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Introducing CARATE: Finally speaking chemistry through learning hidden wave function representations on graph attention and convolutional neural networks†

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Computer-Aided Drug Design is advancing to a new era. Recent developments in statistical modelling, including *Deep Learning*, *Machine Learning* and high throughput simulations, enable workflows and deductions not achievable 20 years ago. The key interaction for many small molecules in the context of medicinal chemistry is via bio-molecules. The interaction between a small molecule and a biological system therefore manifests itself at multiple time and length scales. While the human chemist quite intuitively grasps the concept of multiple scales, most of the computer technologies do not relate multiple scales easily.

Numerous methods try to tackle multiple scales in the realm of computational sciences have been developed. However, up to now it was not clear that the problem of multiple scales is not only a mere matter of computational abilities but even more a matter of accurate representation. Current representations of chemicals lack the descriptiveness necessary for modern modelling questions.

This work introduces a novel representation of small and large molecules. The representation is obtained by the *biochemical and pharmaceutical encoder* (CARATE). Furthermore, the regression and classification abilities of the learned representation by CARATE are evaluated against benchmarking datasets (ZINC, ALCHEMY, MCF-7, MOLT-4, YEAST, Enzymes, Proteins) and compared to other baseline approaches. CARATE outperforms on classification tasks of large biomolecules as well as on quantum chemical regression tasks of small molecules. .

1 Introduction

The wish to accurately predict the outcome of a drug development process is as old as the regulated pharmaceutical industry itself. However, the task of simulating a drug interaction in the body is a multiscale problem operating on many scales.

Up to now, no accurate method has been found to model the whole life cycle of an API inside a mammal. The work on multiscale problems focuses on different aspects of the systems at multiple scales and tries to represent the important aspects of a particular scale accurately by the means of that particular scale. The simulator decides on unimportant parts of a scale and approximates them more efficiently with methods of a larger scale[1].

The problem of multiple scales shows us that our theories do not handle the concept of multiple scales well enough for our computational abilities, such that each multiscale modelling is doomed using our technology alongside our current state of theoretical physics describing the dynamics of the system.

Because of the amount of already performed simulations at various scales, deep learning (DL) becomes a viable approach to speed up computations by approximating simulations in a data-driven way.

Yet, the current representation of chemicals (SMILES, InChI and Lewis-like structures) can't be suitable for modelling because they are in themselves abstractions.

Even worse, the original SMILES algorithm was claimed to be unique[2], but was proven to be non-unique later.[3] It is impossible for fingerprints and SMILES strings to represent a wave function properly and thus methods using these representations are doomed to fail.

The recent surge in application of SMILES for use in DL[4–9] leaves doubts on the applicability of the derived models. On the contrary, large matrix representations are mostly not accurate while being resource intense[10].

To accurately approximate the physical (simulated) properties of a given compound, a more accurate, uniform representation is mandatory.

When different length and time scales are involved, computational expensive methods for the small length scale may become infeasible. For example, to model the interaction of a small molecule with a receptor, one needs to combine quantum chem-

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† Electronic Supplementary Information (ESI) available: [https://codeberg.org/sail.black/carate].

istry (QC) with classical molecular mechanics (MM) at the moment.

The computations performed by the QM/MM approximation still have the QC calculations as a bottleneck. However, recent advances in DL make the prediction of a particular simulation scale accessible[11,12]. Recent prediction of quantum chemical properties with deep learning methods became accurate[13] leading to MD simulations using learned coupled-cluster potentials[14].

Implicit methods might thus solve the equation much more efficiently and accurately.

To speed up the computation, of a QM/MM simulations, the QC computations should be approximated by predicting the desired properties via machine learning methods[15].

There are several exceptional graph-neural networks reported on the Proteins and Enzymes dataset that gained good scores[16–18]. The most prominent ones are hierarchical structure methods employing convolutional layers as well as message passing layers[19,20].

The clustering methods were achieving high accuracies on the PROTEINS and ENZYMES data set (no test set), and high accuracies on the QM family were reported[20].

For example, *Chen et al.* report a similar algorithm to CARATE developed during the same time, but omit results on large datasets, which they used to pretrain their algorithm[9].

