1   **The relative importance of individual attributes varies across preference elicitation**

2   **methods**

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15   **Abstract**

When choosing between different options, we tend to consider specific attribute qualities rather

than deliberating over some general sense of the options' overall values. The importance of each

attribute together with its quality will determine our preference rankings over the available

alternatives. Here, we show that the relative importance of the latent attributes within food rewards

reliably differs when the items are evaluated in isolation compared to when binary choices are

made between them. Specifically, we used standard regression and sequential sampling models to

examine six datasets in which participants evaluated, and chose between, multi-attribute snack

foods. We show that models that assume that attribute importance remains constant across

individual evaluations and binary choices fail to reproduce fundamental patterns in the choice data

and provide quantitatively worse fits to the choice outcomes, response times, and confidence

reports compared to models that allow for attribute importance to vary across preference elicitation

methods. Our results provide important evidence that incorporating attribute-level information into

computational models helps us to better understand the cognitive processes involved in value-

based decision-making.

Keywords: multi-attribute choice, value-based choice, preferential choice, drift-diffusion model,

DDM

Introduction

Most decisions that we make are based on information about a variety of relevant features of the available options. Theories and mathematical models of multi-attribute choice generally agree that, in principle, the decision system in our brains should compare options based on how well they score across all relevant attribute dimensions (Bettman et al., 1998; Gigerenzer & Gaissmaier, 2011; E. J. Johnson & Payne, 1985; Keeney et al., 1993; Levav et al., 2010; Payne et al., 1988, 1993; Russo et al., 1996; Shah & Oppenheimer, 2008). These overall scores, be they based on subjective valuations or more objective features, are typically thought to be calculated as the weighted sums of sub-scores across all dimensions (Bettman et al., 1998; Bhatia & Stewart, 2018; Gigerenzer & Gaissmaier, 2011; E. J. Johnson & Payne, 1985; Levav et al., 2010; Payne et al., 1988, 1993; Russo et al., 1996; Shah & Oppenheimer, 2008). Specifically, each option will be assigned a score along each attribute dimension, and each dimension will be given some weight according to how relevant or important it is to the decision. Simplifications of this strategy that assign equal weights to all attributes (Dawes, 1979; Dawes & Corrigan, 1974), reduce attribute scores to binary better/worse rankings (Russo & Dosher, 1983), or only consider a subset of the attributes have also been proposed (Fishburn, 1974; Tversky, 1972). How well these simpler strategies perform depends on the choice context (Bettman et al., 1998; Gigerenzer & Gaissmaier, 2011; E. J. Johnson & Payne, 1985; Levav et al., 2010; Payne et al., 1988, 1993; Russo et al., 1996; Shah & Oppenheimer, 2008). Regardless of precisely how they are combined, almost every choice is determined by an assessment of multiple attributes. Thus, it is important for both basic and applied researchers to better understand how the attribute composition of choice options (and not just their overall values) influences the decision-making process in the brain.

It is known that individuals' preferences over options that combine monetary gains and

losses with probabilities or time delays may reverse when different methods are used to elicit those

preferences. For example, preferences revealed through choices have been shown to reverse

compared to those elicited by matching, pricing, or rating procedures (Alós-Ferrer et al., 2016;

Alos-Ferrer et al., 2020, 2021; Fischer et al., 1999; Grether & Plott, 1979; Lichtenstein & Slovic,

1971; Seidl, 2002; Tversky et al., 1988, 1990; Weber & Johnson, 2009). A leading explanation for

these preference reversals is that the importance weights on the risk, time, and/or money

dimensions differ across the preference elicitation procedures (Seidl, 2002; Tversky et al., 1988).

Eye-tracking experiments have shown that changes in the proportion of visual fixations to a

lottery's potential monetary outcome relative to its probability across choice and pricing trials are

associated with the differences in the relative weights given to outcomes versus probabilities when

choosing versus setting a price (Alos-Ferrer et al., 2021). This influence of visual attention on

context-dependent weighting is consistent with sequential sampling models that predict that the

effects of overall value and attribute differences on choices are determined in part by the amount

of attention paid to each option or attribute (Busemeyer & Townsend, 1993; Diederich, 1997;

Krajbich et al., 2010; Roe et al., 2001). Together, these theories and data form the basis of our

hypothesis that decision values in naturalistic multi-attribute choices will also be constructed at

the time of choice from the options' basic attributes in a context-dependent manner, rather than

being compared as unitary overall values aggregated across all attributes in a constant fashion. We

aim to show that preference elicitation method impacts the valuation process in consumer choices

over unitary goods whose attributes must be recalled from memory rather than read off a screen.

Consistent with the idea an of attribute-based comparison process, recent work has shown

that the disparity of the options' attribute compositions affects multi-attribute decision making

(Lee & Holyoak, 2021). A pair of options has high disparity if, for example, one option scores

high in the first attribute dimension but low in the second, while the other option scores high in

the second dimension but low in the first (Figure 1a, left panel). On the contrary, a pair of options

has low disparity if both options have similar scores along each attribute dimension (Figure 1a,

middle panel). Notably, two decisions could be equally difficult in the traditional sense that the

overall value ratings of the choice options are equally close together, yet have very different levels

of disparity (Figure 1a, right panel). In multiple independent experiments, Lee & Holyoak (Lee &

Holyoak, 2021) found that choice behavior differs as a function of disparity, such that higher

disparity corresponds to higher choice consistency (i.e., a choice in favor of the option that was

previously rated as having the higher overall value), lower response time, and higher choice

confidence, even after accounting for differences in overall values. Here, we show that

computational models of value comparison that assume an immutable combination of attributes

into the overall option value cannot account for this pattern of results.

