Destabilization of CAR T-cell treatment efficacy in the presence of dexamethasone

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Abstract

Chimeric antigen receptor (CAR) T-cell therapy is potentially an effective targeted immunotherapy for glioblastoma, yet there is presently little known about the efficacy of CAR T-cell treatment when combined with the widely used anti-inflammatory and immunosuppressant glucocorticoid, Dexamethasone. Here we present a mathematical model-based analysis of three patient-derived glioblastoma cell lines treated *in vitro* with CAR T-cells and Dexamethasone. Advanced *in vitro* experimental cell killing assay technologies allow for highly resolved temporal dynamics of tumor cells treated with CAR T-cells and Dexamethone, making this a valuable model system for studying the rich dynamics of nonlinear biological processes with translational applications. We model the system as a non-autonomous, two-species predator-prey interaction of tumor cells and CAR T-cells, with explicit time-dependence in the clearance rate of Dexamethasone. Using time as a bifurcation parameter, we show that (1) the presence of Dexamethasone destabilizes coexistence equilibria between CAR T-cells and tumor cells and (2) as Dexamethasone is cleared from the system, a stable coexistence equilibrium returns in the form of a Hopf bifurcation. With the model fit to experimental data, we demonstrate that high concentrations of Dexamethasone antagonizes CAR T-cell efficacy by exhausting, or reducing the activity of CAR T-cells, and by promoting tumor cell growth. Finally, we identify a critical threshold in the ratio of CAR T-cell death to CAR T-cell proliferation rates that predicts eventual treatment success or failure that may be used to guide the dose and timing of CAR T-cell therapy in the presence of Dexamethasone in patients.

Author summary

Bioengineering and gene-editing technologies have paved the way for advance immunotherapies that can target patient-specific tumor cells. One of these therapies, chimeric antigen receptor (CAR) T-cell therapy has recently shown promise in treating

glioblastoma, an aggressive brain cancer often with poor patient prognosis. Dexamethasone is a commonly prescribed anti-inflammatory medication due to the health complications of tumor associated swelling in the brain. However, the immunosuppressant effects of Dexamethasone on the immunotherapeutic CAR T-cells are not well understood. To address this issue, we use mathematical modeling to study *in vitro* dynamics of Dexamethasone and CAR T-cells in three patient-derived glioblastoma cell lines. We find that in each cell line studied there is a threshold of tolerable Dexamethasone concentration. Below this threshold, CAR T-cells are successful at eliminating the cancer cells, while above this threshold, Dexamethasone critically inhibits CAR T-cell efficacy. Our modeling suggests that in the presence of Dexamethasone reduced CAR T-cell efficacy, or increased exhaustion, can occur and result in CAR T-cell treatment failure.

Introduction

Chimeric antigen receptor (CAR) T-cell therapy is a novel immunotherapy for the treatment of cancer. While initially demonstrating efficacy in haematologic cancers, CAR T-cell therapy also has potential for treating solid tissue tumours, including the highly aggressive brain cancer glioblastoma (GBM) [1–4]. To further develop CAR T-cell therapy for the clinical treatment of GBM, it is essential to understand how CAR T-cells interact with commonly administered medications which may impact CAR T-cell efficacy. The anti-inflammatory synthetic glucocorticoid Dexamethasone (Dex) is a ubiquitous medication for patients with GBM due to the propensity for brain tissue inflammation that accompanies tumor development in GBM, and the severity of the associated medical complications that accompanies inflammation. To study the effects of Dex on CAR T-cell proliferation, killing, and exhaustion, we extend mathematical models developed by us and others to study highly resolved temporal *in vitro* dynamics of patient-derived GBM cell lines under various concentrations of Dexamethasone and CAR T-cells [5].

Glioblastoma is a highly aggressive and unfortunately common form of primary malignant brain tumor. It is noted for its high rates of proliferation and poor survival following chemotherapy, radiotherapy, and surgical resection. The recent development of adoptive CAR T-cell therapy using patient-specific T cells has shown promise in treating GBM targeting the glioma antigen IL13Rα2 [1]. In this study we examine the treatment response to CAR T-cell therapy of three human derived primary brain tumor (PBT) cell lines with high levels of expression of the IL13Rα2 antigen. These treatment experiments are conducted with varying concentrations of Dexamethasone and effector-to-target (E:T) ratios of CAR T-cells to examine the effects of combination therapy.

In a clinical context, patients diagnosed with GBM are commonly prescribed the glucocorticoid steroid Dexamethasone (Dex) to manage inflammation surrounding the site of tumor burden. Importantly, recent work has demonstrated contradictory outcomes in the use of Dex for treating GBM. Specifically, the anti- and pro-proliferative effects of Dex on GBM have been shown to depend on cell type [6]. Furthermore, a previous proof-of-concept experiment demonstrated the ability of high Dex doses (5 mg/kg) to compromise successful CAR T-cell therapy in mice with xenograft GBM tumors, whereas lower doses (0.2-1 mg/kg) had limited effect on *in vivo* antitumor potency [7]. This data suggests a threshold at which Dex negatively impacts CAR T-cell therapy and reinforces the importance of mathematical modeling to infer and understand how Dex influences CAR T-cell therapy efficacy for GBM.

Mathematical modeling has demonstrated value in quantitatively characterizing the interactions between GBM cells and CAR T-cells. Previous work validated this

approach in which the principle components necessary for accurate predictions were identified as: rates of GBM proliferation and cell killing, and CAR T-cell proliferation, exhaustion, and death. These factors were combined into a predator-prey system called CARRGO: Chimeric Antigen Receptor T-cell treatment Response in GliOma [5]. Here we extend this work by incorporating the Dex concentration as a new model parameter, and assume that it follows exponentially depleting pharmacokinetics. We posit that Dex has directly measurable effects on GBM proliferation and CAR T-cell death, and indirectly measurable effects on all other model parameters. We use our extended model to investigate the consequences of combination CAR T-cell and Dex therapy on three *in vitro* GBM cell lines. We establish an experimental protocol that measures treatment effects on GBM cell populations while co-varying initial CAR T-cell populations and Dex concentrations.

