Title
Evidence for shared resources in visuospatial attention: Endogenous attention misleads the decoding of exogenous attention in alpha rhythms

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Contributions
M.L. and A.R. discussed and dreamed up the study. M.L. and J.D.C. designed experiments, collected data, and performed analyses. J.S., S.B. and A.R. provided feedback throughout the project. All authors wrote the manuscript. A.R secured funding and provided lab space and equipment to pursue this study.

Competing Interests
All authors declare no competing interest

Data and Codes availability
Data and codes will be available on OSF:
https://osf.io/z8wkp/?view_only=9cc6c28dc5504ec48bf933f002d6ee8c

Abstract

Prevailing accounts of visuospatial attention differentiate exogenous orienting, which
corresponds to involuntary shifts of attention, from endogenous orienting, which reflects
the voluntary control of attention. While these different forms of attention are functionally
separable, evidence shows that they can nevertheless interact with each other. These
dynamics have been at the center of ongoing debates for more than two decades. One
hypothesis regarding these interactions is that, while both forms of attention orienting map
onto independent functional systems, they are capable of mutual interference. This
viewpoint implies that exogenous attention, a ballistic and stimulus-driven process, is not
impervious to the influence of endogenous attention. Evidence in support of this view
remains sparse and the mechanisms that underlie these interactions remain largely
unknown. The present study tackles these questions by examining whether endogenous
attention influences the neural processes of exogenous attention using multivariate
pattern classification to electroencephalography (EEG). We contrasted the effects of
exogenous attention across two experimental conditions: Single cueing where exogenous
attention is engaged alone, and double cueing where exogenous attention is concurrently
engaged with endogenous attention. Our results show that the simultaneous engagement
of endogenous attention alters the emergence of exogenous attention across cue-related
and target-related neural processes. Exogenous attention is therefore not impervious to
the influence of endogenous attention. More importantly, we observed that classifiers
trained to decode exogenous attention from the power and phase of alpha band activity
during single cueing condition were systematically misled by endogenous attention when
tested in the context of double cueing. Hence, both the power and phase of alpha rhythms
are central to exogenous and endogenous attention. These findings not only highlight
overlapping neural processes between both form of attention orienting, but further
demonstrate that the dynamics of exogenous and endogenous attention are
characterized by limited processing resources.

Significance Statement

Visuospatial attention is often dichotomized into top-down and bottom-up components:
Top-down attention reflects slow voluntary shifts while bottom-up attention corresponds
to fast involuntary demands. A large body of findings supports the view that these forms
of attention orienting are functionally separable. Following longstanding debates about
their interactions, the current study examines the relationship between top-down and
bottom-up attention. Using electroencephalography (EEG) and multivariate pattern
classification techniques, the researchers show that top-down attention modified the brain
activity of bottom-up attention. Moreover, machine learning classifiers trained to decode
bottom-up attention based on alpha band activity (8-12 Hz), a well-known marker of
visuospatial attention, are systematically misled by top-down attention. The researchers
conclude that both forms of visuospatial orienting are supported by several overlapping
neural processes, which implies shared neural resources between them.

Introduction

Researchers often separate the control of visuospatial attention into exogenous and endogenous attention. According to this dichotomous account, exogenous orienting involves reflexive and involuntary shifts of attention triggered by salient events, while endogenous orienting corresponds to the voluntary control of attention based on the goals of individuals (Corbetta et al., 2008; Corbetta & Shulman, 2002; Jonides, 1981; Müller & Rabbitt, 1989; Posner, 1980; Wright & Ward, 2008). A towering body of work underlines critical differences between these two forms of attention orienting, which supports the idea that they map onto distinct independent systems (Chica et al., 2013). For example, exogenous orienting comes about through involuntary responses that quickly engages and disengages from attended locations. Endogenous orienting, on the other hand, corresponds to voluntary shifts of attention that occurs more gradually and enables individuals to attend to sensory events for an extended period of time (Carrasco, 2011). Visuospatial attention therefore involves separate systems that operate via distinct modes of control.

Most documented differences between exogenous and endogenous attention have been identified using the spatial cueing paradigm – an experimental approach for studying visuospatial attention (Chica et al., 2014). Here, researchers typically investigate exogenous orienting using task-irrelevant and peripheral stimuli (e.g., a visual flash occurring at the periphery) and endogenous attention based on task-relevant central cues instructing participants to voluntarily attend to a particular location (e.g., a symbolic cue). The perceptual benefits of visuospatial attention emerge by comparing trials where target events occur at the cued versus the uncued location (Posner et al., 1980). Some studies have examined the interplay between exogenous and endogenous attention using a double-cueing strategy where both forms of attention orienting are concurrently engaged. Following this approach, some findings support the dichotomous account by showing limited interactions between exogenous and endogenous attention during perceptual processing (Landry et al., 2021), while others have uncovered evidence for interferences in demanding context (Berger et al., 2005). Evidence shows that exogenous orienting can interfere with endogenous attention in certain contexts – an observation that emphasizes

the ballistic nature of exogenous attention (Theeuwes, 2019). Yet, the mechanisms that
underlie these interactions remains unclear, as evidenced by ongoing debates about the
dynamics between exogenous and endogenous attention for more than two decades
(Luck et al., 2021).

An emerging hypothesis with regards to attention typologies proposes that these
different forms of visuospatial orienting represent separate functional systems capable of
mutual interference (Berger et al., 2005). Insofar that visuospatial attention operates by
allocating processing resources (Luck et al., 1996), mutual interference entails that
exogenous and endogenous attention compete for these resources. While exogenous
attention emerges via stimulus-driven and ballistic processes, this viewpoint implies that
it is not impervious to the influence of endogenous attention. Hence, exogenous attention
does not solely reflect saliency and bottom-up processing (Folk et al., 1992). Evidence in
support of this prediction, however, remains ambiguous. The current work tackles this
point by exploring the dynamics of exogenous and endogenous attention using
multivariate classification and machine learning – a collection of techniques that allow
neuroscientists to test well-established psychological ontologies by decoding
psychological states from neural data (Kragel et al., 2018). We leveraged these analytical
advances to decode visuospatial attention and test whether endogenous attention
influences cue-related and target-related components of exogenous attention.

