

30 **Abstract**

31 Our conceptual understanding of immune-mediated interactions between parasites is
32 rooted in the theory of community ecology. One of the limitations of this approach is that
33 most of the theory and empirical evidence has focused on resource or immune-mediated
34 parasite competition and yet, there is ample evidence of positive interactions between
35 species that could be generated by immune-mediated facilitation. Here, we develop an
36 immuno-epidemiological framework and apply it to longitudinal infection data of two
37 gastrointestinal helminths that infect a population of free-living rabbits to investigate,
38 through model testing, the mechanisms of immune-mediated facilitation in dual
39 infections. Simulations show that weakened, species-specific IgA antibody responses
40 and unequal, albeit low, IgA cross-reactions explain higher parasite intensities in dual
41 compared to single infections, for both helminths. Simulations also show that rabbits with
42 dual infections shed more free-living stages that survive for longer in the environment,
43 implying greater onward transmission than hosts with single infections. These findings
44 support the hypothesis that the two helminths interact through immune-mediated
45 facilitation which contributes to greater fitness and the long-term co-circulation of both
46 species in the host population.

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48

49 **Keywords:** Intensity of infection, shedding, antibodies, cross-reaction, climate

50 **Introduction**

51 Interference between parasite species, mediated via the host's immune response, is one
52 of the processes frequently proposed to explain interactions between different parasite
53 species, or genetically diverse strains, that co-infect the same host [1-6]. In these
54 instances, immunity is expected to preferentially target the more abundant or virulent
55 parasite and, by reducing its intensity, attenuate the competition on the less abundant
56 species. The two species can still co-exist, but their relative fitness depends on the net
57 outcome of these interactions.

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59 An alternative scenario to competition is where immune-mediated interactions lead to
60 facilitation of either one or both of the co-infecting species [7] (figure 1). For example,
61 many parasites can suppress or divert the immune response in favour of their own
62 survival [8], and this action can benefit a second parasite species through a bystander
63 effect [9,10]. Similarly, because of the polarization and function of different branches of
64 the immune system, the response developed against one species can reduce or prevent
65 the reaction against a co-infecting species [11-14]. In these interactions, the net benefit
66 obtained from co-infection is asymmetrical (figure 1c). The facilitator parasite can control
67 the immune response, or become its target, and in so doing facilitates the second
68 parasite species that profits more than the facilitator, and consequently has greater
69 fitness than when it is the sole parasite in the host. Symmetrical immune-mediated
70 facilitation emerges when both parasite species benefit from their co-infections (figure
71 1b). This can occur through the reduction, suppression or evasion of the immune
72 response against each species, which gains both through greater vital rates and
73 abundance [15-17]. Immune tolerance could be considered an extreme example of
74 facilitation since the host immunity is engaged in repairing the injuries caused by the
75 parasites rather than controlling the infections [18]. Importantly, under these scenarios a

76 parasite will have a selective advantage when it infects hosts already parasitized with
77 the other species, so long as the facilitation is not so strong as to destabilize the
78 interactions [19] or reduce host survival [20,21].

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80 From an ecological perspective, the extent of immune-mediated parasite interaction is
81 the outcome of two fundamental components. First, the immune response against one
82 parasite species that is diverted to fight other parasites, e.g. the loss of specific
83 antibodies that cross-react with other infections, and second, the immune constraints
84 this parasite species experiences by the presence of other species, e.g. the effect of
85 cross-reacting antibodies from other infections (figure 1*b,c*). Therefore, a positive net
86 impact for each species, including any parasite manipulation of the immune reactions,
87 would be expected to facilitate co-infections both within the host and among the co-
88 circulating parasites at the host population level. Theory has shown that in the absence
89 of strong competition between two parasite species, a weak immune-mediated
90 symmetrical facilitation increases the virulence/abundance of both parasites, however,
91 under stronger facilitation parasite growth escapes regulation and the system becomes
92 destabilized [19].

93

94 To test for immune-mediated interactions leading to facilitation, we applied an immuno-
95 epidemiological model to 23 years of infection data and asked whether the interaction
96 between two helminths in dual infected hosts could be explained by immune facilitation,
97 and whether there were positive consequences for parasite fitness, or onwards
98 transmission, at the host population level. We used two helminth species,
99 *Trichostrongylus retortaeformis* and *Graphidium strigosum*, that inhabit different
100 gastrointestinal niches of the European rabbit (*Oryctolagus cuniculus*), the small
101 intestine and stomach respectively, implying that they were unlikely to exhibit direct

102 competition. While both helminths cause chronic infections, *T. retortaeformis*, and less
103 so *G. strigosum*, shows evidence of regulation of abundance and fecundity through host
104 immunity [22-27]. Interestingly, field studies found higher intensities of the first and to a
105 lesser extent the second in rabbits with both helminths, when compared to hosts with
106 single infections [28,29], suggesting a possible positive interaction between the two
107 species.

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109 We investigated two hypotheses within the processes of immune regulation. If
110 symmetrical facilitation is important, we should expect both helminth species from dual
111 infections to experience reduced immune constraints and higher abundance and/or
112 production of free-living stages, than parasites from single infections (figure 1b).
113 However, if asymmetrical facilitation drives the interaction between the two species, then
114 the dynamics for the facilitated parasite should be enhanced but the facilitator should not
115 show substantial changes, when compared to single infections (figure 1c). In the
116 opposite scenario of reduced dynamics, such as decreased intensity of infection and/or
117 parasite fitness for one of both species, this should support immune-mediated
118 interference.

119

120 We tested different candidate frameworks, and model selection was based on the ability
121 of each model to describe the observed dynamics of infection, while identifying a
122 parsimonious mechanism of host-parasite and parasite-parasite interactions. Since we
123 are interested in processes of facilitation through host immunity, rather than competition,
124 and given that the two helminths inhabit different gastrointestinal niches, parasite
125 interference for host resources, including manipulation of host's metabolism or the
126 interaction with the gut microbiome, were beyond the scope of this study.

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Material and Methods

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The System

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Rabbits become chronically infected with the two helminths by eating herbage

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contaminated with infective larvae; once in the host, larvae develop into adults that shed

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eggs with the hosts' faeces (figure S1). Laboratory experiments showed that rabbits

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develop a type 2 anti-inflammatory response against both species. However, while this

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regulates both *T. retortaeformis* intensity and body growth, which then affects fecundity,

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it appears to have a weaker effect against *G. strigosum* that maintains high intensities

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throughout the infection [24-27]. A broader investigation of the immune profile in

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experiments of infection and anthelmintic treatment found a down-regulation of genes

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expressing type 1, type 2 and T-regulatory responses during reinfections with *G.*

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strigosum and much less so with *T. retortaeformis*, both in single and dual infections

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[23]. There was no evidence that *G. strigosum* contributed to this reduction, suggesting

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that the host rather than the parasite was probably responsible for the observed immune

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down-regulation [23]. The general conclusions that *T. retortaeformis*, and to a lesser

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extent *G. strigosum*, is affected by host immunity were also proposed in field studies

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[22,28-31].

