database level, graph types with even numbers of peptide nodes seem to be less common than the following odd numbers. This causes "gaps" for even numbers in the peptide node distributions for theoretical peptides, while these are not present for quantified peptides. For unique or shared peptide nodes these gaps are not existing. In this case also the number zero is possible for the smallest graph type. Zero unique peptides occur rarely, but a little more often

Fig 2. Distribution of numbers of different node types for the bipartite peptide-protein graphs. The distribution of protein nodes, peptide nodes, unique peptide nodes and shared peptide nodes are shown for D1, D2 and D3, on database level (*_fasta) and on the level of quantified peptides (*_quant). Minimal peptide lengths were seven for D1 and D3 and six for D2. The rightmost bar with the label "10+" comprises the values of 10 and above.

on the quantitative than on the database level, especially for D3_quant. These graphs are complex during protein quantification, as there is no unique peptide as an "anchor".

In Fig 3A, the proportions of graphs with exactly one (smallest possible graph, which can easily be handled during inference and quantification) compared to more than one peptide node (all other graphs) is shown. Graph types with more than one peptide node contain at least one shared peptide node and therefore call out for a strategy that uses the potential of these. In general, the proportion of the smallest graph type (light grey bar) increases when going from database to quantitative level. This makes sense, because larger graphs fall apart into smaller ones when non-quantified peptides are missing. For D2, the difference is rather small, as the proportion of the smallest graphs is already high on database level (87.5% vs. 89.5%). For D1 and D3, this proportion increases from 41.3% to 60.9% and 50.0% to 62.9%, respectively, leaving a large number of systems (with an even larger number of affected protein nodes) that are influenced by shared peptides. Protein nodes without a unique peptide node are the most difficult to quantify and are ignored completely or subsumed into protein subgroups by many quantification methods. Fig 3B shows the proportion of graphs that contain at least one of these protein nodes (dark grey bar). It increases on the quantitative level in

comparison to the database level, possibly explained by the disappearance of ₃₈₀
non-quantified unique peptides. For D2, the increase is on a lower level (from 0.1% to ₃₈₁
5.9%) compared to D1 (18.1% to 38.4%). For D3, the proportion of graphs that contain ₃₈₂
at least one protein node without unique peptides is the highest (18.7% on database to ₃₈₃
36.8% on quantitative level). Fig 3C and D show the distribution of uniqueness for ₃₈₄
peptide and protein nodes. The proportion of shared peptides slightly decreases from ₃₈₅
database to quantitative level and is by far the lowest in D2. While the proportion of ₃₈₆
protein nodes with unique and shared peptides both decrease from database to ₃₈₇
quantitative level, the proportion of nodes with only one of the two peptide node types ₃₈₈
increases. Especially for D1 and D3, the frequency of protein nodes with only shared ₃₈₉
peptides strongly increases. These proteins are hard to quantify, as they are missing ₃₉₀
unique peptides and the shared peptides are also influenced by other proteins. On the ₃₉₁
quantitative level, 46.6% and 55.0% of the protein nodes fall into this category for ₃₉₂
D1_quant and D3_quant, respectively, while this proportion is only 6.3% for D2_quant. ₃₉₃

Influence of the inclusion of isoforms ₃₉₄

For data set D3 we conducted the analysis using two different protein sequence ₃₉₅
databases. As described in section *Data sets and corresponding protein databases*, the ₃₉₆
reference proteome databases from human and *E. coli* were downloaded from UniProt ₃₉₇
once containing only canonical sequences and once also including isoforms. In total, the ₃₉₈
database with isoforms contains almost 22,000 additional entries (12 from *E. coli*, the ₃₉₉
remainder from the human part of the database). We chose D3 for this analysis because ₄₀₀
the human database contains the most annotated isoforms among the three analyzed ₄₀₁
species (for mouse, around 7,500 and for yeast 29 isoforms are annotated for the ₄₀₂
corresponding reference proteomes). We expect the largest effect of adding isoforms for ₄₀₃
this data set. ₄₀₄

