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1   Spatio-temporally efficient coding assigns functions to hierarchical structures of the

2   visual system

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Abstract

Hierarchical structures constitute a wide array of brain areas, including the visual system. One of the

important questions regarding visual hierarchical structures is to identify computational principles for

assigning functions that represent the external world to hierarchical structures of the visual system.

Given that visual hierarchical structures contain both bottom-up and top-down pathways, the derived

principles should encompass these bidirectional pathways. However, existing principles such as

predictive coding do not provide an effective principle for bidirectional pathways. Therefore, we

propose a novel computational principle for visual hierarchical structures as spatio-temporally efficient

coding underscored by the efficient use of given resources in both neural activity space and

processing time. This coding principle optimises bidirectional predictions over hierarchical structures

by simultaneously minimising temporally differences in neural responses and maximising entropy in

neural representations. Simulations demonstrated that the proposed spatio-temporally efficient coding

was able to assign the function of appropriate neural representations of natural visual scenes to visual

hierarchical structures. Furthermore, spatio-temporally efficient coding was able to predict well-known

phenomena, including deviations in neural responses to unfamiliar inputs and bias in preferred

orientations. Our proposed spatio-temporally efficient coding may facilitate deeper mechanistic

understanding of the computational processes of hierarchical brain structures.

Keywords

Author Summary

The visual system in the brain is composed of a hierarchical structure where neural signals pass in

both bottom-up and top-down pathways. To account for how such a hierarchical structure attains a

function to represent the external world, previous research has proposed diverse neural

computational principles. Predictive coding, one of those principles, has attracted much attention

recently that can assign representation functions to hierarchical structures but its computation relies

on hypothetical error units. The present study proposes a novel coding principle for hierarchical

structures without the notion of such hypothetical entities, via spatio-temporally efficient coding which

underscores the efficient use of given resources. Spatio-temporally efficient coding optimises

bidirectional predictions in hierarchical structures of the brain and can assign representational

functions to visual hierarchical structures, without complex inference systems or hypothetical neuronal

entities. We demonstrate that spatio-temporally efficient coding predicts well-known features of neural

responses in the visual system such as that deviation in neural responses to unfamiliar inputs and a

bias in preferred orientations.

1. Introduction

It is well-established that a wide array of brain areas have a hierarchical structure, including the visual

system (Felleman and Van Essen, 1991; Mesulam, 1998; Harris et al., 2019; Hilgetag and Goulas,

2020). Studies have identified a link between hierarchical structures and gene expression (Burt et al.,

2018; Hansen et al., 2021), suggesting that hierarchical structures are genetically determined *a priori*.

Given that one of the major functions of the brain is to represent the external world (deCharms and

Zador, 2000; Kriegeskorte and Diedrichsen, 2019), an ensuing question arises: How do *a priori*

hierarchical brain structures attain functions to represent the external world? This question can be

addressed by identifying a fundamental neural coding principle that assigns representational functions

to hierarchical structures.

The traditional view of the neural coding of visual hierarchical structures is bottom-up visual

information processing, whereby simple features are processed in a lower visual hierarchy and more

complex features created by integrating simple features are processed in a higher visual hierarchy

(Hubel and Wiesel, 1962; Hubel and Wiesel, 1968; Riesenhuber and Poggio, 1999; Riesenhuber and

Poggio, 2000; Serre et al., 2007; DiCarlo et al., 2012; Yamins et al., 2014). However, this view does

not consider the role of top-down pathways that are abundant even in the early visual system, such as

the lateral geniculate nucleus (Murphy and Sillito, 1987; Wang et al., 2006) and primary visual cortex

(Zhang et al., 2014; Muckli et al., 2015; Huh et al., 2018).

The role of top-down visual processing is especially prominent in predictive coding (Rao and Ballard,

1999; Spratling, 2017). According to predictive coding, a higher hierarchy performs top-down

predictions of neural responses in a lower hierarchy. Both inference and learning of predictive coding

are based on the minimisation of bottom-up prediction errors. Predictive coding has been used to

explain the neural responses corresponding to prediction errors (Friston, 2005) and extends from the

explanations of perception to action (Friston, 2010; Clark, 2013). A recent study combined predictive

coding with sparse coding (i.e., sparse deep predictive coding) and demonstrate that it could enhance

perceptual explanatory power (Boutin et al., 2021).

Nevertheless, predictive coding has several theoretical shortcomings. Since inference in predictive

coding aims to minimise prediction errors, the hierarchical structure would require an additional

information processing subsystem to perform this inference. In addition, because bottom-up

transmitted information contains only prediction errors, predictive coding requires the presence of

error units (biological neurons) in the hierarchical structure to represent this prediction error, yet such

error units remain as hypothetical entities and evidence for prediction error responses is limited in

some conditions (Solomon et al., 2021).

