

1 **A scalp geometry based parameter-space for optimization and**
2 **implementation of conventional TMS coil placement**

3

4 Yihan Jiang¹, Boqi Du¹, Yuanyuan Chen¹, Lijiang Wei¹, ZhengCao Cao¹, Zong
5 Zhang¹, Cong Xie¹, Quanqun Li¹, Zhongxuan Cai¹, Zheng Li^{1,4}, Chaozhe Zhu^{1,2,3*}

6

7 ¹ State Key Laboratory of Cognitive Neuroscience and Learning, Beijing Normal

8 University, Beijing, China

9 ² IDG/McGovern Institute for Brain Research, Beijing Normal University, Beijing,

10 China

11 ³ Center for Collaboration and Innovation in Brain and Learning Sciences, Beijing

12 Normal University, Beijing, China,

13 ⁴ Center for Cognition and Neuroergonomics, State Key Laboratory of Cognitive

14 Neuroscience and Learning, Beijing Normal University at Zhuhai, Zhuhai, China

15

16 *Address correspondence to: Chaozhe Zhu, Ph.D. State Key Lab of Cognitive

17 Neuroscience and Learning & IDG/McGovern Institute for Brain Research, Beijing

18 Normal University, Beijing 100875, China. Tel: +86 13691341261. E-mail:

19 czzhu@bnu.edu.cn

20 Abstract

21 Transcranial magnetic stimulation efficacy is largely dependent upon coil position
22 and orientation. A good method for describing coil placement is required for both
23 computational optimization (planning) and actual placement (implementation). In
24 coordinate dependent parameter-spaces (CDPs), three-dimensional coordinates are
25 used to represent coil position and three orthogonal unit vectors are used to represent
26 coil orientation. A CDP can precisely describe arbitrary coil placement; therefore it
27 offers great advantage in computational optimization which checks through all
28 possible placements. However, a neuronavigation system is usually required to
29 accurately implement the optimized CDP parameters on a participant's head. Routine
30 clinical practice, on the other hand, often uses the International 10-20 system to
31 describe coil placement. Although the 10-20 system can only perform modeling and
32 placement at limited scalp landmarks, it allows the synthesis of different individuals'
33 targeting effects to find group-optimal parameters; it also allows manual placement,
34 which is important for commonly-seen use cases without individual MRI scans and
35 navigation devices. This study proposes a new scalp geometry based parameter-space
36 (SGP), integrating the advantages of CDP and 10-20 methods. Our SGP 1) can
37 quantitatively specify all possible conventional coil positions and orientations on an
38 individual's scalp, which is important for electrical modeling and optimization, 2)
39 maintains inter-individual correspondence, which is important for synthesizing TMS
40 effects from different individuals and studies. 3) enables fast and simple manual
41 implementation. Demonstration experiments were conducted to illustrate the

42 application of an SGP-based framework for both individual and group-based
43 optimization. A measurement experiment was performed to evaluate speed, precision
44 and reliability of SGP-based manual implementation; results show it surpasses
45 previous manual placement methods.

46 **Keywords:** TMS; targeting; coil placement; electrical modeling; optimization; group
47 synthesis; manual placement.

48 1. Introduction

49 Transcranial magnetic stimulation (TMS), one of the most important in vivo
50 neuromodulation techniques in both basic and clinical neuroscience (Lefaucheur et al.,
51 2020), can cause instant or long-term changes in cognition and behavior by inducing
52 electric currents in the brain via rapidly changing magnetic fields generated by a
53 stimulating coil placed on the scalp (AT et al., 1985). The importance of both coil
54 location and orientation to TMS efficacy have been well demonstrated. For example,
55 it has been reported that TMS antidepressant efficacy is better in lateral and anterior
56 prefrontal coil locations, where underlying cortical regions are more anti-correlated to
57 the subgenual cingulate (Fox et al., 2012; Herbsman et al., 2009). The amplitude of
58 TMS motor-evoked potential (MEP) can vary markedly due to small coil orientation
59 changes of just 10° to 15° (Tarapore et al., 2013). Such coil position and orientation
60 dependent effects have also been investigated in computational modeling studies,
61 which have found that coil position and orientation have complex interaction effects
62 with brain structure, leading to different strengths of induced electric fields. Therefore,
63 coil position and orientation on the scalp should be optimized to ensure efficient
64 stimulation of the target region (Gomez et al., 2021).

65 Coil placement optimization usually consists of two stages: planning and
66 implementation. In the planning stage, the electric fields induced by all possible TMS
67 coil placements are simulated based on an individual's brain structure. This process
68 finds the optimal placement parameters, those that maximize the chosen effect index,

69 for example, the E-field strength at the cortical region of interest (ROI) (Balderston et
70 al., 2020). An electric-field-modeling-based optimization framework for coil
71 placement has been proposed and validated with physiological observations (Opitz et
72 al., 2013; Weise et al., 2020). A fast computational auxiliary dipole method as well as
73 deep-learning-based electric field modeling have further enabled exhaustive search of
74 parameters (Gomez et al., 2021). However, individualized optimization is not a
75 common in routine TMS treatment, due to the need for MRI scans and to the time,
76 computing power and technical proficiency with a complex image analysis pipeline
77 necessary. Therefore, synthesizing individual optimization results into a group-based
78 coil placement atlas would be an important advance, one which can support the coil
79 placement decision process during typical interventions, especially large-throughput
80 clinical practice (Gomez-Tames et al., 2018a, 2020). In the implementation stage, the
81 coil should be placed on the individual's head according to the optimized parameters.
82 The most precise method is using a stereotaxic neuronavigation system to guide
83 placement. However, such an expensive device is unaffordable in many clinical
84 settings, and placements based on manual measurement have become an important
85 alternative (Beam et al., 2009; Vaghefi et al., 2015).

86 Appropriately describing the position and orientation of a coil placement is the
87 common basis of both simulation and optimization *in silico* and actual coil placement
88 *in vivo*. Currently, there are two main types of coil placement descriptions. One type
89 is based on the International 10-20 EEG reference system and its derivatives (10-10
90 and 10-5 systems), while the other type is based on three-dimensional coordinate

91 systems. The International 10-20 system (JASPER & H., 1958) is a proportional scalp
92 landmark system, consisting of 25 landmarks, 4 initial reference points and 21 evenly
93 distributed scalp points iteratively defined by relative proportional distances between
94 prior landmarks, thus taking inter-individual variations in head size into account. The
95 10-20 system was the first coil location description method and has been widely used,
96 such as in the well-known F3 treatment for depression. When using this method, the
97 coil is usually placed tangent to the scalp, with coil center contacting the scalp (called
98 conventional placement) to ensure minimal energy attenuation and easy operation.
99 The coil position (i.e., coil center location) is described by one 10-20 point and the
100 coil orientation (i.e., coil handle direction) can be described using an additional 10-20
101 point to specify the direction the handle points (Saturnino et al., 2019), or more
102 commonly, using the degree between the handle and the mid-sagittal plane
103 (Lefaucheur et al., 2020). The 10-20-system-based description intrinsically provides
104 inter-individual consistency, allowing optimization results from different individuals
105 to be directly combined to form a group-based optimization atlas (Gomez-Tames et al.,
106 2020). However, the 10-20 system includes only 25 scalp positions, so the describable
107 placement space is highly limited. The 10-10 and 10-5 systems provide higher spatial
108 resolution, but they are still enumeration methods, rather than continuous coordinate
109 systems, and therefore unable to describe all possible placements. This may mean that
110 the optimal coil placement is missed. When considering the measurement of points on
111 the scalp, each 10-20 system point can theoretically be measured manually, but the
112 identification of 10-20 landmarks in later steps depends on the positions of 10-20

113 landmarks determined in prior steps (JASPER & H., 1958; Milnik, 2009), making this
114 procedure time-consuming (16 min reported by (Xiao et al., 2017)) and error prone.
115 The Beam F3 method (Beam et al., 2009) and a semi-automatic 10-20 navigation
116 system (Xiao et al., 2017) have been proposed to improve the speed and reliability of
117 10-20 measurements.

