Mice regulate their attentional intensity and arousal to exploit increases in task utility

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ABSTRACT

To meet their survival needs, organisms must continuously select which sensory stimuli to attend to and decide how much attention to pay. Attention's selective aspect has been a cornerstone of behavioral and physiological study, whereas attentional intensity is poorly understood. Autonomic arousal is thought to strongly influence attentional intensity, but evidence is lacking, including regarding if and how organisms self-regulate their arousal to match attentional intensity to its utility. Here, we developed an auditory attentional intensity task for head-fixed mice and vary task utility by changing reward size. We record pupil size and walking speed as proxies of arousal and exploration, respectively. Using simple performance metrics and sequential sampling modeling, we find that mice increase their attentional intensity during periods of high task utility. The utility-related attentional boost is partially mediated by stabilization of pupil-linked arousal around an optimal mid-sized level, and an associated reduction in exploratory behavior. In sum, self-regulation of arousal partially implements strategic attentional intensity allocation.

INTRODUCTION

Attention is limited in capacity and costly to utilize. Therefore, organisms are driven by ongoing behavioral incentives to choose *which* stimuli to attend to, and *how much* to attend to them. Daniel Kahneman termed these the selective and intensive aspects of attention, respectively (Kahneman, 1973). Characterizing the selective aspect of attention has been a cornerstone of systems neuroscience (Carrasco, 2011; Fritz et al., 2007; Maunsell & Treue, 2006). However, attentional intensity has received comparatively little scrutiny. Recent work emphasizes the importance of motivational factors in driving attentional intensity (Brehm & Self, 1989; Ghosh & Maunsell, 2021; Kurzban et al., 2013; Richter et al., 2016; Sarter et al., 2006; Shenhav et al., 2013). This emphasis is in line with the common experience of "paying more attention" when motivated

to perform better, for example in a classroom setting when the instructor indicates the next section will be on the exam.

Manipulation of task utility in perceptual decision-making tasks is a powerful approach to study attentional intensity. Since expectation of reward is a strong motivator (Roesch & Olson, 2004; Schultz, 2000), changes in task utility should lead to matched changes in attentional intensity. In conventional task designs, signal detection-theoretic sensitivity provides a readout of attentional intensity. In line with these ideas, heightened reward expectation increases perceptual sensitivity (Engelmann & Pessoa, 2014; Ghosh & Maunsell, 2021) and reduces reaction times (Locke & Braver, 2008) in humans and non-human primates. Rodents can match their rate of learning to the statistics of a dynamic environment (Grossman et al., 2022), perform cost-benefit analysis (Reinagel, 2021) and adapt their response vigor to task utility (Wang et al., 2013). However, it is not known if rodents can adapt attentional intensity based on task utility.

Global arousal, controlled by neuromodulatory systems that make up the reticular activating system (Aston-Jones & Cohen, 2005; McGinley, Vinck, et al., 2015), is thought to be a key physiological mediator of the effects of motivation on attentional intensity. Some evidence, consistent with traditional metabolic and capacity theories, argues that increased arousal is associated with increased attentional performance (Hasselmo & McGaughy, 2004; Massar et al., 2016; Parikh et al., 2007; Saderi et al., 2021). Other evidence suggests just the opposite, that high arousal is associated with task disengagement, and thus that improved attention occurs with lower arousal (Aston-Jones & Cohen, 2005; Gilzenrat et al., 2010; Jepma & Nieuwenhuis, 2011; Usher et al., 1999). A third view is that optimal performance might occur at moderate, rather than high or low levels of arousal (Brink et al., 2016; Faller et al., 2019; McGinley, David, et al., 2015; Schriver et al., 2018; Yerkes & Dodson, 1908). For example, the locus coeruleus noradrenaline system (LC-NA) has been proposed to control the tradeoff between exploitation and exploration (Aston-Jones & Cohen, 2005; Jepma & Nieuwenhuis, 2011), with optimal exploitation (i.e. task-related attention) occurring at moderate levels of tonic firing.

Fluctuations in pupil size at constant luminance track global arousal state (Joshi & Gold, 2020; McGinley, Vinck, et al., 2015), and the activity of major neuromodulatory systems, including noradrenaline (Breton-Provencher & Sur, 2019; de Gee et al., 2017; Joshi et al., 2016; Murphy et al., 2014; Reimer et al., 2016; Varazzani et al., 2015), acetylcholine (de Gee et al., 2017; Mridha et al., 2021; Reimer et al., 2016), and perhaps serotonin (Cazettes et al., 2021) and dopamine (de Gee et al., 2017). We previously showed that optimal behavioral and neural detection of simple sounds occurred at intermediate levels of pupil-linked arousal (McGinley, David, et al., 2015). We here sought to test whether optimal feature-based attention also exhibits an inverted-U dependence on arousal and whether animals exert self-control on their arousal state to adapt feature-based attention to task utility. We developed a feature-based "attentional intensity task" for head-fixed mice and report behavioral and pupillary signatures of strategic attentional intensity allocation in a large cohort (N=88 mice; n=1983 total sessions). We report that after increases in task utility, mice become more sensitive and efficient decision-makers, helped by the

stabilization of pupil-linked arousal closer to its optimal level, including a suppression of exploratory behavior.

A feature-based attentional intensity task for head-fixed mice

To study the adaptive allocation of attentional intensity, and the role therein of global arousal, we developed a feature-based attentional intensity task for head-fixed mice (**Fig. 1**). A large cohort of mice (N=88; n=1983 sessions) were trained to detect coherent time-frequency acoustic motion (called temporal coherence; (Shamma et al., 2011)), which was embedded in an ongoing random tone-cloud of unpredictable duration (**Fig. 1A**). The task requires continuous listening and sustained attention to achieve high detection performance. Mice were motivated to attend to the tone cloud by being food scheduled and receiving sugar-water reward upon licking during the temporal coherence signal.

We designed the attentional intensity task to be perceptually difficult and therefore highly demanding of attentional resources, so that it would be impossible for mice to sustain consistently high levels of attention and performance during the full session duration (~75 minutes). Thus, mice should increase attentional intensity in high reward blocks, to exploit the high utility, and reduce attentional intensity in low reward blocks. To suppress excessive licking, they received a 14-second time out when they licked during the pre-signal tone cloud. We manipulated task utility by shifting the reward size back and forth between high (12 ul) and low (2 ul) values, in consecutive blocks of 60 trials within the same experimental session. We simultaneously recorded pupil size and walking speed as measures of arousal and exploratory behavior, respectively (**Fig 1B**). See Methods for details.

We defined four simple measures of behavioral performance that are well-suited to quantify behavior in this quasi-continuous listening task: (i) Overall response rate, the number of licks per second of either noise or signal sounds. Overall response rate captures the overall level of engagement, and, in this go / no-go detection task, is analogous to decision bias (also called criterion in signal detection theory). (ii) Discriminatory response rate, the number of licks per second of signal sounds minus the number of licks per second of noise sounds. Discriminatory response rate captures how much more mice licked during signal vs noise sounds and is therefore analogous to sensitivity (also called d' in signal detection theory). We take motivated shifts in discriminatory response rate as the behavioral signature of adaptive allocation of attentional intensity. (iii) Reward rate, the fraction of trials that ended in a hit (a lick during the signal, which was followed by a sugar reward). Reward rate is analogous to accuracy and is affected by both overall and discriminatory response rate. (iv) Reaction time (RT) on hit trials, the delay between signal onset and the correct lick. See Methods for details.

Figure 1. Monitoring behavior and pupil-indexed arousal during the attentional intensity task. (A) Spectrogram of sounds played during three example trials. Mice were head-fixed on a wheel and learned to lick for sugar water reward to report detection of the signal stimulus. Correct go-responses (hits) were followed by 2 or 12 mL of sugar water. Reward magnitude alternated between 2 and 12 mL in blocks of 60 trials. Incorrect go-responses (false alarms) terminated the trial and were followed by a 14 s timeout. **(B)** Example session. From top to bottom: noise stimuli, signal stimuli, reward context, correct licks (hits), incorrect licks (false alarms), reaction time (RT) on hit trials, pupil size and walking velocity.

Mice learn to adaptively allocate attentional intensity

Since the adaptive allocation of attentional intensity is a high-level cognitive function for a mouse, we reasoned that it may rely on extensive experience with the value structure of an environment. To test this, we evaluated the time course of learning for several aspects of the behavior.

