Oligogenic combinations of rare variants influence specific phenotypes in

2 complex disorders

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23 ABSTRACT

24 Genetic studies of complex disorders such as autism and intellectual disability (ID) are often based on enrichment of individual rare variants or their aggregate burden in affected individuals 25 compared to controls. However, these studies overlook the influence of combinations of rare 26 27 variants that may not be deleterious on their own due to statistical challenges resulting from 28 rarity and combinatorial explosion when enumerating variant combinations, limiting our ability 29 to study oligogenic basis for these disorders. We present a framework that combines the apriori 30 algorithm and statistical inference to identify specific combinations of mutated genes associated 31 with complex phenotypes. Our approach overcomes computational barriers and exhaustively 32 evaluates variant combinations to identify non-additive relationships between simultaneously mutated genes. Using this approach, we analyzed 6,189 individuals with autism and identified 33 34 718 combinations significantly associated with ID, and carriers of these combinations showed lower IQ than expected in an independent cohort of 1,878 individuals. These combinations were 35 36 enriched for nervous system genes such as NIN and NGF, showed complex inheritance patterns, 37 and were depleted in unaffected siblings. We found that an affected individual can carry many 38 oligogenic combinations, each contributing to the same phenotype or distinct phenotypes at 39 varying effect sizes. We also used this framework to identify combinations associated with multiple comorbid phenotypes, including mutations of COL28A1 and MFSD2B for ID and 40 schizophrenia and ABCA4, DNAH10 and MC1R for ID and anxiety/depression. Our framework 41 42 identifies a key component of missing heritability and provides a novel paradigm to untangle the 43 genetic architecture of complex disorders.

44

45 SIGNIFICANCE

While rare mutations in single genes or their collective burden partially explain the genetic basis for complex disorders, the role of specific combinations of rare variants is not completely understood. This is because combinations of rare variants are rarer and evaluating all possible combinations would result in a combinatorial explosion, creating difficulties for statistical and computational analysis. We developed a data mining approach that overcomes these limitations to precisely quantify the influence of combinations of two or more mutated genes on a specific clinical feature or multiple co-occurring features. Our framework provides a new paradigm for

- 53 dissecting the genetic causes of complex disorders and provides an impetus for its utility in
- 54 clinical diagnosis.

55 INTRODUCTION

Recent human population growth has led to a rapid increase in the load of rare variants affecting 56 functionally important regions of the genome^{1–3}. Thus, rare variants are collectively more 57 58 abundant in the population compared to common variants, many of which confer significant risk 59 for neurodevelopmental disorders such as autism and intellectual disability⁴. In fact, recent studies have directly implicated rare damaging mutations that are very recent or *de novo* in more 60 than one hundred genes towards neurodevelopmental disorders 5-7. The ability to establish robust 61 associations between rare variants of high effect size and complex disease has made this class of 62 63 variants the primary focus of recent studies. However, a much larger class of rare and variably 64 expressive variants that are individually less deleterious but, in combination, exert large effects towards disease is often overlooked. Variants in this category are often transmitted across 65 66 generations without adverse effects on their carriers until they encounter other similar variants that, when combined, lead to genetic interactions conferring a higher risk for disease than their 67 individual risks^{8,9}. While this phenomenon underpins oligogenic models proposed over the years, 68 studies so far have not focused on detecting combinatorial effects of specific sets of rare variants 69 towards disease phenotypes^{10–13}. 70

Identifying the effects of specific combinations of rare variants towards disease etiology 71 has been challenging for many reasons. First, combinations of rare variants are rarer, and 72 73 extremely large cohorts are required to observe even a few recurrent instances of specific variant combinations¹⁴. Prior studies of oligogenic models for rare variants evaded this problem by 74 aggregating variant information at the sample level and comparing the overall burden of rare 75 variants between groups of individuals (such as cases and controls)^{6,7,15,16}. Second, the 76 77 combinatorial explosion resulting from even a small set of rare variants makes it difficult to 78 exhaustively evaluate all combinations. While sophisticated frameworks such as network 79 analysis and machine learning provide powerful tools to model the composite effects of 80 thousands of variables on a complex system and predict emergent behaviors and quantitative outcomes, adapting them to exhaustively search and delineate the effects of specific 81 combinations of variables is daunting^{17,18}. Furthermore, incorporating an efficient search tool 82 83 into these frameworks and extending them to detect higher-order combinatorial effects would be 84 nearly impossible. *Third*, even when all combinations of rare variants could be exhaustively evaluated within a large cohort, there is a lack of methods that are sensitive enough to detect 85

86 small differences between comparison groups to establish statistical significance. Therefore, an 87 alternate approach that is highly flexible, scalable, and sensitive is necessary to address 88 computational and statistical challenges associated with assessing rare variant combinations. 89 Here, we present a combinatorial framework called *RareComb* that couples the apriori algorithm¹⁹ with binomial tests to overcome the limitations of data sparsity and high 90 91 dimensionality, and systematically analyzes patterns of rare variants between groups of interest to identify specific combinations that are significantly associated with phenotypes²⁰. We apply 92 93 our analysis framework to a discovery cohort of 6,189 children with autism to identify genetic 94 interactions involving pairs and triplets of mutated genes that are enriched in individuals with 95 intellectual disability compared to individuals without intellectual disability. We demonstrate that the carriers of mutations in these specific gene pairs and triplets within an independent 96 97 cohort of 1,878 children have significantly lower-than-expected intelligence quotient (IQ) scores. 98 We also demonstrate the adaptability of our framework by leveraging it to identify mutated gene 99 pairs and triplets significantly associated with two or more comorbid phenotypes among children 100 with autism. Finally, we show how this generalizable and modular framework can be easily 101 extended to identify higher order interactions beyond pairs and triplets of variants. Our stand-102 alone framework does not depend on *a priori* knowledge and can detect rare patterns from high-103 dimensional genetic data to generate interpretable results, making it readily applicable for analyzing cohorts of all size ranges to dissect the genetic basis of complex disorders. 104 105 106 107 108 109 110 111 112

