**Polygenic signals of sexually antagonistic selection in contemporary human**

**genomes**

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## Abstract

Mutations that increase fitness in one sex may decrease fitness in the other. Such "sexually antagonistic" (SA) genetic variants can constrain adaptation and increase variability for fitness components (e.g., survival, fertility, and disease susceptibility). However, detecting SA selection in genomes is immensely challenging, as it requires prohibitively large datasets that combine genomic sequences with individual fitness measurements. Here, we use genotypic and reproductive success data from ~250,000 UK Biobank individuals to comprehensively assess the extent of SA genetic variation in humans. We first develop new theoretical models for signals of SA selection spanning a full generational life cycle—including SA polymorphisms affecting survival, reproductive success and overall fitness. Comparing our models with UK Biobank data, we uncover multiple empirical signals of polygenic SA selection, including sex-differential effects of genetic variants on each fitness component, and positive correlations between sex-differential effects and minor allele frequencies. We show that these signals cannot be explained by simple models of sex differences in purifying selection, or by potential confounders such as population structure and sequence mapping errors. We further show that candidate SA sites disproportionately affect functional genomic regions, including polymorphisms associated with quantitative traits and disease. Finally, we examine historical evolutionary processes affecting candidate SA sites, which are consistent with the drift-dominated dynamics predicted by previous theory. Overall, our results support SA genomic variation in humans and highlight its broader functional and evolutionary consequences.

## Introduction

Adaptation of a population to its environment requires heritable genetic variation for fitness [1]. Although many populations show substantial genetic variation for fitness components [2]— including life-history traits such as maturation rate, lifespan, mating success, and fertility [2,3]— genetic trade-offs between components reduce variation for overall fitness, and thereby limit adaptive potential [4]. For example, a mutation that increases the probability of survival to adulthood might simultaneously decrease adult reproductive success (*e.g.*, [5]), weakening the mutation's net fitness effect [4]. In addition to slowing adaptation [6–8], genetic trade-offs can increase standing genetic variation [2,9], give rise to balancing selection [10,11], and favour evolutionary transitions between mating systems [12,13], modes of sex determination [14] and genome structures [15–18].

Sexually antagonistic (SA) genetic polymorphisms—in which the alleles that benefit one sex are harmful to the other—are a type of genetic trade-off that may be common in sexually reproducing species [19]. Theory shows that SA polymorphisms are likely to arise when mutations differentially affect trait expression in each sex, or when mutations similarly affect traits under divergent directional selection between the sexes [20]. Empirical quantitative genetic studies imply that both conditions are frequently met [21–24] and, accordingly, that SA polymorphisms contribute to phenotypic variation in a range of plant and animal populations (*e.g.* [25–27]), including humans [28–30].

Although there is now abundant evidence that SA polymorphisms contribute to phenotypic variation, efforts to identify and characterise SA alleles in genomic data face two formidable challenges [31]. First, methods using explicit fitness measurements to identify SA polymorphisms (*e.g.*, genome-wide association studies (GWAS) of fitness [32]) are rarely feasible, because it is challenging to obtain fitness measurements for large numbers of genotyped individuals under natural conditions [2]. Second, methods using allele frequency

differences between adult females and males as genomic signals of SA viability selection (*e.g.*, between-sex $F_{ST}$ estimates [31,33–40]) are limited in several ways: they have low power to detect individual SA loci, they cannot distinguish SA selection from sex differences in the strength of selection, they are susceptible to artefacts generated by population structure and erroneous mapping of sequence reads to sex chromosomes [31,38,39,41], and they neglect fitness components other than viability, such as reproductive success [31,42]. Previous studies of human genomic data [33,34,41] have, to varying degrees, been affected by each of these issues [31,39,40,42], such that we currently lack robust evidence of SA genomic variation in humans. More generally, these impediments help to explain the limited catalogue of confirmed SA polymorphisms across species [43–45], which currently comprises a handful of loci with exceptionally large phenotypic effects (*e.g.* [46–50]).

Despite these challenges, new datasets and analytical approaches provide opportunities to identify robust genomic signals of SA selection. First, massive 'biobank' datasets, which are widely used in human genomics, sometimes include both genotype and offspring number data [29,51] that can be used to detect loci with SA effects on reproductive components of fitness [31]. Second, estimates of allele frequency differences between sexes—though ill-suited for confidently identifying individual SA loci affecting viability—may nevertheless be amenable to genome-wide tests for *polygenic* SA viability selection [31,33]. Third, polygenic metrics of sex-differential selection (*e.g.*, between-sex $F_{ST}$) may include an appreciable proportion of genuine SA loci in the upper tails of their distributions, providing a set of candidate loci that can collectively yield insights into the general properties of SA polymorphisms (*e.g.*, their functional characteristics and evolutionary dynamics), despite uncertainty about individual candidates.

Here, we extend [31,33] and develop new statistical tests to detect polygenic signals of SA polymorphism affecting viability, reproduction, and total fitness during a full generational

cycle. We apply them to the UK Biobank [51], a dataset comprising quality-filtered genotype and

offspring number data for ~250,000 men and women. The tests, which are based on between-

sex $F_{ST}$ metrics and the covariance between $F_{ST}$ metrics and minor allele frequencies (MAF),

reveal polygenic signals of SA selection. Specifically: (*i*) $F_{ST}$ estimates are consistently higher

than expected under a null hypothesis in which sex-differential selection is absent; (*ii*) $F_{ST}$

estimates are positively correlated with MAF across loci, as predicted under SA selection. We

support the $F_{ST}$-based results by: (*i*) replicating these analyses using mixed-model association

tests that explicitly control for any systematic differences in the genetic ancestry of female and

male individuals; and (*ii*) showing that loci exhibiting artefactual signatures of SA selection

due to sequence mapping errors [41] do not occur in our quality-filtered dataset. We further show

that candidate SA polymorphisms are preferentially situated in coding and regulatory

sequences, and contribute to variation in a range of morphological, behavioural and medically

relevant phenotypes. Finally, we use genetic diversity data from global human populations to

test for long-term balancing selection, which has been hypothesised to affect SA

polymorphisms [10].

**Results**

**Genomic signals of sex differences in selection: theoretical predictions**

To illustrate our analytical approach, consider a large, well-mixed population containing many

polymorphic, bi-allelic, autosomal loci. At the start of a generation (*i.e.*, at fertilisation),

Mendelian inheritance equalises allele frequencies between the sexes (Fig. 1, left box). Loci

with sex-differential effects on zygote-to-adult survival will accumulate between-sex allele

frequency differences that become apparent among adults (*e.g.*, the black allele becomes

enriched in adult males and deficient in adult females because it improves zygote-to-adult

survival in males but reduces it in females; Fig. 1, middle box). Furthermore, loci with sex-

differential effects on the number of offspring produced will have different transmission rates

to the next generation from surviving females *versus* surviving males (*e.g.*, the black allele

increases transmission to offspring of males but decreases transmission to offspring of females;

Fig. 1, right box). Thus, provided allele frequency and offspring number data are available for

adult females and males, we can, in principle, estimate sex-differential effects of genetic

variation during a full generational life cycle (Fig. 1), even though allele frequencies among

zygotes and gametes are inferred and not directly observed.

