1 **Fine-mapping of nuclear compartments using ultra-deep Hi-C shows that active promoter and**
2 **enhancer elements localize in the active A compartment even when adjacent sequences do not**
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Running Title: Sub-genic discordant compartments

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Abstract

Megabase-scale intervals of active, gene-rich and inactive, gene-poor chromatin are known to
segregate, forming the A and B compartments. Fine mapping of the contents of these A and B
compartments has been hitherto impossible, owing to the extraordinary sequencing depths required to
distinguish between the long-range contact patterns of individual loci, and to the computational
complexity of the associated calculations. Here, we generate the largest published *in situ* Hi-C map to
date, spanning 33 billion contacts. We also develop a computational method, dubbed PCA of Sparse,
SUper Massive Matrices (POSSUMM), that is capable of efficiently calculating eigenvectors for sparse
matrices with millions of rows and columns. Applying POSSUMM to our Hi-C dataset makes it possible to
assign loci to the A and B compartment at 500 bp resolution. We find that loci frequently alternate
between compartments as one moves along the contour of the genome, such that the median
compartment interval is only 12.5 kb long. Contrary to the findings in coarse-resolution compartment
profiles, we find that individual genes are not uniformly positioned in either the A compartment or the B
compartment. Instead, essentially all (95%) active gene promoters localize in the A compartment, but
the likelihood of localizing in the A compartment declines along the body of active genes, such that the
transcriptional termini of long genes (>60 kb) tend to localize in the B compartment. Similarly, nearly all
active enhancers elements (95%) localize in the A compartment, even when the flanking sequences are
comprised entirely of inactive chromatin and localize in the B compartment. These results are consistent
with a model in which DNA-bound regulatory complexes give rise to phase separation at the scale of
individual DNA elements.

Main

The nucleus of the human genome is partitioned into distinct spatial compartments, such that
stretches of active chromatin tend to lie in one compartment, called the A compartment, and stretches
of inactive chromatin tends to lie in the other, called the B compartment[1]. Compartmentalization was
first identified using Hi-C, a method that relies on DNA-DNA proximity ligation to create maps reflecting
the spatial arrangement of the genome[1]. Loci in the same spatial compartment exhibit relatively
frequent contacts in a Hi-C map, even when they lie far apart along a chromosome, or on entirely
different chromosomes[1,2]. Accurate classification of the resulting genome-wide contact patterns
requires a large number of contacts to be characterized at each locus. As such, genome-wide
compartment profiles have only been generated, in the past, at resolutions ranging from 40 kb – 1 Mb[1-
3]. Moreover, extant compartment detection algorithms require operations, such as calculation of
principal eigenvectors[1], which are computationally intractable when the underlying matrices have
millions of rows and columns – such as high-resolution Hi-C matrices.

Although the compartments as a whole are often thought to form as a consequence of phase
separation[3-6], the low resolution of compartment profiles has made it difficult to determine the protein
mechanisms that underlie this process.

Here, we construct an *in situ* Hi-C map in lymphoblastoid cells spanning 42 billion read-pairs and
33 billion contacts. This map contains an average of 22,000 contacts for every kilobase of genome
sequence. We combine this map with a novel algorithm, dubbed POSSUMM, which greatly accelerates
the calculation of the principal eigenvector and the largest eigenvalues of a massive, sparse matrix. This
makes it possible to, e.g., calculate the principal eigenvector for correlation matrices containing millions
of rows, and billions of nonzero entries. Combining our ultra-deep map with POSSUMM, we find that it
is possible to map the contents of the A and B compartments with 500 bp resolution, a 100-fold

improvement in resolution. We also show that when we classify loops based on their appearance, at fine
resolution, in our ultra-deep map, it becomes possible to distinguish between loops that form by
extrusion and those that form via non-extrusion mechanisms.

Generation of an ultra-deep in situ Hi-C map in lymphoblastoid cells spanning 33 billion contacts

We produced an ultra-deep Hi-C map using lymphoblastoid cells from a panel of 17 individuals,
obtaining over 42 billion PE150 read-pairs. This map was generated by aggregating the results of over
150 individual Hi-C experiments. In order to enhance the resolution of the maps, we used a variety of 4-
cutter restriction enzymes in the different experiments, thus enhancing the density of cut sites across
the genome. Together, these experiments yielded 33 billion contacts after alignment, deduplication, and
quality filtering (Table S1). The resulting dataset is far deeper than any prior published Hi-C map. By
comparison, the average published Hi-C map contains roughly 300 million contacts; 93% of Hi-C maps in
the 4DNucleome database[7] have less than 1 billion contacts (Fig. S1A, Table S2); and the widely used
lymphoblastoid Hi-C map generated in Rao et al. contains 4.9 billion contacts (Fig. 1A).

We generated contact matrices at a series of resolutions as fine as 500 bp. These matrices
greatly improved the resolution of all features genome-wide, revealing many additional loops and
domains (Fig. 1B). This high coverage also enhanced the long-range plaid pattern indicative of
compartments (Fig. 1C, S1B), as well as the corresponding compartment domains observed along the
diagonal of the map (Fig. 1D, S1C). Critically, because the number of contacts at every locus was greatly
increased, with an average of 66,000 contacts incident on each kilobase of the human genome (Fig. 1C,
S1B), we were able to distinguish between loci in the A compartment and loci in the B compartment
with much finer resolution.