A possible approach to overcome the shortcomings of both bottom-up processing and predictive

coding in visual hierarchical structures is to make bottom-up predictions similarly to top-down

predictions across hierarchies, instead of transmitting bottom-up prediction errors. These bidirectional

predictions would realise both context-independent bottom-up predictions and context-dependent top-

down predictions (Teufel and Fletcher, 2020). Such bidirectional predictions eliminate the necessity

for hypothetical error units, while presumably elucidating the neural responses of hierarchical

structures underlying bottom-up feature integration and top-down predictive coding. A neural coding

principle underlying bidirectional predictions of hierarchical structures can be found in the theory of

efficient coding that draws upon the efficient use of given resources (Laughlin, 2001; Bullmore and

Sporns, 2012), which crucially include limited time resources related to processing speed (Griffiths et

al., 2015; Lieder and Griffiths, 2020). A possible solution to promote the most efficient use of limited

time resources by the bidirectional prediction system is to render present neural responses equal to

future ones before the occurrence of future neural responses. This can be achieved by minimising the

temporal differences between present and future neural responses. Accordingly, we consider this

temporal difference minimisation as our *learning principle*, referred to as *temporally efficient coding*. A

minimal temporal difference indicates that bidirectional prediction is accurate. Here, *inference* simply

refers to a bidirectional prediction mediated by top-down and bottom-up pathways. Unlike inference in

predictive coding, which requires further error minimisation, inference in temporally efficient coding

involves simple monosynaptic transmission (i.e., a connection that passes via a single step rather

than multiple steps).

Since temporally efficient coding includes a trivial solution, in that neural responses are invariant to

changes in external events. we circumvent this issue by adding a complementary neural coding

(learning) principle that maximises the informational entropy of neural responses. It maximises the

neural response space available to represent the external world under the constraints of both the

number of neurons and maximum firing rates. Maximal entropy coding indicates that the system uses

spatial resources of neural responses efficiently (Attneave, 1954; Barlow, 1961; Laughlin, 1981),

referred to as *spatially efficient coding*. By combining spatially efficient coding and temporally efficient

coding, we propose a neural coding principle termed *spatio-temporally efficient coding* (Fig 1).

It is noteworthy that minimising temporal differences in upper hierarchies may, at first glance, be

reminiscent of the slow feature analysis (Wiskott and Sejnowski, 2002; Berkes and Wiskott, 2005;

Creutzig and Sprekeler, 2008). However, the upper hierarchies of the proposed spatio-temporally

efficient coding need to change dynamically to predict rapidly changing visual inputs and neural

responses of the lower hierarchies, whereas the upper hierarchies of the slow feature analysis need

to change slowly. Minimising temporal differences in spatio-temporally efficient coding does not aim at

extracting slow features, but rather aim at the representation of rapidly changing visual inputs with

stabilizing neural responses as quickly as possible.

To determine how a visual hierarchical structure with spatio-temporally efficient coding represents

external visual events, we repeatedly exposed a visual hierarchical structure to natural scene images,

enabling it to learn the parameters of bidirectional prediction networks between top-down and bottom-

up hierarchies using spatio-temporally efficient coding (Fig 1). Using simulations, we observed that

spatio-temporally efficient coding enabled the visual hierarchical structure to implement desirable

neural representations. In addition, the visual hierarchical structure learned to represent natural scene

images by spatio-temporally efficient coding and could predict well-known perceptual responses. First,

the visual hierarchical structure exhibited deviant neural responses to unfamiliar visual inputs (i.e.,

neural responses to unfamiliar inputs were smaller or larger than those to familiar ones), indicating

selectivity (Margoliash, 1983; Waydo et al., 2006) and/or familiarity suppression (Huang et al., 2018;

Issa et al., 2018) of visual cortical neurons. Second, the visual hierarchical structure demonstrated

simple cell-like receptive fields with preference for horizontal and vertical orientations over oblique

orientations, resembling the orientation preference of visual cortical neurons (Furmanski and Engel,

2000; Li et al., 2003; Girshick et al., 2011). These simulation results demonstrated that the proposed

spatio-temporally efficient coding could assign functions representing the external world to

hierarchical structures in the visual system without theoretical complexity and hypothetical entities.