113 **RESULTS**

114 We hypothesized that two or more genes disrupted simultaneously by rare deleterious mutations contribute to a highly penetrant phenotype, as in an oligogenic model, or lead to a more severe 115 phenotype than when each of the same genes are disrupted individually. We developed 116 117 *RareComb* as a framework that combines data mining and statistical analysis to identify specific 118 combinations (such as pairs, triplets, etc.) of rare variants that show significant associations with 119 one or more phenotypes. *RareComb* analyzes an ' $n \times p$ ' sparse Boolean matrix with 'p' genes in 'n' individuals in three discrete steps (Figure 1). First, it applies the apriori algorithm 120 121 independently in cases and controls to enumerate the frequency of all simultaneously mutated combinations that meet a pre-set minimum frequency threshold (Supp. Figure 1). Second, for 122 123 each qualifying combination of variants, the method derives the expected frequency of simultaneously observing mutations in the constituent genes under the assumption of 124 125 independence. It then independently quantifies the magnitude of deviation of the observed from the expected frequencies using binomial tests in cases and controls, and uses multiple-testing 126 127 adjusted p-values to identify combinations that are statistically enriched in cases but not in controls. Finally, the method calculates effect sizes using Cohen's d and statistical power at 1% 128 129 and 5% significance thresholds, to enable prioritization of a high confidence set of combinations 130 that contribute to the phenotype in an oligogenic manner.

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132 RareComb identifies oligogenic combinations associated with ID and autism

133 We sought to identify pairs and triplets of mutated genes that are significantly associated with

134 intellectual disability (ID) phenotypes by analyzing 6,189 affected individuals from the

135 SPARK²¹ cohort for discovery and 1,878 affected individuals from the SSC²² cohort for

136 validation. To facilitate cross-cohort comparison, we identified 10,217 rare variants (MAF <1%)

137 that were predicted to be deleterious by multiple methods and observed in both cohorts, and

aggregated these variants to genes for the analysis (see **Methods**). We first categorized 1,215

139 probands from the SPARK cohort diagnosed with ID as cases and 4,974 probands without ID as

140 controls (**Figure 2A**). We then applied *RareComb* to cases after constraining it to only evaluate

141 those gene combinations in which simultaneous mutations are observed in at least five probands.

- 142 We identified 25,602 pairs involving 1,956 mutated genes in cases that were observed at a higher
- 143 frequency than expected under the assumption of independence. Similarly, analyzing the controls

using only the 1,956 genes mutated in cases, *RareComb* identified 148 pairs of mutated genes
that were significantly enriched in cases but not in controls (Supp. Table 1), with moderate to
high effect sizes (Cohen's d, 0.08-0.15) and adequate statistical power (70%-100% at 5%
significance threshold) (Supp. Figure 2). These 148 gene pairs belonged to 142 probands, with
74% (105/142) of them carrying more than one significant pair. These observations suggest that
an individual can carry multiple combinations, each contributing to the same phenotype at
varying effect sizes (Supp. Figure 3).

151 We next sought to validate the association of these 148 mutated gene pairs towards intellectual disability. We hypothesized that if the association of the gene pairs with ID in the 152 153 SPARK cohort were truly significant, carriers of mutations in those gene pairs would tend to 154 have lower than average IQ scores in the independent SSC cohort. We found that 90 of the 148 155 significant pairs identified in the SPARK cohort were observed in at least one proband in the SSC cohort. These 90 mutated gene pairs were carried by 91 unique probands, whose average 156 157 full-scale IQ scores (average IQ=68.52) were lower than those of all ascertained probands in the SSC cohort (average IQ=86). To assess the significance of this result, we performed 10,000 158 159 random draws of 91 probands from the SSC cohort to generate a simulated distribution of their 160 average IQ scores. The average IQ of carriers of mutated gene pairs (average IQ=68.52) was significantly lower than the overall distribution of average IQ derived from simulations (average 161 IQ ranged from 73 to 92; empirical p=0) (Figure 2B). Furthermore, the average IQ of the 91 162 163 SSC probands with both mutated genes was significantly lower than the average IQ of 1,252 164 carriers of mutations in only one of the two genes (68.5 versus 82.8; Kolmogorov-Smirnov p = 1.302×10^{-16}) (Figure 2C). When each of the 90 combinations was evaluated individually, 165 166 carriers of mutations in both genes for 73% (66/90) of the combinations showed lower IQ than individuals with mutations in individual genes of the same combination, with 39/90 remaining 167 168 significant after multiple testing correction (Supp. Table 2; Supp. Figure 4). These results 169 provide evidence for synergistic effects of deleterious mutations within specific pairs of genes towards ID phenotypes. 170

We also applied *RareComb* to identify gene triplets associated with intellectual disability using the two cohorts and repeated the simulations to identify 1,593 significant combinations in the SPARK cohort. We selected 570 high-confidence triplets (with ≥90% statistical power at 5% significance threshold; **Supp. Table 3**) and found that 79 probands in the SSC cohort carried at

175 least one of these deleterious triplets. The average IQ score of individuals carrying significant

176 gene triplets (average IQ score=73) was significantly lower than a distribution of average IQ

scores from 10,000 draws of 79 SSC probands (average IQ score=82.5; min=72, max=94;

178 empirical p=0.0011; see **Supp. Figure 5**). This result reiterated that carriers of mutations in the

179 significant gene combinations have lower IQ than a random group of probands. Our results also

180 demonstrate the ability of the framework to identify higher order combinations of mutations that

181 are significantly associated with specific phenotypes in individuals with complex disorders.