Figure 1. Choice disparity. a) A schematic illustration of orthogonal components of choice difficulty: dV and disparity. *The left plot illustrates a "high disparity" choice, and the middle plot illustrates a "low disparity" choice. The orange and green dots represent the alternative options for each choice, each plotted according to its measurements on two attribute dimensions. The example assumes equal importance weights for each attribute, so the iso-value curves are represented by parallel lines with slope -1. The difference in overall value of the options, dV, is the distance between the iso-value curves on which the options lie. Disparity is the distance between the options in the dimension orthogonal to overall value (see Equation 1 below for a mathematical formulation). The right plot shows the location of each choice pair in the transformed dV-disparity space.* **b)** *An example illustration of two choice sets for snack foods, one high disparity (left plot), one low disparity (right plot). As shown by the dashed iso-value lines, all of the available snacks are of comparable overall value (and thus each choice pair is of comparable low dV). However, the two choice pairs are of very different disparity. In the high disparity pair (left), one option scores high on pleasure but low on nutrition, while the other option scores low on pleasure but high on nutrition. In the low disparity pair (right), both options score high on pleasure and low on nutrition.*

Instead, choices between naturalistic multi-attribute stimuli and subsequent confidence

ratings for those choices are best explained by models in which individual attributes are actively

(re)weighted during the comparison process. In our tests, we focus on multi-attribute choices

between naturalistic unitary options with multiple inherent latent features, as opposed to bundled

or conjoint options made up of multiple components (e.g., probability + amount for risky choice;

delay + amount for inter-temporal choice; effort or pain + reward for cost-benefit tradeoffs;

different items for bundled choices). We believe that this type of naturalistic reward, which could

plausibly be treated as an integrated whole, provides a stronger test of whether items are compared

based on fixed weights that yield stable overall values or values constructed from flexible attribute

weights during decisions. We find that models that allow context-dependent attribute weights

during decisions best explain the outcome, response time, and confidence data. However, we also

show that using a subset of attribute-specific ratings together with overall value ratings can help

to better explain the choice data (e.g., when obtaining ratings for the full set of individual attributes

is impractical).

124   **Methods**

Data

We analyzed the data from six previously published experiments (Experiments 1-5 in (Lee

& Holyoak, 2021), plus one unpublished pilot experiment that we label Experiment 0). The total

number of participants across the six datasets was 307, using the same exclusion criteria from the

original study (41 for Experiment 0, 50 for experiment 1, 48 for experiment 2, 54 for experiment

3, 60 for experiment 4, and 54 for experiment 5).

In each experiment, participants completed several distinct phases. They first passively

observed images of individual snack foods (100 in Experiments 0 and 1, 60 in Experiments 2-5).

Second, they provided overall value ratings for each individual snack food. Next, they rated the

pleasure they expected to derive from each food and its nutritional value, in separate experimental

sections (the order of the pleasure and nutrition rating tasks was counterbalanced across

participants). In Experiments 2-5, participants then completed a "non-choice" task (e.g., stating

how similar paired options were to each other), followed by another series of rating tasks (overall

value, pleasure, and nutrition) identical in format to the initial rating tasks. In all experiments,

participants then completed a choice task in which they chose their preferred snack from pairs of

options (50 choice trials for Experiments 0 and 1, 30 choice trials for Experiments 2-5). During

the choice section, after each choice, participants also rated their confidence that the option they

chose was indeed their preferred option on that trial. Lastly, participants completed a final series

of rating tasks (overall value, pleasure, and nutrition) identical in format to the previous rating

tasks. For the purposes of our current study, we only consider those ratings that occurred

immediately prior to the choice task (i.e., the first series of ratings for Experiments 0-1 and the

second series of ratings for Experiments 2-5). See Figure 2 for an illustration of the different tasks.

Figure 2. Task illustration. *An example of what participants saw on the screen during each experimental section. Top row, left to right: Exposure, Value Rating, Pleasure Rating, Nutrition Rating; bottom row: Choice.*

In addition to the aforementioned datasets, we also examined data from an unpublished

pilot auxiliary task that were originally collected along with the primary data reported in (Lee &

Daunizeau, 2021). In the main study, participants provided overall value ratings for 148 food

options, then made 74 choices between pairs of options. Out of the main group of participants, 17

completed the auxiliary task, in which they rated each of the food options in terms of "taste",

"health", "texture", and "appearance". We are thus able to compare versions of our models

(described below) that incorporate four attributes rather than two (the third and fourth attributes

enter the models in the same way as the first and second attributes).

Logistic regression for changes in attribute weights

We fit mixed effects logistic regressions to the binary choice outcomes and the implied

choice outcomes from the overall value rating sessions using the *fitlme* Matlab script. We created

a dummy variable to indicate whether the choice was real ($R = 1$ if the choice was explicit, 0 if

implicit). The regressions included varying intercepts and slopes for each participant, however we

omit these terms in the notation below for conciseness and clarity.