Fig 1. Spatio-temporally efficient coding. This illustration depicts a hierarchical structure of the brain

and learning objectives. The hierarchical structure learns to represent input from the external world,

which is depicted as black squares (e.g., visual input). Open black circles indicate an ensemble of

neuronal units in each hierarchy of the brain. Inference based on spatio-temporally efficient coding is

made by neuronal units as bottom-up and top-down predictions over time (black arrows). Learning in

spatio-temporally efficient coding consists of two objectives: minimising the temporal differences

between present and future neural responses and maximising the informational entropy of neural

responses. For example, predictions (purple arrows) are optimised to minimise the temporal

differences between present neural responses at the corresponding hierarchy (red filled circle) and

future neural responses (circle to the right of the red filed circle) while concurrently   maximising the

informational entropy of neural responses at the corresponding hierarchy (red filled circle).

2. Results

2.1. Spatio-temporally efficient coding in visual hierarchical structures

In the present study, visual information processing in hierarchical structures was established as

biologically inspired temporal processing. Specifically, visual information processing is described as a

function f_t for both image X_{image} and neural responses X_h in each hierarchy h such that it maps

from X_{image} and X_h at time $t-1$ to those at time t:

$$f_t: X_{image,t-1} \times X_{h=1,t-1} \times \ldots \times X_{h=H,t-1} \rightarrow X_{image,t} \times X_{h=1,t} \times \ldots \times X_{h=H,t} \tag{1}$$

where $X_{h,t-1}$ and $X_{h,t}$ are the neural responses X_h at time $t-1$ and t, respectively, at hierarchy h.

The function values of adjacent hierarchies X_h and X_{h+1}, as well as those for X_{image} and $X_{h=1}$, are

mutually influenced, representing the hierarchical structure. These influences are expressed as

mathematical transformations based on synaptic weights, biases, and sigmoid nonlinearities added to

the transformations (see Section 4.2 for details of the transformations). This function f_t makes

inferences using spatio-temporally efficient coding.

Learning in spatio-temporally efficient coding minimises the ensuing objectives of both temporally and

spatially efficient coding. The objective of temporally efficient coding is given by:

$$L_{Temporal} = \sum_{h=0}^{H} \sum_{n=1}^{N} \left(f_t \circ f_{t-1}(X_{image=n}) - f_{t+1} \circ f_t \circ f_{t-1}(X_{image=n}) \right)^2 \tag{2}$$

where $\circ$ is the function composition, $X_{image=n}$ indicates that the image is fixed to the nth sample

throughout the temporal processing, squaring is operated component-wise, and the outer summation

$\sum_{h=0}^{H}(\cdot)$ is operated on the range of f where $h=0$ denotes $X_{h=0} := X_{image}$. The minimisation of the

given objective minimises the temporal differences between present and future neural responses. The

objective of spatially efficient coding is given by

$L_{Spatial} = \sum_{h=1}^{H} \sum_{n=1}^{N} \log P\left(f_t\left(X_{image=n}\right)|_{X_h}\right)$ (3)

where $f_t(\cdot)|_{X_h}$ indicates a restriction of the range of the function value $f_t(\cdot)$ to X_h, and $P(\cdot)$ is a

probability. Because the term within the summations is an estimation of negative informational

entropy, minimising the objective maximises the informational entropy of f_t. Finally, the objective of

spatio-temporally efficient coding is a linear combination of those two objectives:

$L = L_{Temporal} + \lambda L_{Spatial}$ (4)

where λ is a regularisation parameter. A smaller λ indicates a greater emphasis on the temporally

efficient coding objective, whereas a larger λ indicates the opposite.

In the present study, the depth H of hierarchies was set to 2, the minimum depth to realise both

bottom-up and top-down pathways in the same hierarchy (Fig 2A). For a given image, the duration of

temporal processing of f_t was given as 5 (i.e., $t \in [1,5]$) in both learning and inference, because four

time steps are required for the image information to reach the top hierarchy and return over $H = 2$

hierarchies, in addition to one time step to obtain future neural responses. The minibatch size N was

set to 40 (see Section 4.2. for more details).

In our simulations, we repeatedly exposed the hierarchical structure to natural scene images, which

enabled it to learn the bidirectional predictions between top-down and bottom-up hierarchies using

spatio-temporally efficient coding with a range of the balancing parameter λ. Successful learning was

confirmed by minimising or stabilising L during learning. Further, we verified that the learned

hierarchical structure could successfully reconstruct an input image, as shown in Fig 2C.

2.2. Balancing between temporally and spatially efficient coding

The temporally efficient coding objective that minimises the temporal difference between present and

future neural responses not only renders a neural representation suitable for the objective but also

renders the visual information process temporally stable. In contrast, the spatially efficient coding

objective that maximises the informational entropy of neural responses renders the process noisy.

