Fine-mapping methods for complex traits: essential adaptations for samples of related individuals

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Abstract

Fine-mapping causal variants from GWAS loci is challenging in populations with substantial relatedness, such as livestock, as standard methods often assume unrelatedness, leading to poor fine-mapping accuracy. Here, we introduce a comprehensive Bayesian framework to address this. Our approach features BFMAP-SSS for individual-level data, which uses a linear mixed model (LMM) and shotgun stochastic search with simulated annealing. For summary statistics, we develop FINEMAP-adj and SuSiE-adj, novel strategies that directly use standard FINEMAP and SuSiE for samples of related individuals by employing LMM-derived inputs (particularly a relatedness-adjusted linkage disequilibrium matrix). Furthermore, gene-level posterior inclusion probability (PIP_{gene}) is proposed to enhance detection power by aggregating variant signals. Extensive simulations based on pig genotypes show our methods substantially outperform existing tools (FINEMAP, SuSiE, FINEMAP-inf, SuSiE-inf, and GCTA-COJO) in samples of related individuals, achieving notable improvements in fine-mapping accuracy (e.g., up to several-fold increases in AUPRC). PIP_{gene} markedly improves candidate gene identification. Application to

27 Duroc pig traits demonstrates practical utility. This work provides robust, validated methods and

28 associated software and scripts for accurate fine-mapping in populations with complex relatedness.

29 **Key words:** fine-mapping; complex trait; Bayesian; related individuals

Introduction

Genome-wide association studies (GWAS) have successfully discovered many genetic

associations with complex traits and diseases (1). However, these studies primarily identify

associated genomic regions rather than pinpoint the actual causal variants, largely due to linkage

disequilibrium (LD), whereby non-causal variants are correlated with true causal variants (2, 3).

Such associated regions often contain many SNPs, the majority of which have no direct effect on

the trait (4), thereby complicating downstream functional validation. Fine-mapping aims to address

this by statistically prioritizing the most likely causal variants within a GWAS-identified locus,

assuming at least one such variant exists (5) and thus narrowing the field for functional studies.

Statistical fine-mapping methods typically account for LD structure to identify a small set

of putative causal variants, effectively treating the problem as variable selection in a regression

model (6, 7). Given m SNPs in a region, 2^m possible causal models exist, making exhaustive

evaluation computationally prohibitive for densely genotyped regions. Early approaches like

conditional stepwise selection (e.g., GCTA-COJO) (8) identify independent signals but can be

suboptimal, particularly when multiple causal variants in LD are present or when a non-causal

variant strongly tags multiple causal variants (5, 7). Methods like CAVIAR (7) and its extension

CAVIARBF (9) improved upon this by jointly modeling multiple variants and exhaustively

evaluating all possible models with up to a pre-specified small number of causal variants, but faced

computational limitations with larger regions or higher numbers of true causal variants. To address

this challenge, newer approaches were developed. FINEMAP (10) employs shotgun stochastic

search (SSS) (11) to efficiently explore the vast model space, while SuSiE uses Iterative Bayesian

Stepwise Selection (IBSS) with the "Sum of Single Effects" model (12, 13) to search multiple

effects. These methods have become widely adopted due to their improved computational

efficiency. Recent extensions like FINEMAP-inf and SuSiE-inf (14) further refine these by

attempting to model infinitesimal effects within the candidate region.

Despite these advancements, a major limitation of most existing fine-mapping methods,

particularly those based on summary statistics, is their foundation in linear regression models that

assume samples of unrelated individuals. The use of related individuals violates the underlying

model assumption of unrelatedness, potentially distorting LD and subsequent causal variant

identification. While it has become standard to use summary statistics derived from linear mixed

models (LMMs) that account for relatedness and/or infinitesimal background at the GWAS stage

(15, 16), the downstream fine-mapping tools often still do not correctly incorporate this relatedness

structure into their own models. This critical issue of appropriately adapting fine-mapping for

related individuals has particularly been overlooked in livestock genetics, where populations

typically exhibit substantial and complex inter-individual relatedness due to breeding practices.

This study introduces a comprehensive Bayesian fine-mapping framework specifically

designed to address these challenges in samples of related individuals. We aim to demonstrate that

existing summary-statistics-based fine-mapping methods cannot be naively applied to samples of

related individuals and develop comprehensive methodological solutions for related samples. We

build upon our previously developed BFMAP approach, which uses an LMM for individual-level

data and originally employed forward selection (BFMAP-Forward) (17). Here, we enhance the

BFMAP framework by implementing a more robust model exploration strategy, BFMAP-Shotgun

Stochastic Search (BFMAP-SSS), to better handle scenarios with highly correlated causal variants.

Recognizing the widespread use of summary statistics, we further develop novel adaptation

strategies, FINEMAP-adj and SuSiE-adj. These approaches enable the direct use of standard

FINEMAP and SuSiE software with summary statistics obtained from related individuals by

inputting LMM-derived inputs and a relatedness-adjusted LD matrix. Finally, to improve detection

power in genomic regions with challenging LD patterns, as is common in livestock, we propose

and validate the use of gene-level posterior inclusion probability (PIP_{gene}) that aggregates variant-

level evidence.

Through simulations based on real livestock genotypes and application to economically

important traits in Duroc pigs, we demonstrate both the inadequacy of naively applying existing

summary-statistics methods to related individuals and the substantial improvements offered by our

comprehensive methodological solutions (BFMAP-SSS, FINEMAP-adj, SuSiE-adj, and PIPgene)

in fine-mapping performance. This work provides both novel methodologies and practical

adaptations essential for robust identification of causal variants and trait-associated genes in

samples with complex genetic relatedness.

Materials and methods

Fine-mapping with unrelated individuals

89   For a sample of unrelated individuals, the genetic fine-mapping analysis can be represented using

90   the following linear model:

$$\mathbf{y} = \mathbf{Xb} + \mathbf{e} \text{ with } \mathbf{b} \sim \mathcal{N}(0, \mathbf{I}\varphi\sigma_e^2) \text{ and } \mathbf{e} \sim \mathcal{N}(0, \mathbf{I}\sigma_e^2), \tag{1}$$

where $\mathbf{y}$ is an n-vector of covariate-adjusted phenotypes for n individuals, $\mathbf{X}$ is an n-by-m matrix

of standardized genotypes for n individuals and m SNPs in a genomic region of interest, $\mathbf{b}$ is an m-

vector of joint SNP effects, $\mathbf{e}$ is an n-vector of residual effects, and φ and σ_e^2 are hyperparameters

related to variance components. Specifically, φ represents the ratio of per-SNP genetic variance to

residual variance (σ_e^2), and we can set $\varphi=0.01$ to specify a moderate prior variance for SNP effects.

Note that model (1) does not account for genetic relatedness between individuals, restricting its

application to samples of unrelated individuals.

Model (1) can be expressed as follows:

$$\mathbf{y} \sim \mathcal{N}(0, \sigma_e^2(\mathbf{XX}^{\mathrm{T}}\varphi + \mathbf{I})), \tag{2}$$

101   which is further transformed to $\mathbf{X}^{\mathrm{T}}\mathbf{y}/\sqrt{n\sigma_e^2} \sim \mathcal{N}(0, \mathbf{X}^{\mathrm{T}}\mathbf{XX}^{\mathrm{T}}\mathbf{X}\varphi/n + \mathbf{X}^{\mathrm{T}}\mathbf{X}/n)$. Denoting $\mathbf{z} =$

102    $\mathbf{X}^{\mathrm{T}}\mathbf{y}/\sqrt{n\sigma_e^2}$ and $\mathbf{\Sigma} = \mathbf{X}^{\mathrm{T}}\mathbf{X}/n$ (we ignore the error introduced by the estimation of σ_e^2 and the use

103   of n instead of $n-1$), we have

$$\mathbf{z} \sim \mathcal{N}(0, \mathbf{\Sigma\Sigma}\varphi n + \mathbf{\Sigma}), \tag{3}$$

105   where $\mathbf{z}$ is an m-vector of z-scores from linear regression associations and $\mathbf{\Sigma}$ is an m-by-m matrix

106   of Pearson's correlations between m SNPs. It is important to note that model (3) holds for any set

107   of SNPs in the genomic region. For a set of SNPs (denoted as s), let $\mathbf{z}_s$ and $\mathbf{\Sigma}_s$ represent the z-

108   score vector and correlation matrix, respectively. Given model (3), we can compute the Bayes

109   factor of the model (denoted as M) for s over the reduced model including no SNPs:

$$\mathrm{BF}_M = |n\varphi\mathbf{\Sigma}_s + \mathbf{I}|^{-\frac{1}{2}}\exp\left(\frac{1}{2}\mathbf{z}_s^{\mathrm{T}}(\mathbf{I}n^{-1}\varphi^{-1} + \mathbf{\Sigma}_s)^{-1}\mathbf{z}_s\right). \tag{4}$$

Equation (4) demonstrates the computation of Bayes factors for multi-SNP models using

GWAS summary statistics and reference panel SNP correlations. This approach forms the

foundation for genetic fine-mapping tools like CAVIARBF (9) and FINEMAP (10). Compared to

individual-level data calculations under model (2), this method offers enhanced computational

efficiency, particularly when leveraging reference panels like the 1000 Genomes Project (18) for

SNP correlation estimation. However, like model (2), this approach is restricted to unrelated

individuals.