The training regime consisted of three phases. In phase 1, the signal was 6 dB louder than the noise, several classical conditioning trials were included, and reward magnitude was constant throughout the session. During phase 1 mice quickly learned to lick to harvest rewards: the overall response rate increased from ~0 to ~0.6 licks/s (**Fig. 2A**, left). Discriminatory response rate and reward rate also quickly increased across the first few sessions (**Fig. 2D,G,** left). RT gradually decreased by a factor of two during the phase 1 (**Fig. S2E**), a further sign that the mice rapidly learned the task structure. In phase 2, we introduced the block-based changes in reward magnitude. Overall response rate was ~0.3 licks/s at the end of phase 2 (**Fig. 2A**). Through simulations we found that an overall response rate of 0.3 licks/s resulted in the highest reward rate and thus the highest number of rewards (**Fig. S2R**; Methods). Discriminatory response rate and reward rate also gradually increased (**Fig. 2D,G**), and RT decreased further during phase 2 (**Fig. S2E**).

Once mice reached a sufficient level of performance in phase 2 (Methods), they were moved up to the phase 3, the final version of the task, for which signal and noise sounds were of equal loudness and for which the small number of classical conditioning trials were omitted. By this time, mice were sufficiently experienced with the task to maintain a relatively high overall response rate (**Fig. 2B**). However, since they could no longer rely on loudness differences between signal and noise sounds, their discriminatory response rate dropped to approximately zero (**Fig. 2E**). Re-learning the (now purely feature-based) signal detection was, as predicted, perceptually difficult, as indicated by the relatively shallow learning curves. We fitted exponential functions quantify their speed of learning in phase 3 (Methods). The fitted time constants for discriminatory response rate and reward rate collapsed across reward blocks were $\tau = 8$ and $\tau = 7$, respectively (**Fig. S2K,N**). We verified that these time constants were not sensitive to sampling bias (dropout for later sessions; **Fig. S2L,O**). To do so, we refitted exponential functions to discriminatory response rate across sessions, after splitting the group of mice based on the maximum session number they performed in (**Fig. S2D**).

Figure 2. Mice rapidly learn task structure but slowly learn feature-based attention. (A) Overall response rate (Methods) across experimental sessions in learning phases 1 and 2; session numbers are with respect to the last session in phase 2. **(B)** Overall response rate across experimental sessions in learning phase 3, separately for high and low reward blocks. **(C)** As B, but for the difference between high and low reward blocks. Dashed line, exponential fit (Methods). **(D-F)** As A-C, but for discriminatory response rate (Methods). **(G-I)** As A-C, but for reward rate (Methods). All panels: shading, 68% confidence interval across animals (N=88).

We next sought to determine if and how rapidly mice learn to strategically regulate attentional intensity. We found that overall response rate, discriminatory response rate and reward rate were all higher in the high, compared to the low, reward context **(Fig. 2B,E,H**, orange vs. blue), and RT was lower **(Fig. S2F)**. Thus, mice adaptively turned up their feature-based attention after increases in task utility. The fitted time constant for high vs. low reward discriminatory response rate and reward rate were $\tau = 10$ and $\tau = 9$, respectively **(Fig. 2F,I)**, indicating that mice learned to strategically allocate attention roughly at the same pace as perceptual learning.

Performance in a psychometric task variant demonstrates feature-based attention

Due to the within-trial temporal structure, it is theoretically possible that mice learned the to guess the timing statistics of when temporal coherence signals were likely to occur, rather than perceptually attending to and detecting the coherence. To rule out such a purely timing-based strategy, we trained a cohort of mice (N=10; n=142 sessions) in a psychometric variant of the task in which signal coherence was varied randomly from trial to trial, in addition to the block-based utility manipulation. Signal coherence was degraded by manipulating the fraction of tones that moved coherently through time-frequency space **(Fig. 3A**; see Methods). This manipulation is analogous to reducing spatial motion coherence in the classic visual random-dot motion task (Newsome et al., 1989). As would be expected if the mice employed feature-based attention, both discriminatory response rate and reward rate lawfully depended on signal coherence **(Fig. 3B,C)**. Thus, mice attended to tone cloud temporal coherence, a complex, high-order auditory feature.

Figure 3. Performance in a psychometric task variant demonstrates feature-based attention. (A) Example spectrograms of strong (left) and weak (right) signals (Methods). **(B)** Discriminatory response rate (Methods) across three difficulty bins and separately for high and low reward blocks. Stats, 2-way repeated measures ANOVA (factors task utility [high vs. low] and signal strength (coherence) bin [weak, medium, strong]); main effect task utility: $F_{1,9} = 4.6$, $p = 0.060$; main effect signal strength: $F_{2,18} = 5.0$, $p = 0.018$; interaction effect: $F_{2,18} = 0.4$, $p = 0.669$. Error bars, 68% confidence interval across animals (N=10). **(C)** As D, but for reward rate (Methods). Main effect task utility: $F_{1,9} = 16.5$, $p = 0.003$; main effect signal strength: $F_{2,18} = 14.0$, $p < 0.001$; interaction effect: $F_{2,18} = 2.0$, $p = 0.162$.

Intentional intensity increases rapidly after increases in task utility

We next sought to characterize the timescale within a session on which mice adapt their behavior to shifts in task utility. We observed that mice spent the 1st block (termed block '0'; low reward) becoming engaged in the task (**Fig. S4A-D;** see also **Fig. S7F**). Therefore, we focused all analyses on the subsequent six blocks in which the available reward size alternated between 12 and 2 μL. See Methods for details.

We found that the animal's overall response rate was higher in the high compared to low reward blocks (**Fig. 4A-C**). Overall response rate was close to the optimal level (**Fig. S2R**; Methods) in the high reward blocks, while it was substantially lower than that in the low reward blocks (**Fig. 4C**). Crucially, discriminatory response rate was also higher in the high compared to low reward blocks (**Fig. 4D-F**). Thus, during high task utility mice increased their response rate more so during signals than during noise sounds, a behavioral hallmark of attention. Both overall and discriminatory response rate declined across the session (**Fig. 4A,C,D,F**), likely as a result of fatigue and/or satiety. In sum, an increase in task utility boosts feature-based attentional intensity (discriminatory response rate, analogous to sensitivity) as well as boosting the signal-independent probability of responding (overall response rate, analogous to criterion) to the optimal level.

Because the reward context was not cued, the first reward in a block provided a strong and unambiguous indication that a transition had occurred. Therefore, we analyzed time-dependencies within each block in two different ways: (i) aligned to the switch in (unobserved) reward availability (dashed lines in **Fig. 4A,D,G,J**), and (ii) aligned to the first hit trial after block transitions (solid lines). After the first high reward in the high reward block, overall response rate immediately increased by 231.9% compared to just before the switch, and after that did not increase further (**Fig. 4B**). In contrast, when switching from high to low reward, overall response rate immediately decreased by 40.5% and then decreased by a further 39.6% with a time constant of 15 trials (Methods). After the first high reward in the high reward block, discriminatory response rate immediately increased by 171.8% compared to just before the switch, and then increased by a further 4% with a time constant of 4 trials (**Fig. 4E**). When switching from high to low rewards, discriminatory response rate immediately increased with 16.3% and then decreased by a further 58.5% with a time constant of 15 trials. Thus, we found evidence for a hysteresis effect (Ghosh & Maunsell, 2021): mice updated their behavior faster when switching from low to high reward, than the other way around.

The higher discriminatory response rate in the high reward blocks predicts a higher reward rate. However, the higher overall response rate might lower the reward rate: noise stimuli always precede signals on each trial of the task, and thus a higher overall response rate could result in more false alarms than hits. Thus, we wondered if their reward rate increased during periods of high task utility. This was indeed the case. Mice detected the signal on a larger fraction of trials in the high vs. low reward blocks and thus collected more rewards (**Fig. 4G-I**). Mice sustained a stable reward rate of ~28% across the entire session during the high reward blocks (odd numbered blocks), while reward rate was lower in the low reward blocks from the start (block 2) and declined

further across the session (blocks 4 and 6; **Fig. 4G,I**). Mirroring reward rate, RTs were substantially lower in high reward than in low reward blocks, and gradually increased as the experimental session progressed (**Fig. 4J-L**). Reward rate and RT exhibited similar hysteresis effects as the overall and discriminatory response rates (**Fig. 4H,K**). Specifically, mice updated their behavior faster when switching from low to high reward than when switching in the other direction.

For all behavioral metrics, we verified that our results are robust to specifics regarding trial selection (**Fig. S4E-H;** Methods) and are not confounded by effects of time-on-task (**Fig. S4I-L**; Methods). We conclude that mice adapt their decision-making to changes in task utility: they are better and faster at detecting signals during epochs of high task utility.