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183 Oligogenic combinations are enriched for specific inheritance patterns

184 As individual variants can arise *de novo* or be inherited maternally or paternally, variants in pairs 185 of genes can have six possible patterns of transmission (Supp. Figure 6A). We identified a total 186 of 926 occurrences of the 148 pairs of mutated genes enriched among SPARK probands with ID (n=142 probands), of which inheritance could be determined without ambiguity for 887 187 188 instances. We found that one variant occurred de novo and the other variant was inherited from 189 the mother in 244/887 instances (27.5%). Similarly, both mutated genes were inherited from the 190 mother in 226/887 instances (25.4%) or occurred de novo in 221/887 instances (24.9%), while 191 the remaining fraction ($\sim 22\%$) of variant pairs were either inherited from both parents, inherited 192 from the father, or transmitted *de novo* and paternally. To assess the significance of our 193 observations, we performed simulations to establish a baseline expectation of proportions for 194 each category of parental inheritance pattern. We selected 926 pairs of genes in 1000 random 195 draws of all possible mutated gene pairs among SPARK probands and calculated the fraction of 196 instances that fell into each of the six transmission categories. The observed proportion was 197 higher than the simulated proportions for instances when both variants occurred *de novo* (24.9%) 198 versus 17%, empirical p=0) and when one variant was *de novo* and the other was inherited 199 maternally (27.5% versus 25%, p=0.028) (Figure 3A). We repeated this analysis for 7,596 200 children affected with autism in the SPARK cohort compared to 11,740 unaffected parents and 201 identified 110 gene pairs significantly associated with autism (Supp. Table 4). Similar to the 202 results obtained for the ID phenotype, we found that both variants of a gene pair were more likely to occur de novo (24% versus 18%, empirical p=0) or one variant occurring de novo and 203 the other inherited maternally (33% versus 26%, p=0) than expected based on simulation studies 204 205 (Supp. Figure 7). The enrichment of *de novo* or maternally inherited variants for significant

206 gene pairs aligns with published reports that severely affected children tend to carry multiple de207 *novo* mutations or inherit pathogenic rare variants from mildly affected or unaffected carrier 208 mothers^{16,23,24}.

209 We then assessed whether the mutated gene pairs associated with ID were also found in siblings of carrier probands. Restricting our analysis to families with unaffected siblings whose 210 211 probands had mutations in ID-enriched gene pairs, we found that both variants were present in 212 the corresponding sibling for only 53/219 (24.2%) instances of gene pairs, while 102/219 213 (46.6%) had variants in only one of the two genes and 64/219 (29.2%) instances had no variants 214 in either of the genes in the siblings (Supp. Figure 6B). Using simulations, we found a 215 significantly higher proportion of instances with only one of the two variants present in siblings compared to the expected values (46.6% versus 38.5%, p=0.007). Furthermore, the proportion of 216 217 observed instances with neither of the variants present in siblings (29.2% versus 33.1%, empirical p=0.098) or both variants present in siblings (24.2% versus 28.4%, p=0.079) was 218 219 lower than expected (Figure 3B). The observation that only a small fraction of unaffected siblings carried both mutated gene pairs suggests a strong association of these gene pairs with ID 220 221 phenotypes. These results suggest that mutations in pairs of genes significantly associated with a 222 severe phenotype in probands are more likely to occur individually than simultaneously in unaffected siblings of the same family. 223

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225 Genes forming oligogenic combinations are distinct from canonical autism genes

We expanded our analysis to include all 16,556 mutated genes in the SPARK cohort, as opposed to genes with mutations present in both the SPARK and SSC cohorts, and identified 52

significant gene pairs (Supp. Table 5) and 230 triplets associated with the ID phenotype (with

 $\geq 90\%$ statistical power at 1% significance threshold; **Supp. Table 6**). Due to the expanded

230 search space, the mutated gene pairs showed more significant p-values from the binomial tests

when compared to those obtained from the more restricted set of variants overlapping both

232 SPARK and SSC cohorts (Supp. Figure 8). Mutated genes within these combinations included

several genes related to nervous system development, such as *NIN*, *HDC*, *NGF*, and *BRD8*.

Furthermore, 5/52 pairs and 59/230 triplets contained at least one gene associated with autism in

the SFARI database, including *FGFR1*, associated with multiple disorders including Kallmann

syndrome²⁵ and Pfeiffer syndrome²⁶; *RELN*, associated with temporal lobe epilepsy²⁷; *SYNE1*,

associated with spinocerebellar ataxia^{28,29}; and *PNPLA7*, associated with autism and ID³⁰. Thus,
 most genes forming combinations are not involved in canonical autism or ID disorders,
 suggesting synergistic effects of these genes without prior association to disease.

240 We also performed gene ontology enrichment analysis for genes within the combinations and identified seven out of nine significantly enriched GO terms to be exclusively associated 241 242 with nervous system-related functions, including synthesis and metabolism of catecholamines, 243 axon/neuron regeneration, and neuron generation and differentiation (Supp. Figure 9)³¹. 244 Furthermore, the differences in the type and specificity of GO terms enriched for significant pairs versus triplets were apparent, with genes forming pairs involved in nervous system function 245 246 and genes forming triplets associated with both nervous system as well as other biological processes. We next assessed the enrichment and depletion of Human Phenotype Ontology (HPO) 247 248 terms for genes forming significant pairs towards ID phenotypes³². First, we calculated the fraction of all 4,484 genes within the HPO database associated with each HPO term. For 249 example, 30% (1,366/4,484) of all genes in HPO were associated with ID. We compared these 250 expected values calculated for each HPO term with the corresponding fractions observed within 251 252 the 95 genes forming 52 ID-associated pairs using binomial tests. Interestingly, genes associated 253 with HPO terms related to neurodevelopmental phenotypes, such as ID, global developmental delay, seizure, and microcephaly, were significantly depleted within the set of 95 genes forming 254 gene pairs (Supp. Table 7). Next, we evaluated whether genes within each of the 52 significant 255 256 pairs shared one or more common HPO phenotype or disease. Of the 52 pairs, only one pair 257 (DNASE1 & MTR) shared an HPO phenotype ("epilepsy"). This was significantly lower than the expected value obtained from the distribution of the number of shared HPO phenotypes between 258 all possible pairs of genes in the HPO database (1/52, 1.9% ID gene pairs compared to 31.5% of 259 all HPO gene pairs shared one HPO phenotype, $p=2.2\times10^{-16}$; one-sided binomial test) (Supp. 260 261 Figure 10; Supp. Table 8). We note that the 4,484 genes within HPO are potentially biased 262 towards well-studied disorders, making pairs of genes drawn from HPO more likely to share phenotypes than random pairs of genes from the genome. Overall, GO and HPO analyses show 263 264 that genes forming oligogenic combinations are involved in neuronal processes but have not 265 been previously connected to neurodevelopmental phenotypes, indicating the novelty of the 266 associations between these genes and ID phenotypes.