$choice \sim \beta_1 + \beta_2 * DV^a + \beta_3 * DV^b + \beta_4 * R + \beta_5 * DV^a * R + \beta_6 * DV^b * R + \sigma$

Here, choice indicates whether the participant selected the left item in the binary choice

task or if the left item was rated higher in the overall value rating session. The differences in the

ratings for attributes a = pleasure and b = nutrition (DV^a and DV^b) are computed as the rating for

the left option minus the rating for the right option for the respective attributes.

The output of *fitlme* includes estimates and precision (standard error of the estimate or S.E.)

for each of the beta weights in the above equation. To test for our critical difference of difference

measure (the relative impact of pleasure versus nutrition on explicit versus implicit choices), we

calculated a t-statistic as the estimate of β5 minus the estimate of β6 all divided by the square root

of the sum of the S.E. of β5 and the S.E. of β6. We then converted the t-statistic to a p-value based

on standard two-tailed hypothesis testing.

Models

In this study, we consider several variants of the drift-diffusion model (DDM; (Ratcliff,

1978; Ratcliff & McKoon, 2008; Ratcliff & Rouder, 1998)). The specifics of each model are

detailed below. The DDM is a member of the evidence accumulation-to-bound class of models,

wherein the values of the options (in simple two-alternative forced-choice tasks) are repeatedly

compared across time. The so-called evidence that arises in favor of one option over the other is

corrupted by processing (e.g., neural) noise, so repeated samples are accumulated to cancel out the

noise. Once a sufficient amount of evidence has been accrued (i.e., the response threshold is

reached), the process terminates and a choice is made. We fit variants of the DDM in which the

evidence accumulation rate is proportional to the difference in overall value between the options

(ovDDM) or to a weighted linear combination of the differences in individual attributes (maDDM)

to six different empirical data sets. We demonstrate that the maDDM provides a better account of

choice probabilities, mean response times (RTs), and the effects of attribute disparity on choice

outcomes and RT, in terms of both the qualitative predictions and quantitative fits of the models.

Model 1: Overall value DDM (ovDDM)

The first model is a DDM in which only the aggregated, overall values of the two options

influence the evidence accumulation or drift rate on each trial. Specifically, evidence about the

overall value of each option is sampled at each time step, the evidence for the two options is

compared, and the relative evidence in favor of option 1 over option 2 is added to the evidence

accumulator. The cumulative evidence (x) evolves across deliberation time as follows:

200
$$x_t = x_{t-1} + d(\mu_1 - \mu_2) + \varepsilon$$

201
$$\varepsilon \sim N(0, \sigma^2)$$

202
$$x_0 = 0$$

where μ_i is the reported overall value of option $i \in \{1, 2\}$ and σ^2 is white noise in the accumulation

process. Evidence sampling and accumulation proceeds until x reaches a response boundary $\in \{\theta,$

$-\theta\}$, with the sign determining the chosen option (arbitrarily defined as positive for option 1,

negative for option 2). Response time (RT) is equal to t at the moment a boundary is crossed.

Choice probability (p, choice of option 1) and mean RT can be analytically derived (Alós-Ferrer,

2018) as a function of μ_1, μ_2, and σ^2, with θ being fixed (here, to $\theta = 1$ for simplicity):

209
$$DV = \mu_1 - \mu_2$$

210
$$p = \frac{1}{1 + e^{\left(\frac{-2dDV}{\sigma^2}\right)}}$$

211
$$RT = \frac{2p - 1}{dDV}$$

where μ_1 and μ_2 are independent variables, and d and σ^2 are free parameters to be estimated to

capture the individual-specific mean rate of evidence accumulation (drift rate) and level of noise

in the accumulation process, respectively.

Model 2: Multi-attribute DDM (maDDM)

The second model is of the same form as Model 1, except that the evidence accumulator is

driven by two separate evidence streams (one for each attribute dimension: a, b). The process is

otherwise identical, and it unfolds as follows:

220
$$x_t = x_{t-1} + d^a(\mu_1^a - \mu_2^a) + d^b(\mu_1^b - \mu_2^b) + \varepsilon$$

221
$$\varepsilon \sim N(0, \sigma^2)$$

222
$$x_0 = 0$$

223 where μ_i^j is the reported value of option i $\in$ {1,2} along attribute dimension j $\in$ {a,b}, and σ^2 is

224 white noise common to the overall evidence accumulation process. Choice probability and mean

225 RT are derived as:

226
$$DV^a = \mu_1^a - \mu_2^a$$

227
$$DV^b = \mu_1^b - \mu_2^b$$

228
$$p = \frac{1}{1 + e^{\left[\frac{-2(d^a DV^a + d^b DV^b)}{\sigma^2}\right]}}$$

229
$$RT = \frac{2p - 1}{d^a DV^a + d^b DV^b}$$

where d^j are independent free parameters that allow for different rates of evidence accumulation

within each attribute dimension j $\in$ {a,b}.