Materials and methods

Cell lines

Primary brain tumor GBM cell lines were derived as described in [1,8]. All three cell lines come from male donors ages 43, 52, and 59 years old. As this study was focused on the interaction between Dex and CAR T-cells, cell lines were either selected based on espression of IL13Rα2 (PBT030) or engineered to express high levels of IL13Rα2 (greater than 70%) by lentiviral transduction (PBT128 and PBT138) as described in [1,5,8]. For IL13Rα2-targeted CAR T-cell lines, healthy donor CD62 L+ CD45RO+ central memory T-cells were lentivirally transduced to express a second-generation of IL13Rα2-targeting CAR as described in [7]. Summary information regarding cell lines can be found in Table 1.

Table 1. Experimental conditions.

Patient-derived tumor cell line	CAR T-cells	Initial number of tumor cells	Effector to Target (E:T) ratio	Dex concentrations (μg/ml)
PBT030	IL13Rα2 BBζ	10K-20K	1:4, 1:8, 1:20	0, 10^{-4}, 10^{-3}, 10^{-2}, 10^{-1}, 1
PBT128	IL13Rα2 BBζ	10K-20K	1:4, 1:8, 1:20	0, 10^{-4}, 10^{-3}, 10^{-2}, 10^{-1}, 1
PBT138	IL13Rα2 BBζ	10K-20K	1:4, 1:8, 1:20	0, 10^{-4}, 10^{-3}, 10^{-2}, 10^{-1}, 1

Patient-derived brain tumor (PBT) lines, CAR T-cell lines, initial number of cells, effector to target ratios, and Dex concentrations used in *in vitro* experiments.

Experimental conditions

Cancer cell growth and treatment response was monitored with the xCELLigence cell analyzer system [9]. By correlating changes in electrical impedance with number of tumor cells adhered to electrode plates, a measurement of the cell population is reported every 15 minutes. Cell populations of both the tumor cells and CAR T-cells are reported in the non-dimensional units of Cell Index (CI), where 1 CI $\approx$ 10K cells. Previous work has demonstrated that cell index and cell number are strongly correlated [10,11], including in the presence of CAR T-cell treatment [5]. Flow cytometry was used at the experiment endpoint to examine the validity of the cell index-cell number correlation in the presence of Dex, as well as count the non-adherent CAR T-cells. Tumor cells were seeded at 10K-20K cells per well and left either untreated, treated with only Dex, treated with only CAR T-cells, or treated with both Dex and CAR T-cells. All control and treatment conditions were conducted in duplicate, with treatments occurring 24

hours after seeding and followed for 6-8 days (144-192 hrs). CAR T-cell treatments were performed with E:T ratios of 1:4, 1:8, and 1:20. Dex treatment concentrations used were $10^{-4}, 10^{-3}, 10^{-2}, 10^{-1}$, and 1 μg/ml. The experiment design is diagrammed in Fig 1(**a**), and treatment conditions are presented in Table 1. A follow-up experiment was conducted to examine the potential for Dex-induced changes to tumor cell morphology using the IncuCyte live cell imaging system (Fig 2). In this second experiment, E:T ratios of 1:20, 1:40, and 1:80 were used as the CAR T-cells had been engineered to be more efficacious. All other experimental conditions were held constant. See `https://github.com/alexbbrummer/CARRGODEX` for all experimental data.

Fig 1. Diagram of *in vitro* experiments and mathematical model. (**a**) Experiments were conducted using a 96-well plate xCELLigence cell killing assay, where tumor cell adherence modulates electrical impedance. Dexamethasone and CAR T-cells were added simultaneously 24 hours following tumor cell plating, with observation proceeding for 6-8 days (144-192 hrs). CAR T-cells were counted at the experiment endpoint with flow cytometry analysis (FACS). (**b**) A mathematical model similar to a predator-prey system is used to model tumor cell growth, death, and interactions between tumor cells, CAR T-cells, and Dex. The compartmental model is translated into the system of equations in Eqs. (1)-(3).

Mathematical model

To model the interactions between the tumor cells, the CAR T-cells, and Dexamethasone, we extend the predator-prey inspired CARRGO model from Sahoo et al. [5]. We use the principle of mass-action to model the effect of Dex on tumor and CAR T-cell populations, without an explicit assumption of a positive or negative effect of Dex on those cell populations. A compartmental representation of the model is presented in Fig 1(**b**), and all model variables and parameters are presented in Table 2. The tumor cell and CAR T-cell populations are modeled here in units of cell index (CI), a strongly correlated indicator of cell number that is produced by the xCelligence cell

Fig 2. Incucyte live cell imaging of PBT138.eGFP cells 100 hours following treatment shows Dex-induced reduction in CAR T-cell efficacy. (a) No Dex or CAR T-cell treatment (PBT138 culture). Visible are tumor cells of different morphology round (red arrows) and elongated (blue arrow), representing heterogeneous patient-derived glioma cell culture. (b) CAR T-cell only treatment with effector:target cell (E:T) ratio of 1:20. Visible are CAR T-cell aggregates in phase (white circles). (c) Combined CAR T-cell (E:T = 1:20) and Dex (0.1 ng/ml) treatment. CAR T-cell aggregates still visible (white circles) in addition to slight increase in existing tumor cells. (d) Combined CAR T-cell (E:T = 1:20) and Dex (1 μg/ml) treatment showing lack of CAR T-cell aggregates and some increase in tumor cell numbers. White scale bars represent 200 μm.

killing assay measurement system [5, 10, 11]. Expressing the compartmental model as a system of equations,

Table 2. Mathematical model parameters.

Parameter	Description	Unit
ρ	tumor cell net growth rate	day^{-1}
K	carrying capacity	CI
κ_1	tumor killing rate	day^{-1}CI^{-1}
κ_2	net rate of proliferation and exhaustion of CAR T-cells when stimulated by cancer cells	day^{-1}CI^{-1}
θ	CAR T-cell death rate (persistence)	day^{-1}
c_0	effect of Dex on tumor growth	day^{-1}
c_3	effect of Dex on CAR T-cell death	day^{-1}
σ	half-life of Dex	day^{-1}

$$\frac{dx}{dt} = \rho x - \frac{\rho}{K}x^2 - \kappa_1 xy - c_0 Dx \tag{1}$$

$$\frac{dy}{dt} = \kappa_2 xy - \theta y - c_3 Dy \tag{2}$$

$$\frac{dD}{dt} = -\sigma D, \tag{3}$$

where x is the tumor cell population, y is the CAR T-cell population, and D is the concentration of Dexamethasone. Although cell populations are often modelled in terms

of cell number, here we use cell index (CI) to link model parameters with the
experimental xCelligence platform readout data. As determined in previous studies, cell
index and cell number are strongly correlated, with a cell index of one equal to
approximately 10,000 cells.

