Synchronization in the connectome: Metastable oscillatory modes emerge from interactions in the brain spacetime network

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Abstract

A rich repertoire of oscillatory signals is detected from human brains with electro- and

magnetoencephalography (EEG/MEG). However, the principles underwriting coherent oscillations

and their link with neural activity remain under debate. Here, we revisit the mechanistic hypothesis

that transient brain rhythms are a signature of metastable synchronization, occurring at reduced

collective frequencies due to delays between brain areas. We consider a system of damped

oscillators – approximating the short-lived gamma-frequency oscillations generated within neuronal

circuits – coupled according to the diffusion weighted tractography between brain areas. Varying

only the global coupling strength and conduction speed, we identify a critical regime where spatially

and spectrally resolved metastable oscillatory modes (MOMs) emerge at sub-gamma frequencies,

approximating the MEG power spectra from 89 healthy individuals at rest. Further, we demonstrate

that the frequency, duration, and scale of MOMs – as well as the frequency-specific envelope

functional connectivity – can be controlled by global model parameters, while the connectome

structure remains unchanged. Grounded in the physics of delay-coupled oscillators, these numerical

analyses demonstrate how interactions between locally generated fast oscillations in the

connectome spacetime structure can lead to the emergence of collective brain rhythms organized in

space and time.

Introduction

The human brain is one of the most complex networks in nature, exhibiting a rich repertoire of

activity patterns organized not only in space and time but also in the frequency domain. Indeed,

rhythmicity is a central property of brain function – and perhaps of all biotic self-organisation: from

fast gamma activity in neurons to the life-cycle itself[1-4]. Within the broad range of oscillations

emerging at frequencies between 0.05 Hz and 500 Hz, the oscillations detected extracranially with

electro- and magnetoencephalography (EEG/MEG) in resting humans typically peak between 0.5 and

30 Hz, being categorized as delta (~0.5-4 Hz), theta (~4-8 Hz), alpha (~8-13 Hz) and beta (~13-30 Hz)[5].

Notably, these oscillations lock in phase over long distances, generating metastable spatial

topographies lasting up to a few hundred milliseconds[6-8].

Falling significantly below the range of frequencies generated in local neuronal networks by

feedback inhibition (>35Hz, in the gamma frequency range), it is generally agreed that sub-gamma

oscillatory activity does not have a purely local origin and is associated with synchronization

between distant neural assemblies[9-14]. Notably, there is a relation between the distance over which

synchronization is observed and the frequency of the synchronized oscillations[15-17]. Specific brain

circuitries, including among others the thalamocortical loop, have been proposed to play a role in

the generation of rhythmic activity[18-20], which appears disrupted in neurological/neuropsychiatric

disorders [1,21]. Still, the fundamental mechanisms driving the spontaneous emergence of short-lived

spatially and spectrally resolved oscillatory patterns remain unclear[9,22-24].

Given the spatial distance and the finite propagation speed, interactions between brain

areas are intrinsically time-delayed, which can manifest in network activity in the frequency domain.

Indeed, delay-coupled limit-cycle oscillators have been demonstrated to synchronize at frequencies

slower than the natural frequency of the oscillators, leading to a form of *collective* frequency

emerging from synchronization mechanisms[25,26]. Briefly, when *N* phase oscillators – with natural

frequency ω – are coupled together with a time delay τ, they synchronize at a delay- and interaction-

dependent collective frequency Ω given by $\Omega = \omega /(1+K*N*\tau)$, where *K* is the global coupling

strength[25]. However, this phenomenon has so far only been demonstrated for networks of limit-

cycle oscillators[25], and it is unclear how it generalizes to systems where oscillations are not self-

sustained, but instead emerge only transiently.

Computational models have proved helpful for demonstrating how the brain's complex

network structure of long axonal projections connecting brain areas – the so-called structural

connectome[27] - can *shape* brain activity in space and time[28-36]. Particularly, simulations of oscillatory

units interacting in the connectome reveal a critical regime where different subsets of units

temporarily synchronize and desynchronize, leading to transiently correlated activity across spatially

segregated units[30,37-39]. This reinforces the hypothesis that long-range functional connectivity

between brain areas is driven by synchronization mechanisms[24,40-44]. Importantly, when considering

realistic time delays in the Kuramoto model of coupled phase oscillators, periods of increased

synchrony are accompanied by increased power at slower frequencies, generating spatially-

organized band-limited power fluctuations similar to the ones captured with MEG[38]. While these

numerical results revealed the critical role of time delays to generate collective oscillations at

reduced frequencies, it remains to be verified whether this phenomenon holds in the more realistic

setting, wherein local oscillations have fluctuating amplitude – which is neglected in the Kuramoto

model –, as observed empirically in electrophysiological recordings of neural activity[45,46].

Furthermore, understanding the parameters that control the duration, size and occupancy of

collective oscillations is crucial to inform the prediction of therapeutic strategies aimed at

modulating dysfunctional oscillatory brain activity.

