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## 1 Title: Estimating Microbial Population Data from Optical Density

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#### 12 Abstract

- 13 The spectrophotometer has been used for decades to measure the density of bacterial populations
- 14 as the turbidity expressed as optical density OD. However, the OD alone is an unreliable metric
- 15 and is only proportionately accurate to cell titers to about an OD of 0.1. The relationship between
- 16 OD and cell titer depends on the configuration of the spectrophotometer, the length of the light
- 17 path through the culture, the size of the bacterial cells, and the cell culture density. We
- 18 demonstrate the importance of plate reader calibration to identify the exact relationship between
- 19 OD and cells/ml. We use four bacterial genera and two sizes of micro-titer plates (96-well and
- 20 384-well) and show that the cell/ml per unit OD depends heavily on the bacterial cell size and
- 21 plate size. We applied our calibration curve to real growth curve data and conclude the cells/ml –
- 22 rather than OD is a metric that can be used to directly compare results across experiments, labs,
- 23 instruments, and species.

#### Introduction 24

25 The Beer-Lambert law (1) relates the molar concentration (C) of a solute to absorbance of light

26 according to the equation  $C = \Box A$  where  $\Box$  is the molar extinction coefficient and A is the

27 absorbance. Epsilon ( $\Box$ ) is given at a specific wavelength and specific light path, usually a 1 cm

28 light path. That relationship is what allows us to monitor enzyme reactions by absorbance, to

29 measure protein concentrations by absorbance, and to do enzyme-linked immunoassays (ELISA).

30

31 The Beer-Lambert law, however, applies only to solutions in which molecules of solute are

32 uniformly distributed throughout the solvent. It does not apply to suspensions of particulate

33 matter such as microbial cells. Rather than absorbing light, particles scatter light, which is why

34 we express turbidity as OD (optical density) instead of A (absorbance). The relationship

35 between cells/ml and OD is a complex one and depends on several factors including length of

36 light path, size of the particles (cells), and number of particles. There is no simple factor

- 37 equivalent to  $\Box$  that relate number of cells/ml to OD.
- 38

39 It is not a trivial matter to determine the number of cells/ml or the mass of cells in a culture. The

40 classic way was to dry a culture and weigh the cells, a method that does not lend itself to easy

41 measurement of cell densities in small cultures, (to say nothing of the fact that while weighing

42 the dehydrated cells, they absorb moisture from the air and the weight increases even as the

43 balance is watched!). It can be important to determine cell densities easily and quickly, i.e.,

44 when monitoring growth in fermenters to determine when to harvest cells.

45

46 The convenience of measuring cell populations in microtiter plate readers led us to determine the 47 relationship between OD and cells/ml for several microbial species and for plates of different 48 sizes. Given that relationship OD can be used to calculate cell numbers just as A is used to

49 calculate concentration of a solute.

50 51 Spectrophotometers have been used for over 6 decades as a means of measuring the population 52 density of microbial cultures (2-4). Population density is estimated from the turbidity of the 53 culture and is typically expressed as OD (optical density), typically at a wavelength of 600 nm. 54 OD is the negative log of transmittance, which is the fraction of the light that is detected when it 55 is passed through a cuvette that contains a sample of the culture. The Beer-Lambert law states 56 that OD is proportional to the concentration of a solution (1). However, this law does not apply

57 to suspensions of particles (or bacterial cultures) because instead of absorbing light, light is

58 scattered off the axis of the detector (5, 6). As a result, the OD is proportional to the cell titer

59 only up to a limited point, typically an OD of about 0.1 (Figure 3). Above that range, some of

60 the light that is scattered away from the detector by one cell is subsequently scattered back to the

61 detector by another cell (7). As a result, the OD does not increase as fast as does the cell titer

62 and therefore, one cannot rely on OD alone to accurately measure bacterial population densities.