Genetic fine-mapping is fundamentally a model selection problem. Although some fine-

mapping methods, such as GCTA-COJO (8), use *P*-values rather than Bayes factors, they maintain

consistency with Bayesian approaches. Specifically, when GCTA-COJO identifies a small

conditional *P*-value for a SNP, this typically corresponds to a substantially larger log(*BF*) for the

model including this SNP than for the comparable model without this SNP. Bayesian fine-mapping

methods, such as CAVIARBF (9) and FINEMAP (10), evaluate sufficiently many multi-SNP

models to compute posterior inclusion probability (PIP) for each variant in the candidate genomic

region.

SuSiE (13) introduces a novel approach by decomposing the overall genetic effect into a

sum of individual single effects, rather than explicitly evaluating different combinations of

multiple SNPs. This computational innovation, combined with the implementation of variational

Bayes for approximate posterior inference, enables SuSiE to identify multiple causal SNPs with

high computational efficiency. Despite these methodological advances, SuSiE operates within the

same linear framework as CAVIARBF and FINEMAP.

Fine-mapping with related individuals: individual-level data

We previously developed a Bayesian framework for genetic fine-mapping with related individuals,

which we refer to as BFMAP (17). BFMAP uses individual-level genotype and phenotype data

based on the following linear mixed model:

$$\mathbf{y} = \mathbf{X}\mathbf{b} + \mathbf{g} + \mathbf{e} \text{ with } \mathbf{b} \sim \mathcal{N}(0, \mathbf{I}\varphi\sigma_e^2), \mathbf{g} \sim \mathcal{N}(0, \mathbf{G}\eta\sigma_e^2), \text{ and } \mathbf{e} \sim \mathcal{N}(0, \mathbf{I}\sigma_e^2). \quad (5)$$

Model (5) extends model (1) by including an additional random-effect term, **g**, to account for

genetic relatedness and whole-genome infinitesimal effects. **G** represents the genomic relationship

matrix (GRM) (19), and η denotes the ratio of additive genetic variance to residual variance (σ_e^2).

Other terms remain as defined in model (1).

For model implementation, we need to specify both η and σ_e^2. When the effects of

candidate variants (**Xb**) account for only a small proportion of phenotypic variance (typically true

when modeling variants from a small genomic region), we can set the value of η based on the SNP

heritability (h^2) by $\eta = h^2/(1-h^2)$. In practice, we can use the SNP h^2 estimate from the null model

without the **Xb** term to determine η. For the residual variance σ_e^2, we assign the non-informative

Jeffrey's prior, $P(\sigma_e^2) \propto 1/\sigma_e^2$.

For any model M that specifies a set of SNPs to be included, let s denote this SNP set.

Given $D = \{\mathbf{y}, \mathbf{X}, \mathbf{G}, \varphi, \eta\}$, we have the following equation for the marginal likelihood after

integrating out σ_e^2:

$$P(D|M) \propto P(\mathbf{y}|\mathbf{X}, \mathbf{G}, \varphi, \eta, M) \propto (\mathbf{y}^{\mathrm{T}}(\varphi\,\mathbf{X}_s\mathbf{X}_s^{\mathrm{T}} + \eta\mathbf{G} + \mathbf{I})^{-1}\mathbf{y})^{-\frac{1}{2}n}|\varphi\,\mathbf{X}_s\mathbf{X}_s^{\mathrm{T}} + \eta\mathbf{G} + \mathbf{I}|^{-\frac{1}{2}}, \quad (6)$$

where $\mathbf{X}_s$ denotes the genotype matrix for SNP set s. The effective computation of $P(D|M)$ has

been detailed in our previous study (17).

Computing $P(D|M)$ for every possible model is computationally infeasible. We have

implemented two methods in BFMAP to facilitate model selection: one based on forward selection

and the other using shotgun stochastic search (SSS) (11), which we refer to as BFMAP-Forward

and BFMAP-SSS, respectively. The implementation of BFMAP-Forward has been detailed in our

previous study (17). The forward selection procedure sequentially adds independent signals to the

model, repositions them for refinement, and identifies variants related to each signal. For BFMAP-

SSS, we largely follow the implementation in FINEMAP (10). SSS efficiently explores the vast

model space by evaluating neighboring models at each iteration. However, a naïve implementation

may fail to discover causal variants even with a very long chain for certain LD structures. To

address this limitation, we incorporate simulated annealing (20) to ensure more thorough search.

We apply the following linear cooling scheme:

$$T_k = T_0 - k \cdot \Delta_T, \tag{7}$$

where T_0 is the initial temperature, T_k is the temperature at the k-th step, and Δ_T is the temperature

decrement per step. For all analyses in this study, T_0 was set to 100, and Δ_T was fixed at 1. We

performed 100 SSS iterations at each temperature step and set the final temperature to 1. An

additional 100 SSS iterations were conducted at this final temperature to ensure thorough

exploration of the model space.

Fine-mapping with related individuals: summary statistics

In this section, we present a summary-statistics-based fine-mapping method for related individuals,

following the framework of BFMAP (17). Denoting $\mathbf{H} = \mathbf{G}\eta + \mathbf{I}$, we transform model (5) to:

$$\mathbf{X}^T\mathbf{H}^{-1}\mathbf{y} \sim \mathcal{N}\left(0, \sigma_e^2(\mathbf{X}^T\mathbf{H}^{-1}\mathbf{X}\mathbf{X}^T\mathbf{H}^{-1}\mathbf{X}\varphi + \mathbf{X}^T\mathbf{H}^{-1}\mathbf{X})\right). \tag{8}$$

174   Defining a diagonal matrix $\mathbf{D} = \mathrm{diag}(\mathbf{X}^T\mathbf{H}^{-1}\mathbf{X})$ and an m-by-m matrix $\widetilde{\boldsymbol{\Sigma}} = \mathbf{D}^{-1/2}\mathbf{X}^T\mathbf{H}^{-1}\mathbf{X}\mathbf{D}^{-1/2}$,

175   we obtain from (8):

$$\mathbf{z} \sim \mathcal{N}\left(0, \widetilde{\boldsymbol{\Sigma}}\mathbf{D}\widetilde{\boldsymbol{\Sigma}}\varphi + \widetilde{\boldsymbol{\Sigma}}\right), \tag{9}$$

177   where $\mathbf{z} = (\mathbf{D}\sigma_e^2)^{-1/2}\mathbf{X}^T\mathbf{H}^{-1}\mathbf{y}$ (that is, an m-vector of z-scores from linear mixed model

178   associations). For a set of SNPs (denoted as s) in a candidate genomic region, we can readily derive

179   the Bayes factor of the model (denoted as M) for s over the reduced model including no SNPs:

$$180 \qquad \mathrm{BF}_M = \left| \mathbf{D}_s \widetilde{\boldsymbol{\Sigma}}_s \varphi + \mathbf{I} \right|^{-\frac{1}{2}} \exp \left(\tfrac{1}{2} \mathbf{z}_s^{\mathrm{T}} \left(\mathbf{D}_s^{-1} \varphi^{-1} + \widetilde{\boldsymbol{\Sigma}}_s \right)^{-1} \mathbf{z}_s \right), \qquad (10)$$

where $\mathbf{z}_s$, $\mathbf{D}_s$, and $\widetilde{\boldsymbol{\Sigma}}_s$ represent $\mathbf{z}$, $\mathbf{D}$, and $\widetilde{\boldsymbol{\Sigma}}$, respectively, corresponding to SNP set s.

It is important to clarify the treatment of σ_e^2 in equation (10). While our BFMAP

framework (e.g., equation (6)) involves integrating out σ_e^2 using its Jeffrey's prior, the z-scores

used as input for equation (10) inherently treat σ_e^2 as a fixed quantity. This is because z-scores are

standardized statistics that already incorporate an estimate of σ_e^2. However, this difference in

treatment is generally of little practical consequence. For reasonably large samples ($n > 1{,}000$),

the estimate of σ_e^2 is highly precise. Therefore, using z-scores that embed a point estimate of σ_e^2

typically yields results very similar to those that would be obtained from a full Bayesian integration

of σ_e^2.

Equation (10) has a similar form to equation (4). Specifically, while the genotype

correlation matrix in equation (4) for unrelated individuals is defined as $\boldsymbol{\Sigma} = \mathbf{X}'\mathbf{X}/n$, this is

replaced in equation (10) for related individuals by $\widetilde{\boldsymbol{\Sigma}} = \mathbf{D}^{-1/2}\mathbf{X}'\mathbf{H}^{-1}\mathbf{X}\mathbf{D}^{-1/2}$. $\widetilde{\boldsymbol{\Sigma}}$ can be regarded

as relatedness-adjusted genotype correlations, which may substantially differ from $\boldsymbol{\Sigma}$. Using $\widetilde{\boldsymbol{\Sigma}}$

instead of $\boldsymbol{\Sigma}$ is critical for fine-mapping with related individuals. Misuse of unadjusted correlations

can lead to poor performance.