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268

269 Identifying variant combinations towards specific patterns of comorbid phenotypes

270 We adapted our framework to identify significant associations of two or more genotypes with 271 multiple comorbid phenotypes. To identify novel comorbid associations, we eliminated phenotypes that were highly correlated with each other, such as ADHD and reading disorder³³. 272 We analyzed variant profiles of 6,189 autism probands from the SPARK cohort with records of 273 274 comorbid features, including 1,215 individuals with ID, 1,825 with anxiety and depression, and 275 332 with schizophrenia features. We assessed for significant co-occurrences of two or more 276 mutated genes with two or more of the above phenotypes (Figure 4). Using one-tailed binomial 277 tests to compare the observed frequency of combinations of genotypes and phenotypes to the expected frequency, we first identified 169 significant associations between pairs of mutated 278 279 genes and two comorbid phenotypes as well as 82 combinations of three mutated genes and two comorbid phenotypes (Supp. Tables 9 & 10). As some of these significant genotype-phenotype 280 281 combinations can be confounded by high degree of co-occurrence of mutated genes, we next 282 calculated genotype-only p-values using binomial tests for all significant genotype-phenotype 283 associations. For 32/169 combinations of two mutated genes and two comorbid phenotypes and 284 5/82 combinations of three mutated genes and two comorbid phenotypes, the composite 285 genotype-phenotype p-values were significant while genotype-only p-values were not 286 significant, suggesting stronger associations between these variant combinations and phenotypes. 287 For example, even when variants in genes COL28A1 and MFSD2B did not co-occur more 288 frequently than expected under the assumption of independence, these mutated genes cooccurred more frequently than expected among probands with ID and schizophrenia phenotypes. 289 290 Loss-of-function and rare missense mutations in COL28A1 have been reported in individuals 291 with autism^{34,35}, and *MFSD2A*, *a* paralog of *MFSD2B*, has been directly implicated in an 292 autosomal recessive disorder associated with progressive microcephaly, spasticity and brain imaging abnormalities³⁶. Similarly, we found ARVCF and FAT1 to be significantly associated 293 294 with ID and schizophrenia, with ARVCF mapping within the 22q11.2 DiGeorge syndrome 295 region³⁷, while rare *de novo* mutations in FATI being associated with autism and 296 schizophrenia^{6,38}. Finally, we found that the mutations in genes ABCA4, DNAH10 and MC1R 297 significantly co-occurred in individuals with ID and anxiety/depression phenotypes. These

results demonstrate the utility of identifying higher-order associations between genotypes andphenotypes in complex disorders such as autism.

300

301 **DISCUSSION**

Current rare variant analysis strategies are geared towards either searching for individual variants 302 of high effect size whose influence on the phenotype is evident, such as *de-novo* gene-disruptive 303 304 mutations, or comparing rare variant burden to explain collective effects on phenotypes^{7,39,40}. 305 The wider space between these two extremes of the analysis spectrum that involves 306 combinations of rare variants has largely remained understudied. Although digenic diseases and 307 multi-hit models of complex diseases have been used to provide post-hoc explanations for an observed phenomenon, they are not equipped to serve as a framework to actively search and 308 309 identify rare variant combinations that fit oligogenic models for specific phenotypes^{9,12,13}. While machine learning has become the de-facto approach for disease outcome predictions, the lack of 310 311 holy-grail predictors and reduced interpretability due to data sparsity makes it less fit to detect combinatorial effects¹⁷. In addition, the common practice of evaluating feature importance 312 313 metrics of machine learning classifiers falls short of the objective to identify combinations of features that exert higher effect on the phenotype than evident from their independent effects^{17,18}. 314 Furthermore, prior studies to assess combinatorial effects have been inherently biased due to 315 their need to minimize the search space by restricting the analysis to only a subset of genes 316 317 chosen based on *a priori* knowledge^{41–43}. Here, we provide a proof-of-concept analytical 318 framework that remains agnostic to prior evidence and performs exhaustive searches to identify 319 combinatorial effects among rare variants while retaining high granularity of data and 320 interpretability of results.

We use our framework to identify gene pairs and triplets significantly associated with 321 322 intellectual disability and show that several constituent genes are associated with nervous system 323 processes. These mutated gene combinations are more likely to be inherited maternally or occur de novo, are depleted in unaffected siblings from the same family, and are less likely to involve 324 canonical autism or ID genes, suggesting that genes forming significant combinations are less 325 deleterious on their own but manifest effects only when combined with other similar genes 326 327 carrying rare mutations. While previous studies have linked aggregate rare variant burden towards intellectual disability^{44,45}, our results fine map the association to specific combinations 328

329 of constituent genes contributing to the burden. We propose a novel paradigm for dissecting the 330 complexity of genetic disorders, where an affected individual carries multiple combinations of 331 rare variants, and each combination contributes to either the same phenotype or distinct 332 phenotypes at varying effect sizes (Figure 5). A limitation of our method is that it tends to be biased towards genes that are mutated frequently enough to be observed in a combination. This 333 limitation can be addressed by fixing specific primary variants of interest irrespective of their 334 335 frequency and screening for "second-hit" modifiers that significantly co-occur with the primary 336 variant, such as the co-occurrence of RBM8A variants in distal 1q21.1 deletion carriers 337 manifesting thrombocytopenia-absent-radius syndrome and TBX6 variants in 16p11.2 deletion carriers with scoliosis^{46,47}. 338

