Fiber orientation downsampling compromises the computation of white matter tract-related deformation

Zhou Zhou,1 Teng Wang, 2 Daniel Jörgens,2,3 Xiaogai Li1

1 Division of Neuronic Engineering, KTH Royal Institute of Technology, Stockholm, 14152, Sweden.
2 Division of Biomedical Imaging, KTH Royal Institute of Technology, Stockholm, 14152, Sweden.
3 Division of Brain, Imaging, and Behaviour, Krembil Research Institute, Toronto Western Hospital, University Health Network, Ontario, M5T 2S8, Canada.

Corresponding author. Email: zhouz@kth.edu
Abstract

Incorporating neuroimaging-revealed structural details into finite element (FE) head models opens vast new opportunities to better understand brain injury mechanisms. Recently, growing efforts have been made to integrate fiber orientation from diffusion tensor imaging (DTI) into FE models to predict white matter (WM) tract-related deformation that is biomechanically characterized by tract-related strains. Commonly used approaches often downsample the spatially enriched fiber orientation to match the FE resolution with one orientation per element (i.e., element-wise orientation implementation). However, the validity of such downsampling operation and corresponding influences on the computed tract-related strains remain elusive. To address this, the current study proposed a new approach to integrate voxel-wise fiber orientation from one DTI atlas (isotropic resolution of 1 mm\(^3\)) into FE models by embedding orientations from multiple voxels within one element (i.e., voxel-wise orientation implementation). By setting the responses revealed by the newly proposed voxel-wise orientation implementation as the reference, we evaluated the reliability of two previous downsampling approaches by examining the downsampled fiber orientation and the computationally predicted tract-related strains secondary to one concussive impact. Two FE models with varying element sizes (i.e., 6.37 ± 1.60 mm and 1.28 ± 0.55 mm, respectively) were incorporated. The results showed that, for the model with a large voxel-mesh resolution mismatch, the downsampled element-wise fiber orientation, with respect to its voxel-wise counterpart, exhibited an absolute deviation over 30° across the WM/gray matter interface and the pons regions. Accordingly, this orientation deviation compromised the computation of tract-related strains with normalized root-mean-square errors up to 30% and underestimated the peak tract-related strains up to 10%. For the other FE model with finer meshes, the downsampling-induced effects were lower, both on the fiber orientation and tract-related strains. Taken together, the voxel-wise orientation implementation is recommended in future studies as it leverages the DTI-delineated fiber orientation to a larger extent than the element-wise orientation implementation. Thus, this study yields novel insights on integrating neuroimaging-revealed fiber orientation into FE models and may better inform the computation of WM tract-related deformation,
which are crucial for advancing the etiological understanding and computational predictability of brain injury.

**Keywords**

Finite element model; Diffusion tensor imaging; Resolution mismatch; Fiber orientation downsampling; White matter tract-related deformation;

**Graphic abstract**
1. Introduction

Traumatic brain injury (TBI) is a disruption in the brain’s normal function or other evidence of brain pathology secondary to an external insult, typically in the form of direct head impact and inertial loading (Menon et al., 2010). Depending on the severity of insults, the outcome of TBI may vary from temporary unconsciousness accompanied by transient neuronal circuit dysfunction, e.g., concussion (Wolf et al., 2017), to persistent vegetative state along with profound neuronal apoptosis throughout the white matter (WM), e.g., diffuse axonal injury (Maxwell et al., 2003). Given its high morbidity and mortality and the large number of people affected (Brazinova et al., 2021; Peterson et al., 2019), TBI is a critical public health and socio-economic threat worldwide. Sadly, current prediction, prevention and diagnosis strategies for brain injury are still largely in their infancy due to a lack of fundamental understanding of TBI pathogenesis.

Biomechanical models based on the finite element (FE) method are promising instruments to decipher the physics underlying TBI. As numerical surrogates, FE head models can resolve geometrical and mechanical complexities of the human head as well as interfacial conditions among various intracranial components. Many FE models have been established over the past decades in light of their immense potential to explore the pathomechanical cascades from external insults, localized tissue responses, and resultant brain injury (see review articles (Giudice et al., 2019; Madhukar and Ostoja-Starzewski, 2019; Yang and Mao, 2019)). Particularly, advances in neuroimaging, that delineates intracranial structures in a non-invasive fashion, largely accelerate the improvement of anatomical representations in contemporary head models. For example, by leveraging high-resolution computed tomography scans and angiography, several three-dimensional (3D) head models have successfully captured cranial morphology (De Kegel et al., 2019; Li et al., 2017, 2019) and cerebral vasculature (Ho and Kleiven, 2007; Subramaniam et al., 2021; Zhao and Ji, 2020), respectively. Such FE models with high-level structural details often possess fine meshes in order to appropriately resolve the geometrical complexities. For instance, two recent brain models with conforming hexahedral meshes that captured the morphological heterogeneity of the cerebral cortex (i.e., gyri and sulci) and lateral...
ventricles exhibited a mean mesh size of 0.85 mm with up to 1.2 million elements for the brain (Li et al., 2021; Zhou et al., 2022; Zhou et al., 2019b). For head models with smoothed brain surfaces, the number of brain elements varied from 5 k to 202 k with mesh resolutions of 1.8 - 6 mm (Chatelin et al., 2011; Kleiven and von Holst, 2002; Mao et al., 2013; Zhao and Ji, 2019a; Zhou et al., 2016).