Based on our simulations, we confirmed this phenomenon by observing that neural responses were

temporally stable with smaller λ (i.e., weighing toward temporally efficient coding), whereas they

became noisy with larger λ (i.e., weighing toward spatially efficient coding) (Fig 2C). In addition,

when the λ values were too small or too large (i.e., strongly biased to either temporally or spatially

efficient coding), the hierarchical structure failed to represent visual images appropriately (Fig 2D),

highlighting the need for an appropriate balance between spatially efficient coding and temporally

efficient coding in the visual hierarchical structure.

A change in balance between the two objectives also altered the relative strengths between bottom-

up and top-down synaptic connections. Simulation results demonstrated that top-down synaptic

strengths from hierarchies 2 to 1 were increased compared to bottom-up synaptic strengths from

images to hierarchy 1 as λ increased, with an emphasis on spatially efficient coding (Fig 2B, see

Section 4.2 for details on the computation of synaptic strength). This finding suggests that the balance

between spatially and temporally efficient coding could be related to the balance between bottom-up

and top-down synaptic strengths in the brain.

Fig 2. A simulation of spatio-temporally efficient coding. (A) Architecture of the simulation model. An

input image is divided into four subspaces with overlaps, denoted by different colours. A subset of

neuronal units in hierarchy 1 receive corresponding parts of the image (matching colours). There is no

spatial correspondence between hierarchies 1 and 2. Pink and purple arrows indicate bottom-up and

top-down predictions, respectively. (B) The magnitude of synaptic weights on hierarchy 1 units is

compared for different λs, where λ is a balancing parameter in the objective function,

$L = L_{Temporal} + \lambda L_{Spatial}$ (see Eq. 4). Each cross indicates the L2 norm of synaptic weights for each

unit. Black squares indicate the mean. (C) Left: Four different original input images and their

reconstructions from the neuronal responses of hierarchy 1. Right: Representative neural responses

of the hierarchy 1 units for different λs. The neural response is the output of the sigmoid function and

is therefore normalised to a range between 0 and 1. (D) Similar to (C), but with examples of λs that

are too small or too large to balance between temporally and spatially efficient coding.

2.3. Appropriate neural representations of the external world

As a major function of the brain is to represent the external world (deCharms and Zador, 2000;

Kriegeskorte and Diedrichsen, 2019), we investigated whether spatio-temporally efficient coding

creates appropriate neural representations of the external world. We quantified the appropriateness of

neural representations by examining the correlations between a natural scene image space and a

neural response space. Specifically, we first measured the Euclidean distances from a natural scene

image (i.e., reference image) to other natural scene images in the image space and the distances

from the neural responses for the reference image to those for other compared images in the neural

response space (Fig 3A). When calculating the distances between neural responses, we used the

neural responses at five time steps after receiving a given image based on the assumption that the

neural responses became temporally steady after five steps of temporal processing (see Fig 1). We

then measured the Pearson's linear correlation between the distances in the image space and those

in the neural response space. A high correlation indicates that neural responses tend to be similar

when the visual system perceives natural scenes close to each other (in the sense of Euclidean

distance). We set each image sample as a reference and repeated the calculations for the correlation

across all image samples. We defined global similarity as the average correlation obtained by using

the distances from one image to all other images, and local similarity as the average correlation

obtained by using the distances from one image to its neighbouring images only (1% of all images).

For illustration, we visualised the distance from the reference image in Fig 3A to others by projecting

the images onto a 2D space using t-distributed stochastic neighbour embedding (t-SNE) (van der

Maaten and Hinton, 2008). We performed the same visualisation of the corresponding neural

responses in each hierarchy. The distances in the 2D image space were largely preserved in the 2D

neural response space (Fig 3B).

From the simulations, we identified high global similarities (> 0.6) between the natural scene image

space and neural response space (Fig 3C). Global similarities were higher for the lower hierarchy

than for the higher hierarchy, and increased with smaller λ for the lower hierarchy (Fig 3C). Local

similarities were close to 1 for all λs and hierarchies, demonstrating that the spatio-temporally

efficient coding produced locally well-suited neural representations of natural scene images (Fig 3D).