The UK Biobank provides this opportunity, as it includes genotypes and reported

offspring numbers (hereafter "lifetime reproductive success" or LRS, following standard

evolutionary biology terminology [29]) among putatively post-reproductive adults (ages 45-69

after filtering; see Methods). For a focal autosomal locus with alleles $A_1$ and $A_2$, we denote $\hat{p}_f$

and $\hat{p}_m$ ($\hat{q}_f$ and $\hat{q}_m$) the respective estimated frequencies of the $A_1$ ($A_2$) allele in adult females

and males of the UK Biobank. Using LRS data of UK Biobank individuals, projected paternal

and maternal transmission rates of each allele are estimated as:

$$\hat{p}'_m = \frac{M_{11} + \frac{1}{2} M_{12}}{M_{11} + M_{12} + M_{22}} \qquad [1],$$

$$\hat{p}'_f = \frac{F_{11} + \frac{1}{2} F_{12}}{F_{11} + F_{12} + F_{22}}$$

where $M_{ij}$ and $F_{ij}$ represent the cumulative LRS of individuals (males and females, respectively)

with genotype $ij$ (*e.g.*, $M_{11}$, $M_{12}$ and $M_{22}$ correspond to genotypes $A_1A_1$, $A_1A_2$, and $A_2A_2$).

Using $F_{ST}$ [52], we partition between-sex allele frequency differentiation over one

generation into the differentiation due to: 1) sex-differential variation in survival to adulthood

(hereafter "adult $F_{ST}$"; see [31,33,42]); 2) sex-differential variation in adult LRS (hereafter

"reproductive $F_{ST}$"); and 3) sex-differential variation in overall fitness (hereafter "gametic

135      $F_{ST}$"). Single-locus estimates of adult $F_{ST}$, reproductive $F_{ST}$ and gametic $F_{ST}$ are defined,

136      respectively, as:

$$\hat{F}_{ST} = \frac{\left(\hat{p}_f - \hat{p}_m\right)^2}{4\bar{p}(1-\bar{p})} \qquad \text{[2a]},$$

$$\hat{F}_{ST} = \frac{\left(\left(\hat{p}'_f - \hat{p}_f\right) - \left(\hat{p}'_m - \hat{p}_m\right)\right)^2}{4\bar{p}(1-\bar{p})} \qquad \text{[2b]},$$

$$\hat{F}_{ST} = \frac{\left(\hat{p}'_f - \hat{p}'_m\right)^2}{4\bar{p}'(1-\bar{p}')} \qquad \text{[2c]},$$

where $\bar{p} = \left(\hat{p}_f + \hat{p}_m\right)/2$ and $\bar{p}' = \left(\hat{p}'_f + \hat{p}'_m\right)/2$.

In the absence of sex differences in selection (*e.g.*, under neutrality, or under sexually

concordant selection of equal magnitude and direction in each sex), with large sample sizes,

and excluding single-nucleotide polymorphisms (SNPs) with very low minor allele frequencies

(*i.e.*, MAF < 1% in the UK Biobank), we show that adult, reproductive and gametic $\hat{F}_{ST}$

converge, respectively, to the following simple null distributions (*SI Appendix*, Section A):

$$\hat{F}_{ST} \approx \left[1/8N_f + 1/8N_m\right]X \qquad \text{[3a]},$$

$$\hat{F}_{ST} \approx \left[(\sigma_f^2/\mu_f^2)/8N_f + (\sigma_m^2/\mu_m^2)/8N_m\right]X \qquad \text{[3b]},$$

$$\hat{F}_{ST} \approx \left[(1 + \sigma_f^2/\mu_f^2)/8N_f + (1 + \sigma_m^2/\mu_m^2)/8N_m\right]X \qquad \text{[3c]}.$$

where $X$ is a chi-square random variable with one degree of freedom, $N_f$ and $N_m$ denote adult

female and male sample sizes, $\mu_f$ and $\mu_m$ denote mean LRS, and $\sigma_f^2$ and $\sigma_m^2$ denote the

corresponding variances in LRS for sampled adult females and males. All three null

distributions are independent of MAF, provided sites with very low MAFs are first removed.

Relative to the null distributions in eqs. [3a-c], sex differences in selection alter the

distributions of each $F_{ST}$ metric in two important ways. First, sex differences in selection inflate

$\hat{F}_{ST}$ metrics relative to null model predictions (*SI Appendix*, Section B). These inflations may

arise due to polymorphisms under sex-differential selection *and* neutral polymorphisms that

hitchhike with selected polymorphisms, but linkage disequilibrium (LD) alone cannot inflate

genome-wide $\hat{F}_{ST}$ in the absence of genuine selected polymorphisms (*SI Appendix*, Section C).

Thus, $\hat{F}_{ST}$ inflations represent reliable signals of sex-differentially selected polymorphism [31] (if

not of the number of independent selected loci), provided population structure and technical

artefacts are also controlled (as shown below).

Second, sex differences in selection generate statistical associations between $\hat{F}_{ST}$ and

MAF that are indicative of the form of sex-differential selection. Specifically, SA selection can

generate a positive covariance between each $\hat{F}_{ST}$ metric and MAF, whereas sexually concordant

(and/or sex-limited) selection generates a negative covariance (*SI Appendix*, Section B). The

negative covariance under sexually concordant selection arises because purifying selection

disproportionately lowers the frequency of large-effect alleles relative to small-effect alleles,

which is a general feature of loci evolving under purifying selection (see [53]). In contrast, a

positive covariance can arise under SA selection because large-effect SA alleles reach

intermediate frequencies more easily under balancing selection than small-effect SA alleles,

and because intermediate-frequency alleles inflate $\hat{F}_{ST}$ more than low-frequency alleles

(irrespective of the strength of balancing selection; *e.g.*, even under drift). Thus, while any sex

difference in selection can elevate genome-wide $\hat{F}_{ST}$, positive associations between $\hat{F}_{ST}$ and

MAF cannot arise under sex differences in purifying selection alone—instead, they indicate

the presence of SA variation. These predictions apply when current patterns of sex-differential

selection (which affect measures of $F_{ST}$) are similar to historical patterns of selection (which

influence MAF), and are valid under both deterministic and non-deterministic scenarios (*SI*

*Appendix*, Section B). Below, we test for both predicted signals of SA selection in the UK

Biobank dataset.