Numerous findings show commonalities between exogenous and endogenous
attention at the sensory level (Ahrens et al., 2019; Grubb et al., 2015; Hopfinger & West,
2006; MacLean et al., 2009) and across widespread brain networks (Bowling et al., 2020;
Buschman & Miller, 2007; Nobre et al., 1997; Peelen et al., 2004). Recent
electrophysiology work proposes that exogenous and endogenous orienting share a
common neural marker of visuospatial attention: Alpha band dynamics (8-12 Hz; Keefe
& Störmer, 2021). This work therefore provides a reliable neural marker for investigating
trade-offs between exogenous and endogenous attention. In the context of visuospatial
attention, modulations of alpha power are often construed as an index for neuronal
inhibition relative to the selection of information at the sensory level (Klimesch, 2012). In

support of this hypothesis, a recent study showed that inducing changes in alpha power
over the posterior cortex via neurofeedback yielded corresponding modulations of evoked
responses for visual stimuli (Bagherzadeh et al., 2020). This outcome implies that
changes in lateralized alpha rhythms cause shifts of spatial attention across the visual
field. The present work therefore focusses on this marker to quantify how endogenous
attention interacts with exogenous attention.

To evaluate whether exogenous attention is impervious to endogenous attention,
our work compared the cue-related and target-related effects of exogenous attention
across single cueing, where exogenous attention is engaged alone, and double cueing,
where exogenous attention is concurrently engaged with endogenous attention. In our
approach, the endogenous cue preceded the orientation of exogenous attention during
double cueing, thus any modulations of endogenous attention over exogenous attention
would therefore reflect the involvement of top-down resources rather than a perceptual
confound (i.e., changes in the visual display). Moreover, we separated the double cueing
condition into trials where both cues pointed to the same location and trials where they
pointed to opposite locations. Our experimental strategy therefore allowed us to isolate
situations where attention resources are split across the visual field. Lastly, we adjusted
the difference in timing between cues and target events to the respective temporal profiles
of both forms of attention orienting, wherein the perceptual benefits of exogenous
attention are observed early following cue onset (i.e., around 300ms before a target),
while those of endogenous occur later (i.e., around 700ms before a target) (Chica et al.,
2014). We accordingly ensured that the target event would onset within the optimal
window of processing for both endogenous and exogenous attention.

We employed two complementary analyses (i.e., two decoding challenges) to
examine orienting-related and target-related responses of exogenous attention by
applying multivariate statistical techniques over electroencephalography (EEG) data. In
our first challenge, we verified how classifiers trained to decode cue-related and target-
related effects of exogenous attention during the single cueing task would perform when
tested in the context of double cueing. We accordingly hypothesized that interference

from endogenous attention would emerge as a decrease in classification performance.
Classifiers trained to decode exogenous attention in single cueing and subsequently
tested in double cueing should show a lower decoding performance if endogenous
attention interferes with exogenous orienting. We performed these assessments across
different features of the EEG, including the cue-related and target-related event related
potentials (ERPs), and over the amplitude and the phase of alpha oscillations given the
centrality of this neural marker in visuospatial attention. In our second challenge, we
aimed to complement and corroborate our findings by training multivariate classifiers to
decode the cueing condition directly (i.e., single versus double cueing). Our goal was to
validate our findings for cue-related and targeted-related effects of exogenous attention
across single and double cueing. For this analysis, above chance-level performance of
the classifier would indicate differences in exogenous orienting between the single and
double cueing. We further isolated the modulations of endogenous attention by applying
principal component analysis (PCA) over the exogenous cue-related encoding model.
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Results

Thirty-two participants completed spatial cueing conditions in a blocked design
while we recorded their EEG. Participants were instructed to discriminate the orientation
(clockwise versus counter-clockwise) of a Gabor target stimulus displayed either at the
cued or uncued location (Figure 1). Participants completed an exogenous single-cueing
task where we elicited exogenous orienting of attention alone, and in a double-cueing
task that concurrently engaged both endogenous and exogenous orienting. Cue validity
was determined following cue and target contingencies. The order of the experimental
conditions was randomly counterbalanced between participants (see Methods).
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Behavior. We first confirmed that the exogenous cue facilitated discrimination
performance by examining accurate response times (RTs) in the single-cueing condition
via single-trial hierarchical linear regressions (Gelman & Hill, 2006). Note that
discrimination performance was near ceiling across all cueing conditions (i.e., accuracy
rate for single cueing, $\mu=94.4\%$ ($\sigma=3.6\%$) and double cueing, $\mu=93.6\%$ ($\sigma=3.9\%$). Our
regression analysis included exogenous cue validity (i.e., valid vs. invalid) as a fixed

predictor and participants as a random factor for predicting accurate RTs. We found that

exogenous cueing improved discrimination performances, with cue validity as a reliable

predictor (β=-41.28, SE=2.83, 95% CI [-46.83, -35.74]; Figure 1A and Supplementary

Tables 1 and 2). In the double-cueing condition we included the validity of the exogenous

cue, the validity of the endogenous cue, and their interaction as fixed factors in the

regression model, with participants as random predictors. We added these fixed factors

in a stepwise fashion to determine the best-fitting model and assessed evidence for an

interaction between exogenous and endogenous cue validity on RTs. This analysis shows

that the main effects of exogenous cue validity (β=-39.27, SE=3.04, 95% CI [-45.22, -

33.32]) and endogenous cue validity (β=-22.42, SE=3.22, 95% CI [-28.73, -16.11]; Figure

1B, and Supplementary Tables 3 and 4) were statistically reliable. Yet, we could not reject

the null hypothesis for their interaction. This outcome confirms the engagement of both

exogenous and endogenous attention in the double-cueing condition. Moreover, we

observed that evidence weighted against their interaction, as indicated by a Bayes factor

analysis: BF_{01}=105.59).