Development of PCA of Sparse, SUper Massive Matrices (POSSUMM) and its use to create a genome-
wide compartment profile with 500bp resolution.

Extant methods for classifying loci into one compartment or the other typically rely on
numerical linear algebra to calculate the principal eigenvector (called, in this context, "the A/B
compartment eigenvector") and the smallest eigenvalues of correlation matrices associated with the Hi-
C contact matrix. At 100 kb resolution, these matrices typically have thousands of rows and columns and
millions of entries, making them tractable using extant numerical algorithms, such as those
implemented by Homer[8], Juicer[9], and Cooler[10]. However, at kilobase resolution or beyond, these
matrices have hundreds of thousands of rows and hundreds of billions of entries, making them
intractable using the aforementioned tools. For example, computing an eigenvector for chr1 at 500 bp
resolution entails generating a matrix with 250 billion entries and performing a calculation that is
projected to require >4.6 TB of RAM for >16 years (Fig. S1D).

As such, we developed a method, POSSUMM, for calculating the principal eigenvector and the
smallest eigenvalues of a matrix. POSSUMM is based on the power method, which repeatedly multiplies
a matrix with itself in order to calculate the principal eigenvector (Fig. 1D). However, POSSUM does not
explicitly calculate all of the intermediate matrices required by the power method. Instead, it explicitly
calculates only the tiny subset of intermediate values required to obtain the principal eigenvector itself,
not requiring dense matrices, which makes it vastly more efficient (Fig. 1D, Fig. S1EF).

Using POSSUMM, we assigned loci to the A and B compartment at resolutions up to, and
including, 500 bp (Fig. 1C). The calculation of the A/B compartment eigenvector at 500 bp resolution
took only 12 minutes, and 13 GB of RAM (Fig. S1D&G). A and B compartments identified by POSSUM
accurately detect the segregation of active from inactive chromatin (Fig. S1H-K).

The median compartment interval is 12.5 kb long

It is widely thought that compartment intervals (genomic intervals that lie entirely in one
compartments) are typically megabases in length and are partitioned into numerous punctate loops and
loop domains[6,11-13]. To explore this phenomenon, we used our fine map of nuclear compartments to
examine the frequency with which loci alternate from one compartment to the other. Nearly 99% of
compartment intervals were less than 1 Mb in size, and 95% were smaller than 100 kb (Fig. 2A). The
median compartment interval was only 12.5 kb, and thousands of compartment intervals were no
longer than 5 kb (Fig. S1L). In comparison, the median size of CTCF loops in our map was 360 kb in
length, demonstrating that compartment intervals are smaller than individual loops.

Kilobase-scale compartment intervals frequently give rise to contact domains

It is well known that long compartment intervals often give rise to contact domains, i.e.,
genomic intervals in which all pairs of loci exhibit an enhanced frequency of contact among
themselves[6,14-17] (Fig. 1D). Such contact domains are referred to as compartment domains. We found
that even short compartment intervals less than 5 kb frequently give rise to contact domains (Fig. S1M),
demonstrating that intervals of chromatin in the same compartment possess the ability to form contact
domains regardless of scale.

Essentially all active promoter and enhancer elements localize in the A compartment

Next, we compared our fine map of nuclear compartments to ENCODE's catalog of regulatory
elements in GM12878 cells. We examined active promoters (defined as 500 bp near the TSS, absence of
repressive marks H3K27me3 or H3K9me3, and with >= 1 RPKM gene expression in RNA-seq) and found
that nearly all lie in the A compartment: out of 9,324 active promoters annotated in GM12878, only 496
(5%) were assigned to the B compartment (Fig. 2B - left). We noticed that active promoters in the B
compartment had higher values in the principal eigenvector compared to the surrounding regions (Fig.
S1N). Indeed, if we use a slightly more stringent threshold (assigning promoters to the B compartment
only if the corresponding entry of the principal eigenvector is <-.001), we find that only 233 (2.5%) of
promoters are assigned to the B compartment. Notably, when 1 Mb resolution compartment profiles
are used, the number of active promoters assigned to the B compartment increases 4-fold, to ~21% (Fig.
S1O). This is at least in part because the use of coarse resolutions leads to the averaging of interaction
profiles from neighboring loci, such that a DNA element in the A compartment might be erroneously
assigned to the B compartment if most of the flanking sequence was inactive (Fig. 2C, S2A-G).

Similarly, we found that essentially all active proximal enhancers (defined by annotation in
DenDB[18], <=10 kb from a TSS, and overlapping H3K27ac but not H3K27me3 & H3K9me3[19]) lie in the A
compartment (Fig. 2B – middle). Moreover, essentially all active distal enhancers (DenDB[18], >10 kb from
a TSS, with H3K27ac, but not H3K27me3 or H3K9me3[19]) lie in the A compartment (Fig. 2B – right): out of
30,868 active distal enhancers annotated in GM12878, only 1,607 (5%) were assigned to the B

compartment. Many of these distal enhancer elements represent small islands of A-compartment
chromatin in a sea of inactive, B compartment chromatin (Fig. 2D). This demonstrates that individual
DNA elements can escape a neighborhood that is overwhelmingly associated with one compartment in
order to localize with a different compartment (Fig. 2C-E, S2H-I). When 1 Mb resolution compartment
profiles are used, the number of active distal enhancers assigned to the B compartment increases 4.6-
fold, to 23% (Fig. S2J). Again, this is at least in part because the use of coarse resolutions leads to the
averaging of interaction profiles from neighboring loci (Fig. S2H&K).Taken together, we find that
essentially all active regulatory elements, including both promoters and enhancers, lie in the A
compartment, even when immediately neighboring sequences do not.