Model 3: Multi-attribute DDM plus overall value (maDDM+)

Our third model assumes that the drift rate is driven by the separate values of the individual

attributes that were explicitly evaluated (in these experiments, pleasure and nutrition), but that it

is also influenced by other attributes that were not explicitly evaluated. Thus, if the overall value

ratings contain information about the attributes that were rated individually as well as other

attributes that were not rated, including overall value should enhance the model fit. Therefore, in

this model, the evidence accumulator is driven by evidence streams for each explicit attribute

dimension as well as the aggregate overall value estimates. The process is otherwise identical to

that in Models 1 and 2, and it unfolds as follows:

$$x_t = x_{t-1} + d^o(\mu_1^o - \mu_2^o) + d^a(\mu_1^a - \mu_2^a) + d^b(\mu_1^b - \mu_2^b) + \varepsilon$$

$$\varepsilon \sim N(0, \sigma^2)$$

$$x_0 = 0$$

where μ_i^o is the reported overall value for option $i \in \{1, 2\}$, μ_i^j is the reported value of option i ∈

{1,2} along attribute dimension j ∈ {a,b}, and σ^2 is white noise common to the overall evidence

accumulation process. (Note that in cases where the individual attributes are highly correlated

and/or the attribute ratings jointly explain a large portion of the variance in overall values, it may

be necessary to employ orthogonalization or dimensionality reduction techniques, if the goal is to

make inferences about the relative weights or importance of attributes in determining the drift

rate.) Choice probability and mean RT are derived as:

$$DV^o = \mu_1^o - \mu_2^o$$

$$DV^a = \mu_1^a - \mu_2^a$$

$$DV^b = \mu_1^b - \mu_2^b$$

255
$$p = \frac{1}{1 + e^{\left[\frac{-2\left(d^o DV^o + d^a DV^a + d^b DV^b\right)}{\sigma^2}\right]}}$$

256
$$RT = \frac{2p - 1}{d^o DV^o + d^a DV^a + d^b DV^b}$$

257   where d^j are independent free parameters that allow for different rates of evidence accumulation

258   for overall value estimates and within each attribute dimension $j \in \{a, b\}$.

Model fitting procedure

We fit each of the three candidate models to the experimental data, then performed

Bayesian model comparison to determine which of the models (if any) performed better than the

others across the population of participants. For this model fitting and comparison exercise, we

relied on the Variational Bayesian Analysis toolbox (VBA, available freely at https://mbb-

team.github.io/VBA-toolbox/; (Daunizeau et al., 2014)) with Matlab R2020a. Within participant

and across trials, we entered the experimental variables {ratings of overall value, pleasure, and

nutrition for each option} as input and {choice = 1 for left option, 0 for right option; RT; choice

confidence} as output. All ratings and reports of certainty and confidence were rescaled to range

from (0-1). We also provided the model-specific mappings from input to output as outlined in the

analytical formulas above. As we fixed the threshold parameter θ to 1, the parameters to be fitted

were thus the drift rate d and diffusion noise σ^2 terms described above in the model formulations.

VBA requires prior estimates for the free parameters, for which we set the mean equal to 0 and the

variance equal to e^{10} (to allow an arbitrarily large step size during the gradient descent search

algorithm, yet constrain the algorithm to a reasonable search space) for each parameter. The

theoretical drift rate and noise parameters are always positive; we thus constrained the search space

of our model fitting algorithm to the positive domain. VBA then recovers an approximation to

both the posterior density on unknown variables and the model evidence (which is used for model

comparison). We used the VBA_NLStateSpaceModel function to fit the data for each participant

individually, followed by the VBA_groupBMC function to compare the results of the model fitting

across models for the full group of participants.

One benefit of using VBA to fit the data to our models is that it is computationally efficient,

as it relies on Variational Bayesian analysis under the Laplace approximation. This iterative

algorithm provides a free-energy approximation for the model evidence, which represents a natural

trade-off between model accuracy (goodness of fit, or log likelihood) and complexity (degrees of

freedom, or KL divergence between priors and fitted parameter estimates; see (Friston et al., 2007;

Penny, 2012)). Additionally, the algorithm provides an estimate of the posterior density over the

model's free parameters, starting with Gaussian priors. Individual log model evidence scores are

then provided as input to the group-level random-effect Bayesian model selection (BMS)

procedure. BMS provides an exceedance probability that measures how likely it is that a given

model is more frequently implemented, relative to all other models under consideration, in the

population from which participants were drawn (Rigoux et al., 2014; Stephan et al., 2009). This

approach to fitting and comparing variants of DDM has already been successfully demonstrated

in previous studies (Feltgen & Daunizeau, 2021; Lee & Usher, 2021; Lopez-Persem et al., 2016).

An additional benefit of fitting and comparing models within the VBA toolbox is that it

allows us to fit the standard DDM formulas (for choice probability and mean RT) in a generic

manner by simultaneously optimizing parameters over a collection of analytical equations. Thus,

whereas the DDM is summarized by a set of two equations, we can just as easily perform our

model comparison while fitting additional equations alongside the standard DDM equations. We

therefore decided to fit for choice confidence in addition to choice probability and mean RT. We

estimated choice confidence as a linear function of either overall value difference (for Model 1),

individual attribute differences (for Model 2), or both (for Model 3). For each model, we took the

drift rate from the associated DDM equations (see above) to serve as the same value difference

driving confidence. The formulas that we used to estimate confidence under the different models

were thus:

305
$$(M1) \quad confidence = \beta_0 + \beta_1 * d^o DV^o$$

306
$$(M2) \quad confidence = \beta_0 + \beta_1 * (d^a DV^a + d^b DV^b)$$

307
$$(M3) \quad confidence = \beta_0 + \beta_1 * (d^o DV^o + d^a DV^a + d^b DV^b)$$