118 Coordinate dependent parameter-spaces (CDPs) are more powerful descriptive
119 methods for coil placement. CDPs use three-dimensional coordinates and three
120 orthogonal unit vectors to represent position and attitude of the coil (Saturnino et al.,
121 2019). Unlike the 10-20 system, a CDP is a continuous space that can quantitatively
122 describe arbitrary coil placement, which is important for global optimization. One
123 problem is that this space includes regions inside the person's head (i.e., the coil
124 intersects with the head), which are physically inaccessible, as well as large regions
125 far away from the head, where coils are unable to generate efficient stimulation.
126 Therefore, most optimization studies have used conventional placement spaces as
127 search spaces, to reduce the size of the search space and improve the efficiency of
128 optimization results (Balderston et al., 2020; Gomez et al., 2021; Gomez-Tames et al.,
129 2018b). Unlike the 10-20 system, optimal CDP parameters of different individuals are
130 difficult to synthesize. Individually optimal CDP parameters come from different 3D
131 coordinate systems based on different MRI spaces, with different head size and shape.
132 Therefore, how to summarize CDP optimization results from different individuals is a
133 complex problem. In addition, the optimal CDP placement parameters (coil position
134 coordinates and orientation vectors) cannot be directly manually measured. They

135 instead require interactive navigation based on neuronavigation systems for
136 implementation. This is also a reason why CDP is not used more commonly.

137 Taken together, 10-20-based methods and CDP-based methods each have their
138 own advantages in individualized optimization, group synthesis and manual
139 placement, but also drawbacks. The present study aims to combine the advantages
140 together: we propose a scalp geometry based parameter-space (SGP) that can 1)
141 quantitatively specify all possible positions and orientations in conventional
142 placement; 2) maintain inter-individual comparability; 3) be implemented *in vivo* in a
143 fast and simple way, with only tape measure and pen. In the present study, we first
144 provide the SGP definition, then we present a general framework for optimization and
145 implementation of SGP-based coil placement, including both individualized and
146 non-individualized optimization. We provide a demonstration experiment to give a
147 detailed and intuitive presentation of how to apply SGP-based systems during
148 individualized and group-based optimization of TMS coil placement. For the
149 implementation stage, we specifically propose a manual placement protocol that can
150 easily be implemented for arbitrary positions and orientations described by SGPs. We
151 perform two preliminary experiments to evaluate the speed, precision and reliability
152 of manual placement.

153 2. Methods

154 2.1 SGP space (s , φ) for conventional TMS coil placement

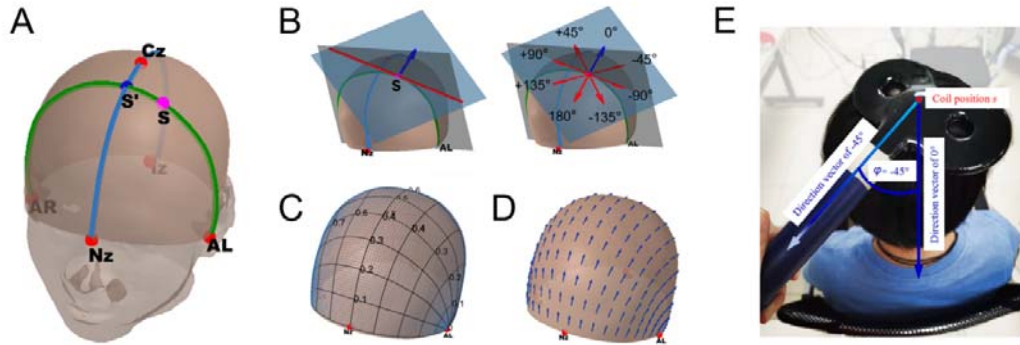
155 Like most individual coil placement optimization studies (Balderston et al., 2020;
156 Gomez et al., 2021; Gomez-Tames et al., 2018b), we also perform optimization in the
157 conventional placement space, defining the coil position as the location of the contact
158 point between the coil center and the person's head and defining the coil orientation as
159 the angle of the handle (in the plane tangent to the head surface) versus the
160 mid-sagittal plane.

161 We utilize our previously proposed Continuous Proportional Coordinate (CPC)
162 system to define the position parameters of an arbitrary scalp point s (P_{NZ} , P_{AL})
163 (Fig.1A). Like the 10-20 system, CPC parameters are calculated from head reference
164 points: nasion (NZ), inion (IZ) and the left/right preauricular points (AL/AR). Given
165 these reference points, the CZ point, also needed for the procedure, can be identified
166 as follows. First, find the midpoint of an arbitrary NZ-IZ curve, Mid_{NZIZ} . Next, find
167 the midpoint (called Mid_{ALAR}) of the curve going through AL, Mid_{NZIZ} and AR. Next,
168 find the midpoint of the curve going through NZ, Mid_{ALAR} and IZ, giving a new
169 Mid_{NZIZ} . Repeat this process until the iteratively found Mid_{NZIZ} meets the iteratively
170 found Mid_{ALAR} : this intersection midpoint is CZ.

171 Then, the coordinates of any point s can be determined by proportional distances
172 on two geodesic curves. One is a reference curve that is independent of s , defined as
173 the intersection of the scalp surface and the plane through NZ, CZ and IZ (i.e.,

174 mid-sagittal plane; blue curve in Fig.1A). The length of the reference curve is denoted
175 as L_{ref} . The other curve, the *active* curve, depends on s and is defined as the
176 intersection of the scalp surface and the plane through AL, AR and s (green curve in
177 Fig.1A). The length of the active curve is denoted as L_{active} . The reference curve and
178 active curve intersect at s' . The first position parameter P_{NZ} is the proportion between
179 curve length from NZ to s' and the full reference curve length, i.e., $P_{\text{NZ}} = L_{\text{NZ-}s'}/L_{\text{ref}}$.
180 The second position parameter P_{AL} is calculated as the proportion between curve
181 length from AL to s and the full active curve length, i.e., $P_{\text{AL}} = L_{\text{AL-}s}/L_{\text{active}}$. In this way,
182 any scalp point s has a pair of corresponding position parameters (Fig.1B).

183 After defining coil location s , the orientation can be defined in the tangent plane
184 of point s (Fig.1B). We first specify a zero-degree direction. The gray plane (Fig.1B)
185 is determined by AL, AR and s , while the blue plane is the tangent plane at point
186 s . These two planes intersect at the red line. The zero-degree direction is defined by a
187 unit vector in the tangent plane that is perpendicular to the red line, starting at s and
188 pointing backwards (blue vector). Any orientation can be obtained by rotation of the
189 zero-degree direction vector (positive anticlockwise, negative clockwise) in the
190 tangent plane. Taking the figure-8 coil as an example, the SGP parameters of a coil
191 placement is shown in Fig.1E.

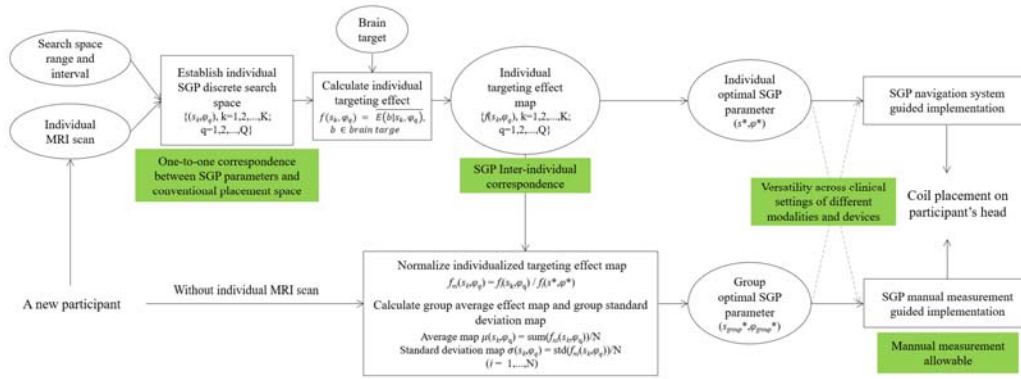


192

193 Figure 1. (A) Definition of coil an example position s (magenta dot, $P_{NZ} = 0.4$, $P_{AL} = 0.4$)
194 involves proportions of lengths along two curves anchored at cranial landmarks. (B)
195 Definition of zero-degree direction (blue vector) and example direction vectors of different
196 orientation φ (red vectors) at coil position s . (C) A discrete version of SGP obtained by evenly
197 dividing each dimension into 10 units. (D) Zero-degree direction vectors at different coil
198 positions. (E) An example showing placement of a coil at position s with orientation $\varphi = -45^\circ$.

199 **2.2 SGP based optimization and implementation of coil** 200 **placement**

201 We first show the pipeline when conditions for individual optimization are
202 available (individual MRI scan provided, computing power and time are sufficient).
203 At the planning stage, the individual's T1 image is segmented into different issues to
204 generate the individual's head mesh and scalp mesh. Using the individual's scalp
205 mesh, search space range and search interval as input, a discrete SGP search space
206 $\{(s_k, \varphi_q), k=1, \dots, K; q=1, \dots, Q\}$ can be constructed. By changing total position number
207 K and total orientation number Q , the search space can be defined with arbitrary
208 density.