Our method is fast and scalable, allows for fine-tuning combinatorial searches based on 339 340 frequency, statistical power, and multiple testing criteria, and can be adapted to enable computational approximations to further improve run time and assess higher-order combinations 341 342 beyond triplets. While larger sample sizes are generally required for detecting smaller frequency differences, we note that our framework achieves reliable statistical power even with modest 343 344 sample sizes, implying that our framework could be applied to exome sequencing studies of 345 other neurodevelopmental disorders that have not been explored for combinatorial effects. This approach can also be used to address a variety of research questions involving rare event 346 combinations, including searching for protective effects of rare variants where simultaneous 347 348 mutations are enriched in controls but not in cases, and finding combinations that exhibit specific 349 enrichment or depletion patterns in more than two phenotypic groups. In summary, we provide a 350 conceptual framework and the necessary tools to identify the oligogenic basis for complex disorders such as autism and intellectual disability, which hitherto was restricted to the analysis 351 of canonical disorders such as Hirschsprung disease⁴⁸ and Bardet-Biedl syndrome¹². 352

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354

355 MATERIALS AND METHODS

We developed *RareComb* to address computational and statistical challenges associated with 356 357 combinatorial analysis of rare variants. *RareComb* first uses the apriori algorithm to efficiently 358 count the frequencies of co-occurring variant combinations. It then uses one-tailed binomial tests 359 to compare the observed frequency of each variant combination to the expected frequency derived under the assumption of independence among the constituent variants within each 360 361 combination (Figure 1). This method can be applied to identify variant combinations that are 362 significantly enriched in cases but not in controls. In studies involving multiple comorbid phenotypes, this method can also be used to detect associations between specific combinations of 363 364 variants and one or more (comorbid) phenotypes (see Supplementary Note). The general principles of our method, built using the basic axioms of probability theory, can be easily 365 366 extended to a variety of problems involving rare higher-order combinations (Supp. Figure 11). 367

368 Identifying frequencies of rare variant combinations

369 *RareComb* utilizes the apriori algorithm to efficiently calculate frequencies of variant

370 combinations from sparse Boolean matrices (of 0s and 1s) (Supp. Figure 12A). The apriori 371 algorithm has been successfully applied to analyze consumer behavior, where identifying products frequently purchased together could benefit a company^{49,50}. While an algorithm that is 372 used to derive insights from patterns within highly frequent events (i.e. frequent itemset mining) 373 374 might not seem like a good fit to analyze rare variant combinations, its ability to perform 375 disciplined search based on both built-in and user-specified constraints makes it an ideal 376 counting tool. For example, the apriori algorithm avoids enumerating each of the 50 million pairs 377 or 167 billion triplets from just 10,000 variants, and instead prunes the search-space based on user-defined criteria such as minimum frequency threshold and size of combinations (pairs, 378 379 triplets, etc.) (Supp. Figure 12B). RareComb applies an additional constraint to the algorithm to 380 limit its search to co-occurring events, which further reduces the search space (see

381 Supplementary Note). *For example*, when considering variants A and B, only the frequency of

382 the presence of both variants (A=1 & B=1) is counted, and not absence of either or both variants

383 (A=1 & B=0; A=0 & B=1; or A=0 & B=0).

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386 Statistical Inference

387 *RareComb* utilizes the p-values of one-tailed binomial tests to establish the magnitude of enrichment for each rare variant combination (Figure 1). For each combination, *RareComb* 388 389 formulates null and alternate hypotheses for the binomial test by considering the event of observing all constituent variants together within a group of individuals as success and all other 390 391 possibilities as failure in a binomial trial: 392 $H_0: \pi = \pi_0$ 393 $H_a: \pi > \pi_0$ 394 where, 395 π = Probability of *observing* all constituent rare variants of a combination together within a cohort, i.e., P(A=1 & B=1)396 $\pi_0 = Expected$ probability derived from the frequency of individual variants of a 397 398 combination, under the assumption of independence, i.e., P(A=1) * P(B=1). *RareComb* then compares the null binomial distribution derived using the sample size of the 399 group (n) and the expected probability (π_0) (i.e., X ~ Binom(n, p = π_0)) with the observed 400 probability (π), and calculates the probability of observing rare variants occurring together at 401 least as frequently as they were observed within the cohort (i.e. p-value). 402 In case-control analyses, this method is applied independently to each group, and the p-403 values between them are compared. The combinations exhibiting enrichment in both cases and 404 controls, likely due to proximity of variants in linkage disequilibrium, are eliminated, following 405 406 which the p-values in cases are adjusted for multiple-testing to identify statistically significant 407 combinations that exhibit enrichment in cases but not in controls. Finally, the effect sizes are 408 calculated using Cohen's d and the statistical power is measured using 2-sample 2-proportion 409 tests, as additional metrics to prioritize the final set of significant rare variant combinations. In 410 genotype-comorbid phenotype association analyses, the method is applied just once to the entire 411 cohort, with multiple-testing adjusted p-values serving as a sufficient metric to identify high 412 quality associations between genotypes and two or more co-occurring phenotypes. 413 414 Statistical power and computational performance of the method

415 We measured the relationship between sample size and statistical power for both binomial and 2-

416 sample 2-proportion tests used in the framework. It took 1,356 samples for the binomial test to

417 achieve a statistical power of 80% to establish statistical enrichment between expected and 418 observed co-occurrence frequencies of 0.1% and 0.5% (Supp. Figure 13). This number 419 increased to 6,469 when the test needed to be more sensitive to compare frequencies of 0.3% and 420 0.5%. Similarly, it took 7,840 samples for the 2-sample 2-proportion test to achieve 80% power to establish statistical difference between co-occurrence frequencies of 2% and 0.5% observed in 421 two groups (Supp. Figure 14). The sample size requirement increased to 14,633 to differentiate 422 423 frequencies of 1.5% and 0.5% at 80% statistical power. These results align with the known 424 relationship between sample size and statistical power, and indicate that our method can be reliably applied to analyze reasonably modest-size cohorts. 425