309   **Results**

Changes in attribute weights

We begin by testing whether the relative importance or weight that people place on each

of the pleasure and nutrition attributes differs between the overall value rating and choice tasks,

even though, in theory, the same valuation processes should be employed in both cases. Other

attribute weights may change as well, but we focus on pleasure and nutrition because we have the

most data on those two attributes. Such a change would be important because it would suggest that

individual attributes guide choices in a different way than they influence isolated evaluations of

one option at a time. Participants in the studies we examined typically chose the more pleasurable

of the two food options in the choice task. Therefore, we used mixed effects (MFX) logistic

regression to determine if pleasure weights reliably increased relative to nutrition weights during

choices. We analyzed the pooled data across all six experiments and included random intercepts

and slopes for all regressors as a function of experiment number and participant in the MFX logistic

regression. In addition to differences in pleasure and nutrition attributes, the regression model

included a dummy variable that distinguished between explicit and implicit choices (*real* = 1 for

explicit choices, 0 for implicit). Thus, we regressed choice on differences in pleasure (dP) and

nutrition (dN) ratings in addition to the interactions between dP and *real* and dN and *real*. The

resulting regression coefficients are shown in Table 1. Critically, the difference in difference of

the impact of dP minus the impact of dN in explicit versus implicit choices was positive and

significant (difference = 0.053, *p* = .005; Figure 3). The result demonstrates that when making

binary choices, participants were more heavily influenced by pleasure than by nutrition, relative

to when they rated the overall value of each food item in isolation. This difference in the influence

of the attributes between the different valuation tasks suggests that computational models using

attribute-level information should explain choices better than a model based on overall value

ratings alone.

MFX Regression Output (pre)			
Fixed effects coefficients	*Estimate*	*S.E.*	*p-value*
intercept	0.506	0.005	0.000
real (intercept)	0.009	0.005	0.079
dP	0.810	0.022	0.000
dN	0.191	0.017	0.000
dP * real	0.021	0.014	0.134
dN * real	-0.032	0.013	0.012

335   **Table 1. MFX regression output (pre-choice ratings).**
336

We repeated the comparison of explicit and implicit choices using post-choice ratings to

test the possibility that increased familiarity with the choice options, rather than differences in the

preference elicitation method, were responsible for the changes in the relative importance weights

of the pleasure and nutrition attributes. By the time that participants entered these final ratings,

they were very familiar with the full set of options, as well as with their own subjective assessments

of overall value, pleasure, and nutrition across the options. Thus, if the changes in attribute weights

between choice and rating tasks remained, it would provide strong evidence against the possibility

that familiarity or exposure time explained the observed differences in relative weights. We found

similar results using post-choice instead of pre-choice ratings (Table 2). The critical difference in

difference measure of the impact of dP minus the impact of dN in explicit versus implicit choices

was again positive and significant (difference = 0.042, p = .015; Figure 3). Thus, the finding that

pleasure was weighted more heavily than nutrition during binary choices compared to individual

ratings holds when using ratings made either before or after the choice session.

MFX Regression Output (post)			
Fixed effects coefficients	*Estimate*	*S.E.*	*p-value*
intercept	0.500	0.006	0.000
real (intercept)	0.016	0.005	0.002
dP	0.827	0.022	0.000
dN	0.195	0.018	0.000
dP * real	0.004	0.013	0.787
dN * real	-0.039	0.011	0.000

351   **Table 2. MFX regression output (post-choice ratings).**
352

355   **Figure 3. Attribute weights differ across tasks.** *The difference between MFX coefficients for*
356   *pleasure and nutrition (dP - dN) is greater for explicit versus implicit choices (i.e., individual value*
357   *rating comparisons). Bar height represents the difference of difference measure, error bars*

358   *represent S.E. The left bar is for MFX regression based on pre-choice ratings, the right bar is for*
359   *MFX regressions based on post-choice ratings.*
360

Qualitative Model Predictions

The diffusion decision models we tested make distinguishable predictions regarding the

impact of two important features of binary choices: overall value difference and attribute disparity.

Lee and Holyoak (Lee & Holyoak, 2021) introduced the term *disparity* as a secondary

characteristic of a decision, orthogonal to the primary characteristic most often used in the field:

overall value difference (often referred to as choice difficulty, where lower value difference

implies higher difficulty). The disparity between two options {i,j} with respect to two attribute

dimensions (here, P for pleasure and N for nutrition) is calculated as:

$$disparity_{i,j} \triangleq \left| \frac{[P_i \, N_i] * \begin{bmatrix} -b_P \\ b_N \end{bmatrix} - [P_j \, N_j] * \begin{bmatrix} -b_P \\ b_N \end{bmatrix}}{\left\| \begin{matrix} -b_P \\ b_N \end{matrix} \right\|} \right| , \text{for options } i, j. \tag{1}$$

where b_P and b_N are the importance weights for the P and N attributes, respectively. Note that it

would be straightforward to extend this formula to incorporate more than two options or more than

two attributes. Disparity calculated in this way effectively transforms the variable space from

attribute dimensions to decision dimensions (see Figure 1 above).