Neural responses exhibited certain noise with spatio-temporally efficient coding, especially when λ

was high (Fig 2C). We investigated whether this noise interfered with the neural representations of the

visual images. To assess the interference by noise, we assumed that the neural responses converged

to represent a given image after certain time steps of the bidirectional predictions. Here, we set the

time step to 10 and measured the variability in neural responses from time step 1 (i.e., when receiving

an input image) to time step 9 until convergence. Temporal variations were computed using the

Euclidean distance from the neural responses at each time step (1, …, 9) to neural responses at time

step 10. We also computed the Euclidean distance from the neural responses at time step 10 and

those for an image that was the nearest to the given image in the image space. We compared the

temporal variations above with this distance to the nearest neighbouring image by calculating the ratio

of the temporal variations over the distance to the nearest neighbouring image. A ratio exceeding 1

indicates that the noise could significantly interfere with neural representations to be confused with

nearby images. Within the range of our simulation parameters ($\lambda \in [10, 100]$), the ratio was kept below

1 on average for the majority of time steps at each hierarchy, even with higher values of λ (Fig 3E),

indicating that the noise caused by maximising entropy with spatially efficient coding did not

significantly interfere with neural presentations over time.

Fig 3. Neural representations of visual images by spatio-temporally efficient coding. (A) Examples of

relative Euclidean distances from the reference image (Ref. left) to other images in the natural scene

image space are depicted on the horizontal axis. Relative Euclidean distances from the neural

representations of the reference image at hierarchy 1 to those of corresponding other images are

depicted on the vertical axis. (B) Left: Visualisation using t-distributed stochastic neighbour

embedding (t-SNE). The colour code indicates normalised distances from the reference image in (A)

to all other images in the natural scene image set, measured in the t-SNE-generated natural scene

image space. The black cross indicates the reference image in (A). Middle: Visualisation of neural

responses of images at hierarchy 1 using t-SNE. The colours of each neural response represent the

normalised distance of the corresponding image measured in the left plot. Similar patterns of colour

codes indicate that the similarity between images is well preserved in neural representations. Right:

The same visualisation of neural responses at hierarchy 2. (C) Global similarity based on correlations

of Euclidean distances between overall natural scene images (N = 4,212) with those of corresponding

neural responses. Error bars indicate standard deviations. (D) Local similarity based on correlations of

Euclidean distances between overall natural scene images (N = 42) with those of corresponding

neural responses. (E) The ratio of the temporal variations of neural responses relative to the

Euclidean distance from the nearest image (see text for details on the computation of temporal

variations). The dotted lines denote the ratio of 1. Error bars indicate standard deviations.

2.4. Deviant neural responses to unfamiliar inputs

The visual system often responds selectively to sensory inputs (Margoliash, 1983; Waydo et al.,

2006). Even for the type of sensory inputs to which the visual system is responsive, unfamiliar inputs

induce larger neural responses compared to familiar inputs (Huang et al., 2018; Issa et al., 2018).

These large neural responses to unfamiliar inputs are thought to be due to prediction errors (Issa et

al., 2018). Accordingly, we investigated whether spatio-temporally efficient coding could predict the

phenomenon of large neural responses to unfamiliar inputs without the introduction of prediction error

responses mediated by error units.

In the simulations, the visual hierarchical structure learned to be familiar with natural scene images,

and novel handwritten digit images were used as unfamiliar visual inputs (Fig 4A). The simulation

results revealed that neural responses were distributed over middle values for familiar images and

over smaller or larger values for unfamiliar inputs (Fig 4B and 4C), suggesting that spatio-temporally

efficient coding could predict the phenomenon of deviant neural responses to unfamiliar inputs.

Further, we investigated the neural responses to locally unfamiliar and globally familiar images. We

composed new images such that a portion of only one quadrant of the image was unfamiliar, and the

rest was familiar (Fig 5A). According to global precedence (Navon, 1977; Rezvani et al., 2020), such

partially unfamiliar images are preferentially perceived as familiar ones. The simulation results

demonstrated that deviant neural responses were predominantly localised to the hierarchy 1 units

connected to unfamiliar portions of the images (Fig 5B). In addition, deviant neural responses rarely

propagated to hierarchy 2 units (Fig 5C) and thus did not perturb hierarchy 1 units connected to

familiar inputs in return (Fig 5D and 5E), consistent with the predictions of global precedence.

Fig 4. Neural response distributions for familiar and unfamiliar inputs. (A) Natural scene images are

used as familiar inputs (for learning in the visual hierarchical structure) and handwritten digit images

are used as unfamiliar inputs (not used in learning). (B) Examples of neural response distributions of

hierarchy 1 units for each of the five time steps of bidirectional predictions, corresponding to images in

(A). The colour scale indicates the proportion. (C) Overall neural response distributions in response to

all input images (either familiar or unfamiliar) at hierarchies 1 and 2, respectively.