Moreover, there is a report of a hyperparameter scan for meta learning graph models that shows a good fitting of the PROTEINS dataset of 73.8 %[21]. Yet, the performance does not seem to be satisfactory.

Also, in the original GAT paper, the authors did not fit the algorithm on either of the ENZYMES or PROTEINS datasets but achieved good results on the protein-interaction dataset (PPI)[22]. The PPI data set, however, is minimal and may not be representative for any fitting behavior.

Yet, graph-based methods do not reach the accuracy necessary for accurate simulation because all methods neglect self-interaction, a foundational quantum mechanical principle.

Either the graph-based algorithm ignores self-interaction, or the given input neglects self-interaction.

The current graph-based methods thus lead to an already flawed ground truth and are doomed to fail.

Therefore, most methods have in common that they try to incorporate quantum chemical principles but are missing the self interaction terms.

Presently, it is barely possible to perform simulations of decent size and complexity on edge devices or personal computers. Typically, the equipment involved consists of a couple of nodes on a high-performance cluster. Only insiders can access high-performance clusters, giving rise to a more and more arcane elite.

A novel method equipped with outstanding algorithms may lead to a new era of edge simulations to enable scientists and accelerate as well as democratize progress in the natural and life sciences.

Up to now, however, to the best of my knowledge, no algorithm with short training times and competitive prediction abilities has been reported.

This work investigates if deep learning methods can be exploited to solve the time independent Schrödinger equation instead of bypassing it via predictions. The working idea is to use molecular graphs, encode them into a wave-function and decode them subsequently such that the eigenvalue equation 2 is solved.

Under the hood, molecular graphs are adjacency matrices that can be equipped with more features through multiple annotation matrices, such that the graph representation carries much more information than plain SMILES strings.

The problem then looks similar to a classical deep learning method, framing the families of the eigenvalue problems described in 4 as a problem that can be tackled via deep learning.

This work aims to close the gap by providing a robust method that makes sure, that both, the representation, the neural-network, and the training process obey quantum physical principles.

2 Related Work

Predicting physical properties of chemical compounds with statistical methods is indeed a well-known topic in the literature. Recent work comparing the representations of molecules for the QM-9 prediction performance of a feed forward neural network (FNN) indeed showed that the quality of predictions of physical properties highly depends upon the molecular representation[23].

The recent advances in natural language processing (NLP) introduced by the self attention mechanism in bidirectional auto encoders[24] showed that respective algorithms (BERT technology) can learn semantic properties of the input[25]. Especially, the BERT algorithm has abilities to organize and structure information[26].

Because molecular descriptors can be learned in a data-driven way[27] the self-attention mechanism made room for innovation around self-attention deep neural networks in computational chemistry working on the SMILES or similar text representations of molecules with good classification and regression results[28].

Indeed, semi-empirical potentials are well-known to the community of computational chemists. Especially, the extended-tight-binding methods are fitted in a statistical manner from a large set of molecules and celebrate a huge success[29].

Thus, to the community, it does not seem to be relevant why something works as long as it works. In contrast to most semiemprical potentials, deep-learning methods offer explainability through dedicated algorithms such as LRP[30] and others.

A fundamentally different, yet equally promising approach to a text-based encoding is to use numerical representations such as fingerprints, substructures, or graphs. Indeed, there is a recent study investigating the potential of unified fingerprints for small and biomolecules[31].

However, one-shot-learning based on self-attention LSTM with encoded molecular graphs as inputs showed more decent results[32].

Many approaches to model the molecular structure with graph neural networks (GNNs) have been applied. To increase computational efficiency, a self-attention mechanism has been rudimentary applied to graph convolutional networks as well (GCNs)[28].

In 2017, the group around *Schütt et al.* proposed *SchNet* and their benchmark dataset *ISO17*[33]. The key improvement

in *SchNet* was to get hold of the molecular geometry as a graph while using convolutions to craft weighted feature importance in the molecule.

Another way to achieve better structure recognition is to apply message passing networks[34]. Moreover, multi-headed self attention has been applied to GNN encoded molecular structures through a self attention mechanism[35].

This work completes the series on the application of attention-based algorithms to chemical problems. This work investigates a multi-headed graph self-attention model (GAT)[22] with graph-convolutions as an encoder for chemical classification and regression tasks, with significant results.