A summary of the characteristics of the generated bipartite peptide-protein graphs ₄₀₅
with and without isoforms, on database and quantitative level, can be found in S5 Table. ₄₀₆
The *in silico* digest of the database with isoforms now contains 27% more accessions, ₄₀₇
only about 100,000 new peptides are generated, i.e. 3.4%. It can be observed that over ₄₀₈
500,000 of formerly unique peptides are shared after adding isoforms, but the large ₄₀₉
majority remains isoform-unique, i.e. peptides are shared but only between a canonical ₄₁₀
sequence and its isoforms (see Table 2). From the new peptide sequences, the majority – ₄₁₁
around 90% – is unique for one isoform. In total there is a shift from 43.2% shared ₄₁₂
peptides in the canonical database to 58.4% in the database including isoforms (also ₄₁₃
including isoform-unique peptides). It can be observed that the number of bipartite ₄₁₄
peptide-protein graphs slightly decreases when isoforms are added. Two formerly ₄₁₅
separate graphs may be connected by an isoform if it shares peptides with proteins from ₄₁₆
both graphs. The number of graphs with only one protein node decreases by 11.6%. ₄₁₇

Allowing isoforms in the database leads to a slight decrease of quantified peptides. ₄₁₈
Again, the number of graphs decreases. The largest ten isomorphism classes do not ₄₁₉
change heavily, but it can be observed that graph types without any unique peptide ₄₂₀
become more frequent (e.g. the W-shaped graph that rises from 2.73% to 3.80%, see S5 ₄₂₁
Fig (a) and (b)). As a conclusion, while the number of graphs decreases slightly, the ₄₂₂
graphs become slightly larger and there are more protein nodes without unique peptides ₄₂₃
when including isoforms (see Fig 4). ₄₂₄

Discussion ₄₂₅

Despite the large number of methods and tools available for protein inference and ₄₂₆
quantification, there is currently no commonly accepted method for dealing with shared ₄₂₇

Fig 3. Aggregated characteristics of bipartite peptide-protein graphs over the different data sets A: Relative frequency of graphs with one or with more than one peptide node (most simple graph type vs. all other). B: Relative frequency of graphs with none vs. one or more protein nodes, that are not connected to any unique peptide node. C: Relative frequency of unique vs. shared peptide nodes (in terms of belonging to a single vs. multiple protein nodes). D: Relative frequency of protein nodes with only unique peptides vs. unique and shared peptides vs. only shared peptides. Please note: As described in the 'Methods' section, peptide nodes may contain multiple peptide sequences and protein nodes may contain multiple protein accessions.

peptides. Especially the problem of quantifying proteins with only quantified shared peptides is often overlooked by subsuming the protein into a protein group together with the other proteins of the shared peptide. Bipartite peptide-protein graphs have been used in the past to illustrate the protein inference and quantification problem.

Table 2. Unique and shared peptides stemming from *in silico* digestion of D3_fasta and D3_iso_fasta (without and with isoforms).

	without isoforms			
with isoforms	unique	shared	not existing	sum
unique*	1,218,900	0	93,856	1,312,756
isoform-unique**	485,723	0	10,087	495,810
shared	26,027	1,319,690	103	1,345,820
sum	1,730,650	1,319,690	104,046	3,154,386

* Unlike the rest of this paper, unique is defined here as unique for a protein accession. However, the difference between protein nodes and accessions is negligible when looking at the database level.
** Isoform-unique peptides are defined as shared peptides that are shared only between isoforms of the same protein.

Fig 4. Distribution of peptide node type combinations with and without the inclusion of isoforms. Relative frequency of protein nodes with only unique peptides vs. unique and shared peptides vs. only shared peptides for data set D3, with and without isoforms. Please note: As described in the 'Methods' section, peptide nodes may contain multiple peptide sequences and protein nodes may contain multiple protein accessions.

Here, we used the characterization of these graphs as an approach to assess the difficulty of this problem for a given data set. The investigation of bipartite peptide-protein graphs is therefore highly relevant to the current research in proteomics. Furthermore, the analysis of bipartite graphs can also be applied to the field of proteoform research by including isoforms and and peptides with PTMs [?].

In our study we saw that the minimum peptide length is a crucial setting for the *in silico* digestion of proteins and has a huge impact on the structures of the bipartite graphs. Allowing too small peptides leads to large graphs that cover a majority of the proteins inside a database which is not informative. It also does not reflect the situation for real measurements, as small peptides are rarely found or even searched for in database searches. The minimal peptide length that fits best to the data also varies by

database and organism. Here, we have chosen the smallest peptide length which leads ⁠443
to a comparable size of the largest and the second largest graph (seven for D1 and D3 ⁠444
and six for D2) for further investigation. Smaller peptides were not or very rarely ⁠445
quantified in the data sets and lead to a largest graph that covers the majority of ⁠446
protein nodes. If such a large graph would really occur on the quantitative level, this ⁠447
would be a complicated case for protein quantification, because of the high complexity ⁠448
of the interactions of the different proteins via small shared peptides. If we further ⁠449
increase the minimal peptide length on the other hand, we would omit a high number of ⁠450
edges and lose important information about the connection between proteins via shared ⁠451
peptides, that we want to keep. ⁠452