Pharmacokinetic studies report the plasma half-life of Dex as being approximately
200 minutes, resulting in $\sigma = \ln(2)/3.\bar{3}$ hr^{-1} [12,13]. We do not explicitly model the
mechanism by which Dex is cleared from the system, which can be through cell uptake,
evaporation, or absorption into the culture media. Here we simply assume the
elimination of Dex is equivalent to the Dex plasma half-life. While the Dex interaction
terms are explicitly subtracted from the population growth rates, we make no
presumptions on the signs of the interaction constants, c_0 and c_3. This has the effect of
allowing for both scenarios where Dex can be either anti-proliferative (i.e. $c_0, c_3 < 0$) or
pro-proliferative (i.e. $c_0, c_3 > 0$) to either the CAR T-cells or tumor growth [6,14].

We next convert this three-species, autonomous population model into a two-species,
non-autonomous model. We formulate the model this way to study how the
concentration of Dex influences the predicted long-term stability of the CAR T-cell and
tumor cell populations, which essentially considers time as a bifurcation parameter. To
perform this conversion, note that Eq. (3) can be solved separately as $D(t) = D_0 e^{-\sigma t}$.
Upon substitution for $D(t)$, we arrive at the following system of equations

$$\frac{dx}{dt} = \left(\rho - c_0 e^{-\sigma t}\right) x \left[1 - \frac{\rho x}{\left(\rho - c_0 e^{-\sigma t}\right) K}\right] - \kappa_1 xy \tag{4}$$

$$\frac{dy}{dt} = \kappa_2 xy - \left(\theta + c_3 e^{-\sigma t}\right) y \tag{5}$$

where we factored terms to reflect the anti/pro-proliferative potential of Dex, and
re-scaled the constants c_0 and c_3. Letting $\rho(t) = \rho - c_0 e^{-\sigma t}$, $K(t) = \rho(t)K/\rho$, and
$\theta(t) = \theta + c_3 e^{-\sigma t}$, our model takes the simplified form of

$$\frac{dx}{dt} = \rho(t)x \left(1 - \frac{x}{K(t)}\right) - \kappa_1 xy \tag{6}$$

$$\frac{dy}{dt} = \kappa_2 xy - \theta(t)y \tag{7}$$

which is reminiscent of the original CARRGO model [5]. The definitions of $\rho(t)$, $K(t)$,
and $\theta(t)$ demonstrate how the signs of the constants c_0 and c_3 can determine the
anti/pro-proliferative effect of Dex on the tumor cells and CAR T-cells. Specifically, if
$c_0 > 0$, then Dex is anti-proliferative to the tumor cells, lowering the effective growth
rate $\rho(t)$ and carrying capacity $K(t)$. If $c_0 < 0$, then Dex is pro-proliferative to the
tumor cells, raising the effective growth rate $\rho(t)$ and carrying capacity $K(t)$. On the
other hand, if $c_3 > 0$, then Dex is anti-proliferative to the CAR T-cells, increasing the
effective death rate $\theta(t)$. If $c_3 < 0$, then Dex is pro-proliferative to the CAR T-cells,
decreasing the effective death rate $\theta(t)$.

Parameter estimation

The fitting procedure used to estimate model parameters consisted of a combination of
particle swarm optimization (PSO) and the Levenberg-Marquardt algorithm (LMA).
PSO is a stochastic global optimization procedure inspired by biological swarming [15].

PSO has been used recently for parameter estimation in a variety of initial value problems across cancer research and systems biology [16–19]. These optimization procedures were used to minimize the weighted sum-of-squares error between measured and predicted tumor cell and CAR T-cell populations. PSO was used first to determine rough estimates of model parameters. This was followed by use of LMA to fine-tune parameter values.

Although the mathematical model has 8 parameters, we show that the model in Eqs. (6)-(7) is structurally identifiable from the experimental data. This allows for explicit measurement and inference of all the parameters in the model, including c_0 and c_3, and thus the effects of Dex on the tumor cells and CAR T-cells independently. In particular, two replicates (wells) of tumor cells were grown untreated with CAR T-cells but with and without Dex treatments to independently identify the tumor growth rate, ρ, carrying capacity K, and the effect of Dex on the tumor growth rate and carrying capacity c_0. Additionally, two replicates of tumor cells treated with CAR T-cells were conducted with and without Dex. This allowed us to independently identify the tumor killing rate with and without Dex, κ_1, the CAR T-cell proliferation/exhaustion with and without Dex, κ_2, the CAR T-cell death rate θ, and the effect of Dex on the CAR T-cell death rate c_3. See Supplemental Information for identifiability analysis, and `https://github.com/alexbbrummer/CARRGODEX` for all experimental data and computational code to reproduce the model fitting, parameter estimates, and figures. All model fitting was performed using the programming language Python.

Stability analysis

With the simplified form of our CARRGO with Dex model in Eqs. (6)-(7), the equilibrium solutions are identified as $P_1 = (0,0)$, $P_2 = (K(t), 0)$, and $P_3 = \left(\frac{\theta(t)}{\kappa_2}, \frac{\rho(t)(K(t)\kappa_2 - \theta(t))}{K(t)\kappa_1\kappa_2}\right)$ where $(x, y) = $ (tumor cells, CAR T-cells). These solutions are referred to as 'Death', 'Tumor Proliferation', and 'Coexistence' respectively. Given the structure of the dynamical system in Eqs. (6)-(7), eigenvalue analysis shows that the 'Death' and 'Tumor Proliferation' equilibria are never stable solutions (see Supplemental Information). Interestingly, this does not preclude our ability to predict tumor death or proliferation. On the contrary, observed and measured tumor death and proliferation occur within the parameter space that defines the coexistence equilibrium. Careful examination of the coexistence equilibrium stability can elucidate this point.