Next, we examined whether exogenous cue validity varied across single and

double cueing conditions. Here, we performed two separate analyses. First, we evaluated

exogenous cue validity across single cueing and double cueing when both cues indicate

the same location (i.e., both exogenous and endogenous were engaged to the same

location). We specified exogenous cue validity (valid vs. invalid cues), cueing task (single

vs. double-cueing task) and their interaction as fixed predictors, and participants as

random factors. We used a stepwise approach to assess the statistical reliability of our

predictors. The best-fitting model included exogenous cue validity (β=-41.28, SE=2.93,

95% CI [-47.02, -35.55]), cueing task (β=39.98, SE=4.18, 95% CI [31.78, 48.18]), and

their interaction (β=-19.91, SE=5.31, 95% CI [30.33, -9.49]) as predictors of RTs (Figure

1C, and Supplementary Tables 5 and 6). Second, we examined the cueing effect of

exogenous attention across single cueing and double cueing when both cues indicated

opposite locations (i.e., both exogenous and endogenous were engaged to different

locations). The best-fitting model included exogenous cue validity (β=-41.31 SE=2.93,

95% CI [-47.02, -35.55]), cueing task (β=18.13, SE = 3.34, 95% CI [11.59, 24.69]), and

their interaction (β=24.48, SE = 5.37, 95% CI [13.98, 35.07]) as predictors of RTs (Figure

1D, and Supplementary Tables 7 and 8). Together, these results show that endogenous

attention influences the cueing effect of exogenous attention. This effect remains

regardless of the spatial location of endogenous attention i.e., when both cues are

engaged towards the same location or when they are split.

Figure 1. **A.** Top panel: in the single cue condition each trial began with a fixation screen, followed by the onset of the exogenous cue and lastly, the Gabor target at the valid or invalid location. The exogenous cue was task-irrelevant and predicted the upcoming target's location at chance-level. The scatter plot depicts group (black dots) and participant (grey dots) average RTs on the task. Error bars represent bootstrapped 95% C.I. Bottom panel: single-trial hierarchical regression model coefficients. Error bars represent 95% C.I.

B. Top panel: the double cueing condition comprised both exogenous and endogenous cueing where the exogenous cue did not predict the target's location and the endogenous cue predicted the target's location 66.66% of the time. The endogenous cue (i.e., fixation semicircles, where the white side indicated where the target was likely to occur; see Methods for details) appeared after a jittered interval, followed by the exogenous cue, and finally the target event. The scatter plot shows group (black dots) and subject (grey dots) average RTs. Error bars represent bootstrapped 95% C.I. Bottom panel: single-trial hierarchical regression model coefficients. Error bars represent 95% C.I. **C.** Single-trial hierarchical regression model coefficients where evaluated the effect of cueing condition on exogenous cue validity.

Electrophysiology. Challenge I – *Generalizing neural decoding of exogenous attention*
from single to double cueing. We trained SVM classifiers to decode cue-related and
target-related neural processes of exogenous attention based on EEG signals (Hong et
al., 2020). Here, we aimed to decode (1) the direction of exogenous attention orienting
(i.e., left versus right orienting of exogenous attention) from cue-related EEG; and (2) cue
validity (i.e., valid versus invalid trials) from target-related EEG. Our approach follows
from (Bae & Luck, 2018). Decoding was performed at the participant level using a three-
fold cross-validation procedure where 2/3 of trials were randomly selected to train the
classifier and validation was assessed on the remaining 1/3 of the trials. We decoded
exogenous attention across each time-point separately through the time series (see
supplementary Figure 1). For the first sets of analyses, we trained and validated
classifiers in the single cueing and subsequently assessed their performance in the
double cueing condition. We reasoned that poorer classification performance in the
double cueing task would indicate that endogenous attention alters the neural features of
exogenous attention. See methods for details.

We separated the double cueing condition into trials where both cues indicated the
same location and those where both cues indicated opposite locations, which yielded
three comparisons across these analyses: We contrasted the classifiers' performance for
single cueing against that of the double cueing conditions when the exogenous and
endogenous cues were directed to the same location in the double cueing task, we
compared single cueing against double cueing when both cues indicated opposite
locations in the double cueing task, and we compared classification performances from
the double cueing condition when both cues indicated the same location versus when
they both indicated opposite locations. We relied on cluster-corrected pairwise t-tests over
decoding accuracy rates across the time series for these comparisons. We applied this

analytical approach to cue-related and target-related waveforms. Our goal was to
examine the effects of double cueing across established neural markers of exogenous
attention. We used cue-related lateralized alpha index (LAI) and intertrial phase clustering
(ITPC) of alpha oscillations to decode exogenous attention orienting.

Decoding based on cue-related waveforms highlights the impact of the double
cueing condition on single cueing. Here, we first validated our approach by showing that
classification was above chance level for decoding the orientation of exogenous attention
during single cueing and double cueing conditions (supplementary Figure 2A), thereby
substantiating our approach. We observed that SVM classification could recover the
direction of exogenous attention better than chance even when endogenous attention is
concurrently engaged. We then compared classification performance across single
cueing, double cueing for the same location, and double cueing for opposite locations.
Critically, these contrasts show that classification performance worsens in the double
cueing task compared to the single task for cue-related ERPs (Figure 2A). These effects
occurred between 144ms and 496ms when both cues were directed towards the same
location during double cueing. In turn, we found an early cluster (i.e., from 108ms to
180ms) and two late clusters (i.e., from ~448ms to ~596ms and from 636ms to 704ms)
when the cues indicated opposite locations. Following our hypothesis, evidence shows
that the concurrent engagement of endogenous attention modulates the neural dynamics
of exogenous orienting, both when they align to the same location and when they are split
across opposite locations. Furthermore, we observed a late significant cluster occurring
from 628ms to 740ms when contrasting trials where both cues indicate the same direction
versus when trials where both cues indicate opposite locations. This pattern denotes that
classification returned to baseline more quickly when both cues were directed to opposite
locations, which is consistent with the idea that endogenous orienting allows exogenous
attention to be sustained at a particular location for an extended period when both forms
of orienting are engaged towards the same location. Altogether, these results reveal that
endogenous attention alters the neural dynamics of exogenous orienting.