Chen et al. introduced the idea of bidirectional transformers to chemistry on graphs. Yet, they still work on SMILES and did also not publish their results on large benchmark datasets[9]. The idea of obtaining a better representation through graph-deep learning is becoming more and more popular, however many chemists are still working on SMILES representations[20].

3 Theoretical Part

For quantum chemistry at any scale, we want to solve the time-dependent Schrödinger equation when considered with the dynamic behavior of the system.

$$H\Psi(r,t) = E\Psi(r,t) \tag{1}$$

As elaborated above, one of the working hypotheses is that the current machine learning methods, including modern deep learning methods, mostly do only bypass the time-independent Schrödinger equation by making predictions.

$$H\Psi(r) = E\Psi(r) \tag{2}$$

But what does it mean to solve the equation 2? We are generally interested in finding eigenvalues and eigenfunctions of a system for a particular operator (in this case, the Hamiltonian). Very often, only the eigenvalues are of interest.

The solution to the time-dependent part of equation 1 is, however, rather simple. First one starts by separating the variables

$$\Psi(r,t) = \Xi(t)\Psi(r) \tag{3}$$

And then solve for the positional part and the time-dependent part separately. The time-dependent part has standard solutions that have an analytical expression.

The time-independent part, however, has solutions that are not solvable by analytical means for many electron systems. The only way to solve for the time-independent part of the Schrödinger equation is thus numerically.

The accuracy of each method for solving equation 2 is thus theoretically bounded by the hardware limits of the machine performing the calculations.

The more interesting problem is to solve the time-dependent Schrödinger equation. Once the TISE is solved, the dynamics can be computed efficiently.

Solving the TISE with deep learning is not a new idea and prominent on tech blogs since 2017[36]. The article by *Steinke* provides a first hint that the problem is tractable with neural networks.

In the academic literature, the topic occurs in some volume a little bit later[37–40]. However, the methods presented by the authors differ from this paper fundamentally by explicitly incorporating the flaws and approximations classical quantum chemistry must make by design.

The key innovation in algorithms exploiting deep learning is not backpropagation, but is the automatic differentiation (AD). It has been shown that AD can be exploited to tackle quantum chemical calculations because with AD by optimizing basis sets in the Hartree-Fock scheme[41]. Moreover, applying physical regularizers were shown to be beneficial in modelling wave-functions via backpropagation[42].

The approximations and flaws include the Born-Oppenheimer-Approximation (BOA), using Kohn-Scham density functional instead of wave-functions, and the approximation of the wave-function as an expansion of an infinite basis set.

The standard expansion of the wave function into atomistic basis functions needs numerous determinant calculations (Slater Determinants) and are thus lengthy to perform. The self-critical comments on FermiNet conclude that the scalability of FermiNet might not be exactly useful for practical quantum chemistry[37].

Moreover, most authors ignore that most quantum chemical methods, including the coupled-cluster methods, rely on the Hartree-Fock optimized basis sets as their starting point.

In the end, all quantum chemical methods want to solve the eigenvalue equation 2. It is thus mathematically always the same problem, just the direction from which it is tackled differs.

The creativity in problem-solving comes thus from solving the general equation for arbitrary observables

$$\lambda = \frac{\langle \Psi(r)|A|\Psi(r)\rangle}{\langle \Psi(r)|\Psi(r)\rangle} \tag{4}$$

In most cases, chemists are not interested in the wave-function or how it has been constructed and an explicit calculation might not always be necessary.

It might even lead to misleading concepts that chemists then apply in other disciplines without having any means of critically thinking about the applied models.

For example, the orbital concept is a simplification that comes from the aforementioned approximations made by theoretical chemists and was made popular during the 20th century in the western community, especially, by Linus Pauling.

Most ironically, Linus Pauling also introduced the construction of arbitrary wave functions through combining atomistic wave functions into hybrid orbitals (molecular orbitals) using group theory in his valence bond theory.