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The dynamics of the two helminths could also be negatively affected by ecological

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processes of intra-specific competition for resources. Previous studies indicated that this

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is probably not the main mechanism of regulation for *T. retortaeformis* but could play a

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role for *G. strigosum*, especially at high abundances [26,31]. For example, rabbits

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nutritionally constrained, through coprophagic restriction and on a fixed diet, carried the

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same *T. retortaeformis* intensities as animals on a fixed diet only [32].

152

153 An important component of soil-transmitted helminths is the development and survival of
154 eggs and larvae in the environment. Temperature and rainfall affect the survival of both
155 *T. retortaeformis* and *G. strigosum* free-living stages [33-35] while at the host population
156 level, climate and seasonality were found to be important for subsequent infection and
157 thus parasite fitness [31].

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159

Model Datasets

160 Here, we present the datasets and assumptions used for our mechanistic immuno-
161 epidemiological model, while in the next section we describe the model framework. The
162 study focused on a population of rabbits (population A) sampled monthly between 1980
163 and 2002 from our site in Scotland. For every rabbit collected, the abundance of *T.*
164 *retortaeformis* and *G. strigosum* was quantified by aliquots using standardized
165 parasitological techniques [36]. We classified rabbits with one helminth species as
166 single-infected and with both species as dual-infected. It is possible that some of the
167 adults with single infections may have been previously infected with the other species
168 that was subsequently eliminated. Rabbits do not appear to be able to clear *G.*
169 *strigosum* [23-25,28,37] but old hosts can remove *T. retortaeformis* [24,27], although in
170 endemic settings reinfection is relatively fast and the fraction of single infected hosts is
171 really quite low; nevertheless, dubious cases were removed. To avoid interference with
172 myxoma virus infection [11,28] rabbits with myxomatosis symptoms were excluded. Host
173 age was arranged into eight classes, from age class 1 (one-month old) to age class 8
174 (8+ months old) [22,28] and lifespan was considered to be about one year [38].

175

176 Population A provides 23 years of robust individual host data on the two helminths but
177 lacks information on host immunity. Since our aim is to integrate the immune response
178 of the rabbit with the dynamics of its parasites, we used data on serum antibody IgA and

179 IgG data obtained from a second rabbit population (population B) located ~5 kilometres
180 away in a similar ecosystem and sampled for a much shorter time period (2004-2011),
181 following the same standardized procedures as in population A [29]. Antibody data were
182 available for six out of those eight years. Given its shorter time series of infection and
183 following a preliminary investigation (SI-1.3 and 1.4), antibodies from population B were
184 used to inform the parameterization of the immune response for the longer sampling of
185 population A. This was based on similar dynamics of the two helminths (compare figure
186 S2 with figure 2 and statistical results in SI-1.3 and 3.3) and the rabbits' age structure
187 (SI-1.4) at the two populations.

188

189 We selected species-specific IgA antibodies to represent host immunity against each of
190 the two helminths. Naturally, this is an over-simplification of the immune response, and it
191 was determined by the following reasons. First, IgA is the most abundant
192 immunoglobulin at mucosal surfaces, including the lamina propria of the gastrointestinal
193 tract where it plays a critical role in the humoral response against gut infections [39].
194 Second, IgA is an important contributor to the regulation of helminth abundance and vital
195 rates [40-45], where the degree of protection is strongly affected by the host-helminth
196 system and its history of infection [46-48]. In this system, we found that IgA (but not IgG)
197 follows the dynamics of the two helminths, suggesting a rapid response and a
198 reasonable representation of the immune response that does exhibit some regulatory
199 properties but no long-term protection [23-27]. Third and most important, we needed a
200 variable with an antigenic-specific immune response that could allow the quantification of
201 separate reactions, namely species-specific and cross-reacting signals and, as such,
202 would capture the essence of symmetric/asymmetric interactions, while avoiding
203 additional complexities of adding extra variables and unnecessary assumptions. Our
204 selection was also for a variable that could be easily quantified from large field datasets.

205 Moreover, antibodies are tractable model tools since we can select among different
206 isotypes based on the parasite-specific relationship of interest.
207
208 Species-specific serum IgA was originally quantified using excretory/secretory products
209 of adult parasites, as a source of antigen, and the enzyme-linked immunosorbent assay
210 (ELISA) [29]. Tests of *in vitro* antibody performance and competitive abilities between
211 the two helminths indicated good selective abilities to discriminate between the two
212 helminths when they co-occur [29]. Despite these *in vitro* analyses, we did not exclude
213 the possibility of antibody cross-reactivity, especially at high intensities of infection.
214 Finally, weather variables on mean air temperature and relative humidity were collected
215 daily from the nearby Hutton Institute (UK).

216

217

Model Framework

218 We used a deterministic, age-structured, immuno-epidemiological model with climatic
219 forcing, previously selected among different candidate models for this rabbit-helminth
220 system [30,31]. The model was then expanded to analyse hosts with single and dual
221 infections and to explicitly include the contribution of species-specific and cross-reacting
222 IgA responses. The demography of the host population was also included. We assumed
223 that the within-host helminth dynamic can be captured as:

224

$$225 \quad \frac{\partial P_i(a, t)}{\partial t} + \frac{\partial P_i(a, t)}{\partial a} = \Phi(a)F_i(t) \exp \left[- \left(r_{ii}I_i(a) + r_{ij}I_j(a) \right) \right] (1 - P_i(a, t)/\delta_i)^+ - (\mu_i + \mu_H)P_i(a, t),$$

$$226 \quad \text{with } (1 - P_i(a, t)/\delta_i)^+ = \begin{cases} (1 - P_i(a, t)/\delta_i) & \text{if } (1 - P_i(a, t)/\delta_i) > 0 \\ 0 & \text{otherwise} \end{cases} \quad (\text{Eq. 1})$$

227

228 where: the intensity of infection (IOI) of the focal helminth P_i ($i = T$ for *T. retortaeformis* or
229 $i = G$ for *G. strigosum*), changes with host age, a in days, and time, t . The intensity of the