426 We also measured the run times for the case-control analysis to identify significant pairs and triplets of mutated genes using simulated data of three discrete sizes of samples (5,000, 427 428 10,000, and 50,000 individuals) and genes (5,000, 10,000, and 15,000 genes). The apriori algorithm was run on single-core CPUs with 256 GB memory and was constrained to analyze 429 430 combinations observed in at least 0.15% of the samples. Given the memory-intensive nature of the apriori algorithm implemented in the 'arules' package, 256 GB was chosen to maintain 431 432 uniformity⁵¹. However, smaller input files could be processed successfully using much less 433 memory. As expected, the runtimes were proportional to the size of the combination (pairs versus triplets) and the number of input variables (Supp. Figure 15). While the increase in run 434 time with the increase in sample size is apparent for pairs, lower runtimes observed with running 435 436 50,000 samples compared to 5,000 samples for triplets can be attributed to stochasticity of the 437 input data. Overall, the analysis of gene pairs took between one minute and 12 minutes while triplets took between two minutes and 150 minutes. Since several factors influence the runtime 438 of the method, a trial-and-error approach to determine an optimal minimum frequency threshold 439 for co-occurring events can help identify relevant combinations without resulting in insufficient 440 441 memory due to combinatorial explosion.

442

443 Samples

444 We used whole exome sequencing data from 6,189 affected males from the Simons Foundation

445 Powering Autism Research (SPARK)²¹ and 1,878 affected males from 2,247 simplex families

446 from the Simons Simplex Collection (SSC)⁵² cohort from the Simons Foundation Autism

447 Research Initiative (SFARI)⁵³. We selected only male probands for our analysis to avoid any

- 448 confounding effect due to gender or ascertainment bias^{54,55}. While diagnosis information for
- 449 intellectual disability (ID), anxiety, attention deficit hyperactivity disorders (ADHD),
- 450 schizophrenia, language and sleep disorders were encoded as binary variables for the SPARK
- 451 samples, full-scale intelligence quotient (IQ) scores were available for the SSC cohort.
- 452

453 **Data preparation and quality control**

impact could not be easily assessed.

454 Variant Call Format (VCF) files obtained from exome sequencing data were annotated using

455 ANNOVAR⁵⁶ for rsID information and variant frequency using ExAC⁵⁷ and gnomAD⁵⁸. To

456 overcome the limitations of using a single method to predict pathogenicity, the effects of non-

- 457 synonymous mutations were annotated using 11 prediction methods: SIFT⁵⁹, Polyphen2⁶⁰
- 458 (HDIV), Polyphen2 (HVAR), LRT⁶¹, MutationTaster⁶², MutationAssessor⁶³, FATHMM⁶⁴,
- 459 MetaSVM⁶⁵, PROVEAN⁶⁶, REVEL⁶⁷, and CADD⁶⁸. Briefly, all missense, stop-loss/gain, and
- 460 start-loss/gain variants within exonic, 3', and 5' UTR regions with minor allele frequencies $\leq 1\%$
- 461 identified based on both ExAC and gnomAD databases were selected. Then, variants with allele
- 462 depth of \geq 15 and allele balance between 25% and 75% for heterozygous variants and > 90% for
- 463 homozygous variants were selected as high-quality variants. Deleteriousness of the variants were
- 464 measured and reported differently by each prediction method. REVEL provided a score between
- 465 0 and 1, with higher scores indicating higher level of deleteriousness, while Polyphen2 and
- 466 MutationAssessor classified variants into one of three categories. *For example*, Polyphen2

467 classified variants as 'Deleterious', 'Possibly damaging', or 'Tolerated', while MutationAssessor

- 468 classified variants as 'High', 'Medium', or 'Low'. The other nine methods classified variants as
- 469 either 'Deleterious' or 'Tolerated'. Pathogenicity reported by each tool was encoded as a binary
- 470 variable, with the categories 'Possibly damaging' and 'Medium' encoded as 0.5. Thus, the
- 471 composite pathogenicity score derived from the 10 tools could range between 0 and 10. Missense
- 472 variants with a cumulative score of ≥ 4 and stop-loss/gain predicted as 'deleterious' either based
- 473 on CADD score (CADD phred >30) or MutationTaster were considered deleterious for all
 474 analyses. Indels and other smaller structural variants were not considered, as their functional
- 475 476
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479 Gene Ontology (GO) and Human Phenotype Ontology (HPO) enrichment analyses

- 480 Gene Ontology term enrichment analyses were performed using the 'Gene Ontology API'
- 481 accessed using the 'post' command of the python package 'requests' (python version 3.7)³¹. All
- 482 analyses were performed using parameters for *homo sapiens* (organism = '9606') to identify
- 483 biological processes enrichment (annotDataSet = 'GO:0008150') using binomial tests. HPO
- 484 enrichment analyses were performed using data from the 'genes' to phenotype' file obtained
- 485 from the HPO website³². Since enrichment of phenotypes is not automatically evaluated by HPO,
- 486 we used customized R scripts to derive baseline expectations that could be compared against the
- 487 actual observations to determine significance using the p-values from binomial tests.
- 488

489 Statistical analysis

490 All statistical analyses were performed using R v3.6.1 (R Foundation for Statistical Computing,

- 491 Vienna, Austria)⁶⁹ and Python $(v3.7)^{70}$. All data-related plots were generated using the R
- 492 package ggplot2⁷¹.
- 493