Figure 4. Rapid and adaptive shifts in mouse decision-making after changes in task utility. (A) Overall response rate (Methods) across three high and three low reward blocks in the same experimental session.

Dashed lines, locked to block onset; solid lines, locked to first hit in block. **(B)** As A, but collapsed across blocks of same reward magnitude. Green window, trials used when pooling data across trials within a block (as in panel C). **(C)** As A, but collapsed across trials within a block. Horizontal red line, optimal overall response rate (Methods). Stats, 2-way repeated measures ANOVA (factors task utility [high vs. low] and time-on-task [1, 2, 3]); main effect task utility: $F_{1,87} = 317.3$, $p < 0.001$; main effect time-on-task: $F_{2,174} = 103.3$, $p < 0.001$; interaction effect: $F_{2,174} = 39.1$, $p < 0.001$. **(D-F)** As A-C, but for discriminatory response rate (Methods). Main effect task utility: $F_{1,87} = 63.0$, $p < 0.001$; main effect time-on-task: $F_{2,174} = 17.1$, $p < 0.001$; interaction effect: $F_{2,174} = 4.0$, $p = 0.019$. **(G-I)** As A-C, but for reward rate (Methods). Main effect task utility: $F_{1,87} = 22.5$, $p < 0.001$; main effect time-on-task: $F_{2,174} = 27.1$, $p < 0.001$; interaction effect: $F_{2,174} = 22.8$, $p < 0.001$. **(J-L)** As A-C, but for reaction time (RT) on hit trials. Main effect task utility: $F_{1,87} = 571.1$, $p < 0.001$; main effect time-on-task: $F_{2,174} = 25.8$, $p < 0.001$; interaction effect: $F_{2,174} = 0.9$, $p = 0.401$. All panels: shading or error bars, 68% confidence interval across animals (N=88).

Evidence accumulation modeling shows that high task utility increases signal engagement

We next sought to computationally dissect the elements of the decision-making process, which give rise to the observed effects of task utility on overt behavior (**Figs. 1-4**). One key computational element is evidence accumulation. Accumulating evidence increases the signal-to-noise ratio of decision-relevant evidence, by averaging across a set of noisy observations made over time. Evidence accumulation allows for detection of dynamic time-varying stimuli, such as the temporal coherence used in this study. As such, evidence accumulation is thought to underlie most decisions, ranging from the relatively simple ones based on perceptual evidence as studied here (Gold & Shadlen, 2007), to high-level cognitive decisions such as which career to pursue. Rodents can perform evidence accumulation (Brunton et al., 2013; Hanks et al., 2015). It is unknown if and how evidence accumulation is shaped by task utility.

By simultaneously considering choices and their latency, sequential sampling models can be used to decompose observed choice behavior into its constituent cognitive processes, including evidence accumulation (Bogacz et al., 2006; Brody & Hanks, 2016; Gold & Shadlen, 2007; Ratcliff & McKoon, 2008). The drift diffusion model describes the perfect accumulation (i.e., without forgetting) of noisy sensory evidence in a single decision variable that drifts to one of two decision bounds. Crossing the decision bound triggers the response and hence determines reaction time (Bogacz et al., 2006; Brody & Hanks, 2016; Laming, 1968; Ratcliff & McKoon, 2008). When the evidence is stationary (i.e., its mean does not vary over time), this model produces the fastest decisions for a fixed error rate (Bogacz et al., 2006). However, in most real-life perceptual decisions, as modeled in our attentional intensity task, the relevant evidence is not stationary. In this case, perfect integration is suboptimal, because it results in an excessive number of false alarms due to integration of pre-signal noise (Ossmy et al., 2013). We thus used a computational model of the decision process based on leaky (i.e. forgetful) integration (**Fig. 5A,B**; (Usher & McClelland, 2001); Methods).

Our model contained six key parameters, which we evaluated for effects of task utility (**Fig. 5A,B**; Methods): (i) bound height, which controls the speed-accuracy tradeoff and overall response rate; (ii) leak, which controls the timescale of evidence accumulation; (iii) mean drift rate, which

controls the efficiency of accumulation of the relevant sensory feature (coherence); (iv) attention lapse probability, which is the fraction of trials on which the relevant sensory evidence is not accumulated; (v) non-decision time, which is the speed of pre-decisional evidence encoding and post-decisional translation of choice into motor response; and (vi) a mixture rate, which sets a fraction of trials on which the mouse makes an automatic response to trial onset, and thus does not engage in evidence accumulation. In the model, bound height, leak, drift rate and attention lapse probability co-determine the fraction of correct responses and their associated RTs (**Fig. S5A-D**). However, their effects on the decision variable are distinct and can therefore be dissociated by simultaneously fitting choices as well the shape of their associated reaction time distribution (**Fig. 5B-E**); (Shinn et al., 2020)). The fitted model accounted well for the behavior in the attentional intensity task, with accurate predictions for choices and RTs (**Fig. 5C-E**). We considered three alternative models (Methods), which provided worse fits, both qualitatively (**Fig. S5E-J**) as well as quantitatively (**Fig. S5K**).

Figure 5. Accumulation-to-bound model accurately and precisely describes decision-making in the attentional intensity task. Schematic of bounded accumulation model accounting for the fraction of go-responses and their associated reaction times (RT). **(B)** The decision-dynamics were governed by leak (k) and gaussian noise during noise stimuli, and additionally by the attention lapse probability (p) and drift rate (v) during the signal stimuli. **(C)** Reward rate (defined as % correct licks on all trials containing signal sounds) in the high (top) and low (bottom) reward blocks, separately for binned noise durations. Black line, model fit. **(D)** RT distribution for correct licks (hits) in the high (top) and low (bottom) reward blocks. Black line, model fit. **(E)** As D, but for incorrect licks (false alarms).

Because of the prominent time-on-task effects we observed in our performance measures (**Fig. 4**), we varied all model parameters with block number (see Methods). We found that the drift

rate was higher, and the leak and attention lapse probability were lower in the high vs. low reward blocks (**Fig. 6A-C**). These three parameter dependencies all suggest that attentional intensity is greater in the high-reward context. This pattern did not depend on the specifics of the model. In each of the alternative models, leak and attention lapse probability were lower in the high compared to low reward blocks (**Fig. S6A-C**). Drift rate was also higher in the high compared to low reward blocks when modeling the fast errors with variability in starting point instead of a mixture rate (**Fig. S6C**; Methods). There was no significant effect of task utility on the other model parameters (**Fig. 6D-F**). The biggest effect of time-on-task was on the attention lapse rate (**Fig. 6C**).

Lower leak indicates more sensory stimulus engagement, which is a signature of attentional intensity. However, in our attentional intensity task, with non-stationary evidence, low leak is not necessarily optimal because more noise is accumulated. Therefore, we used simulations to identify the optimal leak for the task (**Fig. S6D,E**). Leak estimates were lower than optimal in the high reward blocks, and higher than optimal in low reward blocks, indicating that mice overshoot their leak in both reward contexts, but in opposite directions. The high integration time constant (1 / leak) in the high reward blocks indicates that they were more engaged with the stimulus, but also meant that extensive pre-signal noise was integrated, leading to an excess of false alarms and a high overall response rate. The higher drift rate and lower attention lapse probability in the high compared to low reward blocks contributed to a positive effect of task utility on discriminatory response rate and reward rate.

In sum, we found that that an increase in task utility resulted in robust changes of the decision computation, all of which support improved attention. Specifically, evidence accumulation persisted across a longer timescale (lower leak), was more efficient (higher drift rate) and was more reliable (lower attention lapse probability).

Figure 6. High task utility improves multiple aspects of the decision computation. (A) Fitted leak estimates (kernel density estimate of 50 bootstrapped replicates) separately per block number. Main effect task utility (fraction of bootstrapped parameter estimates in the low reward blocks higher than in the high reward blocks): p = 0.013. **(B)** As A, but for drift rate. Main effect task utility: p = 0.040. **(C)** As A, but for attention lapse probability. Main effect task utility: p < 0.02. Main effect time-on-task (fraction of bootstrapped parameter estimates in the first two blocks higher than in the last two blocks): p = 0.02. **(D-F)** As A, but for bound height, non-decision time and mixture rate, respectively. All panels: all further main effects of task utility, time-on-task or interaction effects were not significant (p > 0.05).

Mice regulate arousal state closer to optimal levels during periods of high task utility

We previously showed that optimal signal detection behavior in a simple tone-in-noise detection task occurred at intermediate levels of arousal (McGinley, David, et al., 2015). We thus wondered (i) if a similar inverted-U dependence of performance on arousal was observed in the more-complex attentional intensity task, and (ii) if mice spend more time close to this optimal arousal state during periods of high task utility, which would suggest adaptive self-regulation of arousal.