Fig 5. Neural response distributions for partially unfamiliar inputs. (A) Image reconstruction from

neural responses over time. Using spatio-temporally efficient coding of learned natural scene images,

the visual hierarchical structure reconstructs a familiar image well from time steps 2 to 5 (top). The

same hierarchical structure also reconstructs a partially familiar image well, with the exception of a

part of the image, marked by a yellow dotted line (bottom). (B) Neural response distributions of

hierarchy 1 units corresponding to each of the four parts of the image. Box colours match with the

image parts in (A). The green box contains unfamiliar input. (C) Neural response distributions of

hierarchy 2 units. Note that there is no spatial segregation of hierarchy 2 units corresponding to the

parts of the image (see Fig 2A). (D, E) The ratios of the distance (relative temporal variation) between

neural responses for familiar and partially unfamiliar inputs relative to the average distance from an

image to neighbouring images (N = 42) at hierarchies 1 (D) and 2 (E), respectively. The scale bars

indicate the standard deviation. The dotted horizontal line indicates a ratio of 1.

2.5. Preferred orientation biases of receptive fields

Neurons in the visual system prefer horizontal and vertical orientations over oblique orientations

(Furmanski and Engel, 2000; Li et al., 2003). Indeed, orientation discrimination is more sensitive to

horizontal and vertical orientations than to oblique orientations (Girshick et al., 2011). These biases

are due to the environmental statistics of natural scenes (Girshick et al., 2011). We investigated

whether hierarchy 1 units in the visual hierarchical structure that learned by spatio-temporally efficient

coding of natural scene images exhibited such biases. We presented a moving bar oriented in one of

eight angles that moved in the direction perpendicular to the orientation angle (Fig 6A) and defined

the response of each unit to that orientation by the largest response during presentation. We then

defined the preferred orientation of each unit as the orientation that elicited the largest response.

Simulation results revealed that hierarchy 1 units preferred horizontal and vertical orientations over

oblique orientations in all λ conditions (Fig 6B), consistent with the orientation bias of visual cortical

neurons and in accordance with context-independent bottom-up prediction (Teufel and Fletcher,

2020).

Fig 6. Orientation preference of hierarchy 1 units. (A) Orientation images used to test the visual

orientation preference of neuronal units at hierarchy 1 in the visual hierarchical structure that learned

by the spatio-temporally efficient coding of natural scene images. White bars in each of the eight

orientations are moved in the perpendicular directions denoted by blue dotted arrows. (B) Histograms

of the orientation preference of hierarchy 1 units at time step 5 for different values of λ.

3. Discussion

The present study aimed to find computational principles that enables visual hierarchical structures to

attain the function to represent external visual information. To address the lack of neural coding

principles to encompass both bottom-up and top-down pathways, we propose spatio-temporally

efficient coding as a novel computational model. As a principled way of efficiently using given

resources in both neural activity space and processing time, this coding principle optimises

bidirectional predictions over hierarchical structures by simultaneously minimising temporally

differences in neural responses and maximising entropy in neural representations. Simulation results

showed that the proposed spatio-temporally efficient coding assigned the function of appropriate

neural representations of natural scenes to a visual hierarchical structure and that it could predict

deviations in neural responses to unfamiliar inputs and a bias in preferred orientations, which are well

known characteristics of the visual system.

Cortical Hebbian-like spike-timing-dependent plasticity (STDP) (Feldman, 2000; Froemke and Dan,

2002) is a potential mechanism underlying the temporally efficient coding proposed in this study. If

bidirectional predictions of the hierarchical structure increase future postsynaptic responses, STDP

will strengthen these synaptic connections, which may increase future postsynaptic responses.

Indeed, this phenomenon is underscored by a minimisation of the temporal difference in neural

responses, rendering near future neural responses closer to distant future neural responses. As such,

the concept of temporally efficient coding proposed herein is consistent with cortical Hebbian-like

STDP.

Since its initial proposal (Attneave, 1954; Barlow, 1961), spatially efficient coding has been validated

experimentally (Laughlin, 1981). However, observed correlations between neurons, which maximise

entropy to a lesser extent compared to mere spatially efficient coding assuming no inter-neuronal

correlations, have yet to be incorporated into the principle of spatially efficient coding. Empirically

observed neuronal correlations may drive computational processes of the brain away from strict

spatially efficient coding. Recent studies suggest that biological visual systems are intermediate

between strict spatially efficient coding and correlated neural responses (Stringer et al., 2019).

Therefore, to create biologically plausible computational models, it is necessary to mitigate the

spatially efficient coding objective by combining firing-rate-dependent correlations (de la Rocha et al.,

2007). This enables more accurate predictions of visual perception mediated by visual hierarchical

structures. As we focused on integrating spatially efficient coding with temporally efficient coding for

computation in hierarchical structures, this study did not incorporate the correlations between neurons

in spatially efficient coding, which will be pursued in follow-up studies.