171 Many genes exhibit discordant compartmentalization, with the TSS in the A compartment and the TTS
172 in the B compartment

When exploring the fine map of nuclear compartmentalization, we noticed many genes where
the TSS and TTS localize to opposite compartments (Fig. 3A., see also Fig. 1D,2C,2E). These intra-genic
compartmental switches are more easily seen at large genes (Fig. 3B, S3AB). We therefore asked if gene
size can affect the compartment localization of the TTS. Indeed, average profiles of compartmental
status revealed that TSSs were most likely to be in the A compartment (Fig. 3C), but that the likelihood
of lying in the A compartment decreases steadily as one examines increasingly distal portions of the
gene body, such that the TTSs of large genes are more likely to localize to the B compartment (Fig.
3C&D, S3C). This was especially evident if we consider very large genes (Fig. S3D), where the TSS was
overwhelmingly in the A compartment, but the TTS was usually in the B compartment.

We next asked if genes with discordant compartmentalization (i.e., the TSS was in compartment
A, but the TTS was in compartment B) could be explained by different chromatin marks at the TSS vs.
TTS. We examined chromatin marks at the TTS in active genes larger than 20 kb and found that
diminished levels of active marks at the TTS, specifically RNAPII, H3K4me1, and H3K36me3, were
correlated with presence of discordant compartmentalization (Fig. 3E, Fig. S3E). Notably, although
repressive chromatin marks are frequently seen at loci in the B compartment, genes with discordant
compartmentalization typically lacked such marks at the TTS (Fig. 3E, S3E). We also found that
chromatin marks at the TSS were not predictive of whether the gene exhibited discordant
compartmentalization (Fig. S3E&F).

Finally, we sought to determine if discordant compartmentalization was associated with
transcriptional pausing as measured by GRO-Seq. We found that elongating genes longer than 20 kb
were more likely to exhibit concordant compartmentalization (Fig. 3F), whereas paused genes were
more likely to exhibit discordant compartmentalization (Fig. 3G).

Taken together, these data support a model where an active TSS localizes to the A compartment
but brings with it only a small portion of the gene body, depending on the elongation status (Fig. 3H).

198 Loop extrusion forms diffuse loops, whereas compartmentalization forms punctate loops

199   We examined loops in our Hi-C dataset. Using SIP[20] and HiCCUPS[2], we identified 32,970 loops.
200 Ninety-one percent of these loops contained a CTCF-bound motif at both anchors, with a strong
201 preference for the convergent orientation (Fig. S4A).

202    Interestingly, when we examined loops at 1 kb resolution, we noticed that the signal is diffuse
203 (Fig. 4A, S4B), indicative of frequent contacts proximal to the CTCF binding sites (Fig. 4B). The elevated
204 contact frequency decays as the distance from the corresponding anchors increases (Fig. 4C, rainbow) (a
205 loss of signal of c.a. -6% from one bin to the next; i.e. -6%/kb compounding). Curiously, this decay rate is
206 much slower than the decay rate reflected by the diagonal of the Hi-C map (Fig. 4C, S4C – expected) (c.a.
207 -28%/kb), which is thought to reflect the properties of the chromatin polymer. The decay was
208 unchanged as a function of loop size or sequencing depth (Fig. S4DE).

209    We wondered whether this slow decay in contact frequency was seen for loops in other species.
210 We therefore examined hundreds of loops observed in a published high-resolution Hi-C map from
211 *Drosophila melanogaster* Kc167 cells at 1 kb resolution[14,21] (Fig. 4D&E). Interestingly, the loops in
212 *Drosophila* decayed at a rate (c.a. -20%/kb) that matched the diagonal of the *Drosophila* Hi-C map (c.a. -
213 23%/kb) and was much faster than the rate seen for human CTCF-mediated loops (Fig. 4F). This suggests
214 that CTCF loops create interactions between sequences bound by CTCF, as well as interactions between
215 CTCF bound and adjacent sequences. However, in *Drosophila*, Pc loops only create interactions directly
216 between the Pc bound sequences.

217    Finally, we examined loops previously identified in *C. elegans*[20,22,23]. The loop decay was slower
218 (c.a. -11%/kb) than the decay seen at the diagonal (c.a. -24%/kb) (Fig. 4F, green vs. grey), and was more
219 similar to the rate of decay seen for human CTCF-mediated loops than the one observed for *D.*
220 *melanogaster* loops (Fig. 4F, Fig. S4I).

221    It was notable that the type of decay observed (fast or slow) matched the putative mechanism
222 by which the loops formed. CTCF-mediated loops in human are bound by, and dependent on, the SMC
223 complex cohesin (Fig. S4H), and form by cohesin-mediated extrusion[24-27]. Similarly, the loops in *C.*
224 *elegans* are bound by the SMC complex condensin and we previously suggested that they are formed by
225 condensin-mediated loop extrusion[20,22,23]. Indeed, the interactions between loop-adjacent sequences
226 are in further support of loop formation by extrusion in *C. elegans*. By contrast, *Drosophila* loops are
227 much less likely to be bound by CTCF, cohesin, condensin, or other extrusion-associated proteins[14].
228 Instead, they are bound by the Polycomb complex, *Pc*, and may form by means other than extrusion[28-30].