To address these fundamental questions, we build a phenomenological brain network model

with realistic connectivity and time delays, where each node is described by a Stuart-Landau

oscillator operating in the subcritical regime, i.e., responding to a stimulus with an oscillation with

decaying amplitude [34,35,47]. As the amplitude dynamics introduces an additional degree of

complexity, it needs to be verified if the analytic predictions made for coupled limit-cycle

oscillators[48] (valid for phase oscillators or supercritical Stuart-Landau oscillators) still hold[49]. Selecting

40Hz as a typical frequency of gamma oscillations, we set all units with identical natural frequency to

exclude additional effects of frequency dispersion[50,51], and perturb all units with uncorrelated white

noise, considering that units resonate at their natural frequency in the presence of background noisy

activity[52]. Assuming the generalizability of collective synchronization frequencies to delay-coupled

damped oscillators, we hypothesize to identify a critical range of global model parameters (global

coupling and conduction speed) where metastable synchronization generates the transient

emergence of sub-gamma collective oscillations, approximating features of human MEG recordings.

Results

Dynamical regimes of the brain network model

The reduced brain network model comprises *N*=90 dynamical units representing anatomically

defined brain areas coupled according to a normative structural connectome of the human brain

(see *Methods – Structural Connectome*) with reciprocal (i.e., bidirectional/symmetric) coupling C_{NxN}

and distance D_{NxN} matrices (Figure 1a). Each unit is described by a Stuart-Landau oscillator operating

in the underdamped regime, such that when perturbed it decays to a fixed-point equilibrium with a

damped oscillation at a natural frequency ω (Figure 1b, see *Methods* and *Supplementary Methods*,

Section I).

***Figure 1 – Collective oscillations emerge at reduced frequencies from synchronization in the presence of delays. a** – The*

phenomenological brain network model consists in N=90 nodes representing brain regions with links representing diffusion

*tracts between them. **b** – A Stuart-Landau oscillator in the subcritical regime responding to perturbation (vertical arrow)*

with an oscillation with decaying amplitude (left), in contrast with the super critical regime where the amplitude remains

*constant (right). **c** – Simulated collective signal and corresponding power spectrum obtained for three levels of global*

coupling, with a mean conduction delay of 5 milliseconds and in the presence of white noise. For weak coupling (left) the

simulated signal exhibits oscillations peaking close to the node's natural frequency. For intermediate coupling (middle),

To verify that novel frequencies emerge purely from delayed interactions, the natural

frequency of all units is set at ω = 40Hz (representing the resonant frequency of isolated neural

masses driven by feedback inhibition) and each unit is perturbed with uncorrelated white noise. The

model – represented mathematically by a system of delay coupled differential equations – is solved

numerically for two parameter ranges: the global coupling strength, *K*, which scales all pairwise

connections, and the mean conduction delay, $\langle \tau \rangle$, which scales the time delays between units in

proportion to the diffusion tract lengths (Figure 1, see Methods for details).

The synchrony degree of the system, evaluated using the Kuramoto Order Parameter (KOP),

is modulated by the global coupling strength *K*: for weak coupling all units exhibit oscillations close

to the natural frequency ω and for sufficiently strong coupling all units tend to synchronize at a

global collective frequency Ω, which, in the presence of time-delays, is distinct from the natural

frequency ω (Figure 1c-d). In the critical range between incoherence and full synchrony, periods of

weakly stable synchronization drive slow fluctuations in the KOP (Figure 1c-d, middle).

Observing the levels of synchrony and metastability across the range of parameters explored

(Figure 1e), we find that the critical value of K above which the system can synchronize increases

logarithmically with the mean delay, in line with analytic predictions for coupled oscillators with

heterogeneous delays[54] (see Supplementary Methods, Section II, Figure S5). When synchronization

occurs in the presence of delays, we observe a sharp decrease in the global peak frequency, closely

approximating the analytic prediction given by $\Omega = \omega / (1 + K^* N^* \langle \tau \rangle)$ (Figure 1e) (see Supplementary

Methods, Section II, Figure S6). These findings serve to verify that the phenomenon of

synchronization at reduced collective frequencies is not restricted to coupled phase oscillators and

generalizes to units in the subcritical regime as long as damped oscillations emerge in response to

external noisy perturbation (see Supplementary Methods, Section II, Figure S7). Further, it

demonstrates that the peak frequency of synchronization can be predicted analytically from global

variables such as the mean natural frequency ω, the number of units N, the coupling strength K, and

the mean delay $\langle \tau \rangle$. The robustness of this prediction to distributed natural frequencies is reported

in *Supplementary Figure S8*.

Simulations reveal spectral features of human brain activity

126   One characteristic feature of MEG (and EEG) signals from healthy humans at rest is the

127   transient emergence of oscillations in the alpha frequency range (~8-13Hz), resulting in a peak in the

128   power spectrum whose prominence varies strongly across people (see Figure 2a for the normalized

129   power spectrum of MEG signals from 89 healthy young adults resting with eyes open from the

130   Human connectome Project open-source database; details in *Methods* section).

131   We find that the brain network model approximates the average MEG power spectrum of

awake resting subjects within the critical region of high metastability where synchronization occurs

at reduced collective frequencies (comparing Figure 2c with Figure 1e). In detail, for each pair of

model parameters we calculate the squared Euclidean distance between the power spectrum of the

simulated signals (Figure 2b) and the MEG power spectrum averaged across all sensors and all

subjects (Figure 2a), revealing the greatest disparity when no delays are considered or if the global

coupling is too weak (see Methods for details).

