Humans prioritize walking efficiency or walking balance based on environmental risk

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Abstract

In human gait, the body’s mechanical energy at the end of one step is reused to achieve forward progression during the subsequent step, thereby reducing the required muscle work. During the single stance phase, humans rely on the largely uncontrolled passive inverted pendular motion of the body to perpetuate forward motion. Since inverted pendula are unstable, these passive body dynamics, while improving walking efficiency, also indicate that the individual will be less able to withstand an external perturbation during the single stance phase. Here we test the novel hypothesis that humans manipulate passive anterior-posterior (AP) stability via active selection of step length to either achieve energy-efficient gait or to improve stability when balance is threatened. We computed the AP margin of stability, which quantifies the passive dynamic stability of gait, for multiple steps as healthy young adults (N=20) walked on a clear and on an obstructed walkway. Participants used passive dynamics to achieve energy-efficient gait for all but one step; when crossing the obstacle with the leading limb, AP margin of stability was increased and indicated cautious gait, reflecting the greater threat to balance arising from a potential trip. Furthermore, AP margin of stability increased while approaching the obstacle, indicating that humans employ a proactive strategy of manipulating passive dynamics to meet the demands of the locomotor task. Finally, the step length and the center of mass motion co-varied to maintain the AP margin of stability for all steps in both tasks at the specific values for each step. We conclude that humans actively regulate step length to maintain specific levels of passive stability for each step during unobstructed and obstructed gait.
1. Introduction

On a clear, straight path, humans reduce the energy required for walking by selecting appropriate step length [1, 2]. The selected step length ensures that the kinetic energy at the end of a step is sufficient to passively rotate the body over the new stance foot, thereby achieving forward progression at low energetic cost. That is, humans rely on the largely uncontrolled passive motion of the body during the single stance phase of gait to perpetuate forward motion. This motion during the single stance phase resembles that of an inverted pendulum, and given that passive inverted pendula are unstable, the inverted pendular phase of walking may have the property that neighboring trajectories of the body’s center of mass (CoM; abbreviations in Table 1) diverge. Therefore, although the overall gait cycle is usually stable (the divergence of CoM trajectories during the inverted pendular phase is corrected during the step to step transition via foot placement and/or push-off adjustments [3]), the largely passive motion during the single stance phase suggests that individuals will be less able to resist external perturbations and may be more susceptible to falling due to disturbances encountered during this phase. Therefore, although not aggressively controlling every phase in the gait cycle improves energy efficiency, it may also increase the threat to balance.

Given the zero-sum contributions of the passive inverted pendular motion to energy efficiency and stability, humans likely modulate the passive dynamics to either enhance forward progression or prioritize balance, as the context demands. The threat to balance will be low during unobstructed, straight-line walking, and therefore, passive dynamics will be used to improve efficiency. In contrast, when a locomotor task involves a higher risk of a forward loss of balance, e.g., when risk of tripping is higher, the passive dynamics will be more stable.

Furthermore, stability changes in motor behaviors cannot occur instantaneously, but must evolve over a characteristic time determined in part by the inertia of the body [4]. Therefore, we argue that a shift along the efficiency-stability spectrum will occur over multiple steps – at least for locomotor tasks that afford the time and space for such a shift to occur. For example, while crossing a visible, stationary obstacle, gait stability is altered not only when the feet cross the obstacle (i.e., crossing steps). Rather, changes in stability will be evident in the steps leading up to the obstacle (i.e., approach steps) to facilitate the transition from
unobstructed to obstructed gait. In the approach steps, visual information about the hazard is being gathered [5, 6] and spatio-temporal gait characteristics (gait speed and foot placement variability) are modified [7]. However, proactive stability adaptations in the anterior-posterior (AP) direction during approach have not been examined, and it is likely that these stability adaptations are a critical component of maintaining forward progression through challenging environments.

We used the margin of stability in the anterior-posterior direction (MOSAP), a stability metric derived from the inverted pendulum model of gait [8], to investigate these ideas. MOSAP at heel contact during unobstructed gait is negative [9-11] indicating energy-efficient walking. Further, MOSAP is higher while crossing an obstacle compared to unobstructed gait [12, 13], suggesting that passive stability is improved when the risk of tripping is higher [14]. Since the step length influences the passive stability (MOSAP is a function of step length and the body’s motion), we argue that humans actively select step length to maintain MOSAP in a given locomotor context.