Applying the approximation $\mathbf{D} \approx \mathbf{I}\tilde{n}$ (where $\tilde{n}$ is the average of the diagonal elements of $\mathbf{D}$

and $\mathbf{I}$ is the identity matrix) to equation (10) transforms it into equation (11):

$$198 \qquad \mathrm{BF}_M = \left| \tilde{n}\varphi \widetilde{\boldsymbol{\Sigma}}_s + \mathbf{I} \right|^{-\frac{1}{2}} \exp \left(\tfrac{1}{2} \mathbf{z}_s^{\mathrm{T}} \left(\mathbf{I}\tilde{n}^{-1} \varphi^{-1} + \widetilde{\boldsymbol{\Sigma}}_s \right)^{-1} \mathbf{z}_s \right), \qquad (11)$$

which has a structural form the same as equation (4). This approximation mirrors that used by

GRAMMAR-Gamma (21), $\mathbf{X}_j^{\mathrm{T}}\mathbf{H}^{-1}\mathbf{X}_j \approx c\mathbf{X}_j^{\mathrm{T}}\mathbf{X}_j = cn$, where $\mathbf{X}_j$ represents the vector of

standardized genotypes for SNP j and c is a constant across all SNPs. The structural similarity

between equations (11) and (4) enables direct use of existing summary-statistics-based fine-

mapping tools (e.g., FINEMAP and SuSiE) for related individuals. The use involves two steps: 1)

calculate $\mathbf{z}$, $\tilde{n}$, and $\widetilde{\boldsymbol{\Sigma}}$ as described in this section, and 2) input these as z-scores, sample size, and

LD matrix, respectively, into FINEMAP and SuSiE. We refer to these adapted methods as

FINEMAP-adj and SuSiE-adj.

Posterior probability metrics

208   Given the Bayes factor BF_M or the marginal likelihood $P(D|M)$ of model M (which defines a

209   specific set of candidate causal SNPs, s), its posterior model probability is calculated as:

$$P(M|D) = \frac{P(D|M)P(M)}{\sum_{M' \in \Gamma} P(D|M')P(M')} = \frac{\text{BF}_M P(M)}{\sum_{M' \in \Gamma} \text{BF}_{M'} P(M')}, \tag{12}$$

where Γ represents the model space and M' represents any individual model in the model space.

We use a standard binomial prior, $P(M) = \pi^{|M|}(1-\pi)^{m-|M|}$, to induce sparsity in BFMAP,

where $|M|$ is the model size (number of SNPs in M) and π is the prior probability that a SNP is

causal. This prior implies an expected model size of $m\pi$. Following standard fine-mapping practice

(9, 10), π is set to $1/m$, reflecting an expectation of one causal variant *a priori*.

The posterior inclusion probability (PIP) quantifies the probability that a specific SNP has

a non-zero effect, given the observed data and priors (22). For SNP j, the PIP is computed as:

$$\text{PIP}_j = \sum_{M \in \Gamma} \mathbb{I}(j \in M) P(M|D), \tag{13}$$

where $\mathbb{I}(j \in M)$ is an indicator function returning 1 if j is included in model M and 0 otherwise.

This definition of PIP is used by methods that explore a broad model space, such as FINEMAP,

SuSiE, FINEMAP-inf, SuSiE-inf, FINEMAP-adj, SuSiE-adj, and BFMAP-SSS.

Our BFMAP-Forward implementation, however, operates via a stepwise forward selection

procedure. Consequently, it calculates a posterior conditional inclusion probability (PCIP). A

variant's PCIP is the posterior probability of the variant having a non-zero effect, conditional on

the set of variants already incorporated into the model. While PCIPs are by definition conditional

(unlike marginal PIPs), they serve as the direct analogue to PIPs for BFMAP-Forward throughout

this study.

Finally, to aggregate evidence at the gene level, we propose gene-level PIP (PIP_{gene}),

defined as the posterior probability that a given gene harbors at least one non-zero-effect variant.

This metric is computed by summing the posterior probabilities of all models containing at least

one SNP within the gene:

$$\text{PIP}_{\text{gene}} = \sum_{M \in \Gamma} \mathbb{I}(\text{gene} \cap M \neq \emptyset) P(M|D), \qquad (14)$$

where $\mathbb{I}(\text{gene} \cap M \neq \emptyset)$ indicates whether any SNP in the gene is included in model M. This

gene-level aggregation offers a complementary perspective involving a trade-off between

localization precision and power. For PIP_{gene} calculation, gene boundaries were defined using

Ensembl annotations and extended by 3kb upstream and downstream to include potential

regulatory regions.

Data simulation

We evaluated fine-mapping methods using genotype data from 31,301 Duroc pigs provided by

Smithfield Premium Genetics (Roanoke Rapids, NC, USA). The animals were genotyped with the

PorcineSNP60 BeadChip (Illumina Inc., San Diego, CA, USA) and genotypes were imputed to

34,615,361 autosomal variants using SWIM 1.0 (23). This full set of imputed variants was then

filtered for minor allele frequency (MAF) $\geq$1%, Hardy-Weinberg equilibrium ($P \geq 1 \times 10^{-8}$), and

IMPUTE2 info score ≥0.8, resulting in ~11.7 million quality-controlled variants on autosomes.

From these quality-controlled variants, we randomly selected a 4-Mb region on chromosome 1

containing 6,504 variants for the simulation study.

Quantitative traits were simulated using model (5) with a heritability of 0.5 using MPH

(24). The GRM **G**, used to model the covariance of polygenic effects due to genetic relatedness,

was computed using 10,000 randomly selected, quality-controlled chip SNPs. We positioned 1, 2,

or 3 causal variants within the central 2-Mb region, collectively explaining either 1% or 4% of

phenotypic variation (PVE). Simulations used samples of 5,000 or 10,000 randomly selected

individuals, generating 100 replicates for each of the 12 scenarios (3 causal variant counts × 2 PVE

levels × 2 sample sizes).

For gene-based fine-mapping evaluation, we partitioned the 4-Mb candidate region into

100 equal blocks to serve as gene proxies. This block size approximates the average pig gene

length of ~33 kb derived from the Sscrofa11.1 genome annotation (Ensembl release 113) (25). To

generate the required summary statistics for fine-mapping from each simulated dataset, we

conducted association tests for variants in the candidate region using two approaches: 1) a linear

mixed model (LMM) implemented in GCTA-MLMA (v1.94.1) (26), and 2) a linear regression

model in PLINK 2.0 (--glm) (27) using the top 20 genotype principal components as covariates

for population structure control. GCTA-MLMA used the same GRM as in the trait simulation.

Furthermore, required LD matrices were generated from each simulation sample's genotype data:

both the standard SNP correlation matrix (Σ) as in model (3) and the relatedness-adjusted

correlation matrix ($\tilde{\Sigma}$) as in model (9). The standard matrix (Σ) was used by GCTA-COJO,

FINEMAP, SuSiE, FINEMAP-inf, and SuSiE-inf, while the relatedness-adjusted matrix ($\tilde{\Sigma}$) was

used by FINEMAP-adj and SuSiE-adj.

Performance evaluation in simulations

The performance of various fine-mapping approaches was benchmarked using the datasets generated across the 12 distinct simulation scenarios (3 causal variant counts × 2 PVE levels × 2 sample sizes). It is important to note that while 100 replicates were generated for each scenario, not all replicates resulted in a significant association signal within the candidate region when analyzed by GCTA-MLMA. Specifically, only those simulation replicates where at least one variant in the candidate region achieved a GCTA-MLMA P-value $< 1 \times 10^{-5}$ were retained for subsequent fine-mapping evaluation. This yielded a minimum of 74 such replicates for any given scenario, with detailed counts available in Supplementary Table S1.

The methods evaluated included our novel approaches (BFMAP-SSS, FINEMAP-adj, SuSiE-adj, and PIP_{gene}), our previously described BFMAP-Forward method (17), and several well-established reference methods: FINEMAP v1.4.2 (10), SuSiE (as implemented in susieR v0.12.35) (12, 13), FINEMAP-inf v1.3, SuSiE-inf v1.4 (14), and GCTA-COJO (--cojo-slct in GCTA v1.94.1) (8, 28). BFMAP-Forward and BFMAP-SSS were implemented in BFMAP v0.65, while FINEMAP-adj and SuSiE-adj directly used FINEMAP and SuSiE, respectively, with adapted inputs designed for related individuals. For consistency across all applicable methods, a causal variant's prior PVE and the maximum number of causal variants were set to 0.01 and 5, respectively, in all simulation datasets. Furthermore, the same GRM, constructed from the 10,000 quality-controlled chip SNPs as detailed in the trait simulation, was used by all our LMM-based fine-mapping methods requiring such an input, specifically BFMAP (both BFMAP-Forward and BFMAP-SSS) and our -adj approaches (FINEMAP-adj and SuSiE-adj). For a comprehensive comparison, reference methods were applied twice, using association statistics as input from LMM (GCTA-MLMA) and, separately, from linear regression (PLINK 2.0 --glm).

We applied consistent *P*-value-based pre-filtering for fine-mapping across methods.

Specifically, for GCTA-COJO (--cojo-slct), the significance threshold in its stepwise procedure (-

-cojo-p) was set to 1×10^{-3}. Similarly, for all other fine-mapping tools evaluated (FINEMAP,

SuSiE, FINEMAP-inf, SuSiE-inf, and our BFMAP and -adj approaches), only variants with a

GWAS *P*-value $< 1 \times 10^{-3}$ from the respective input summary statistics (GCTA-MLMA or PLINK

2.0 --glm) were included in the fine-mapping analysis. This initial filtering threshold was chosen

to reduce the computational burden of model searching for each tool while aiming to be sufficiently

inclusive of potentially causal variants. Unless otherwise specified, all other parameters for these

software tools were maintained at their default values.