We quantified arousal as the diameter of the pupil measured immediately before each trial (Methods), and first characterized the relationship between pre-trial pupil-linked arousal and behavioral performance, irrespective of the reward context. Replicating our earlier work, we observed highest discriminatory response rate and shortest RTs on trials characterized by mid-size pre-trial pupil size (**Fig. 7A,B**; Methods). We additionally observed highest overall response rate on trials characterized by mid-size pre-trial pupil size (**Fig. 7C**), and a linear and generally negative relationship between reward rate and pre-trial pupil size (**Fig. 7D**). The low overall response rate in the low pupil-linked arousal state resulted in fewer false alarms, and thus more trials on which the signal was played, which provided an opportunity to make a correct lick.

We defined the optimal level of arousal as the average of the pre-trial baseline pupil sizes for which discriminatory response rate, overall response rate, and reward rate were maximal and RT was minimal (mean across four green dots in **Fig. 7A-D**). Across animals, this optimal pre-trial baseline pupil size was 30.0% of its maximum (green line in **Fig. 7G**). The pre-trial pupil size was often larger than this optimum and tended to increase throughout an experimental session (**Fig. 7E,F**). Crucially, pre-trial pupil size was smaller, and closer to its optimum, in the high vs. low reward blocks (**Fig. 7E,F**). Furthermore, the pre-trial pupil size was also more stable (less variable) in the high vs. low reward blocks (**Fig. 7G & Fig. S7L-N**). To capture how close the animal's arousal state on each trial was to the optimal level, we computed the absolute difference between each pre-trial's pupil size and the optimal size (Methods). Mice spent more time closer to the optimal arousal state in the high vs low reward blocks (**Fig. 7H,I**), and mice were decreasingly effective at down-regulating their arousal state towards the optimal level as the session progressed (**Fig. 7H,I**).

We tested whether changes in task utility better predicted changes in pre-trial pupil size or its distance from optimal in two ways. First, we compared the effect sizes of the main effects of

task utility on both arousal measures (**Fig. 7F,I**): the partial η^2 was 0.325 for pre-trial pupil size and 0.566 for its distance from optimal. Second, we performed a logistic regression of block-wise reward magnitude [0,1] on either z-scored block-wise pre-trial pupil size or its distance from optimal. The fitted coefficients were negative in both cases, but significantly smaller for the distance from optimal measure (**Fig. 7J**). Thus, during heightened task utility, mice do not stereotypically downregulate their arousal state, but instead up and down regulate their arousal state closer to its optimal level.

Figure 7. Mice regulate arousal state closer to optimal level during high task utility. (A) Relationship between pre-trial pupil size and discriminatory response rate (Methods). A 1st order (linear) fit was superior to a constant fit ($F_{1,163}$ = 5.1, p = 0.024) and a 2nd order (quadratic) fit was superior to the 1st order fit ($F_{1,963}$ = 4.0, p = 0.046; higher order models were not superior; sequential polynomial regression; Methods). Grey line, fitted 2nd order polynomial; green data point, optimal pre-trial pupil size bin (Methods); asterisk, walking trials (Methods). **(B)** As A, but for reaction time (RT) on hit trials. 1st order fit: $F_{1,163}$ = 2.5, p = 0.116; 2nd order fit: $F_{1,963}$ = 4.9, p = 0.027; higher order models were not superior. **(C)** As A, but for overall response rate (Methods). 1st order fit: $F_{1,163}$ < 0.1, p = 0.957; 2nd order fit: $F_{1,963}$ = 8.3, p = 0.004; higher order models were not superior. **(D)** As A, but for reward rate (Methods). 1st order fit: $F_{1,163}$ = 5.5, p = 0.020; higher order models were not superior. **(E)** Pre-trial pupil size collapsed across blocks of same reward magnitude. **(F)** As E, but collapsed across trials within a block. Stats, 2-way repeated measures ANOVA (factors task utility [high vs. low] and time-on-task [1, 2, 3]); main effect task utility: $F_{1,87}$ = 41.8, p < 0.001;

main effect time-on-task: $F_{2,174} = 51.0$, $p < 0.001$; interaction effect: $F_{2,174} = 6.3$, $p = 0.002$. **(F)** Histogram of pre-trial pupil measures (Methods) separately for the high and low reward context, and for still and walk trials (Methods). Green line, optimal pre-trial pupil size (Methods). **(H,I)** As E,F, but for absolute distance from optimal pre-trial pupil size (Methods). Main effect task utility: $F_{1,87} = 113.2$, $p < 0.001$; main effect time-on-task: $F_{2,174} = 39.7$, $p < 0.001$; interaction effect: $F_{2,174} = 3.0$, $p = 0.051$. **(J)** Coefficients from logistic regression of block-wise task utility [high vs. low] on either mean pre-trial pupil size (left) or absolute distance from optimal pre-trial pupil size (right). Stats, Wilcoxon signed-rank test. All panels: shading or error bars, 68% confidence interval across animals (N=88).

As walking velocity has traditionally been used as a marker of behavioral state (McGinley, David, et al., 2015; Polack et al., 2013), we additionally analyzed the animal's walking on the wheel. Although overall response rate was substantially higher on trials associated with pre-trial walking, discriminatory response rate and reward rate were substantially lower and near zero (asterisks in **Fig. 7A,C,D**), suggesting that licks during walking were essentially random. Like pre-trial pupil size, walk probability was lower in the high, compared to low, reward blocks (**Fig. S7O-Q**). Our findings that both pupil-linked and walk-related arousal were higher in the low reward blocks indicate that mice did not use the low reward blocks to rest, but instead to engage in alternative exploratory behaviors, consistent with some models of the function of locus coeruleus (Aston-Jones & Cohen, 2005), which plays a major role in pupil control (Breton-Provencher & Sur, 2019; de Gee et al., 2017; Joshi et al., 2016; Reimer et al., 2016; Varazzani et al., 2015).

Adaptive shifts in pupil-linked arousal partially mediate improved behavior during high task utility.

Having observed that epochs of high task utility are associated with both a more optimal arousal state and increased behavioral performance, we wondered to what extent the arousal optimization could explain the performance effect. To address this, we tested for statistical mediation of baseline pupil in the apparent effect of task utility on reward rate (fraction of correct-go responses; **Fig. 8A**). We found that (the indirect path of) block-wise increases in task utility predicting block-wise decreases in distance from the optimal arousal state, in turn driving block-wise increases in reward rate, partially mediates the apparent effect of task utility on reward rate (**Fig. 8B**; 9.97% of the total effect). Similar results of the mediation analysis were observed if we used the pre-trial pupil size, pre-trial pupil size standard deviation or walking probability (**Fig. S8**). Taken together, we conclude that regulating pupil-linked arousal towards the optimal level partly implements the adaptive behavioral adjustments to match attention allocation to task utility.

Figure 8. Adaptive changes in pupil-linked arousal partially mediate behavioral improvements seen during high task utility. (A) Schematic of mediation analysis of task utility to correct responses (reward rate), via pre-trial pupil-linked arousal (Methods). Arrows, regressions; coefficient $a \times b$ quantifies the 'indirect' (mediation) effect; coefficient c' quantifies the 'direct effect'. **(B)** Fitted regression coefficients of the a-path (blue), b-path (red) and the indirect path (mediation; pink). Stats, Wilcoxon signed-rank test.

<div align="center">DISCUSSION</div>

To efficiently meet their survival needs, organisms must regulate both the selective and intensive aspects of their attention. The study of attention has largely focused on its selective aspect (Carrasco, 2011; Fritz et al., 2007; Maunsell & Treue, 2006), while overlooking the intensive one, but see (Ghosh & Maunsell, 2021). We here developed a feature-based attention task for head-fixed mice with non-stationary task utility. By applying quantitative modeling to a large behavioral and physiological dataset we show that during high utility, mice: (i) collect more rewards, (ii) accumulate perceptual evidence more efficiently, reliably, and across longer timescales, (iii) stabilize their pupil-linked arousal state closer to an optimal level; and (iv) suppress exploratory locomotor behavior. In sum, regulating pupil-linked arousal towards an optimal level partially implements behavioral adjustments that adaptively adjust attentional intensity based on task utility.