Partially inspired by the experimental findings that functional impairment and morphological damage of axonal fibers were relevant to the strain regime imposed on the experimental tissue (LaPlaca et al., 2007; Montanino, 2020; Morrison III et al., 2011; Wu et al., 2021b), fiber orientation delineated by diffusion tensor imaging (DTI) has been integrated into FE models in recent years to inform the computation of axonal fiber deformation. Thus far, various techniques have been proposed for such an integration. For example, Zhou et al. (2021a) projected the strain tensor along the real-time fiber orientation to obtain the deformation along the fiber tracts (i.e., tract-oriented strain, which is alternatively termed as axonal strain or fiber strain in the literature), while Giordano et al. (2014) instead simulated the brain as a hyper-viscoelastic fiber-reinforced anisotropic medium with the fiber orientation integrated into the constitutive law to inform the fiber reinforcement. In these two referred studies, a critical issue of resolution mismatch between FE and DTI voxel exists. To address this, the voxel-wise fiber orientation in DTI was spatially downsampled and then implemented into FE models with one synthetic orientation per element (referred to as element-wise orientation implementation, hereafter). The process of spatially resampling orientation information in DTI voxels to match the FE resolution is referred to as orientation downsampling. This or similar element-wise orientation implementation technique has been used in other studies (Chatelin et al., 2011; Colgan et al., 2010; Giordano and Kleiven, 2014; Giordano et al., 2017; Hernandez et al., 2019; Kraft and Dagro, 2011; Kraft et al., 2012; Laksari et al., 2020; Sahoo et al., 2016; Sullivan et al., 2015; Zhao and Ji, 2019b; Zhou et al., 2021b). To circumvent the orientation downsampling, Garimella et al. (2019) explicitly incorporated the whole WM fiber tractography reconstructed from DTI into a head model in which multiple fibers were embedded within one WM element, while Ji et al. (2015) transformed the fiber orientation of WM voxels from the DTI space into the coordinate system of the FE head model then...
computed the tract-oriented strain at the voxel level by resolving the strain tensor of the WM element from pre-computed simulation to the fiber orientation of these transformed voxels. Regardless of these above-described disparities as well as other model-specific choices, maximum tract-oriented strain has been congruently reported as an appropriate measure of injury by several independent groups (Giordano and Kleiven, 2014; Wu et al., 2021a; Zhao et al., 2017; Zhou et al., 2021b). More recently, Zhou et al. (2021b) proposed three new tract-related strain metrics, measuring the normal deformation perpendicular to the fiber tracts (i.e., tract-perpendicular strain), and shear deformation along and perpendicular to the fiber tracts (i.e., axial-shear strain and lateral-shear strain, respectively), all of which exhibited superior injury predictability over maximum principal strain. Note that the tract-oriented strain, tract-perpendicular strain, axial-shear strain, and lateral-shear strain are collectively referred to as tract-related strains, each of which characterizes one aspect of the loading regime endured by the fiber tracts.

Given that the computation of any tract-related strain is directly dependent on the fiber orientation, appropriate integration of DTI-delineated fiber orientation into FE models is crucial. When limited to the element-wise orientation implementation involving orientation downsampling, the validity of the orientation downsampling operation has not been appropriately verified. For example, Giordano et al. (2014) averaged the fiber orientation obtained from DTI with a resolution of 2 mm × 2 mm × 3.6 mm to match the resolution of an FE model with an average element size of 6 mm. Similarly, Sahoo et al. (2014) downsampled the fiber orientation from a DTI atlas with an isotropic resolution of 1 mm³ for another FE model with mesh sizes ranging from 1.14 mm to 7.73 mm. Nevertheless, neither study has quantitatively compared the downsampled orientation information with its counterparts originally conveyed in DTI. Moreover, how the downsampling procedures affect the FE-derived tract-related strains remains to be systematically assessed.

Thus, the aim of the current study is to quantitatively evaluate the consequence of orientation downsampling on the computed WM tract-related deformation. To achieve this, a new approach was proposed to integrate the voxel-wise fiber orientation in DTI into FE models by embedding fiber
orientations from multiple voxels within one element. This new approach and two existing
downsampling algorithms were respectively implemented into two FE head models with different
levels of mesh sizes. By setting the responses determined by the newly proposed voxel-wise
implementation as the reference, the reliability of two alternative downsampling approaches was
quantitatively evaluated. We thus tested the hypothesis that orientation downsampling causes a
systematical loss of orientation information and further compromises the computation of tract-related
strains.

2. Methods

2.1. Finite element brain models

Two previously developed head models with different mesh resolutions were used in this
study, i.e., the KTH model (Kleiven, 2007) (Fig. 1A-B) and the ADAPT model (Li et al., 2021) (Fig. 1C-D).
Each model consists of critical head components, including gray matter, WM, skull, scalp, subarachnoid
cerebrospinal fluid (CSF), ventricles, superior sagittal sinus, transverse sinus, meninges, falx, and
tentorium. The brain in both models was discretized by hexahedral elements with spatially
heterogeneous element sizes. Following the tissue classification protocol proposed by Zhou et al.
(2021b), the KTH model includes 1197 WM elements with a resolution of 6.37 ± 1.60 mm (range of
1.96 - 9.83 mm); the ADAPT model contains 113678 WM elements with a mesh size of 1.28 ± 0.55 mm
(range of 0.34 - 3.23 mm). Numerical commonalities and differences between these two models are
summarized in Table A1 in Appendix as well as previous studies (Kleiven and von Holst, 2002; Li et al.,
2021). Responses of both models have shown good correlation with experiments of brain strain, brain-
skull relative motion, and intracranial pressure (Kleiven, 2006; Li et al., 2021; Zhou et al., 2019c; Zhou
et al., 2019d; Zhou et al., 2018). Both models have been used to uncover the brain injury mechanism
(Kleiven and von Holst, 2002; Li, 2021; Zhou et al., 2019a), evaluate the brain injury risk (Kleiven, 2007;
Zhan et al., 2021), and inform the contrivance of advanced protective devices and treatment strategies
(Fahlstedt et al., 2021; Wang et al., 2020).
Fig. 1. Two finite element head models with varying mesh resolutions. For the KTH head model with relatively coarse mesh, an isometric view of the head with the skull open to expose the brain is presented in subfigure (A) in which a skull-fixed coordinate system with the origin at the head’s center of gravity, while the pia mater and white matter are shown in subfigure (B) with the pia mater in translucency. Similar views are presented for the ADAPT head model with relatively fine mesh in subfigures (C) and (D). The brain FE elements are shown with mesh outlines in subfigures (A) and (C) to illustrate the mesh resolution.