To evaluate fine-mapping accuracy, variants from each method were designated as

putatively causal based on their respective PIPs (or PCIPs for BFMAP-Forward) using thresholds

ranging from 0.0 to 1.0. Performance was primarily quantified using recall (also known as

sensitivity or power) and precision (also known as positive predictive value). Recall is the

proportion of true causal variants correctly identified (calculated as TP / (TP + FN)), and precision

is the proportion of designated putatively causal variants that are indeed true causal (calculated as

TP / (TP + FP)). Here, TP, FP, and FN represent the number of true positives, false positives, and

false negatives, respectively, determined at a given PIP (or PCIP) threshold and averaged over all

simulation replicates retained for fine-mapping evaluation per scenario (Supplementary Table S1).

Precision and recall were also calculated for gene-level PIPs using the same approach, with genes

rather than variants as the unit of evaluation.

Given that GCTA-COJO (--cojo-slct) does not compute PIPs, a modified evaluation

strategy was necessary. Variants identified by GCTA-COJO were ranked by first prioritizing those

from its jma output, followed by variants in its cma output, with the latter ranked by their

conditional *P*-values. This *P*-value-based ranking was then used to assess GCTA-COJO's ability

to prioritize true causal variants relative to the PIP/PCIP-based rankings from other methods.

Specifically, we evaluated its recall by selecting the top *k*-ranked variants (where *k* ranged from 1

to 20) as putatively causal. For each *k*, recall was calculated as the proportion of all true causal

variants that were included in this top *k* selection, averaged across all qualifying simulation

replicates per scenario.

Duroc pig trait analysis

This study also analyzed several economically important traits from the same cohort of Duroc pigs

described in the 'Data simulation' section. Phenotype data, collected by Smithfield Premium

Genetics between 2015 and 2021, included growth traits for ~27,000 animals (off-test body weight

[WT], back fat thickness [BF], and loin muscle depth [MS]) and reproduction traits for 3,290 sows

(number of piglets born alive [NBA], born dead [NBD], and weaned [NW]). The three growth

traits were collected at the end of the performance test, as detailed in Bergamaschi et al. (29). All

phenotypes were pre-adjusted to remove systematic environmental effects, including farm and

physiological sources of variation. For association and fine-mapping analyses, we utilized the

~11.7 million quality-controlled autosomal variants (derived as detailed in the 'Data simulation'

section).

GWAS was performed using SLEMM-GWA v0.89.5 (30), which provides accuracy

comparable to GCTA-MLMA but with orders of magnitude greater computational efficiency

(Supplementary Figure S1). Association peaks were identified by visual inspection of the

Manhattan plot for each trait, with a *P* -value threshold of 1×10^{-5}. For each retained peak,

candidate region boundaries were established by extending 2 Mb upstream and downstream from

the position of the minimum *P*-value variant. Variants with $P < 1 \times 10^{-3}$ within each defined

candidate region were then retained for subsequent fine-mapping analyses. The same 10,000

quality-controlled chip SNPs selected for the trait simulation were used to construct the GRM for

methods requiring it (e.g., SLEMM and our BFMAP and -adj approaches).

Results

Method overview

This study introduces a framework for fine-mapping complex traits in samples of related

individuals, addressing analyses with both individual-level data and summary statistics. Figure 1

provides a schematic representation of this framework, illustrating the relationships between

existing methods and the novel approaches developed herein.

Typical fine-mapping tools, such as FINEMAP and SuSiE, usually use summary statistics.

Their underlying models are derived from linear regression assuming samples of unrelated

individuals, which limits their direct applicability or accuracy when substantial relatedness is

present (Figures 1A and 1C). To overcome this, we developed BFMAP, a Bayesian fine-mapping

approach first introduced for individual-level livestock data using forward selection (BFMAP-

Forward) (17). BFMAP employs a linear mixed model (LMM) that explicitly accounts for whole-

genome infinitesimal effects and genetic relatedness through a genomic relationship matrix (GRM)

(Figure 1B). In this study, alongside the established BFMAP-Forward, we introduce BFMAP-SSS,

a novel BFMAP implementation coupling shotgun stochastic search (SSS) with simulated

annealing for enhanced model space exploration.

Building upon the BFMAP framework, we developed a strategy to leverage its advantages

within a summary statistics context. The BFMAP model, initially designed for individual-level

data, can be transformed into an equivalent model based on summary statistics (Figure 1D).

Through an approximation ($\mathbf{D} \approx \mathbf{I}\tilde{n}$), analogous to the one used in GRAMMAR-Gamma, this

transformed model yields a functional form identical to that underlying standard FINEMAP and

SuSiE. This key structural equivalence enables the direct adaptation of these existing tools for

accurate fine-mapping in related individuals. This adaptation involves a two-step process: first,

calculating relatedness-aware inputs (including standard LMM-derived z-scores ($\mathbf{z}$), an effective

sample size ($\tilde{n}$), and a relatedness-adjusted linkage disequilibrium (LD) matrix ($\tilde{\boldsymbol{\Sigma}}$), as detailed in

Materials and methods); and second, providing these as the conventional z-score, sample size, and

LD matrix inputs to FINEMAP or SuSiE. We term these adapted methods FINEMAP-adj and

SuSiE-adj.

It is noteworthy that recently proposed fine-mapping methods, FINEMAP-inf and SuSiE-

inf, are conceptually related to our LMM-based approaches (BFMAP, FINEMAP-adj, and SuSiE-

adj) in that both incorporate terms to account for infinitesimal effects (Figure 1E). However, a key

distinction is that FINEMAP-inf and SuSiE-inf model the infinitesimal effects of variants within

the candidate fine-mapping region, whereas our methods model whole-genome infinitesimal

effects via GRM.

Finally, recognizing the challenges of fine-mapping to single-variant resolution in

populations with extensive LD, such as livestock, we propose the use of gene-level posterior

inclusion probability (PIP_{gene}). This metric aggregates variant-level evidence to assess the overall

evidence for a gene harboring at least one non-zero-effect variant, offering a balance between

localization precision and detection power (Figure 1F). In the subsequent sections, the

performance of our novel contributions (BFMAP-SSS, FINEMAP-adj, and SuSiE-adj), alongside

our previously developed BFMAP-Forward approach (17), is evaluated in comparison with

existing approaches (FINEMAP, SuSiE, FINEMAP-inf, SuSiE-inf, and GCTA-COJO) for fine-

mapping in related individuals.

Simulation benchmarks

To rigorously evaluate the fine-mapping approaches, we conducted simulation studies based on

real Duroc pig genotypes across 12 distinct scenarios. These scenarios varied by the number of

true causal variants (1, 2, or 3), the total proportion of variance explained (PVE) by these causal

variants (1% or 4%), and the sample size (5,000 or 10,000 individuals). For each scenario, 100

replicates were generated, though only those yielding significant GWAS associations (GCTA-

MLMA $P < 1 \times 10^{-5}$) were retained for fine-mapping evaluation, ensuring robust downstream

analysis (see Materials and methods for details).

Impact of relatedness adjustment on genotype correlations

Summary-statistics-based fine-mapping methods critically rely on an accurate LD matrix

reflecting correlations between genotypes. In samples of related individuals, one might naively

compute a standard LD matrix directly from the observed genotypes. However, as we have

theoretically established in Material and methods (Section 'Fine-mapping with related individuals:

summary statistics'), a relatedness-adjusted LD matrix ($\tilde{\Sigma}$) is required to properly account for the

genetic relatedness among individuals in fine-mapping. To empirically illustrate the impact of this

adjustment, we compared elements of the standard LD matrix (Σ) with those of the relatedness-

adjusted LD matrix ($\tilde{\Sigma}$) within our 4-Mb candidate region for simulations (Supplementary Figure

S2). This comparison revealed substantial differences between the two types of correlations.

Notably, the relatedness adjustment (transforming Σ to $\tilde{\Sigma}$) often led to a shrinkage of correlation

magnitudes, particularly for variants that exhibited strong positive or negative correlations in the

standard Σ matrix. Consequently, applying fine-mapping methods with a standard, unadjusted LD

matrix in samples of related individuals, rather than the appropriate relatedness-adjusted version,

can severely compromise fine-mapping performance and the accuracy of causal variant

identification.

Performance of reference methods with different input association statistics

We first assessed the performance of established reference fine-mapping methods (FINEMAP,

SuSiE, FINEMAP-inf, SuSiE-inf, and GCTA-COJO) using two types of input association statistics:

those derived from a LMM (via GCTA-MLMA) accounting for relatedness and whole-genome

infinitesimal effects, and those from a standard linear regression model (via PLINK 2.0 --glm)

with top 20 genotype principal components for population structure control.

GCTA-COJO consistently demonstrated slightly superior performance when using LMM-

derived association statistics across all simulation scenarios (Supplementary Figure S3). For the

other reference methods (FINEMAP, SuSiE, and their -inf variants), the choice of input statistics

had a more nuanced impact. In scenarios with 1 or 2 causal variants, these methods generally

favored linear regression inputs in 4% PVE settings, whereas LMM-derived statistics were often

preferred in 1% PVE settings, as reflected by precision-recall curves (Figure 2) and area under the

precision-recall curve (AUPRC) values (Table 1). This distinction was less apparent in scenarios

with 3 causal variants. Notably, SuSiE-inf frequently encountered convergence issues when using

LMM-derived association statistics but performed robustly with linear regression inputs.