63

64 To precisely estimate cell titers from observed OD measurements, it is necessary to calibrate the

65 spectrophotometer. The relationship of OD to cell titer depends on four components: 1) the

configuration of the spectrophotometer, 2) the length of the light path through the suspension, 3) 66

67 the size of the cells, and 4) the cell culture density. Therefore, it is necessary to calibrate each

68 spectrophotometer model separately for each microbial species that is to be studied.

69

- 70 Until about a decade ago ODs were determined by putting a sample of the culture into a cuvette
- of, typically, a 1 cm light path. Determining the growth rate required sampling from a culture at
- timed intervals and recording the OD at each time point. In practical terms it was difficult to
- follow more than about 20 cultures simultaneously. The advent of using a microtiter plate reader
- to monitor the growth of cultures in the wells of a microtiter plate permits high throughput
- 75 measurements of microbial growth kinetics. However, the same considerations of calibration
- apply to microtiter plate readers as to spectrophotometers (7). Microtiter plates have various
- sizes (i.e., 96-wells, 384-wells) which means each well has different depths. Therefore, it is
- necessary to calibrate a plate reader separately for each size plate.
- 79
- 80 A recent study shows the benefit of plate reader calibrations using silica microspheres (8).
- 81 However, they focus their study on only *E. coli* and do not consider microtiter plate size, well-
- 82 depth, or other sizes of bacterial species. Here, we demonstrate the importance of calibrating a
- 83 plate reader using a Biotek Epoch 2 plate reader, both 96-well and 384-well microtiter plates and
- 84 four bacterial species that span a wide range of cell sizes. We then apply the calibration to a set
- 85 of growth curves for *Escherichia coli* and show that using cells/ml yields the same growth rates
- 86 as using OD.

# 8788 Results

- 89 <u>Calibration curves</u>
- 90 Standing overnight cultures for each organism (E. coli DH5a, S. epidermidis, B. megaterium
- 91 and P. putida) were concentrated to about 2.5 x  $10^9$  cells/ml in mineral salts (M9) buffer, 2x
- 92 serially diluted. Each dilution, plus a buffer blank, was distributed to four wells (96 well plate) or
- 6 wells (384 well plate) and the ODs were measured. For each dilution, the mean OD was
- 94 corrected by subtracting the mean OD of the blank (buffer) well, and corrected ODs were
- 95 graphed vs the number of viable cells. Stevenson et al (7) suggested that a quadratic relationship
- 96 exists between cell number and OD. However, to identify the best possible fit, we wanted to
- 97 explore other relationships. We fit curves to the resulting points based on assumption of four
- 98 relations- a linear relationship, a quadratic relationship, a cubic relationship, and a polynomial of
- degree 4 relationship. *E. coli* fits are shown as representative data (Figure 1) and the
- 100 corresponding  $R^2$  values, the correlation coefficients of the fits, for the other genera measured are 101 also shown in Table 1.
- 101
- 103 The linear fit is clearly inappropriate, with  $R^2 = 0.95$  for both 96 and 384 well plates. To choose 104 among the other fits, we considered  $R^2$  as a measure (Table 1). We found that the  $R^2$  criterion for
- 105 the polynomial of degree 4 fit is the best for *E. coli*.
- 106
- 107 We similarly calibrated the plate reader with *Staphylococcus epidermidis*, *Pseudomonas putida*,
- 108 and *Bacillus megaterium*. In each case the polynomial of degree 4 was the best fit. The
- 109 approximate cells/ml with the polynomial of degree 4 using the general equation:  $A OD^4 + B$
- 110  $OD^3 + C OD^2 + D OD + E$  where A, B, C, D and E are the coefficients of the terms. Table 2
- 111 shows the polynomial degree 4 equations for each organism and plate size. We also considered
- another criterion for goodness of fit, Root Square Mean Error (RMSE) (data not shown). The
- smaller is RMSE the better is the fit. By RMSE criterion, polynomial degree 4 was also
- 114 consistently the best fit.
- 115