230 helminth-specific IgA response, I_i , changes with host age, a ; $\Phi(a) = \Phi_0 \left(\frac{200+9a}{3340} \right)^\gamma$ is an
231 allometric function describing the age-dependent host feeding rate, with Φ_0 and γ being
232 suitable constants for each helminth species [30]. Given the similar IgA responses to
233 infective third stage larvae (L3) and adults [24,25], and to avoid model redundancy, we
234 focused on adults, assuming that there is no time delay from the ingestion of L3 to
235 parasite maturation. The r parameters account for the effect of the immune response on
236 the parasite intensity of infection, specifically, $r_{ii}(a)$ is the age-dependent and species-
237 specific IgA response that is stimulated by, and targets, parasite i , while $r_{ji}(a)$ represents
238 the age-dependent and species-specific IgA stimulated by parasite j ($j \neq i$) that targets
239 parasite i in dual-infected rabbits. r_{ii} and r_{ji} regulate the intensity of the stimulus triggered
240 by the parasite; setting $r_{ji}=0$ ($j \neq i$) accounts for single infections. IgA is modelled to impact
241 within-host parasite establishment and survival. Since the two helminths colonize
242 different niches we did not consider direct inter-specific competition although we
243 included the non-negative term $(1 - P_i(a, t)/\delta_i)^+$, which quantifies the intra-specific
244 intensity-dependent effect on helminth establishment, with δ_i representing the carrying
245 capacity of helminth species i . μ_i is the species-specific natural mortality rate of
246 established parasites while μ_H is the host natural mortality rate ($\mu_H = 0.0069 \text{ days}^{-1}$) [38];
247 the total mortality rate of parasites μ includes both μ_i and μ_H .
248
249 $F_i(t)$ is the risk of infection (RI) of the host by parasite i and quantifies the density of free-
250 living helminths available for infection on the herbage at time t . $F_i(t)$ is driven by the
251 intensity of infection in the host, P_i , and the linear effects of air temperature, $\tau(t)$, and
252 relative humidity, $H(t)$, on the mortality of free-living stages, $\mu_{Fi}(\tau(t), H(t))$ [31] as:
253

$$254 \quad \frac{dF_i}{dt} = \alpha'_{pi} \int_{a_{min}}^{a_{max}} e^{-\mu_H a} f(t-a) P_i(a, t) da - \mu_{Fi}(\tau(t), H(t)) F_i \quad (\text{Eq. 2})$$

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256 with $\alpha'_{pi} = \alpha_{pi} s_i R$. The quantity α'_{pi} describes the rate at which eggs are shed by an
257 infected host and includes the total annual recruitment of rabbits, R , into the host
258 population, the total number of eggs shed by an adult parasite per unit of time, s_i ,
259 independent of host age, and the survival of free-living stages, α_{pi} . In the model, eggs
260 hatch directly into infective stages to help reduce model complexity while retaining the
261 fundamental biological characteristics of the system and the emphasis on the within-host
262 processes, and yet permitting an estimate of parasite fitness. The relative impact of
263 weather on the loss of free-living stages is set as: $\mu_{Fi}(\tau(t), H(t)) =$
264 $\alpha_{0i} - \alpha_{1\tau i} \tau(t) - \alpha_{1hi} H(t)$, where α_{0i} represents the baseline natural parasite mortality rate,
265 while $\alpha_{1\tau i}$ and α_{1hi} depict changes in the mortality rates driven by temperature and
266 humidity, respectively [31]. The proportional change of $F_i(t)$ with the host intensity of
267 infection is described by the term $\int_{a_{min}}^{a_{max}} e^{-\mu_H a} f(t-a) P_i(a, t) da$, where $a_{max} = 283$ days
268 is the maximum age of an individual recorded in the data and $a_{min} = 30$ days, which is
269 approximately the age when naïve rabbits switch from milk to herbage and are exposed
270 to infective stages. The first age class of naïve rabbits is initiated by assigning a null
271 intensity of both infection and IgA. $F_i(t)$ explicitly depends on the age structure of the
272 host population and thus, accounts for host reproduction, $f(t)$, the relative number of
273 births at time t , and host survival, $e^{-\mu_H a}$, which represents the probability that rabbits are
274 still alive at age a . We modelled $f(t)$ as a beta probability density function calibrated
275 against the fraction of 2-months old rabbits (SI-2.1). We assumed that infections with the
276 two helminths occur through simultaneous ingestion, which is commonly expected in
277 natural conditions; eggs are also shed simultaneously [29]. Table 1 summarizes the
278 model variables and parameters.

279

280 As the framework (Eqs. 1 and 2) is rather complex, and to identify the model that
281 represents the best compromise between complexity and data availability, we focused
282 on population A dataset to quantify the functional relationships and fundamental
283 mechanisms of helminth dynamics, and used population B for the details on the host
284 immune response. The first nontrivial problem we faced was fitting the model to data
285 from population A with all the observed combinations of helminth abundances in dual-
286 infected rabbits, including changes in the proportion of hosts with single and dual
287 infections over time. To reduce this computational difficulty, the rabbit population was
288 grouped in four subsets of infection data and the model was independently fitted to
289 individual rabbits from each of these subsets: i)- rabbits with *T. retortaeformis* and free of
290 *G. strigosum*, ii)- rabbits with *G. strigosum* and free of *T. retortaeformis*; iii)- rabbits with
291 both parasites but fitting to *T. retortaeformis* data only and iv)- rabbits with both parasites
292 but fitting to *G. strigosum* data only. Animals free of both helminths at the time of
293 sampling, i.e. not currently infected, were included in every subset to provide the naïve
294 condition, once dubious cases were identified and removed.

295

296 A similar approach was used for assigning the IgA values to rabbits from population A.
297 The IgA data from population B were initially grouped into the four subsets and, for each
298 one, the continuous age-related immune values $I_i(a)$ and $I_j(a)$ were obtained by
299 interpolating a 4th order polynomial function to the relationship between mean IgA and
300 host age, weighted by sample size (figure S2a and b). Different smoothing functions
301 were examined and the 4th order polynomial fitted well our data. Rabbits from population
302 A were then assigned an interpolated IgA value according to their type of infection and
303 age.

304

305 The second non-trivial problem was related to model selection [49] and the possible
306 overfitting when using a model with many free parameters. We tested five hypothesis-
307 driven models (three for single infections) that represented different mechanisms of
308 parasite regulation: i)- no constraints and parasites are affected by birth-death
309 processes, ii)- immune-mediated constraints through IgA responses, iii)- intra-specific
310 intensity-dependent constraints for host's resources and, for the dual-infected hosts, we
311 also examined iv)- cross-immunity via IgA responses (table 2). The complexity of the
312 framework was explored by considering models that included these mechanisms in
313 different combinations. Model selection and parameter calibration were performed
314 independently for each of the four subsets using individual data from population A.