In the 'Coexistence' scenario, the equilibrium is $P_3 = \left(\frac{\theta(t)}{\kappa_2}, \frac{\rho(t)(K(t)\kappa_2 - \theta(t))}{K(t)\kappa_1\kappa_2}\right)$. Importantly, the model parameters that determine the final tumor cell population are the ratio of the CAR T-cell death rate and the CAR T-cell proliferation/exhaustion after the Dex has cleared, θ/κ_2. Thus, if either CAR T-cell death is low with respect to CAR T-cell proliferation, or CAR T-cell proliferation is high with respect to death, then $\theta/\kappa_2 \approx 0$, and tumor death can occur as the coexistence equilibrium. We next examine how the conditions for stability depend on the model parameters, in particular the Dex concentration.

The eigenvalues of the Jacobian for the coexistence equilibrium are

$$\lambda_{\pm} = \frac{\rho(t)\theta(t)}{2\kappa_2 K(t)} \left\{ -1 \pm \left[1 + \frac{4\kappa_2 K(t)}{\rho(t)} \left(1 - \frac{\kappa_2 K(t)}{\theta(t)} \right) \right]^{1/2} \right\} \tag{8}$$

Recalling that $\rho(t) = \rho - c_0 e^{-\sigma t}$ and $K(t) = \frac{\rho - c_0 e^{-\sigma t}}{\rho} K$, then $\frac{K(t)}{\rho(t)} = \frac{K}{\rho}$. Substitution of the expressions for the time-dependent growth rate, carrying capacity, and death rate results in

$$\lambda_{\pm} = \underline{\frac{\rho\left(\theta + c_3 e^{-\sigma t}\right)}{2\kappa_2 K}} \left\{ -1 \pm \left[1 + \frac{4\kappa_2 K}{\rho}\underline{\left(1 - \frac{\kappa_2 K\left(\rho - c_0 e^{-\sigma t}\right)}{\rho\left(\theta + c_3 e^{-\sigma t}\right)}\right)} \right]^{1/2} \right\} \qquad (9)$$

In Eq. (9), the term underlined in blue determines oscillatory behavior, while the term underlined in red determines the stability of the oscillatory states (spiraling in, spiraling out, or as a fixed limit cycle). By convention, only the parameters characterising the effects of Dex on tumor growth and CAR T-cell death, c_0 and c_3, can take on negative values. Thus, after the Dex has cleared, any oscillatory coexistence state will be stable. This consequence highlights the value of our decision to model the system as non-autonomous. In the event that Dex is pro-proliferative to the CAR T-cells such that $c_3 < -\theta$, then there will always be at least one positive eigenvalue (with or without oscillations), and the equilibrium will be temporarily unstable until the Dex has sufficiently cleared the system.

To determine the condition for oscillatory states, we require non-zero imaginary components of the eigenvalues, $\Im(\lambda_{\pm}) \neq 0$, which results in the following condition

$$\left(\frac{\rho - c_0 e^{-\sigma t}}{\theta + c_3 e^{-\sigma t}}\right) > \frac{\rho}{\kappa_2 K} + \left(\frac{\rho}{2\kappa_2 K}\right)^2 \qquad (10)$$

In Eq. (10) we can see that the existence of oscillations about the coexistence equilibrium are again determined by the relative sizes of $\theta(t)$ and κ_2.

Results

Experimental results of this study demonstrate that high concentrations of Dexamethasone can attenuate tumor eradication even when CAR T-cell therapy would otherwise have been successful (Fig 2). This phenomenon was observed directly in cell line PBT128 (Fig 3), PBT138 (S1 Fig) and it can be inferred for cell line PBT030 between effector-to-target ratios 1:4 and 1:8 (S2 Fig and S3 Fig, respectively). A reduction in CAR T-cell efficacy is observed regardless of treatment success or failure at different effector-to-target ratios (E:T) for all three cell lines (Fig 4 and Supporting Information S1 Fig and S3 Fig). Importantly, our predator-prey model that incorporates Dex can predict these changes in CAR T-cell efficacy and connect them to key features of CAR T-cell function (e.g. proliferation, exhaustion, and death).

Our modeling identifies that Dex treatment destabilizes the coexistence equilibrium and forces the system into a new equilibrium state upon Dex clearance (Fig 5). We predict that this process is a result of a Dex-induced increase in CAR T-cell proliferation, $c_3 < -\theta$, followed by an increase in CAR T-cell death, θ increasing, and either a decrease or fixation of cancer cell stimulated proliferation of CAR T-cells, κ_2 decreasing or approx. constant. We interpret these combined effects as facilitating CAR T-cell exhaustion (Fig 6). These responses are manifest in a cycle of pseudo-progression, pseudo-regression, and a final stage of tumor progression. Importantly, we identify a threshold on the ratio of CAR T-cell death to CAR T-cell proliferation/exhaustion rates, ($\theta/\kappa_2 \approx 0.4$ CI), that appears to predict successful tumor eradication ($\theta/\kappa_2 < 0.4$ CI), or proliferation ($\theta/\kappa_2 > 0.4$ CI). We find that this threshold is valid across all three PBT cell lines, initial CAR T-cell populations, and Dex concentrations (Fig 7).

Fig 3. Graphs of measured and predicted (**a**) tumor cells, (**b**) CAR T-cells, and (**c**) Dex concentration over time for tumor cell line PBT128 with an initial effector-to-target ratio of 1:4. Temporal measurements of (**a**) tumor cells measured by xCelligence cell index (CI) values and (**b**) CAR T-cell levels with initial and final measurements represented by symbols, and CARRGO model predictions are represented by lines. Experimental measurements for the tumor cell population are down-sampled by 1/10 for clarity. Colors and symbol types represent different initial Dex concentrations (see top legend). The progression of the tumor cell curves as initial Dex concentration increases demonstrate the effect of Dex to reduce CAR T-cell efficacy.