We further investigated whether endogenous orienting impacts the cueing benefits
of exogenous attention by decoding exogenous cue validity based on target-related
waveforms. We validated that classification was above chance-level during single-cueing
(supplementary Figure 2B). We similarly confirmed that SVM could decode exogenous
cue validity in the context of double cueing (supplementary Figure 2B). Consistent with
our behavioral findings showing that the concurrent engagement of endogenous attention
interferes with the cueing effect of exogenous orienting, classification performance of
exogenous cue validity was inferior during double cueing (Figure 2B). Comparing single
and double cueing conditions yielded significant clusters between 196ms to 284ms
whenever both cues were directed towards the same target event during double cueing,
and between 288ms to 292ms when the cues directed exogenous and endogenous
attention to opposite directions for double cueing.

Figure 2. Multivariate classification of exogenous orienting and cue validity in both single and double cueing conditions. We examined trials in the double cueing condition where both cues indicated the same or opposite locations separately. We compared classification performances using cluster-corrected pairwise t-tests. Grey lines indicate significant clusters for each comparison. Shaded areas represent the SEM. **A.** Decoding the direction of exogenous orienting based on cue-related ERPs. **B.** Decoding exogenous attention cue-validity based on target-related ERPs.

Lastly, we used alpha band dynamics to decode the orienting of exogenous
attention. We first validated that classification was above chance level for both the LAI
and ITPC during single cueing, thereby confirming the reliability of our approach for
uncovering the effects of exogenous attention (supplementary Figure 3A and 3B).
Critically, our results show that classifiers trained to decode exogenous attention in the

context of single cueing are systematically misled by the direction of endogenous
attention when tested in the context of double cueing condition. Classification
performance was above chance level when both cues indicated the same spatial location
in the double cueing task, and then below chance level when both cues indicated opposite
locations (Figure 3; supplementary Figure 3A and 3B). This effect was apparent when we
compared decoding accuracy between same and opposite cueing conditions during
double cueing across power and phase of alpha rhythms: Significant clusters emerged
between 72ms and 368ms for the LAI and from the onset of the cue until 496ms for the
ITPC (Figure 3). This outcome provides compelling evidence regarding significant overlap
between both systems across brain activity in the alpha band (8-12 Hz).

Figure 3. Multivariate classification of exogenous orienting and cue validity in both single and double cueing conditions. We examined trials in the double cueing condition where both cues indicated the same or opposite locations separately. We compared classification performances using cluster-corrected pairwise t-tests. Grey lines indicate significant clusters for each comparison. Shaded areas represent the SEM. **A.** Decoding of exogenous cue orienting based on cue-related LAI (see methods). **B.** Decoding of exogenous orienting based on cue-related alpha ITPC.

Electrophysiology. Challenge II – *Decoding cueing conditions.* We aimed to corroborate
our primary findings by decoding the cueing condition: Single versus double cueing. We
hypothesized that classification performance would be above chance if endogenous
attention interferes with exogenous orienting given that this is the only difference between
cueing conditions. Our decoding approach was similar to the one we previously described
where we trained SVM classifiers based on a three-fold cross validation approach

(supplementary Figure 1). We separated trials where both cues indicated the same spatial

location or opposite locations in the double cueing condition (see Methods for details).

For cue-related brain activity, we trained SVM classifiers to distinguish the cueing

conditions from lateralized ERPs (i.e., contralateral minus ipsilateral exogenous cue-

related waveforms), LAI, and lateralized alpha band ITPC. For target-related processes,

we examined exogenous cue validity (i.e., exogenous cue valid minus exogenous cue

invalid) across ipsi- and contralateral sides relative to the target event.

Our results corroborated our previous findings. For cue-related waveforms, SVM

classifiers differentiated cueing conditions (Figure 4A and 4D). Specifically, we observed

significant clusters ranging from 140ms to 476ms when both cues indicated the same

location for double cueing, and from 108ms to 614ms when both cues indicated opposite

locations for double cueing. In the same vein, we observed significant clusters for LAI and

phase clustering for alpha rhythms only when both cues were indicating opposite

locations during double cueing, which is largely consistent with Challenge I (Figure 4B,

4C, 4E, 4F). Here, a large cluster emerged from 88ms to 432ms after cue onset for LAI

(Figure 4E), and then from -24ms to 492ms after cue onset for the phase clustering of

alpha oscillations (Figure 4F). These results complement our previous findings and

suggest that the concurrent engagement of endogenous attention impacts exogenous

cue-related EEG components.

Decoding Exogenous Orienting - Single vs. Double Cueing **Same** Location

Figure 4. Multivariate classification of cueing conditions based on cue-related ERPs, LAI, and phase clustering. We assessed classification performance separately for trials in the double cueing condition where both cues indicated the same location (**A,B,C)** and opposite location (**D,E,F)**. Grey lines indicate above chance-level classification based on cluster-corrected t-tests. Bold lines represent the averaged time series and shaded areas the SEM.

Similarly, we observe evidence for interference between both systems when
decoding cueing conditions based on target-related waveforms (Figure 5). Here, we found
that classification was better than chance across both contra- and ipsilateral trials when
both cues were directed toward the same location. We observed a significant cluster from
236ms to 304ms for the contralateral side (Figure 5A), and a much larger one from 72ms
to 372ms for the ipsilateral side (Figure 5B). In turn, for trials where both cues indicated
opposite locations during double cueing, we observed a significant cluster on the
ipsilateral side only, between 168ms and 280ms (Figure 5C, 5D). These results confirm
our hypotheses, showing that endogenous attention influences exogenous cue validity–
even when both forms of orienting are engaged towards the same target event.