229    These findings suggest that the mechanism of loop formation influences whether loops will be
230 punctate or diffuse, with extrusion-mediated loops forming diffuse peaks and compartmentalization-
231 mediated loops forming more punctate features.

233 Diffuse loops enhance the contact frequency of nearby promoter-enhancer interactions

234    Using Fit-Hi-C[31], we called promoter-enhancer interactions at 1 kb resolution on human chr1.
235 We examined those interactions where both the promoter and enhancer lie within 100 kb of a loop
236 anchor. In some cases, these interactions lie completely inside the loop, but in others they cross the
237 loop anchor. Both cases exhibited strongly enriched contact frequency as compared to enhancer-
238 promoter interactions that are unrelated to CTCF loops, i.e., near permutated random sites (Fig. 4G).
239 These data suggest that CTCF loops enhance the contact frequency of promoter-enhancer interactions,
240 even when both elements lie outside the loop (Fig. 4H). By contrast, in *Drosophila*, Fit-Hi-C interactions
241 between promoters and enhancers tend to be much shorter (Fig. S4J).

243 Deletion of CTCF's RNA binding domains leads to more punctate loops

Interestingly, we observed some variability in the decay rate for different loops (Fig. S4K). This
decay did not correlate strongly with either CTCF motif strength, CTCF ChIP-seq peak strength, or Rad21
ChIP-seq peak strength (Fig. S4L-O). Instead, we found that CTCF-mediated loops exhibiting slower decay
are associated with higher levels of transcription (Fig. 4I) and chromatin accessibility (Fig. S4P) near the
loop anchors. This suggests that nearby transcriptional activity could impact how CTCF interacts with the
nearby sequences and / or with the loop extrusion process.

The CTCF protein contains 11 zinc finger domains. Recently, it was shown that ZF1 and ZF10 bind
to RNA, and that deletion of these two domains causes weakening of loops throughout the genome[32].
We performed aggregate peak analysis on the published Hi-C in ZF1 and ZF10 mutants[32] using "bullseye"
plots in order to explore the effect of these deletions on loop decay. Interestingly, we found that loops
appeared more punctate in both CTCF RNA binding mutants (Fig. 4J). This effect was especially
pronounced in the ZF1 mutant.

Taken together, these findings are consistent with a model where CTCF's RNA-binding domains
and the presence of bound RNAs results in more diffuse contacts between loop anchors, and thus to
enriched contacts among regulatory elements near the loop.

Discussion

By generating a Hi-C map with extraordinary sequencing depth (33 billion PE, or 9.9 terabases of
uniquely mapped sequence), we create the first fine-map of nuclear compartmentalization.

Our findings demonstrate that compartment intervals and compartment domains can be far
smaller than previously appreciated. This contrasts with the common hierarchical model of chromosome
organization in which compartments are partitioned into TADs and loops[6,11-13]. In fact, our results
indicate that compartment intervals can be so small that active DNA elements will localize with the A
compartment even when surrounded by inactive chromatin localizing in the B compartment (Fig. 5).

Strikingly, we find that essentially all distal enhancer elements lie in the A compartment. This
contrasts with earlier work, using coarse-resolution maps of compartmentalization, which only report
general enrichment of active distal enhancers in the A compartment, rather than as an absolute
characteristic of active enhancers[33,34]. Similarly, many previous studies have reported a coarse
enrichment of active genes in the A compartment[6], yet we find that essentially all active promoters lie in
the A compartment.

We also observe that the likelihood that a locus lies inside the A compartment declines as one
moves away from the promoter, along the gene body. Interestingly, we observe numerous genes with
discordant compartmentalization, where the TSS and TTS tend to be in different compartments. This
observation suggests that opposing compartments need not correspond to widely separated locations
within the nucleus. For instance, recent work indicates that compartments could be phase-separated
droplets[35], suggesting that the TSS and TTS of a gene with discordant compartmentalization might be
physically proximal within the nucleus, in neighboring A and B droplets (Fig. 5).

The finding that active promoters – specifically, active TSSs – are overwhelmingly localized in the
A compartments; that TTS compartment status correlates with RNAPII levels at the TTS; and that genes
with discordant compartmentalization tend to be transcriptionally paused is consistent with a model in
which RNAPII drives localization to the A compartment. Although a recent RNAPII degradation study
showed little effect on genome organization, these experiments did not achieve the sequencing depth

required to perform fine mapping of nuclear compartmentalization, nor to resolve phenomena such as
genes with discordant compartmentalization[36]. Alternatively, other components of the transcription
complex that travel along the gene body during transcription elongation may be responsible for
mediating interactions that assign sequences to the A compartment. In future studies, it will be of great
interest to examine how RNAPII and other components of the transcription complex impact genome
organization at the TSS and TTS separately.

We note that our data represent averages within the cellular population, and it is unclear where
each component lies during the transcriptional process itself. In the future, fine mapping of nuclear
compartments in single cells will be needed to decipher these dynamics. Moreover, we note that our
study did not attempt to study subcompartments or models with >=3 distinct compartment states[2,37],
which will be an important topic for future analyses.