- 116 The equations are different for each species, and within a species for 96 and 384 well plates
- 117 (Table 2). This emphasizes the need to calibrate each species and plate size separately. We
- 118 provide these equations solely as examples, and we emphasize that they should not be used for
- 119 instruments other than the Biotek Epoch 2.
- 120

121 The Cells/ml @ OD = 1 decreases as CV (cell volume) increases according to a quadratic

- 122 function in which Cells/ml @ OD = 1 is 2.1 e8 x  $CV^2$  5.9 e9 x CV +4.0 e10, with  $R^2$  = 0.998
- 123 for 96-well plates and 1.2 e8 x  $CV^2$  3.4 e9 x CV +2.3 e10, with  $R^2 = 0.999$  for 384-well plates.
- 124 This is consistent with Koch's 1961 and Stevenson et al's 2016 finding (2, 7).
- 125
- 126 Application of calibration curve to real growth curve data
- 127 The growth of two *E. coli* strains and one *S. epidermidis* strain at 37° in LBD medium was
- 128 monitored. Population density was measured as corrected OD and cells/ml based on a quadratic-
- 129 fit calibration curve. Figure 2 shows a plot of one well for *S. epidermidis* strain and highlights
- 130 that the curves based on OD and cells/ml are almost identical. For the *S. epidermidis* culture in
- 131 Figure 2, the growth rate based on OD was  $\mu = 0.01459 \pm 0.000412 \text{ min}^{-1}$  based on 6 points from
- 132 140 through 240 minutes, with R = 0.9984. Based on cells/ml, the growth rate was similar,
- 133  $\mu = 0.01354 \pm 0.000285 \text{ min}^{-1}$  based on 6 points from 140 through 240 minutes, with R= 0.9983.
- 134

135 Figure 3 shows a growth curve of *E. coli* based on OD and the same curve based on scaled

- 136 cells/ml. Above an OD of 0.1 the OD (open circles) is significantly below the scaled cells/ml,
- 137 illustrating that the proportionality of cells/ml to OD falls off above OD = 0.1.
- 138

139 The program GrowthRates (9) version 5.1 (<u>https://bellinghamresearch.com/</u>) was used to

- 140 estimate the growth rates in 12 wells for *E. coli*K12 strain DH5, the uropathogenic *E. coli* strain
- 141 CFT073 (10), and *S. epidermidis* strain. ATCC 12228 (11). We found the growth rate estimates
- similar when comparing corrected OD to cell/ml using the polynomial degree 4 fit. The growth
- 143 rate estimated from cells/ml was significantly different from the growth rate based on OD for *E*.
- 144 *coli* CFT073 and *S. epidermidis* (Table 3).
- 145

146 The growth rates estimated from OD and from cells/ml are not the same. Which estimates

- 147 should we trust more? We trust the rates based on cells/ml because at ODs above 0.1 the OD
- 148 readings fall off as the true population density (cells/ml) increases.
- 149

# 150 **Discussion**

- 151
- 152 Our work highlights the importance of calibrating a microplate reader. We use four different
- bacterial genera to explore the relationships between corrected OD and cells/ml. First, we
- 154 compared a quadratic, cubic and polynomial degree 4 fit to bacterial growth data and show that
- 155 for all four genera, the best calibration fit is a polynomial of degree 4 (Table 1). To highlight the
- importance of calibrating the plate reader separately for 96-well and 384-well plates, we show
- 157 the differences in the polynomial degree 4 equations. This difference likely arises from the
- different culture depths, hence different light path lengths, in 96- vs 384- well plates (Table 2).
- 159 We also emphasize the importance of separate calibrations for each genus (Table 2). The
- 160 calibration coefficients depend upon the cell volume, with the sum of those coefficient
- 161 decreasing as a cubic function as the microbial cell volume increases. Good calibration and

162 application of the calibration curve clearly depends upon consistent well volumes, not only

- 163 within a single experiment, but between experiments.
- 164

165 Growth rates estimated from OD and cells/ml are not identical (Table 3), but we trust the rates 166 estimated from cells/ml more than those estimated from OD.