Therefore, our primary goal was to establish that humans control passive dynamic stability, which will be reflected in the control of MOSAP during unobstructed as well as obstructed walking. We propose and test the novel hypothesis that the central nervous system responds to changes in the body’s motion with a corresponding correction in step length so that the MOSAP itself is invariant at each heel contact. MOSAP will be maintained at different values during unobstructed vs. obstructed walking. Our second goal was to quantify any proactive adaptations in MOSAP while approaching an obstacle. MOSAP at heel contact is the distance from the anterior boundary of the base of support (the leading heel) to the extrapolated center of mass, or XcoM, which reflects the center of mass (CoM) state [8, 15]. To address our first goal, we employed the uncontrolled manifold (UCM) method [16]. For each heel contact, we computed the synergy index that quantifies the co-variation in the step length and the XcoM that maintains MOSAP. A positive synergy index indicates that MOSAP was actively controlled, i.e., stabilized at the specific across-trial mean MOSAP for that step. A higher value indicates a stronger synergy or higher stability of MOSAP. We emphasize that stability of MOSAP is different from the stability of gait. MOSAP is the measure of gait stability. In contrast, the synergy index indicates the efficacy of control at stabilizing or maintaining MOSAP at a specific
value for a given step. To address our second goal, i.e., to identify any proactive changes in gait stability, we compared the MOS\textsubscript{AP} values for the steps leading up to, while crossing and then resuming unobstructed gait after crossing an obstacle.

We hypothesized that the synergy index will be greater than zero, indicating that the step length and the XcoM co-vary to stabilize MOS\textsubscript{AP} for all steps in both tasks (H1). In particular, we expect a positive synergy index for both positive and negative MOS\textsubscript{AP} values (for various steps). Next, we hypothesized a task by step interaction for the synergy index (H2). The synergy index will not be different across tasks (unobstructed and obstructed) for the steps at the start and end of the walkway, but the synergy index will be lower while crossing an obstacle placed in the middle of the walkway. The lower synergy index will reflect the greater motor demands associated with the crossing steps; larger muscle activations required for stepping over the obstacle [17] will be associated with greater noise [18], which will make stabilization more difficult. Finally, we hypothesized a task by step interaction for MOS\textsubscript{AP} (H3). The MOS\textsubscript{AP} will not be different across tasks for the steps at the start and end of the walkway, but the MOS\textsubscript{AP} will be higher for the approach steps 1-2 steps before the obstacle and for the crossing steps. These changes are consistent with prioritization of safety over energy optimality [13, 19, 20].

Table 1. Abbreviations.

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Description</th>
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<tr>
<td>Anterior-posterior</td>
<td>AP</td>
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<tr>
<td>Medial-lateral</td>
<td>ML</td>
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<tr>
<td>Foot placements</td>
<td>fp</td>
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<tr>
<td>Center of mass</td>
<td>CoM</td>
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<tr>
<td>Center of mass velocity</td>
<td>$V_{\text{CoM}}$</td>
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<tr>
<td>Leg length</td>
<td>$l$</td>
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<tr>
<td>Acceleration due to gravity</td>
<td>$g$</td>
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<tr>
<td>Base of support</td>
<td>BOS</td>
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<tr>
<td>Extrapolated center of mass</td>
<td>XcoM</td>
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Margin of stability in anterior-posterior direction \[ \text{MOS}_{\text{AP}} \]
Uncontrolled manifold \[ \text{UCM} \]
Orthogonal manifold \[ \text{ORT} \]
Synergy index \[ \Delta V \]
Synergy index z transformed \[ \Delta V_z \]
Variance along the uncontrolled manifold \[ V_{\text{UCM}} \]
Variance along the orthogonal manifold \[ V_{\text{ORT}} \]

2. Materials and Methods

2.1 Participants

Twenty-six healthy young adults participated in the study. We excluded six participants due to poor kinematic tracking. Data from 20 participants (14 females, 22.3 ± 3.7 years, 1.7 ± 0.1 m, 66.9 ± 14.6 kg) were used for analysis. All participants walked without aid, had no orthopedic, neuromuscular, or dementia disorders, and were independent in daily activities. Vision was normal or corrected-to-normal. The study was approved by the University’s Institutional Review Board, and all participants provided written informed consent.

2.2 Equipment and Procedures

Participants walked at their self-selected speed on a 6.0 m walkway and stepped over an obstacle when present (Fig. 1A). The obstacle was 100 cm wide × 0.4 cm deep. The height of the obstacle was scaled to 25% of the participant’s leg length. The obstacle was made of black Masonite and designed to tip if contacted. The starting position was determined for each participant such that they took five steps before reaching the obstacle, crossed the obstacle with the right leg first and stopped three to four steps later (Fig. 1A).