315

316 To increase model adherence to observed data the shape parameter γ , pertaining the
317 rabbit's feeding rate, $\Phi(a)$, was initially tuned by fitting the most complex model (M2 for
318 single and M4 for dual infections) to the annual mean intensities of infection by host age,
319 simultaneously in single and dual infections of each helminth species. We then used this
320 value for all the models, including the less complex ones. During model fitting, γ was
321 kept fixed while all the other parameters were recalibrated to the individual data of each
322 of the four subsets. The best-performing model formulation was selected using the
323 Akaike Information Criterion [49] and the lowest AIC. To allow the system to reach
324 regime conditions during calibration, the model was simulated for an initial warm-up of
325 23-years that was then removed, full details of this procedure are reported elsewhere
326 [31].

327

328 The numerical integration of the model was achieved using MATLAB® *ode45* solver
329 function based on an explicit Runge-Kutta solution with adaptive time step size [50]. For
330 each of the four subsets of data, we compared the empirical helminth intensity in every

331 rabbit to the expected intensity of infection by time and age of every host provided by the
332 model output, assuming that the intensity of infection is distributed as a negative
333 binomial [28] with age- and time-dependent mean $P(a,t)$ and aggregation parameter k ,
334 calibrated together with the model parameters [28]. The parameters combination that
335 maximized the likelihood function was selected using a non-linear solver based on the
336 Nelder-Mead simplex algorithm [51].

337

338 Finally, to provide a statistical measurement of the differences between single and dual
339 infected rabbits, the model simulated quantities of interest, namely, intensity of infection,
340 abundance of eggs shed, risk of infection (i.e. viable free-living stages) and antibody
341 response, were compared using Generalized Linear Models (GLM, with normal or
342 negative binomial distribution of errors). Type of infection (single or dual) was entered as
343 categorical variable, while host age was included as a continuous variable. The additive
344 effects and two-way interactions of the explanatory variables were examined. For
345 consistency, the same analysis was repeated using the empirical data (SI-1.2).

346

347

Results

348 Here we present simulations from the best selected model and parameter calibration on
349 population A, the focus of our study. All the statistical results are reported in SI-3.

350

351

Epidemiology of Single and Dual infections

352 The model that best described the four subsets of infection data comprised the species-
353 specific IgA response and the intra-specific intensity-dependence for single infections,
354 dual infections also included IgA cross-reaction between the two helminths (table 2, SI-
355 3.1). Individual-based simulations captured the average trends of infection by host age
356 (figure 2), but less so the large intra-annual variation observed in the empirical data

357 (figure S6). For both helminths the simulated intensities by host age were significantly
358 higher in rabbits with dual than single infections (table S3). *T. retortaeformis* rapidly
359 accumulated with host age and maintains high intensities in older rabbits (figure 2a),
360 while accumulation of *G. strigosum* intensities was slower (figure 2b). Consistent with
361 these model results, the empirical intensities of infection by host age were significantly
362 higher in rabbits with dual than single infection, for both helminths (figure 2, table S3).

363

364 ***Immune response and Immune-mediated parasite facilitation***

365 The estimation of immunological parameters yields information on the immunological
366 mechanism that could generate the epidemiological patterns observed. Simulations
367 indicate that the stimulus to develop a specific IgA response to *T. retortaeformis* is
368 stronger in rabbits with single than dual infections ($r_{TT} = 0.734$ vs 0.338 , table 3). In this
369 latter group, the cross-reaction stimulus for a specific IgA response against *G. strigosum*
370 that also attacks *T. retortaeformis* is essentially null ($r_{GT} = 0.00016$). The projected
371 relationships between intensity of infection and IgA stimuli indicate that a proportional
372 increase in the specific IgA stimulus (r_{TT}) will reduce *T. retortaeformis* intensities, while
373 the stimulus for an IgA response to *G. strigosum* that cross-reacts with *T. retortaeformis*
374 (r_{GT}) remains extremely weak and will have no impact on this helminth (figure 3a). When
375 we consider the estimated species-specific antibody response against *T. retortaeformis*,
376 r_{TTI} , values are significantly lower in dual than single infection, and for rabbits of all age
377 groups (figure 4a, table S4). These results suggest that the higher *T. retortaeformis*
378 intensities in dual-infected hosts are caused by the weakening of the stimulus to a
379 specific IgA response that is diverted against *G. strigosum* (also see below) and a
380 negligible immune-mediated interference by this latter helminth in the form of a weak
381 cross-reaction, r_{GTI} . We note that, while empirical data only quantify specific IgA's, the
382 model allows us to quantify both the species-specific (r_{iIi}) and the cross-reactive (r_{jIi})

383 relative strength of IgA, namely the effect of an increase (or decrease) of IgA on the
384 intensity of infection.

385

386 The intra-specific carrying capacity, δ , is higher in rabbits with dual than single infections
387 (789.74 vs 651.6, respectively, table 3) supporting the lower intensity-dependent control
388 in this latter group.

389

390 For *G. strigosum*, simulations showed that the stimulus to develop a specific IgA
391 response is low (table 3), and lower in rabbits with single ($r_{GG}= 0.121$) than dual infection
392 ($r_{GG}= 0.208$). The stimulus for an IgA response specific to *T. retortaeformis* that cross-
393 reacts against *G. strigosum* is four times higher ($r_{TG}= 0.804$), implying interference from
394 this helminth. Moreover, the investigation of how *G. strigosum* intensities will change in
395 relation to changes in the antibody stimuli indicates that the simulated intensities will
396 decline with a proportional increase of r_{TG} and less so of r_{GG} (figure 3b). Examination of
397 the estimated antibody response, $r_{GG}I$, by host age showed that values are significantly
398 higher in rabbits with dual than single infections (figure 4b, table S4), although it is
399 important to observe that these values remain consistently low. All together, these
400 findings suggest that dual-infected rabbits should control *G. strigosum* more successfully
401 than single-infected hosts. However, the generally low IgA response, even for the cross-
402 reaction, could explain the significantly higher intensities observed in dual-infected hosts
403 (table S3).

404

405 Previous studies proposed that intensity-dependence could be more important for the
406 dynamics of this parasite [31]. Our simulations indicate that parasite carrying capacity is
407 slightly higher in hosts with dual than single infections ($\delta= 83.45$ and 78.71, respectively,

408 table 3), suggesting the tendency for weaker restrictions of *G. strigosum* intensities in
409 this latter group, as previously noted for *T. retortaeformis*.