Our ultra-deep Hi-C map also helped identify interesting properties of chromatin loops. In
particular, we observe that CTCF-mediated loops are highly diffuse, more so than would be predicted
based on polymer behavior alone (Fig. 5). Interestingly, this diffusivity is observed for loops that form by
extrusion, such as loops in human[2,24-27] and *C. elegans*[20,22,23], but is not observed for loops that are
believed to form by compartmentalization, such as the numerous *Pc*-associated loops observed in
Drosophila[14,21,29,30]. Intriguingly, variations in diffusivity between different loops could explain
differences in domains signal (See Supplemental Discussion, Fig. S5).

In vitro studies have found that large chromatin complexes can impede looping factors[38,39], and
cohesin was shown to build up near transcriptionally active regions[40]. Yet studies have also reported
independence of CTCF loops and transcription[36,41,42], bringing the relationship between transcription and
CTCF looping in question. Recently, it was shown that CTCF RNA-binding domains, ZF1 and ZF10, are
important for looping[32]. Our finding that loop-decay is altered in CTCF RNA-binding mutants supports
the argument that transcription can impact fine-scale chromatin organization in mammals, as does the
correlation between TTS compartmental domains and elongation status.

Our POSSUMM method, a novel numerical linear algebra algorithm for calculating principal
eigenvectors, is now available as part of the Juicer pipeline for Hi-C analysis. Our power analyses suggest
that fine mapping of nuclear compartments at sub-kilobase resolution becomes possible for maps
containing 7 billion contacts or more (See Supplemental Discussion, Fig. S6&S7). As sequencing costs
continue to decline, we expect that fine mapping of nuclear compartments will become increasingly
common.

Methods

Library Preparation, Initial Processing, and Quality Metrics

Hi-C libraries were prepared according to the published *in-situ* method[2]. The full map represents a
mixture of libraries prepared by digestion of various 4-cutter restriction enzymes, MboI, MseI, and NlaIII.
Reads were aligned to the hg19 genome, processed, Knight-Ruiz (KR) normalized using Juicer[9].
Subsampled Hi-C maps were created by uniform random selection of read-pairs from the 33.3 billion Hi-
C dataset. We provide a script for subsampling Hi-C data at https://github.com/JRowleyLab/HiCSampler.

Compartment Analysis

Compartments were identified using the A/B eigenvector of the Hi-C matrix using POSSUM. POSSUMM
can be downloaded from: https://github.com/aidenlab/EigenVector and is also now implemented in the
ENCODE version of the Juicer pipeline: https://github.com/ENCODE-DCC/hic-pipeline.

Introduction to PCA of Sparse, SUper Massive Matrices (POSSUM)

We note that the so-called "A/B compartment eigenvector" is simply the eigenvector of A corresponding
to its largest eigenvalue, where X is given by the Hi-C contact matrix. This is equivalent to the first
principal component in Principal Component Analysis. We note that in our case, X is a large, sparse
matrix, containing millions of rows, millions of columns, and tens of billions of nonzero entries (dubbed
a "Sparse, SUper Massive Matrix").

Suppose we seek to calculate the largest eigenpairs, λ_i, v_i of A in this case. Although X is sparse, we note
that both Y and A are dense matrices. Unfortunately, storing dense matrices with millions of rows and
columns in memory is impossible. Hence we cannot use any method for calculating the eigenvectors of
A that would require us to explicitly calculate either Y or A. Similarly, traditional sparse matrix methods
for eigendecomposition are not usable here, again because A - the correlation matrix we hope to
analyze - is a dense matrix.

Therefore, in order to calculate eigenvectors for A, we began by implementing a method that makes it
possible to calculate the matrix-vector product Av (where v is an arbitrary vector) using a sparse
representation of X, i.e., without explicitly computing either A or Y. See POSSUMM details below for a
more complete description.

Next, we note that there are many methods for calculating eigenvectors in which the input matrix only
appears via a matrix-vector product. These include the Power method, the Lanczos method, and their
many variants[43]. Thus, in principle, any of these methods - for which there are many implementations in
Fortran, C, C++, Matlab, and R - can be combined with the sparse Av product calculation described
above in order to calculate eigenpairs of A. In practice, methods combining these two approaches are
not available.

To the best of our knowledge, the sole exception is a method in the R package *irlba,* which was released
while this study was being performed. The details of this method are unpublished, but the method itself
is available at https://cran.r-project.org/web/packages/irlba/index.html. However, *irlba* cannot handle
cases where X has more than roughly two billion nonzero entries, which is exceeded in the present case.
It also does not enable parallelization, which limits performance in highly demanding settings.

POSSUMM combines sparse Av product calculation with the power method, is extremely memory-
efficient, and enables parallelization via multi-threading.

POSSUMM Details.

To identify compartments from sparse Hi-C matrices, we began by excluding all rows and columns with 0
variance. Let X be a matrix with column vectors $X^{(1)}, \dots, X^{(n)}$. Let $Y^{(i)} = (X^{(i)} - c_i)/\sigma_i$ $1 \le i \le n$,
where c_i is the mean of X_i and σ_i is its standard deviation. Let $Y = (Y^{(i)}, \dots, Y^{(n)})$ be an n x n matrix with
column vectors. The correlation matrix of X is $A = Y^T Y$ where Y^T is transposed Y. Since A is symmetric
and positive semi-definite it has n real eigenvalues $\lambda_1 \ge \lambda_2 \ge \cdots \ge \lambda_n \ge 0$ and n eigenvectors.
$v_1, \dots, v_n$ where $A v_i = \lambda_i v_i$.