Comparative performance of proposed and existing fine-mapping methods

Overall, GCTA-COJO's performance in prioritizing causal variants was generally comparable to

or slightly poorer than established PIP-based methods across the simulation scenarios

(Supplementary Figure S3). Consequently, while its results are available, our primary comparative

focus shifts to the PIP/PCIP-based methods.

A consistent pattern emerged when comparing our developed methods (BFMAP-Forward,

BFMAP-SSS, FINEMAP-adj, and SuSiE-adj) against the established approaches (FINEMAP,

SuSiE, FINEMAP-inf, SuSiE-inf). Our methods designed for related individuals consistently and

substantially outperformed these existing tools across all 12 simulation scenarios, as illustrated by

the precision-recall curves (Figure 2) and the AUPRC values (Table 1). This performance

advantage for our methods was particularly pronounced in scenarios with larger sample sizes or

higher PVE. For instance, when AUPRCs were averaged across the six scenarios (3 causal variant

counts × 2 PVE levels) with 10,000 individuals, BFMAP-SSS (average AUPRC = 0.234) showed

approximately a 3.8-fold higher AUPRC than the best-performing reference method, SuSiE using

LMM-derived association statistics (average AUPRC = 0.049) (Table 1). Specifically, FINEMAP-

adj and SuSiE-adj, which incorporate relatedness-adjusted LD matrices and LMM-derived

association statistics, achieved remarkable improvements over their counterparts (FINEMAP and

SuSiE) that use standard LD matrices. When AUPRCs were averaged across the six scenarios (3

causal variant counts × 2 PVE levels) with 10,000 individuals, FINEMAP-adj yielded a 5.4-fold

higher AUPRC than standard FINEMAP, and SuSiE-adj a 3.1-fold higher AUPRC than standard

SuSiE. These substantial gains were achieved when standard FINEMAP and SuSiE were provided

with LMM-derived association statistics, their generally optimal input type under these conditions

with 10,000 individuals (Table 1).

Among our LMM-based approaches, the overall differences in fine-mapping performance

were relatively small (Table 1, Figure 2). BFMAP-SSS, employing shotgun stochastic search,

performed best overall. BFMAP-Forward, which uses a forward selection strategy, showed

performance comparable to or slightly less favorable than FINEMAP-adj and SuSiE-adj that

implement more exhaustive model space exploration.

Fine-mapping challenges in livestock populations and impact of simulation parameters

It is crucial to note the inherent difficulty of fine-mapping in livestock populations, characterized

by strong LD and extensive genetic relatedness among individuals. Even with methods explicitly

accounting for relatedness and whole-genome infinitesimal effects, performance can be

constrained. For instance, in the simulation scenario with 3 causal variants, 10,000 individuals,

and 1% PVE, the best-performing reference method (SuSiE, using its optimal input) yielded an

AUPRC of only 0.024 (Table 1). While our novel methods offered a substantial improvement (e.g.,

BFMAP-SSS achieved an AUPRC of 0.077 in the same scenario), these results underscore that

fine-mapping in such populations remains a formidable task.

The simulation parameters also highlighted expected trends. Performance for most

methods improved with fewer causal variants or larger PVE for the candidate region. A key

observation was the differential response to increased sample size: while our relatedness-aware

approaches (BFMAP-Forward, BFMAP-SSS, FINEMAP-adj, and SuSiE-adj) uniformly benefited

from larger sample sizes, the methods originally designed for unrelated individuals (FINEMAP,

SuSiE, and their -inf variants) showed limited improvement or, in some instances, even a decline

in performance as sample size increased when applied to these related samples (Table 1). This

underscores the critical importance of appropriately modeling genetic relatedness, especially in

larger cohorts of related individuals.

Gene-level PIPs increase detection power in fine-mapping

To address the challenges of fine-mapping at single-variant resolution, particularly in populations

with extensive LD like the Duroc pigs in this study, we evaluated the utility of our proposed gene-

level posterior inclusion probability (PIP_{gene}). The calculation of PIP_{gene} requires posterior model

probabilities for variant sets, which are not standard outputs for all fine-mapping tools. Therefore,

for this specific evaluation, we computed PIP_{gene} using the outputs from BFMAP-Forward,

BFMAP-SSS, and FINEMAP-adj, as these methods provide the necessary model-level

information. This selection of methods is sufficient to demonstrate the advantages of gene-level

aggregation over variant-level PIPs, an orthogonal comparison to the inter-method performance

benchmarks detailed previously.

The application of gene-level fine-mapping resulted in a substantial improvement in the

ability to correctly identify causal genes (i.e., our defined gene proxy blocks containing one or

more true causal variants) for all three methods evaluated (BFMAP-Forward, BFMAP-SSS, and

FINEMAP-adj). This enhancement is evident from the precision-recall curves, which consistently

show superior performance for gene-level PIPs compared to variant-level PIPs across all 12

simulation scenarios (Figure 3). The AUPRC values further underscore the benefits of gene-level

aggregation (Table 2). The AUPRC for identifying causal genes was markedly higher than that for

identifying individual causal variants across all methods and scenarios. Notably, the magnitude of

this performance gain was often greatest in the more challenging simulation scenarios. For instance,

in the scenario with 3 causal variants, 1% PVE, and 10,000 individuals (a setting where variant-

level fine-mapping proved particularly difficult), gene-level aggregation yielded dramatic

improvements. At the variant level, BFMAP-Forward, BFMAP-SSS, and FINEMAP-adj achieved

AUPRCs of 0.061, 0.077, and 0.076, respectively. In contrast, when evidence was aggregated to

the gene level using PIP_{gene}, these same methods achieved AUPRCs of 0.305, 0.420, and 0.406,

respectively (Table 2). This represents an approximate 4- to 5.5-fold increase in AUPRC,

highlighting the substantial power gained by shifting the inferential focus from individual variants

to gene units in complex fine-mapping contexts.

Computational performance

We evaluated the runtime of our LMM-based fine-mapping methods using simulated datasets with

2 causal variants (4% PVE) for 5,000 and 10,000 individuals, focusing on the same 4-Mb candidate

region (3,837 and 4,371 pre-filtered SNPs, respectively) as used in our main simulation

benchmarks. Analyses were conducted on an Intel Xeon Gold 6230 CPU. Key fine-mapping

parameters, such as the prior PVE per causal variant (0.01) and the maximum number of assumed

causal variants (5), were kept consistent with the main simulation benchmarks.

Wall-clock times for all methods, representing the analysis of a single simulation replicate,

are detailed in Supplementary Table S2. BFMAP-Forward was the fastest approach, completing

analyses in approximately 0.3 minutes (5,000 individuals) and 0.5 minutes (10,000 individuals)

with 20 CPU threads. FINEMAP-adj required approximately 1.5 minutes (5,000 individuals) and

2.3 minutes (10,000 individuals) using 20 threads; these times include the pre-calculation of the

relatedness-adjusted LD matrix. Both BFMAP-Forward and FINEMAP-adj showed limited

additional speedup when using 20 threads compared to single-thread execution. BFMAP-SSS,

while generally the most accurate in fine-mapping benchmarks, was the most computationally

intensive, with wall-clock times of approximately 52 minutes (5,000 individuals) and 170 minutes

(10,000 individuals) using 20 threads. SuSiE-adj, which utilizes the susieR package and operates

on a single thread, completed its analyses in approximately 1.3 minutes (5,000 individuals) and

2.3 minutes (10,000 individuals), comparable to single-threaded FINEMAP-adj.

Application to Duroc pig traits

We applied our novel fine-mapping methods to analyze six economically important traits in the Duroc pig population previously described. To identify candidate genomic regions for fine-mapping, we first performed GWAS for each trait using the mixed-model approach implemented in SLEMM-GWA. All six traits produced high-quality Manhattan plots, five of which displayed association peaks with an inclusive significance threshold of $P < 1 \times 10^{-5}$ (Supplementary Figure S4). Using this threshold, we identified 46 candidate region-trait pairs: 43 for performance traits and 3 for reproduction traits (Supplementary Table S3).

To identify putative causal variants and genes within these candidate regions, we initially employed BFMAP-SSS due to its strong performance in simulations. This fine-mapping identified 30 variants with a PIP > 0.1 and 2 variants with a PIP > 0.5 across all region-trait pairs (Supplementary Table S4). Recognizing the potential to enhance discovery by aggregating variant-level evidence, we then calculated the gene-level PIP (PIP_{gene}) for all annotated genes within each candidate region, with gene boundaries defined as detailed in Material and methods. This approach identified 87 gene-trait pairs with $PIP_{gene} > 0.1$, of which 22 pairs had a $PIP_{gene} > 0.5$ (Supplementary Table S5). These results underscore the utility of this gene-based strategy for prioritizing candidate genes.

The power of PIP_{gene} was particularly evident in regions where individual variant PIPs were low. For example, a candidate region on chromosome 1 (chr1:51,300,453-55,300,453) associated with back fat thickness (BF) (Figure 4A) contained no variants with a PIP greater than 0.03 (Figure 4B), making variant prioritization challenging. However, the PIP_{gene} analysis revealed that *MRAP2* emerged with a strong signal ($PIP_{gene} = 0.669$, distinctly higher than other genes in the region; Figure 4C). The *MRAP2* gene encodes melanocortin receptor accessory protein 2, which regulates

melanocortin receptor activity and energy homeostasis (31). Previous studies have identified loss-

of-function *MRAP2* variants as pathogenic for monogenic hyperphagic obesity in humans (32, 33),

and *Mrap2*-knockout mice develop severe early-onset obesity with increased fat mass and

adipocyte hypertrophy (33). These findings strongly support *MRAP2* as a biologically plausible

candidate for the BF association observed in our study.