410

411 Collectively, the weakening or fundamentally low IgA responses, and the resulting higher
412 intensities of both helminths in dual infections, support the hypothesis of immune-
413 mediated facilitation between the two species. These higher intensities are generated
414 despite a clear uneven in the immune response against the two helminths.

415

416 ***Parasite fitness and Risk of infection***

417 Given the soil-transmitted nature of *T. retortaeformis* and *G. strigosum*, the density of
418 viable free-living stages on the pasture represents the risk of infection for hosts exposed
419 to these stages, and can be considered a proxy for onward transmission and parasite
420 fitness. The density of free-living stages is the sum of the abundance of eggs shed by
421 every host and their mortality rate. We used simulation results to examine whether
422 parasite immune-mediated facilitation has symmetrical or asymmetrical consequences
423 for parasite fitness. The estimated abundance of eggs shed on the pasture is
424 significantly higher in rabbits with dual than single infections, for both helminths (table
425 S5). Eggs shedding peaks in young and a decrease in older animals for *T. retortaeformis*
426 while there is a constant increase with host age for *G. strigosum* (figure S7a,b).

427

428 On the herbage, the population of free-living stages is affected by environmental factors
429 (biotic and abiotic) with higher mortalities for *T. retortaeformis* than *G. strigosum* (table
430 3). Throughout the study period, the mortality rate of free-living stages produced by
431 rabbits with single and dual infections is, respectively: $\mu_{FT} = 3.52$ and 1.58 day^{-1} for *T.*
432 *retortaeformis* and $\mu_{FG} = 0.009$ and 0.003 days^{-1} for *G. strigosum*. Part of this loss is

433 driven by weather: temperature has a strong impact on *T. retortaeformis* ($\alpha_{1\tau} = 0.445$
434 and 0.207 for single and dual infections, respectively) while humidity is more relevant to
435 *G. strigosum* ($\alpha_{1H} = 0.004$ and 0.002). The ecological differences between the two
436 helminths are also clear from the baseline natural mortality rate of free-living stages, α_0 ,
437 which is a component of μ_{Fi} . Mortality is higher for *T. retortaeformis* ($\alpha_0 = 7.39$ and 3.60
438 for single and dual infections, respectively) than for *G. strigosum* ($\alpha_0 = 0.328$ and 0.194),
439 indicating that larvae are on the pasture for a shorter period of time for the former
440 helminth. More important, simulations suggest that under analogous environmental
441 conditions, free-living stages from both helminths experience lower natural and climate-
442 driven mortality, and thus remain available for onward transmission for longer, when
443 derived from rabbits with dual infections (compare α_0 and μ_{Fi} from single and dual
444 infections).

445

446 There is strong seasonality in the accumulation of free-living stages on the herbage, and
447 hence the risk of infection (figure 5). *T. retortaeformis* accumulation is at the highest in
448 August primarily through the shedding of young and newly infected rabbits and drops in
449 June, coinciding with the peak of newly born rabbits (figure S3). *G. strigosum* shows the
450 highest densities around March, when the population is composed predominantly of
451 adults and the lowest around July, especially for dual infected hosts, with the arrival of
452 newborn hosts. In both cases, rabbits dual-infected generate significantly more viable
453 free-living stages throughout the year, than single-infected rabbits (table S6). Therefore,
454 while differences between the two helminths are expected because of their ecological
455 characteristics, both *T. retortaeformis* and *G. strigosum* from dual-infected rabbits exhibit
456 significantly higher fitness, including higher intensities of infection, than helminths from

457 single infections, supporting the hypothesis of symmetrical immune-mediated facilitation
458 between the two parasites.

459

460

Discussion

461 We applied an immuno-epidemiological model to empirical data of two helminths from a
462 population of rabbits and the findings support the hypothesis that immune-mediated
463 facilitation can explain *T. retortaeformis* and *G. strigosum* higher intensities in rabbits
464 with dual compared to single infections. Dual infections are facilitated by weakened
465 species-specific IgA responses and unequal IgA cross reactions. Our multi-scale
466 approach also suggests a symmetrical immune-mediated facilitation where weak IgA
467 stimuli contribute to greater number of eggs shed and higher survival of the free-living
468 stages, and thus higher transmission, when compared to parasites derived from hosts
469 with single infections. Given that rabbits with dual infections represent the large majority
470 of the sampled population (figure S4), the dynamics of the two helminths is primarily
471 driven by this group of hosts.

472

473 Cross-immunity, where protection to one species provides some defence against a
474 second species, has been proposed in a variety of systems [e.g. 1-3,6,52]. Our study
475 offers novel insights by showing that, although some immune-mediated interference
476 between two helminths is likely to occur, IgA cross-reacts disproportionately and has
477 small impact on parasite intensity, it is essentially null against *T. retortaeformis* and has
478 a low effect against *G. strigosum*. This pattern is consistent with theoretical work
479 showing that two parasites will increase abundance and persist in the host if immune-
480 mediated facilitation is not too strong to destabilize the system [19]. The evidence in
481 animal systems of positive interactions between parasite species [1,2,53], suggests

482 some level of immune-mediated facilitation, irrespective of the specific immune
483 mechanism involved. Examples of facilitation through host immunity have been
484 frequently described for HIV associated co-infections in humans, such as HIV-malaria or
485 HIV-Tb [58,59]. Positive interactions between micro- and macro-parasites, mediated by
486 trade-offs in the immune functions and responses, are expected to benefit one or both
487 parasites [11,13]. For helminth co-infections, synergistic effects could emerge
488 throughout diverse processes; for example, the allocation of IgE against helminth
489 species could help explain the positive correlation between *Ascaris lumbricoides* and
490 both *Trichuris trichiura* and hookworm infections in humans (15, 54-56). Similarly, the co-
491 circulation of *Trichostrongylus* spp., *Haemonchus contortus* and *Teladorsagia*
492 *circumcincta* in domestic and wild animal populations is facilitated by their immuno-
493 modulatory properties [57] and could be complemented by asymmetric immune
494 reactions.