Participants performed 20 trials each of walking with an obstacle (obstacle-crossing task) and walking without an obstacle (no obstacle task). We collected kinematic data at 100 Hz with a motion capture system (Vicon Vero, Oxford, UK) with marker clusters placed bilaterally on the lower back, thigh, shank, and foot. We digitized the joint centers and posterior aspect of
the heels to identify their locations relative to the marker clusters. We also digitized the top edge of the obstacle to identify its position.

**Figure 1. Experimental task and basic definitions.** Illustration of foot placements while approaching (fp₄ to fp₋₁), crossing (fp₊₁ and fp₊₂) and after crossing (fp₊₃) the obstacle, and of steps while approaching (Step₋₃ to Step₋₁), crossing (Step₀ and Step₊₁) and after crossing (Step₊₂) the obstacle (A). Definitions of the extrapolated center of mass (XcoM) and margin of stability, MOSₚ. Step length, XcoM and MOSₚ are computed at the moment of lead heel contact in a coordinate frame located where the rear heel contacted the ground (B).
2.3 Analysis

Some trials were discarded due to poor kinematic tracking. To have the same number of trials for all participants and tasks, we selected 15 trials with good kinematic data. Fifteen trials are sufficient for reliable quantification of the synergy variables [21]. We filtered all kinematic data using a zero-lag, 4th order, low-pass Butterworth filter with a cut-off of 7 Hz. We identified seven foot placements (Fig. 1A) using the AP position of the heel [22]. We quantified spatiotemporal gait parameters and margin of stability at heel contact at the seven foot placements (fp-4 to fp+3) and six steps (Step-3 to Step+2; Fig. 1A). Step length was defined as the distance between two consecutive heel contacts. CoM position was computed as the centroid of the triangle formed by the left and right anterior superior iliac spines and the center of the left and right posterior superior iliac spines [23]. CoM velocity was obtained by differentiating the CoM position data. The extrapolated center of mass (XcoM) was calculated in the sagittal plane as [15]:

\[ X_{CoM} = CoM + \frac{V_{CoM}}{g\sqrt{T}}, \]

where CoM is the anterior-posterior CoM position, \( V_{CoM} \) is the anterior-posterior CoM velocity, \( g \) is the acceleration due to gravity, and \( l \) is the participant’s leg length (Fig. 1B). Leg length was calculated as the sagittal-plane distance between the CoM and the ankle of the limb that contacted the ground. We used the average of the leg length values obtained from the 15 trials for each step [24]. We computed \( MOS_{AP} \) at the instant of leading heel contact in a coordinate frame fixed at the location of the rear heel contact (Fig. 1B):

\[ MOS_{AP} = \text{Step length} - X_{CoM}, \quad (1) \]

i.e., the distance from the anterior boundary of the base of support (BOS), defined by the position of the leading heel, to the XcoM. Negative \( MOS_{AP} \) (XcoM ahead of the anterior boundary of the BOS) indicates that the body possesses sufficient energy to passively rotate over the upright position and fall forward. This is interpreted as instantaneous passive instability in the gait. In contrast, positive \( MOS_{AP} \) values (XcoM is behind the anterior boundary of the BOS) indicate that the body does not possess sufficient energy to rotate beyond the
upright position, and it will eventually fall backward. This is interpreted as instantaneous
passive stability, presumably because the rear leg can arrest a backward fall.

We used the uncontrolled manifold (UCM) analysis to quantify the synergy stabilizing
MOS\textsubscript{AP} at heel contact. A synergy is co-variation in a redundant sets of input body variables that
maintains important output variables that define task performance. The UCM method has been
widely used to quantify the synergistic covariation in body variables in a variety of human
movements including gait ([25, 26]; see [27, 28] for recent reviews). Importantly, in addition to
identifying task-specific covariation, the UCM method identifies the salient task variables
controlled by the nervous system.

Here, we use the UCM method to evaluate the hypothesis that the input variables – step
length and XcoM, co-vary to stabilize the output variable, i.e., MOS\textsubscript{AP}. We performed the
analysis separately for each step for both tasks. We first obtain from the constraint equation
(Eqn. 1), the Jacobian matrix that relates small changes in the step length and XcoM to changes
in MOS\textsubscript{AP}: \( J = \begin{bmatrix} 1 & -1 \end{bmatrix} \). The one-dimensional null space of this Jacobian defines the UCM, and its
one-dimensional compliment defines the orthogonal (ORT) manifold. We pool the across-trial
step length and XcoM data for a particular step. The deviation in the step length and XcoM data
for each trial from the across-trial mean is projected onto the UCM and the ORT manifolds. The
variances in these projections are the \( V_{UCM} \) and the \( V_{ORT} \), respectively. These variance
components yield the synergy index:

\[
\Delta V = \frac{V_{UCM} - V_{ORT}}{\left(\frac{V_{UCM} + V_{ORT}}{2}\right)}.
\]