Today, most (quantum) chemistry is building on this idea. The general quantum chemical calculation is built up through calculating better wave functions obtained from simpler wave functions. The order of building the wave function starts from atomic orbitals (AO), and goes over molecular orbitals (MOs), Slater de-

terminants (SD) and finally many-electron wave functions (ME).

$$\chi \rightarrow \phi \rightarrow \Phi \rightarrow \Psi \tag{5}$$

$$\text{AO} \rightarrow \text{MO} \rightarrow \text{SD} \rightarrow \text{ME}$$

Starting from the idea of constructing hybrid wave functions, it is not far off taking other features and combining them into even more sophisticated wave functions that are then combined in to a system-wide wave function.

The concept of constructing a wholistic wave function directly from diverse input features or smaller wave functions inherently explored in this work by applying the CARATE algorithm to the datasets Alchemy and Zinc. Both datasets, Alchemy and Zinc, have a diverse set of features.

Thus, this works aims to construct Ψ directly from the annotated molecular graph taking the annotated graph nodes and edges as building blocks for the wavefunction Ψ.

Thereby, the new method CARATE shall skip at least two steps in equation 5 and be independent of the BOA.

The new method CARATE does not rely on Euclidean coordinates and thus operates in another space than the Euclidean space. The method does not rely on Hartree-Fock calculations but uses the variational principle by default.

4 Methods

The whole code was forged into a framework called CARATE and moved later to a package called *aiarc*. Both packages are open source and available on Codeberg a German association for the advancement of open-source software (`https://codeberg.org/sail.black/carate`). The package can be obtained via PyPi and pip, too (`https://pypi.org/project/carate/`).

The package contains a documentation hosted on readthedocs.io as well as notebooks providing the analysis of the training trajectories and some tutorials on how to start a run from a notebook.

The configuration files are provided as supporting information, as well as extra plots, trajectories, log files, and trained models. The reader is referred to the codeberg of the package to obtain the supporting information.

Also, the QM9 dataset was omitted because the proof of concept solving the problem presented by QM9 was already tackled via the ALCHEMY dataset. The ALCHEMY dataset even presents a more difficult task, as there are more heavy atoms per molecule on average than in the QM9 dataset.

For the reader with historical interest, the notebooks containing the first experiments are also published (`https://codeberg.org/cap_jmk/carate-notebooks`)

In general, the training on GPU is slightly faster, the CPU was chosen as the reference chip. The accuracy of the model is sometimes slightly lower and less reproducible across different CUDA versions and GPUs at different times.

For the presented work, an AMD Ryzen 9 7950X processor at 4,5 GHz and 64 MB L3-Cache alongside 64 GB of RAM were used on a Debian 12 Bookworm system.

Different systems were tested during the development and all

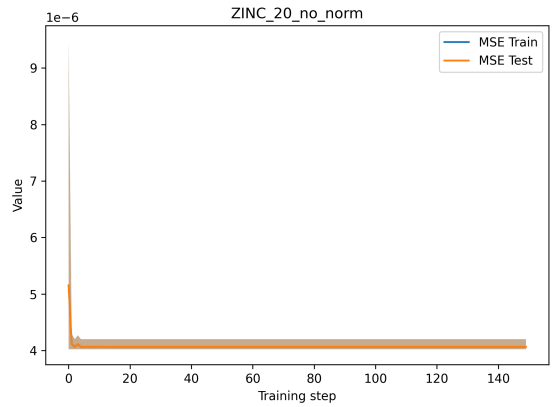

Fig. 1 Accuracy trajectories for both training and test sets for $n = 5000$ training steps on the ZINC dataset (bottom).

produced the same results. Among the tested systems were Ubuntu 20.04, 22.04, Debian 11, EndeavorOS, and Debian 12. The algorithms were reproducible on all of them. Thus, both the Arch Linux and common Debian distributions are suitable for modelling tasks associated with the package.

Both methods, regression and classification, use the basic encoder structure and apply specific architectures on top of the encoder structure for each specific task. For classification, the outputs of the encoder were transformed into logits using a sigmoid function. For regression, a linear layer was stacked on top of the encoder structure.

The training was performed in batches with no cross validation to model the low data regime within a multiscale simulation properly.

To test the classification abilities of the model we tested it against the drug discovery datasets for small molecules YEAST, MOLT-4, MCF-7 obtained from the TUDataset without any further preparation (Table 2).