495

496 We can expect that one of the consequences of immune-mediated facilitation will be
497 greater parasite fitness. We found that rabbits with dual-infections contribute to a larger
498 number of free-living stages that are available for onward transmission, than did rabbits
499 with single infection. Our model did not explicitly quantify the relationships between IgA
500 and parasite size or fecundity, where both fecundity and shedding are directly related to
501 parasite body length [23,29], but coupled shedding to infection intensity, which is then
502 modulated by IgA. Some of these relationships were previously examined and showed a
503 negative relationship between IgA and *G. strigosum* body length in single infections and
504 between IgA and *T. retortaeformis* body length or abundance in co-infections [23]. A
505 combination of positive and negative relationships was also found between the vital
506 rates of both helminths and type 1, type 2 and T-regulatory immune variables [23],
507 confirming the complex interactions between parasite demography and the host immune

508 response. Indeed, the immune response to an infection is the results of a large number
509 of functions and factors, each of which has distinct roles and degree of specificity. Our
510 model framework describes a small constituent of this immune network, and gratifyingly
511 captured the effects, while other immune processes could also have potentially
512 contributed to the weaker net response of dual infected rabbits. More broadly, our results
513 are consistent with studies from other systems on the importance of IgA to helminth
514 growth, fecundity and shedding [60-63].

515

516 In addition to the diverse tolerance of the two helminths to weather [33-35], the higher
517 natural mortality of *T. retortaeformis* on the pasture is probably associated with the faster
518 life history of this parasite, namely, faster egg hatching rate [34] and faster within-host
519 maturation [64], when compared to *G. strigosum* [65]. Crucially, free-living stages
520 derived from rabbits with dual infections exhibited longer survival leading to higher
521 probability of onwards transmission. Laboratory studies showed that fewer antibodies
522 bind to eggs of *T. retortaeformis* than *G. strigosum*, and egg volume decreases for the
523 first and increases for the second during a single-dose infection experiment [66]. While
524 there was no clear evidence that antibodies altered egg size or hatchability, the impact
525 could be relevant in natural settings, when both the host and the helminths are under
526 environmental constraints. For instance, the low IgA specific response to *T.*
527 *retortaeformis* in hosts with dual-infections could lead to eggs of higher quality, such as
528 larger size or more tolerant to thermal changes, by females in better conditions. For *G.*
529 *strigosum* the mechanism is less clear but could also be related to improved female
530 conditions and enhanced egg quality with better tolerance to moisture variation.

531

532 Our data-informed modelling approach contributes to advances in the understanding of
533 immune-mediated facilitation on infection and transmission. The mechanistic

534 understanding of these processes, and the contribution to parasite dynamics and fitness,
535 is still limited and in great need of empirical evidence. There is also a need to improve
536 the realism of modelling multiple infections, particularly for macro-parasites. The
537 proposed framework can be adapted to test alternative and more complex immune-
538 mediated formulations beyond the species examined in this study. *T. retortaeformis* and
539 *G. strigosum* share similarities with other gastrointestinal helminths of animals, including
540 human parasites, and our findings have relevance across a broad range of ecological
541 settings. The fundamental challenge is to identify the key variables that can clarify the
542 mechanisms of regulation across scales and influences parasite fitness. Gathering this
543 information can be daunting but is a prerequisite for laying the foundation of a better
544 understanding of the ecological role of co-infection in disease spread and persistence,
545 which is essential for developing control measures tailored on these groups of hosts.

546

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551

552 **Ethic statement**

553 We used rabbit data already available from previous studies where sampling was performed
554 according to field procedures approved by the Institutional Animal Care and Use Committee of
555 The Pennsylvania State University (IACUC # 26383 and 34489). All animal work adhered to the
556 guidelines laid out in the Guide for the Care and Use of Laboratory Animals. 8th ed. National
557 Research Council of the National Academies. National Academies Press Washington DC.

558

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754 **Table 1.** Variable and parameter definitions, and their units for model equations 1 and 2.

755 The symbols a and t represent age and time in days.

756

Variable/ parameter	Definition	Unit
$P(a,t)$	Intensity of infection	parasites * rabbit ⁻¹
$F(t)$	Risk of infection	parasites * (grass unit) ⁻¹
$\Phi(a)$	Age-dependent host feeding rate	grass unit * (day * rabbit) ⁻¹
$l(a)$	Age-dependent host immune response	-
γ	Allometric exponent of the host feeding rate	-
Φ_0	Host feeding rate for reference body mass of 3340g	grass unit * (day * rabbit) ⁻¹
μ_i	Natural mortality rate of parasite i within the host	days ⁻¹
μ_H	Host natural mortality rate	days ⁻¹
δ	Parasite carrying-capacity	(parasites * rabbit ⁻¹) ⁻¹
μ_F	Weather-dependent mortality rate of free-living parasites	days ⁻¹
α_0	Parasite baseline mortality rate in the environment associated with worm features	days ⁻¹
$\alpha_{1\tau}$	Effect of temperature on mortality rate of free-living parasites	days ⁻¹ * °C ⁻¹
α_{1h}	Effect of humidity on mortality rate of free-living parasites	days ⁻¹ * units of relative humidity ⁻¹
$\tau(t)$	Mean daily air temperature from min and max records	°C
$H(t)$	Daily relative air humidity from dry-web bulb temperature, atmospheric pressure at 101.3kPa	%
α'_p	Parasite shedding rate * host total recruitment	rabbit * (grass unit * days) ⁻¹
r_{ii}	Intensity of immune response to parasite i triggered by i	-
r_{ji}	Intensity of immune response to parasite i triggered by j	-
k	Parasite aggregation from negative binomial distribution	-

757

758 **Table 2.** Tested hypotheses and related mechanisms for single and dual infections of both
 759 helminths with the corresponding model complexity p , indicated by the number of
 760 parameters to be calibrated for each data subset.
 761

Models	Single infection	Dual infection	Parameter constraints	p
M0	Parasite Birth-Death only	Parasite Birth-Death only	$r_{ji} = 0$ for any j and i ; $\delta_i = \infty$	8
M1	Birth-Death + Specific Imm.	Birth-Death + Specific Imm.	$r_{ji} = 0$ for $j \neq i$; $\delta_i = \infty$	9
M2	Birth-Death + Specific Imm. + Intensity Depend.	Birth-Death + Specific Imm. + Intensity Depend.	$r_{ji} = 0$ for $j \neq i$	10
M3	-	Birth-Death + Specific Imm. + Cross Imm.	$\delta_i = \infty$	10
M4	-	Birth-Death + Specific Imm. + Cross Imm. + Intensity Depend.	-	11