Given the observed (and well-established) variability between MEG power spectra across

individuals (Figure 2a), we investigate the extent to which this variability can be associated with

changes in global model parameters, while keeping the structural connectivity unchanged. To do so,

we identify the pair of model parameters that approximates the individual MEG power spectra of

each of the 89 participants, falling in 29 pairs of parameters (white asterisks in Figure 2b). Notably,

this reveals a confined region in parameter space for a range of average delays $\langle \tau \rangle$ of 2 to 11

milliseconds, with slight changes in the coupling strength and conduction speed maximizing the fit to

individual MEG power spectra, while the structural connectivity remains unchanged. These results

do not exclude the role of individual variability in structural connectivity across subjects but reveal

additional parameters that modulate a network's frequency spectrum. This serves to demonstrate

that the same connectome structure can support distinct activity patterns depending on global

model parameters, with longer/shorter time delays and stronger/weaker coupling inducing shifts in

the peak frequency and modulating the distribution of power across the spectrum (Figure 2b).

Metastable Oscillatory Modes emerge from weakly stable cluster synchronization

In the range of parameters where the model optimally approximates the power spectrum of

MEG signals, fluctuations in the magnitude of the order parameter are driven by metastable cluster

synchronization. In other words, when the coupling is strong, but not sufficiently strong to stabilize

full synchronization, some subsets of units that are more strongly connected together (i.e.,

clusters/communities) can engage in partially-synchronized modes that remain stable for a short

period in time. Given the presence of time delays, these clusters do not synchronize at the natural

frequency of the individual units (ω=40Hz), but instead synchronize at slower cluster-specific

collective frequencies, leading to the emergence of metastable oscillatory modes (MOMs) at sub-

gamma frequencies.

To detect the occurrence of MOMs and characterize them in space and time, we band-pass

filter the simulated signals in 4 frequency bands (delta 0.5-4Hz, theta 4-8Hz, alpha 8-13Hz and beta

13-30Hz). In Figure 3, a coloured shade is added when the amplitude in each frequency band

exceeds 5 standard deviations of the amplitude in that same frequency range detected in

simulations without delays (see Supplementary Methods, Section IV, Figure S11).

a - Simulated signals in 90 coupled units filtered below 30 Hz ($\omega_0 = 40$ Hz, **K = 10**, $\langle\tau\rangle = 3$ms)

Amplitude 5*STD > baseline
0.5-4 Hz   4-8 Hz   8-13 Hz   13-30 Hz

b - Power < 30Hz vs Phase synchrony (r = 0.7595)

Mean Amplitude Envelope   Kuramoto Order Parameter

Time (seconds)

*Figure 3. Sub-gamma oscillations emerge from weakly stable cluster synchronization. **a** – An example of the simulated*

signals in all 90 units plotted over 25 seconds, each representing a brain area from the AAL brain parcellation template,

filtered below 30 Hz to highlight the sub-gamma oscillatory activity typically detected with MEG. Shades indicate the time

points of increased power in the delta (yellow), theta (red), alpha (blue) and beta (green) frequency bands. For each

frequency band, the threshold was defined as 5 standard deviations (STD) of the amplitude – in the same frequency bands –

*when no delays were considered. **b** –The mean amplitude envelope (blue) of the filtered signals shown in panel A correlates*

with r=0.7595 with the phase synchronization evaluated by the Kuramoto Order Parameter (orange, right y-axis).

As shown in Figure 3, we find that MOMs are structured both in space and in time.

Specifically, the units synchronizing together exhibit the simultaneous emergence of an oscillation at

the same collective frequency, leading to the vertical alignment of shaded areas, particularly visible

for the alpha frequency range in Figure 3a. Notably, for different sets of parameters, the

configuration of Figure 3a changes strongly. Indeed, while for very weak coupling, almost no supra-

threshold oscillations are detected (Supplementary Methods, Section IV, Figure S12), for stronger

coupling globally synchronized supra-threshold oscillations emerge transiently in the delta band

(Figure 4). For longer delays, oscillations are detected with a less definitive temporal alignment

between brain areas (Supplementary Methods, section IV, Figure S13).

Figure 4 - Global delta waves emerge for strong coupling. *a* – *The simulated signals in all 90 units plotted over 25 seconds,*

each representing a brain area from the AAL brain parcellation template, filtered below 30 Hz to focus on the sub-gamma

oscillatory activity typically detected with MEG. Shades highlight the time points of increased power in the delta (yellow),

theta (red), alpha (blue) and beta (green) frequency bands. For each frequency band, the threshold was defined as 5

standard deviations (STD) from the amplitude in the same frequency bands when no delays were considered. *b* –*The mean*

amplitude envelope (blue) of the filtered signals shown in panel A correlates with r=0.8247 with the phase synchronization

evaluated by the Kuramoto Order parameter (orange, right y-axis).

Furthermore, the power at sub-gamma frequencies is found to correlate strongly with the

instantaneous phase synchronization evaluated by the KOP over time (r=0.7595 and r=0.8247 for

Figure 3b and Figure 4b correspondingly). This demonstrates that the emergence of oscillations at

sub-gamma frequencies in the simulations is modulated by fluctuations in the synchrony degree.

We further define quantitative metrics to characterize the MOMs emerging at different frequency

bands for different sets of model parameters in terms of their duration (i.e., consecutive time that

the power remains above threshold), their size (i.e., the number of units simultaneous displaying

power above threshold) and occupancy (i.e., the proportion of time that the power is detected

above threshold). As can be seen in Figure 5, in the range of parameters where optimal fits to MEG

data are obtained (central panel), the alpha MOMs last longer, recruit more units and occur more

often. Importantly, we demonstrate that global parameters, such as the coupling strength and the

conduction speed, modulate the spatiotemporospectral properties of the whole system in a non-

trivial way, while the dynamics at the local level and the underlying structural network remain

unchanged.