Decoding Exogenous Orienting - Single vs. Double Cueing **Same** Location

A. Contralateral Waveforms   **B.** Ipsilateral Waveforms

Decoding Exogenous Orienting - Single vs. Double Cueing **Opposite** Locations

C. Contralateral Waveforms   **D.** Ipsilateral Waveforms

Figure 5. Multivariate classification of cueing conditions based on target-related ERPs for contra- and ipsilateral channels (i.e., cue valid minus cue invali. We assessed classification performance for contralateral trials to the target when both cues indicated the same location (**A**) and the opposite location (**C**). We repeated this analysis for ipsilateral trials (**C**) and (**D**). Grey lines indicate significant clusters against chance-level based on cluster-corrected t-tests. Bold lines represent the averaged time series and shaded areas of the SEM.

Electrophysiology. Encoding model of exogenous orienting. We examined encoding
models for the classification of exogenous orienting based on cue-related ERPs to better
isolate the influence of endogenous attention during double cueing. Based on previous
work, we expected that double cueing would modulate exogenous attention at the
sensory level (Fernández & Carrasco, 2020; Hopfinger & West, 2006). To test this
hypothesis, we first trained classifiers in the single and double cueing conditions
separately, and then computed interpretable SVM weights of these models using an
established procedure (Haufe et al., 2014). See supplementary Figure 4 for the averaged
decoding accuracy of these models across single and double cueing. Next, we applied
principal component analysis (PCA) to these weights to identify the underlying
components pertaining to exogenous orienting of attention based on cue-related

waveforms. We performed this procedure separately for trials when both cues indicated

the same location, and when both cues indicated opposite locations in the double cueing

condition. See methods for more details. This procedure yielded two significant

components of the exogenous cue-related encoding model. The first component

explained 57% of the variance and was marked by a posterior and lateralized topography.

This component showed early variation of the SVM weights after cue onset, trailed by

slower variations (see supplementary Figure 2). These patterns suggest that this

component reflects sensory processes. We compared single and double cueing

conditions, which revealed two clusters involving trials when both cues indicate opposite

locations – a first one ranging from 204ms to 268ms post-cue, and a second one from

360ms to 456ms (Figure 6A). Likewise, we report significant differences in the endocding

models of exogenous orienting between trials when the cue indicated the same vs the

opposite location in the double cueing condition. A first one from 156ms to 472ms and a

second one from 560ms to 668ms (Figure 6A). Conversely, we did not observe any

differences for the second component, which explained 28.5% of the variance and was

marked by a more anterior pattern and slowed deflection of SVM weights from 200ms to

500ms post-cue (Figure 6B).

Figure 6. Comparison of single (pink), double cueing for same cueing location (blue), and double cueing for opposite cueing locations across first (**A**) and second (**B**) PCA components for the exogenous cue-related encoding model. Grey lines indicate significant clusters based on cluster-corrected pairwise t-tests. Bold lines represent the averaged time series and shaded areas of the SEM.

Discussion

Exogenous and endogenous orienting correspond to distinct control systems of
visuospatial attention (Chica et al., 2013). Some reports highlight experimental contexts
where we observe interactions between them, thereby challenging the idea that they
operate completely independently from one another (Ahrens et al., 2019; Grubb et al.,
2015; Hopfinger & West, 2006; MacLean et al., 2009). Yet, these dynamics remain
unclear (Berger et al., 2005; Luck et al., 2021). In the present work, we combined
multivariate statistics with single and double spatial cueing procedures to examine the
influence of endogenous attention over exogenous attention. Contrary to the idea that
exogenous orienting is impervious to top-down factors (Landry et al., 2021; Pinto et al.,
2013), our behavioral and neurophysiological results highlight that endogenous attention
impacts exogenous attention across both cue-related and target-related processing.
Critically, our findings not only show that classifiers trained to decode the effects of
exogenous attention during single cueing perform worst when tested in the context of
double cueing, but also highlight that classifiers trained to decode the direction of
exogenous attention can be misled by the parallel engagement of endogenous attention.
Our findings therefore provide evidence of overlap and shared neural resources between
exogenous and endogenous attention at the sensory level of processing.

Past EEG studies relate the cueing of exogenous attention to an early posterior
component emerging at the sensory level (Hopfinger & West, 2006; Störmer et al., 2019).
Following this pattern, classifiers trained to decode exogenous orienting in the single
cueing context, based on cue-related waveforms, achieved a lower performance when
tested in the double cueing context 150ms after cue onset. Furthermore, our results
indicate that the concurrent engagement of endogenous attention alters early visual
processes, as evidenced by our encoding model of exogenous orienting. These results
align with brain imaging assays indicating that exogenous and endogenous attention
modulate neurons in the sensory areas (Dugué et al., 2020; Müller & Ebeling, 2008) . The
present study therefore extends this body of work by showing that top-down attention
alters the subsequent emergence of exogenous attention over posterior brain areas. We
markedly observed this influence by comparing classification performances of exogenous
attention within the double cueing condition. When both cues indicated the same target

location, decoding performance remained above chance-levels for a longer period than
when they indicated opposite spatial locations. Combining both forms of attention
orienting therefore entails functional consequences for exogenous attention. The current
work also shows that the interference of endogenous attention over exogenous orienting
yields sensory consequences for exogenous attention – an effect we observed across
behavioral and neurophysiological data. This outcome follows earlier work showing that
both exogenous and endogenous processing interact during sensory processing of target
events (Hopfinger & West, 2006).