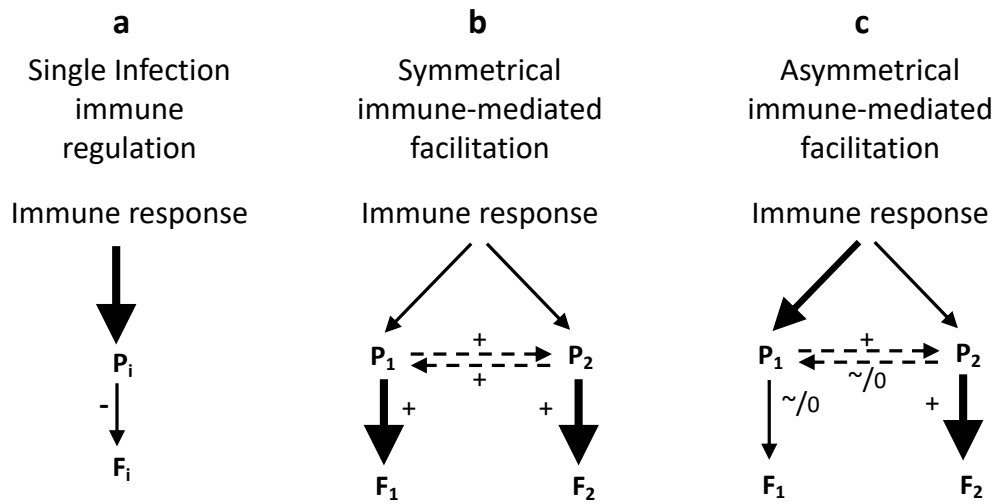
762

763 **Table 3.** Parameter values estimated from the best-fitted model for *T. retortaeformis* (TR)
764 and *G. strigosum* (GS) in single- (SI) and dual- (DU) infected hosts. Parameter definitions
765 are reported in table 1. $F(0)$ refers to the initial condition of the warm-up period of model
766 simulations while γ is included as a constant value. AIC= Akaike Information Criterion
767 value, LL= log-likelihood, RMSD= Root Mean Square Deviation.
768

Parameters	TR-SI	TR-DU	GS-SI	GS-DU
γ	3.09	3.09	5.73	5.73
Φ_0	1.70	0.4738	1.84	0.430
μ_i	0.0040	0.00219	0.212	0.0161
δ	651.6	789.74	78.71	83.45
$F(0)$	76.42	6.28	61.30	3.28
α_0	7.39	3.60	0.328	0.194
$\alpha_{1\tau}$	0.445	0.207	0.0022	0.00019
α_{1h}	-0.0003	0.00254	0.00375	0.00236
α_p'	1.86	3.322	0.129	0.1323
k	0.220	0.244	0.146	0.423
r_{ii}	0.734	0.338	0.1206	0.208
r_{ji}	-	0.00016	-	0.804
Parameters	10	11	10	11
AIC	17,074	19,204	3,052	10,878
LL	8,624	9,591	1,516	5,428
RMSD	576	999	49.2	73.4

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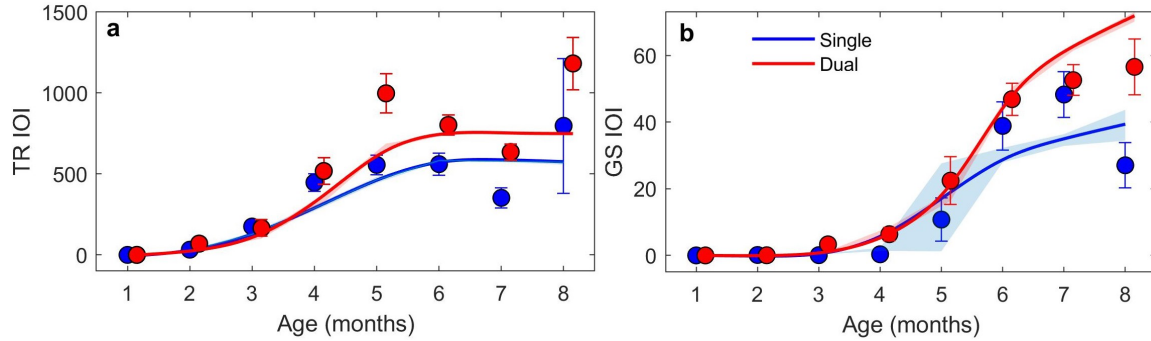
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772 **Figure 1.** Scenarios of immune-parasite interaction in single infections (a) and dual-
773 infections (b and c) for two parasite species (P_i , $i = 1, 2$) and consequences for their fitness
774 (F_i , $i = 1, 2$). Symmetrical and asymmetrical immune-mediated facilitation is presented for
775 the dual infection. We report: the magnitude (arrow thickness) and type of the effect (null=
776 0, sub-typical= \sim , positive= $+$, negative= $-$) and the parasite indirect interactions (dotted
777 arrow). **a-** Standard scenario were immunity directly affects parasite, P_i , traits (i.e.
778 abundance, development or fecundity) and reduces its fitness, F_i ; examples: many
779 helminth species, including *T. retortaeformis* in rabbits (Cattadori et al. 2005). **b-** Immunity
780 decreases against each parasite, P_1 and P_2 , and this benefits their fitness, F_1 and F_2 ,
781 compared to case a; P_1 - P_2 interactions (e.g. positive or unclear reaction) do not reduce
782 the positive net immune effect on F_1 and F_2 ; examples: hookworm and *Ascaris*
783 *lumbricoides* in humans (Fleming et al. 2006), HIV- *Mycobacterium tuberculosis* in
784 humans (Pawlowski et al. 2012), this study. **c-** Processes and impacts are as described
785 in case b, however, P_1 - P_2 asymmetrical interactions benefit the fitness F_2 of P_2 but lead to
786 sub-typical (\sim) or unclear (0) increase in fitness F_1 for P_1 , compared to case a; example:
787 *Trichuris muris*-*Schistosoma mansoni* in mice (Bickle et al. 2008) or *H. polygyrus*-
788 *Trichinella spiralis* in mice (Behnke et al. 1993).