Figure 5. Characterization of metastable oscillatory modes (MOMs) emerging from the system for different sets of

parameters. *MOMs are characterized in terms of duration (i.e., consecutive time that the power remains above threshold),*

size (i.e., the number of units simultaneous displaying power above threshold) and occupancy (i.e., the proportion of time

that the power is detected above threshold over the entire simulation), for each frequency band. This demonstrates that the

same network structure, i.e., the connectome, can exhibit different oscillatory modes organized in space and in time,

depending on global parameters of the system, namely the Global Coupling strength and the Conduction Delays (which are

inversely proportional to the conduction speed). In the critical range of parameters (central plot), oscillations in the alpha

frequency band emerge more frequently and involve more units. Notably, globally synchronized delta oscillations – as

typically observed in states of reduced consciousness – are associated to an increase in the global coupling strength. Error

bars represent 1 standard deviation. See also Video V1.

The implicit sensitivity to global model parameters is illustrated in Video V1, where the

emergence of supra-threshold oscillations in different frequency bands is represented over time in

the brain for five distinct sets of parameters.

Video V1 (Still image) - Metastable Oscillatory Modes (MOMs) emerge from interactions in the Connectome spacetime

structure only for sufficient coupling and conduction times. *While the structural connectome is the same for all*

simulations, MOMs can emerge with different size, duration and occupancy depending on global parameters modulating

the collective dynamics of the system. Each brain area is represented as a sphere located at its centre of gravity. Spheres

are coloured every time the amplitude of the simulated at a given frequency band (colour-coded) exceeds 5 standard

deviations from the baseline power.

223   To link with studies of functional connectivity in MEG, we further investigate how the model

224 parameters modulate the correlation between the amplitude envelopes across frequency bands. To

225 do so, we band-pass filter the signals in each frequency band, extract the amplitude of the Hilbert

226 transform and report the envelope correlation matrices in Figure 6 for each frequency band and for

227 four representative sets of model parameters. For weak coupling, the envelope correlations are

228 close to zero (Pearson's correlation coefficient cc<0.1 for all pairs of brain areas), indicating that the

229 coupling is insufficient to drive meaningful functional connections between brain areas. For global

230 parameters in the optimal range (here K=10 and $\langle\tau\rangle$=3ms), different brain areas exhibit correlated

231 envelopes, with stronger correlations (up to cc=0.78) being detected in the alpha frequency range. In

232 contrast, for strong coupling the functional connectivity in the alpha is reduced down to a maximum

233 pairwise correlation of cc=0.25, while in turn the envelopes of delta and theta oscillations are

234 strongly correlated across the brain (up to cc=0.89). Keeping the optimal range of global coupling,

235 K=10, but increasing the delays to an average of $\langle\tau\rangle$=20ms, envelope functional connectivity is

236 detected mostly in the delta frequency range. This illustrates how, given the same underlying

237 spacetime network structure (i.e., the matrices of coupling weights C and distances D), changes in

238 global parameters strongly affect the envelope functional connectivity patterns at different

239 frequency bands.

Figure 6. Influence of global model parameters in frequency-specific envelope functional connectivity patterns. For

different sets of model parameters, we report the frequency-specific envelope correlation matrices (colormap limits are

scaled by the maximum absolute correlation and centred at zero). Next to each matrix, each of the N=90 brain areas is

represented as a sphere placed in its centre of gravity and coloured according to the maximum envelope correlation to any

other brain area.

To illustrate the level of functional connectivity across the brain, next to each correlation

matrix in Figure 6, we represent each area as a sphere placed at its centre of gravity and coloured

according to the strongest correlation with any other brain area. This shows that, for the optimal

range of parameters, the areas exhibiting the strongest functional connectivity in the alpha band are

distributed mostly in posterior and dorsal cortical areas, aligning with empirical observations of

stronger functional connectivity in the alpha band in the visual and somatomotor systems. However,

it is important to consider that the specific spatial configuration of functional connections is

inherently dependent on the resolution and topology of the structural connectome, which is known

to depend on the parcellation scheme and on the brain parts (i.e., cortical, subcortical) considered.

In Supplementary section V, we report the same results using a structural connectome including 200

cortical-only brain areas[55]. These results suggest that the phenomenology of MOMs is robust to

changes in the parcellation scheme (Supplementary Figures S16 and S17). Most importantly, this

analysis illustrates how frequency-specific functional connectivity patterns depend sensitively on

global variables modulating the distributed dynamics, while the structural connectivity remains

unchanged.

Discussion

This work addresses the physical mechanisms underlying brain rhythms detected

empirically employing a reductionist perspective to ground the inner complexity of

encephalographic signals to universal theoretical principles[56,57]. Approaching the problem from a

macroscopic perspective, we focus on the emergent properties of interacting dynamical units, where

the collective ensemble engages in functionally relevant activity patterns that cannot be inferred

from the isolated units alone[58-61].