**UK Biobank SNP data**

The sample size after removing individuals with close relatedness or non-White British

ancestry (see Methods) was $N = 250,297$ ($N_m = 116,661$ males and $N_f = 133,636$ females). We

removed rare polymorphic sites (MAF < 1%), sites with low genotype or imputation quality,

and sites potentially driving artefactually high between-sex allele frequency differences based

on criteria identified by Kasimatis et al. [41]. These criteria were based on differences in missing

rates between sexes, deficits of minor allele homozygotes, and excess heterozygosity (*i.e.*,

beyond what can be plausibly be explained by sex differences in selection; see *SI Appendix*,

Section D). Unless noted, we focus on quality-filtered genotyped SNPs (N = 544,635) in the

main text. Results from LD-pruned genotyped SNPs and imputed SNPs (N = 7,844,649)

closely match genotyped data and are presented in the *SI Appendix* (Sections E-H), along with

full statistical tables.

**Polygenic signals of sex differences in selection in genome-wide $\widehat{F}_{ST}$ distributions**

We tested for sex differences in selection by calculating adult $\widehat{F}_{ST}$, reproductive $\widehat{F}_{ST}$ and

gametic $\widehat{F}_{ST}$ (eqs. [2a-c]) in the UK Biobank, and contrasting these standardised estimates of

allele frequency differentiation between sexes against: (*i*) their respective theoretical null

distributions (eqs. [3a-c]), and (*ii*) empirical null distributions generated by a single random

permutation of male and female labels among individuals or, in the case of reproductive $\widehat{F}_{ST}$, a

single permutation of LRS among individuals of a given sex (see Methods).

All three $\widehat{F}_{ST}$ metrics showed significantly greater differentiation than predicted by their

theoretical and empirical null distributions, consistent with sex differences in selection

contributing to genome-wide allele frequency differentiation between the sexes. Mean adult

$\widehat{F}_{ST}$ in the observed data was larger than predicted by both null distributions (theoretical null:

$2.012 \times 10^{-6}$; permuted null: $2.014 \times 10^{-6}$; observed: $2.107 \times 10^{-6}$; Wilcoxon and Kolmogorov-

Smirnov tests, p<0.001; Fig. 2A,D; *SI Appendix*, Section E, Figs. S1-5; Tab. S1), with a 20.4%

excess of SNPs in the top 1% quantile of the theoretical null and a 16.5% excess in the top 1% quantile of the empirical null ($\chi^2$ tests, p<0.001). Mean reproductive $\hat{F}_{ST}$ was larger than predicted by both nulls (theoretical: $8.667 \times 10^{-7}$; permuted: $8.770 \times 10^{-7}$; observed: $9.049 \times 10^{-7}$; Wilcoxon and Kolmogorov-Smirnov tests, p<0.001; Fig. 2B,E; *SI Appendix*, Section E, Figs. S1-5; Tab. S1), with a 17.9% excess of SNPs in the top 1% quantile of the theoretical null and a 11.5% excess in the top 1% quantile of the empirical null ($\chi^2$ tests, p<0.001). Mean gametic $\hat{F}_{ST}$ was larger than predicted by both nulls (theoretical: $2.874 \times 10^{-6}$; permuted: $2.874 \times 10^{-6}$; observed: $2.986 \times 10^{-6}$; Wilcoxon and Kolmogorov-Smirnov tests, p<0.001; Fig. 2C,F; *SI Appendix*, Section E, Figs. S1-5; Tab. S1), with a 17.1% excess of SNPs in the top 1% of the theoretical and empirical nulls ($\chi^2$ tests, p<0.001).

Signals of sex differences in selection in adult, reproductive, and gametic $\hat{F}_{ST}$ were polygenic: although each $\hat{F}_{ST}$ metric was markedly inflated on a genome-wide scale, no individual locus reached a p-value below the Bonferroni-corrected threshold ($9.181 \times 10^{-8}$; *SI Appendix*, Section E, Figs. S6-7). For example, the minimum p-values were $3.260 \times 10^{-7}$ for adult $\hat{F}_{ST}$ (minimum q-value=0.101), $7.036 \times 10^{-7}$ for reproductive $\hat{F}_{ST}$ (minimum q-value=0.383), and $2.858 \times 10^{-6}$ for gametic $\hat{F}_{ST}$ (minimum q-value=0.346).

**Positive associations between $\widehat{F}_{ST}$ and MAF indicate SA selection**

To distinguish polygenic signals of SA selection from other modes of selection that might also give rise to elevated $\hat{F}_{ST}$ (*e.g.*, selection acting only on one sex, or differences in the strength but not the direction of selection between sexes), we examined the association between MAF and each $\hat{F}_{ST}$ metric. This association can be positive under SA selection but should be negative under sex-differential purifying selection, provided patterns of sex-differential selection are relatively consistent over time (see above). Consistent with SA selection, we observed positive correlations between MAF and all three $\hat{F}_{ST}$ metrics (adult $\hat{F}_{ST}$, $\rho$=0.014, p<0.001; reproductive

$\widehat{F}_{ST}$, $\rho$=0.010, p<0.001; gametic $\widehat{F}_{ST}$, $\rho$=0.010, p<0.001; Fig. 3A-C; *SI Appendix*, Section F,

Figs. S9-13; Tab. S2), with all correlations stronger in observed than null data (*SI Appendix*,

Section F, Fig. 3D-F; Figs. S10,12).

**Signals of SA selection persist after controlling for sex-specific population structure**

In principle, genome-wide elevations in $\widehat{F}_{ST}$ can arise entirely from systematic differences in

ancestry (population structure) between sexes and in the absence of genuine sex differences in

selection [31,42]. We therefore replicated our analyses using mixed-model association tests that

are analogous to $\widehat{F}_{ST}$ but which explicitly correct for population structure.

We first evaluated signals of sex differences in viability selection by performing a

GWAS of sex [31,41,54] using standardised estimates of the log-odds ratio ($\hat{\mathcal{L}}_{ST}$; see Methods). $\hat{\mathcal{L}}_{ST}$

quantifies between-sex allele frequency differences among adults (like adult $\widehat{F}_{ST}$) while

controlling for population structure by including a kinship matrix of genome-wide relatedness

between individuals. As expected, $\hat{\mathcal{L}}_{ST}$ was highly correlated with adult $\widehat{F}_{ST}$ (Spearman's

$\rho$=0.988; p<0.001; *SI Appendix*, Section E, Fig. S8) and was elevated relative to an empirical

null distribution generated through permutation of sex labels (null mean $\hat{\mathcal{L}}_{ST}$: $5.000\times10^{-7}$; mean

observed: $5.188\times10^{-7}$; Wilcoxon and Kolmogorov-Smirnov tests, p<0.001; *SI Appendix*,

Section E, Figs. S1-5; Tab. S1), with a 14.0% excess of SNPs in the top 1% quantile of the

empirical null ($\chi^2$ test, p<0.001), and a significant SNP-heritability of sex

($h_{SNP}^2$±SE=0.014±0.002).