209

210 Figure 2. Framework for SGP-based optimization and implementation of coil placement.

211 Individualized optimization pipeline is shown at the top, and group-based optimization

212 pipeline without individual MRI data is shown at the bottom. In the last step, solid lines point

213 to the typical implementation, while dotted lines point to alternatives. The main properties of

214 SGP that enable the process are emphasized in green boxes.

215 We can then simulate the electric field distribution $E(s_k, \phi_q)$ for each placement in

216 the search space based on the head model mesh constructed from the individual's data.

217 Additionally, stimulation intensity, coil configuration and tissue electrical

218 conductivities can be added into this modeling process, or default parameters

219 (provided in software like SimNIBS (SimNIBS Developers, 2020)) can be used. Next,

220 given a brain target (can be defined using anatomical, functional or connectivity

221 properties) and an optimization strategy (here e.g., maximize the electric field strength

222 inside the target), we can calculate the targeting effect $f(s_k, \phi_q)$ as the average electric

223 field strength inside the target for each placement (s_k, ϕ_q) and find the optimal

224 parameter (s_*, ϕ_*) for this individual:

225

(1)

$$(s^*, \varphi^*) = \underset{k \in \{1,2, \dots, K\}, q \in \{1,2, \dots, Q\}}{\operatorname{argmax}} f(s_k, \varphi_q) \quad (2)$$

226
227
228 At the implementation stage, the coil placement can be implemented on the
229 person's head very precisely with the guidance of an SGP-based navigation system (in
230 development). Alternatively, placement can be indirectly implemented by
231 transforming the SGP parameters to three-dimensional CDP parameters (when the
232 individual's T1 image is available) and using a CDP neuronavigation system (like
233 BrainSight) to guide placement. Another alternative is to implement placement via
234 manual measurement.

235 In circumstances not permitting individualized optimization, one possible
236 solution is to summarize the normalized targeting effect map $f_{ni}(s_k, \varphi_q)$ from different
237 individuals i ($i=1,2,\dots,N$) in a database into a group average targeting effect map to
238 guide placement. SGP parameters intrinsically correspond across individuals,
239 therefore, if the search space is the same for different individuals, the results can be
240 directly synthesized.

241 First, for each individual i , the individual's targeting effect at (s_k, φ_q) are
242 normalized by dividing by the maximum targeting effect.

$$f_{ni}(s_k, \varphi_q) = \frac{f_i(s_k, \varphi_q)}{f_i(s^*, \varphi^*)},$$
$$i \in \{1,2, \dots, N\}, k \in \{1,2, \dots, K\}, q \in \{1,2, \dots, Q\} \quad (3)$$

243
244
245 Then, the normalized individual targeting effects of many individuals can be
246 synthesized into an average targeting effect map.

$$\mu(s_k, \varphi_q) = \frac{\sum_{i=0}^N f_{ni}(s_k, \varphi_q)}{N} \quad (4)$$

247

248 The standard deviation of the targeting effect map across different individuals
249 can also be calculated.

$$\sigma(s_k, \varphi_q) = \sqrt{\frac{\sum_{i=0}^N (f_{ni}(s_k, \varphi_q) - \mu(s_k, \varphi_q))^2}{N}} \quad (5)$$

250

251 If there exists a placement parameter setting with relatively large average
252 targeting effect μ and relatively small standard deviation σ , then it can be chosen as
253 a group-appropriate placement parameter ($s_{group}^*, \varphi_{group}^*$). The group-appropriate
254 placement can be implemented through an SGP-based navigation system or through
255 SGP-based manual measurement.

256 **2.3 SGP Manual measurement**

257 Tools needed in the manual measurement process include two tape measures, a
258 marker, a protractor (or visual estimation) and a calculator (or mental calculation).

259 For any given position s (P_{NZ}, P_{AL}) and orientation φ , the measurement steps are
260 as follows:

261 (1) Find 4 reference points, the Nasion, Inion and left and right preauricular points on
262 the head (Fig.3[1]). Time: about 30 seconds.

263 (2) Find point the CZ point and the reference curve. Time: about 3 minutes.

264 First, find the midpoint of an arbitrary NZ-IZ curve, Mid_{NZIZ} . Next, find the midpoint
265 of the curve connecting AL, Mid_{NZIZ} and AR, Mid_{ALAR} . Next, find the midpoint of the
266 curve connecting NZ, Mid_{ALAR} and IZ and set it as a new Mid_{NZIZ} . Iterate the above
267 two steps until Mid_{NZIZ} meets Mid_{ALAR} . This common midpoint is CZ. The curve
268 connecting NZ-CZ-IZ is the reference curve (Fig.3[2]).

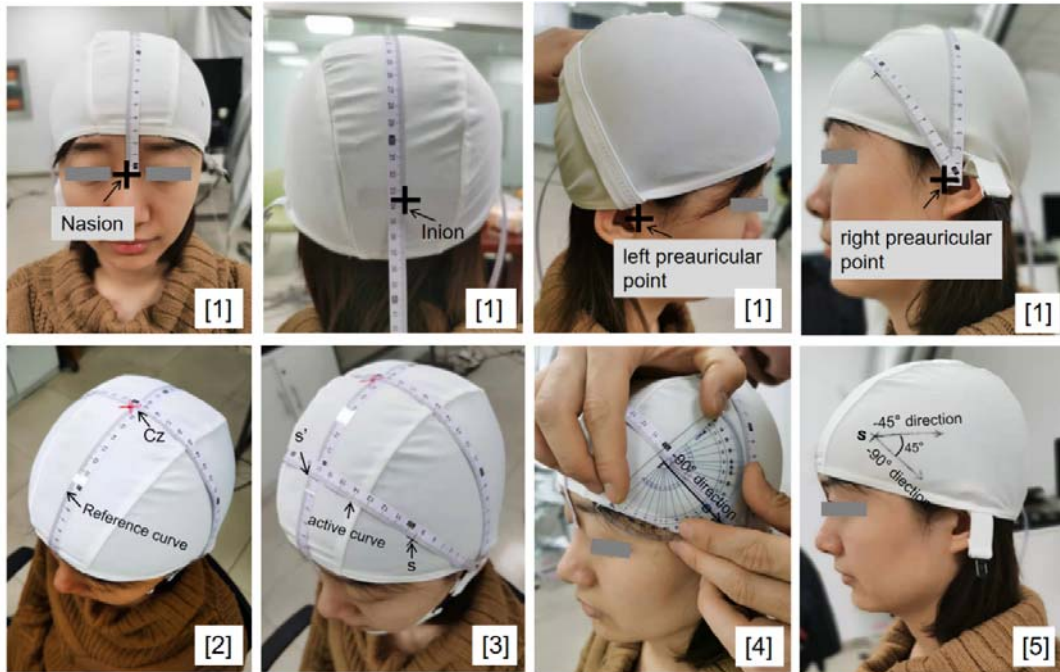
269 (3) Find point s' , the active curve and point s . Time: about 1.3 minutes

270 First, measure the length of reference curve L_{ref} , calculate the length value $P_{NZ} \times L_{ref}$.
271 Then, mark point s' as the point along the reference curve that is $P_{NZ} \times L_{ref}$ distance
272 from NZ. The curve connecting AL, s' and AR is the active curve. Next, measure the
273 length of active curve L_{active} and calculate the length value $P_{AL} \times L_{active}$. Then, mark
274 point s as the point along the active curve that is $P_{AL} \times L_{active}$ distance from AL
275 (Fig.3[3]).

276 (4) Find the -90° direction and arbitrary orientation φ . Time: about 20 seconds.

277 The direction from point s to AL along the active curve is the -90° direction. Using a
278 protractor (or visual estimation), find orientation φ based on the -90° direction
279 ([Fig.3[4]).

280 (5) Use a marker or an eyebrow pencil to mark point s and orientation φ on the cap
281 (Fig.3[5]). Time: about 40 seconds.



282

283 Figure 3. Illustration of manual measurement of SGP parameters. (1) Mark 4 reference points:
284 Nasion, Inion and left and right preauricular. (2) Find CZ and the reference curve. (3) Find
285 point s' , the active curve and point s . (4) Find the -90° direction and orientation φ . (5) Mark
286 point s and orientation φ on the cap.

287 **2.4 Manual measurement experiment: evaluating speed,** 288 **precision and reliability**

289 Five healthy adults (mean age = 23.7, 3 females, 2 male) were enrolled in a
290 preliminary study to investigate the speed, precision and reliability of manual position
291 measurement. Nine typical positions (P_{NZ} , P_{AL} : (0.27,0.26), (0.53,0.25), (0.79,0.24),
292 (0.22,0.47), (0.52,0.50), (0.78,0.53), (0.24,0.72), (0.50,0.77), (0.75,0.75)) uniformly
293 distributed on the scalp surface were set as targets. For each participant, nine positions
294 were measured by three trained TMS technicians at two time points over the course of

295 one month, with at least 24 hours separating measurement sessions (n = 270 total
296 measurements, 30 at each scalp target). The first step of position measurement,
297 finding the CZ and reference curve, is the same for different targets and therefore that
298 process was performed only once at the start and shared for other points.