167

168 Why is it worth the effort to calibrate a plate reader? First, because it allows us to express the

169 maximum population density, i.e., the carrying capacity of the medium, in terms of cells/ml

- 170 rather than OD. Consider the maximum OD for *E. coli* CFT073 and *S. epidermidis* in 96 well
- 171 plates (Table 3). These values are very similar (0.622 and 0.610 respectively), but for *E. coli*, the
- 172 OD of 0.622 represents only 8.2 x  $10^8$  cells/ml. On the other hand, the OD of 0.610 for *S*. 173 *epidermidis* represents 1.25 x  $10^{10}$  cells/ml. This is a fifteen-fold difference in the number of
- 174 cells per milliliter in each overnight culture. This difference is important to consider when
- performing experiments that depend on the number of cellular divisions or cells present, such as
- 176 cellular communication (12, 13) and antibiotic susceptibility (14-17) and biofilms (18).
- 177

178 Knowing the relationship between OD and cells/ml is not just valuable during growth rate

determinations. For instance, when monitoring the growth yield in a fermenter it is very

180 valuable to know the actual population density to decide when to harvest the cells. For S.

- epidermidis if the yield according to OD is OD = 2.5 that is five times the yield when OD = 0.5.
- 182 The cells/ml at OD = 2.5 is  $1.2 \times 10^{12}$ , which is 125 times the yield when OD = 0.5 (9.5 x  $10^9$  cells/ml).
- 183 184

185 Probably the most important reason to calibrate plate readers is to use a consistent metric for

186 expressing population densities. By expressing population densities in cells/ml, rather than OD,

- 187 experiments can be directly compared from different instruments, different labs, and even
- 188 different genera. Our work shows that using cells/ml as a metric permits reliable measurements
- 189 of growth rates as does using OD (Table 3) because cell/ml allows consistency when expressing

190 population densities. To measure bacterial growth rates more precisely, we encourage all to

- 191 calibrate their instruments and to express their results in cells/ml.
- 192

# 193 Methods

# 194 Bacterial Strains

195 We used four bacterial strains of different genera: *Escherichia coli* K12 strain DH5 [] (F-

196  $\varphi$ 80lacZ $\Delta$  M15  $\Delta$  (*lacZYA-argF*) U169 recA1 endA1 hsdR17 (rK-mK+) phoA supE44  $\lambda$ - thi-1

- 197 gyrA96 relA1) from ThermoFisher, Escherichia coli strain CFT073 O6:K2:H1 (10),
- 198 Pseudomonas putida strain ATCC 12633, Staphylococcus epidermidis strain ATC12228 (11)
- and Bacillus megaterium strain ATCC 14581.
- 200

# 201 Plate Reader Calibration

202 To identify the colony forming units per genus, we inoculated four standing overnight cultures

for each genus. Cultures were inoculated at 37°C in 10mL of LB (10 g tryptone, 5 g yeast extract,

- 204 10 g NaCl per liter) and placed in 15mL culture tubes with tightly sealed caps that allowed no
- aeration for 16-18 hours. Cultures of each genus were combined into a 50-mL conical tube and
- spun down at 4,000 rpm for 15 minutes at 4 °C then resuspended in 4mL M9 buffer, this led to a
- 207 4X concentrated starting bacterial culture. Two sets of fifteen dilutions were made. The first,