Our results demonstrate an important, and previously underappreciated, role for motivation in driving attentional intensity. Critically, mice sustained their highest level of performance – encapsulated in the reward rate – across the three high-reward blocks interspersed across a long-lasting and difficulty sustained attention task. Performance was comparably high in only the first low-reward block and then declined dramatically in subsequent low-reward blocks. A parsimonious interpretation of these findings is that early in the session mice are hungriest and least fatigued, and thus highly motivated to work for any reward. Later in the session, when more satiated and fatigued, only large rewards are sufficient to motivate them to increase their attentional intensity (Hernández-Navarro et al., 2021). Another factor, which may increase performance in the low reward and blunt an even larger attention allocation effect, is that in our task design mice need to keep performing at a sufficiently high level to detect the switch to a high-reward block.

Growing evidence supports that neural computation and behavioral performance are not stationary within a session due to fluctuations in internal state. State-dependent neural activity has been observed in primary sensory cortices (Goris et al., 2014; McGinley, David, et al., 2015) and sensory-guided behavior (McGinley, David, et al., 2015) but not in relation to attentional intensity. Recently, spontaneous shifts between engaged, biased, and/or disengaged states have been inferred from behavior (Ashwood et al., 2022; Weilnhammer et al., 2021). Utility-based shifts in behavior

(but not attention) have been observed in rodents (Reinagel, 2021; Wang et al., 2013). Other than in humans, the regulation of attentional intensity has only been observed in monkeys (Ghosh & Maunsell, 2021).

Our results, demonstrating motivated shifts in attentional intensity, suggest a cost-benefit analysis being used to adapt performance level to an evolving motivational state (Botvinick & Braver, 2015; Shenhav et al., 2013). Neural underpinning of such top-down control of attentional intensity are yet to be elucidated. Orbital frontal cortex (OFC) and dorsal anterior cingulate cortex (dACC) are likely candidate regions since both perform value computations related to optimizing behavior (Akam et al., 2021; Botvinick & Braver, 2015; Shenhav et al., 2013; Tremblay & Schultz, 2000), and these structures are strongly connected to neuromodulatory nuclei, including LC (Arnsten & Goldman-Rakic, 1984; Aston-Jones & Cohen, 2005; de Gee et al., 2017; Joshi & Gold, 2022; Porrino & Goldman-Rakic, 1982).

Our results also demonstrate an important role of arousal in mediating adaptive adjustments in attentional intensity. This role for pupil-indexed arousal is in contrast with the large literature on pupil dilation as a readout of attentional capacity (also called effort) driven by fluctuations in task difficulty (Alnæs et al., 2014; Hess & Polt, 1964; Kahneman et al., 1967; Kahneman & Beatty, 1966; Laeng et al., 2012), including work on pupil-indexed listening effort (Peelle, 2018; Pichora-Fuller et al., 2016). In this literature, the magnitude of the task-evoked pupil response is typically measured during the stimulus and compared between conditions that differ in difficulty; for example, employing multiple levels of speech degradation or memory load. Here, motivational factors are customarily neglected (Pichora-Fuller et al., 2016). In our attentional intensity task, the perceptual difficulty (temporal coherence) was held constant across the entire session, and motivation (driven by task utility) was changed in blocks. Furthermore, we focus on the pre-stimulus, so-called 'tonic,' pupil-linked arousal measured before each trial, rather than peri-stimulus, so-called 'phasic,' pupil dilation. Future work should determine the interaction of these complementary arousal functions in behavior, perhaps by combining non-stationarity in both task utility and perceptual difficulty.

An important question opened by our results is which neuromodulatory systems contribute to attentional intensity. Our finding that tonic pupil-linked arousal is lower in the low reward blocks is in line with the adaptive gain theory of LC function (Aston-Jones & Cohen, 2005; Gilzenrat et al., 2010; Jepma & Nieuwenhuis, 2011), but see (Bari et al., 2020). Our results are not in line with the idea that increased acetylcholine mediates attention (Hasselmo & McGaughy, 2004; Sarter et al., 2006), but see (Robert et al., 2021). The willingness to exert behavioral control is thought to be mediated by tonic mesolimbic dopamine (Hamid et al., 2016; Niv et al., 2007; Wang et al., 2013) and/or serotonin (Gutierrez-Castellanos et al., 2022). However, the willingness to work is likely more related to overall response rate, while attentional intensity is more related to discriminatory response rate. Future work is needed to determine the precise roles of neuromodulatory systems in adaptive allocation of attentional intensity.

The specific pattern we observed in the arousal dependence of performance and its relation to task utility likely illustrates both general principles as well as task- and species-specific patterns. For example, in contrast to our findings, a previous human study reported higher pre-trial pupil size during high reward blocks (Massar et al., 2016). This task was perceptually easy, while our attentional intensity task was hard. An extensive literature shows that the relationship between tonic arousal and behavioral performance depends on task difficulty, with higher arousal being more optimal for easier tasks (Sörensen et al., 2021; Yerkes & Dodson, 1908). The discrepancy between the findings reported by Massar et al. (2016) and ours might also be due to species difference (but see (de Gee et al., 2020): perhaps humans in laboratory conditions are on average in a lower arousal state than mice and thus sit on the opposite side of optimality. However, this is not the case for all individuals; moving closer to the optimal arousal state after increases in task utility involves either increases or decreases in arousal, depending on one's starting point.

Taken together, our results add to the growing evidence for an inverted-U, three-state model for the role of arousal in behavioral performance (McGinley, David, et al., 2015; McGinley, Vinck, et al., 2015; Schriver et al., 2018). This model accounts for the prominent exploration-exploitation tradeoff (Aston-Jones & Cohen, 2005; Gilzenrat et al., 2010; Jepma & Nieuwenhuis, 2011) as the right side of the inverted-U; pupil size was larger and mice walked more in low-reward blocks, a form of combined aroused and active exploration. In these low reward blocks, mice were also less likely to attend to and accumulate the relevant sensory evidence (coherence). This result is in line with a recent observation that lapses in perceptual decisions reflect exploration (Pisupati et al., 2021). When pupil was smallest, below optimal levels, animal's exhibited rare and slow behavioral responses, indicative of a resting form of disengagement. Thus, increases in task utility motivate mice to pay more attention, helped by the stabilization of pupil-linked arousal closer to its optimal level.

METHODS

Animals

All surgical and animal handling procedures were carried out in accordance with the ethical guidelines of the National Institutes of Health and were approved by the Institutional Animal Care and Use Committee (IACUC) of Baylor College of Medicine. Experiments were conducted using a total of 88 mice (74 male, 14 female) aged older than 7 weeks at study onset. Wild-type mice were of C57BL/6 strain (Jackson Labs) (N=51; 1 female). Various heterozygous transgenic mouse strains used in this study were of Ai148 (IMSR Cat# JAX:030328; N=6; 3 females), Ai162 (IMSR Cat# JAX:031562; N=10, 3 females), ChAT-cre (IMSR Cat# JAX:006410; N=3; all male) and ChAT -cre crossed with Ai162 (N=18; 7 females). This variety in genetic profile was required to target specific neural circuitries with 2-photon imaging; the results of the imaging experiments will be the focus of another report. Mice received ad libitum water. Mice received food ad libitum on weekends but were otherwise placed on food restriction to maintain a 90% normal body weight. Animals were trained Monday-Friday. Mice were individually housed were kept on a regular light-dark cycle, and all experimental manipulations were done during the light phase.

Head post implantation

The surgical station and instruments were sterilized prior to each surgical procedure. Isoflurane anesthetic gas (2–3% in oxygen) was used for the entire duration of all surgeries. The temperature of the mouse was maintained between 36.5°C and 37.5°C using a homoeothermic blanket system. After anesthetic induction, the mouse was placed in the stereotaxic. The surgical site was shaved and cleaned with scrubs of betadine and alcohol. A 1.5-2 cm incision was made along the scalp mid-line, the scalp and overlying fascia were retracted from the skull. A sterile head post was then implanted using dental cement.

Behavioral task

Each trial consisted of three consecutive intervals (**Fig. 1A**): (i) the "noise" interval, (ii) the "signal" interval, and (iii) the inter-trial-interval (ITI). The duration of the noise interval was randomly drawn beforehand from an exponential distribution with mean = 5 s (**Fig. S1A**); this was done to ensure a flat hazard rate of signal start time. In most sessions (82.8 %), randomly drawn noise durations greater than 11 s were set to 11 s. In the remainder of sessions (17.2 %), these trials were turned into catch trials consisting of 14 seconds of noise. For the results it did not matter whether sessions included catch trials or not (**Fig. S4M-P**). The duration of the signal interval was 3 s. The duration of the ITI was uniformly distributed between 2 and 3 s.