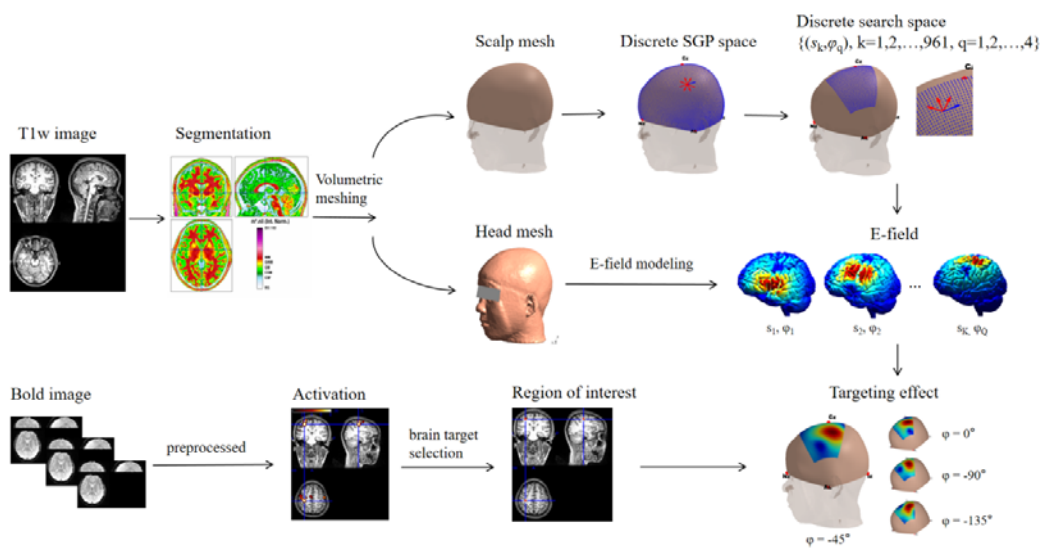
299 We used a commercial 3D digitizer (Fastrak™, Polhemus) to perform a dense
300 sampling of each participant's head from which the head point cloud was
301 reconstructed. The position of the point identified by manual measurement was
302 recorded by the 3D digitizer. The position of the target point was calculated on the
303 reconstructed head point cloud (acting as ground truth). Distance between the
304 identified point and ground truth target point was calculated as the measurement error
305 (quantifying precision). We separately evaluated inter-technician reliability relative to
306 a group-averaged target coordinate and intra-technician reliability relative to a
307 technician-specific average (following the reliability definition in (Trapp et al.,
308 2020)).

309 Furthermore, four healthy adults (mean age = 25.3, 4 females, 1 male) were
310 enrolled in a preliminary study to investigate the precision of the manual orientation
311 measurement. For each participant, four orientations (0°, 45°, 90°, 135°) were
312 measured at three scalp positions ((0.27,0.26), (0.52,0.5), (0.75,0.75)) by three trained
313 TMS technicians (n=144 total measurements), following the manual measurement
314 protocol. Additionally, technicians also measured 45° via visual observation, to
315 evaluate the precision of this common clinical practice. The direction vector of the
316 manually identified orientation was recorded by the 3D digitizer; the direction vector

317 of the target orientation was calculated from the participant's head point cloud
318 generated by dense sampling on the head (acting as ground truth). The angle between
319 the identified orientation and the ground truth target orientation was calculated as the
320 measurement error (quantifying precision).

321 **2.5 Demonstration experiment for individualized and** 322 **group-based optimization**

323 A demonstration experiment using real data was conducted to illustrate how the
324 SGP-based optimization protocol works. We show the utility of this protocol in
325 generating “coil placement targeting effect atlases” that relate coil placement to
326 individualized or group-based targeting effects. These atlases can be used to guide
327 researchers and clinicians in deciding optimal coil placement for a specific brain
328 target. The brain target in this demonstration is the motor cortex.



329
330 Figure 4. The SGP-based individualized optimization protocol

331 Input MRI Data Acquisition:

332 Each individual's high-resolution T1-weighted structural image was acquired on a
333 Siemens Trio 3T MRI Scanner (TR/TE, 2530/3.5ms; flip angle, 9°; field of view, 176
334 mm × 256 mm; slices, 256; thickness, 1.0 mm; voxel size, 1 mm × 1 mm × 1 mm).
335 The individual's BOLD functional images were acquired on a Siemens Trio 3T MRI
336 Scanner (TR/TE, 2000/28ms; flip angle, 90°; field of view, 102 mm × 102 mm; slices,
337 32; thickness, 2.0 mm; voxel size, 2 mm × 2 mm × 2 mm; volumes, 156) during a
338 finger tapping task, including seven rest blocks of 24 s with fixation point and six task
339 blocks of 24s with right-hand tapping by the first dorsal interosseous muscle. Four
340 dummy scans were completed at the beginning of each run to allow for stabilization
341 of the MR signal. To achieve a higher resolution, BOLD images were focused to
342 cover the cortical motor areas, so an additional whole EPI volume was acquired for
343 co-registration (TR/TE, 6000/28ms; flip angle, 90°; field of view, 102 mm × 102 mm;
344 96 slices; 2 mm isotropic resolution).

345 Experimental procedure:

346 1) Based on the SPM12 (<https://www.fil.ion.ucl.ac.uk/spm/software/spm12/>,
347 Ashburner and Friston, 2005) segmentation routine, the individual's T1 image was
348 segmented into six tissue images (gray matter, white matter, cerebrospinal fluid (CSF),
349 bone, soft tissue, and air/ background). Subsequently, the scalp mesh was extracted
350 from a smoothed and binarized head image (gray matter + white matter + CSF + bone
351 + soft tissue) (Xiao et al., 2018) and the head model mesh was created with
352 SimNIBS's default pipeline "headreco"(Nielsen et al., 2018). Time: about 2 hours.

353 2) We identified four cranial landmarks NZ, AL, AR and IZ in the individual T1
354 image using MRIcron software and located the CZ point using Jurcak's iterative
355 algorithm (Tsuzuki et al., 2007). Based on these reference points, a discrete SGP
356 space was established by uniformly dividing the geodesic curves (including active
357 curve and reference curve) into 100 portions (spatial resolution = 1%, i.e., $\Delta P_{NZ} = 1\%$
358 reference curve, $\Delta P_{AL} = 1\%$ active curve) and the angle into 8 intervals ($\Delta\phi = 45^\circ$).
359 The search space was sampled from this discrete SGP space. The search had 31×31
360 grid positions ($P_{NZk} = 0.3:0.01:0.6$, $P_{ALk} = 0.2:0.01:0.5$) centered around the scalp
361 point ($P_{NZ} = 0.5$, $P_{AL} = 0.35$), which is supposed to be the best target for the motor
362 system according to a meta-analysis study (Jiang et al., 2020)). The inter-point
363 distance was 1% of the reference or active curve length. Four coil orientations were
364 searched per position: from 0° to 135° at 45° intervals. 961 coil positions and 4
365 orientations combined into 3844 coil placement configurations $\{(s_k, \phi_q) \mid k=1,2,\dots,961 ;$
366 $q=1,2,\dots,4\}$, as shown in Fig.4.

367 3) For each coil placement configuration, a three-dimensional scalp coordinate
368 corresponding to the coil position s_k and three three-dimensional vectors X, Y, Z
369 corresponding to the coil orientation ϕ_k were obtained on the scalp mesh using custom
370 Python code. Specifically, the X vector of SimNIBS corresponded to the coil handle
371 direction vector in our definition, the Y vector corresponded to the normal vector to
372 the tangent plane, and the Z vector was the cross product of X and Y. Given the
373 converted three-dimensional coil placement parameters and the head mesh model as
374 input, we ran simulation in SimNIBS to calculate the induced E-field distribution

375 $E(b|s_k, \varphi_q)$. The electrical conductivities (S/m) were set as the defaults, white matter:
376 0.126, gray matter: 0.275, CSF: 1.654, bone: 0.01, scalp: 0.465, eyes: 0.5, silicone
377 rubber: 29.4 and saline: 1.0.