494 Software Availability

495 *RareComb* is available as an open-source (https://github.com/girirajanlab/RareComb) R package 496 that can be downloaded from the Comprehensive R Archive Network (CRAN) repository⁷². It can also be installed into development environments via interfaces such as Rstudio⁷³ using the 497 498 command install.packages('RareComb'). The tool provides several functionalities that allow 499 users to run the types of analyses described in this manuscript. The functionalities are as follows: 500 (1) Identify rare event combinations statistically enriched within a single group; (2) Identify rare 501 event combinations statistically enriched in cases but not in controls; (3) Identify rare event 502 combinations enriched in cases but depleted in controls; (4) Identify statistically enriched rare 503 event combinations that include at least one element from an user-supplied list; and (5) Identify 504 genotypes statistically enriched within individuals manifesting two or more comorbid 505 phenotypes. Each functionality takes a Boolean matrix as input and provides a set of user-506 adjustable parameters to customize the analysis, and delivers the results in a tabular format as csv 507 files. Detailed instructions on the available functionalities and parameters built into RareComb and their usage can be found on the GitHub page or CRAN website. A shiny app illustrating the 508 ideas behind *RareComb* is available online at https://girirajanlab.shinyapps.io/RareComb/⁷⁴. 509

510 **DECLARATIONS**

511 Ethics approval and consent to participate

- 512 As these data were de-identified, all our samples were exempt from IRB review and conformed
- 513 to the Helsinki Declaration. No other approvals were needed for the study.
- 514

515 **Consent for publication**

- 516 All authors agree and consent for publication of the manuscript.
- 517

518 **Competing interests**

519 The authors declare that no competing interests exist in relation to this work.

520

521 Authors' contributions

522 VK and SG conceived the project. VK performed the analyses, generated the plots/images, and

523 wrote and revised the manuscript; SG supervised the research and wrote and revised the

524 manuscript. All authors read and approved the final draft of the manuscript.

525

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- 533 investigators, clinical sites, and staff for the consortia. The authors appreciate obtaining access to
- 534 genetic and phenotypic data for SPARK and SSC through the Simons Foundation Autism
- 535 Research Initiative (SFARI) Base. Approved researchers can obtain the SSC and SPARK
- 536 population datasets described in this study by applying at https://base.sfari.org.

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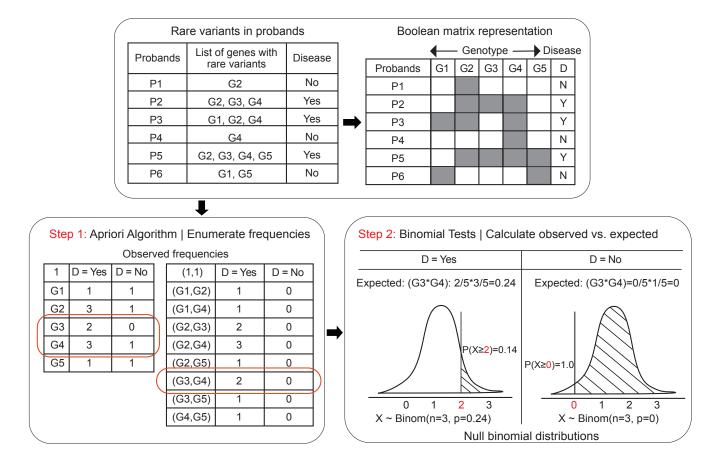
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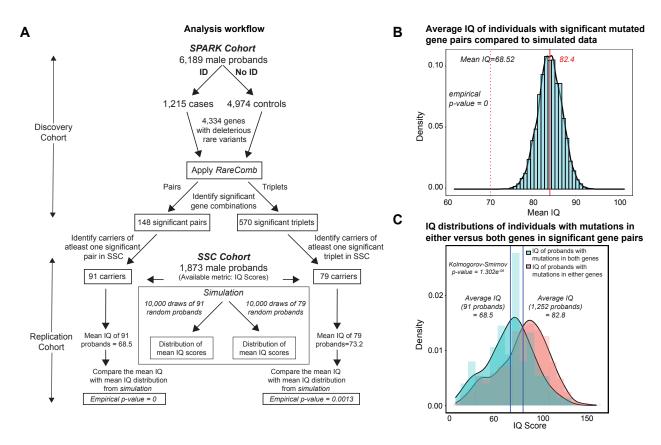
726 **MAIN FIGURES**



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728 Figure 1: Conceptual overview of combinatorial analyses using RareComb. A Boolean 729 representation of genotype (mutated genes, G1, G2, etc) and disease status for probands (P1, P2, 730 etc) is shown. In step 1, the apriori algorithm is applied to the Boolean input matrix to calculate 731 the frequencies of individual (for example, G1) and simultaneous occurrences of events (G1 and 732 G2) that meet the user-specified criteria, including the size of combinations (pairs, triplets, etc.) 733 and minimum frequency threshold of simultaneous occurrences. In step 2, independently in case 734 and control groups, for each combination, the binomial test is applied to compare the observed 735 frequency of simultaneous occurrence of events with its corresponding null binomial distribution 736 of the expected frequencies calculated under the assumption of independence. Binomial test for gene pair G3 and G4 is shown as an example. 737 738

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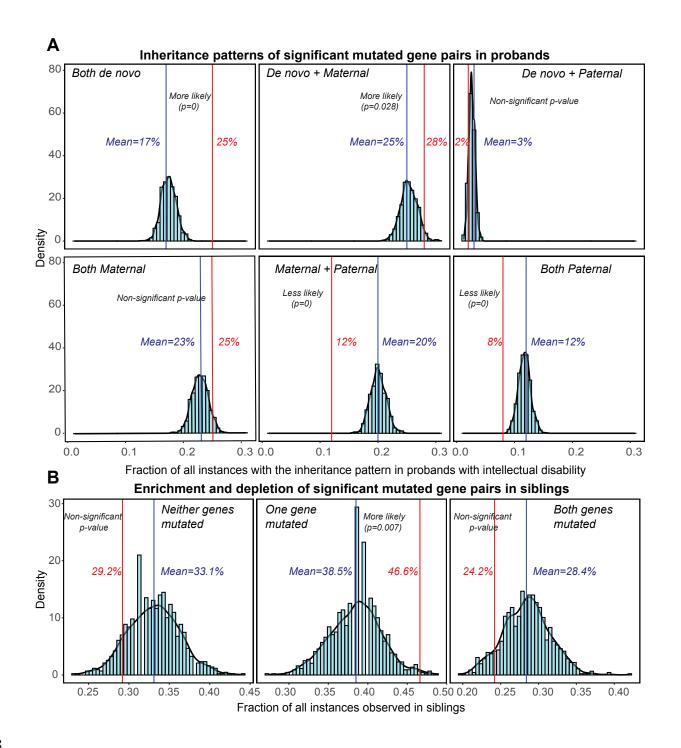