We then tested for a signal of sex differences in selection through reproductive fitness

components by performing separate GWAS for LRS in females and males (controlled for

population structure) and quantifying the difference between female and male effect sizes using

a *t*-statistic ($|t|$; see Methods). As expected, the distribution of $|t|$ was highly correlated to

reproductive $\widehat{F}_{ST}$ (Spearman's $\rho$=0.921; p<0.001; *SI Appendix*, Section E, Fig. S8) and was

elevated relative to an empirical null generated by permutation of LRS within each sex (null

mean $|t|$=0.797, observed mean $|t|$=0.817, Wilcoxon and Kolmogorov-Smirnov tests, p<0.001;

*SI Appendix*, Section E, Figs. S1-5; Tab. S1), with an 17.9% excess of SNPs in the top 1%

quantile of the empirical null ($\chi^2$ test, p<0.001). Finally, $\hat{\mathcal{L}}_{ST}$ and $|t|$ were both positively

correlated with MAF ($\hat{\mathcal{L}}_{ST}$: $\rho$=0.014, p<0.001; $|t|$: $\rho$=0.010, p<0.001; *SI Appendix*, Section F,

Figs. S9-13; Tab. S2), confirming the signals of SA selection detected with $\hat{F}_{ST}$ metrics.

**Functional analyses of candidate SA SNPs**

If loci with high $\hat{F}_{ST}$ (or related metrics) include genuine SA polymorphisms, they should

preferentially be found in functionally important regions in the genome, whereas such

enrichment is not expected if the observed $\hat{F}_{ST}$ inflation results from random chance,

genotyping errors, or sex-specific population structure. We therefore conducted several

enrichment tests, both to support our inference that SA selection is occurring and to explore

functional effects of candidate SA loci.

First, we asked whether sites with high sex-differentiation were disproportionately

situated in "genic" regions, defined broadly to include coding and regulatory elements (see

Methods). This test revealed consistently positive associations between each metric of sex-

differential selection and genic status (Binomial GLMs: adult $\hat{F}_{ST}$, p=0.021; $\hat{\mathcal{L}}_{ST}$, p=0.018;

reproductive $\hat{F}_{ST}$, p=0.0497; $|t|$, p=0.025; gametic $\hat{F}_{ST}$, p=0.026; Fig. 4A-C; *SI Appendix*,

Section G, Figs. S14-15; Tab. S3). Polygenic patterns of genic enrichment in the imputed data

were similar to the genotyped data (*SI Appendix*, Section G, Fig. S16; Tab. S3), though

extremely differentiated loci were less often genic in the imputed data, which may reflect

higher genotype uncertainty among imputed sites and the consequently higher likelihood of

artefacts.

Second, we used summary statistics from the Neale laboratory database of UK Biobank

GWAS to explore whether metrics of sex-differential selection were associated with candidate

loci for 43 phenotypes, chosen for their medical relevance and/or relationship to phenotypic

sex differences. Though few traits were associated after FDR-correction in the genotyped data

(*SI Appendix*, Section G, Fig. S17), we found multiple associations in the imputed data, where

the number of loci (and thus statistical power) is larger (Fig. 4D). For example, several disease-

relevant traits (high blood pressure; red blood cell count; diseases of the musculoskeletal

system and connective tissue; heel bone mineral density) and behavioural traits (neuroticism

score) were associated with metrics of sex-differential survival and LRS (Mann-Whitney tests;

FDR-corrected $p < 0.05$). We also found trait associations that were unique to metrics of sex-

differential survival (white blood cell count; body fat percentage) and LRS (standing height;

platelet count). Loci affecting testosterone had lower-than-average gametic $\hat{F}_{ST}$.

**Evolutionary histories of candidate SA SNPs**

To gain insights into the evolutionary dynamics of candidate SA sites, we tested for signals of

long-term balancing selection, which can, under certain scenarios of selection and dominance,

stably maintain SA polymorphisms over long periods of time [10]. We used three metrics of

balancing selection: allele age estimates from the Atlas of Variant Age database [55], between-

population $\hat{F}_{ST}$ from four worldwide non-European populations from the 1000 Genomes

Project [56], and three independent sets of candidate loci for balancing selection [57–59]. In each

case, we looked for associations between $\hat{F}_{ST}$ metrics of sex-differential selection and metrics

of balancing selection, while controlling for ascertainment bias of intermediate-frequency

alleles (which are, on average, older) among highly sex-differentiated sites (*i.e.*, Fig. 3; see

Methods). Under long-term balancing selection, we would expect candidate SA alleles (and

linked loci) to be older, to exhibit lower between-population $\hat{F}_{ST}$, and to disproportionately co-

localise with previous candidates for balancing selection, compared to non-candidate SA sites

with similar allele frequencies in the UK Biobank.

We found no significant associations between metrics of sex-differential selection and

metrics of balancing selection, including allele age (adult $\hat{F}_{ST}$, Spearman's $\rho$=0.001, p=0.353;

reproductive $\hat{F}_{ST}$, Spearman's $\rho$=0.000, p=0.919; gametic $\hat{F}_{ST}$: Spearman's $\rho$=0.002, p=0.092;

Fig. 5; *SI Appendix*, Section H, Figs. S18,21,22; Tab. S4), between-population $\hat{F}_{ST}$ (*SI*

*Appendix*, Section H, Fig. S19; Tab. S5), or previous candidates for balancing selection (*SI*

*Appendix*, Section H, Figs. S20,21,23; Tabs. S6-8). Overall, there is no compelling evidence

for long-term balancing selection among candidate SA SNPs.

**Discussion**

Sex differences in directional selection on phenotypes have been reported in a wide range of

animal taxa [21–23,60], including post-industrial human populations [29,30], yet population genomic

signals of SA selection have been extremely difficult to establish. The reason is simple: sexual

reproduction equalises autosomal allele frequencies between the sexes every generation, which

restricts genetic divergence between males and females and, in effect, precludes the use of tests

that are commonly used to detect other forms of selection (*e.g.*, McDonald-Kreitman tests for

positive selection and $F_{ST}$ outlier tests for spatially-varying selection [61–63]). Published studies

using human genomic data illustrate the challenges of studying SA polymorphisms, including

sample sizes that may be insufficient for detecting polygenic signals of selection [31,33,34], lack

of controls for population structure or technical artefacts [33,34], and/or absence of data

concerning reproductive components of fitness [33,34,41].

Here, by developing new metrics of SA genomic variation and applying them to data

from a quarter-million UK adults, we present robust evidence for polygenic sex-differential

selection in humans. Specifically, UK Biobank individuals showed sex differences in allele

frequencies—both among adults and their (projected) offspring—that consistently exceeded

expectations defined by our theoretical null models for viability, reproductive and total fitness,

and these signals persisted after controlling for sex-specific population structure. Our analyses

of reproductive $\hat{F}_{ST}$ and $|t|$ metrics are particularly compelling because they control for allele

frequency differences between samples of adults of each sex and rule out factors that might

otherwise affect estimated adult allele frequencies in the UK Biobank (*e.g.*, mis-mapping of

reads to sex chromosomes, participation bias [54]; see below). These elevations in reproductive

$\hat{F}_{ST}$ and $|t|$ are consistent with previous observations in post-industrial human populations,

including variation in female and male LRS [64] (a necessary precondition for sex-differential

selection), widespread sex differences in the genetic basis of quantitative traits (*e.g.*, in the UK

BioBank [65]), and SA selection on phenotypes (*e.g.*, height [29,30] and multivariate trait

combinations [64]), which should collectively lead to SA polymorphisms throughout the genome

[20]. In particular, our finding that candidate loci for standing height were positively associated

with reproductive $\hat{F}_{ST}$ and $|t|$ is in line with earlier reports of SA selection acting on adult height

[29,30]. Furthermore, the positive associations we report between MAF and $\hat{F}_{ST}$ (and related

metrics) are consistent with SA selection and cannot be explained by simple models of sex

differences in purifying selection. Though it is conceivable that contemporary patterns of

selection (which influence $\hat{F}_{ST}$) are sufficiently different from historical patterns of selection

(which influence MAF) that our models do not reflect the evolutionary causes of the positive

associations between MAF and $\hat{F}_{ST}$, SA polymorphisms represent a parsimonious explanation

for the positive correlation we detect [29,30].