In all analyzed settings, the most simple graph type with only one protein and one ⁠453
peptide node is the most frequent one. In this case, the sequences in the peptide node ⁠454
are unique to the protein node, which may consist of multiple protein accessions that ⁠455
could not be distinguished by their peptides (i.e. they form a protein group). These ⁠456
systems are an easy case for protein inference or quantification. As there are unique ⁠457
peptides, there is strong evidence for the presence of the corresponding protein (or at ⁠458
least one of the proteins within the node). A simple strategy for quantification, like ⁠459
averaging the peptide quantities, may work well in these cases. However, one has to ⁠460
keep in mind that no matter which quantification method is used, this will only lead to ⁠461
a common quantity for all the members of a protein node if it consists of multiple ⁠462
protein accessions. ⁠463

The composition of graph types differs between database and quantitative level. ⁠464
Larger bipartite graphs split up into smaller ones when going from the database to the ⁠465
quantitative level, while at the same time graph types containing proteins without any ⁠466
unique peptide become more prominent. Aggregated characteristics over the whole set ⁠467
of bipartite graphs confirm these findings. There are two opposing effects when ⁠468
comparing database level and quantitative level. First, the proportion of the smallest ⁠469
possible graph (situation with simple solution for quantification) becomes larger. ⁠470
Second, the proportion of proteins without unique peptides is considerably higher on ⁠471
quantitative than on the database level. For these proteins, inference and quantification ⁠472
becomes more challenging, especially in cases where there is no unique peptide in the ⁠473
graph at all. This indicates the importance of considering the quantified peptides ⁠474
instead of assessing the difficulty of quantification only based on the corresponding ⁠475
databases. The reason for the huge differences between database and quantitative level ⁠476
is that many theoretical peptides remain unquantified. These missing peptides cause ⁠477
the graphs to fall apart if these are shared peptides. Missing unique peptides cause ⁠478
some protein nodes to completely lose their unique peptides. These protein nodes may ⁠479
collapse with another node with the exactly same set of quantified peptides, thus ⁠480
leading to a smaller graph. In other cases, they remain in a protein node without ⁠481
unique peptides, which is a challenge for protein quantification algorithms. ⁠482

We defined the uniqueness of peptides on the level of nodes, i.e. a peptide is ⁠483
considered unique if it belongs to only one single protein node. Especially on the ⁠484
quantitative level, this protein node may contain multiple protein sequences/accessions ⁠485
that are indistinguishable regarding their quantified peptides. We have chosen this ⁠486
definition because protein accessions within one node are not distinguishable regarding ⁠487
their (quantified) peptides and therefore in any case only one quantity for this protein ⁠488
group can be calculated. ⁠489

There are also large differences in the characteristics of the bipartite graphs between ⁠490
the three different data sets for theoretical as well as quantified peptides. For example, ⁠491
the analysis of D2 leads to a higher proportion of unique peptide nodes and a more ⁠492
frequent occurrence of the most simple graph type. This makes the overall protein ⁠493
inference and quantification considerably easier than for D1 or D3. A possible ⁠494

explanation could be the different complexities of the predominantly underlying organisms, mouse (D1), yeast (D2), and human (D3). The yeast genome is clearly smaller than the mouse or human genome (around 12 Mb [51] vs. over 2,600 Mb [52] vs. over 2,800 Mb [53], respectively), and the same holds for the proteome (around 6,000 vs. over 50,000 vs. over 75,000 protein entries without isoforms in the UniProt reference proteomes, respectively). Already on the database level, the percentage of unique peptide nodes and of protein nodes with only unique peptides for D2 is much higher than for D1 or D3. This indicates that the complexity of protein quantification can vary a lot for different organisms and data sets, which may also have an impact on the choice of a suitable protein quantification method. For D2 a simple quantification method, like averaging the unique peptides, might work well for most proteins. For D1 or D3, in contrast, this would leave many proteins unquantifiable (46.6% and 55.0%, respectively) because of the lack of unique peptides and would also ignore a lot of information from the large number of shared peptides (47.9% and 53.2%, respectively) (see Fig 3C and D). In this case a more appropriate method that takes into account the shared peptides and the graph structures is crucial to get the most out of the acquired peptide data.

Independent from the peptide quantification method applied, these characteristics can easily be generated and interpreted. In the future, different MS techniques might turn out to generate graphs more close to the database level than others, which may have a huge impact on the quality and difficulty of protein quantification. To reach the same graph shape as on the database level, not all of the theoretically possible peptide sequences need to be identified and quantified but at least one peptide sequence per peptide node, which may be much more realistic.