We first show the qualitative predictions that each model (simulated under its participant-

specific best fitting parameters) makes with respect to the effects of value difference (dV) and

disparity (D) on choice consistency, RT, and choice confidence, and how this compares to the

empirical data (Figure 4). To generate the synthetic data, we used the real trial-by-trial values faced

by each individual participant (value of option 1, or v1; value of option 2, or v2; pleasure of option

1, or p1; pleasure of option 2, or p2; nutrition of option 1, or n1; nutrition of option 2, or n2), along

with each participant's best-fitting parameters for each of the three model specifications. Note: we

coded the data such that option 1 always had the higher overall value. Next, we performed mixed

effects regressions of choice (binomial), of RT (linear), and of confidence (linear) on dV and D,

pooling all simulations together and including study and participant as random effect regressors.

Model 3 is the only model from the set we examined that is able to account for the relative

magnitudes and directionality of the associations dV and D show with choice consistency (whether

or not the higher-rated option was chosen), RT, and confidence (see Figure 4).

Figure 4. Model predictions. *Qualitative predictions of the effects of value difference (dV = value of option 1 – value of option 2) and disparity (D; see equation 1) on choice consistency, log(RT),*

390   *and confidence in the empirical (top row) and simulated data (rows 2-4; shown for responses*
391   *simulated using the best fitting parameters for each model; bar heights represent mean mixed*
392   *model regression coefficients across participants; error bars represent s.e.m.).*
393

Quantitative model comparisons

To quantitatively evaluate the models, we computed specific pairwise model comparisons

as well as a simultaneous comparison of all three diffusion decision model specifications. First,

we compared the fit of the model based on overall value (Model 1) to a model based on individual

attribute values (Model 2), to test our hypothesis that decision makers place different importance

or decision weights on attributes during choices than when rating the overall value of each option

in isolation. If the attributes are weighted and aggregated the same way during ratings and choices,

then Model 1, which uses the comprehensive overall value of the foods to estimate choices should

outperform Model 2, which only uses a subset of the foods' attributes (pleasure and nutrition) to

estimate choice outcomes, response times, and reported confidence levels. If instead attributes are

weighted differently during choices compared to ratings, then the flexibility to estimate attribute-

specific decision weights may give Model 2 the advantage even though it is based on only two

attributes out of a larger set. Across all six datasets (studies 0-5 from (Lee & Holyoak, 2021)), the

participant population was split evenly between supporting Models 1 and 2 (estimated model

frequency of 0.50 for each; see Figure 5A).

Figure 5. Pairwise model comparison results. *A) ovDDM (model 1) versus maDDM (model 2).*
B) ovDDM (model 1) versus maDDM+ (model 3). *C) maDDM (model 2) versus maDDM+ (model*
3). *D) Simultaneous comparison of ovDDM (model 1), maDDM (model 2), and maDDM+ (model*
3). We show here the probability that each model best accounted for the data at the participant
level (left panel), across the six studies we examined; each cell represents the probability that the
model (column) best represents the behavior of the participant (row). The black dashed lines serve
to indicate which participants belonged to each of the six datasets. We also show the probability
that each model best explains the data across the participant population (right panel), across all
studies. Here, the black dashed line indicates chance level if all models were equally probable a
priori.

Next, we tested a model in which we tried to combine the advantages of the comprehensive

overall value ratings together with the flexibility to estimate choice-specific weights for a subset

of the individual attributes. We fit a third DDM model (Model 3) that used the pleasure and

nutrition ratings as well as information about the foods' values beyond those two attributes, in the

form of the reported overall value. This provides a measure to quantify the benefit of including

individual attribute ratings in the model in addition to overall value ratings. Model 3 performed

much better than Model 1. Across all six datasets, Model 3 had an exceedance probability of 1 and

an estimated model frequency of 0.92 (see Figure 5B).

We also tested Model 3 against Model 2, to quantify the benefit of including overall value

ratings in the model in addition to individual attribute ratings (pleasure and nutrition). Model 3

performed much better than Model 2. Across all six datasets, Model 3 had an exceedance

probability of 1 and an estimated model frequency of 0.96 (see Figure 5C).

When we formally compared all three models simultaneously, the results were consistent

with the pairwise comparisons reported in the preceding paragraphs. Across all datasets, the

winning model was Model 3, with an exceedance probability of 1 and an estimated model

frequency of 0.90. Model 1 had an estimated frequency of 0.07, and Model 2 had an estimated

frequency of 0.03 (see Figure 5D).

As a robustness check, we repeated the above model comparisons using the final post-

choice ratings from each experiment (i.e., Rating 2 for Experiments 0-1 and Rating 3 for

Experiments 2-5). If somehow the initial ratings were exceptionally noisy or mis-calibrated, we

might expect to find different results when using final ratings to drive the models. All model

comparison results reported above were qualitatively identical (and quantitatively similar) when

using final rather than initial ratings. The only difference was that M1 gained a small amount (6%)

of support when using post-choice ratings (consistent with the idea that the accuracy of overall

value ratings was refined during choice deliberation; (Lee & Daunizeau, 2021)).

The last model comparison analysis that we performed examined the dataset for which we

had overall value ratings as well as four individual attribute ratings (taste, health, texture,

appearance). Here, the model in which the attributes each individually contributed (Model 2)

outperformed the standard DDM based on overall value ratings alone (Model 1; but note the small

sample size, n=17). In the other model comparisons, the results were the same as with our main

datasets. Even though this additional dataset had attribute ratings covering a larger range of

potentially relevant attributes (4 versus 2), Model 3 still dominated the model comparison

(exceedance probability = 1; estimated model frequency for Model 3 = 0.96, for Models 1 and 2 =

0.02 each; see Figure 6).