A second illustrative example for BF is the candidate region on chromosome 6

(chr6:144,948,358-148,948,358; Figure 4D). In this locus, fine-mapping with BFMAP-SSS

identified three prioritized variants (each with PIP > 0.1) that are located within the *LEPR* gene.

This gene encodes the leptin receptor, which mediates leptin signaling in energy homeostasis and

body weight regulation (34). The *LEPR* gene showed a strong gene-level signal ($PIP_{gene} = 0.861$),

consistent with its well-established role in regulating energy homeostasis and body composition

(35–37). Mutations in this gene can cause severe early-onset obesity, hyperphagia, and

hypogonadotropic hypogonadism in humans (38, 39). While PIPs of all other variants in the

candidate region were < 0.05 (Figure 4E), our PIP_{gene} analysis highlighted an additional candidate

gene, *DNAJC6* ($PIP_{gene} = 0.875$; Figure 4F). This gene encodes auxilin-1 , a DNAJ/HSP40 family

protein that regulates resting metabolic rate (40) and has been shown to suppress adipogenesis and

energy metabolism in adipocytes (41). These findings demonstrate the ability of PIP_{gene} to enhance

detection power for relevant genes whose signals might be diffuse at the individual variant level.

Finally, we compared our summary-statistics-based methods (FINEMAP-adj and SuSiE-

adj) against individual-level BFMAP-SSS by re-analyzing the two illustrative BF candidate

regions. At the variant level, SuSiE-adj PIPs showed high concordance with BFMAP-SSS PIPs in

both regions (Supplementary Figures S5A and S5B). For FINEMAP-adj, variant PIPs on the

chromosome 1 region were highly concordant with BFMAP-SSS (Supplementary Figure S5A)

and stable across iteration lengths (Supplementary Figures S6A and S6C), including the default

iteration settings. The chromosome 6 region, however, proved more challenging for FINEMAP-

adj: while its concordance with BFMAP-SSS improved with increased iterations from the default

settings (plateauing around 10,000 iterations) (Supplementary Figures S6B and S6D), FINEMAP-

adj still showed substantial discrepancy from BFMAP-SSS, with a PIP correlation between the

two methods of 0.594 even with 50,000 iterations (Supplementary Figure S5B). Despite the

variant-level discrepancy for FINEMAP-adj on the chromosome 6 region, PIP_{gene} values derived

from the FINEMAP-adj runs with 50,000 iterations were highly correlated with those from

BFMAP-SSS in both regions (chr1: 0.999; chr6: 0.945; Supplementary Figure S5C and S5D).

Gene-level aggregation yielded more highly consistent inferences between FINEMAP-adj and

BFMAP-SSS, even when variant-level concordance is limited (Supplementary Figure S6).

Discussion

Fine-mapping complex traits in populations with extensive relatedness, such as livestock, presents

significant statistical challenges. Standard fine-mapping methodologies, predominantly developed

for human genetics studies involving largely unrelated individuals, can falter or yield unreliable

results when applied naively to these populations. This study addresses this critical gap by

introducing a comprehensive framework. This includes BFMAP (a Bayesian approach for

individual-level data, encompassing our previously developed BFMAP-Forward (17) and the

novel BFMAP-SSS implementation), innovative summary-statistics adaptations (FINEMAP-adj

and SuSiE-adj), and a gene-level aggregation metric (PIP_{gene}), all designed to improve fine-

mapping under such complex conditions of relatedness.

A key contribution of this work is the clear demonstration, both theoretically and through extensive pig genotype-based simulations, that appropriately modeling relatedness is critical for achieving accurate fine-mapping. Our results unequivocally show that standard fine-mapping tools (GCTA-COJO, FINEMAP, SuSiE, and their -inf variants), even when provided with summary association statistics from mixed models, exhibit substantially poorer performance than our relatedness-aware methods (BFMAP-Forward, BFMAP-SSS, FINEMAP-adj, and SuSiE-adj) designed to correctly utilize relatedness information (Figure 2, Table 1). The performance gap, reflected in markedly poorer precision-recall profiles and lower AUPRC values for existing methods (GCTA-COJO, FINEMAP, SuSiE, and their -inf variants) (Figure 2, Table 1), underscores the potential for a high proportion of false positives in previous fine-mapping studies in livestock that applied human-centric fine-mapping methods not designed for samples of related individuals (e.g., 42–46). It is important to note that simply §using LMM-derived summary association statistics was insufficient to overcome the fundamental limitations of these methods when applied to samples of related individuals. This highlights the critical need for approaches that explicitly integrate relatedness, primarily through a relatedness-adjusted LD matrix, as implemented in our -adj methods, or via direct LMM modeling as in BFMAP.

Among our proposed relatedness-aware methods, BFMAP-SSS generally emerged as the most accurate, likely due to its sophisticated shotgun stochastic search with simulated annealing allowing for a more thorough exploration of the model space. FINEMAP-adj and SuSiE-adj also performed well, trailing BFMAP-SSS and slightly outperforming BFMAP-Forward (Table 1, Figure 2). This performance hierarchy aligns with theoretical expectations: the forward selection strategy of BFMAP-Forward is inherently less exhaustive than the search algorithms in BFMAP-SSS or the variable selection approaches underpinning SuSiE (and thus SuSiE-adj). The slight

performance edge of BFMAP-SSS over the -adj methods may stem from the GRAMMAR-

Gamma-like approximation employed to allow the FINEMAP and SuSiE programs to be directly

applied using appropriately transformed summary statistics (LMM-derived z-scores and effective

sample size $\tilde{n}$) and a relatedness-adjusted LD matrix ($\tilde{\Sigma}$). While developing new programs for

FINEMAP-adj and SuSiE-adj from scratch to circumvent this approximation is feasible, the

current -adj approaches offer substantial practical advantages by leveraging well-established,

existing software, especially given their performance close to BFMAP-SSS.

The choice among our developed methods in practice will depend on a balance of factors.

BFMAP-SSS offers the highest accuracy but is the most computationally intensive. For studies

where computational resources are a constraint, FINEMAP-adj, SuSiE-adj, and BFMAP-Forward

provide much faster alternatives with only a modest trade-off in accuracy compared to BFMAP-

SSS (Figure 2, Supplementary Table S2). FINEMAP-adj, BFMAP-SSS, and BFMAP-Forward

also readily provide the posterior model probabilities necessary for calculating PIP_{gene}, a feature

not directly available from SuSiE-adj (which builds on SuSiE) without further methodological

development. Furthermore, users should be aware that FINEMAP-adj (which builds on FINEMAP)

can sometimes require extended iterations for convergence in complex regions, whereas SuSiE-

adj, benefiting from SuSiE's efficient variable selection, is generally robust in convergence. We

therefore recommend BFMAP-SSS when maximal accuracy is paramount and resources permit;

FINEMAP-adj when gene-level insights are desired with good speed; SuSiE-adj for fast and robust

variant-level fine-mapping without immediate need for PIP_{gene}; and BFMAP-Forward as a rapid

option for individual-level data.

A significant challenge in livestock genomics is the extensive and complex LD structure,

usually making fine-mapping at single-variant resolution exceedingly difficult. Our proposed

PIP_{gene} metric addresses this by aggregating variant-level evidence, thereby enhancing the power

to detect trait-associated genes, albeit with a trade-off in localization precision from variant to gene.

As demonstrated in our simulations, the improvement in detection power (AUPRC) using PIP_{gene}

was substantial, particularly in challenging scenarios with low PVE and multiple causal variants,

where gene-level AUPRCs were up to 5.5-fold higher than variant-level AUPRCs (Table 2, Figure

3). This utility was further underscored in our analysis of Duroc pig traits, where PIP_{gene}

successfully highlighted biologically relevant genes such as *MRAP2* and *DNAJC6* for back fat

thickness, even when underlying variant PIPs were diffuse or individually weak (Figure 4).

Furthermore, this approach led to the identification of other promising candidate genes, such as

DYRK4 as a novel candidate for back fat thickness, whose high PIP_{gene} values warrant further

investigation (47). These findings collectively highlight the value of our fine-mapping framework

for enhancing candidate gene discovery in livestock.

Despite the advancements presented, this study has limitations. A primary limitation is our

simulation design. While based on real pig genotypes, evaluations focused on a single 4-Mb

candidate region where we simulated only 1-3 variants as having larger causal effects. This,

combined with an infinitesimal background modeled by 10,000 genome-wide chip SNPs,

represents one specific model of genetic architecture; real traits exhibit greater heterogeneity in

the number, effect size distribution, and genomic location of causal variants. Furthermore, the

GRM used to model this infinitesimal background was constructed directly from these 10,000

known infinitesimal-effect SNPs and was then supplied as input to GRM-dependent fine-mapping

methods. This perfect concordance between the SNPs defining the simulated infinitesimal

background and those in the analytical GRM is an idealization not reflective of real-world

scenarios, where GRMs are estimated from available marker data (often LD-pruned) and may not

fully capture true genetic covariance or perfectly align with the underlying polygenic architecture.