2.2. Implementation of element-wise fiber orientation into FE brain models

To compute WM fiber tract-related deformation, fiber orientation from an open-access ICBM DTI-81 atlas (181 × 217 × 181 voxels, 1 mm isotropic, Fig. 2A) (Mori et al., 2008) was respectively integrated into the KTH model and ADAPT model using two previously proposed downsampling approaches. As exemplified by the KTH model in Fig. 2, the brain mesh was voxelized to obtain a reference volume (Fig. 2B), which was further aligned with the brain volume of the ICBM DTI-81 atlas via a diffeomorphic Demon registration (Li et al., 2021) (Fig. 2C). Then, for each WM element in the brain model, corresponding voxels in the DTI atlas enclosed by the given element were identified (Fig. 2D). Similarly, a registration operation was also conducted to spatially align the ICBM DTI-81 atlas with the brain mask of the ADAPT model.
Fig. 2. Spatial alignment between the DTI volume (i.e., ICBM DTI-81 atlas in subfigure (A)) and the brain mask of KTH model (B) with the outcome shown in subfigure C. For each WM element in the brain model, corresponding voxels in the DTI atlas enclosed by the given element were identified, which is illustrated by one representative element in subfigure D. Note that the DTI voxels in subfigure D are illustrated as spheres to show the voxel positions, while these spheres do not indicate these voxels are structurally isotropic.

To integrate the fiber orientation from multiple voxels into each WM element (Fig. 2D) toward element-wise orientation implementation, either the first eigenvectors of the diffusion tensors or the diffusion tensors themselves in these identified voxels were respectively downsampled using equations (1) (referred to as vector-averaged approach) and (2) (referred to as tensor-averaged approach) via a distance-weighted averaging scheme. In this scheme, the information from those voxels closer to the centroid of the element was more heavily weighted:

\[
\mathbf{v}_{\text{elem}} = \frac{\sum_{i=1}^{N} \mathbf{v}_i e^{-d_i}}{\sum_{i=1}^{N} e^{-d_i}} \tag{1}
\]

\[
\mathbf{T}_{\text{elem}} = \frac{\sum_{i=1}^{N} \mathbf{T}_i e^{-d_i}}{\sum_{i=1}^{N} e^{-d_i}} \tag{2}
\]

where \(\mathbf{v}_{\text{elem}}\) and \(\mathbf{T}_{\text{elem}}\) are respectively the mean first eigenvector and the mean diffusion tensor calculated for each WM element; \(N\) is the number of selected voxels for the respective WM element; \(\mathbf{v}_i\) and \(\mathbf{T}_i\) are respectively the first eigenvector and diffusion tensor of each selected voxel; \(d_i\) is the distance from the voxel to the element centroid. Note that, before the implementation of equation (1), the angle between \(\mathbf{v}_i\) and a preselected reference vector (i.e., the X-axis in the skull-fixed
coordinate system in Fig. 1 in the current study) was examined. Under the condition that the angle was greater than 90°, the direction of \( \mathbf{v}_i \) would be flipped (i.e., \(-\mathbf{v}_i\)). As highlighted by Zhao and Ji (2019b), such a flip operation was needed since fiber orientation is expressed with either \( \mathbf{v}_i \) or \(-\mathbf{v}_i\), and it is necessary to ensure the consistency in the eigenvector across all the voxels and circumvent improper cancellation in equation (1).

The resultant orientation from equations (1) and (2) was respectively implemented at an element-wise basis. For the vector-averaged approach (equation 1), \( \mathbf{v}_{elem} \) was considered the mean fiber orientation for each element (Fig. 3A), similar to the approach in Chatelin et al. (2011) and Zhao and Ji (2019b). For the tensor-weighted approach (equation 2), the first eigenvector of \( \mathbf{T}_{elem} \) was regarded as the mean orientation for each element (Fig. 3B), the same as the strategies in Zhou et al. (2021b) and Giordano et al. (2014).

![Fig. 3. Color-coded orientation maps with the orientation implemented either at an element-wise basis using the vector-averaged approach (A) and tensor-averaged approach (B) or at a voxel-wise basis using the voxel-wise approach (C). The outline of the brain mask with the differentiation of ventricles used for image registration is superimposed to the orientation map.](image)

### 2.3. Implementation of voxel-wise fiber orientation into FE brain models
To circumvent the downsampling procedures, we proposed a new approach by embedding orientations from multiple voxels within one element toward voxel-wise orientation implementation. In the same way as for the two downsampling approaches described above, DTI voxels enclosed by each WM element were identified at first based on their spatial correspondence (Fig. 2D). For each WM element, the first eigenvectors of all identified voxels (i.e., $v_i$ in equation (1)) were wholly embedded into a given element without downsampling (see section 2.4). Thus, the fiber orientation was implemented at a voxel-wise basis (referred to as the voxel-wise approach hereafter) with an isotropic resolution of 1 mm$^3$ given by the DTI atlas (Fig. 3C).