Based on our simulations, we observed that the learning of bidirectional prediction networks with

spatio-temporally efficient coding was hindered when the balancing parameter λ was too small or too

large (Fig 2D). Therefore, it was necessary to confine λ within a certain range, in which the

magnitude of λ affected neural responses such that a larger λ rendered responses more variable

(Fig 2C). Such increased variability is likely to originate from recurrent responses via higher

hierarchies rather than the noise of neural responses. This was confirmed by the observation that top-

down synaptic weights become larger than bottom-up synaptic weights when λ increased (Fig 2B).

Although a large λ attenuated the appropriateness of neural representations (Fig 3), it rendered

stronger top-down synaptic connections in hierarchy 1 (Fig 2B), which is consistent with the previous

finding that top-down synaptic connections are stronger than bottom-up connections in the lateral

geniculate nucleus (Sillito et al., 2006). As to why top-down synaptic weights increase with a larger λ

value (Fig 2B), we speculate that learning via spatio-temporally efficient coding may increase the

range of neural responses to maximise entropy through top-down pathways. While the bottom-up

pathways originating from external inputs are invariant during learning, the top-down pathways

originating from higher hierarchy neural responses are more flexible to adjustment to maximise

entropy during learning.

The deviant neural responses to unfamiliar inputs observed in this study (Fig 4 and 5) arise from

compact, well-organised neural representations for familiar inputs (distributed over the middle value).

As such, neural representations for familiar inputs extrude neural responses to unfamiliar inputs into a

range of deviant neural responses. We conjecture that the visual system may generate deviant neural

responses via a similar mechanism. Simulations in the present study demonstrated that neural

responses were distributed around smaller or larger extremes for unfamiliar inputs and around

intermediate values for familiar inputs (Fig 4B and 4C). In a separate analysis, we allowed the neural

responses to familiar inputs be distributed only around lower values, similar to sparse coding

(Olshausen and Field, 1996; Olshausen and Field, 1997), and observed that neural responses to

unfamiliar inputs only exhibited higher values.

Spatio-temporally efficient coding predicted a bias in preferred orientations (Fig 6). In this regard,

spatially efficient coding alone has been reported to predict bias in preferred orientations (Ganguli and

Simoncelli, 2014). Notably, spatio-temporally efficient coding was able to predict this bias well, even

when λ was low, that is, when the spatially efficient coding objective was less weighted (Fig 6B).

Therefore, this bias prediction should be viewed as a result of spatio-temporally efficient coding, not

as a result of spatially efficient coding alone.

The present study has several limitations. First, for simplicity, our simulation model contained only two

hierarchies. However, it is necessary to explore how spatio-temporally efficient coding operates in

models with more hierarchies. We also modelled 64 neuronal units at each hierarchy, as we assumed

that this would be sufficient to represent the natural scene images used in this study. Nevertheless,

the interactions between the number of neuronal units, levels of hierarchy, and spatio-temporally

efficient coding require further investigation. Second, we demonstrated that the visual hierarchical

structure could learn to represent static natural scene images with spatio-temporally efficient coding,

but future follow-up studies will investigate whether the visual hierarchical structure learns to

represent moving scenes using the same coding principle. Finally, the scope of the present study was

limited to the visual system given that its hierarchical structure is well documented, but spatio-

temporally efficient coding may be applied to other systems (e.g., somatosensory system) or to

movements and planning.

3.1. Conclusions

In the present study, we proposed spatio-temporally efficient coding, inspired by the efficient use of

given resources in neural systems, as a neural coding mechanism to assign representational

functions to the hierarchical structures of the visual system. Simulations demonstrated that the visual

hierarchical structure could represent the external world (i.e., natural scenes) appropriately using

bidirectional predictions (Fig 3). Furthermore, spatio-temporally efficient coding predicted the well-

known properties of visual cortical neurons, including deviations in neural responses to unfamiliar

images (Fig 4 and 5) and bias in preferred orientations (Fig 6). Our proposed spatio-temporally

efficient coding may facilitate deeper mechanistic understanding of the computational processes of

hierarchical brain structures.

4. Methods

4.1. Datasets

For the simulations, van Hateren's natural scene image dataset (van Hateren and van der Schaaf,

1998) was used. The dataset was downloaded from http://bethgelab.org/datasets/vanhateren/. The

images were downsized to 64×96 pixels. For the comparison tests, the MNIST handwritten digit

dataset   (Lecun   et   al.,   1998)   was   used.   The   dataset   was   downloaded   from

http://yann.lecun.com/exdb/mnist/. The images were resized to 64×96 pixels to fit the images used

in the simulations. All image data were rescaled between 0 and 1.