While our main simulations effectively highlighted performance differences using this consistent

GRM, we further investigated the impact of using a more "practical" GRM, constructed from

10,000 randomly selected quality-controlled genome-wide variants (from the ~11.7 million). Re-

analyzing all simulation scenarios with FINEMAP-adj and SuSiE-adj using this practical GRM

(for both LMM-GWAS summary statistic generation and as input to the -adj methods) yielded

fine-mapping performance highly concordant with that obtained using the "simulation-derived"

GRM (Supplementary Figure S7, Supplementary Table S6). This result suggests that while GRM

misspecification remains a theoretical concern, our -adj approaches demonstrate robustness to this

aspect of GRM construction, at least with reasonably dense marker-based GRMs. While our study

effectively demonstrates the advantages of relatedness-aware methods under the tested

architectures, further research exploring a wider array of simulated genetic complexities will be

valuable for comprehensively understanding their performance boundaries across all potential

real-world scenarios. Secondly, the current implementations, particularly those involving matrix

operations on the GRM or relatedness-adjusted LD, may face scalability challenges with datasets

involving hundreds of thousands of individuals, a scale becoming increasingly common. Further

algorithmic refinements will be needed to cater to such massive datasets. Thirdly, our current

PIP_{gene} formulation, which sums posterior model probabilities for models including any variant

within a gene region, can be systematically influenced by gene length and variant density. Under

the standard fine-mapping prior that assigns equal *a priori* causal probability to each variant,

longer genes with more variants inherently have greater opportunities to accumulate signal, leading

to higher PIP_{gene} values that may not solely reflect biological enrichment for causality. Future

refinements could explore incorporating more sophisticated priors that account for gene size or

variant density to further enhance the specificity of gene-level inference. Fourthly, our real data

analysis relied on imputed sequence data for SNPs and indels; other structural variations were not

considered, and differential imputation quality across variants could introduce unmodeled

uncertainty.

Future research could focus on several exciting avenues. Incorporating functional

annotation data into the prior model probabilities for variants or genes (17, 48–50) holds

considerable promise for further enhancing the statistical power and accuracy of our methods.

Additionally, while this study focused on fine-mapping GWAS signals for complex traits, the

principles of accounting for relatedness (particularly through adjusted LD matrices and mixed

models) are broadly applicable. Investigating the performance and adaptation of our framework

for other types of genetic analyses in samples of related individuals, such as fine-mapping

expression quantitative trait loci (eQTLs) (51–54), represents a valuable direction.

In conclusion, this study provides a robust suite of fine-mapping tools (BFMAP-Forward,

BFMAP-SSS, FINEMAP-adj, and SuSiE-adj) and a novel gene-level aggregation strategy (PIP_{gene})

specifically designed for and validated in populations with complex relatedness, such as livestock.

By properly accounting for genetic relationships and whole-genome infinitesimal effects, these

methods offer substantial improvements in accuracy and power over existing approaches, paving

the way for more reliable identification of causal variants and genes underlying complex traits in

these important populations.

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Author contributions

J.J. conceived and designed the study and developed the methodologies. J.Wang carried out the simulation studies and pig trait analyses. F.T., Y.H., and C.M. contributed to data preprocessing. J.Wang, J.J., and J.Wei performed data visualization. J.J. and J.Wang wrote the manuscript. All authors reviewed and approved the final manuscript.

Conflict of interest

Y.H. was employed by Smithfield Premium Genetics. The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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Data availability

BFMAP can be downloaded at https://github.com/jiang18/bfmap. Tutorials for FINEMAP-adj and SuSiE-adj are available at https://github.com/JJWang259/FineMapping-RelatedIndividuals. The

Duroc pig data used in this study are property of Smithfield Premium Genetics (Rose Hill, NC, USA). Restrictions apply to the availability of these data, which were used under license for the current study and are not publicly available. Requests to access these datasets may be granted under a negotiated research agreement and should be directed to Kent Gray, General Manager (kgray@smithfield.com).

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 Figure legends

Figure 1. Overview of fine-mapping methods for unrelated and related individuals.

Overview of fine-mapping approaches for samples of unrelated (A, C, and E) and related (B, D,

and F) individuals. (A) Linear regression provides the foundation for fine-mapping in samples of

unrelated individuals. (B) BFMAP employs linear mixed models with genomic relationship matrix

for fine-mapping in samples of related individuals. (C) Standard summary-statistics methods

(FINEMAP and SuSiE) are derived from the linear regression framework. (D) Adapted methods

(FINEMAP-adj and SuSiE-adj) use relatedness-adjusted correlations $(\tilde{\Sigma})$ and effective sample size

$(\tilde{n})$ derived from the BFMAP framework. Through the approximation $\mathbf{D} \approx \mathbf{I}\tilde{n}$, these methods

achieve compatibility with standard FINEMAP and SuSiE implementations. (E) FINEMAP-inf

and SuSiE-inf extend their respective base methods by modeling infinitesimal effects within

candidate regions. (F) All methods produce variant-level posterior inclusion probability (PIP; or

PCIP for BFMAP-Forward) as output. Gene-level PIP, available for methods that provide posterior

model probabilities (BFMAP-Forward, BFMAP-SSS, FINEMAP-adj, and FINEMAP),

aggregates variant-level evidence for prioritizing causal genes.

Figure 2. Precision-recall curves for identifying causal variants using PIPs across simulation

scenarios.

GWAS summary data were derived from GCTA-MLMA (LMM) or PLINK 2.0 --glm (LM).

Results are shown for different sample sizes (5,000 and 10,000 individuals), PVE levels (1% and

4%), and numbers of causal variants (1-3), with A-L representing the 12 simulation scenarios.

Figure 3. Precision-recall curves for identifying causal genes across simulation scenarios.

Results show the ability of three methods (BFMAP-Forward, BFMAP-SSS, and FINEMAP-adj)

to identify causal genes (defined as gene proxy blocks containing true causal variants) under

different sample sizes (5,000 and 10,000 individuals), PVE levels (1% and 4%), and numbers of

causal variants (1-3). A-L represent the 12 simulation scenarios.

Figure 4. Fine-mapping results for two candidate regions.

BFMAP-SSS fine-mapping analysis of two genomic regions associated with back fat thickness:

chr1:51,300,453–55,300,453 and chr6:144,948,358–148,948,358. (A) and (D) show locus zoom

plots displaying local association signals within each interval. (B) and (E) show the PIPs of

individual variants, and (C) and (F) show the PIPs of genes.

Figure S1. Comparison of GCTA-MLMA and SLEMM-GWA for GWAS of back fat

thickness in 26,731 Duroc pigs.

Both methods used identical GRMs constructed from 10,000 randomly selected chip SNPs and

analyzed 1,000,000 randomly selected imputed variants. (A) Chi-square association test statistic

comparison. (B) Computational time comparison. Analyses were conducted on a Linux server with

2×Intel Xeon Gold 6258R CPUs and 512 GB memory using 20 threads.

Figure S2. Comparison of standard and relatedness-adjusted genotype correlation

matrices.

(A) Scatter plot comparing pairwise genotype correlation coefficients between the standard matrix

(Σ) and relatedness-adjusted matrix ($\tilde{\Sigma}$) for all SNP pairs. The red dashed line represents $y = x$. (B)

Density distributions of genotype correlation coefficients for both matrix types. Both matrices

were computed using 5,000 randomly selected individuals and 2,456 pre-filtered variants on the

chr1 region from one simulation replicate. The standard matrix (Σ) represents conventional SNP

correlations, while the adjusted matrix ($\tilde{\Sigma}$) accounts for genetic relatedness among individuals as

described in model (9) with an input heritability parameter of 0.494.

Figure S3. Comparison of fine-mapping methods for identifying causal variants across

simulation scenarios.

The y-axis shows the proportion of true causal variants correctly identified when selecting the top

k-ranked variants (x-axis, k = 1 to 20) across 12 simulation scenarios. Results are shown for

different sample sizes (5,000 and 10,000 individuals), PVE levels (1% and 4%), and numbers of

causal variants (1-3). Panels A-L represent the 12 simulation scenarios.

Figure S4. Manhattan plots for GWAS of six quantitative traits in Duroc pigs.

Manhattan plots showing GWAS results for three growth traits (off-test body weight [WT], back

fat thickness [BF], and loin muscle depth [MS]) analyzed in ~27,000 pigs and three reproduction

traits (number of piglets born alive [NBA], born dead [NBD], and weaned [NW]) analyzed in

3,290 sows. Association analyses were performed using SLEMM-GWA with ~11.7 million

quality-controlled autosomal variants. GRMs were constructed from 10,000 randomly selected

chip SNPs. Horizontal lines indicate genome-wide significance thresholds ($P < 5 \times 10^{-8}$, red) and

suggestive significance thresholds ($P < 1 \times 10^{-5}$, blue).

Figure S5. Comparison of PIPs between BFMAP-SSS and adapted summary-statistics-

based fine-mapping methods across two genomic regions.

Scatter plots comparing variant-level (A, B) and gene-level (C, D) PIPs between BFMAP-SSS and

adapted summary-statistics methods for back fat thickness. (A) and (C) show results from

chr1:51,300,453-55,300,453 including 4,350 variants. (B) and (D) show results from

chr6:144,948,358-148,948,358 including 5,195 variants. The dashed line represents y = x.

Figure S6. Impact of FINEMAP-adj iteration lengths on PIPs across two genomic regions.