2.4. Real-time fiber orientation for the computation of tract-related strains

To inform the computation of tract-related strains with real-time fiber orientation, an embedded element approach was leveraged to track the real-time fiber orientation following the approach presented earlier (Zhou et al., 2021a). For all the three above-mentioned approaches, the orientation information was concretely represented by truss elements (serving as slave elements) which were embedded within the WM elements (serving as master elements). Note that the truss elements only served as instruments to monitor the temporal orientation of fiber tracts at each time step (Zhou et al., 2021a). They were simulated as a null constitutive model with nominal density and cross-sectional area (see Table A2 in Appendix or a previous work (Zhou et al., 2021a)) and do not contribute any mechanical stiffness. Thus, the current study does not suffer from volume redundancy or stiffness redundancy, which are two commonly-seen drawbacks of the embedded element method (Garimella et al., 2019).

For both the vector-averaged and tensor-averaged approaches, only one truss element was embedded per WM element. In particular, for the vector-averaged approach, the truss element is oriented in the same direction as that of $v_{elem}$, while, for the tensor-averaged approach, the direction of the truss elements is aligned with the first eigenvector of $T_{elem}$. For the voxel-wise approach, multiple truss elements were embedded in one WM element, in which truss elements angled along
the direction of the first eigenvector of those voxels (i.e., $v_i$ in equation (1)) within the given element.

As is common across the three approaches, both ends of the truss elements fell within the boundaries of their master elements by adjusting the length of the embedded truss elements. Thus, nodal motion of a given truss element was governed exclusively by its master element. Consequently, the real-time fiber orientation during head impacts was reflected by the temporal direction of the truss element, which was updated at each solution cycle of the time-marching simulation.

To compute WM tract-related deformation, both the Green-Lagrange strain tensors for all WM elements and the orientation of embedded truss elements were iteratively obtained at each timestep from pre-computed simulations within the global coordinate system. The strain tensor of each WM element was further rotated to the coordinate systems with one axis aligned with the real-time fiber orientation, through which four strain-based metrics relating to the fiber deformation were extracted (Fig. 3), i.e., tract-oriented strain, tract-perpendicular strain, axial-shear strain, and lateral-shear strain. For the vector-averaged approach, the strain tensor of each WM element was only related to one real-time fiber orientation, which is also the case for the tensor-averaged approach. For the voxel-wise approach, the strain tensor of one given WM element was related to the temporal direction of all the truss elements encased by the given WM element.

The implementation of the embedded element method for tracking the real-time fiber orientation and the computation of the four tract-related strains are described with greater details in Zhou et al. (2021a) and Zhou et al. (2021b), respectively.
**Fig. 4.** Illustration of the four tract-related strains with respect to the fiber tract. Tract-oriented strain and tract-perpendicular strain measure the normal deformation along and perpendicular to the fiber tracts, while axial-shear strain and lateral-shear strain measure shear deformation along and perpendicular to the fiber tracts.

### 2.5. Impact simulation

To study the influence of fiber orientation downsampling on the computation of tract-related deformation, a concussive impact (i.e., case 157H2) from the National Football League dataset (Sanchez et al., 2019) was simulated using the KTH model and the ADAPT model with embedded fiber orientation implemented by the vector-averaged approach, tensor-averaged approach, and voxel-wise approach, respectively. In case 157H2, the football player was laterally struck, resulting in high angular velocities in the coronal and sagittal planes. In the simulation, the translational and rotational velocities were prescribed to the rigid skull with the velocity profiles expressed with respect to the skull-fixed coordinate system. The impact was recorded for 50 ms with the computational time detailed in Table 1. The model responses were output at every 1 ms.

<table>
<thead>
<tr>
<th>Time</th>
<th>Vector-averaged approach</th>
<th>Tensor-averaged approach</th>
<th>Voxel-wise approach</th>
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<tbody>
<tr>
<td>KTH model</td>
<td>50 minutes</td>
<td>50 minutes</td>
<td>4 hours</td>
</tr>
<tr>
<td>ADAPT model</td>
<td>33 hours</td>
<td>33 hours</td>
<td>67 hours</td>
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</table>

### 2.6. Data analysis

Identical to those of the orientation information being integrated into the FE models, spatial resolutions of FE-derived responses were at the voxel level for the voxel-wise approach and at the element level for the vector- and tensor-averaged approaches. To address this disparity, all responses were mapped back to the imaging space of the ICBM DTI-81 atlas. This was intuitive for the voxel-wise approach, given that a one-to-one correspondence between the voxel and truss element was established. For the tensor- and vector-averaged approaches in which orientation information in multiple voxels was downsamped to be a single vector and further embedded in one WM element in the form of one truss element, responses based on the single truss element were assigned to all the voxels enclosed by the given WM element. Such mapping operations synchronized the response...
resolutions and facilitated direct comparisons among the three approaches. Response-encoded contours were generated in the imaging space.

To quantify the local fiber orientation embedded within the FE models, the skull-fixed coordinate system was selected as the reference. Adapting the strategy by Giordano et al. (2017), the fiber orientation was expressed in terms of two Eulerian angles, i.e., elevation angle ($\alpha$) and azimuth angle ($\beta$) (Fig. 5, Table 2A). To identify the localized alteration of fiber orientation associated with the downsampling procedures by either the vector- or tensor-averaged approaches, absolute deviations in elevation angle and azimuth angle between the voxel-wise approach and each of the two downsampling approaches were calculated at the voxel-wise level, respectively (Table 2B).

![Fig. 5. Characterization of the fiber orientation (gray arrow in solid line) by means of elevation angle ($\alpha \in [0^\circ, 90^\circ]$) and azimuth angle ($\beta \in [0^\circ, 90^\circ]$). These angles are expressed with respect to the skull-fixed coordinate system with a whole-head thumbnail on the top-left corner.](image)

To further evaluate the consequence of orientation downsampling on the computation of fiber deformation, four tract-related strains (Fig. 4 and Table 2A) were extracted from FE models with the real-time fiber orientation described above. For each of the four strains, the absolute difference between the voxel-wise approach and two downsampled approaches was respectively calculated per voxel (Table 2B) and was further expressed in the form of normalized root-mean-square error (NRMSE; normalized by the mean value determined by the voxel-wise approach). To quantify the influence of the orientation downsampling on the peak strain responses, the 95th percentile maximum values of four tract-related strains were extracted across the whole WM. All data analyses were performed in MATLAB (2016b; Mathworks, Natick, MA).