To test the performance on protein graphs, the ENZYMES and PROTEINS datasets were chosen. The datasets were obtained from the TUDataset using the PytorchGeometric API without any further preparation.

For each example, five-fold stratified cross-validation for statistical significance of the results was performed.

The datasets were obtained from TUDataset[43], and MoleculeNet[44] through the PyTorchGeometric API[45]. Each dataset was used as is, to see how CARATE performs on raw data. The only preprocessing applied was rescaling to the target's unit, as would be done during a simulation.

If the data set was given in SMILES format, the SMILES format was converted to a molecular graph representation implemented in PytorchGeometric[45].

All GAT and GNN implementations were applied from or achieved with the PytorchGeometric[45] library. Other deep learning building blocks were implemented using the PyTorch[46] and Numpy[47] library.

The CARATE network consists of an input layer consisting of a GCN and GAT layer. To use the encoder in regression and classification tasks, another GCN layer followed by task-specific layers

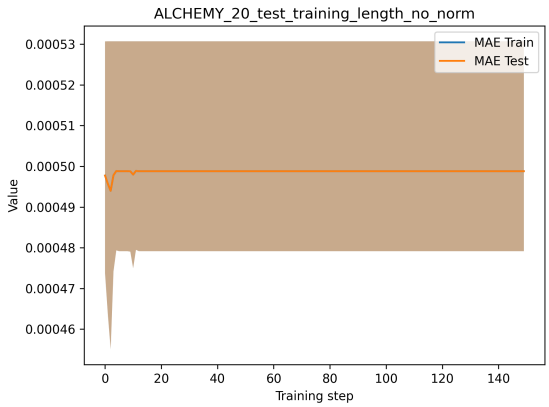

Fig. 2 Accuracy trajectories for both training and test sets for $n = 5000$ training steps on the ALCHEMY dataset.

are added to the stack (compare Figure 3)

To test the encoding to property prediction, the encoder-predictor model was tested against physical regression tasks on the ALCHEMY[48] and ZINC data sets obtained from TUDatasets[43].

For each task, no more than 150 training iterations are necessary for a good convergence. The convergence is thus quite fast.

In fact, early stopping was beneficial in most cases, such that longer training results may lead to less accurate results, especially for the classification tasks. The described degradation of the convergence behavior indicates that the algorithm is prone to overfitting.

The architecture for the regression tasks differs from the classification to obtain multitask regression results, instead of multitask classification only by the output function applied to the network.

The results are compared to GIN-ε[43,49].The GINE-ε network uses batch normalization as well as zero mean and unit variance normalization.

Table 1 Regression performance compared to baseline GINE-ε[43].

Method	ZINC	ALCHEMY
CARATE	0.0016 ± 0.0002	0.00050 ± 0.00005
GINE-ε[43]	0.084	0.103

5 Results

For the small-molecule regression tasks consisting of the ZINC and the ALCHEMY dataset, the training converged after less than 10 epochs (usually two epochs) up to numerical accuracies (table 1. There is a slight dependence on the train-test-split (figures 1,2).

The protein classification tasks consisting of the ENZYMES and PROTEINS datasets showed exceptional results that outperformed all reported benchmarks (table 2).

On both protein classification tasks, ENZYMES, and PROTEINS, CARATE provides best of class fits, with accuracies up to 100 % on certain splits (compare figures5, 6). The algorithm was prone to slight overfitting on both datasets.

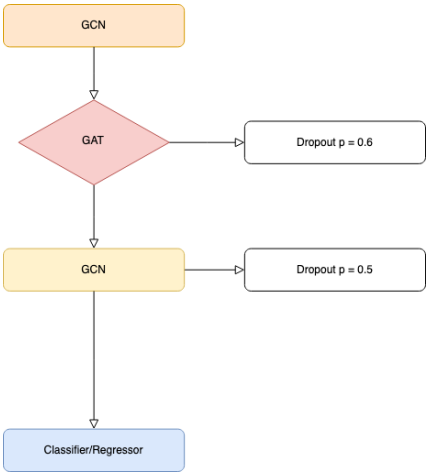

Fig. 3 General architecture of the CARATE network used for classification and regression tasks.