These eigenvectors are a basis of R^n (i.e., a set of vectors which are independent and span the space) if
$\lambda_i \ne \lambda_j$ and $v_i \perp v_j$ (i.e., $v_i^T v_j = 0$). To compute v_1 using the power method (a.k.a power iterations),

suppose that $\lambda_1 > \lambda_2$ and let x_0 be any nonzero vector in R^n, we define the recursive relation:

$x_{k+1} = A x_k = A^{k+1} x_0$. We can represent x_0 as $x_0 = a_1 v_1 + \cdots + a_n v_n$ and therefore $A^k x_0 =$

$a_1 \lambda_1^k v_1 + \cdots + a_n \lambda_n^k v_n = \lambda_1^k (a_1 v_1 + a_2 \left(\frac{\lambda_2}{\lambda_1}\right)^k v_2 + \cdots + a_n \left(\frac{\lambda_n}{\lambda_1}\right)^k v_n)$. Once we have estimates of the

eigenvector and the two largest eigenvalues, we can estimate the error given that $\left\lVert v - v_1 \right\rVert \leq$

$\frac{\lVert Av - \lambda_1 v \rVert}{\lVert \lambda_1 - \lambda_2 \rVert}$. To find an estimate of λ_2 we know that $v_2 \perp v_1$ and $\lVert v_1 \rVert = 1$. Let x_0 be any vector and let

$x_{k+1} = A(x_k - c_k v_1)$ where $c_k = v_1^T x_k$ (and then $(x_k - c_k v_1) \perp v_1$). If $\lambda^{(k)}_2 = \lVert A x_k \rVert / \lVert x_k \rVert$ the

using the same argument as before $\lambda^{(k)}_2 \rightarrow \lambda_2$ as $k \rightarrow \infty$. This is true even if $\lambda_2 \approx \lambda_3$ (x_k may not

converge to v_2, but λ_2 wil converge to λ_2). In this way we have an estimate of λ_1 and λ_2 and may

estimate the error in v. Since $A = Y^T Y, Ax = Y^T(Yx) = ((Yx)^T Y)^T$, we do not need to compute A

(which has the complexity of $O(n^3)$). We used two matrix vector products at every iteration (which

have the complexity of the number of nonzero elements in Y which is at most *O(n)*). Moreover, if X is

large a naïve multiplication of a vector by a matrix can still take a long time and storing Y may require a

large amount of memory. For example, to store human chr1 at 1 kb resolution (where $n \approx 250000$) 500

GB of RAM would be required just to store Y. With sparse implementation we recall that $Y =$

$(Y^{(i)}, \ldots, Y^{(n)})$ where $Y^{(i)} = \frac{X^{(i)} - c_i - c_i}{\sigma_i} = \frac{X^{(i)}}{\sigma_i} - \frac{c_i}{\sigma_i}$. While $\frac{X^{(i)}}{\sigma_i}$ is sparse, $\frac{X^{(i)}}{\sigma_i} - \frac{c_i}{\sigma_i}$ is not. In lieu of explicit

computation, let $1 = (1,1,\ldots,1)^T$ then $Y^{(i)} = \frac{X^{(i)}}{\sigma_i} - \frac{c_i}{\sigma_i} 11$ and then $Y = XS - 1 \cdot 1 \cdot r^T$ where

$S = [1/\sigma_1 \ddots 1/\sigma_n]_n$ and $r = [c_1/\sigma_1 \vdots, \ldots, c_n/\sigma_n]^T$ and then $Yx = (X \cdot S)x - 1 \cdot r^T \cdot x$. Let $Z = X \cdot S$.

Since $r^T x = \sum_{i=1}^n r_i x_i$, $Yx = Zx - (\sum_{i=1}^n x_i r_i)1$. Since Z is as sparse as X we can do everything with

sparse matrices as $x^T Y = x^T Z - (x^T 1)r^T = x^T Z - (\sum_{i=1}^n x_i)r^T$. Projected time and memory usage

were calculated by fitting a power decay curve, R^2 of fit = 0.95 for time, and R^2 of fit = 0.98 for memory

usage.

After compartment calling, chromatin marks were profiled at features that overlap A or B compartments

by overlapping with ChIP-seq peaks and by using average signal profiles created by pyBigWig from the

deepTools package[44]. ChIP-seq peaks and bigwig files were obtained from the ENCODE Roadmap

Epigenomics project[45]. We filtered promoters with bivalent marks as active genes that had 2-fold higher

H3K27me3 or H3K9me3 signal compared to the average at promoters. Contiguous compartment domain

sizes were calculated by requiring at least two consecutive bins to have the same sign in the

eigenvector. To create profiles of A compartmental status along genes, we assigned genes to elongating,

mid, and paused. Elongation status was determined by RPKM GRO-seq signal within 250 bp of the TSS

compared to the gene body, excluding 500 bp from the TSS. Differences between Promoter – Gene Body

GRO-seq signal were ranked and placed into three equal categories considering only genes >= 20 kb in

size.