**Table 2** – Summary of variables quantifying the fiber orientation implemented by three approaches and tract-related strains (A) and expression quantifying the absolute differences associated with the orientation downsampling (B). In each variable, the subscript indicates the basis that the orientation information is
implemented (i.e., \( vxl \) for the voxel-wise basis, \( elm \) for the element-wise basis), while the superscript indicates the orientation downsampling approaches (i.e., \( v \) for vector-averaged approach, \( T \) for tensor-averaged approach).

<table>
<thead>
<tr>
<th>A</th>
<th>Variable</th>
<th>Description</th>
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<tbody>
<tr>
<td>( \alpha_{vxl}, \alpha^v_{elm}, \alpha^T_{elm} )</td>
<td>Elevation angle of the undeformed fiber orientation implemented by voxel-wise approach, vector-averaged approach, and tensor-averaged approach, respectively.</td>
<td></td>
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<tr>
<td>( \beta_{vxl}, \beta^v_{elm}, \beta^T_{elm} )</td>
<td>Azimuth angle of the undeformed fiber orientation implemented by voxel-wise approach, vector-averaged approach, and tensor-averaged approach, respectively.</td>
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<tr>
<td>( MTOS_{vxl}, MTOS^v_{elm}, MTOS^T_{elm} )</td>
<td>Peak of tract-oriented strain across the entire simulation with the fiber orientation implemented by voxel-wise approach, vector-averaged approach, and tensor-averaged approach, respectively.</td>
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<tr>
<td>( MTPS_{vxl}, MTPS^v_{elm}, MTPS^T_{elm} )</td>
<td>Peak of tract-perpendicular strain across the entire simulation with the fiber orientation implemented by voxel-wise approach, vector-averaged approach, and tensor-averaged approach, respectively.</td>
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<tr>
<td>( MASS_{vxl}, MASS^v_{elm}, MASS^T_{elm} )</td>
<td>Peak of axial shear strain across the entire simulation with the fiber orientation implemented by voxel-wise approach, vector-averaged approach, and tensor-averaged approach, respectively.</td>
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<tr>
<td>( MLSS_{vxl}, MLSS^v_{elm}, MLSS^T_{elm} )</td>
<td>Peak of lateral shear strain across the entire simulation with the fiber orientation implemented by voxel-wise approach, vector-averaged approach, and tensor-averaged approach, respectively.</td>
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<tr>
<th>B</th>
<th>Expression</th>
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<td>\alpha_{vxl} - \alpha^v_{elm}</td>
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<td>MLSS_{vxl} - MLSS^v_{elm}</td>
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### 3. Results

To clarify the differences in elevation angle and azimuth angle quantifying the fiber orientation integrated into FE models and four tract-related strains measuring the deformation of fiber tracts among the three orientation implementation approaches, this section is organized in a hierarchical
order to facilitate the readers’ understanding. We firstly illustrate the analysis based on the results of one randomly selected WM element of each FE model and then extend the analysis across the whole white matter region.

### 3.1 Effects of orientation downsampling on the responses of one representative element

For one representative WM element in the KTH model (Fig. 6A-C) encasing 361 voxels, the mean values for $\alpha_{vxt}$ and $\beta_{vxt}$ in the voxel-wise approach were 64.1° (range of 47.8° - 89.5°) and 66.3° (range of 54.6° - 73.3°), respectively. Due to the downsampling operation, the resultant elevation and azimuth angles were 66.7° ($\alpha_{eelm}^v$) and 66.2°($\beta_{eelm}^v$) for the vector-averaged approach, and 61.9°($\alpha_{eelm}^T$) and 64.8°($\beta_{eelm}^T$) for the tensor-averaged approach, all of which fell within the range measured from the voxel-wise approach (Fig. 6B). Similarly, the range of each tract-related strain calculated from the voxel-wise approach covered its counterparts by the two downsampling approaches (Fig. 6C). Using the results determined by the voxel-wise approach as the reference, the NRMSE values ranged from 4.2% in MASS to 25.4% in MTPS for the vector-averaged approach, and from 4.7% in MASS to 25.9% in MTPS for the tensor-averaged approach.

A similar analysis was performed on one randomly-selected element enclosing 36 voxels in the ADAPT head model (Fig. 6D-F). All the response variables of interest determined by the voxel-wise approach covered their counterparts from the two downsampling approaches. For fiber orientation, the voxel-wise approach (Fig. 6D) exhibited a range of 38.9° – 47.1° for $\alpha_{vxt}$ (mean value: 42.3°) and 49.6° - 58.8° for $\beta_{vxt}$ (mean value: 53.1°), while fiber angles measured from the vector- and tensor-averaged approaches were commensurable with each other (i.e., $\alpha_{eelm}^v$: 42.3° vs. $\alpha_{eelm}^T$: 42.3°; $\beta_{eelm}^v$: 53.1° vs. $\beta_{eelm}^T$: 52.9°) (Fig. 6E). For the strain-based metrics, the two downsampling approaches lead to nearly identical values in all four tract-related strains (Fig. 6F). The NRMSE values for the tensor-average approach spanned from 1.8% (MASS) to 5.7% (MTOS) compared with the voxel-wise approach. The same NRMSE values were also noted for the vector-average approach when limiting the precision to one digit.
**Fig. 6.** (A) Embedded truss elements implemented in one representative WM element in the KTH model with a whole-head thumbnail showing the view angle. The truss elements are coloured in blue and red for the vector- and tensor-averaged approaches, respectively, while in gray for the voxel-wise approach. (B) Boxplots of elevation angle ($\alpha$) and azimuth angle ($\beta$) of the truss elements in subfigure (A). (C) Boxplots of four tract-related strains for the representative element in subfigure (A). Similar figures are also shown for one representative WM element in the ADAPT model in subfigures (D-F) in the right column. Note that in subfigures (A) and (B), the representative WM element enclosed 361 voxels for the KTH model and 32 voxels for the ADAPT model. Thus, some of the truss elements (in grey) implemented by the voxel-wise approach were overlapped with each other from the given view angles.