The noise stimulus was a "tone cloud" and consisted of consecutive chords of 20 ms duration (gated at start and end with 0.5 ms duration). Each chord consisted of 12 pure tones, selected in semitone steps from 1.5-96 KHz. For the signal stimulus, after the semi-random (jittered from evenly log-spaced tones by 1-2 semitones) first chord, all tones moved coherently upward by one semitone per chord (20 ms). The ITI-stimulus was pink noise, which is highly perceptually distinct from the tone cloud. Stimuli were presented at an overall intensity of 55 dB (root-mean square [RMS]) using Tucker Davis ES-1 electrostatic speakers.

Mice were head-fixed on a wheel and learned to lick for sugar water reward to report detection of the signal stimulus. Correct go responses (hits) were followed by 2 or 12 mL of sugar water. Reward magnitude alternated between 2 and 12 mL in blocks of 60 trials. Incorrect go-responses (false alarms) terminated the trial and were followed by a 14 s timeout. Correct no-go responses (correct rejecting the full 14 s of noise) in the sessions that contained catch trails were also followed by 2 or 12 mL of sugar water.

Training mice to perform the attentional intensity task involved three separate phases. In phase 1, mice performed a version of the task that involved louder signal than noise sounds (58 vs. 52 dB, respectively), several classical conditioning trials (5 automatic rewards during the signal sounds), and no block-based changes in reward magnitude (5 mL after every hit throughout the session). Phase 1 lasted for four experimental sessions (**Fig. S2A**). In phase 2, we introduced the block-based changes in reward magnitude. Once mice obtained a reward rate higher than 25% and the fraction of false alarm trials was below 50% for two out of three sessions in a row, they were moved up to the phase 3. Phase 2 lasted for 2 - 85 (median, 9) experimental sessions (**Fig. S2B**).

Phase 3 involved the final version of the task, with signal and noise stimuli of equal loudness and without the classical conditioning trials.

In a subset of experiments, the signal quality was systematically degraded by reducing the fraction of tones that moved coherently through frequency space. This is similar to reducing motion coherence in the classic random-dot motion task (Newsome et al., 1989). In these experiments, signal coherence was randomly drawn beforehand from six different levels: easy (100% coherence; as in the main task), hard (15-45% coherence), and four levels linearly spaced in between.

After session exclusion criteria (**Fig. S3**), a total of 88 mice performed between 5 and 60 sessions (2100–24,960 trials per subject) of the final version of the attentional intensity task (phase 3), yielding a total of 1983 sessions and 823,019 trials. A total of 10 mice performed the experiment with degraded signals; they performed between 5 and 28 sessions (2083–11,607 trials per subject), yielding a total of 142 sessions and 58,826 trials.

Data acquisition
Custom Labview software synchronized all sounds, licks, videos of the pupil and wheel motion. Licks were detected using a custom-made infrared beam-break sensor.

Pupil size. We continuously recorded the eye contralateral to the cuff implantation with a Basler GigE camera (acA780-75gm), coupled with a fixed focal length lens (55 mm EFL, f/2.8, for 2/3"; Computar) and infrared filter (780 nm long pass; Midopt, BN810-43), positioned approximately 8 inches from the mouse. An off-axis infrared light source (two infrared LEDs; 850 nm, Digikey; adjustable in intensity and position) was used to yield high-quality image of the surface of the eye and a dark pupil. Images (504 × 500 pixels) were collected at 15 Hz, using a National Instruments PCIe-8233 GigE vision frame grabber. To achieve a wide dynamic range of pupil fluctuations, an additional near-ultraviolet LED (405-410 nm) was positioned above the animal and provided low intensity illumination that was adjusted such that the animal's pupil was approximately mid-range in diameter following placement of the animal in the set-up and did not saturate the eye when the animal walked. Near-ultraviolet LED light levels were lower during two-photon imaging experiments, to avoid noise on the photo-multiplier tubes.

Walking speed. We continuously measured treadmill motion using a rotary optical encoder (Accu, SL# 2204490) with a resolution of 8,000 counts/revolution.

Analysis and modeling of choice behavior
All analyses were performed using custom-made Python scripts, unless stated otherwise.

Session exclusion criteria. We excluded the first 15 sessions (3 weeks) from each animal from the analyses (**Fig. S3A**). Additionally, we excluded sessions with (i) fewer than 300 trials (**Fig. S3B**);

or (ii) bad quality pupil data (**Fig. S3C-E**); or (iii) a reward rate of less than 15% of trials (**Fig. S3F,G**). We then analyzed data from only those mice with at least five sessions (**Fig. S3H**).

Trial exclusion criteria. We excluded the first (low-reward) block of each session, as mice spent the 1st block (termed block '0'; low reward) becoming engaged in the task (**Fig. S4A-D;** see also **Fig. S7F**). We found that a fraction of trials began during a lick bout that started in the ITI. These trials were immediately terminated and were recorded as false alarms. These rare "false start trials" (a 2.45±0.17 % s.e.m. of trials across mice), were removed from the analyses. When pooling data across trials within a block, we always excluded the first 14 trials after the first hit in each block (in both high and low reward blocks; see also *Time course of behavioral adjustments*, below).

Behavioral metrics. Due to the quasi-continuous nature of the task, we could not use classic signal detection theory (Green & Swets, 1966) to compute sensitivity (d') and choice bias (criterion). As alternatives, which are likewise orthogonal measures (**Fig. S2Q**), we computed "discriminatory response rate" and "overall response rate". We defined discriminatory response rate as:

$$R_S = \frac{N_{HIT}}{T_S} - \frac{N_{FA}}{T_N} \qquad \text{Eq. 1}$$

where N_{HIT} is the number of hit trials, N_{FA} is the number of false alarm trials, T_S is the total time a signal sound was played (in s) and T_N the total time a noise sound was played. We defined overall response rate as:

$$R_o = \frac{N_{HIT} + N_{FA}}{T_S + T_N} \qquad \text{Eq. 2}$$

Reward rate was defined as the percentage of trials that ended in a hit (lick during the signal). Reaction time on hit-trials was defined as the time from signal onset until the lick.

To characterize the theoretical relationship between discriminatory response rate and overall response rate (**Fig. S2Q**), and to calculate the optimal overall response rate in our task (**Fig. S2R**), we generated a simulated data set. Specifically, we generated synthetic trials that matched the empirical trials (noise duration was drawn from an exponential distribution with mean = 5 s; truncated at 11 s). We then systematically varied overall response rate by drawing random lick times from exponential distributions with various means (1 / rate) and assigned those (random) lick times to the synthetic trials. We varied the overall response rate (rate) from 0 to 1 licks / s, in steps of 100. In each iteration, the decision agent performed 500K simulated trials. For each iteration we then calculated the resulting reward rate and discriminatory response rate.

Time course of learning. To characterize animal's learning, we fitted the following function:

$$B(s) = a \cdot e^{-b \cdot s} + c \qquad \text{Eq. 3}$$

where B is a behavioral metric of interest, s is session number with respect to start phase 3, and a, b and c the free parameters of the fit.

Time course of behavioral adjustments. To calculate the speed of behavioral adjustments to changes in task utility, we fitted the following function:

$$B(t) = a \cdot \ln(t) + b \cdot t + c \qquad \text{Eq. 4}$$

where B is a behavioral metric of interest, t is trial number since first correct lick (hit) in a block, and a, b and c the free parameters of the fit. We then calculated the difference between the maximum and minimum of the fitted function and calculated the trial number for which 95% of this difference was reached. For overall response rate, discriminatory response rate and reward rate, this occurred on average at 15 trials after the first correct lick in a low-reward block (**Fig. 4B,E,H**). Therefore, when pooling data across trials within a block, we always excluded the first 14 trials after the first hit in each block (in both high and low reward blocks). We verified that our conclusions are not affected by specifics of the trial selection procedure (**Fig. S4E-H**).

Accumulation-to-bound modeling. We fitted the reaction time data with an accumulation-to-bound model of decision-making. The model was fitted to all data of all animals combined, but separably for the different block numbers. The model was fitted based on continuous maximum likelihood using the Python-package PyDDM (Shinn et al., 2020). We formulated a single accumulator model that describes the accumulation of noisy sensory evidence toward a single choice boundary for a go-response.

 In the "basic model", the decision dynamics were governed by leak and gaussian noise during noise stimuli, and additionally by the drift rate during the signal stimuli (**Fig. 5A,B**):

$$\Delta y = (-y \cdot k + s \cdot v) \cdot \Delta t + cdW \qquad \text{Eq. 5}$$

where y is the decision variable (black example trace in **Fig. 5B**), k is the leak and controls the effective accumulation time constant ($1/k$), s is the stimulus category (0 during noise sounds; 1 during signal sounds), v is the drift rate and controls the overall efficiency of accumulation of relevant evidence (coherence), and cdW is Gaussian distributed white noise with mean 0 and variance $c^2 \Delta t$. Evidence accumulation terminated at bound height a (go response) or at the end of the trial (no-go response), whichever came first. The starting point of evidence accumulation was fixed to 0.