Importantly, we further tested the modulations of endogenous attention over
exogenous attention across alpha rhythms – a well-established marker of visuospatial
attention (Klimesch, 2012). This analysis revealed that SVM classifiers trained to decode
exogenous attention in the single cueing condition were systematically misled by the
direction of endogenous attention in the double cueing condition. Specifically,
classification performance was above chance level when the direction of endogenous
attention matched that of exogenous attention, and below when endogenous and
exogenous indicated opposite spatial locations. This result implies that endogenous
attention interferes with the neural processes of exogenous attention through alpha band
activity. Accordingly, the present study not only corroborates the centrality of alpha waves
across both forms of visuospatial attention (D'Andrea et al., 2019; e.g., Keefe & Störmer,
2021; Störmer et al., 2016; Thut et al., 2006), but also reveals significant overlap between
them for this neural marker. This is consistent with the idea that both attention systems
tap into a common neural resource indexed by alpha rhythms. One prevailing hypothesis
posits that alpha oscillations reflect inhibitory and selection processes – two key elements
in the emergence of selective attention (Klimesch, 2012). This viewpoint postulates that
alpha waves capture spatiotemporal aspects of attention through modulations of neuronal
excitability at the sensory level such that attending to a particular location in our visual
field reduces local inhibition and increases feedforward processing at the contralateral
visual site (Jensen & Mazaheri, 2010). Moreover, the timing of these effects are indexed
by the periodicity of oscillatory patterns, which yields rhythmic sampling of sensory inputs
(Haegens et al., 2011). Following this overarching view, our findings suggest that both

exogenous and endogenous attention tap onto these neural processes to facilitate

perceptual processing, as indexed alpha oscillations.

In their pursuit to elucidate the dynamics of exogenous and endogenous attention,

Berger et al. (2005) submit that their relationship is marked by competition for limited

resources. This viewpoint implies that they are capable of mutual interference, whereby

exogenous attention is not impervious to the influence of endogenous attention. Relying

on neural markers of visuospatial attention and multivariate pattern classification, our

findings support this hypothesis by showing that endogenous attention overlaps with

exogenous attention across alpha rhythms. The selection of information emerges by

allocating resources that prioritize perceptual processing (Luck et al., 1996; Theeuwes,

2019). Our study shows that the capacities of bottom-up and top-down attention to recruit

these resources are shared and limited.

Methods

Participants. We recruited 42 participants (29 women, mean age = 22.2(sd = 3.09)) based

on convenience sampling. Each individual received monetary compensation of $10/hour

for completing 4 different tasks in one testing session lasting approximately 2 hours. All

participants had normal or corrected-to-normal vision, had no prior history of neurological

disease, and provided consent. The experiments were approved by the McGill Ethics

Board Office (Certificate #511-0516).

We excluded data from ten participants: Seven participants were excluded due to

the overwhelming presence of EEG recording artifacts. One participant did not complete

all tasks. We excluded one participant because they performed below chance-level

(~40% averaged across all conditions). Lastly, one participant was excluded due to a high

volume of timeout errors (response times > 1500ms on ~11% of trials overall). Data

analysis therefore proceeded from the data of 32 individuals (24 women, Mean age =

21.9 (SD = 2.6)). We determined our sample size based on previous work using the

double cueing experimental approach (Landry et al., 2021). In this work, simulations

following effect size estimates of performance revealed that 6 participants were required

to achieve a power of .8 for the within-individual cueing effects of exogenous and
endogenous orienting in a target discrimination task when alpha is set .05. The sample
size for the present work was therefore more than adequate to detect the desired attention
effect at the behavioral level, and almost twice that of previous EEG experiments
investigating combined effects of exogenous and endogenous orienting (Hopfinger &
West, 2006; Keefe & Störmer, 2021).

Stimuli, Apparatus & Design. Participants viewed tasks on a 24-in BenQ G2420HD
monitor sitting approximately 60 cm away, where stimuli presentation was controlled via
MATLAB R2015b (Mathworks Inc., Natick, MA, USA) using the third version of the
Psychophysics toolbox (Brainard & Vision, 1997; Kleiner et al., 2007; Pelli, 1997). The
screen was set to 75hz. All stimuli were black (i.e., RGB values of 0, 0, 0; 1.11 cd/m^2) and
white (i.e., RGB values of 255, 255, 255; 218.8 cd/m^2) drawings on a grey background
(i.e., RGB values of 128, 128, 128; 70.88 cd/m^2). The fixation marker was an empty circle
made from a black line drawing subtending a radius of 1.2° located in the center of the
screen. Two target placeholders were located at 8.7° away from the fixation marker on
the left and right side of the screen. These placeholders consisted of black line drawings
of empty circles with a 2.4° radius. We cued exogenous attention by briefly changing the
line drawing from one of the placeholders to white. To ensure that this cue solely engaged
exogenous orienting, the cue-target spatial contingency was set to 50%, such that the
cue was task-irrelevant and not predictive of the target's location per the standard in the
field (Chica et al., 2014). We cued endogenous attention by coloring the inside of the
fixation marker, wherein the right or left half of the circle was shaded in black and the
other half in white. The side of the fixation marker that turned white indicated where the
target was likely to occur. For example, if the right side turned white, the target was 66.6%
likely to appear in the right placeholder. In this way, we avoided using overlearned
directional cues, like an arrow, to engage endogenous attention (Ristic & Kingstone,
2012; Ristic & Landry, 2015). The targets were sinusoidal black and white gratings
enveloped by a Gaussian with a spatial frequency of 3 cpd and tilted 5° degrees clockwise
or counter-clockwise from vertical.

Procedure. Participants completed four tasks: A non-cueing task, a single exogenous
cueing task, a single endogenous cueing task, and a double cueing task where both
exogenous and endogenous orienting occured. Participants performed 10 practice trials
prior to each task which consisted of 384 trials each. Task order was randomized across
participants. In the current manuscript, we analyzed data for the non-cueing, the
exogenous cueing, and the double cueing tasks in this manuscript.

Participants were asked to stare at the center of the screen throughout the
experiment, while we assessed their eye movements using electro-oculogram. We jittered
the latencies between the fixation point and the cues, between the endogenous and the
exogenous cues, and between the cues and the target event based on a uniform
distribution to minimize the effects of temporal prediction following spatial cueing. In this
regard, cue-target latencies were adjusted following the temporal profiles of exogenous
and endogenous so that attention facilitation would be maximized for each (Chica et al.,
2014).