### 3.2 Effects of orientation downsampling on the responses of whole white matter region

The above-described analysis illustrated by one representative element per model was extended to the whole WM region. To quantify the extent of orientation downsampling in both brain models, the number of voxels identified for each WM element was examined. For the KTH model, the number of voxels per WM element was $312 \pm 198$ (range of 6-980) (**Fig. 7A**). Consequently, 1197 truss elements were respectively embedded per the implementation of vector- and tensor-averaged approaches, while 373976 truss elements for the voxel-wise approach (**Fig. 7C**). For the ADAPT model, a mean of 3 voxels (range of 1-57) was identified for a typical WM element (**Fig. 7B**). The numbers of truss elements introduced by both downsampling approaches were 113678, in comparison with 433299 by the voxel-wise approach (**Fig. 7D**).
Fig. 7. Number of DTI voxels selected for each of the WM element (A-B) and brain model with WM elements and embedded truss elements implemented by the voxel-wise approach (C-D) in the KTH model (left column) and ADAPT model (right column). For better illustration, the brain model in subfigures (C) and (D) is shown in translucency with the WM element in only one hemisphere being visible.

In both models, the three approaches resulted in similar distributions of $\alpha$ in the deep brain regions, such as the corpus callosum with the $\alpha$ consistently around 90°. Nevertheless, in the KTH model, the absolute deviation in $\alpha$ over 30° due to the orientation downsampling exhibited a patchy distribution, spreading across the WM/gray matter interface and the pons regions (highlighted in Fig. 8A). Such patchily-distributed differences were not seen in the ADAPT model with relatively fine meshes, in which only a handful of isolated voxels with absolute differences in $\alpha$ over 30° were revealed. Similar trends were also noted in $\beta$ (Fig. A1 in Appendix).
Fig. 8. Coronal cross-sections of elevation angle ($\alpha$) of fiber orientation (A) and MTOS (B) determined by the voxel-wise approach and two downsampling approaches along with the absolute difference associated with fiber orientation downsampling. Each cross-section is provided at the whole-brain level along with an enlarged view for the pons regions, in which the gray matter region is colored in dark gray.

To evaluate the consequence of orientation downsampling on the computation of fiber deformation, four tract-related strains were calculated from both models with the fiber orientation...
either directly implemented at the voxel-wise level or downsampled to the element-wise level. For the KTH model (Fig. 8B), both downsampling approaches introduced considerable differences (i.e., absolute difference exceeding 0.1) in MTOS, particularly in the pons regions. The NRMSE values across the WM region were 36.0% and 35.2% for the vector- and tensor-averaged approaches, respectively (Table 3). Similar trends were also noted for the other three tract-related strains (Fig. A2 in Appendix). Quantitatively, the NRMSE values of other three tract-related strains across all WM region ranged from 19.0% (MLSS) to 22.8% (MTPS) for the vector-averaged approach, and from 18.5% (MLSS) to 22.0% (MTPS) for the tensor-averaged approach (Table 3).

When switching to the ADAPT model, orientation downsampling only introduced absolute differences of MTOS over 0.1 to a few voxels (Fig. 8B). This was further confirmed by the NRMSR value based on MTOS (Table 3), i.e., 4.5% for the vector-averaged approach and 4.6% for the tensor-averaged approach. Consistent with that of MTOS, the NRMSE values for the other three tract-related strains in the ADAPT model were consistently less than 5% both for the vector- and tensor-averaged approaches (Table 3). Strain contours of the resting three tract-related strains for the ADATP model are shown in Fig. A2 in Appendix.

Table 3 – NRMSE in tract-related strains associated with fiber orientation downsampling in the KTH and ADAPT models. (A) Voxel-wise approach vs. Vector-averaged approach; (B) Voxel-wise approach vs. Tensor-averaged approach. The NRMSE values were computed across all WM voxels.

<table>
<thead>
<tr>
<th>A</th>
<th>NRMSE (%)</th>
<th>KTH model</th>
<th>ADAPT model</th>
<th>B</th>
<th>NRMSE (%)</th>
<th>KTH model</th>
<th>ADAPT model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Voxel-wise approach vs. Vector-averaged approach</td>
<td>MTOS</td>
<td>36.0</td>
<td>4.5</td>
<td>MTOS</td>
<td>35.2</td>
<td>4.6</td>
<td></td>
</tr>
<tr>
<td></td>
<td>MTPS</td>
<td>22.8</td>
<td>3.5</td>
<td>MTPS</td>
<td>22.0</td>
<td>3.5</td>
<td></td>
</tr>
<tr>
<td></td>
<td>MASS</td>
<td>20.6</td>
<td>3.2</td>
<td>MASS</td>
<td>20.1</td>
<td>3.1</td>
<td></td>
</tr>
<tr>
<td></td>
<td>MLSS</td>
<td>19.0</td>
<td>2.8</td>
<td>MLSS</td>
<td>18.5</td>
<td>2.8</td>
<td></td>
</tr>
</tbody>
</table>

We further quantified the influence of the orientation downsampling on the peak tract-related deformation by extracting the 95th percentile value of maximum tract-related strains across the whole WM region (Fig. 9). When limiting the comparison to the two downsampling approaches, only minor differences (less than 1%) were found between them independent of the strain types and FE models.
When extending the comparison by incorporating the voxel-wise approach, the tensor-averaged downsampling approach underestimated the peak strains in the KTH model ranging from 1.7% in MTOS to 12.4% in MASS. For the ADAPT model, the differences in the peak values between the voxel-wise approach and the two downsampling approaches were consistently less than 1%.