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Figure 2: Combinations of rare variants contributing to intellectual disability (ID) 742

phenotype. (A) An outline of the approach used to identify and validate mutated gene pairs and 743 744 triplets enriched in probands with ID is shown. We tested whether mutated gene pairs identified as significant in one cohort (SPARK) are also associated with severe phenotypes in an 745 independent cohort (SSC). To test this, we obtained the mean IQ score of individuals from the 746 SSC cohort carrying significant combinations identified from the SPARK cohort. Empirical p-747 values were then calculated based on the deviation of the mean IQ from the distribution of mean 748 IQ scores obtained from 10,000 random draws in the simulation. (B) The mean IQ of individuals 749 750 with mutated gene pairs in the SSC cohort was significantly lower (empirical p-value=0) when compared to the distribution of mean IQ scores obtained from the simulation. (C) Histogram 751 shows the distributions of IO scores of SSC probands who carried mutations in either genes 752 versus both constituent genes of the significant gene pairs. The distributions were significantly 753 754 different from each other (p-value = 1.302×10^{-6} , Kolmogorov-Smirnov test). 755

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759 Figure 3: Analysis of parental and sibling inheritance patterns of significant gene pairs

760 associated with ID. (A) Fraction of all instances of significant gene pairs observed within each

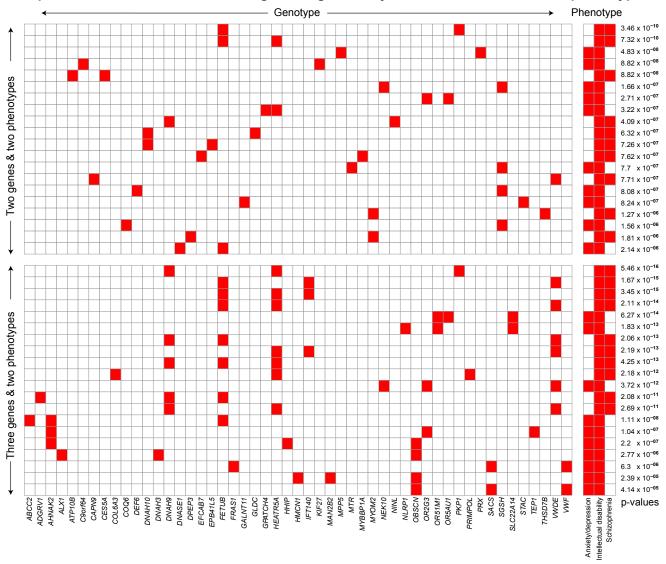
of the six possible parental inheritance patterns (red) compared against 1,000 simulations is

shown (blue). During each simulation, random mutated gene pairs from the SSC cohort were

selected, the inheritance status of the mutations was identified, and the fraction of those instances

belonging to one of the six pre-defined categories was calculated. Comparing the observed

- 765 fractions with the simulated fractions indicate statistical enrichment for two specific inheritance
- 766 patterns based on empirical p-values: both variants being *de novo*, and one variant being *de novo*
- and the other transmitted from the mother. **(B)** Histograms show the carrier status of significant
- gene pairs in siblings of carrier probands (red) compared against 1,000 simulations (blue).
- Among significant pairs, both genes were mutated in only 24.2% of all siblings (compared to
- 28.4% in simulations), whereas one of the two genes was mutated in 46.6% of all siblings
- (compared to 38.5% in simulations). These results show that mutations are more likely to be
- observed in just one of the two genes within the gene pairs and are less likely to be observed
- simultaneously in siblings of carrier probands.
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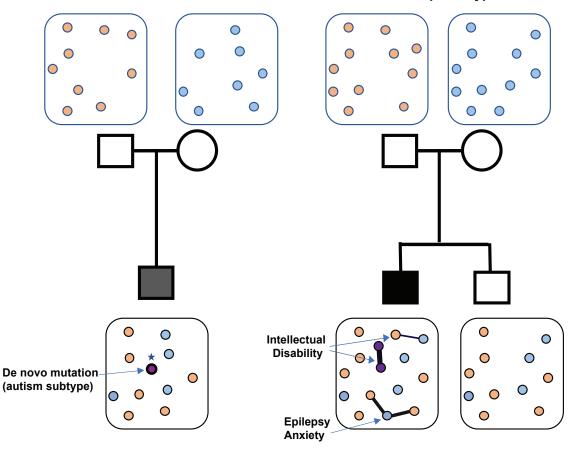


Specific combinations of mutated genes significantly associated with comorbid phenotypes



Figure 4: Analysis of comorbid phenotypes using *RareComb*. We analyzed the genotypes of
probands with anxiety/depression, ID, or schizophrenia. The heatmap shows combinations of
two or three mutated genes that were significantly enriched in individuals with specific patterns
of comorbid phenotypes compared to the expected frequency under the assumption of

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Rare variants and their combinations associated with phenotype

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Figure 5: Rare variant models for complex disorders. The schematic shows two models for 788 789 the genetic etiology of complex disorders. Circles represent rare variants present that are either 790 de novo or inherited from a parent. On the left, individual high-effect de novo variants are 791 strongly associated with a phenotype of interest. On the right, rare variants within an individual 792 combine in multiple ways and contribute towards distinct phenotypes. The thickness of the connecting lines denotes effect sizes, and an affected individual can carry multiple oligogenic 793 combinations of rare variants, each of which contributes to the same or distinct phenotypes. This 794 795 extension of the oligogenic model enables further dissection of the genetic architecture of complex disorders. 796