At first glance, the signals of SA viability selection in adult $\hat{F}_{ST}$ and $\hat{\mathcal{L}}_{ST}$ metrics may

seem surprising given the low rates of infant and juvenile mortality in post-industrial human

populations [64]. However, mortality after fertilisation but before birth is common (on the order

of 50% [66]), giving ample opportunity for sex differences in mortality to generate allele

frequency differences [67]. Another possibility, raised by Pirastu et al. [54], is that sex differences

in adult allele frequencies arise because of sex differences in the genetic basis of individuals'

predisposition to take part in the UK Biobank study, which relies upon active participation. To

support this interpretation, they reported significant SNP heritability of sex (a polygenic

measure of sex differences in allele frequencies) in biobanks relying on active participation

(UK Biobank; 23andMe), and non-significant SNP heritability in biobanks using passive

participation (Biobank Japan; Finngen; iPsych). However, this result might instead reflect

differences in statistical power, as passive participation studies are considerably smaller than

active participation studies. Further work (*e.g.*, parent-offspring trio analyses that control for

participation effects [67]; replication studies in other Biobank-scale datasets) will be required to

conclusively distinguish the relative contributions of SA selection and participation bias on

allele frequency differentiation among male and female adults, and to assess whether SA

variants affecting viability tend to increase or decrease LRS within and across sexes.

We also found that candidate SA sites were preferentially found within coding and

regulatory elements, and contributed to variation in morphological, physiological, behavioural,

and medically relevant phenotypes. These functional analyses provide further evidence that

elevated between-sex $\hat{F}_{ST}$ reflects selection rather than technical artefacts. They also lend

support to the hypothesis that SA alleles contribute to disease susceptibility [9]. For example,

loci associated with bone mineral density and red blood cell count showed elevated signals of

SA selection. Bone mineralisation and red blood cell count are sexually dimorphic traits that

positively genetically correlate with musculoskeletal disease and high blood pressure [68].

Accordingly, loci associated with musculoskeletal disease and high blood pressure also showed

elevated sex-differentiation.

Our analyses do not reveal clear signals of long-term balancing selection among

candidate SA sites, which may stem from several factors. First, balancing selection—to the

extent that it maintains SA polymorphisms—may be too recent to generate a clear statistical

signal in our analyses [69]. Second, balancing selection at SA loci may be *effectively* weak, owing

to relatively small $N_e$ in humans [70] and the high susceptibility of SA alleles to genetic drift [71].

Third, long-term balancing selection may be present, but statistical tests for it may be too weak

to stand out from the background noise of false positives in our metrics and the datasets used

to quantify balancing selection [72]. Overall, evidence that SA polymorphisms contribute to

standing genetic variation—as in our study—is at present stronger than evidence that they are

stably maintained by balancing selection (but see [32]).

To what extent should we expect the patterns reported here to replicate across studies?

Many taxa exhibit greater variance for reproductive success than humans [73], generating higher

potential for polygenic signals of SA selection. In line with this, polygenic inflation of adult

$\hat{F}_{ST}$ has previously been documented in modest samples of pipefish and flycatchers [31,36,37],

suggesting that sex differences in selection might be stronger in those species than in humans.

Yet while polygenic signals of SA selection may replicate across studies, candidate SA

polymorphisms may not. One reason is that environmental differences between populations

(*e.g.*, cultural differences in family planning between human populations) could alter the set of

loci under SA selection. Additionally, the noisiness of polygenic signals of SA selection [31,42],

along with the near-certainty that most polymorphic loci have small effects on fitness [74],

generates variation in the set of candidate SA polymorphisms *identified* across populations or

generations, even if causal SA polymorphisms do not differ. Similar predictions apply to

scenarios of polygenic local adaptation with high gene flow [75], whose population genetic

dynamics strongly parallel SA selection [31,76].

Finally, the extent to which signals of balancing selection will co-occur with SA

polymorphisms awaits further study, but given the pronounced sensitivity of SA balancing

selection to genetic drift [71,77], we should expect the relationship between signals of SA selection

and balancing selection to vary with $N_e$. For example, previous work in *Drosophila*

*melanogaster* indicates that candidate SA polymorphisms segregate across worldwide

populations and even species [32], and in contrast to the results of our study, these candidates are

putatively maintained under balancing selection. A parsimonious explanation for these

contrasting findings is that the effectiveness of balancing selection is lower in humans than

fruit flies due to much smaller $N_e$.

**Methods**

**Quality control of UK Biobank data**

Access to UK Biobank data was granted under project number 52049. We used sample-level

information provided by the UK Biobank (see [51] for details) to perform individual-level

(phenotypic) quality controls. Specifically, we excluded individuals with high relatedness (3rd

degree or closer), non-White British ancestry, high heterozygosity and high missing rates.

Individuals whose reported sex did not match their inferred genetic sex, whose age was less

than 45 years, and aneuploids were also excluded. In addition to site-level quality-controls

implemented by the UK Biobank [51], we used PLINK and PLINK2 [78] to remove sites that were

non-diallelic, had MAF<1%, missing rates>5%, and p-values<$10^{-6}$ in tests of Hardy-Weinberg

equilibrium. These filters were applied to all autosomal genotyped and imputed sites. We

further removed imputed sites with INFO score ≤0.8, denoting poor imputation.

**Artefact filtering in UK Biobank data**

Mis-mapping of autosomal reads to sex chromosomes can generate between-sex allele

frequency differences in the absence of sex differences in selection [31,41] (though note that such

artefacts are not expected to inflate metrics of adult reproductive success, since these metrics

control for any sex differences in allele frequencies among adults). To remove mis-mapping

artefacts, we excluded: (*i*) sites with heterozygosity levels that exceeded what could plausibly be expected under SA selection (see below and *SI Appendix*, Section D); (*ii*) sites with a deficit of minor allele homozygotes; (*iii*) sites exhibiting large differences in missing rate between sexes. These three patterns have previously been shown to associate with mis-mapping of reads to sex chromosomes [41].