Specifically, we first demonstrate the generalizability of a synchronization mechanism

described for networks of delay-coupled *limit-cycle* oscillators to networks of delay-coupled *damped*

oscillators (i.e., in the subcritical range of a Hopf bifurcation). This is important for the neuroscience

field, since empirical electrophysiological recordings show that local field oscillations in the gamma

frequency band are *not* limit-cycle oscillations (as considered in previous models using the Kuramoto

of coupled oscillators[20]), but instead emerge only transiently. Therefore, the substantial reduction of

brain areas to phase oscillators in Cabral et al. (2014) has raised concerns on the generalizability of

the proposed mechanism to more realistic settings, given the demonstrated importance of

considering the amplitude dynamics on the connectivity between phases [48,49,62,63].

Subsequently, we extend on previous brain network modelling works by demonstrating that

the synchronization frequency can be approximated analytically from global model parameters,

namely the number of units, the mean coupling strength, the average time delay between units, and

the mean natural frequency of the units. Regarding the latter, we show that the collective

synchronization frequency is insensitive to the spread of frequencies across units, in line with

theoretical predictions[25] (Supplementary Figure S8).

These insights are crucial to explain the macroscopic spatiotemporally organized oscillatory

signals detected with EEG/MEG at sub-gamma frequencies, without explicitly introducing these

oscillations in the model[64]. Here, we consider that only gamma-frequency oscillations can be

generated at the local neuronal level, with power at other frequencies resulting purely from

synchronization with time delays. Furthermore, we demonstrate the impact of global model

parameters in the modulation of frequency-specific collective oscillations emerging across space and

time. The detailed characterization of metastable oscillatory modes in terms of number of units

synchronizing together, duration and occupancy provides a new framework to analyse collective

brain oscillations complementary to frequency-specific envelope functional connectivity analysis.

Our hypothesis is endorsed using a phenomenological brain network model, reduced to its

key essential ingredients to allow efficient numerical approximations to analytic predictions, but at

the same time sufficiently complex to allow a fair approximation of MEG spectral features. The

deliberate reductionist perspective inherent in this brain network model is intended to link with

theoretical works on delay-coupled oscillatory systems[25,54,65,66]. Towards this end, we consider only

N=90 identical units with same natural frequency, same damping coefficient (scaled by the distance

to the Hopf bifurcation) and same noise level, coupled in the structural connectome. Therefore, we

focus solely on the effects of global variables, namely the global coupling K and the mean conduction

delay $\langle\tau\rangle$ in the emerging synchronization phenomena. To establish the construct validity of our

numerical simulations, we show that the peak synchronization frequency can be approximated by

the analytic prediction derived for synthetic networks of coupled Kuramoto oscillators with time

delays [25]. Further, in line with theoretical predictions[54,67], we find that the complex spacetime

topology of the structural connectome widely expands the critical border between incoherence and

global synchrony where fluctuations in the order parameter are indicative of metastability[25]. Despite

its simplicity, this model provides a robust framework to test a theoretically grounded mechanistic

scenario for the spontaneous formation of frequency-specific long-range coherence in complex

networks.

While the investigation of mechanistic principles and control parameters benefits from

reduced complexity, adding heterogeneity is certainly needed to improve the fitting to real brain

activity from individuals in different conditions. Building up on these fundamental aspects, additional

degrees of complexity can be added to the model, namely by considering more fine-grained

connectome structures, considering non-homogeneous intrinsic frequencies and damping

properties, or even replacing the noisy input by dynamic concentration patterns to mimic local

neuromodulatory effects. Further, given the potential generalizability of this synchronization

mechanism, we expect our analysis may provide valuable insight to interpret some of the complex

self-organizing phenomena emerging in more realistic biophysical models of neural networks[68,69] for

which a precise analytic prediction cannot be solved.

Our findings reinforce the idea that conduction delays – often neglected in network models

of whole brain activity due to the added complexity – play a crucial role in shaping the frequency

spectrum of coupled oscillatory systems. Although the frequency of the oscillations considered

herein is relatively fast with respect to the ultra-slow fluctuations (<0.1 Hz) detected with functional

Magnetic Resonance Imaging (fMRI), it is important to highlight that metastable synchronization

drives power fluctuations on ultra-slow timescales, and therefore, even relatively short time delays

can significantly modulate spontaneous activity at ultra-slow time-scales. We note that for the

numerical integration of stochastic delay differential equations to be stable and align with analytic

predictions, the time step for numerical integration needs to be sufficiently small and a running

history needs to be saved for the length of the maximum delay between units, which significantly

increases the computation times when compared to simulations where delays are neglected (here

the numerical results were found to stabilize for dt $\leq 10^{-4}$ seconds, see Supplementary Figures S18-

S20).

The discovery of multistability in systems of delay-coupled oscillators, initially described in

1999 by Young and Strogatz[65] and extended to heterogeneous delays in 2009 by Lee, Ott and

Antonsen[54], was crucial to develop the theoretical hypothesis behind this work, opening grounds to

speculate that this phenomenon may be related to the maintenance of the right balance between

integration and segregation in living brains[70,71]. Beyond the range where the model best

approximates healthy awake brain activity, we find that higher coupling enhances global order,

where the whole brain displays slow coherent oscillations in the delta-range (0.5-2Hz), which nicely

approximate the most powerful brain rhythms detected during unconscious states such as slow-

wave sleep, coma or anaesthesia. On the other hand, operating at weaker coupling hinders the

formation of MOMs at sub-gamma frequencies, altering the spectral profile similarly to what is

observed in M/EEG recordings of patients with neuropsychiatric disorders associated to

disconnection, such as schizophrenia, where the power in alpha appears to be significantly

reduced[72-75]. Such abnormal interactions within cortico-subcortical oscillatory networks may emerge

from specific local deregulation or neural circuit disruption[76]. However, how a local change may alter

the communication between brain-areas and brain network dynamics remains an open question.