The synergy index \( \Delta V \) has a threshold value of zero. When \( \Delta V > 0 \), \( V_{UCM} > V_{ORT} \). In general, this
implies that the control is organized so that most of the variability in the inputs is channeled
along the UCM, and therefore, it does not alter task performance, i.e., the output. Here, \( \Delta V > 0 \)
implies that the step length and XcoM covary to stabilize MOS\textsubscript{AP}, and we conclude that MOS\textsubscript{AP} is
a controlled variable. Conversely, when \( \Delta V < 0 \), \( V_{UCM} < V_{ORT} \). This implies that most of the
variability in the inputs alters task performance. Finally, \( \Delta V = 0 \) indicates that there is no task-
specific co-variation in the step length and XcoM. Here, \( \Delta V \leq 0 \) indicates that MOS\textsubscript{AP} is not a
controlled variable.
The synergy index $\Delta V$ ranges from -2 to 2. Therefore, it was z-transformed for statistical analysis [26, 29]:

$$\Delta V_z = \frac{1}{2} \log \left[ \frac{2 + \Delta V}{2 - \Delta V} \right].$$

Note that $\Delta V = 0$ translates to $\Delta V_z = 0$. We report $\Delta V_z$ values in the Results section and use $\Delta V_z$ values to draw inferences, consistent with most previous studies [27].

### 2.4 Statistical analysis

To determine whether the synergies were present, we performed separate, one-sample t-tests to test if $\Delta V_z$ was significantly different from zero for each step in the two tasks (H1). To determine whether the gait task and foot placement affected the synergy index (H2) and MOSAP (H3), we performed a two-way (task × step) repeated measures ANOVA on these variables. To identify the source of changes in the synergy index and in MOSAP, we performed the same ANOVA separately on the variance components ($V_{UCM}$, $V_{ORT}$), and on the CoM position, CoM velocity at heel contact and step length, respectively. For all ANOVA tests, we fit a generalized linear model with nested random effects. For the ANOVA on UCM variables and step length, the participant was the random effect. For all other variables, the trial number within each participant was the random effect. Tukey-Kramer adjustments were used to perform the following planned pairwise comparisons: (1) across-task comparison at each of the six steps (or seven foot placements), and (2) all across-step (or foot placement) comparisons for the obstacle-crossing task only. All analyses were performed using the PROC GLIMMIX procedure in SAS 9.4 (Cary, NC, USA) with significance set at 0.05.

### 3. Results

Figure 2 shows data from one participant and represents the overall results. The figure illustrates (1) the changes in various outcome variables while approaching, crossing, and resuming gait after crossing an obstacle, and (2) how the variables compare with unobstructed gait for each step. All outcome variables showed a task × step interaction (supporting H2 and...
indicating that the pattern of changes in the variables across steps was different for the obstruction-crossing task compared to the no obstacle task. The largest across-task changes were observed in all outcomes for the two crossing steps (Step₀ and Step₊1), and across-task changes were apparent in some outcomes in the approach to the obstacle (Step₋₃ to Step₋₁). All variables showed across-step changes for the obstacle-crossing task. The synergy index was greater than zero, indicating that the step length and the XcoM co-varied to stabilize MOSₐp for all steps in both tasks (supporting H1). In the detailed results below, we first present the results for the UCM outcome variables describing the stability of MOSₐp. Then we present the results for MOSₐp, followed by results for the variables that constitute MOSₐp: CoM position relative to front heel, CoM velocity at heel contact, and step length.
Figure 2. Representative data from one participant. Figure illustrates changes in various outcomes while approaching and crossing an obstacle, and then resuming unobstructed gait (blue ellipses). Steps during unobstructed gait are included for comparison (red ellipses). The 45° line separates the regions of positive and negative MOS_{AP}; the white region above the line represents passively unstable behavior, and the gray region below the line represents passively stable behavior. The 45° line also represents the direction of the uncontrolled manifold (UCM). Variations in step length and XcoM along this direction do not change MOS_{AP}. The ellipses are centered at the centroid of the across-trial data for each step, and the major axes are aligned with the 45° line. However, the flatness of the ellipses is representative. Changes in mean values of the MOS_{AP} are reflected in the position of the ellipses in each chart. The flatness of the ellipse reflects the synergy index, with flatter ellipses indicating higher synergy indices that reflect stronger covariation between the step length and XcoM.
3.1 UCM variables

Synergy index

The synergy index ($\Delta V_z$) was significantly greater than zero at all steps for both tasks ($t_{19} < 15.97, p < 0.01$; Fig. 3A).