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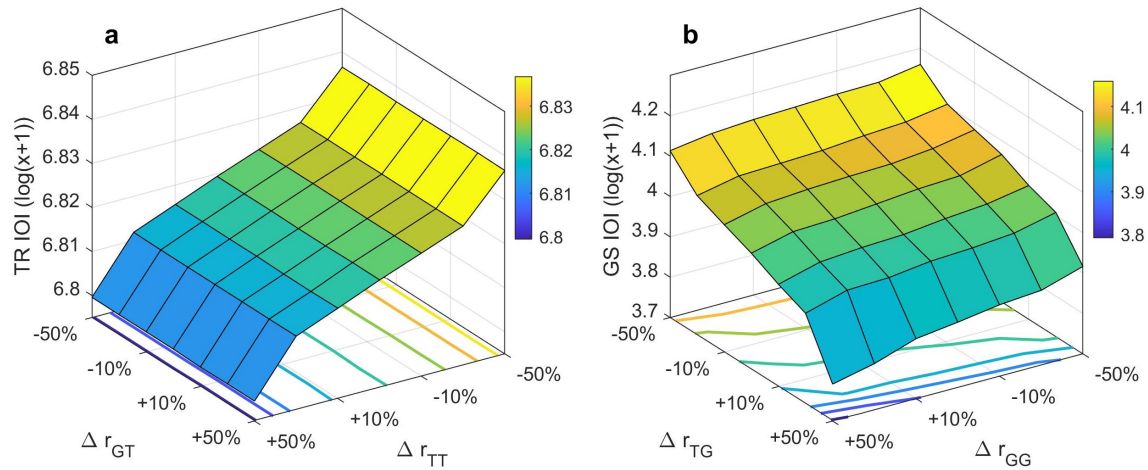
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792 **Figure 2.** Relationship between intensity of infection (IOI) and host age for *T.*
793 *retortaeformis* (TR, a) and *G. strigosum* (GS, b) in single- (blue) and dual- (red) infected
794 hosts from population A. Mean and S.E. data are reported from individual-based model
795 simulations (lines and shadow bands) and field monitoring (circles and bars, these latter
796 ones calculated under the assumption that the data follow a negative binomial
797 distribution). Only simulations referring to collected rabbit data are reported. Small S.E.
798 bars and bands could be masked by circles or lines. IOI at age 1 is forced to start at 0
799 since rabbits are exposed to the risk of infection at about 30 days of age when they switch
800 from milk to herbage.

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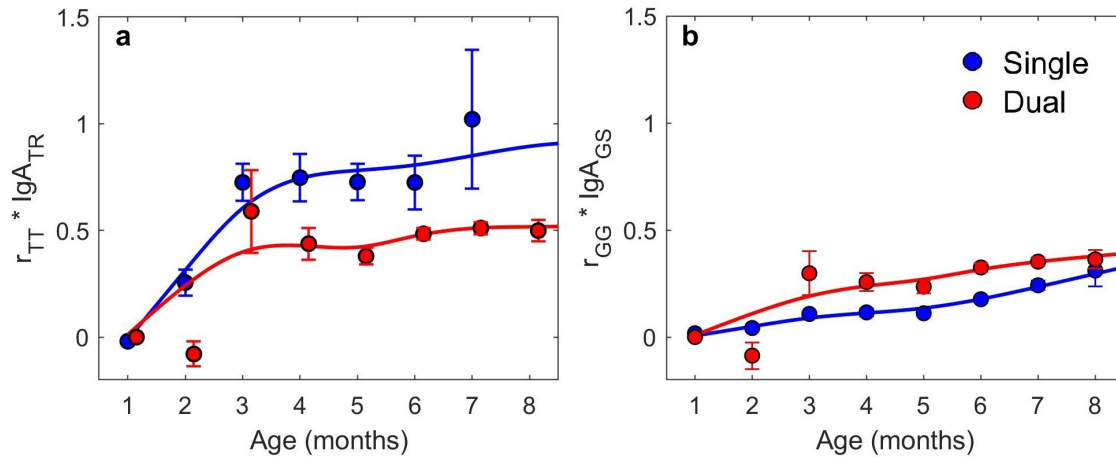


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804

805 **Figure 3.** Three-way relationships among model-predicted intensity of infection (IOI) and
806 relative changes in species-specific (Δr_{TT} or Δr_{GG}) and cross-reacting (Δr_{TG} or Δr_{GT}) stimuli
807 to IgA production for *T. retortaeformis* (TR, a) and *G. strigosum* (GS, b). Predictions are
808 from the selected best model for dual infections (M4) fitted on population A. The bivariate
809 incremental variation (% of increase or decrease) in the immune parameters, r_{ii} or r_{ji} , is
810 relative to the baseline estimated values reported in table 3. The IOIs (heat surface) are
811 obtained via sensitivity analysis where the immune parameters are incrementally changed
812 one at a time, with respect to their estimated values, and simulations are run while holding
813 all the other parameters constant. The contour lines represent the predicted IOI values
814 from the heat map at specific r_{ii} and r_{ji} values.

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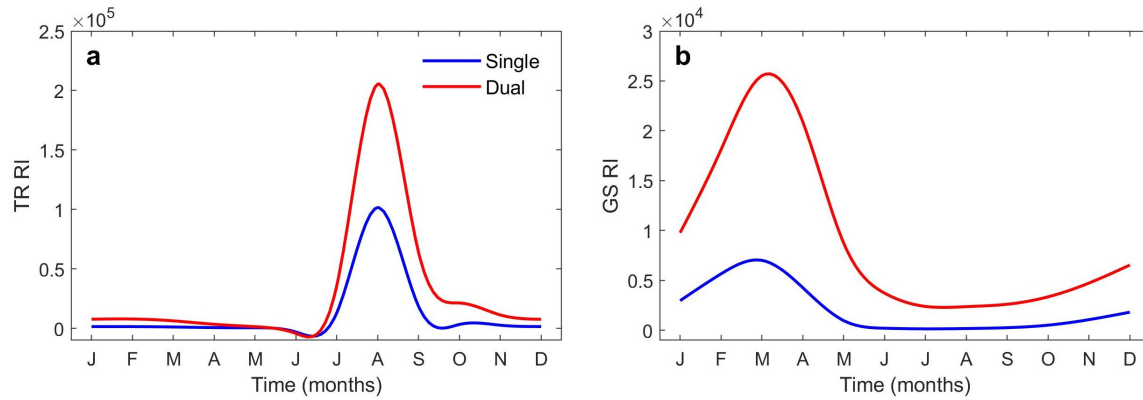


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818 **Figure 4.** Relationship between the contribution of species-specific IgA response, $r_{ii} \text{ IgA}$,
819 by host age for *T. retortaeformis* (a) and *G. strigosum* (b) in single- (blue) and dual- (red)
820 infected hosts from population A as inferred from the model. The simulated $r_{ii} \text{ IgA}$ values
821 (mean and S.E.) and the 4th order polynomial curves, weighted by sample size, are
822 reported. Small S.E. are masked by the circles.

823



824

825

826 **Figure 5.** Estimated seasonality of the mean risk of infection (RI) by sampling month for *T.*
827 *retortaeformis* (TR, a) and *G. strigosum* (GS, b) in single- (blue) and dual-infected (red) hosts
828 from population A.