Overall, these results are aligned with recent works proposing that spontaneous transitions between

multiple space-time patterns on complex networks provide a solid theoretical framework for the

interpretation of the non-stationary but recurrent macroscopic patterns emerging spontaneously in

brain activity, and ultimately supporting brain function[77,78]. From a technical perspective, it may be

surprising that this kind of itinerant dynamics emerges under symmetrical coupling between nodes;

in the sense that asymmetric coupling is normally required for breaking detailed balance – and

engendering stochastic chaos of the sort described above. However, the dynamics of each node are

generated with asymmetric Jacobians, suggesting that symmetry breaking of intrinsic connectivity is

a sufficient condition for the nonequilibrium dynamics that characterise real brains.

While metastability appears to be crucial for brain function, the specific role of MOMs to

support cognitive functions remains unclear[4,24,71,79,80]. One possibility is that the areas engaged in a

MOM are directly involved in long-range functional integration, but another is that these areas are

inhibited by entering in a collective low-energy mode[13,41]. Shedding some light on this open

question, we find that synchronization with delays induces not only a shift to slower frequencies but

also a decrease in amplitude, in line with theoretical studies reporting amplitude death in systems

with distributed delays[81] (see the vertical axes in Figure 1c). From a 'metabolic' perspective, this

shows that MOMs can be approached as 'low energy modes' with respect to high power gamma

oscillations, providing a physical explanation for the emergence of the so-called 'idle rhythms'[82].

Although the functional implications of this mechanism are beyond the scope of this work, we

expect it will provide fertile grounds for the formulation of novel falsifiable predictions to be further

tested. Moreover, these findings give room to further investigations of how local perturbations can

affect the spatiotemporospectral dynamics on the macroscopic scale, to gain insight on the

mechanisms of action of perturbative strategies such as transcranial magnetic stimulation or deep

brain stimulation.

Materials and Methods

Ethics statement

369   All human data used in this study is from the public repository of the Human connectome Project

370   (HCP)[83] (https://www.humanconnectome.org), which is distributed in compliance with international

371   ethical guidelines.

Structural connectome

The *NxN* matrices of structural connectivity, C, and distances, D, used for the network model were

derived from a probabilistic tractography-based normative connectome provided as part of the

leadDBS toolbox (https://www.lead-dbs.org/)[84]. This normative connectome was generated from

diffusion-weighted and T2-weighted Magnetic Resonance Imaging (MRI) from 32 healthy

participants (mean age 31.5 years old ± 8.6, 14 females) from the HCP. The diffusion-weighted MRI

data was recorded for 89 minutes on a specially-designed MRI scanner with more powerful gradients

then conventional scanners. The dataset and the acquisition protocol details are available in the

Image & Data Archive under the HCP project (https://ida.loni.usc.edu/). DSI Studio (http://dsi-

studio.labsolver.org) was used to implement a generalised q-sampling imaging algorithm to the

diffusion data. A white-matter mask, derived from the segmentation of the T2-weighted anatomical

images, was used to co-register the images to the b0 image of the diffusion data using the SPM12

toolbox (https://www.fil.ion.ucl.ac.uk/spm/software/spm12/). Within the white-matter mask,

200,000 most probable fibres were sampled for each participant. Then, fibres were transformed to

the standard Montreal Neurological Institute (MNI) space applying a nonlinear deformation field

derived from the T2-weighted images via a diffeomorphic registration algorithm[85]. The individual

tractograms were then aggregated into a joint dataset in MNI standard space resulting in a

normative tractogram representative of a healthy young adult population and made available in the

leadDBS toolbox[84].

The *NxN* matrices were computed from the normative tractogram using the Automated Anatomical

Labelling (AAL) parcellation scheme[86] with N=90 cortical and subcortical areas, by calculating the

number of tracts, *C(n,p),* and mean tract length, *D(n,p),* between the voxels belonging to each pair of

brain areas *n* and *p.* Details on the additional dataset and parcellation scheme used in

Supplementary Material are reported in Supplementary Methods section V and Figure S14.

MEG power spectra from healthy participants

The power spectra from human resting-state MEG signals were also downloaded from the Human

connectome Project (HCP) database as a FieldTrip structure in a MATLAB file. The MEG power

spectra are provided for 89 healthy participants at rest (mean age 28.7 years old, range 22–35, 41

female) distinct from the 32 participants from which the structural connectomes were derived, but

with similar age range and gender ratio. Resting-state MEG signals were recorded on a Magnes 3600

MEG (4D NeuroImaging) with 248 magnetometers for 6 minutes and the "powavg" pipeline was

used to obtain the power spectrum of the resting state MEG data in each MEG sensor. Briefly, the

signals were segmented, Hanning-tapered, Fourier-transformed and the power spectrum was

averaged over all segments. Notch filters were applied to remove the power line noise (cut-off

frequencies 59-61 Hz and 119-121 Hz). Additional details are explained in the HCP reference manual

(https://humanconnectome.org/storage/app/media/documentation/s1200/HCP_S1200_Release_Re

ference_Manual.pdf). The MEG power spectra were averaged across the 248 sensors to obtain a

power spectrum representative of each subject.