378 After the electric-field modeling, the targeting effect $f(s_k, \varphi_q)$ was calculated for
379 each (s_k, φ_q) . Following the protocol proposed by Balderston (2020), we defined $f(s_k, \varphi_q)$
380 as the electric field strength inside an individualized region of interest (ROI). The
381 individualized motor ROI was set as a 5-mm spherical region centered on the
382 individual's activation peak coordinate in a robust finger-tapping task (analyzed with
383 FMRI Expert Analysis Tool). Calculating each placement configuration took about 2
384 minutes, 3844 configurations together took about 128 hours.

385 4) We found the individual's optimal position s^* and orientation parameter φ^* as
386 those with maximum average E-field strength in the ROI.

387 5) We calculated the individualized targeting effect map and optimal placement
388 parameter for 8 participants (5 males, 3 females, mean age 26.4 ± 2.1 years), and then
389 summarized the normalized individualized targeting effect map into a group-level
390 average targeting effect map and a standard deviation map. The group-level
391 appropriate placement was the position and orientation that had a relatively large
392 average targeting effect and relatively small standard deviation across participants.

393 3. Results

394 3.1 Manual measurement experiment: evaluating speed, 395 precision and reliability

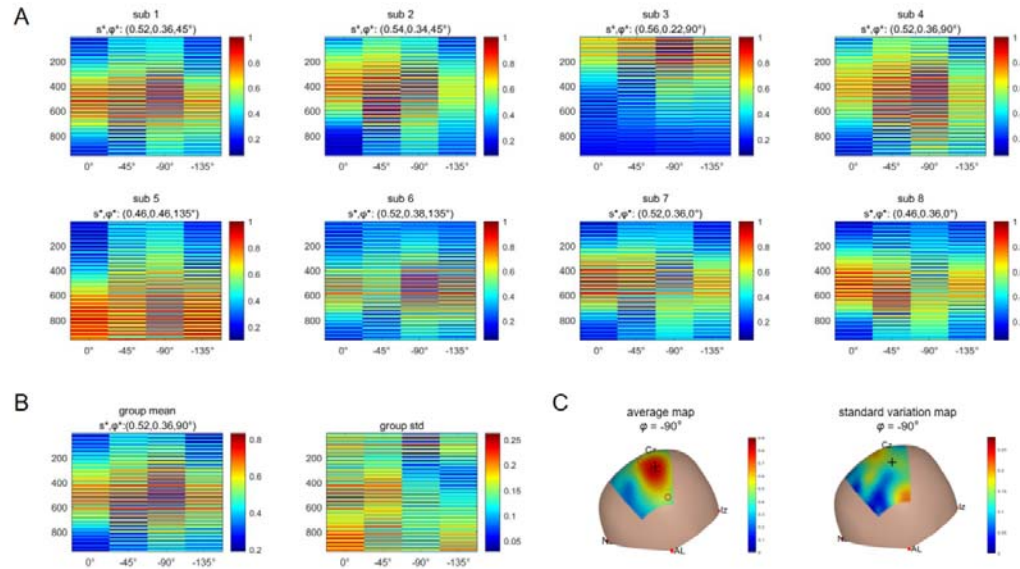
Speed	Mean	SD	Maximum	Minimum
Measurement of the Cz point and the reference curve (step 1, 2)	(minute)			
Technician 1	3.22	0.98	4.99	1.67
Technician 2	3.64	0.42	4.70	3.24
Technician 3	3.38	0.75	4.88	2.24
Measurement of scalp position s (step 3)	(minute)			
Technician 1	1.33	0.47	3.30	0.68
Technician 2	0.91	0.24	1.62	0.51
Technician 3	0.86	0.20	1.61	0.54
Measurement of orientation ϕ with protractor (step 4)	(minute)			
Technician 1	0.59	0.22	1.13	0.37
Technician 2	0.75	0.16	0.91	0.53
Technician 3	0.57	0.23	0.80	0.36
Precision	Mean	SD	Maximum	Minimum
Measurement of scalp position s	(mm)			
Technician 1	3.74	2.15	10.94	0.95
Technician 2	3.96	2.56	10.07	0.67
Technician 3	4.60	2.74	11.57	0.65
Measurement of 45° with protractor	(degree)			
Technician 1	3.51	1.70	6.72	0.98
Technician 2	6.38	1.76	9.18	4.25
Technician 3	2.96	1.66	5.22	1.39
Measurement of 45° with visual estimation	(degree)			
Technician 1	4.50	2.02	8.06	1.93
Technician 2	9.38	3.11	13.97	6.86
Technician 3	7.65	3.54	13.28	3.30
Measurement of other orientations with protractor	(degree)			
Technician 1	4.36	3.10	6.31	0.78
Technician 2	6.74	2.03	8.74	4.69
Technician 3	2.91	1.46	4.30	1.38
Reliability	Mean	SD		
Intra-technician reliability	(mm)			
SGP	3.53	1.86		
Beam F3 (Trap et al.,2020)	9.30	6.20		
5.5 cm (Trap et al.,2020)	11.70	6.80		
Inter-technician reliability	(mm)			
SGP	4.72	2.20		
Beam F3 (Trap et al.,2020)	9.50	6.10		
5.5 cm (Trap et al.,2020)	12.20	6.60		

396

397 Table1. The speed, precision and reliability of SGP manual measurement

398 Summing together the mean measurement time for each step in the placement
399 process, the whole placement process (Step1,2 + Step3 + Step4) takes about 5.08
400 minutes in total. The longest is about 7.78 minutes and the shortest is only 3.12
401 minutes. The overall average accuracy of all technicians measured at all locations (9
402 locations) was 4.1 ± 2.51 mm. Among them, 73% of measurements' errors were less
403 than 5mm. The overall angle accuracy of all technicians at all angles ($0^\circ, 45^\circ, 90^\circ, 135^\circ$)
404 with protractor was $4.24 \pm 2.24^\circ$. We compared the measurement by protractor to
405 visual estimation at 45° and found that errors from protractor were significantly
406 smaller than errors from estimation (mean = 4.09° versus 6.51° , $t = 2.9668$, $df = 46$,
407 $p < 0.01$), but using a protractor required more time. For both intra-technician and
408 inter-technician reliability, the SGP-based protocol (intra-technician: 3.53 ± 1.86 mm;
409 inter-technician: 4.72 ± 2.2 mm) performed better than the BeamF3 method
410 (intra-technician: 9.3 ± 6.2 mm; inter-technician: 9.5 ± 6.1 mm) and 5.5cm method
411 (intra-technician: 11.7 ± 6.8 mm; inter-technician: 12.2 ± 6.6 mm), as reported in Trapp
412 et al., 2020.

413 **3.2 Demonstration experiment for individualized and**
 414 **group-based optimization**



415

416 Figure 5. A) Individualized targeting effects for 961 positions (y-axis) and 4 orientations
 417 (x-axis). Optimal position and orientation (s^* , φ^*) that maximizes individualized targeting
 418 effect is shown in the subtitle. B) Group-based targeting effect map, standard deviation map
 419 and the group-appropriate parameters. C) Scalp visualization of group-based targeting effect
 420 map and the standard deviation map at group-appropriate orientation ($\varphi = -90^\circ$).
 421 Individualized optimal positions that maximize individual targeting effects at $\varphi = -90^\circ$ are
 422 marked with red circles; the group-based appropriate position is marked with a black cross.

423 TMS electrical effects in the motor cortex were modeled for 961 positions and 4
 424 orientations. As shown in Fig.5A, both different positions and orientations will lead to
 425 different electrical effects at the ROI. The personalized optimal positions were
 426 (0.52,0.36), (0.54,0.34), (0.56,0.22), (0.52,0.36), (0.46,0.46), (0.52,0.38), (0.52,0.36)
 427 and (0.46,0.36) for the seven participants. These positions were distributed around the

428 10-20 landmark C3 (0.50,0.35). The individually optimal orientations included all
429 searched orientations, 0° , -45° , -90° and -135° , showing inter-individual variation in
430 orientation. The group-based appropriate parameter was (0.52,0.36, -90°), with a
431 maximum average targeting effect $\mu = 0.83$ and a relatively small standard deviation
432 $\sigma = 0.14$.

433 4. Discussion

434 In this article, we proposed a scalp-geometry based parameter-space to describe
435 TMS coil placement and showed how to apply SGP in different clinical settings for
436 coil placement optimization and implementation.

437 4.1 Properties of scalp geometry-based parameter

438 SGP describes the position and orientation of TMS coils based on the geometric
439 properties of the head. For the coil position s , the geometry information to be
440 measured includes the position of five reference points (NZ, IZ, CZ, AL, AR) and the
441 arc length of four geodesics (NZ- s ', NZ-IZ, AL- s and AL-AR). For the orientation of
442 the coil at point s , the geometric information to be measured includes the intersection
443 line of the tangent plane at point s and the plane of the active arc, and the rotation
444 angle of the line around point s .