There was a task $\times$ step interaction for the synergy index $\Delta V_z$ ($F_{5,209} = 2.89, p = 0.015; \eta_p^2 = 0.3$; Fig. 3A). Post-hoc comparisons across tasks revealed that $\Delta V_z$ was lower during the obstacle-crossing task compared to the no obstacle task for the lead (step0) and trail crossing steps (step+1). Post-hoc comparisons across steps for the obstacle-crossing task revealed that $\Delta V_z$ was lower at the lead crossing step (step0) compared to all non-crossing steps except step-2, and $\Delta V_z$ was lower at the trail crossing step (step+1) compared to the last step (step+2).

Variance components

There was a task $\times$ step interaction for $V_{UCM}$ ($F_{5,209} = 3.12, p = 0.009; \eta_p^2 = 0.3$; Fig. 3B). Post-hoc comparisons across tasks revealed that $V_{UCM}$ was higher for the obstacle-crossing task compared to the no obstacle task at all but the first two steps (step-3 and step-2). Post-hoc comparisons across steps for the obstacle-crossing task revealed that $V_{UCM}$ was higher at the lead crossing step (step0) compared to the first two steps (step-3 and step-2).

There was a task $\times$ step interaction for $V_{ORT}$ ($F_{5,209} = 16.51, p < 0.001; \eta_p^2 = 0.3$; Fig. 3C). Post-hoc comparisons across task revealed that $V_{ORT}$ was higher during the obstacle-crossing task compared to the no obstacle task at the lead (step0) and trail (step+1) crossing steps. Post-hoc comparisons across steps for the obstacle-crossing task revealed that $V_{ORT}$ was higher at the lead crossing step (step0) compared to all other steps, and $V_{ORT}$ was higher at the trail crossing step (step+1) compared to all steps except the lead crossing step (lower for step+1 compared to step0) and the preceding step (step-1; no significant difference).
Figure 3. Outcomes of the synergy analysis. Synergy index (A), $V_{UCM}$ (B), and $V_{ORT}$ (C). Data are across-subject means ($N=20$), and error bars denote standard error. Asterisks denote significant across-task differences at that step ($p < 0.05$). Across-step pairwise comparisons for the obstacle-crossing task are indicated by the row of letters above the horizontal axis for each panel. Steps that do not have letters in common are significantly different from each other (i.e., A is different from B, but A is not different from AB).
3.2 Margin of stability

**MOS$_{AP}$**

We observed a task × step interaction for MOS$_{AP}$ ($F_{6,4167} = 886.89$, $p < 0.001$; $\eta^2_p = 0.9$; Fig. 4A). Post-hoc comparisons across tasks revealed that MOS$_{AP}$ was higher (more stable) for the obstacle-crossing task than the no obstacle task at all except the first (fp-4) and last two foot placements (fp+2 and fp+3). MOS$_{AP}$ was more negative (less stable) for fp+2 (after trail foot crossing) for the obstacle-crossing task. All pair-wise across-step comparisons for the obstacle-crossing task are depicted in Fig. 4A. For brevity, we describe only some of the significant differences. Changes in MOS$_{AP}$ occurred before the obstacle was reached; MOS$_{AP}$ was higher (less stable) for fp-1 relative to the two preceding foot placements. For the two crossing steps, MOS$_{AP}$ first changed from negative to positive for fp+1, and then changed to the most negative value for fp+2 relative to all foot placements.

**CoM position relative to the rear heel**

A task × step interaction was observed for the CoM position relative to the rear heel ($F_{6,4167} = 391.20$, $p < 0.001$; $\eta^2_p = 0.9$; Fig. 4B). Post-hoc comparisons across tasks revealed that CoM was closer to the rear heel at the foot placements of all approach steps and the lead crossing step (fp-4 to fp+1) for the obstacle-crossing task than the no obstacle task. Conversely, CoM was closer to the front heel at the foot placement for the trail crossing step (fp+2) for the obstacle-crossing task. All pair-wise across-step comparisons for the obstacle-crossing task are depicted in Fig. 4B. For brevity, we describe only some of the significant differences. CoM position changed for the last three foot placements. The CoM was closer to the rear foot at the foot placement for the lead crossing step (fp+1). It shifted forward, so that it was closer to the front heel at the foot placement for the trail crossing step (fp+2). Finally, for the last step (fp+3), CoM position was consistent with that for the approach steps.

**CoM velocity at heel contact**
We observed a task × step interaction for the CoM velocity at heel contact ($F_{6,4167}=161.52, p < 0.001; \eta_p^2 = 0.8$; Fig. 4C). Post-hoc comparisons across tasks revealed that the CoM velocity was lower for the obstacle-crossing task compared to the no obstacle task at all but the first and the last foot placements (fp-4 and fp+3). Post-hoc comparisons across steps for the obstacle-crossing task revealed that the CoM velocity was lower at the first (fp-4) and last (fp+3) foot placement compared to other foot placements, except at the lead foot crossing (fp+1), where the CoM velocity was lower compared to all other foot placements.