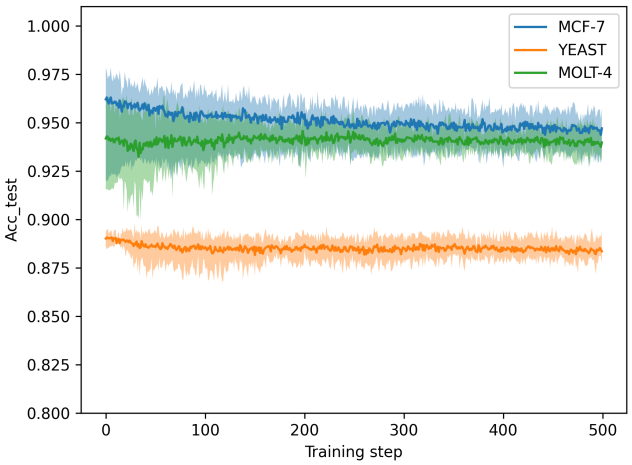

Fig. 4 Trajectory of the training accuracy using the datasets MCF-7, MOLT-4, and YEAST

Table 2 Classification performance of CARATE as compared to other state of the art GNNs and kernel classifiers.

Method	MCF-7	MOLT-4	YEAST	Enzymes	Proteins
CARATE	97 ± 2	95.4 ± 0.9	89.4 ± 0.4	95 ± 9	92 ± 9
1-WL	94.5	94.6	89.2	50.8	72.6
WL-OA	-	-	88.2	56.4	73.4
GR	91.7	92.1	88.2	29.5	71.6
SP	91.7	92.1	88.3	39.3	75.6
GIN-e	92	92.4	88.3	38.7	72.2
GIN-e-JK	91.8	92.2	88.2	39.3	72.2

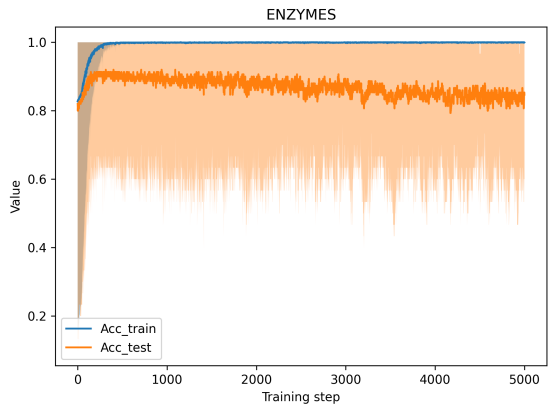

Fig. 5 Accuracy trajectories for both training and test sets for $n = 5000$ training steps on the ENZYMES dataset.

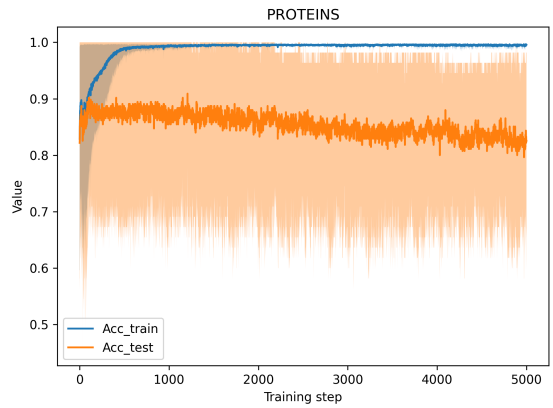

Fig. 6 Accuracy trajectories for both training and test sets for $n = 5000$ training steps on the PROTEINS dataset.

6 Discussion

The aim of efficiently learning a decent molecular to property representation from a dataset has been achieved. The proposed architecture can be applied to small and large biomolecules alike with satisfying results. The CARATE encoder enables multi-class classification and regression tasks.

Moreover, the multi-headed self-attention mechanism allows efficient learning and prediction in low data regimes. Besides, the CARATE algorithm may detect flawed data in given data sets or uncover statistically unrelated data, thus giving hints on where to improve the quality of the data in a data lake.

On the contrary, in the highly distorted data regime, the CARATE algorithm may be inferior to classical methods based on supported vector machines or random forest classifiers. The behavior, however, is expected, as GAT units are inserted flexibly to detect chemical patterns.