Dexamethasone can promote tumor progression

Our experimental results suggest that Dex may disproportionately promote or enable early proliferation of both the tumor cells and CAR T-cells. Two possible mechanisms for this effect are: (1) a direct increase in tumor proliferation through changing cell morphology and reducing intracellular cytoplasm to create more space for tumor cells to proliferate and thus reduce cell contact inhibition [20]. However, our experimental results and modeling do not necessarily support this mechanism (Fig 2). The second, and more likely mechanism, is by reducing the efficacy of CAR T-cells which in our model corresponds to an increase in the CAR T-cell death parameter, θ, and a decrease in the CAR T-cell proliferation parameter, κ_2. In Fig 3 we see that final populations of tumor cells for line PBT128 increase as a function of increasing initial Dex concentration. Specifically, the system dynamics range from complete tumor cell death for initial Dex concentrations of 0.0 μg/ml, 1×10^{-4} μg/ml, 1×10^{-3} μg/ml, and 1×10^{-2} μg/ml to tumor progression for initial Dex concentrations of 1×10^{-1} μg/ml, and 1 μg/ml. We also see a noted decrease in initial CAR T-cell growth as the initial Dex concentration is increased.

The loss of CAR T-cell treatment efficacy as a result of Dex can be observed across

Fig 4. Time series of tumor cell populations for PBT128 across various CAR T-cell E:T ratios of 1:4 (**a**), 1:8 (**b**), and 1:20 (**c**). Colors and symbol types vary to reflect initial Dex concentrations (see top legend). Tumor persistence is seen to increase due to increasing initial Dex concentration regardless of the different starting CAR T-cell E:T ratios. Symbols represent measured data, while lines represent CARRGO model predictions. Experimental measurements for the tumor cell population are down-sampled by 1/10 for clarity.

all CAR T-cell E:T ratios. In Fig 4 we see how increasing the initial Dex concentration continually increases the final tumor population when compared to the Dex control for the PBT128 cell line. Interestingly, the extent to which pseudo-regression occurs for the medium and low dose CAR T-cell groups is noticeably diminished as Dex increases.

Also notable are the cases of medium initial CAR T-cells (E:T = 1:8) and high initial Dex (0.1 μg/ml -1 μg/ml), where the final tumor cell population has surpassed the initial pseudo-progression peak. Flow cytometry measurements of these high Dex concentrations in the absence of CAR T-cell treatment for PBT128 demonstrate that the xCelligence Cell Index metric begins to overestimate tumor cell number (S4 Fig). This effect was also observed in PBT030 (again in the absence of CAR T-cells), but not PBT138, and led to our omission of the Dex-only treatments in this analysis.

Dexamethasone induced destablization of coexistence

Analysis of the coexistence eigenvalue stability helps to elucidate the effect that Dex has on the system dynamics. Fig 5 presents bifurcation diagrams for two different experimental scenarios with the same initial CAR T-cell population but different initial Dex concentrations. Fig 5**a** shows the coexistence eigenvalues as functions of time for the experimental conditions of high initial CAR T-cells (E:T = 1:4) and a low initial

Dex concentration of 1×10^{-3} μg/ml in which productive tumor cell death occurred. Fig 5**b** shows the coexistence eigenvalues as functions of time for the experimental conditions of high initial CAR T-cells (E:T = 1:4) and a high initial Dex concentration of 1×10^{-1} μg/ml and corresponds to tumor cell progression. To illustrate how the time-dependence of the eigenvalues influences the system dynamics, streamplots of Eqs. (6)-(7) are presented as insets for each experimental scenario.

In the scenario with an initial Dex concentration of 1×10^{-3} μg/ml (Fig 5 **a**), the coexistence equilibrium begins as a stable spiral for the duration of the Dex clearance and the remainder of the experiment. As the Dex clears, the real and imaginary components of the eigenvalues decrease in magnitude. These temporal changes in the eigenvalues shift the location and shape of the system trajectory, as shown in the figure inset. In particular, during the times $t_1 = 32$ hrs and $t_2 = 40$ hrs, as the Dex is still clearing, the system is predicted and observed to oscillate about the changing coexistence equilibrium P_3. At the times t_1 and t_2 real component of the eigenvalue is large enough to facilitate in-spiraling. By $t_3 = 60$ hrs, effectively all of the Dex has cleared, and the phase space trajectory is soon to pass through a zero in tumor cell population, terminating the dynamics.

In the scenario with a higher initial Dex concentration of 1×10^{-1} μg/ml (Fig 5 **b**), the coexistence equilibrium begins as an unstable fixed point (times $t_1 = 32$ hrs and $t_2 = 38$ hrs). After twice the half-life of Dex (≈ 7 hrs), a Hopf bifurcation occurs and the system transitions through a limit cycle (time $t \approx 40$ hrs) and into a stable spiral (time $t_3 = 42$ hrs). When the system is in an unstable state, the instantaneous trajectory predicted by Eqs. (6)-(7) show pseudo-progressive growth. As in the previous scenario with 1×10^{-3} μg/ml of Dex, the system enters a stable spiral by the time all of the Dex has cleared ($t_3 = 60$ hrs) that would result in zero tumor cells. However, in this scenario, once the Dex has fully cleared the system the coexistence eigenvalue is a stable spiral that importantly no longer passes through a zero in the tumor cell population.

Tumor cell killing and CAR T-cell exhaustion

To examine the effect of Dex on total tumor cell killing we compare tumor cell growth trajectories for CAR T-cell only treatment, and combined CAR T-cell and Dex treatments in Fig 6. For the combined treatment scenarios, we focus on experimental conditions at the threshold of treatment success and treatment failure, and along a Dex-gradient of treatment failure (Fig 6 **a**, **c**, and **e** for cell lines PBT030, PBT128, and PBT138, respectively). Accompanying each growth trajectory are barplots of the inferred model parameters (Fig 6 **b**, **d**, and **f**), which help to identify how Dex interacts separately with the tumor cells and CAR T-cells. We chose not to examine Dex only treatments as flow cytometry measurements indicated a loss in the strength of the correlation between xCelligence cell index and flow cytometry-measured cell number in these treatment scenarios [10, 11]. The correlation was observed to be maintained in combined treatment scenarios, with correlation coefficients of = 0.97 in cell line PBT138, 0.70 in cell line PBT128, and 0.30 in cell line PBT030 (S1 Supporting Information).