To remove sites with artificially inflated heterozygosity, we estimated $F_{IS}$ for each SNP, defined as:

$$\hat{F}_{IS} = \frac{P_{Aa}}{2\bar{p}(1-\bar{p})} - 1$$

where $P_{Aa}$ denotes the frequency of heterozygotes for a given locus and $\bar{p}$ the sex-averaged allele frequency. For a SA locus at polymorphic equilibrium, the distribution of $\hat{F}_{IS}$ is well approximated by a normal distribution with expectation and variance as follows:

$$E[\hat{F}_{IS}] \approx \frac{1}{2n} + \frac{p(1-p)}{4}\left(\frac{s_{max}}{1-ps_{max}}\right)^2$$

$$var[\hat{F}_{IS}] = \frac{1}{n}$$

where $n$ is total sample size of adults, $p$ the minor allele frequency, and $s_{max} = \max(s_m, s_f)$ with $s_m$ and $s_f$ representing male and female selection coefficients (*SI Appendix*, Section D). To identify SNPs with excess heterozygosity, we compared $\hat{F}_{IS}$ in the observed data to expected $\hat{F}_{IS}$ under strong SA selection ($s_{max}$=0.2) by performing a one-tailed Z-test for excess heterozygosity. We thus obtained p-values for each locus, corrected p-values for multiple testing using Benjamini-Hochberg false discovery rates [79], and removed sites with FDR q-values below 0.05. Note that this test was designed to eliminate mapping errors, but it will also eliminate sites under strong (but not weak or moderately strong) sex-differential selection. The net effect of applying this filter is a slightly conservative test of sex-differential selection.

To identify sites with a deficit of minor allele homozygotes, we compared the observed

frequency of minor allele homozygotes to the expected frequency under Hardy-Weinberg

equilibrium ($p^2$, where $p$ is the frequency of the minor allele) by performing a one-tailed

binomial test, removing sites with FDR q-values below 0.05. Tests for excess heterozygosity

and deficits of minor allele homozygotes were performed across all individuals (regardless of

sex), and also for each sex separately. Sites were removed if they exhibited q-values below

0.05 in any of the three tests (*i.e.*, both sexes combined, females, and males). Finally, to assess

differences in missing rate between the sexes, we performed a $\chi^2$ test, removing sites with

FDR q-values below 0.05.

Reassuringly, applying these filters eliminated all 8 sites that Kasimatis et al. [41]

identified as false-positives for SA viability selection in the genotyped data. One remaining

site (rs114928327) appeared in the imputed data but exhibited lower-than-average adult $\hat{F}_{ST}$

and $\hat{\mathcal{L}}_{ST}$.

**Quantifying polygenic signals of sex differences in selection**

*$\hat{F}_{ST}$-based metrics*

Allele frequencies in adults of each sex were obtained directly from sequence data and used to

calculate adult $\hat{F}_{ST}$ for each polymorphic site (post-filtering). Allele frequency differences

between sexes were estimated using the $\hat{F}_{ST}$ metrics presented in eqs. [2a-c]. Data on offspring

number were obtained from field 2405 "Number of children fathered", for males, and field

2734 "Number of live births", for females (hereafter "lifetime reproductive success" (LRS)).

Because some individuals were asked to report offspring number at repeated assessment points,

we considered the maximum offspring number reported as the definitive value of LRS for that

individual. Though mis-estimation of LRS for each individual cannot be definitively excluded

(*e.g.*, due to mis-reporting, or additional reproduction after data collection), we minimised this

possibility by removing individuals: (*i*) younger than 45 years of age (see "Quality control of

UK Biobank data"); (*ii*) reporting fewer offspring at a later assessment point than at an earlier

assessment point; (*iii*) with 20 or more reported offspring numbers (large offspring numbers

often ended in zero—*e.g.,* 20, 30, 50, 100—and were thus considered less reliable).

Furthermore, we note that uncounted LRS data adds imprecision but should not systematically

bias our analyses. Finally, previous research indicates that offspring number represents a good

proxies for LRS in post-industrial human populations, based on observations of positive

genetic correlations between offspring and grand-offspring numbers across generations [80].

The theoretical null distributions presented in eqs. [3a-c] apply to genome-wide data in

which the sample of female and male sequences are constant across loci. For each null, we

adjusted for locus-specific missing data (which causes variation in locus-specific sample sizes)

by allowing sample sizes to vary across loci (*i.e.*, $N_{f_i}$ and $N_{m_i}$ adults, or $2N_{f_i}$ and $2N_{m_i}$

sequences, per diploid locus *i*).

*Case-control GWAS of sex*

To complement the test for sex-differential viability selection based on adult $\hat{F}_{ST}$, we performed

a GWAS of sex [31,41,54]. By analogy to adult $\hat{F}_{ST}$, loci with sex-differential effects on viability

in a GWAS of sex will tend to have relatively large absolute log-odds ratios (corresponding to

relatively large allele frequency differences between sexes). Unlike adult $\hat{F}_{ST}$, this approach

additionally permits the inclusion of covariates in the GWAS to account for population

structure and other possible confounders [31].

We used BOLT-LMM to run a mixed-model GWAS [81], using a kinship matrix to

account for population structure. The kinship matrix was constructed from a subset of 241,669

LD-pruned genotyped SNPs (settings '--indep-pairwise 50 10 0.2' in PLINK; MAF>0.01). We

added individual age (field 54) and assessment centre (field 21003) as fixed-effect covariates.

To facilitate comparisons with adult $\hat{F}_{ST}$, we standardised the regression coefficients (log-odds

ratios) from the GWAS by allele frequency, such that:

$$\hat{\mathcal{L}}_{ST} = (\sqrt{\bar{p}(1-\bar{p})}\hat{\mathcal{L}})^2$$

where $\hat{\mathcal{L}}$ is the log-odds ratio and $\bar{p}$ is the sex-averaged allele frequency among adults. We also

quantified a genome-wide signal of sex-differential viability selection by estimating the SNP-

heritability of sex, in BOLT-LMM.

*t-statistic for sex differences in GWAS of LRS*

To complement the test for sex differences in selection on LRS based on reproductive $\hat{F}_{ST}$, we

performed a GWAS of LRS in each sex separately, using a mixed-model GWAS implemented

in BOLT-LMM, which allowed us to correct for population structure in effect size estimates.

Following [82], we quantified differences in male and female effect size estimates by means of a

*t*-statistic, defined as:

$$|t| = \left| \frac{\beta_M - \beta_F}{\sqrt{SE_M^2 + SE_F^2 - 2\rho SE_M SE_F}} \right|$$

where $\beta_M$ and $\beta_F$ are estimated effect sizes obtained from sex-stratified

GWAS, $SE_M$ and $SE_F$ are sex-specific standard errors, and $\rho$ is the between-sex rank

correlation among genome-wide LD-pruned loci. Loci with elevated values of $|t|$ in observed

relative to permuted data denote candidate loci with sex-differential effects on LRS.