445 This scalp geometry-based definition leads to several basic properties. First, a set
446 of parameters in SGP space has a one-to-one correspondence to a conventional TMS
447 coil placement. Given a conventional coil placement on the scalp, each coil center
448 location corresponds to a unique position parameter s defined by two arc length

449 proportions (P_{NZ}, P_{AL}) and each coil handle direction corresponds to a unique rotation
450 ϕ from the zero vector of s in the tangent plane. Conversely, for any given set of SGP
451 parameters (s, ϕ) , there is a unique corresponding coil placement: placing the coil
452 center at s and turning the handle ϕ degrees from the zero vector in the tangent plane.
453 This one-to-one correspondence allows SGP-based methods to accurately navigate
454 and record any possible scalp position and orientation.

455 Second, the parameter space has inter-individual consistency. That is, if we place
456 coils on different individuals' scalps using the same SGP parameter, these placements
457 are consistent. That is a natural property shared by both the 10-20 system and the SGP.
458 They use reference points to define subsequent curves and measure proportional
459 positions on the curves. Reference points are scalp landmarks consistent between
460 different people and the proportional measurement take head size variations into
461 account. Therefore, the proportional position s' on the reference curve has
462 inter-individual consistency, and the active curve defined by AL, AR and s' also has
463 consistency. The direction of the intersection between the active curve plane and the
464 tangent plane of s is consistent, thus the coil handle direction a certain angle from this
465 intersection direction also has inter-individual consistency. These properties allow the
466 SGP to be used as a standard space to compare and synthesize results from different
467 individuals or different studies, to obtain more generalizable conclusions. As shown in
468 Fig.5, preliminary results show that the differences in targeting effect distributions
469 among different individuals are not very large (std<0.27 normalized effect) so there
470 are similarities that support synthesis.

471 Third, the SGP is quantitatively measurable both *in silico* and *in vivo*. All the
472 information needed to define SGP are measurable geometric parameters on the
473 head, which provides the theoretical basis for measurability. *In silico*, we can
474 reconstruct the scalp mesh from MRI images, calculate arbitrary SGP-based positions
475 and orientations and use computational modeling such as electric field simulation to
476 traverse over the targeting effects of potential placements (as shown in the
477 demonstration experiment). *In vivo*, the scalp mesh can be reconstructed from a dense
478 sampling of a participant's scalp with a 3D digitizer. Any error between the current
479 placement's SGP position and the target one can be computed in real-time to help
480 achieve accurate coil placement. Meanwhile, positions in SGP can be measured
481 manually in clinical practice, in a fast and simple way that is free of additional
482 equipment. As shown in the methods, the measurement only involves measuring four
483 geodesic distances: NZ-*s'*, NZ-IZ, AL-*s* and AL-AR and one angle from the zero
484 direction. In our manual measurement experiment, we recorded the speed, precision
485 and reliability of three technicians while they performed these steps. The speed of
486 placement (about 5 minutes) was quick compared to the reported time required for the
487 10-20 method to only measure the position (16 minutes, Xiao 2016). Our error was
488 <5mm in 73% of measurements, comparable to the reported discrepancies of the
489 BeamF3 (<9.9 mm in 75% of participants). Our reliability (intra-technician:
490 3.53 ± 1.86 mm; inter-technician: 4.72 ± 2.20 mm) is better than the BeamF3 method
491 (intra-technician: 9.3 ± 6.2 mm; inter-technician: 9.5 ± 6.1 mm) or 5.5cm method
492 (intra-technician: 11.7 ± 6.8 mm, inter-technician: 12.2 ± 6.6 mm) for both

493 intra-technician and inter-technician reliability (Trapp et al., 2020). These
494 experimental results show that, in the absence of navigational equipment and complex
495 computing capacity, coil parameters can be manually measured on the scalp with
496 good accuracy and speed.

497 **4.2 Comparison of SGP with 10-20 and CDP methods**

498 How to describe the position and orientation of coil placement is the common
499 basis of optimization and actual placement. Different description methods for coil
500 placement may have different effects on optimization and actual placement. Below,
501 we compare our description method with two existing description methods from three
502 perspectives: individualized optimization, group synthesis and real-world
503 implementation of the coil placement protocol.

504 **Performance of different methods in individualized optimization**

505 The goal of optimization is to go through all possible coil placements to find the
506 best placement. Therefore, it is important for a description method to be able to
507 describe all potential coil placements. Coil placements can be divided into physically
508 unachievable (part of the coil intersects with the head) and physically achievable
509 placements. Physically achievable placements also include large areas far away from
510 the scalp that are not able to generate efficient stimulation due to electric field
511 attenuation. Therefore, the physically realizable space with practical significance is
512 mainly composed of conventional placements (coil placed in a plane tangent to the
513 scalp with coil center contacting the scalp). Conventional placement space contains

514 the commonly used placements in clinical practice and is adopted in most
515 optimization studies as the search space.

516 The 10-20 method and its extensions (like 10-10 and 10-5) are essentially a set of
517 finite points rather than a continuous parameter space. It can only describe a limited
518 number of protocols in conventional placement space, which is a significant problem
519 for optimization. On the other hand, CDP is a continuous space that can quantitatively
520 describe position and posture of any coil placement, which is conducive to global
521 optimization. However, taking the space occupied by the person's head into account,
522 many parameters in CDP are physically impossible or far away from the
523 head. Therefore, CDP-based optimization usually requires parameters to be
524 constrained to the conventional placement space, which leads to a complex constraint
525 optimization problem. The proposed SGP space is based on head geometry. All SGP
526 parameters are constructed according to head geometry, therefore it only includes
527 conventional placement with coil center contacting the scalp tangentially, removing
528 any intersecting or far away placements, which reduce the size of the search space and
529 improve the efficiency of optimization. Moreover, optimization based on SGP is an
530 unconstrained optimization problem, which is usually much simpler than constrained
531 optimization problems in a mathematical sense. Meanwhile, SGP is also a continuous
532 space, so it will not leave out any possible conventional placement, as compared to
533 10-20 methods and their extensions.

534 Performance of different methods in group synthesis

535 As mentioned in the Introduction, in some clinical practice individualized
536 optimization is impossible due to the absence of MRI scans or lack of time and
537 computing power. Synthesis of individualized results from previously recorded
538 databases into a group atlas can be an important alternative to guide placement in such
539 cases. Inter-individual consistency of coil placement is a requisite for synthesis.
540 Although the descriptive capacity of the 10-20 system and its extensions are
541 insufficient, 10-20 system points have natural correspondence between individuals,
542 which enables the optimization results based on 10-20 system to be summarized
543 directly. For example, Gomez-Tames (2019) synthesize individual deep TMS dosage
544 in targeted deep brain regions at different 10-20 positions into a group-level dosage to
545 overcome the limitations of using individualized head models to characterize coil
546 performance in a population, providing a group-level dosage atlas to guide coil
547 placement for each deep region. Like the 10-20 system, the definition of SGP is also
548 determined based on the geometric parameters of the head, which are consistent
549 between individuals. Therefore, the optimization results from different individuals can
550 be summarized directly, as shown in our demonstration experiment.

551 CDP parameters, on the other hand, are based on individual-specific
552 three-dimensional coordinate systems: the space where individualized electric field
553 modeling is performed, i.e., the native T1 image space. So, in order to synthesize the
554 result of different individuals, their CDP parameters in native space have to be
555 registered to a standard CDP space based on MNI space. That means an additional

556 registration process is needed. Although the registration between spaces (via images)
557 based on brain intensity values or brain surface geometries is commonly done in
558 many software, there is much less work on how to perform a registration between
559 scalps, where the coil position is located. Moreover, this process not only involves the
560 registration of coil position points, but also involves the registration of a directional
561 vector, which is even more complicated. Little effort has been done in this
562 area. Another feasible way is to convert the optimization result from individual CDP
563 space into SGP space (each three-dimensional coordinate can be converted to a
564 proportional coordinate s and each set of three three-dimensional vectors can be
565 convert to a rotation angle φ in the tangent plane of s), then optimized results can be
566 summarized directly.