If the important pattern is not well represented in the data set, the attention mechanism may forget the pattern due to the dropout probability of 0.6. To overcome this issue, highly distorted data sets can be modelled by adjusting the learning or dropout rate and training for more epochs and achieve similar to or better than baseline results.

In fact, the performance of the algorithm might as well be increased by modifying the architecture in subsequent work via adjusting the network stack, using batch-normalization or a slightly different dropout-rate or dropout localization.

ALCHEMY is a multitasking method, and ZINC only predicts a single class problem. Thus, the method generalizes to many operator problems from equation 7.

The MAE is used in the general Hartree-Fock scheme, making it a physically sound metric.

7 Conclusions

The accurate results on quantum chemical datasets indicate that the algorithm is learning a wave function ψ to solve the Schrödinger equation via the last regression layer such that the general Eigenvalue equation

$$\hat{A}\Psi = \lambda\Psi \tag{6}$$

can be applied to understand the calculation. When considered with multitask problems, the network solves

$$\hat{A}_i\Psi = \lambda_i\Psi \tag{7}$$

The experiments indicate that A_i can be a non-linear operator, as the activation function is the LEAKY-RELU function for the GAT units[22].

Thus, the network solves the generalized form of equation 2. The high accuracy for most of the classification and regression tasks suggests that the multi head GAT units are decent encoders for molecular structures.

When considering the initial motivation of solving the eigenvalue problem of an operated acting on a wave function, we must conclude that the encoding of the molecule through the CARATE unit represents indeed a wave function and the operator acting on the wave function is represented by the final classification or

regression layer of the network.

The principle must by definition be self-replicating such that one can add layer after layer and would still satisfy the eigenvalue equations.

Especially, if presented with a descriptive data regime, CARATE shows low training times while achieving high accuracies for biomolecules and small molecules alike.

The idea of CARATE is similar to the SchNet[33] but incorporating a self-interaction term such that high accuracies can be achieved. By incorporating more physical knowledge into the model, the encoding was framed as a Markov graph in the wider sense.

Even though there is a high dropout probability and one dropout layer is stacked as the last layer, accuracies are high.

On the other hand, it is known that large neural networks can model implicit attention[50], and thus the explicit attention mechanism models the investigated problems sufficiently. By modelling the mutli-headed self-attention explicitly, the algorithm becomes intentionally more accurate and efficient.

Simulations utilizing CARATE seem promising. However, to verify the results, in later studies more experiments are necessary. It would be interesting how CARATE performs classification on larger datasets of biomolecules and small molecules because the fitting abilities of the proposed algorithm appear to be very high on large datasets such as ZINC and ALCHEMY.

In a recent master's thesis, the construction of extremely detailed wave-functions via random forests to solve a multi-scales problem of biodegradability was investigated successfully, leading to high calculation accuracies[51].

The GAT layer uses masked attention[22] such that at least two training epochs are needed for the numerical fit. The masked attention mechanism is actually similar to the convolutional mechanism, such that only the direct neighbors are relevant for the attention mechanism.

The attention mechanism is a message-passing mechanism and the message needs to propagate at least once. On small molecules the fit is thus fast and fitted after mostly two epochs.

For larger graphs such as the ENZYMES and PROTEINS dataset, the message needs to travel longer and thus the training takes more iterations.

The interesting fitting behavior gives a first intuition into the similarity of dynamic simulations and the training of deep-learning algorithms on molecular graphs.

The fitting behavior also suggests that the algorithm is coarse-graining by default and coarse graining dynamically, as CARATE can fit data sets of both large graphs and small molecular graphs with high accuracies.

Thus, CARATE is behaving scale-invariant and shows fractal behavior, as the algorithm can act on any graph across multiple scales simultaneously, incorporating self-similarity by default. The algorithm may thus have mathematical connections to Rado graphs or fractal graphs in general.

The CARATE graph-based algorithm does not rely on the BOA or other approximations and can fit experimental data to high accuracies, too. Thus, the method of using wave-functions that are neural network encodings of molecular graphs are superior to classical *ab initio* methods, as the BOA finds its limits already at diatomic transition metal fluorides[52].

The wave function is not encoded in the Euclidean space and does not rely on atomic coordinates. This is an interesting approach, but it gets rid of the BOA by design.