In the non-cueing task, participants viewed the fixation stimulus between 1276ms
and 1782ms, which was immediately followed by the onset of the target event that stayed
on the screen until participants' responses. Note the non-cueing task was used as a
baseline against which we regressed the sensory effects of cue stimuli for the target-
related analysis (see the *Electroencephalography* section below).

In the exogenous orienting task, participants were first presented the fixation
marker followed by the exogenous cue between 707ms and 2412ms, which stayed on
the screen for 104ms, and then the target would onset at one of the target's locations
following a jitter between 0ms and 198ms post-cue. The target remained on the screen
until participants' response.

In the double cueing task, participants were first presented with the fixation marker
followed by the endogenous cue after 267ms to 1506ms. The endogenous cue stayed on
the screen until the end of the trial. The stimulus onset asynchrony between the

endogenous cue and the target event varied between 440ms and 906ms. The exogenous

cue would then onset before the target stimulus between 106ms and 307ms, and stayed

on the screen for 107ms (see Figure 1). As we mentioned previously, the exogenous cue

was uninformative about the target's location, whereas the endogenous cue was made

task-relevant by indicating the correct target location for 66.6% of trials. Participants were

aware of these contingencies. Participants were instructed to discriminate the orientation

of the Gabor target as quickly and accurately as possible on a QWERTY keyboard by

pressing the F key to input counter-clockwise orientation and the J key to input clockwise

orientation. Inter-trial period was set to 1s.

Data analyses for behavioral performance. Participants' discrimination performance was

near ceiling - averaged accuracy rate was ~93%. We therefore only examined accurate

response times (RTs). We removed trials where participants made anticipation (i.e., RTs

< 150ms) or timeout (i.e., RTs > 1500ms) errors, which accounted for less than 2% of

trials overall, as well as wrong key presses, less than 1% of trials. We used hierarchical

linear regression models (Gelman & Hill, 2006) to test the effects of cueing (i.e., valid

versus invalid) and task (i.e., single versus double cueing), wherein predictors were

added in stepwise fashion. We applied a chi-square goodness-of-fit test over the deviance

to determine whether predictors significantly improved the fit and assessed Bayesian

information criterion (BIC) to confirm which model best fit the data. We also estimated

Bayes factor weighting evidence for the null against the alternative hypothesis

(Wagenmakers, 2007) :

525                                  $BF_{10} = e^{\Delta BIC_{01}/2}$

We ran four statistical analyses on the behavioural performance of participants.

First, we ran a regression on the single exogenous cueing condition where we included

cue validity as a fixed factor. Second, for the double cueing task, we ran a regression

where we included exogenous cue validity, endogenous cue validity, and their interaction

as fixed predictors. Given that our approach focused on comparing the single and double

cueing conditions, we examined if the cueing effect of exogenous attention varied as a

function of task (i.e., single and double cueing). Here, we ran a regression where we

included exogenous cue validity and cueing condition (i.e., single versus double cueing

condition) as fixed factors. We performed two such analyses: Once where double cueing

involved trials where both cues indicated the same location, and then again when both

cues indicated opposite locations. We included participants as a random factor for all

regression models.

Electroencephalography. We recorded neurophysiology using 64 Ag/AgCl active

electrodes EEG at a sampling rate of 1000 Hz (ActiCap System; Brain Products GmbH;

Gilching, Germany) positioned following the 10-20 system. We additionally monitored eye

blinks and eye movements through bipolar electrodes placed at the outer canthi, as well

as the superior and inferior orbits of the left eye. Impedances of all electrodes were kept

below 10 kΩ. All electrophysiological signals were amplified (ActiChamp System; Brain

Products GmbH; Gilching, Germany). Electrodes were referenced online to C4, and re-

referenced offline to an average reference. Preprocessing and analysis were conducted

in BrainVision Analyzer (ActiChamp System; Brain Products GmbH Inc.; Gilching,

Germany) and MATLAB (R2020a; Mathworks Inc., Natick, MA) using Brainstorm (Tadel

et al., 2011) and custom scripts. We downsampled the data to 250 Hz and applied two

IIR Butterworth filters: a first High-pass 0.1 Hz filter of 8th order and a 60Hz notch filter.

We then topographically interpolated bad channels (1.12% of channels). Next, we

performed an independent component analysis to identify artifacts relating to eye

movements and blinks using the BrainVision Analyzer Ocular correction ICA tool. We

corroborated these analyses with the electro-oculogram. We corrected the EEG signal

following these artifacts. We visually inspected EEG signals to manually remove atypical

noise patterns, as well as activity exceeding ± 200 µV across all electrodes. All triggers

were realigned according to our photodiode stimulations linked to the onset of the

exogenous cue, the endogenous cue, and the target event.

For target-related events, in lieu of the adjacent response filter method (Woldorff,

1993), we removed event-related responses from exogenous and endogenous cueing by

taking the residuals of the linear regression model using the non-cueing condition as

baseline. A hierarchical linear regression was run with condition as a dummy coded fixed

factor, and subjects as a random factor. 'Raw' Residuals were obtained from   the

MATLAB function *residuals()* for all channels and subjects.

Event-related potentials. We analyzed cue-related and target-related event-related

potentials. To compute the waveforms, we first applied a FIR bandpass-pass filter

between 0.5 and 15 Hz and then divided the EEG into epochs spanning -200 and 1000ms.

We baseline corrected ERPs from -100 to 0ms.

Lateralized alpha index. We computed the alpha lateralized index (LAI) based on time-

resolved modulations of alpha power. These neural rhythms were computed for cue-

related epochs across all channels between -200 and 1000ms. We first estimated the

instantaneous amplitude of alpha waves (i.e., 8 to 12hz) related to the exogenous cue

using the real part of the complex filter Hilbert transformation, and then computed the LAI

following the direction of the cue at each time point according to the following equation:

$$\frac{\alpha\ power\ contralateral - \alpha\ power\ ipsilateral}{\alpha\ power\ contralateral + \alpha\ power\ ipsilateral}$$

Contra- and ipsilateral sides were defined according to the direction of exogenous

attention. Note that we computed LAI for lateral channels only, which excluded central

channels, while we paired every lateral channel with its corresponding match on the

opposite side (e.g., O1 and O2). Lastly, we z-score normalized the LAI from baseline

activity between -100 and 0ms.