*Statistical comparisons of null and observed distributions*

Null distributions for each metric of sex differences in selection (*i.e.*, adult $\hat{F}_{ST}$, $\hat{\mathcal{L}}_{ST}$,

reproductive $\hat{F}_{ST}$, $|t|$, and gametic $\hat{F}_{ST}$) have been theoretically derived (for the $\hat{F}_{ST}$ metrics; see

*SI Appendix*, Section A) and/or obtained empirically through permutation (all five metrics).

Empirical null distributions were generated as follows. For adult $\hat{F}_{ST}$, gametic $\hat{F}_{ST}$ and $\hat{\mathcal{L}}_{ST}$, we

performed a single permutation of female and male labels and re-calculated the statistic in the

permuted data. For reproductive $\hat{F}_{ST}$ and $|t|$, we performed a single permutation of LRS values

within each sex—without permuting sex—and re-calculated the statistic in the permuted data.

Permuting LRS without permuting sex allows allele frequencies to differ between sexes (as

would happen if, for example, sex-differential viability selection is occurring among juveniles)

while randomising effects of genotype on LRS (which ensures that sex-differential selection

on LRS cannot contribute to the empirical null). Performing a single permutation for each

metric was sufficient for our purposes because we were focussed on testing a cumulative signal

of selection across loci, rather than establishing statistical significance at the single-locus level.

To test for elevations of each metric relative to the (theoretical or empirical) nulls, we

performed Wilcoxon Rank-Sum and Kolmogorov-Smirnov tests. These tests assess differences

in the median and distribution of the observed and null data, respectively. As a complementary

way of comparing observed and null data, we quantified enrichment of observed values in the

top 1% of each null using a $\chi^2$ test. Finally, we estimated the difference between the mean

value of the metric in the observed data and the mean value of the metric in each null, obtaining

95% confidence intervals and empirical p-values through bootstrapping (1,000 replicates;

where each replicate consists of the set of relevant genotyped or imputed SNPs, sampled with

replacement).

**Associations between metrics of sex differences in selection and MAF**

To test for associations between metrics of sex differences in selection and MAF, we performed

a Spearman's rank correlation between each metric and MAF. We also tested whether the

relationship between metrics of sex differences in selection and MAF was more pronounced in

the observed data than in the (theoretical or empirical) nulls by estimating the difference

between correlations in the observed data and correlations in the null data among 1,000

bootstrap replicates (as above), thereby generating 95% confidence intervals and empirical p-

values.

**Functional analyses**

Following research on candidate locally adapted loci [83–85], we tested whether loci exhibiting

elevated values of each metric of sex-differential selection were disproportionately situated in

putatively functional regions of the genome. We categorised SNPs as either intergenic or non-

intergenic based on annotations obtained with SnpEff [86]. We then fitted a logistic regression

model to our data, with annotation (genic/intergenic) as the binary response variable and the

metric of sex differences in selection under consideration as an independent variable. We also

examined whether associations between metrics of sex differences in selection and genic status

were more pronounced in the observed data than under (theoretical or empirical) nulls by

calculating the difference between the regression coefficients in the observed and null data

among 1,000 bootstrap replicates (as above).

We compared our five metrics to previously-documented GWAS hits from Neale

laboratory's analyses of all UK Biobank traits [68]. Briefly, we compared the average value of

the focal metric (*e.g.*, adult $\hat{F}_{ST}$ or $|t|$) between loci that were and were not associated ($\alpha = 10^-$

$^4$) with the focal phenotype (n = 43 traits) using a Mann-Whitney test, and then FDR-corrected

the resulting p-values. These analyses were performed on LD-pruned SNPs to reduce pseudo-

replication due to LD between loci. Analyses are fully documented (including code and results)

at https://lukeholman.github.io/ukbb_sex_fst.

**Quantifying signals of long-term balancing selection**

*Allele ages*

If candidate SA variants experience sufficiently strong and sustained balancing selection

relative to the countervailing effects of genetic drift, we expect them to be older than the

genome-wide average [69]. We used the Atlas of Variant Age database to obtain allele age

estimates for genome-wide variants [55]. Estimates of allele age in this database apply to the non-

reference (*i.e.*, alternative) allele and are derived from coalescent modelling of the time to the

most recent common ancestor using the "Genealogical Estimation of Variant Age" method (see

[55] for details). Estimates of allele age make use of genomic data from: (*i*) the 1000 Genomes

Project; (*ii*) the Simons Genome Diversity Project; (*iii*) both datasets combined. For each site

in the UK Biobank, we obtained the median estimate of allele age from the combined dataset

(when available), from the 1000 Genomes Project, or the Simons Genome Diversity Project

(when neither alternative estimate was available).

*Between-population $F_{ST}$*

If candidate SA variants experience sufficiently strong balancing selection maintaining a fixed

polymorphic equilibrium, they should exhibit lower-than-average allele frequency differences

*between* populations [69]. We obtained allele frequency data from four non-European populations

from the 1000 Genomes Project: Southern Han Chinese (CHS, N=105); Yoruba Nigerians

(YRI, N=108); Puerto Ricans (PUR, N=104) and Gujarati Indians (GIH, N=103). For each

pairwise combination of populations, we estimated between-population $\hat{F}_{ST}$, as:

$$\hat{F}_{ST} = \frac{(\hat{p}_1 - \hat{p}_2)^2}{4\bar{p}(1 - \bar{p})}$$

where $\hat{p}_1$ and $\hat{p}_2$ are allele frequency estimates in the relevant pair of populations, and $\bar{p} =$

$(\hat{p}_1 + \hat{p}_2)/2$.

*Previous candidates for balancing selection*

If candidate SA variants experience strong balancing selection, they should disproportionately

co-occur with previously identified candidates for balancing selection. We used three

independent sets of candidate sites for balancing selection to investigate this possibility [57–59]:

(*i*) the dataset of Andrés et al. [57], which consists of 64 genes exhibiting elevated polymorphism

(as determined using the Hudson-Kreitman-Aguadé test) and/or intermediate-frequency alleles

across 19 African-American or 20 European-American individuals; (*ii*) the dataset of

DeGiorgio et al. [59], which consists of 400 candidate genes exhibiting elevated $T_1$ or $T_2$ statistics

among 9 European (CEU) and 9 African (YRI) individuals. $T_1$ or $T_2$ statistics quantify the

likelihood that a genomic region exhibits levels of neutral polymorphism that are consistent

with a linked balanced polymorphism; (*iii*) the dataset of Bitarello et al. [58], which consists of

1859 candidate genes exhibiting elevated values of "Non-Central Deviation" (NCD) statistics.

NCD statistics also quantify the likelihood that given genomic regions are situated nearby a

balanced polymorphism, using polymorphism data from 50 random individuals from two

African (YRI; LWK) and European (GBR; TSI) populations and divergence data from a

chimpanzee outgroup.

We assigned each site in the UK Biobank dataset to a gene using SnpEff [86] and

categorised sites as candidates or non-candidates for balancing selection based on whether they

were annotated as belonging to a candidate or non-candidate in each of the three

aforementioned datasets.