Fig. 9. Comparison of 95th percentile maximum tract-related strains determined by the voxel-wise approach and the two downsampling approaches in the KTH and ADAPT models.

4. Discussions

The current work proposed a new approach to incorporate voxel-wise fiber orientation from DTI into FE models by embedding orientations from multiple voxels within one element and evaluated the reliability of two previously-used orientation downsampling approaches with one orientation per element. By setting the responses from the voxel-wise implementation as the reference, it was verified that, for a model with a large mesh-image resolution mismatch, the orientation downsampling introduced an absolute deviation of fiber orientation over 30° across the WM/gray matter interface and the pons regions. This further compromised the computation of tract-related strains with the NRSMR values up to 30% and underestimated the peak tract-related strains up to 10%. For the other FE model with finer meshes, the downsampling-induced effect was lower, both on the fiber orientation and tract-related strains. Taken together, the voxel-wise orientation implementation is recommended in future studies as it leverages the DTI-delineated fiber orientation to a larger extent than the element-wise orientation implementation.
4.1 Implementing DTI-delineated fiber orientation into finite element brain models

In light of their orientation-dependent natures, tract-related strains require fiber orientation information to inform their computation. Although DTI has been available for decades to delineate axonal tracts, challenges remain on how to adequately integrate the high-resolution fiber orientation into FE models with nonidentical mesh resolutions. In preference to the element-wise orientation implementation with only one fiber orientation embedded within one WM element (e.g., the vector- and tensor-averaged approaches evaluated in the current work), the voxel-wise approach proposed in the current study addressed the mesh-imaging resolution mismatch by embedding orientation from multiple voxels within one element. This voxel-wise approach further served as the reference to evaluate the reliability of the vector- and tensor-averaged approaches. As enumerated by the NRMSE values and underestimated peak strain responses, our work quantified the loss of orientation information due to downsampling and the consequently compromised computation of tract-related strains, which is particularly true for the model with coarse meshes.

When comparing the results across all three approaches (one with, and two without downsampling), it was found that responses of these two downsampling approaches fell within the range of their counterparts by the voxel-wise approach, as partially demonstrated by one representative element per model (Fig. 6). Such findings provided certain support to the vector- and tensor-averaged approaches and indicated that the results in previous studies based on downsampled approaches were not absurdly inaccurate, such as the one by Zhou et al. (2021a) using the tensor-averaged approach and the other by Chatelin et al. (2011) using the vector-averaged approach. Despite this, incorporating voxel-wise fiber directions without downsampling (e.g., the voxel-wise approach in the current study) provides a better representation of WM fiber orientation and should be regarded as the rule of thumb.

When limiting the comparison to the results revealed by the vector- and tensor-averaged approaches, these two schemes performed alike, regardless of the FE models. This was substantiated
by the similar distribution and magnitude of orientation information and tract-related strains revealed by these two approaches (Fig. 8, Fig. 9, and Table 3). Such similar performances were expected given that both approaches practically downsampled the same orientation information from DTI, with the only difference being the sequential order of eigenvector computation and the distance-weighted averaging. For the vector-averaged approach, the principal eigenvectors of tensors in these voxels enclosed by one WM element were computed at first. Then all eigenvectors were averaged by a set of weighting factors based on the distances between the DTI voxels and elemental centroid, outputting a single synthetic vector as the mean fiber orientation of the given element. For the tensor-averaged approach, the tensors of all enclosed DTI voxels were averaged at first with the output as a synthetic tensor, and then the principal eigenvector of the synthetic tensor was regarded as the mean fiber direction. In the current study, the same weighting factors were used in both averaging approaches, which further explained the similar performances between the vector- and tensor-averaged approaches.

Compared with the voxel-wise approach proposed in the current study, another promising alternative that could largely leverage the DTI-delineated orientation information is to embed the whole fiber tractography with continuous trajectories into FE models (Garimella, 2017; Hajiaghamemar and Margulies, 2021; Hajiaghamemar et al., 2020; Wu et al., 2019; Zhao et al., 2016). Despite its great potential, this approach conforms to multiple challenges associated with tractography reconstruction (Maier-Hein et al., 2017). Thus, the voxel-wise approach proposed in the current study can be regarded as an alternative to the previous tractography-based efforts, collectively reinforcing further the importance of leveraging the maximum amount of orientation information into the FE models toward an authentic prediction of tract-related deformation.

4.2 Limitations and path forward

Although this study yielded new insights on how to integrate the neuroimage-delineated fiber orientation into FE models, certain limitations should be acknowledged. First, besides the vector- and
tensor-averaged approaches evaluated in the current study, other orientation downsampling strategies exist in the literature. For example, Li et al. (2021) implemented the principal eigenvector from the voxel closest to the centroid of the element as the mean fiber direction for the given element, while Kraft and Dagro (2011) added the principal eigenvectors of all voxels encased by the element with the outcome as the fiber direction. It is expected that these two referred approaches would perform similarly to the vector- and tensor-averaged approaches. Secondly, the current study simulated the brain as an isotropic and homogeneous medium, as no complete consensus has been reached yet about the mechanical heterogeneity and anisotropy of the human brain tissue. Relevant limitations have been exhaustively discussed in our recent publications (Zhou et al., 2021a; Zhou et al., 2021b) and are not repeated here. Nevertheless, we acknowledge that extending the current study to the context of modelling the brain as an anisotropic and heterogeneous object can be another interesting aspect for future work with the effort initiated by Zhao and Ji (2019b). Thirdly, across all the three approaches investigated in the current study, the orientation information of WM fiber tracts is based on the primary eigenvector of a rank-2 symmetric tensor. It has been well recognized that the tensor model is a limited approximation of fiber architecture, especially in those regions with fiber bundles intertwined and crossed (Jeurissen et al., 2013). The current study can be extended by exploiting more advanced models (Frank, 2001; Tournier et al., 2004) that better describe the diffusion in voxels with multidirectional fiber tracts. Lastly, although the voxel-wise approach proposed in the current study addresses the resolution mismatch between DTI voxel and FE, this approach remains to confront another resolution mismatch between strain tensors of brain elements (element-wise basis) and fiber orientation reflected by the direction of embedded truss elements (voxel-wise basis). This is reflected by the fact that the strain tensor of one given WM element was related to the temporal direction of all the truss elements encased by the given WM element to compute tract-related strain. Future work is planned to address this critical aspect with one alternative solution recently published by Ji and Zhao (2022).