Brain Network Model

The Stuart-Landau (SL) equation (first term in Equation 1) is the canonical form to describe the

behaviour of a system near an Andronov-Hopf bifurcation, i.e. exhibiting the birth of an oscillation

from a fixed point[42,87]. In other words, it is used to describe systems that have a static fixed point

(like a resting spring), but respond to perturbation with an oscillation, which may damped or self-

sustained depending on the operating point of the system with respect to the bifurcation (see

Supplementary Methods, Figure S1). This model allows to designate complex-systems behaviour

among several applications, bridging the gap between the simplicity of the Kuramoto model and the

extensiveness of the phase-amplitude frameworks[88,89]. It describes how the oscillator behaves both

when it is weakly attracted to a limit cycle (displaying only damped oscillations in response to

perturbation) and, on the other hand, when it is purely restricted to a limit cycle (oscillations remain

self-sustained).

Our analysis is based on a system of N=90 SL oscillators coupled in the connectome, considering

both the connectivity strength, C_{np}, and the conduction delays, τ_{np}, between each pair of brain

areas n and p. The conduction delays are defined in proportion to the fiber lengths between brain

areas, assuming an homogenous conduction speed v, such that $\tau_{np} = D_{np}/v$, where D_{np} is the

length of the fibres detected between brain areas n and p. To simulate how the activity in node n is

affected by the behaviour of all other nodes p ($p \in N \wedge p \neq n$), we describe the interaction

between nodes in the form:

$$\frac{dZ_n}{dt} = Z_n[a + i\omega - |Z_n^2|] + K \sum_{p \neq n}^{N} C_{np}[Z_p(t - \tau_{np}) - Z_n(t)] + \beta\eta_1 + i\beta\eta_2 \, , \forall n \in N, \qquad (1)$$

where the complex variable $Z_n(t)$ describes the state of the nth oscillator at time t. The first term in

equation (1) describes the intrinsic dynamics of each unit, the second term describes the input

received from coupled units and the last terms represent uncorrelated white noise (see

Supplementary Methods, Sections I and II for detailed analysis of the model).

With this approach, we consider that the first term of Eq. 1 represents the natural excitability of

neuronal assemblies, where $\omega = 2\pi * f_f$ is the angular frequency, with f_f as the fundamental

frequency in Hertz. For our proof of concept, we set all nodes with identical natural frequency $\omega_0 =$

$2\pi * 40Hz$, representing the undifferentiated ability of a neural mass to engage in gamma-

frequency oscillations.

The parameter a determines the position of the each unit with respect to the limit cycle. For $a > 0$,

a stable limit cycle appears via a superciritical Hopf bifurcation, while when $a < 0$ there is only a

stable fixed point at the origin $Z_n = 0$, so the bifurcation point is at a = 0. Importantly, if a is

sufficiently close to the bifurcation, the system is still weakly attracted to the limit cycle and damped

oscillations emerge in response to external input, with a decay time scaled by a. In this work, we

pick a value of $a = -5$ for all nodes, such that a single input drives a damped oscillation decaying

after ~1s, approximating the slowest decay time-constants of inhibitory receptors (Figure S4)

(τdecay(GABAB) $\approx$ 500-1000ms). In Supplementary Methods (section II, Figure S7) we show that our

results are qualitatively similar for a broad range of a values, both positive and negative, thus

demonstrating the generalizability of synchronization at collective frequencies to coupled oscillatory

systems with fluctuating amplitude, be they damped or self-sustained. We note that this mechanism

only fails when the units have an overdamped response (exponential decay without oscillation),

which, in this case, only occurred for $a = -500$. Thus it is of great interest in future research to

investigate whether the local bifurcation parameters can be tuned based on sensitive observables to

fit the MEG data of different individuals in different conditions.

The second term represents the total input received from other brain areas, scaled by parameter K,

which sets the strength of all network interactions with respect to the intrinsic node dynamics.

Because we wish to focus on the nonlinear phenomena introduced by time delays, we model the

node-to-node interactions using a particular *linear diffusive coupling*, as the simplest approximation

of the general coupling function, considering *delayed* interactions. Here, the signal of node n at time

t is calculated with respect to the activity of all other nodes p at time $t - \tau_{np}$ (where τ_{np} is the time

delay between *n* and *p*), scaled by the relative coupling strength given by C_{np}.

The third term of Equation 1 represents the added uncorrelated noise to each unit (with real and

imaginary components η_1 and η_2). In this analysis, the system is perturbed with uncorrelated white

noise, where η_1 and η_2 are independently drawn from a Gaussian distribution with mean zero and

standard deviation $\beta = 0.001$ (integrated as $\beta * \sqrt{dt}$).

In this framework, our whole-brain network model is purely bottom-up (i.e., not inferred

from the MEG data we aim at explaining). For a qualitative comparison with the literature in delay-

coupled oscillatory systems [25,54,65], we explore the network dynamics as a function of the coupling

strength K and the mean delay $\langle \tau \rangle = \langle D \rangle / v$, where $\langle D \rangle$ is the mean length of all fibres detected

between each pair of brain areas. For each set of parameters, the model is solved numerically for 50

seconds with an integration step $dt = 10^{-4}$ seconds.