Figure 6. Model comparison results for four-attribute choice data. *A) ovDDM (model 1) versus maDDM (model 2).* ***B)*** *ovDDM (model 1) versus maDDM+ (model 3).* ***C)*** *maDDM (model 2) versus maDDM+ (model 3).* ***D)*** *Simultaneous comparison of ovDDM (model 1), maDDM (model 2), and maDDM+ (model 3). We show here the probability that each model best accounted for the data at the participant level (left panel), across the six studies we examined; each cell represents the probability that the model (column) best represents the behavior of the participant (row). We also show the probability that each model best explains the data across the participant population (right panel), across all studies. The black dashed line indicates chance level if all models were equally probable a priori.*

Model recoverability

To verify that our model-fitting procedure is suitable for this specific analysis, we performed a test of model recoverability. Specifically, we took as the model input the actual data for each participant in Studies 1-6 (ratings of overall value, pleasure, and nutrition for each option). We then simulated the set of choice probabilities, mean RTs, and confidence reports for each participant, separately according to each of our models, using the actual participant-specific fitted parameters for each model. Finally, we fit all simulated data (per simulated participant) to each of our models and performed the same formal model comparison as with our real experimental data. The results of this procedure can be seen in Figure 7 as a model confusion matrix. This matrix shows, for each true generative model, the percentage of simulated participants (under that model) that were attributed to each of the best fit models by our model-fitting procedure. As shown in the matrix (Figure 7A), there was a fair bit of confusion leading to Model 3 being inappropriately ascribed to simulated participants whose data was generated under Model 1 or Model 2. We speculated that this confusion might have been driven by the confidence reports, because these were heavily biased towards the upper end of the scale and less easy to distinguish between models (compared to RT). We thus repeated the model recovery analysis, this time using only the standard DDM equations (choice probability and RT, but not confidence). As shown in the matrix (Figure 7B), model confusion was low and the procedure attributed the true generating model as the best

fitting model for the vast majority of the simulated participants (recovery accuracy: *87% for Model*

1, 66% for Model 2, 69% for Model 3). There was still some confusion between Model 3 and

Models 1 and 2, which is expected because Model 3 is essentially a combination of Models 1 and

2. Nevertheless, this confusion seems to have hurt Model 3 as much as it helped (i.e., the matrix is

relatively symmetrical), so the results of our quantitative model comparison should be valid. To

confirm the validity of our formal model comparison results reported above (which were based on

choice probability, RT, and confidence), we repeated that analysis while excluding confidence

data. The model comparison results without confidence were nearly indistinguishable from those

we report with confidence, once again showing that model 3 is clearly the best.

Figure 7. Model recovery analysis. *Each cell in the "confusion matrix" summarizes the*
percentage of simulated participants (under each true model) for which our model-fitting
*procedure attributed each of the (best fit) models: **A)** choice probability, RT, and confidence; **B)***
choice probability and RT only (i.e., the standard DDM). Note that there was a fair amount of
confusion when including confidence, but when including only the standard DDM variables, our
fitting procedure attributed the true model as the best fitting model for 87%, 66%, 69% of the time
for Models 1-3, respectively.
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502   **Discussion**

The construction of a choice option's subjective value is an active, malleable process. We

have shown that when options are composed of multiple distinct attributes, the manner in which

these attributes are evaluated and potentially combined to determine the overall value of each

option relative to the other depends on the valuation context. Specifically, the contributions of

inherent attributes such as pleasure and nutrition to the overall value of food rewards differs when

the foods are evaluated in isolation compared to when choices are made between pairs of foods,

even though the goal of the valuation process should be the same in both cases. These findings

indicate that preferences over naturalistic multi-attribute goods are sensitive to the details of the

methods used to elicit them, providing novel evidence of this phenomenon outside the domain of

risky choice.

Most options that humans need to evaluate and choose from in daily life have multiple

attributes or dimensions, and we found that these attributes are combined in a context-dependent

manner to determine an option's value. Previous work on naturalistic multi-attribute decisions has

shown that people form option representations based on a large number of separate underlying

attributes (Bhatia & Stewart, 2018). Our results on both choice outcomes and post-decision

confidence ratings are consistent with these findings. In addition, our model simulation and

comparison results show that the representations that determine an option's subjective value differ

between rating and binary choice tasks. From the simulation tests, it is clear that decision models

based on a fixed, unitary overall value do not generate the influence of disparity (Lee & Holyoak,

2021) on choices, response times, or confidence reports seen in the empirical data. In terms of

quantitative model comparisons, if the overall values of the foods in these six studies were

invariant across the ratings and choice tasks, than models using only the overall values to determine

the drift rate (Model 1) would be preferred over models using either a subset of the food attributes

(i.e., Model 2 with pleasure and nutrition) or individual attributes plus the overall values (Model

3). This is because relative to Model 1, Model 2 adds complexity (one additional parameter) while

at the same time reducing the completeness of the information about the food items – assuming

overall value is determined by more than just pleasure and nutrition. Instead, the model

comparisons showed a tie between Models 1 and 2 in our primary data sets. However, we also

report preliminary evidence from a dataset with ratings of four separate attributes that multi-

attribute model specifications such as Model 2 do far better when they include ratings for more

than two individual attributes. Moreover, if overall value representations were constant, then

Model 3 would add redundant complexity compared to Model 1 and be penalized for that

complexity without benefiting from greater explanatory power in the comparisons. In fact, Model

3 (overall value + pleasure + nutrition) is the best in terms of generating the observed effects of

attribute disparity and accounting for the pattern of choice outcomes and response times.