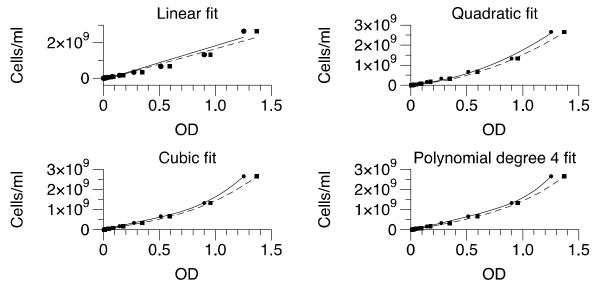
- starting cultures were diluted at concentrations that gave the most countable number of colonies.
- 209 These were  $10^6$ ,  $10^7$ ,  $10^8$  for *E. coli*, and  $10^4$  and  $10^5$  for *S. epidermidis*, *P. putida*, and *B*.
- 210 megaterium. Dilutions were plated on LB agar, inoculated at 37 °C overnight and counted the
- 211 following day. The second set of dilutions were 15 two-fold dilutions from the starting culture.
- Each tube was plated in 96-well plates (4 replicates 200 µl per well) and 384-well (6 replicates,
- 213 80µl per well) plus blank wells (only M9) for each plate size. The OD<sub>600</sub> was measured every 5
- 214 minutes for 30 minutes using the Biotech Epoch 2 plate reader. We report the corrected OD, that
- 215 is the OD of only media subtracted from each experimental reading. Aggregated data was used in
- 216 combination with the colony counts to obtain the individual calibration for each genus.
- 217
- 218 Please see supplementary materials file "Plate Reader Calibration Protocol.pdf" for detailed step-
- 219 by-step protocol, and the file "Calibration calculator.xlsx" which facilitates using that protocol.
- 220

## 221 Growth Rate Experiments

- 222 Standing overnight cultures of *E. coli* and *S. epidermidis* were diluted (1:20) to obtain a starting
- 223 OD of 0.02 0.03. Cultures were then plated across the row of a 96-well plate (12 replicate wells)
- and the  $OD_{600}$  was measured every 20 minutes for 22 hours. The growth rates were calculated
- from the OD measurements using the program GrowthRates (9) version 5.1
- 226 (https://bellinghamresearch.com/).
- 227
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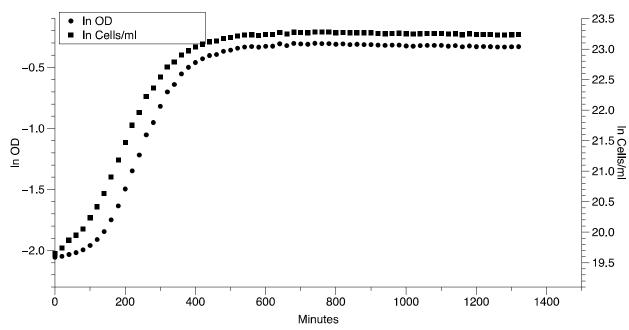
#### 232 Figures:



233 234

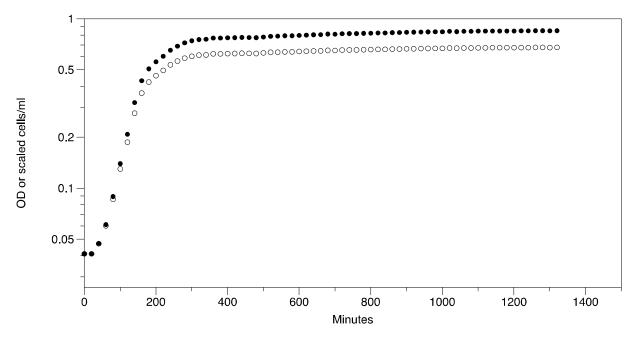
Figure 1: Relationship between cells/ml and OD with different fits. The solid lines and round points represent 96-well measurements, and the dashed lines and square points represent 384well measurements for *E. coli*.

238 239



240

Figure 2. Growth curves of *S. epidermidis* in one well based on different measures of population
density. The natural log of OD (circles) and cells per mL (squares) is plotted over time (minutes).
243
244



245 246

Figure 3. Growth curves based on OD (open circles) and based on scaled cells/ml (closed
circles). Cells/ml have been scaled to fit on the same scale as OD by dividing cells/ml by 1.07 x
10<sup>9</sup>.