Loop Analysis

Loops were identified by HiCCUPS[2] or SIP[20] at multiple resolutions. For HiCCUPS, we used parameters –

m 2000 –r 500,1000,5000,10000 –f .05,.05.05.05. For SIP we used an FDR 0.05 at each resolution with

the parameters for resolutions of 500 bp; -d 15 –g 3.0; 1 kb: -d 17 –g 2.5; 5 kb: -d 6 –g 1.5; and 10 kb: -d

5 –g 1.3. Loops called by both methods were combined by placing all loops into 10 kb bins, and if

HiCCUPS and SIP called the same loop within the 10 kb bin, then only one instance of this loop was kept.

Loops in subsampled maps were overlapped with loops called in the full 20.3 billion map if the loop was

within +/- 25 kb of each other. Overlap of loops with CTCF was done using a published list of CTCF ChIP-

seq peaks and motifs[2]. Central 1 kb bins were assigned to those where we could unambiguously assign a

CTCF ChIP-seq peak to a unique bin at motifs in convergent orientation. Only loops with unambiguous

CTCF assignment were used in decay analysis. Bullseye plots were created using SIPMeta[20] and the
decay was calculated as the average at each Manhattan distance (ring) moving away from the central
bin. These values were plotted as a ratio to the central bin's signal. The central bin of loops called at AUC
values were computed using Simpson's rule. Loops were placed into five equally sized categories
(quintiles) based on AUC values. AUC values between WT, ΔZF1, and ΔZF10 were normalized by the
diagonal to account for differences in the expected decay. The decay percentage rate of change listed in
the main text was calculated by averaging the number of kb between each 10% loss of signal.

Fit-Hi-C[31] interactions were identified in 1 kb bin-pairs with an FDR 0.05. 3D loop models were created
with Pastis[46] using the raw Hi-C matrix. Models were visualized in ChimeraX[47].

Comparison with Other Datasets

Hi-C read-pairs from CTCF ΔZF1, ΔZF1, and wild-type were downloaded from GSE125595[32] and
processed with juicer to the mm10 genome. Hi-C maps from the *D. melanogaster* dm6 genome and the
C. elegans ce10 genome were obtained from our previously published work[20,21]. Hi-C maps used in our
metric comparison are listed in Tables S2 and S3.

Enhancers were downloaded from DENdb[18] and active enhancers were defined as those that overlap
with H3K27ac ChIP-seq peaks in GM12878. Histone modification ChIP-seq data was obtained from the
ENCODE reference epigenome series (ENCSR977QPF) and RNAPII ChIP-seq peaks were combined from
RNAPII, RNAPIISer2ph, and RNAPIISer5ph (ENCSR447YYN and ENCSR000DZK)[19,48], with overlapping
peaks merged into a single peak. GRO-seq data from GM12878 was downloaded from GSM1480326[49],
and chromHMM states for GM12878 were downloaded from the Roadmap Epigenomics Project[45].

Data and Code Availability

Hi-C data can be downloaded from ENCODE Accession: ENCSXXXXX. Our programs for subsampling,
noise estimation, and eigenvector calculation on sparse matrices can be downloaded from
https://github.com/JRowleyLab/HiCSampler, https://github.com/JRowleyLab/HiCNoiseMeasurer, and
https://github.com/aidenlab/EigenVector. These are open source and include source code as well as
implementations in python and C++.

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Author Contributions

559 H.G prepared Hi-C libraries for sequencing with samples prepared by S.K., K.M., M.E.T, and J.S.S. H.G.,
560 H.H., Y.E., A. Krishna, A. Kalluchi, M.P., S.S.P.R., O.D, D.U., M.H.N., and E.D. contributed ideas and in
561 performing various quality metrics. M.J. and G.C. created 3D loop models. M.O. created POSSUM.
562 D.H.P., V.G.C, W.S.N, E.L.A., and M.J.R. supervised the work and wrote the manuscript. All other analyses
563 were performed by M.J.R.

Ethics Declarations

565 We declare that the authors have no competing interests in this work.

Figure Legends

Figure 1. By combining ultra-deep Hi-C and POSSUMM, we generated a fine map of nuclear compartmentalization achieving 500bp resolution.

A) Schematic representing the total mapped read-pairs in the current study compared to earlier published Hi-C studies.

B) Example locus showing Hi-C signal in 500 bp bins in our full map with 20.3 billion intrachromosomal read-pairs (left) and when read-pairs are subsampled to 1 billion (right).

C) Example of compartment interactions in a Hi-C map identified by the eigenvector in 500 bp bins (bottom track). Black track displays transcription measured by GRO-seq. Black square represents the region shown in Fig. 1D.

D) Zoomed in view of a compartment domain.

E) Overview of the power method and POSSUM for calculating the eigenvector. See Methods for details.

Figure 2. Nearly all active TSSs and Enhancers localize to kilobase-scale A compartments

A) Cumulative fraction of compartment domain sizes when identified at 500 bp resolution.

B) Percentage of active gene promoters, proximal enhancers, and distal enhancers assigned to A (green)
or B (purple) compartment domains when identified by the 500 bp compartment eigenvector.

C) Example of small compartment domains only identifiable at high-resolution (red asterisks). Log
transformed and distance normalized Hi-C map is shown alongside the eigenvector tracks at various bin
sizes.

D) Examples an active enhancers denoted by H3K27ac and H3K4me1 signal localizing to the A
compartment and surrounded by the B compartment.

E) Examples an active promoters denoted by GRO-seq signal localizing to the A compartment and
surrounded by the B compartment.