4.2. Detailed descriptions of spatio-temporally efficient coding

For convenience, $X_{h=0}$ denotes X_{image}. The details of the visual information processing f_t are as

follows: If $h > 0$, then

$$f_t|_{X_{h,t}} = \sigma\big(W_{h+1,h}^T X_{h+1,t-1} + W_{h-1,h}^T X_{h-1,t-1} + b_h\big) \qquad (5)$$

where $X_{h,t}$ is an X_h value vector at time t, $f_t(\cdot)|_{X_{h,t}}$ indicates restricting the range of the function

value $f_t(\cdot)$ to $X_{h,t}$, $W_{h+1,h}$ is a synaptic weight matrix from hierarchy $h+1$ to h, T is the transpose

of a matrix, b_h is a bias vector at hierarchy h, and $\sigma(\cdot)$ is a sigmoid function. In the case of

$h + 1 > H$, the $W_{h+1,h}^T X_{h+1,t-1}$ term should be omitted. If $h = 0$, then

$$f_t|_{X_{0,t}} = F\left(X_{h=1,t-1}\right) \tag{6}$$

where $F(\cdot)$ is a neural network with two hidden layers to enable detailed reconstruction of images.

The activation function of the last layer of $F(\cdot)$ is a sigmoid function, as in the case of $h > 0$, in the

hidden layer, it is a rectified linear unit.

To minimise the objective of spatially efficient coding, it is necessary to calculate the probability

$P\left(f_t|_{X_h}\right)$. Instead of calculating the exact probabilities, we obtained pre-normalised densities in the

sense of probabilities without a partition function. As the value of the partition function is fixed, it does

not affect the minimisation process. Kernel density estimation was used to obtain $P\left(f_t|_{X_h}\right)$. Using a

Gaussian kernel with width $0.1(\dim X_h)^{1/2}$, the neural response density $Q\left(f_t|_{X_h}\right)$ and compensation

density $Q'\left(f_t|_{X_h}\right)$ at $f_t|_{X_h} \in X_h$ were obtained. Then, the pre-normalised density of interest is

$$P\left(f_t|_{X_h}\right) = \frac{Q\left(f_t|_{X_h}\right)}{Q'\left(f_t|_{X_h}\right)}. \tag{7}$$

The compensation density $Q'\left(f_t|_{X_h}\right)$ is obtained using pseudo-uniformly generated samples on

$X_h = [0,1]^{\dim X_h}$ instead of the neural responses. The compensation density is necessary to

compensate for the non-uniform intrinsic expectation of $Q(\cdot)$ resulting from the fact that X_h is

bounded.

In the present study, the depth of the hierarchies was 2, and images with 64×96 size were divided

into four overlapping 38×58 patches. Each patch was connected to 16 of 64 hierarchy 1 units.

Further, 64 hierarchy 1 units were fully connected to 64 hierarchy 2 units (Fig 1A). Four neural

networks $F(\cdot)$ were connected from hierarchy 1 units to four image patches. Each neural network

$F(\cdot)$ had two hidden layers with 128 and 1024 units, respectively.

Because $L = L_{Temporal} + \lambda L_{Spatial}$ is differentiable, the minimisation of the objective in spatio-

temporally efficient coding was performed with a gradient descent. The Adam optimiser (Kingma and

Ba, 2015) was used to perform the stochastic gradient descent with momentum. The parameters of

the Adam optimiser used in this study were $\alpha = 0.001$, $\beta_1 = 0.9$, $\beta_2 = 0.999$, and $\epsilon = 10^{-8}$. The

optimisation lasted 10^4 iterations for each repetition and restarted with five repetitions. For each

iteration, the duration of temporal processing f_t was five (i.e., $t \in [1,5]$), and the minibatch size was

40.

Simulation   codes   for   spatio-temporally   efficient   coding   are   available   from

[https://github.com/DuhoSihn/Spatio-temporally-efficient-coding] (Sihn, 2021).

Data availability statement

All simulation and analysis codes are available at: https://github.com/DuhoSihn/Spatio-temporally-

efficient-coding and on Zenodo (doi: 10.5281/zenodo.5298182)

CRediT authorship contribution statement

Duho Sihn: Conceptualization, Methodology, Software, Validation, Formal analysis, Investigation,

Resources, Data Curation, Writing - Original Draft, Writing - Review & Editing, Visualization,

Supervision, Project administration. **Sung-Phil Kim**: Writing - Original Draft, Writing - Review & Editing,

Visualization, Supervision, Project administration, Funding acquisition.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships

that could have influenced the work reported in this paper.

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Orientation: 0 (rad)

Orientation: $\pi/2$ (rad)

$\lambda = 10$

$\lambda = 30$

$\lambda = 100$