#### **Tables:**

#### 

252 Table 1:  $R^2$  values for the different fits for each of the four bacterial genera measured.

Organism		96 well		384 well			
Organism	Quadratic	Cubic	Polynomial	Quadratic	Cubic	Polynomial	
S. epidermidis	0.9987	0.99995	1.0	0.99989	0.99995	0.99999	
E. coli	0.99452	0.99961	1.0	0.99815	0.99995	1.0	
P. putida	0.99824	0.99996	0.99996	0.99821	0.99987	0.99992	
B. megaterium	0.99977	099999	1.0	0.99882	0.99936	0.99997	

253 Organisms are listed in order of cell volume.

#### 257 Table 2: Calibration equations and cell size

Species	Plate	Polynomial Degree 4 Equation, Cells/ml =	Cells/ml	Cell Vol
	Size		@ <b>OD</b> = 1	
<i>S</i> .	96	$4.3e10 \text{ OD}^4$ - $3.8e10 \text{ OD}^3$ + $1.2e10 \text{ OD}^2$ + $1.7e10 \text{ OD}$ + $1.7e8$	$3.42 \times 10^{10}$	$1 \mu^3$
epidermidis				
•	384	$-2.5e10 \text{ OD}^{4} + 4.2e10 \text{ OD}^{3} - 1.2e10 \text{ OD}^{2} + 1.5e10 \text{ OD} + 9.4e7$	$2.01 \times 10^{10}$	
E. coli	96	$1.6e9 \text{ OD}^4$ -2.3e9 $\text{OD}^3$ +1.3e9 $\text{OD}^2$ +1.0e9 $\text{OD}$ +5.1e5	$1.6 \times 10^9$	9.8 $\mu^{3}$
	384	$3.3e8 \text{ OD}^4$ - 2.1e8 $\text{OD}^3$ + 4.9e8 $\text{OD}^2$ + 8.3e8 $\text{OD}$ + 4.2e4	$1.44 \times 10^9$	
P. putida	96	$2.4e8 \text{ OD}^4$ - 2.7e8 $\text{OD}^3$ + 6.4e7 $\text{OD}^2$ + 4.7e8 $\text{OD}$ + 1.4e5	$5.04 \times 10^8$	$12.3 \mu^3$
	384	$3.7e8 \text{ OD}^4$ -6.8e8 $\text{OD}^3$ +3.8e8 $\text{OD}^2$ +3.7e8 $\text{OD}$ +8.2e5	$4.41 \times 10^8$	
<i>B</i> .	96	$4.4e8 \text{ OD}^4$ - $4.9e8 \text{ OD}^3$ + $3.2e8 \text{ OD}^2$ + $5.9e8 \text{ OD}$ + $4.3e6$	$8.64 \times 10^8$	$17 \mu^3$
megaterium				-
	384	$-1.2e9 \text{ OD}^{4} + 3.6e9 \text{ OD}^{3} - 2.7e9 \text{ OD}^{2} + 1.2e9 \text{ OD} - 5.3e6$	8.95x10 <sup>8</sup>	

261 Table 3: Comparison of growth rates based on OD and cells/ml.

201 140	ne 5. comp	unison of S	lowin futos bu			1111.			
E. coli K12 DH5α			E. coli CFT073			S. epidermidis ATCC 12228			
	μ	R	max OD or cells/ml	μ	R	max OD or cells/ml	μ	R	max OD or cells/ml
OD	0.0212	0.9968	0.348	0.0235	0.9989	0.622	0.0155	0.9989	0.610
cells/ml	0.0207	0.9984	$4.36 \ge 10^8$	0.0253	0.9990	8.21 x 10 <sup>8</sup>	0.0139	0.9986	1.25 x 10 <sup>10</sup>
p-value	0.55			0.0024			9.19e-6		

Values are means of 12 replicates. In all cases the S.E. was < 0.05 of the mean.

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