Root mean square error (RMSE) (A, B) and correlation (C, D) of PIPs calculated between

BFMAP-SSS and FINEMAP-adj at variant level (red) and gene level (blue) across different

iteration settings. (A) and (C) show results from chr1:51,300,453-55,300,453, and (B) and (D)

from chr6:144,948,358-148,948,358. The x-axis represents FINEMAP-adj iteration numbers.

Asterisks (*) indicate actual iteration numbers when applying default convergence settings.

Figure S7. Impact of GRM construction on fine-mapping accuracy.

Precision-recall curves comparing FINEMAP-adj and SuSiE-adj when using different GRMs for

fine-mapping. Solid lines represent analyses using the same 10,000 chip SNPs used to construct

the GRM during the trait simulation (Simulation-10k-SNP GRM), while dashed lines represent

analyses using a different set of 10,000 randomly selected variants from the imputed sequence data

(Random-10k-variant GRM). Results are shown under different sample sizes (5,000 and 10,000

individuals), PVE levels (1% and 4%), and numbers of causal variants (1-3). Panels A-L

correspond to the 12 simulation scenarios.

Tables

Table 1. AUPRC for causal variant identification by fine-mapping methods across simulation

scenarios.

Sample size	Method	Number of causal variants						Average
		1		2		3		
		PVE=0.01	PVE=0.04	PVE=0.01	PVE=0.04	PVE=0.01	PVE=0.04	
5,000	BFMAP-SSS	0.128	0.419	0.052	0.223	0.028	0.093	0.157
	BFMAP-Forward	0.124	0.379	0.032	0.143	0.011	0.061	0.125
	FINEMAP-adj	0.126	0.381	0.051	0.173	0.030	0.080	0.140
	SuSiE-adj	0.117	0.388	0.036	0.159	0.026	0.066	0.132
	FINEMAP (LMM)	0.067	0.064	0.024	0.020	0.013	0.013	0.034
	FINEMAP (LM)	0.033	0.169	0.010	0.042	0.006	0.020	0.047
	FINEMAP-inf (LMM)	0.033	0.021	0.016	0.012	0.010	0.011	0.017
	FINEMAP-inf (LM)	0.026	0.139	0.011	0.044	0.004	0.023	0.041
	SuSiE (LMM)	0.120	0.192	0.032	0.032	0.019	0.022	0.070
	SuSiE (LM)	0.037	0.187	0.009	0.039	0.005	0.019	0.049
	SuSiE-inf (LMM)	0.021	0.027	0.009	0.016	0.005	0.009	0.015
	SuSiE-inf (LM)	0.019	0.201	0.008	0.040	0.003	0.018	0.048
10,000	BFMAP-SSS	0.188	0.468	0.096	0.378	0.077	0.199	0.234
	BFMAP-Forward	0.140	0.469	0.053	0.250	0.061	0.157	0.188
	FINEMAP-adj	0.189	0.463	0.089	0.303	0.076	0.188	0.218
	SuSiE-adj	0.207	0.478	0.086	0.225	0.066	0.149	0.202
	FINEMAP (LMM)	0.046	0.056	0.023	0.037	0.015	0.027	0.034
	FINEMAP (LM)	0.027	0.065	0.009	0.039	0.017	0.035	0.032
	FINEMAP-inf (LMM)	0.024	0.028	0.011	0.017	0.006	0.018	0.017
	FINEMAP-inf (LM)	0.023	0.070	0.006	0.043	0.014	0.017	0.029
	SuSiE (LMM)	0.109	0.051	0.040	0.038	0.024	0.032	0.049
	SuSiE (LM)	0.028	0.119	0.009	0.022	0.016	0.034	0.038
	SuSiE-inf (LMM)	0.018	0.016	0.012	0.012	0.009	0.008	0.013
	SuSiE-inf (LM)	0.011	0.059	0.004	0.021	0.007	0.022	0.021

Note: AUPRC values were calculated by varying PIP thresholds (or PCIP for BFMAP-Forward) from 0 to 1 and
computing the area under the resulting precision-recall curves. GWAS summary data were derived from GCTA-
MLMA (LMM) or PLINK 2.0 --glm (LM). Results are shown for different sample sizes (5,000 and 10,000
individuals), PVE levels (1% and 4%), and numbers of causal variants (1-3).

Table 2. AUPRC for causal gene identification by fine-mapping methods across simulation

scenarios.

Sample size	Method	Number of causal variants					
		1		2		3	
		PVE=0.01	PVE=0.04	PVE=0.01	PVE=0.04	PVE=0.01	PVE=0.04
5,000	BFMAP-SSS	0.584	0.836	0.404	0.686	0.267	0.507
	BFMAP-Forward	0.535	0.780	0.277	0.548	0.149	0.371
	FINEMAP-adj	0.574	0.811	0.403	0.622	0.265	0.479
10,000	BFMAP-SSS	0.688	0.856	0.467	0.782	0.420	0.662
	BFMAP-Forward	0.618	0.828	0.341	0.585	0.305	0.527
	FINEMAP-adj	0.693	0.852	0.455	0.721	0.406	0.635

Note: AUPRC values were calculated by varying PIP thresholds (or PCIP for BFMAP-Forward) from 0 to 1 and
computing the area under the resulting precision-recall curves. Results show the ability of three methods (BFMAP-
Forward, BFMAP-SSS, and FINEMAP-adj) to identify causal genes (defined as gene proxy blocks containing true
causal variants) under different sample sizes (5,000 and 10,000 individuals), PVE levels (1% and 4%), and numbers
of causal variants (1-3).

Figure 1

Figure 2

Figure 3

Figure 4

[A]

Linear regression

$$\mathbf{y} = \mathbf{Xb} + \mathbf{e}$$

$$\mathbf{b} \sim \mathcal{N}(0, \mathbf{I}\varphi\sigma_e^2) \qquad \mathbf{e} \sim \mathcal{N}(0, \mathbf{I}\sigma_e^2)$$

y: covariate-adjusted phenotypes.

$\mathbf{X}$: standardized genotypes for a SNP set in the candidate region.

$\mathbf{b}$: joint SNP effects for the SNP set.

φ: the ratio of per-SNP genetic variance to residual variance.

Samples of unrelated individuals

[B]

Linear mixed model

$$\mathbf{y} = \mathbf{Xb} + \mathbf{g} + \mathbf{e}$$

$$\mathbf{b} \sim \mathcal{N}(0, \mathbf{I}\varphi\sigma_e^2) \quad \mathbf{g} \sim \mathcal{N}(0, \mathbf{G}\eta\sigma_e^2) \quad \mathbf{e} \sim \mathcal{N}(0, \mathbf{I}\sigma_e^2)$$

$\mathbf{g}$: vector of individual genetic values .

$\mathbf{G}$: genomic relationship matrix to model relatedness.

$$\eta = h^2/(1 - h^2)$$

Samples of related individuals

BFMAP-Forward & BFMAP-SSS

[C]

Summary-statistic-based methods

$$\mathbf{z} \sim \mathcal{N}(0, \mathbf{\Sigma\Sigma}\varphi n + \mathbf{\Sigma})$$

Genotype correlation matrix:

$$\mathbf{\Sigma} = \mathbf{X}^\mathrm{T}\mathbf{X}/n$$

FINEMAP & SuSiE

[D]

Adapted summary-statistic-based methods

$$\mathbf{z} \sim \mathcal{N}(0, \widetilde{\mathbf{\Sigma}}\mathbf{D}\widetilde{\mathbf{\Sigma}}\varphi + \widetilde{\mathbf{\Sigma}}) \approx \mathbf{z} \sim \mathcal{N}(0, \widetilde{\mathbf{\Sigma}}\widetilde{\mathbf{\Sigma}}\varphi\tilde{n} + \widetilde{\mathbf{\Sigma}})$$

Relatedness-adjusted genotype correlation matrix:

$$\widetilde{\mathbf{\Sigma}} = \mathbf{D}^{-1/2}\mathbf{X}^\mathrm{T}\mathbf{H}^{-1}\mathbf{X}\mathbf{D}^{-1/2}$$

$$\mathbf{H} = \mathbf{G}\eta + \mathbf{I} \qquad \mathbf{D} = \mathrm{diag}(\mathbf{X}^\mathrm{T}\mathbf{H}^{-1}\mathbf{X}) \approx \mathbf{I}\tilde{n} \qquad \tilde{n} = \frac{1}{m}\sum_{i=1}^{m} \mathrm{D}_{ii}$$

FINEMAP-adj & SuSiE-adj

[E]

Modeling regional infinitesimal effects

$$\mathbf{y} = \mathbf{Xb} + \mathbf{Z}\boldsymbol{\alpha} + \mathbf{e}$$

$$\boldsymbol{\alpha} \sim \mathcal{N}(0, \mathbf{I}\tau^2)$$

$\mathbf{Z}$: genotype matrix for all SNPs in the candidate region.

$\boldsymbol{\alpha}$: infinitesimal effects for all SNPs in the candidate region.

FINEMAP-inf & SuSiE-inf

[F]

Output

Posterior inclusion probability (PIP)

PIP for variant j: $\mathrm{PIP}_j = \sum_{M \in \Gamma} \mathbb{I}(j \in M)P(M|D)$

PIP for a gene: $\mathrm{PIP}_{\mathrm{gene}} = \sum_{M \in \Gamma} \mathbb{I}(\mathrm{gene} \cap M \neq \emptyset)P(M|D)$

Available for BFMAP, FINEMAP, and FINEMAP-adj