It remains an open question if the experimental data from the small compound datasets (MCF-7, YEAST, MOLT-4) are noisy and CARATE correctly misclassifies given samples. However, experiments with wave functions obtained from random forests suggest that it is possible to identify mislabeled data points in experimental data sets[51].

In the end, models should be derived from experimental values rather than theoretical considerations, such that new theories and models derived from CARATE or similar algorithms trained on experimental data of high quality may give new insights into the theoretical foundations of chemistry.

To summarize, the key qualities of the developed software and algorithms are:

- The algorithm fits up to numerical accuracy on the ZINC and ALCHEMY tasks.
- The algorithm shows best of class fits even after two years for classification problems Proteins and Enzymes up to 100% accuracy on certain splits
- The software can run on edge devices
- The algorithm has low training times
- The algorithm is explainable on the basic theoretical level. Further through the theoretical foundations, it has been discussed that too much explainability might hurt the creativity of a chemist.
- The software does not require expert knowledge.
- The software produces reproducible algorithms.

8 Outlook

Based on the accurate regression results, the GNC-GAT encoding enables the subsequently stacked layers to model a given, well-described problem accurately.

Considering the success of the general theoretical mindset presented in this work, a more in depth-study about the theoretical implications of the described mathematical relations is mandatory to derive a more solid theoretical framework.

The study is being prepared under the working title *Understanding chemistry through explaining quantum chemical calculations from graph-neural networks*.

This future work aims to use methods from the community of explainable AI, to understand the theoretical foundation of the superior fitting behavior of CARATE.

Future work will also focus on applying CARATE to multi-scale simulation problems, many class multitask learning, transfer learning[22], and flawed or fraudulent data detection in chemical data sets.

It is also interesting how CARATE and derived algorithms perform on excited state dynamics, as this paper shows that CARATE

does not rely on the BOA as a mandatory approximation. Therefore, CARATE could bypass the current limitations of excited state dynamics introduced by methods of state-of-the-art quantum chemical methods. It would also be interesting how CARATE performs compared to multi reference methods.

Conflicts of interest

There are no conflicts to declare. Though for researching the patent system, a patent was filed in 2021 in the US. The patent was removed in 2023 by their government and would have required refiling. The author refused to refile the patent, as he did not believe in patents anyway.

The work was entirely funded with private funds of the author that were obtained through working in food delivery jobs.

It is also worthy to note that some censorship happened, and some actors tried to suppress the research presented in this article in different ways.

The author was cut off academic resources, raw data vanished from different infrastructures, the author was threatened and denied funding as well as publishing opportunities in the first two years after the first experiment.

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Special thanks go to my family and friends, the Berlin AI/ML community - especially to all members of BLISS e.V. - and my mentors at the different universities, companies, and research institutes in Berlin.

Without you, I would not be where I am today. Also, the paper would not have advanced to this stage. The work started as a small project. Still, the potential to improve the current way of doing quantum chemistry presented itself early during the first experiments.

The more time passed, the more work was done to finally prove more related theorems through different approaches. Thus, I want to thank especially Prof. Wolber, Katrin Denziger, Dr. Amsel, and Prof. Kümmerer for their support of the related Master projects. During the master projects, I had more time to study other perspectives on the relationship of deep learning and quantum physics.

This work needed a lot of reflection and questioning, even though the results were clear right from the beginning.

During this time, the software advanced to a reproducible state and the paper is more complete than the first preprint I wrote back 2021.

The context for making sense of the results happened through many projects and was frozen by publishing as much of my research as possible, even though it is mostly in preprint stage or using other formats than classical research papers. You can refer to my Research Gate profile to obtain the documents.

A distortion might happen easily and especially during mid-2022 through 2023, a lot of research in the wider academic circle of mine was influenced and took influence through dialogues and discussions.

The whole theoretical and scientific implications of solving the eigenvalue problem related to wave functions via DL were not understood, neither was the relation to wave mechanics clear to the community at the point of the first experiments of this work.

This has many reasons, and one of them for sure is the ongoing censorship of the works related to chemistry and graph neural networks. Plenty of publications were only available on preprint servers, and one may assume the articles ran into the same problems.

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