567 Performance of different methods in real-world implementation

568 The actual stimulation effect of TMS depends not only on the computational
569 optimization of coil placement parameters, but also on whether the coil can be placed
570 accurately according to the optimal parameters on a person's head *in vivo*. Ideally,
571 precise placement can be achieved with a neuronavigation system. However,
572 expensive neuronavigation systems are not always available. If manual measurement
573 can be done quickly and simply while sacrificing little accuracy, it can be practical for
574 clinical settings. According to the definition, each 10-20 point can be measured
575 manually by a sequence of steps, with later measurements dependent on prior
576 measurements. However, multiple measurements and calculations can be excessively
577 time-consuming (e.g., measuring the P4 point can take about 16 minutes as reported

578 in Xiao et al., 2016). In addition, with more measurements comes more opportunity
579 for human error. BeamF3 is a simpler and faster method that was proposed to improve
580 the speed of finding the F3 position for prefrontal coil placement. It simplified the F3
581 position measurement steps to only three skull measurements. However, its
582 transformation formula only works for F3 and cannot be generalized directly to other
583 locations. Mir-Moghtadaei has published a series of articles (Mir-Moghtadaei et al.,
584 2015, 2016, 2017) to establish a scalp heuristic that can transform CDP positions to
585 skull measurement (e.g., 25% Nasion-Inion for locating the dorsomedial prefrontal
586 cortex). It is more precise than the BeamF3 method, as it is based on individuals' MRI
587 scans. However, in cases where MRI scans are not available, the scalp-based heuristic
588 needs an anatomical MRI database and cannot be generalized to other locations.

589 The SGP has obvious advantages in coil placement implementation. In cases
590 where an SGP-based navigation system (navigate to s and φ directly on the scalp, in
591 development) is available, both the individual and group optimal placement can be
592 implemented accurately. For those who do not have an SGP navigation system but
593 have traditional CDP-based neuronavigation systems like BrainSight, we provide an
594 alternative. That is, if the individual's T1 image is available, the SGP individual
595 parameters can be transformed into CDP parameters and used by BrainSight (using
596 the T1 image to sample the scalp mesh and calculate the CDP position and direction
597 vectors corresponding to (s, φ) on the scalp mesh, then using an NDI optical camera
598 to register the mesh in computational space and the person's scalp in the real world,
599 then navigating to the CDP position and direction vectors). In the absence of

600 navigation systems, SGP parameters can also be implemented by manual
601 measurement of s and ϕ . Each scalp placement can be measured independently,
602 therefore providing a very fast (< 5 minute), accurate (73%<5 mm error) and low-cost
603 protocol to realize arbitrary coil placement, which can be especially useful in
604 large-throughput clinical practice.

605 Taken together, the SGP method combines the advantages of the 10-20 method
606 and the CDP method in individual optimization, group synthesis and real-world
607 implementation. When considering these three aspects simultaneously, SGP provides
608 an improved coil placement protocol that can be flexibly applied to different
609 situations.

610 **4.3 Limitation and further directions**

611 Extension of scalp geometry-based parameters

612 The limitations of the SGP are related to its advantages, that is, the SGP is
613 constrained to conventional placements on the scalp. Although conventional
614 placement represents the main coil placement protocol in clinical practice and most
615 optimization studies use conventional placement space as the search space,
616 conventional placement does not include all physically achievable coil placements.
617 For example, the SGP-based parameters do not include a tilt angle from the tangent
618 plane. The hand-held coil placement cannot always be strictly located on the tangent
619 plane and will thus introduce tilt error. Some studies have pointed out that the tilt
620 angle will affect the electric field distribution. So, it may be useful to record the tilt

621 angle for hand-held placement for more accurate modeling and understanding of TMS
622 effects. However, it is difficult to record such an angle without the help of a
623 navigation system, so this remains a practical problem.

624 Another problem is that the current discrete SGP is established by
625 uniform interval sampling of the s and φ parameters. The uniform sampling of s
626 (continuous proportional coordinate) can result in nonuniform Euclidean distances
627 between unit-value coordinates. As shown in Fig.1C, sampling points are sparse
628 around the vertex (inter-point Euclidean distance of about 3.7mm), while much denser
629 around the ears (inter-point Euclidean distance can reach less than 1 mm). If the
630 search space is not near the ears and is in a small area, discrete SGP can be
631 approximately uniform in Euclidean distance; but if the search space is the full head,
632 the equal interval SGP parameter sampling may not be appropriate as it will generate
633 too many points around the ear. An improved discrete sampling based on the
634 Fibonacci lattice method (González, 2010) can help to make the resulting Euclidean
635 distances uniform.

636 Extension of SGP-based coil placement optimization

637 Our preliminary results showed inter-individual differences in optimal placement
638 parameters. This may be a true individual difference: like Balslev (D et al., 2007)
639 reported a range of 63° in optimal orientations across different participants. However,
640 it may depend on the selection of ROI: even in the motor area, the most common
641 optimal orientation varies when targeting different precise locations (Gomez-Tames et
642 al., 2018b). It may also depend on the selection of E-field variables: we used the

643 E-field magnitude (which leads to the same result for φ and $180^\circ-\varphi$); using the
644 perpendicular component and tangential component may lead to significantly
645 different optimal coil placements (Gomez et al., 2021). Our demonstration mainly
646 follows the protocol proposed by Balderston (2020), that chose to maximize the
647 E-field magnitude in the 5-mm ROI centered at the functional activation peak.
648 However, the model for calculating simulated effects needs further refinement, and
649 further studies can explore other optimization strategies to provide a more
650 comprehensive understanding.

651 In addition to optimizing the primary TMS effect in the targeted ROI via electric
652 modeling, we can also optimize based on secondary network effects propagated to
653 distal regions via functional connectivity. For example, we can model anti-depressant
654 effects by calculating the resting-state connectivity between DLPFC and subgACC
655 (Fox et al., 2012; Siddiqi et al., 2020), where more anti-correlated connectivity leads
656 to better efficacy. The electric modeling and functional connectivity modeling can
657 also be combined into one optimization protocol (Balderston et al., 2020).

658 Besides using computational modeling effects to optimize placement, we can also
659 use TMS clinical effects for optimization by continuously recording TMS coil
660 placement and treatment effects in clinical studies and performing a meta-analysis to
661 find placements with better effects. One problem that hinders the synthesis is the
662 inconsistency of recorded descriptions. As reviewed in Lefaucheur et al., 2020, some
663 records use 10-20 descriptions like F3 to report the original scalp location, while
664 others report MNI coordinates, which are line projection results from the original

665 scalp position in CDP space. The SGP is a unified system compatible with different
666 descriptions. It can summarize existing conventional coil placements recorded in
667 various manners by converting them into SGP parameters, regardless of whether the
668 coil positions were described using 10-20 method, 5-cm method or the targeted brain
669 locations obtained from a line projection. Therefore, SGP can provide a standard
670 framework to facilitate synthesis of TMS effects at different positions and orientations
671 from different studies. SGP can be used to map efficacies of different kinds of TMS
672 treatments, like anti-depressant effects, motor evoked potential effects and so on,
673 resulting in disorder-specific coil placement atlases to guide clinical practice.

674 Finally, in addition to describing and optimizing TMS coil placement, SGP is also
675 suitable for other transcranial techniques that place optodes or electrodes on the scalp.
676 For example, SGP can be used to describe and optimize the electrode positions for
677 transcranial direct current stimulation (tDCS).

678 Acknowledgements

679 This work was supported by the National Natural Science Foundation of China (grant
680 no. 82071999 and 61431002). The authors declare no competing financial interests.
681 We thank Ye Xin for the assistance in conducting the experiments.

References

AT, B., R, J., & IL, F. (1985). Non-invasive magnetic stimulation of human motor cortex. *Lancet*
(*London, England*), *1*(8437), 1106–1107. [https://doi.org/10.1016/S0140-6736\(85\)92413-4](https://doi.org/10.1016/S0140-6736(85)92413-4)

Balderston, N. L., Roberts, C., Beydler, E. M., Deng, Z. de, Radman, T., Lubner, B., Lisanby, S. H.,

- Ernst, M., & Grillon, C. (2020). A generalized workflow for conducting electric field-optimized, fMRI-guided, transcranial magnetic stimulation. *Nature Protocols*, *15*(11), 3595–3614. <https://doi.org/10.1038/s41596-020-0387-4>
- Beam, W., Borckardt, J. J., Reeves, S. T., & George, M. S. (2009). An efficient and accurate new method for locating the F3 position for prefrontal TMS applications. *Brain Stimulation*, *2*(1), 50–54. <https://doi.org/10.1016/j.brs.2008.09.006>
- D, B., W, B., C, M., & RC, M. (2007). Inter-individual variability in optimal current direction for transcranial magnetic stimulation of the motor cortex. *Journal of Neuroscience Methods*, *162*(1–2), 309–313. <https://doi.org/10.1016/J.JNEUMETH.2007.01.021>
- Fox, M. D., Buckner, R. L., White, M. P., Greicius, M. D., & Pascual-Leone, A. (2012). Efficacy of transcranial magnetic stimulation targets for depression is related to intrinsic functional connectivity with the subgenual cingulate. *Biological Psychiatry*, *72*(7), 595–603. <https://doi.org/10.1016/j.biopsych.2012.04.028>
- Gomez, L. J., Dannhauer, M., & Peterchev, A. V. (2021). Fast computational optimization of TMS coil placement for individualized electric field targeting. *NeuroImage*, *228*, 117696. <https://doi.org/10.1016/J.NEUROIMAGE.2020.117696>
- Gomez-Tames, J., Hamasaka, A., Hirata, A., Laakso, I., Lu, M., & Ueno, S. (2020). Group-level analysis of induced electric field in deep brain regions by different TMS coils. *Physics in Medicine and Biology*, *65*(2). <https://doi.org/10.1088/1361-6560/AB5E4A>
- Gomez-Tames, J., Hamasaka, A., Laakso, I., Hirata, A., & Ugawa, Y. (2018a). Atlas of optimal coil orientation and position for TMS: A computational study. *Brain Stimulation*. <https://doi.org/10.1016/j.brs.2018.04.011>