From the perspective of our mathematical model, the effect of Dex on the CAR T-cells is to reduce efficacy through inducing exhaustion. In going from treatment success to failure, the CAR T-cell death rate, θ, increases and for cell lines PBT030 and PBT138 the tumor cell killing, κ_1, decreases while CAR T-cell proliferation, κ_2, remains fixed, while in cell line PBT128 the tumor cell killing remains fixed while CAR T-cell proliferation, κ_2, decreases. These shifts dramatically increase the predicted coexistence equilibrium for the tumor cell population, given as θ/κ_2. Next is the effect of Dex on the CAR T-cell death rate, c_3, which switches from positive to negative between success and failure across all cell lines. This shift suggests that during treatment success there is high turnover of CAR T-cells due to the Dex-induced increase in CAR T-cell death and

Fig 5. Stability analysis of coexistence equilibria for CARRGO model with Dex under the experimental conditions of tumor cell line PBT128 with an initial CAR T-cell E:T ratio of 1:4. Initial Dex concentrations are 1×10^{-3} μg/ml (**a**) and 1×10^{-1} μg/ml (**b**). Bifurcation diagrams (main graphs) demonstrate how Dex modulates the temporal dynamics of the coexistence equilibria. Inset graphs show phase space diagrams demonstrating transient state of coexistence equilibria as time evolves and Dex clears. In (**a**) the initial Dex concentration of 1×10^{-3} μg/ml is too small to facilitate exhaustion of the CAR T-cells, thus the coexistence equilibrium is a stable spiral. However, the equilibrium position is still seen to translate through the phase space, and the predicted trajectory deform, while Dex is clearing. In (**b**) the initial Dex concentration of 1×10^{-1} μg/ml is sufficiently large enough to facilitate exhaustion of the CAR T-cells, thus the coexistence equilibrium is an unstable fixed point (dashed lines) until a sufficient level of Dex has cleared and the system returns to a stable spiral (solid lines). Unlike the lower initial Dex concentration scenario in (**a**), the coexistence equilibrium has translated, and the predicted trajectory has narrowed, such that the tumor population no longer reaches a value of zero, resulting in tumor progression.

Fig 6. Comparison of tumor cell measurements and CARRGO model fits (**a**, **c**, and **e**), and CARRGO model parameters (**b**, **d**, and **f**) for CAR T-cell only treatments, and combination CAR T-cell and Dex treatments for each tumor cell line studied. For the combined treatment scenarios, we focus on experimental conditions at the threshold of treatment success and treatment failure, and along a Dex-gradient of increasing tumor progression. For PBT030 (**a**, **b**) the conditions at the threshold of treatment success are E:T = 1:4 and 1 μg/ml of Dex, and E:T = 1:8 and 10^{-4} μg/ml for treatment failure. For PBT128 (**c**, **d**) the conditions at the threshold of treatment success are E:T = 1:4 and 10^{-3}μg/ml of Dex, and E:T = 1:4 and 10^{-1} μg/ml for treatment failure. For PBT138 (**e**, **f**) the conditions at the threshold of treatment success are E:T = 1:20 and 10^{-4} μg/ml of Dex, and E:T = 1:20 and 10^{-3} μg/ml for treatment failure. Symbols represent average of two replicates, and error bars represent sample ranges. Note that experimental measurements presented are downsampled by 1/10 for clarity.

Fig 7. The ratio of CAR T-cell death (θ) to CAR T-cell proliferation/exhaustion (κ_2) rates predict CAR T-cell treatment success (tumor cell death) or failure (tumor cell progression). We observed that a ratio of $\theta/\kappa_2 \approx 0.4$ CI as the predicted final tumor cell population serves as a threshold for observed tumor progression or death. The threshold of $\theta/\kappa_2 \approx 0.4$ CI was consistent across all three tumor cell lines (denoted by color), CAR T cell E:T ratios (denoted by shape), and initial Dex concentrations (denoted by location along the horizontal axis). Conditions not shown are PBT030 with an E:T ratio of 1:20 which all resulted in tumor cell progression, PBT128 with an E:T ratio of 1:8 and 1:20 which all resulted in tumor cell progression, and PBT138 with E:T ratios of 1:8 and 1:4 which all resulted in tumor cell death.

the cancer cell stimulated CAR T-cell proliferation. After Dex clears, CAR T-cell death returns to a small rate resulting in treatment success. In the failure scenario Dex again promotes CAR T-cell growth, $c_3 < 0$, yet increases CAR T-cell exhaustion by reducing the size of κ_2. Our interpretation of these combined effects is that Dex results in CAR T-cell exhaustion.

Predicting treatment success or failure

Analysis of treatment success and failure across all experimental conditions identifies an essential threshold, T_0, for the predicted tumor cell equilibrium population. As shown in Fig 7, we observe an approximate threshold of $T_0 \approx 0.4$ CI such that for values of $\theta/\kappa_2 < T_0$, total tumor cell death occurs after a brief period of pseudo-progression. Alternatively, for values of $\theta/\kappa_2 > T_0$, tumor cell persistence occurs after pseudo-progression and pseudo-response. Importantly, for the cell lines PBT128 and PBT138, we can see a transition from treatment success to treatment failure at fixed levels of initial CAR T-cells (0.25CI for PBT128 and 0.05CI PBT138) and as initial Dex concentration increases from 10^{-2} to 10^{-1} μg/ml. For tumor cell line PBT030, the transition from treatment success to failure occurs primarily as a result of changes in the initial number of CAR T-cells administered, with E:T ratios of 1:4 resulting in success, and 1:8 resulting in failure.

Discussion

In this work we demonstrate how mathematical modeling can be leveraged to identify and quantify how the commonly used anti-inflammatory synthetic glucocorticoid Dexamethasone may undermine CAR T-cell treatment efficacy in glioblastoma.