The superior ability of DDM and regression models including attribute-level information

to explain the effects of disparity on choices, RTs, and confidence reports indicates that the

importance of one or more attributes reliably differs during binary choices relative to ratings.

Specifications of the models that use reports of overall value as the input to the evidence

accumulation process implicitly hold the relative importance of each attribute fixed, and thus

cannot account for differences in value computation between ratings of single options and choices

over two or more options. In contrast, a multi-attribute model specification directly estimates the

importance weights for each attribute within the choice context and is therefore better able to

explain choice behavior. However, these models are agnostic about how or why the importance of

specific attributes differs when individuals are computing the overall value of a single option

compared to choosing between two options.

Many sequential sampling models of decision making posit that attention and salience play

an important role in value computation and comparison. Examples of such models are Decision

Field Theory (DFT; Townsend & Busemeyer, 1993), an extension of DFT known as the Multi-

Attribute Dynamic Decision (MADD) model (Diederich, 1997), and the attentional DDM (aDDM;

Smith & Krajbich, 2019; Krajbich, Armel, & Rangel, 2010). In the DFT model, the drift rate can

vary across deliberation time if, for example, one option is more salient but the other is truly more

valuable. The MADD model makes the multi-attribute nature explicit, and the drift rate fluctuates

over time as the decision maker shifts focus across the set of relevant attributes. Although the

aDDM has generally been applied to the overall values of options, or to distinct items within a

bundle (Fisher, 2017, 2021b), it would be conceptually similar to the MADD if applied at the

attribute level for goods that are inherently multidimensional. Query theory is similar to these

sequential sampling models in that it holds that the order in which a decision maker considers

different aspects (or attributes) of an option alters its resultant valuation (E. Johnson et al., 2007;

Weber et al., 2007). In all these models, it is assumed that options or attributes that receive more

attention will be favored during the value comparison process. However, the relationship between

value and attention is most likely bidirectional to some extent (Anderson et al., 2011; Callaway et

al., 2021; Gluth et al., 2018; Jang et al., 2021; Towal et al., 2013; Westbrook et al., 2020).

Differences in the amount of attention directed to specific attributes during the evaluation

and decision contexts could explain changes in the relative importance of the attributes across

those contexts. Consistent with this idea, changes in the proportions of visual fixations to locations

on a computer screen indicating the monetary amount versus the probability of winning when

pricing versus choosing between lotteries are associated with inconsistencies between the two

preference elicitation contexts (Alos-Ferrer et al., 2021; Kim et al., 2012). Fixation patterns

towards monetary amount versus delay affect temporal discounting rates (Fisher, 2021a), although

whether this might vary in pricing versus choice contexts has not been tested. Internal attention

processes may have effects similar to visual attention for naturalistic multi-attribute goods. The

focus of internal attention is more difficult to measure than visual attention (i.e., fixation locations),

but studies combining decision tasks with neuroimaging or electrophysiology and machine

learning techniques may give us a window into these cognitive processes (Aoi et al., 2020; Peixoto

et al., 2021). Experimental manipulation of focus on a specific attribute (Fisher, 2018; Hare et al.,

2011) may also prove useful, if an appropriate method to dynamically shift attention within each

trial is developed.

There may be other unknown mechanisms beyond differences in attention allocation that

led to changes in the importance weights given to attributes during rating compared to choice tasks.

Although both the rating and choice processes are noisy to some extent, noise is an unlikely

explanation of our results. Unbiased noise in the two tasks could not account for the consistent

increases in the weight on pleasure relative to nutrition during the choice versus rating tasks.

However, it is possible that changes in motivation, engagement, or perceptions of the food items

and/or task goals may have differed in the overall value rating compared to binary choice sessions

instead of or in addition to any change in attribute-level attention. The current data do not allow

us to examine these alternative mechanisms in detail, and it will be important to address them in

future studies.

In addition to providing further insight into the mechanistic nature of value-based

decisions, our current work has practical implications for future studies of decision-making. We

have shown that it is best to use as much attribute-level information as possible when modeling

decisions over multi-attribute stimuli. Most, if not all, naturalistic stimuli are composed of multiple

attributes, thus most studies of decision-making should incorporate attribute-level information. At

the same time, it will often be impractical to collect information on a large number of attributes,

especially if one needs subjective opinions about the attributes from each participant in an

experiment. Our results indicate that combining attribute-specific and overall values may be a good

compromise between attempting to include comprehensive attribute-level information and

conforming to practical constraints. Naturally, which attribute-level information to obtain and how

to best combine it with some type of overall value rating will depend on the hypotheses and

experimental design. Given the clear evidence that the value-comparison process is based on

context-dependent attribute weights, experiments that use a well-designed combination of

attribute-specific and aggregate-level information should prove to be the most useful in advancing

our understanding of many important decision mechanisms. We believe that the datasets we

examined in this study may be the only ones currently available that include subjective ratings of

both overall value and individual attributes. It would be beneficial if future studies also collected

such comprehensive data, for without it, effects such as what we have discussed here might never

be exposed.

<div style="text-align:center">**References**</div>

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