- Gomez-Tames, J., Hamasaka, A., Laakso, I., Hirata, A., & Ugawa, Y. (2018b). Atlas of optimal coil orientation and position for TMS: A computational study. *Brain Stimulation*, *11*(4), 839–848.
<https://doi.org/10.1016/j.brs.2018.04.011>
- González, Á. (2010). Measurement of Areas on a Sphere Using Fibonacci and Latitude-Longitude Lattices. *Mathematical Geosciences*, *42*(1), 49–64.
<https://doi.org/10.1007/S11004-009-9257-X>
- Herbsman, T., Avery, D., Ramsey, D., Holtzheimer, P., Wadjik, C., Hardaway, F., Haynor, D., George, M. S., & Nahas, Z. (2009). More Lateral and Anterior Prefrontal Coil Location Is Associated with Better Repetitive Transcranial Magnetic Stimulation Antidepressant Response. *Biological Psychiatry*, *66*(5), 509–515.
<https://doi.org/10.1016/j.biopsych.2009.04.034>
- JASPER, & H., H. (1958). The ten-twenty electrode system of the international federation. *Electroencephalogr. Clin. Neurophysiol.*, *10*, 370–375.
- Jiang, Y., Li, Z., Zhao, Y., Xiao, X., Zhang, W., Sun, P., Yang, Y., & Zhu, C. (2020). Targeting brain functions from the scalp: Transcranial brain atlas based on large-scale fMRI data synthesis. *NeuroImage*, *210*, 116550. <https://doi.org/10.1016/J.NEUROIMAGE.2020.116550>
- Lefaucheur, J. P., Aleman, A., Baeken, C., Benninger, D. H., Brunelin, J., di Lazzaro, V., Filipović, S. R., Grefkes, C., Hasan, A., Hummel, F. C., Jääskeläinen, S. K., Langguth, B., Leocani, L., Londero, A., Nardone, R., Nguyen, J. P., Nyffeler, T., Oliveira-Maia, A. J., Oliviero, A., ... Ziemann, U. (2020). Evidence-based guidelines on the therapeutic use of repetitive transcranial magnetic stimulation (rTMS): An update (2014–2018). In *Clinical Neurophysiology* (Vol. 131, Issue 2, pp. 474–528). Elsevier Ireland Ltd.

<https://doi.org/10.1016/j.clinph.2019.11.002>

Milnik, V. (2009). Anleitung zur Elektrodenplatzierung des internationalen 10–20-Systems. *Das*

Neurophysiologie-Labor, 31(1), 1–35. <https://doi.org/10.1016/J.NEULAB.2008.12.002>

Mir-Moghtadaei, A., Caballero, R., Fried, P., Fox, M. D., Lee, K., Giacobbe, P., Daskalakis, Z. J.,

Blumberger, D. M., & Downar, J. (2015). Concordance Between BeamF3 and

MRI-neuronavigated Target Sites for Repetitive Transcranial Magnetic Stimulation of the

Left Dorsolateral Prefrontal Cortex. *Brain Stimulation*, 8(5), 965–973.

<https://doi.org/10.1016/J.BRS.2015.05.008>

Mir-Moghtadaei, A., Dunlop, K., Mansouri, F., Giacobbe, P., Kennedy, S. H., Lam, R. H.,

Vila-Rodriguez, F., Daskalakis, Z. J., Blumberger, D. M., & Downar, J. (2017). Scalp-based

heuristics for locating the nodes of the salience network for use in neurostimulation. *Brain*

Stimulation: Basic, Translational, and Clinical Research in Neuromodulation, 10(2), 479.

<https://doi.org/10.1016/J.BRS.2017.01.404>

Mir-Moghtadaei, A., Giacobbe, P., Daskalakis, Z. J., Blumberger, D. M., & Downar, J. (2016).

Validation of a 25% Nasion–Inion Heuristic for Locating the Dorsomedial Prefrontal Cortex

for Repetitive Transcranial Magnetic Stimulation. *Brain Stimulation: Basic, Translational,*

and Clinical Research in Neuromodulation, 9(5), 793–795.

<https://doi.org/10.1016/J.BRS.2016.05.010>

Nielsen, J. D., Madsen, K. H., Puonti, O., Siebner, H. R., Bauer, C., Madsen, C. G., Saturnino, G. B.,

& Thielscher, A. (2018). Automatic skull segmentation from MR images for realistic volume

conductor models of the head: Assessment of the state-of-the-art. *NeuroImage*, 174, 587–598.

<https://doi.org/10.1016/J.NEUROIMAGE.2018.03.001>

- Opitz, A., Legon, W., Rowlands, A., Bickel, W. K., Paulus, W., & Tyler, W. J. (2013). Physiological observations validate finite element models for estimating subject-specific electric field distributions induced by transcranial magnetic stimulation of the human motor cortex. *NeuroImage*, *81*, 253–264. <https://doi.org/10.1016/j.neuroimage.2013.04.067>
- Saturnino, G. B., Puonti, O., Nielsen, J. D., Antonenko, D., Madsen, K. H., & Thielscher, A. (2019). SimNIBS 2.1: A Comprehensive Pipeline for Individualized Electric Field Modelling for Transcranial Brain Stimulation. *Brain and Human Body Modeling*, 3–25. https://doi.org/10.1007/978-3-030-21293-3_1
- Siddiqi, S. H., Taylor, S. F., Cooke, D., Pascual-Leone, A., George, M. S., & Fox, M. D. (2020). Distinct Symptom-Specific Treatment Targets for Circuit-Based Neuromodulation. *Https://Doi.Org/10.1176/Appi.Ajp.2019.19090915*, *177*(5), 435–446. <https://doi.org/10.1176/APPI.AJP.2019.19090915>
- Tarapore, P. E., Findlay, A. M., Honma, S. M., Mizuiru, D., Houde, J. F., Berger, M. S., & Nagarajan, S. S. (2013). Language mapping with navigated repetitive TMS: Proof of technique and validation. *NeuroImage*, *82*, 260–272. <https://doi.org/10.1016/j.neuroimage.2013.05.018>
- Trapp, N. T., Bruss, J., King Johnson, M., Uitermarkt, B. D., Garrett, L., Heinzerling, A., Wu, C., Kosciak, T. R., ten Eyck, P., & Boes, A. D. (2020). Reliability of targeting methods in TMS for depression: Beam F3 vs. 5.5 cm. *Brain Stimulation*, *13*(3), 578–581. <https://doi.org/10.1016/j.brs.2020.01.010>
- Tsuzuki, D., Jurcak, V., Singh, A. K., Okamoto, M., Watanabe, E., & Dan, I. (2007). Virtual spatial registration of stand-alone fNIRS data to MNI space. *NeuroImage*, *34*(4), 1506–1518. <https://doi.org/10.1016/J.NEUROIMAGE.2006.10.043>

Vaghefi, E., Cai, P., Fang, F., Byblow, W. D., Stinear, C. M., & Thompson, B. (2015). MRI guided brain stimulation without the use of a neuronavigation system. *BioMed Research International*, 2015. <https://doi.org/10.1155/2015/647510>

Weise, K., Numssen, O., Thielscher, A., Hartwigsen, G., & Knösche, T. R. (2020). A novel approach to localize cortical TMS effects. *NeuroImage*, 209(March 2019). <https://doi.org/10.1016/j.neuroimage.2019.116486>

Xiao, X., Zhu, H., Liu, W.-J., Yu, X.-T., Duan, L., Li, Z., & Zhu, C.-Z. (2017). Semi-automatic 10/20 Identification Method for MRI-Free Probe Placement in Transcranial Brain Mapping Techniques. *Frontiers in Neuroscience*, 11(Pt 1), 105–111.