In modeling this system, we chose to use a non-autonomous (explicit in time) approach in order to assess the dynamical stability of the system as a function of Dex concentration. By treating time as a bifurcation parameter, variations in system stability and predicted phase space trajectories can be visualized (Fig 5). This approach facilitates understanding of treatment success and failure due to an overabundance of Dex and in the context of stability analysis. Specifically, in scenarios where treatment succeeded, as in Fig 5($\mathbf{a}$), the coexistence equilibrium remained stable throughout the duration of Dex clearance. On the other hand, in scenarios where high levels of Dex led to treatment failure and tumor outgrowth, as in Fig 5($\mathbf{b}$), the coexistence equilibrium was initially unstable until sufficient Dex cleared from the system.

Insight gained from studying tumor-CAR T-cell dynamics can aid in understanding how Dex compromises CAR T-cell efficacy. Destabilization of the coexistence equilibrium is driven by changes to the experimentally derived model parameters θ, κ_2, and c_3 (Fig 6 and Eq. (10)), which represent the death rate of CAR T-cells, the proliferation or exhaustion of the CAR T-cells, and the effect of Dex on the CAR T-cell death rate, respectively. These changes are interpreted as Dex promoting tumor cell growth and CAR T-cell growth at early times (due to $c_3 < -\theta$), yet once the Dex has cleared the CAR T-cells become exhausted, no longer proliferating enough to keep up with natural death or facilitate tumor cell killing. CAR T-cell exhaustion, indicated by a decrease in κ_2, is a primary cause of tumor progression as determined by the increase in the predicted final tumor cell population, θ/κ_2 (Fig 6). Importantly, this Dex-induced shift from CAR T-cell proliferation to exhaustion is highlighted by the differences in phase space trajectories between treatment success and treatment failure presented in Fig 5.

A notable feature of the mathematical model is the fact that it captures a wide range of dynamics observed in multiple experimental conditions [5]. This is despite its relative simplicity compared to other mathematical models of immunotherapies [21–24]. A recent commentary regarding predator-prey like models, including the model presented here, is the possibility of oscillating solutions which are unlikely to be observed in patients [25, 26]. We note that the coexistence equilibrium is accompanied with phase-space trajectories that accurately describe experimental data. This includes scenarios of treatment success and tumor death ($x = 0$), allowing for informative and quantitative biological inference.

Nonetheless, several possible extensions of our model exist and are worth consideration in future analyses. A common extension is to generalize the interaction between tumor cells and CAR T-cells to a higher order Holling Type form [21–23]. Generally, the Holling Type II and III interactions are used to model changes in cell-cell interactions, notably predator-prey handling time and density-dependent behavior. Additionally, where the CARRGO model combines CAR T-cell proliferation and exhaustion into one parameter, κ_2, other approaches may incorporate a second T-cell type altogether [25, 27], a population of macrophages [24], or explicitly accounting for the pharmacodynamic and pharmacokinetics of CAR T-cell dynamics [28]. Interestingly, recent theoretical work has shown that a two T-cell type predator-prey model with Holling Type I interactions can, in the appropriate limits and conditions, reduce to a single T-cell type predator-prey model with a Holling Type II interaction [23]. While such model extensions can be enlightening, our approach aims to balance model complexity with the dimensionality and resolution of the experimental data.

Limitations and simplifications

Several limitations and simplifications were made in the course of this work that
naturally suggest follow up studies. Although there is potential to construct models
with many interacting immune populations, the fact that the xCelligence cell killing
assay is an *in vitro* system lacking an immune system naturally limits the model
complexity that is experimentally accessible. Related to this is the clearance rate of the
Dexamethasone, assumed here to have a fixed value of approximately 200 minutes. In
patient populations, some level of variation in the clearance rate is to be expected due
to physiological differences [12,13]. Future work examining how variation in the
clearance rate affects treatment success would be of interest. Furthermore, the fact that
T-cells are non-adherent to the cell killing assay precludes proposed models that require
high temporal resolution of the T-cell dynamics. Presently, our experimental protocol
includes only 2 datapoints for the CAR T-cells: the initial and final timepoints.
Although this results in a boundary value problem from a mathematical point of view
and uniquely determined solution for the CAR T-cell population, an immediate benefit
from a modeling perspective would be high temporal resolution measurement of CAR
T-cell dynamics similar to the tumor cells. Finally, another simplification is that this
modeling framework does not include spatial variations in tumor cell, CAR T-cell, or
Dex density. Due to the highly structured nature of the brain and heterogeneity of
glioblastoma tumors, including hypoxia, necrosis, and extensive invasion through the
brain, spatial considerations may be important.

Potential applications and clinical relevance

Translating our findings to clinical applications requires refining understanding of the
treatment success or failure threshold in terms of clinically accessible information for a
typical GBM patient. Presently, typical clinically relevant Dex dosage levels for GBM
related inflammation are believed to be below the threshold of Dex-induced treatment
failure identified in this study [7]. However, as advances in personalized medicine
continue to develop patient-specific treatment plans, the question is no longer how much
Dex is too much, but instead how many CAR T-cells are too few? This question is
essential for designing patient specific adaptive therapies and in use of clinical decision
support software. Furthermore, it requires knowledge of the spatial extent of individual
tumors, the *in vivo* spatial heterogeneity of CAR T-cells and Dexamethasone
concentrations, and patient response and tolerance to timed-drug delivery.

A growing subject of importance is understanding sex and age-based differences in
the immunological responses of patient derived cell lines, and how those difference
translate to an individual level in clinical applications [29]. In this work, all GBM cell
lines were derived from male patients of a similar age (43, 52, and 59 years old),
suggesting that future *in vitro* work would benefit from including a greater diversity of
patients across both age and sex.

The strategy of adaptive therapy involves reducing cancer killing treatments away
from the maximum tolerated dosages, as they can lead to the emergence of treatment
resistant clones. Instead, these therapies are aimed toward minimum necessary dosages
in order to maintain genetically diverse tumor populations that remain susceptible to
treatment [30]. In such scenarios it becomes vital to know if the reduced CAR T-cell
dosing begins approaching the treatment success or failure threshold in comparison to
the Dex dosage that patient is likely to be receiving already.