 In the "attention lapse model", the decision dynamics were additionally governed by a attention lapse probability:

$$\Delta y = (-y \cdot k + s \cdot l \cdot v) \cdot \Delta t + cdW \qquad\qquad \text{Eq. 6}$$

where l is a Bernoulli trial, that determined with probability p the fraction of trials on which the relevant sensory evidence s was accumulated.

The "attention lapse + starting point variability model" was the same as the "attention lapse model", but the starting point of evidence accumulation was additionally uniformly distributed between 0 and sz. Fast errors are typically accounted for by allowing starting point of evidence accumulation to be variable (Laming, 1968).

The "full model" was the same as the "attention lapse model", but included a mixture rate, a binomial probability that determined the fraction of trials on which the decision dynamics were not governed by equation 6, but instead on which reaction times were randomly drawn from a gaussian distribution with mean μ and variance σ (μ and σ were fixed across block number). A similar dual process model was recently proposed for rats making perceptual decisions based on auditory information (Hernández-Navarro et al., 2021).

To calculate the optimal leak in the attentional intensity task (**Fig. S6D,E**), we generated a simulated data set. In our simulations, we generated synthetic trials that matched the empirical trials (noise duration was drawn from an exponential distribution with mean = 5 s; truncated at 11 s). We then systematically varied leak from 0 to 10, in steps of 0.2; the other parameters were the same as estimated from the empirical data (**Fig. 6**). In each iteration, we let a decision agent defined in this way "perform" 500K simulated trials. For each iteration we then calculated the resulting discriminatory response rate and reward rate.

Analysis of pupil data
All analyses were performed using custom-made Python scripts, unless stated otherwise.

Preprocessing. We measured pupil size and exposed eye area from the videos of the animal's eye using DeepLabCut (Mathis et al., 2018; Mridha et al., 2021). In approximately 1000 training frames randomly sampled across all sessions, we manually identified 8 points spaced at approximately evenly around the pupil, and 8 points evenly spaced around the eyelids. The network (resnet 110) was trained with default parameters. To increase the network's speed and accuracy when labeling (unseen) frames of all videos, we specified video-wise cropping values in the DeepLabCut configuration file that corresponded to a square around the eye. The pupil size (exposed eye area) was computed as the area of an ellipse fitted to the detected pupil (exposed eye) points. If two or more points were labeled with a likelihood smaller than 0.1 (e.g., during blinks), we did not fit an ellipse, but flagged the frame as missing data. We then applied the following signal processing to the pupil (exposed eye) time series of each measurement session: (i) resampling to 10 Hz; (ii) blinks were detected by a custom algorithm that marked outliers in the z-scored temporal derivative of the pupil size time series; (iii) linear interpolation of missing or poor data due to blinks (interpolation time window, from 150 ms before until 150 ms after missing data); (iv) low-pass filtering (third-order Butterworth, cut-off: 3 Hz); and (v) conversion to

percentage of the 99.9 percentile of the time series (McGinley, David, et al., 2015; Mridha et al., 2021).

Quantification of pre-trial pupil size. We quantified pre-trial pupil size as the mean pupil size during the 0.25 s before trial onset. Pre-trial pupil size was highest after previous hits (**Fig. S7A-C**), likely because the phasic lick-related pupil response did not have enough time to return to baseline. We thus removed (via linear regression) components explained by the choice (go vs. no-go) and reward (reward vs. no reward) on the previous trial. We obtained qualitatively identical results without removing trial-to-trial variations of previous choices and rewards from pre-trial pupil size measures (**Fig. S7I-K** & **Fig. S8A**). To capture how close the animal's arousal state on each trial was to the optimal level, we computed the absolute difference between each pre-trial's pupil size and the optimal size. Here, optimal size (30.0% of max) was defined as the pre-trial baseline pupil size for which discriminatory response rate, overall response rate and reward rate were maximal, and RT was minimal (mean across four green dots in **Fig. 7A-D**).

Analysis of walking data
The instantaneous walking speed data was resampled to 10 Hz. We quantified pre-trial walking speed as the mean walking velocity during the 2 s before trial onset. We defined walking probability as the fraction of trials for which the absolute walking speed exceeded 1.25 cm/s (**Fig. S7D**).

Statistical comparisons
We used a one-way repeated measures ANOVA to test for the effect of signal coherence (**Fig. 3B,C**). We used a 3 × 2 repeated measures ANOVA to test for the main effect of task utility and time-on-task (block number of a given reward magnitude), and their interaction (**Fig. 4C,F,I,L** & **Fig. 7G,K**).

We used Bayesian information criterion (BIC) for model selection and verified whether the added complexity of each model was justified to account for the data (**Fig. S5K**). A difference in BIC of 10 is generally taken as a threshold for considering one model a sufficiently better fit.

We used sequential polynomial regression analysis (Draper & Smith, 1998), to quantify whether the relationships between pre-trial pupil size and behavioral measures were better described by a 1st order (linear) up to a 5th order model (**Fig. 7A-D**):

$$\mathbf{Y} = \beta_0 1 + \beta_1 \mathbf{X} + \beta_2 \mathbf{X}^2 \qquad \text{Eq. 7}$$

where **Y** was a vector of the dependent variable (e.g., bin-wise discriminatory response rate), **X** was a vector of the independent variable (e.g., bin-wise pre-trial pupil size), and β as polynomial coefficients. To assess the amount of variance that each predictor accounted for independently, we orthogonalized the regressors prior to model fitting using QR-decomposition. Starting with the zero-order (constant) model and based on F-statistics (Draper & Smith, 1998), we tested whether

incrementally adding higher-order predictors improves the model significantly (explains significantly more variance). We tested zero-order up to second-order models.

We used mediation analysis to characterize the interaction between reward context, pre-trial pupil size and reward rate (**Fig. 8**). We fitted the following linear regression models based on standard mediation path analysis:

$$\mathbf{C} = i_0 1 + c\mathbf{R} \tag{Eq. 8}$$

$$\mathbf{P} = i_1 1 + a\mathbf{R} \tag{Eq. 9}$$

$$\mathbf{C} = i_2 1 + c'\mathbf{R} + b\mathbf{P} \tag{Eq. 10}$$

where **C** was a vector of the block-wise reward rate (fraction of correct licks), **R** was a vector of the block-wise reward context (0 for low reward; 1 for high reward), **P** was a vector of block-wise pre-trial pupil measures, and c, c', a, b, i_0, i_1 and i_2 were the free parameters of the fit. The parameters were fit using freely available Python software (Vallat, 2018).

All tests were performed two-tailed.

Data availability
Data will be made publicly available upon publication.

Code availability
Analysis scripts will be made publicly available upon publication.

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END NOTES

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Competing interests

The authors declare no competing interests.

Figure S1. (A) Histogram of noise durations. In most sessions (82.8 %), randomly drawn noise durations greater than 11 s were set to 11 s (resulting in the last bin in the histogram). In the remainder of sessions (17.2 %), these trials were turned into catch trials consisting of 14 seconds of noise.

Figure S2. (A) Histogram of experimental session number in learning phase 1. **(B)** Histogram of experimental session number in learning phase 2 (with respect to last session number in phase 2). **(C)** Histogram of experimental session number in phase 3. **(E)** RT on hit trials (Methods) across experimental sessions in learning phases 1 and 2; session numbers are with respect to the last session in phase 2. **(F)** RT on hit trials across experimental sessions in learning phase 3. **(C)** As F, but for the difference between high and low reward blocks. Dashed line, exponential fit (Methods). **(H)**. Overall response rate across experimental sessions in learning phase 3, collapsed across reward context. Dashed line, exponential fit (Methods). **(I)** As H, but separately for mice who performed at least 25 sessions in phase 3, and mice who performed at least 50 sessions in phase 3. **(J)** As I, but for the difference between the high and low reward blocks. **(K-M)** As H-J, but for discriminatory response rate. **(N-P)** As H-J, but for reward rate. **(Q)** Simulation of relationship between discriminatory response rate and overall response rate (Methods). **(R)** Simulation of relationship between reward rate and overall response rate (Methods). Red line, optimal overall response rate (reward rate peaks).