**Step length**

We observed a task × step interaction for the step length ($F_{5,3569} = 149.09; p < 0.001; \eta_p^2 = 0.9$; Fig. 4D). Post-hoc comparisons across tasks revealed that step length was longer during the obstacle-crossing task compared to the no obstacle task at the lead (step0) and trail crossing (step+1) steps. Post-hoc comparisons across steps for the obstacle-crossing task revealed that step length increased one step before the crossing step (step-1) compared to the first step (step-3). Step length was highest for the lead crossing step (step0), and then it shortened for the trail crossing step (step+1), but remained longer than all steps except step0. Finally, step length was the shortest for the last step (step+2) compared to all other steps.
Figure 4. MOS_{AP} and its components. MOS_{AP} (A), CoM position at heel contact (B), CoM velocity at heel contact (C) and step length (D). Data are across-subject means (N=20), and error bars denote standard error. Asterisks denote significant task difference at that step (p < 0.05). Across-step pairwise comparisons for the obstacle-crossing task are indicated by the row of letters above the horizontal axis for each panel. Steps that do not have letters in common are significantly different from each other (i.e., A is different from B, but A is not different from AB).
4. Discussion

Our goals were to establish that MOS\textsubscript{AP} is actively controlled during unobstructed as well as obstructed walking, and to quantify any proactive adaptations in MOS\textsubscript{AP} during obstacle crossing. We report the novel finding that the central nervous system responds to changes in the body’s motion with a corresponding correction in step length so that the MOS\textsubscript{AP} itself is invariant at each heel contact (supporting H1). We also observed that the synergy index was lower while crossing an obstacle compared to earlier and later steps and compared to the corresponding steps during unobstructed gait (supporting H2). Finally, we observed proactive changes in MOS\textsubscript{AP} in anticipation of a threat to balance; MOS\textsubscript{AP} changed across steps for unobstructed versus obstructed gait (supporting H3). We argue below that (1) the positive synergy indices indicate that the passive stability is not a byproduct of another process, but that the step length is actively controlled to exploit the passive dynamics to achieve forward progression at low energetic cost; and (2) the proactive changes in the mean MOS\textsubscript{AP} for the obstacle-crossing task reflect a stability-efficiency tradeoff. Because the MOS\textsubscript{AP} quantifies the passive dynamic stability of gait, our results indicate that humans employ a passive dynamics manipulation strategy to exploit the passive AP body motion to meet specific ends dictated by the locomotor task.

4.1 Active control of MOS\textsubscript{AP} during unobstructed and obstructed gait

The synergy index provides evidence for the control of MOS\textsubscript{AP}

The first major finding of this study is that MOS\textsubscript{AP} is a controlled variable for obstructed as well as unobstructed gait (\(\Delta V_z > 0\) for all steps; Fig. 3A). In particular, the synergy index remains significantly larger than zero, even though the input variables that define the MOS\textsubscript{AP} change over multiple steps for the obstacle-crossing task (Figs 2 and 4), and even when the gait is passively unstable (MOS\textsubscript{AP} < 0 for all but one step in our data). Thus, the UCM analysis provides strong quantitative evidence that MOS\textsubscript{AP} is controlled.

The variance components (Figs 3B, 3C) provide information regarding the underlying processes that stabilize MOS\textsubscript{AP}. Higher \(V_{ORT}\) indicates higher variability in MOS\textsubscript{AP}, whereas...
higher $V_{UCM}$ indicates greater compensatory covariance between XcoM and step length. We observed that MOS$_{AP}$ is more variable for the crossing steps (up to 205% increase in $V_{ORT}$ compared to earlier steps; Fig. 3C). This likely arises from the larger muscle activations and joint moments required for the crossing steps compared to unobstructed steps [17, 30]. Higher activations would increase signal-dependent noise [18], which will lead to more variable MOS$_{AP}$. However, this increase is offset by an increase in $V_{UCM}$ (up to 103% increase compared to earlier steps; Fig. 3B). This compensation leads to MOS$_{AP}$ stabilization overall (Fig. 3A).