5. Conclusion
The present study proposed a new approach to incorporate voxel-wise fiber directions from DTI into FE models by embedding fiber orientations from multiple voxels within one element and evaluated the reliability of orientation downsampling with one fiber orientation per element. This newly proposed approach and two existing downsampling alternatives were respectively implemented into two FE models with varying levels of element sizes. Two orientation downsampling approaches were shown to cause systematical loss of fiber orientation information and further compromised the accuracy of tract-related strain, particularly for the model with a large mesh-imaging resolution mismatch. For the model with refined meshes, these downsampling-induced effects were partially compensated. Collectively, the voxel-wise orientation implementation provides a better representation of fiber orientation and is recommended to be used in the future. Therefore, this study yields insights on integrating neuroimaging-informed fiber information into FE models to improve the accuracy of FE-derived WM tract-related deformation.

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Data availability

Scripts for mapping the fiber orientation information in diffusion tensor imaging to finite element brain models can be obtained by emailing request to the corresponding author.
Author contributions

Zhou Zhou: Conception and study design, Finite element simulation, Imaging analysis, Data processing, Visualization; Writing – review & editing; Teng Wang: Conception and study design, Imaging analysis, Review & editing; Daniel Jörgens: Revision, Data analysis and illustration, Review & editing; Xiaogai Li: Conception and study design, Imaging analysis, Review & editing.

Conflict of Interest

The authors declare that they have no conflict of interest.

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Appendix

Table A1 - Summary of differences and commonalities between the KTH model and ADAPT model. Note that the mesh sizes are reported in the form of mean ± standard deviation (range).

<table>
<thead>
<tr>
<th>Geometry</th>
<th>KTH model</th>
<th>ADAPT model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Image source</td>
<td>Visible human database</td>
<td>ICBM-152 atlas</td>
</tr>
<tr>
<td>Intracranial volume (dm³)</td>
<td>1.53</td>
<td>2.12</td>
</tr>
<tr>
<td>Brain volume (dm³)</td>
<td>1.37</td>
<td>1.57</td>
</tr>
<tr>
<td>Number of brain elements</td>
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<td>1513198</td>
</tr>
<tr>
<td>Number of white matter elements</td>
<td>1197</td>
<td>113678</td>
</tr>
<tr>
<td>Size of brain elements (mm)</td>
<td>6.34 ± 1.93 (1.93~11.35)</td>
<td>0.85 ± 0.35 (0.23~3.25)</td>
</tr>
<tr>
<td>Size of white matter elements (mm)</td>
<td>6.37 ± 1.60 (1.96~9.83)</td>
<td>1.28 ± 0.55 (0.34~3.23)</td>
</tr>
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</table>
**Material**

<table>
<thead>
<tr>
<th>Material</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Brain</td>
<td>A second-order Ogden model for nonlinearity with tension-compression asymmetry in combination with six-order Prony series for viscoelasticity</td>
</tr>
<tr>
<td>Cerebrospinal fluid</td>
<td>Elastic fluid</td>
</tr>
<tr>
<td>Falx/tentorium/dura mater</td>
<td>Elastic Simplified rubber</td>
</tr>
<tr>
<td>Pia mater</td>
<td>Elastic Simplified rubber</td>
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</table>

**Element formulation**

<table>
<thead>
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<th>Material</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Brain/cerebrospinal fluid</td>
<td>Hexahedral elements with selectively reduced integration</td>
</tr>
<tr>
<td>Falx/tentorium/dura mater/pia mater</td>
<td>Quadrilaterals with fully integrated Belyschoko-Tsay membrane</td>
</tr>
</tbody>
</table>

**Interface**

<table>
<thead>
<tr>
<th>Interface</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Brain-skull interface</td>
<td>Sliding-only contact</td>
</tr>
<tr>
<td>Brain-ventricle interface</td>
<td>Continuous mesh</td>
</tr>
</tbody>
</table>

**Fiber orientation**

| Image source                  | ICBM DTI-81 atlas                                |

**Table A2 – Material properties for the embedded truss elements.**

<table>
<thead>
<tr>
<th>Element type</th>
<th>Cross-sectional area (m²)</th>
<th>Constitutive model</th>
<th>Density (kg/m³)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Truss</td>
<td>1 e-11</td>
<td>MAT_NULL</td>
<td>1 e-11</td>
<td>(Zhou et al., 2021a)</td>
</tr>
</tbody>
</table>

**Fig. A1.** Coronal cross-sections of azimuth angle (β) of fiber orientation determined by the voxel-wise approach and two downsampling approaches along with the absolute difference associated with orientation downsampling. In each contour, the gray matter region is colored in dark gray.
Fig. A2. Coronal cross-sections of MTPS (A), MASS (B), and MLSS (C) determined by the voxel-wise approach and two downsampling approaches along with the absolute difference associated with orientation downsampling. In each contour, the gray matter region is colored in dark gray.