Figure S3. (A) Histogram of session identifiers. We excluded sessions 1-15 (first three weeks of training; dashed red line). **(B)** Histogram number of trials per session (after excluding sessions in panel A). We excluded sessions with fewer than 300 trials (dashed red line). **(C)** Histogram of median pupil size per session (after excluding sessions in panel B). We excluded sessions with a median pupil size smaller than 0.1 or larger than 0.7 (dashed red lines). We verified that the pupil data in these excluded sessions was of bad quality (due to closed eye, mucus, or improper lighting conditions). **(D)** Average pupil response (slope) aligned to licks (after excluding sessions in panel C). For every session, we computed the average lick-related pupil response as the mean pupil slope in the window 0 to 1 s from lick (grey window). **(E)** Histogram of session-wise lick-related pupil response magnitude (after excluding sessions in panel C). We excluded sessions with a pupil response smaller than 1% max per second (dashed red lines). We verified that this step removed additional bad quality pupil data (due to closed eye, mucus, or improper lighting conditions). **(F)** Fraction of trials containing a signal plotted against reward rate (after excluding sessions in panel E). Every data point is a unique session. We excluded sessions with a reward rate smaller than 15%. **(G)** As G, but for fraction of trial on which the animal licked on the y-axis. **(H)** Histogram of number of sessions per animal (after excluding sessions in panel F,G). We excluded animals with fewer than 5 remaining sessions.

Figure S4. (A) Overall response rate in the first (low reward) block of the session. Dashed lines, locked to block onset; solid lines, locked to first hit in block. **(B)** As A, but for discriminatory response rate (Methods). **(C)** As A, but for reward rate (Methods). **(D)** As A, but for reaction time (RT) on hit trials. **(E-H)** As main Fig. 4C,F,I,L, but when using all trials within a block (Methods). Main effects task utility are as follows:

Panel E: $F_{1,87} = 317.3$, $p < 0.001$. Panel F: $F_{1,87} = 63.0$, $p < 0.001$. Panel G: $F_{1,87} = 14.5$, $p < 0.001$. Panel H: $F_{1,87} = 638.3$, $p < 0.001$. **(I-L)** As main Fig. 4C,F,I,L, but when controlling for time on task. The white circles are the average of the two adjacent blocks of the same task utility. Main effects task utility are as follows: Panel I: $F_{1,87} = 274.0$, $p < 0.001$. Panel J: $F_{1,87} = 55.8$, $p < 0.001$. Panel K: $F_{1,87} = 17.9$, $p < 0.001$. Panel L: $F_{1,87} = 411.6$, $p < 0.001$. **(M,N)** As main Fig. 4F,I, but only for 82.8% of sessions without catch trials (Methods). Main effects task utility are as follows: Panel M: $F_{1,69} = 58.9$, $p < 0.001$. Panel N: $F_{1,69} = 9.6$, $p = 0.003$. **(O,P)** As main Fig. 4F,I, but only for 17.2% of sessions with catch trials (Methods). Main effects task utility are as follows: Panel M: $F_{1,43} = 15.0$, $p < 0.001$. Panel N: $F_{1,43} = 22.9$, $p < 0.001$. **(Q)** Histogram of trial number counted from first hit in a block (across all animals and experimental sessions). Dashed red line, cutoff for plotting in Fig. 4A,D,G,J.

Figure S5. (A). Top: simulated overall response rate as a function of bound height (*a*) and leak (*k*) (Methods). Remaining parameters match those estimated based on the empirical data collapsed across the high and low reward blocks. Bottom: simulated overall response rate as a function attention lapse probability (*p*) and drift rate (*v*). Remaining parameters match those estimated based on the empirical data collapsed across the high and low reward blocks. **(B-D)** As A, but for discriminatory response rate, reward rate and RT on hit trials, respectively. **(E)** Left: Reward rate (defined as % correct licks on all trials containing signal sounds) in the low reward blocks, separately for binned noise durations. Middle: RT distribution for correct licks (hits) in the low reward blocks. Right: RT distribution for incorrect licks (false alarms) in the low reward blocks. Black lines, "basic model" fit. In the "basic model", the decision dynamics were governed by leak and gaussian noise during noise stimuli, and additionally by the drift rate during the signal stimuli (Methods). Red arrows, the "basic model" failed to capture the shape of the RT distribution associated with correct licks, and failed to capture early RTs associated with incorrect licks in the low reward blocks. **(F)** As E, but for the high reward blocks. **(G,H)** As E,F, but for the "attention lapse model". The "attention lapse model" was the same as the basic model but included an attention lapse probability (Methods). Red arrow, the "attention lapse model" failed to capture early RTs associated with incorrect licks in the low reward blocks. **(I,J)** As E,F, but for "attention lapse + starting point variability model". The "attention lapse + starting point variability model" was the same as the attention lapse model, but the starting point of evidence accumulation was not fixed at 0 but was drawn from an uniform distribution (Methods). Red arrow, the "attention lapse + starting point variability model" still failed to fully capture early RTs associated with incorrect licks in the low reward blocks. **(K)** We compared the BIC between the four different models (Methods). The BIC for the "basic model" was used as a baseline for each dataset. Lower BIC values indicate a model that is better able to explain the data, considering the model complexity; a difference BIC of 10 is generally taken as a threshold for considering one model a sufficiently better fit. Formal model comparison based on Bayesian information criterion (BIC) favored the full model.

Figure S6. (A) Leak and drift rate estimates from the "basic model" (Methods), separately per block. **(B)** As A, but for the "attention lapse" model. **(C)** As A, but for the "attention lapse + starting point variability model" (Methods). **(D)** Simulated discriminatory response rate as a function of leak (k), separately for two sets of parameters that match those estimated based on the empirical data in the high and low reward blocks. Orange and blue dashed lines, estimated leak in the high and low reward blocks, respectively. **(E)** As D, but for simulated reward rate.

Figure S7. (A) Pupil size across time on hit trials, separately for high and low reward blocks. Left, locked to licks; right, locked to next trial's onset. **(B)** As A, but on false alarm trials. **(C)** As A, but for miss trials. Left, locked to trial offset (end of 3-s signal sound). **(D)** Histogram of pre-trial walking velocity (across all animals and experimental sessions; Methods). Red line, cutoff for defining walking. **(E)** Histogram of pre-trial pupil size (across all animals and experimental sessions), separately for still and walking trials. **(F)** Pre-trial pupil size in the first (low reward) block of the session. Dashed lines, locked to block onset; solid lines, locked to first hit in block. **(G)** Pre-trial pupil size across three high and three low reward blocks in the same experimental session. Dashed lines, locked to block onset; solid lines, locked to first hit in block. **(H)** As G, but for absolute distance from optimal pre-trial pupil size (Methods). **(I)** Pre-trial pupil size without previous trial's outcome regressed out (Methods) across three high and three low reward blocks in the same experimental session. Dashed lines, locked to block onset; solid lines, locked to first hit in block. **(J)** As I, but collapsed across blocks of same reward magnitude. **(K)** As I, but collapsed across trials within a block. Stats, 2-way repeated measures ANOVA (factors task utility [high vs. low] and time-on-task [1, 2, 3]); main effect task utility: $F_{1,87} = 35.2$, $p < 0.001$; main effect time-on-task: $F_{2,174} = 42.9$, $p < 0.001$; interaction effect: $F_{2,174} = 1.3$, $p = 0.283$. **(L-N)** As G-I, but for standard deviation of pre-trial pupil size. Main effect task utility: $F_{1,87} = 108.8$, $p < 0.001$; main effect time-on-task: $F_{2,174} = 25.3$, $p < 0.001$; interaction effect: $F_{2,174} = 8.4$, $p < 0.001$. **(O-Q)** As G-I, but for walk probability (Methods). Main effect task utility: $F_{1,87} = 53.2$, $p < 0.001$; main effect time-on-task: $F_{2,174} = 0.1$, $p = 0.935$; interaction effect: $F_{2,174} = 3.6$, $p = 0.029$. All panels: shading or error bars, 68% confidence interval across animals (N=88; n=1983 sessions).

Figure S8. (A) With pre-trial pupil size as mediation, fitted regression coefficients of the a-path (blue), b-path (red) and the indirect path (mediation; pink). Indirect path tested against 0: $p < 0.001$ (Wilcoxon signed-rank test). **(B)** As A, but for pre-trial pupil size with previous trial's outcome regressed out (Methods) as mediator. **(C)** As A, but for standard deviation of pre-trial pupil size as mediator. **(D)** As A, but for fraction of walked trials as mediator. All panels: error bars, 68% confidence interval across animals (N=88; n=1983 sessions).