**Does the synergy arise from passive mechanics, or do neural mechanisms indicate active control?**

It is unlikely that passive mechanics of the gait cycle alone can explain the positive synergy indices that we observed. It is indeed likely that mechanics contribute; for example, a greater push off force would result in a more anterior XcoM at the next heel contact, but it would also tend to produce longer steps [2], thereby helping to maintain MOS$_{AP}$. However, the step length is not entirely determined by a passively swinging leg. Rather, activity in the leg muscles and power at the hip and knee joints indicate active control of the forward swinging limb, which will alter the step length from what a passively swinging limb would yield [31]. It is plausible that variations in muscle lengths from their reference values, arising from variations in push off forces, will engage spinal stretch reflexes that will alter step length and contribute to the observed MOS$_{AP}$ synergy [32]. This explanation is consistent with the view that for steady state, level gait, humans rely on spinal feedback for control in the AP direction [33, 34].

The contribution of neural mechanisms to the MOS$_{AP}$ synergy may be even greater for obstructed gait. We observed large fluctuations in the MOS$_{AP}$ over the approach and crossing steps (174% increase for fp+1 over fp-1, and a 292% decline for fp+2 over fp+1; Fig. 4A). Nevertheless, the synergy index, although lower (38% decline for Step0 relative Step-1; Fig. 3A), remained positive. The positive synergy index despite large fluctuations in related variables over consecutive steps suggests the involvement of supraspinal mechanisms. Indeed, supraspinal centers are involved in the control of the obstacle crossing steps [17]. Spinal reflex responses in the stance leg flexors are enhanced, likely due to increased activity in the
prefrontal cortex, in preparation for swinging the leg over the obstacle. Furthermore, the
prefrontal cortical activity remains enhanced (compared to unobstructed walking) while
swinging the leg over the obstacle [17]. It is also known that visual information about the
obstacle is gathered during approach and used to alter gait characteristics [5, 6]. Gathering and
using visual information also implicates higher brain centers in the control of obstructed gait,
supporting our view that the MOS\textsubscript{AP} synergy arises from spinal and supraspinal neural circuits.
We note both spinal and supraspinal structures are frequently mentioned as candidate
neurophysiological bases of synergies [35], although the specific mechanisms are unknown.

Our ideas parallel a similar proposal by Dingwell and colleagues. They investigated step-
to-step changes in the MOS in the medio-lateral (ML) direction in externally destabilized
environments and argued that MOS\textsubscript{ML} is controlled during level walking [24, 36, 37]. The focus
of previous research on ML stability – versus AP stability – is consistent with the view that level
gait requires more control along the ML direction, and minimal control along the AP direction
[33]. The UCM analyses performed here show that the MOS is also controlled in the AP
direction by regulating step length – not only in gait tasks that require proactive adaptations,
but also during unobstructed gait.

4.2 Proactive changes in MOS\textsubscript{AP} and the compromise between
stability and energy efficiency

The second major finding of this study is that the MOS\textsubscript{AP} changes while approaching the
obstacle. When compared to unobstructed gait, greater stability was apparent three steps
before the obstacle (Fig. 4A). Changes in MOS\textsubscript{AP} during approach and crossing resulted from
reduced speed, a more posterior CoM, and increased step length for some steps (Figs. 4B, 4C,
4D). Previous work has demonstrated that changes in MOS\textsubscript{AP} and MOS\textsubscript{ML} were evident during
the swing phase immediately prior to taking unnaturally long or quick steps [38], and in MOS\textsubscript{ML}
one step before reaching the obstacle [39]. Here we extend this finding and demonstrate that
MOS\textsubscript{AP} changes several steps before reaching the obstacle, indicating that the transition from
unobstructed to obstructed gait occurs over several steps.
Our findings extend the argument that passive dynamic stability is modulated in response to perceived risk [14, 20]. For example, the substantive increase in MOSAP for the lead crossing step (Figs. 2, 4A) reflects cautious gait and may be a preemptive strategy against a potential trip that will lead to a forward fall [40]. Similarly, the even-more-substantive transition back to the least stable passive dynamics (lowest MOSAP; Fig. 4A) following the trail crossing step may reflect the reduced risk of a forward fall after the trail foot has crossed the obstacle, and the exploitation of passive dynamics to propel the body forward to regain gait speed.

These fluctuations in passive dynamic stability increase the energetic cost of locomotion. The increase in MOSAP over approach steps, and especially the positive MOSAP for the crossing step, indicates that the trailing leg must push off more so that the body can rotate about and beyond the stance ankle. Furthermore, the lead crossing step (step0) is a slower and longer step (Figs 3C, 3D), which is inconsistent with the typical combination of a slower and shorter step during unobstructed gait which reduces energetic cost [1, 41]. Therefore, our results reflect a tradeoff between stability and energy efficiency, consistent with similar arguments offered in the context of stair descent [20], and model-based optimization computations of obstacle crossing behaviors [19].