Alternatively, one can vary the concentration and timing of the Dexamethasone
dosages to still provide therapeutic levels of Dex yet avoid compromising CAR T-cell
efficacy. Previous theoretical work analysing pulsed drug delivery shows promise for this
alternative approach [31]. Yet still, another treatment strategy could be patient

preconditioning with Dexamethasone followed with delayed, and perhaps pulsed, CAR ₄₁₇ T-cell delivery. Recent simulated studies investigating preconditioning with ₄₁₈ chemotherapy [32] or targeted radionuclide therapy [33] followed with CAR T-cells ₄₁₉ suggests that combination pretreatment and time-delay approaches have clinical value, ₄₂₀ in particular for providing therapeutic dosages at lower total concentrations. Based on ₄₂₁ the duration of observable changes to the phase-space trajectory in Fig 5, we suggest a ₄₂₂ time-delay of 2-3 Dexamethasone half-lives. ₄₂₃

While adaptive therapy protocols have yet to be fully implemented in CAR T-cell ₄₂₄ treatment plans, data driven methods such as clinical decision support systems and ₄₂₅ other machine learning inspired approaches have been proposed for patient ₄₂₆ monitoring [34]. Here, algorithms are trained on historical patient treatment data in an ₄₂₇ effort to assess the likelihood that new patients will develop cytokine release syndrome ₄₂₈ or immune effector cell-associated neurotoxicity syndrome as a result of CAR T-cell ₄₂₉ therapy. Typical management plans involve, among other things, the use of ₄₃₀ corticosteroids such as Dexamethasone. In this context, our results emphasize the need ₄₃₁ to better resolve the threshold of treatment success in combining CAR T-cells and Dex ₄₃₂ given that severe and unexpected complications can occur when trying to predict a ₄₃₃ treatment response that involves nonlinear drug interactions. ₄₃₄

An essential component to understanding and predicting combination CAR T-cell ₄₃₅ and Dexamethasone treatment success in clinical scenarios is the spatial extent and ₄₃₆ heterogeneity of tumors and the spatial variation of CAR T-cell and Dexamethasone ₄₃₇ concentrations. While advances in medical imaging and patient-specific treatment ₄₃₈ planning are aiding this effort, equally important is the development of ₄₃₉ spatially-dependent models that can accurately account for observed variation. Recent ₄₄₀ work in this direction has shown promise, demonstrating the ability of mathematical ₄₄₁ models to combine genotypic evolution with spatial aggregation to describe ₄₄₂ heterogeneous tumor growth [35]. ₄₄₃

Conclusion ₄₄₄

In this work, we present an analysis of experimental data designed to untangle the ₄₄₅ interaction between glioblastoma cancer cells, CAR T-cells, and the anti-inflammatory ₄₄₆ glucocorticoid, Dexamethasone. We examined three different human derived primary ₄₄₇ brain tumor glioblastoma cell lines and found that Dexamethasone can act to promote ₄₄₈ tumor growth and exhaust CAR T-cells, thereby undermining treatment success. In ₄₄₉ cases of extreme dosing, this results in complete treatment failure and tumor ₄₅₀ progression. Our use of a non-autonomous, explicitly time-dependent predatory-prey ₄₅₁ model to characterize the interactions demonstrates that Dexamethasone acts to ₄₅₂ destabilize the coexistence equilibrium between CAR T-cells and tumor cells. ₄₅₃ Furthermore, we observe that the predicted coexistence equilibrium population for the ₄₅₄ tumor cells, defined as the ratio of the CAR T-cell death rate to the CAR T-cell ₄₅₅ proliferation/exhaustion rate, serves as an experimental threshold for treatment success ₄₅₆ or failure. This work has important implications for future clinical applications of ₄₅₇ combination therapy using CAR T-cell and Dexamethasone, as well as demonstrates the ₄₅₈ value of using non-autonomous models for pharmacodynamics. ₄₅₉

Supporting information ₄₆₀

S1 Supporting Information. Supplementary Text. Contains analysis of ₄₆₁ regression between xCelligence cell index and flow cytometry cell number, stability ₄₆₂ analysis for the 'Death' and 'Tumor Proliferation' equilibria, structural identifiability of ₄₆₃

the CARRGO with Dex model, and methods for parameter estimation by particle swarm optimization.   464
                                                                        465

S1 Fig.   Data and model fits for PBT138 with E:T=1:20. Graphs of tumor   466
cells, CAR T-cells, and Dex concentration over time for tumor cell line PBT138 with an   467
initial effector to target ratio of 1:4. Temporal measurements of tumor cell population   468
and the initial and final CAR T-cell measurements are represented by symbols, and   469
CARRGO model predictions are represented by lines. Colors and symbol types vary to   470
reflect initial Dex concentrations (see top legend). The progression of the tumor cell   471
curves as initial Dex concentration increases demonstrate the effect of Dex to reduce   472
CAR T-cell efficacy. In particular, CAR T-cell treatment is successful at low Dex initial   473
Dex concentrations (0, 10^{-4}, and 10^{-3} $\mu g/ml$) and fails at higher initial Dex   474
concentrations (10^{-2}, 10^{-1}, and 1 $\mu g/ml$), resulting in tumor cell progression.   475
Experimental measurements for the tumor cell population are down-sampled by 1/10 for   476
clarity.   477

S2 Fig.   Data and model fits for PBT030 with E:T=1:4. Similar graphical   478
information as S1 Fig. presented for tumor cell line PBT030 with an initial   479
effector-to-target ratio of 1:4. For all initial Dex concentrations, treatment success is   480
observed, resulting in complete tumor death.   481

S3 Fig.   Data and model fits for PBT030 with E:T=1:8. Similar graphical   482
information as S1 Fig. presented for tumor cell line PBT030 with an initial   483
effector-to-target ratio of 1:8. For all initial Dex concentrations, treatment failure is   484
observed, resulting in tumor cell progression that generally increases with increasing   485
initial Dex concentrations.   486

Data Availability   487

All data and code used to perform the analyses and generate figures are available on a   488
Github repository at `https://github.com/alexbbrummer/CARRGODEX`.   489

Acknowledgments   490

Research reported in this publication was supported by the National Cancer Institute of   491
the National Institutes of Health under grant numbers R01CA254271 (CB),   492
R01NS115971 (CB, RR), and P30CA033572. The content is solely the responsibility of   493
the authors and does not necessarily represent the official views of the National   494
Institutes of Health. The authors would also like to acknowledge the support of the   495
Marcus Foundation.   496

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