To reflect the situation within a peptide search engine, we *in silico* digested the whole protein database that was used for searching the respective raw data. We decided to include all possible tryptic peptides inside the desired length range, which also includes all possible peptides with up to two missed cleavages, if they do not exceed the upper limit of 50 amino acids. This blows up the number of peptides. However, it is exactly the situation that the search engines face. Often, the miscleaved peptides will behave similar to the smaller counterparts in regards to uniqueness and will therefore often be contained in the same peptide node. However, we still capture the case in which a longer miscleaved peptides is unique while the shorter version is not.

One has to be careful though, as different specifications (e.g., enzyme for digestion, mass spectrometer type, fragmentation and ionization techniques) may have an impact on the resulting graphs on the quantitative level, although this was not investigated here. Additionally, on the database level the complexity may appear higher or lower dependent on small variations of the settings (e.g., minimal peptide length, allowed number of missed cleavages). The additional consideration of isoforms was performed on data set D3 as an example. While this makes the graphs more complicated and rises the number of protein nodes without unique peptides, isoforms may explain otherwise dubious peptide intensities and can be of high interest for the biological research question.

We did not investigate the influence of peptides with PTMs here, but the bipartite graphs could be helpful for assessing the situation for quantifying different proteoforms with the same peptide sequence. We showed that the underlying organism has a huge effect both on the database and the quantitative level. As a consequence, this kind of study would have to be repeated for other organisms of interest. This again highlights the need to generate the bipartite graphs also for only the quantified peptides and not only for all possible peptides from the database, and then to compare these two scenarios.

Conclusion

In this paper, we analyzed bipartite graphs of protein-peptide relationships using three different quantitative data sets, originating from different(ly complex) species, as well as the corresponding protein databases. Our aim was to better understand the relationship between proteins and peptides and the implications for protein inference and quantification. In general, looking at bipartite peptide-protein graphs and aggregated characteristics is helpful to judge how complex the protein inference and quantification will be for a particular data set. It can also give a hint whether simple protein quantification methods like averaging the unique peptide intensities would lead to a sufficient proportion of quantified proteins or if they would miss a large potential of the data. Depending on the data set, shared peptides can make up a large proportion of all quantified peptides, especially when isoforms are considered. This is accompanied by a large number of protein nodes without unique peptides, which are often overlooked by protein quantification algorithms. As a consequence, there is an urgent need for protein quantification methods that take into account the graph structures and that can use this information to reliably quantify proteins without unique peptides.

Supporting information

S1 Table. **Search engine parameters for the three data sets.**

S2 Table. **Overview over the quantitative peptide-level data sets.**

S3 Table. **Influence of different minimal peptide lengths on the bipartite graphs for D2_fasta.**

S4 Table. **Influence of different minimal peptide lengths on the bipartite graphs for D3_fasta (without isoforms)**

S5 Table. **Comparison of bipartite graph characteristics without and with isoforms on data set D3 (with minimal peptide length of seven amino acids).**

S1 Fig. **Count and relative frequency of shared and unique peptide sequences depending on the peptide length.** Peptide length is given in amino acids. As an example, the values for data set D1 are shown. Uniqueness is here defined as belonging to only one protein node, which may consist of multiple protein accessions.

S2 Fig. **Bipartite graphs of the ten largest isomorphism classes found in data set D1.** (a) D1_fasta, (b) D1_quant, with number of occurrences and percentage of all graphs.

S3 Fig. **Bipartite graphs of the ten largest isomorphism classes found in data set D2.** (a) D2_fasta, (b) D2_quant, with number of occurrences and percentage of all graphs.

S4 Fig. **Bipartite graphs of the ten largest isomorphism classes found in data set D3** (a) D3_fasta, (b) D3_quant, with number of occurrences and percentage of all graphs.

S5 Fig. Bipartite graphs of the ten largest isomorphism classes found in data set D3_iso. (a) D3_iso_fasta, (b) D3_iso_quant, with number of occurrences and percentage of all graphs.

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Availability of data and materials

The datasets supporting the conclusions of this article are available in the ProteomXChange Consortium at http://proteomecentral.proteomexchange.org via the PRIDE partner repository and can be accessed with the dataset identifiers PXD024684 (D1), PXD030577 (D2) and PXD030603 (D3).

Competing interests

The authors declare that they have no competing interests.

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K.S.: Conceptualization, Methodology, Software, Formal Analysis, Writing – Original Draft, Visualization
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