Kuramoto Order Parameter

467   To evaluate the global synchrony of the simulated network activity over time, we use the Kuramoto

468   order parameter:

$$R(t)e^{i\Theta(t)} = \frac{1}{N}\sum_{n=1}^{N} e^{i\theta_n(t)} \qquad (2)$$

where $\theta_n(t)$ is the phase of each node, given by the argument of Z_n. The temporal evolution of the

Order Parameter $R(t)$ provides an instantaneous measure of the degree of synchrony of the

ensemble. Since we add noise in the simulations, we first band-pass filter the signals Z_n around the

peak frequency of the ensemble. A steady order parameter indicates a stable solution (be it

asynchronous, $\langle R(t)\rangle$~0 or synchronous $\langle R(t)\rangle$~1), whereas fluctuations in the order parameter are

indicative of *Metastability*, driven by constant transitions between different weakly stable

solutions[68]. For the analysis in parameter space, we take the mean $\langle R(t)\rangle$ as a measure of the global

synchronization while the standard deviation $STD(R(t))$ indicates how much $R(t)$ fluctuates in

time[53].

Analytic Prediction of Collective Frequency of Synchronization

478   Previous theoretical studies have shown analytically that coupled oscillatory networks with

479   homogeneous delays can find stable solutions at multiple collective frequencies Ω. Let us consider

480   the Kuramoto transition in a population of phase oscillators defined by Equation 3:

$$\dot{\theta}_n(t) = \omega_0 + K\sum_{p\neq n}^{N} C_{np}\sin\left[\theta_p\left(t-\tau_{np}\right)-\theta_n(t)\right], \qquad (3)$$

481   and the fully synchronized, uniformly rotating one-cluster state $\theta_n = \cdots = \theta_N = \Omega t$.

482   Substituting this expression into Equation 3 we obtain [25,26,65,81,90]:

$$\Omega = \omega_0 - KN\sin(\Omega\tau) \qquad (4)$$

483   where ω_0 corresponds to the nodes' intrinsic frequency and τ is the homogeneous time delay

484   between nodes. As K is increased and full synchrony is approached, the system finds an equilibrium

485   point at the lowest stable solution for Equation 4, which is given by:

$$\Omega_{min} = \omega_0/(1 + KN\tau) \qquad (5)$$

486 Note that, for collective oscillations to emerge, the global coupling K needs to be sufficiently strong

487 such that the synchronized solutions are at least weakly stable. To approximate the analytic

488 prediction from equation (5), the coupling matrix was normalized by its mean, such that <C>=1.

Model Performance

We perform a parameter space exploration by tuning the two free parameters K and $\langle \tau \rangle$. We

choose to increase K exponentially as a power of 10 from 10^{-1} to $10^{1.7}$ in steps of $10^{0.1}$, to ensure a

range that covers from weak to strong coupling. $\langle \tau \rangle$ is explored in the range from 0 ms to 30 ms in

steps of 1 ms.

We measure the fitting between the empirical sensor MEG PS for each of the 89 subjects and the

simulated PS for each pair of parameters as the squared Euclidean distance, resulting in one fitting

value for each subject. This can be regarded as a maximum likelihood procedure under the

assumption of Gaussian observation noise.

Metastable Oscillatory Modes

To detect MOMs and characterize them in space and time, we band-pass filter the simulated signals

in each frequency band and obtain the corresponding amplitude envelopes using the Hilbert

transform for each band. Subsequently, we consider that a node (or brain area) engages in a MOM if

the amplitude increases 5 standard deviations above the amplitude in that frequency range. We

define the baseline threshold considering the simulations with the optimal K but with zero delays.

Since some areas are more coupled together than others, even with "zero delays" these areas may

exhibit more power across frequencies that is purely due to noisy interactions. Therefore, we define

a different threshold for each node and each band.

Envelope Functional Connectivity Patterns

Following standard procedures to estimate frequency-specific functional connectivity in empirical

source-projected MEG data[44], we first bandpass filter the simulated signals in each frequency band

of interest, compute the analytic signal using the Hilbert transform and then calculate the

correlation matrices between the amplitude (i.e. the absolute value) of the analytic signal. This is

done in one optimal point (K=10, $\langle\tau\rangle$ =3ms), for weak coupling (K=0.1, $\langle\tau\rangle$ =3ms), strong coupling

(K=50, $\langle\tau\rangle$=3ms), no delays (K=10, $\langle\tau\rangle$ =0ms) and long delays (K=10, $\langle\tau\rangle$=20ms). The same analysis is

then performed for N=200, and shown in Supplementary Methods (Section V, Figure S 17).

Author contributions

Conceptualization: JC, MLK, GD

Methodology: JC, JV, KF, GD

Investigation: JC, FC

Visualization: JC, FC

Funding acquisition: JC, VL, MLK, GD

Project administration: JC, GD

Supervision: VL, KF, MLK, GD

Writing – original draft: JC, FC

Writing – review & editing: JC, FC, JV, CB, RL, KF, VL, MLK, GD

Competing interests:

521   Authors declare that they have no competing interests.

Data and materials availability:

522   All simulations and analysis were performed in MATLAB2021b. The codes and materials used in this
523   study are publicly available at: https://github.com/fcast7/Hopf_Delay_Toolbox .

524
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