Figure 3. Many genes exhibit discordant compartmentalization.

A-B) Examples of genes of various sizes where the TSS is in the A compartment while the TTS is in the B
compartment. GRO-seq signal is shown as an indicator of the gene's transcription status.

C) Scaled average profiles of the A compartment signal (positive eigenvector) relative to the TSS for
short (blue), mid-sized (gold), large (pink), and randomly selected (black) genes.

D) Percentage of TTSs that localize to the B compartment for genes of various sizes (left).

E) ChIP-seq signal at the TTS of discordant A/B genes vs. concordant A/A genes. Genes are sorted by the
TTS compartmental signal.

F) Scaled average profiles of the A compartment signal (positive eigenvector) relative to the TSS for
elongating (blue), mid (red), paused (black), or randomly selected (grey) genes.

G) Percentage of TTs that localize to the B compartment for paused, mid, or elongating genes.

H) Top: Simple diagram of A compartment signal relative to gene size. Bottom: Diagram of TSS and TTS
localization to the A compartment depending on gene size and elongation status.

Figure 4. CTCF loop-decay enhances proximal interactions and is dependent on RNA-binding domains.

A) Example of broad signal enrichment near CTCF loops when binned at 1 kb.

B) Average signal at CTCF loops when binned at 10, 5, or 1 kb, centered on convergent CTCF anchors.

C) Average Hi-C signal in 1 kb bins at each radial distance away from the CTCF loop anchors (rainbow).
Average signal of the diagonal decay is shown for reference (grey) to estimate interactions due to
polymeric distance. AUC=area under the curve.

D) Example of punctate signal enrichment at Pc loops in *D. melanogaster* when binned at 1 kb.

E) Average signal at *D. melanogaster* Pc loops when binned at 10, 5, or 1 kb.

F) Average Hi-C signal in 1 kb bins at each radial distance away from human CTCF loop anchors (blue) vs.
D. melanogaster Pc loops (orange), and *C. elegans* X-chromosome loops (green). Average signal at the *C.*
elegans Hi-C diagonal is shown for reference (grey). AUC=area under the curve.

G) Enrichment of Fit-Hi-C enhancer-promoter interactions within 100 kb of loops inside the loop (blue)
or crossing over loop boundaries (green). Values are shown as enrichment vs random regions of equal
size and number as loops.

H) Diagram of how CTCF loops can shorten distances between enhancers (orange) and promoters (blue)
even when both are located outside of the loop.

I) Average GRO-seq signal at CTCF loop anchors and neighboring loci for loops divided into 5 distinct
decay categories.

J) Average Hi-C signal in WT (left), ΔZF1 (middle), or ΔZF10 (right) CTCF mutants at CTCF loops. AUC=area
under the curve

Figure 5 Sub-genic compartmentalization and diffuse CTCF looping organize the human genome.

Diagram depicting localization of active enhancers and TSSs to the A compartment, while TTSs are
oriented to the B compartment dependent on transcription elongation status. This sub-genic and precise
enhancer compartmentalization combines with diffuse CTCF loops to mediate genome organization.

A Hi-C Contact Sequencing Depth

~5 Bil   ~33 Bil

~10 Mil

First Hi-C
Map (2009)   Rao et al.,
             (2014)   This Study

B 500 bp Resolution

chr1:17.35-17.65 Mb

11   1

20.3e9   1e9

Intrachromosomal
Read-Pairs

C chr3: 153-185 Mb

chr3: 153-161 Mb

Distance Norm. Hi-C

GRO-seq

Eigen   A
500 bp   B

D chr3-153.8-154.15 Mb

GRO-seq

DHX36

A
B

E   Power Method

                                                    Key   Sparse Matrix   Scalar
                                                           Dense Matrices
                                                           Column Vector   Row Vector

rescaled
contact
matrix

1   col
     means   v

POSSUM

Figure 1

A

Cumulative Fraction

96% <= 100 kb
99% <= 1 Mb

Compartment Size (kb)

B

Active Promoters
(Gene RNA-seq TPM > 1)

5%

95%

A vs B

Proximal Active Enhancers
(<=10 kb from TSS)

3%

97%

A vs B

Distal Active Enhancers
(>10 kb from TSS)

5%

95%

A vs B

C

GRO-seq
Genes
500 bp
1 kb
5 kb
10 kb
25 kb
50 kb
100 kb
250 kb
500 kb
1 mb

Eigenvector

ZNF138

500 bp
1 kb
5 kb

Eigenvector

1 mb
500 kb
250 kb
100 kb
50 kb
25 kb
10 kb
5 kb
1 kb
500 bp

GRO-seq

chr7: 63.5-64.4 Mb

Log Dist. Norm. Hi-C

2
0
-2

D

Distal Active Enhancers

H3K27ac
H3K4me1
A vs B
CSMD3
chr8:114.3-116 mb

H3K27ac
H3K4me1
A vs B
No Genes in Area
chr21:33.46-33.56 mb

E

Active Genes Inside Large Inactive Region

GRO-seq
A vs B
chr10:52.5-54.5 Mb

CSTF2T
chr10:53.450-53.465 Mb

GRO-seq
A vs B
chr2:16-17.6 Mb

FAM49A
chr2:16.72-16.82 Mb

Figure 2

Figure 3

Figure 4

Figure 5