In sum, inspecting changes in MOSAP across tasks and steps leads to the conclusion that MOSAP is proactively adjusted (1) during the approach, likely to facilitate the transition from unobstructed gait to the movements required to clear the obstacle, (2) while crossing an obstacle, likely to prioritize safety over energy optimality, and (3) when resuming level gait to regain gait speed. The large fluctuations in MOSAP reflect a tradeoff between stability and energy efficiency.

4.3 Limitations

We estimated the CoM location using four pelvis markers [23]. A rigorous whole-body model could have provided slightly different estimates of the CoM motion. However, these differences would influence MOSAP similarly across all conditions, and using a different method to obtain CoM kinematics would likely yield similar qualitative results and overall conclusions,
especially given the large effect sizes for all our outcome variables. We also observed effects of gait initiation and termination in our data. Gait was initiated one step before the examined steps, and gait was terminated one or two steps after the trail crossing step. Using a longer walkway – with more steps before and after the obstacle – may alter the values of our outcome variables. We do not expect that these changes will influence our key conclusions (control of and proactive changes in MOSAP). However, effects of gait initiation and termination on MOSAP behavior may be worth an independent investigation.

5. Conclusion

We demonstrated that the XcoM and the step length covary to maintain MOSAP, indicating that MOSAP is controlled during unobstructed and obstructed gait. In conjunction with the consistently negative MOSAP values for most of the analyzed steps, we conclude that the MOSAP is controlled to exploit the passive dynamics and achieve forward progression at low energetic cost. Furthermore, the value of MOSAP is proactively altered while approaching an obstacle, and MOSAP shows substantial fluctuations for the two crossing steps. These changes reflect a tradeoff between stability and energy efficiency. The changes during approach and lead crossing steps indicate increasingly cautious gait with a growing preference for stability, whereas the opposite change after the trail crossing step indicates a reversion to improving efficiency when the risk to balance is reduced. Thus, our results indicate that humans employ a passive dynamics manipulation strategy to exploit the passive AP body motion to meet specific ends dictated by the locomotor task. We conclude that the UCM analysis of MOSAP provides new information regarding the control of balance during walking, especially for gait tasks requiring proactive adaptations, and our methods could be valuable in understanding the effects of age and pathology on gait.
References


Supporting information

**S1 Fig. Figure 1.tif. Figure 1.** Experimental task and basic definitions. Illustration of foot placements while approaching (fp-4 to fp-1), crossing (fp+1 and fp+2) and after crossing (fp+3) the obstacle, and of steps while approaching (Step-3 to Step-1), crossing (Step0 and Step+1) and after crossing (Step+2) the obstacle (A). Definitions of the extrapolated center of mass (XcoM) and margin of stability, MOSAP. Step length, XcoM and MOSAP are computed at the moment of lead heel contact in a coordinate frame located where the rear heel contacted the ground (B).

**S2 Fig. Figure 2.tif. Figure 2.** Representative data from one participant. Figure illustrates changes in various outcomes while approaching and crossing an obstacle, and then resuming unobstructed gait (blue ellipses). Steps during unobstructed gait are included for comparison.
The 45° line separates the regions of positive and negative MOSAP; the white region above the line represents passively unstable behavior, and the gray region below the line represents passively stable behavior. The 45° line also represents the direction of the uncontrolled manifold (UCM). Variations in step length and XcoM along this direction do not change MOSAP. The ellipses are centered at the centroid of the across-trial data for each step, and the major axes are aligned with the 45° line. However, the flatness of the ellipses is representative. Changes in mean values of the MOSAP are reflected in the position of the ellipses in each chart. The flatness of the ellipse reflects the synergy index, with flatter ellipses indicating higher synergy indices that reflect stronger covariation between the step length and XcoM.

**S3 Fig. Figure 3.tif.** Figure 3. Outcomes of the synergy analysis. Synergy index (A), $V_{UCM}$ (B), and $V_{ORT}$ (C). Data are across-subject means (N=20), and error bars denote standard error. Asterisks denote significant across-task differences at that step ($p < 0.05$). Across-step pairwise comparisons for the obstacle-crossing task are indicated by the row of letters above the horizontal axis for each panel. Steps that do not have letters in common are significantly different from each other (i.e., A is different from B, but A is not different from AB).

**S4 Fig. Figure 4.tif.** Figure 4. MOSAP and its components. MOSAP (A), CoM position at heel contact (B), CoM velocity at heel contact (C) and step length (D). Data are across-subject means (N=20), and error bars denote standard error. Asterisks denote significant task difference at that step ($p < 0.05$). Across-step pairwise comparisons for the obstacle-crossing task are indicated by the row of letters above the horizontal axis for each panel. Steps that do not have letters in common are significantly different from each other (i.e., A is different from B, but A is not different from AB).