*Statistical associations between metrics of sex-differential selection and balancing selection*

To test whether signals of sex differences in selection were associated with signals of balancing

selection, we performed Spearman's rank correlations between alternative allele age (scaled

by alternative allele frequency in the UK Biobank, to control for ascertainment bias) and each

metric of sex differences in selection. For between-population $\hat{F}_{ST}$, we performed multiple

linear regressions, with metric of sex differences in selection as the independent variable and

MAF in the UK Biobank as a fixed-effect covariate (to control for ascertainment bias). For

previous candidates for balancing selection, we performed multiple logistic regressions, where

candidate/non-candidate status was treated as a binary response variable, metric of sex

differences in selection as the independent variable, and UK Biobank MAF as a fixed-effect

covariate. We also tested whether associations between metrics of balancing selection and sex

differences in selection were more pronounced in the observed data than under (theoretical or

empirical) null. This was done by calculating the difference between the summary statistics

(*i.e.*, correlation or regression coefficients, as outlined above) in the observed and null data

among 1,000 bootstrap replicates.

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## Author contributions

Conceptualization: FR, LH, TC; Methodology: FR, LH, TC; Investigation: FR, LH, TC; Visualization: FR, LH, TC; Funding acquisition: TC; Project administration: FR, TC; Supervision: FR, LH, TC; Writing – original draft: FR, TC; Writing – review & editing: FR, LH, TC.

## Competing Interests

Authors declare no competing interests.

## Data accessibility

Within the restrictions of the UK Biobank MTA agreement, metadata will be made available in the Supplementary Materials. Further metadata will be made available on public data sharing platforms, and code will be made available on public github repositories upon publication (/filruzicka/polygenic_SA_selection_in_the_UK_biobank/ and /lukeholman/ukbb_sex_fst/).

**Figure 1. Partitioning signals of sex differences in selection among fitness components.** A pair of autosomal alleles at a locus are represented by black and white dots, representing male-beneficial and female-beneficial alleles, respectively; $\hat{p}_f$, $\hat{p}_m$, $\hat{p}'_f$, and $\hat{p}'_m$ depict sex-specific frequency estimates for a given allele at different stages of the life cycle (see main text for details). Autosomal allele frequencies are equalised between sexes at fertilisation (left box; females, top; males, bottom), resulting in negligible allele frequency differentiation at this stage of the life cycle. Differentiation between sexes can arise in the sample of adults (middle box) due to sex differences in viability selection among juveniles (orange arrow), and in the projected gametes (right box) due to sex differences in lifetime reproductive success (LRS) among adults (green arrow). Data on sex-specific allele frequencies and LRS thus allow the estimation of sex-differential effects of genetic variants on each fitness component (including overall fitness; purple arrow), despite the absence of allele frequency data among zygotes (left box) and gametes (right box), which are inferred and not directly observed.

**Figure 2. Polygenic signals of SA selection: inflation in $\widehat{F}_{ST}$ metrics relative to their nulls.**

**A-C.** Proportion of sites (coloured, observed; grey, permuted) falling into each of 100 quantiles of the theoretical null distributions of adult $\widehat{F}_{ST}$ (A), reproductive $\widehat{F}_{ST}$ (B) and gametic $\widehat{F}_{ST}$ (C). Theoretical null data (*x*-axes) were generated by simulating $\widehat{F}_{ST}$ values (nSNPs = 544,635) from the relevant theoretical null distributions (*i.e.*, eqs. [3a-c] for adult, reproductive and gametic $\widehat{F}_{ST}$, respectively). In the absence of sex differences in selection, approximately 1% of SNPs should fall into each quantile of the relevant theoretical null (dashed line). **D-F.** Difference between the mean of each metric (adult, reproductive and gametic $\widehat{F}_{ST}$, respectively) in observed and empirical null data (coloured histograms) and in observed and theoretical null data (white histograms), across 1,000 bootstrap replicates. Vertical line intersects zero (no difference between observed and null data). Differences are greater than zero across comparisons and metrics for all bootstrap replicates, so all p-values are p<0.001.

**Figure 3. Polygenic signals of SA selection: positive associations between $\widehat{F}_{ST}$ metrics and**

**MAF. A-C**. Mean MAF (coloured, observed; grey, permuted; black, theoretical) among 100

quantiles of adult $\widehat{F}_{ST}$ (D), reproductive $\widehat{F}_{ST}$ (E) and gametic $\widehat{F}_{ST}$ (F). Quantiles for theoretical

null data were obtained as in Fig. 2A-C; quantiles for observed and permuted data were

obtained from observed and permuted $\widehat{F}_{ST}$ distributions for each respective metric. **D-F.**

Difference between the Spearman's rank correlation in the observed and empirical null data

(coloured histograms) and between observed and theoretical null data (white histograms),

across 1,000 bootstrap replicates, where the correlation is between each $\widehat{F}_{ST}$ metric (adult,

reproductive and gametic $\widehat{F}_{ST}$, respectively) and MAF. Vertical line intersects zero (no

difference between observed and null data). Differences are greater than zero across

comparisons and metrics for all bootstrap replicates, so all p-values are p<0.001.

**Figure 4. Candidate SA polymorphisms are more likely to be functional and contribute to trait variation. A-C.** Genic enrichment (coloured, observed; grey, permuted; black, theoretical) in each of 100 quantiles of adult $\hat{F}_{ST}$ (A), reproductive $\hat{F}_{ST}$ (B) and gametic $\hat{F}_{ST}$ (C). Quantiles for theoretical null data, permuted data and observed data were obtained as in Fig. 3A-C. Genic enrichment is defined as the proportion of sites in a given quantile that are genic divided by the proportion of all sites that are genic. Loess curves (±SE) are presented for visual emphasis. **D.** Relationships between five metrics of sex-differential selection and candidate loci for various UK Biobank phenotypes (as analysed by the Neale laboratory), using an LD-pruned set of imputed SNPs. Each tile compares the mean value of the relevant metric of sex-differential selection between variants that are associated and not associated with the

focal phenotype, with colours denoting the ratio of means (with ratios >1 indicating *e.g.* higher

$\hat{F}_{ST}$ among associated than non-associated variants), and statistical significance assessed using

a Mann-Whitney test (*, FDR-adjusted p<0.05; ~, unadjusted p<0.05).

**Figure 5. No evidence that candidate SA polymorphisms are older than average.** Mean

age of the alternative (*i.e.*, non-reference) allele (coloured, observed; grey, permuted; black,

theoretical) across 100 quantiles of adult $\hat{F}_{ST}$ (A), reproductive $\hat{F}_{ST}$ (B) and gametic $\hat{F}_{ST}$ (C).

Quantiles for theoretical null data, permuted data and observed data were obtained as in Fig.

3A-C. All panels correct for ascertainment bias of alternative allele frequencies. For

visualisation purposes, this was done by averaging, in each $\hat{F}_{ST}$ quantile, mean allele age across

20 quantiles of alternative allele frequency in the UK Biobank (such that alternative allele

frequency is approximately equal across $\hat{F}_{ST}$ quantiles).

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