Intertrial phase clustering. To examine the phase component of alpha oscillations, we

computed intertrial phase clustering (ITPC) for exogenous cue-related EEG activity

across all channels between -200 and 1000ms centered around the cue. This analysis

rests on the imagery part of the complex filter Hilbert transformation, which tracks the

phase angle of the oscillation (Cohen, 2014). We obtained ITPC time-resolved phase

alignment across trials based on the following equation:

$$ITPC_{tf} = |\ n^{-1} \sum_{r=1}^{n}\ \ e^{ik_{tfr}}\ |$$

Where, n corresponds to the number of trials and $e^{ik_{tfr}}$ provides the complex polar

representation of the phase angle k on trial r for the index for time and frequency tf. Lastly,

we transformed ITPC indices into z-scores from baseline ranging from -100 to 0ms.

Multivariate decoding analyses. Our goal was to evaluate whether endogenous attention

modulates cue-related and target-related exogenous attention using multivariate

statistical approach (Hong et al., 2020). We tackled this objective using complementary

analyses. First, we trained SVM classifiers to decode the effects of exogenous attention

during single cueing and then evaluated the performance of these classifiers in the

context of both single and double cueing conditions. Comparing classification accuracy

from the single and double cueing conditions based on models that were only trained in

the single cueing condition allowed us to assess the generalization of decoding

performance going from single cueing to double cueing. We hypothesized that a decrease

in decoding performance from single to double cueing would reflect interference from

endogenous attention on exogenous attention – i.e., that exogenous attention is not

impervious to the concurrent engagement of endogenous attention. In our secondary

complementary approach, we trained linear SVM classifiers to decode cueing conditions

-- i.e., single versus double cueing. We therefore aimed to directly explore the interference

of endogenous attention over exogenous attention.

Our decoding analyses followed from Bae and Luck (2018). We trained linear

support vector machines (SVM) based on exogenous cue-related and target-related EEG.

In our first series of analyses, we accordingly trained the classifiers to determine the

direction of exogenous attention orienting – left versus right orienting based on cue-

related components, and to determine exogenous cue validity – cue valid against cue

invalid based on target-related EEG components. Separate trials were used for the

training and testing of our classifiers following a three-fold cross-validation plan.

Classifiers were trained separately for each participant and time-points across the cue-

related and target-related time series.

We performed multivariate decoding analyses using linear support vector machine

(SVM) implemented in MATLAB's (i.e., *fitcsvm*). Following our three-fold cross-validation

procedure, 2/3 of trials were randomly selected to train the classifier, and the remaining

1/3 of the trials were used to test the performance of the SVM. Specifically, we organized

the data of each participant into three equally sized bins of trials and averaged these trials

together to produce three separate time-series. Two of the three averaged time-series

served as the training dataset, and the remaining average served as the testing set.

Decoding accuracy was determined on the correct identification of the data we left-out.

We iterated through all possible combinations of training such that each averaged time-

series served as the testing set once. For each participant, we performed 50 iterations of

the above binning, averaging, and decoding procedure. As we mentioned previously, we

applied our decoding strategy across two decoding challenges.

Challenge I: Generalization of decoding going from single to double cueing. We wanted

to assess how classifiers trained in the single cueing condition generalize to the double

cueing condition. Here, we trained and tested the SVM classifiers following the approach

we described previously on the data from the exogenous single cueing condition. Next,

we tested the ability of these SVM classifiers to decode exogenous attention in the context

of double cueing. Critically, for the double cueing condition, we assessed trials where

both attention cues pointed to the same and opposite directions separately. We applied

this approach to cue-related ERPs, LAI patterns, and phase clustering to assess both

cue-related and target-related effects (see Methods *Electroencephalography*).

First, we evaluated cue-related exogenous orienting responses based on ERPs,

LAI patterns, and phase clustering. We trained SVM classifiers to decode cue direction –

i.e., left orienting versus right orienting (Hong et al., 2020). Each bin used to produce

averaged time series for decoding comprised 25 trials.

Second, we evaluated target-related ERPs as a function of exogenous cueing.

Here, we decoded cueing effects – i.e., exogenous cue valid versus exogenous cue

invalid. To ensure that the classifier did not rely on the target's location, we performed our

decoding analysis separately for target events occurring on the left- and right-hand side

of the screen, and averaged the classification performance across both locations

thereafter. Each bin used to generate the averaged time series for decoding included 21

trials.

Decoding was performed for each participant, cueing condition, and

neurophysiological features (i.e., ERPs, LAI and phase clustering). We averaged

decoding accuracy for each participant, cueing condition, and neurophysiological

features. We used a five-sample sliding window -- i.e., a 20ms window to smooth the

average decoding accuracy time series. We then computed pairwise t-statistics at each

time point to ssstest decoding performance against chance-level (i.e., 50% decoding

accuracy). We additionally used t-statistics to compare: i) single cueing against double

cueing--when both cues indicate the same direction; ii) single cueing against double

cueing--when both cues indicate opposite directions, and iii) double cueing--same

direction against double cueing--opposite direction. We applied cluster-corrected

permutation tests to control for family-wise type-II error. We performed 1000 permutations

where we randomly varied the data and then contrasted observed cluster sizes against

surrogate distributions for the null hypothesis. The cluster forming threshold was set to p

< .05. We applied this statistical approach for all decoding analyses.

Challenge II: Decoding cueing conditions. Our secondary and complementary analysis

focused on decoding the cueing conditions (i.e., exogenous single cueing versus double

cueing). We followed a similar three-fold procedure as described previously, except for

the following changes described below.

For exogenous orienting cue-related EEG, we examined the cue-related

lateralized ERP, LAI and the lateralized alpha phase clustering. To get at this, we

averaged trials from bins separately for ipsilateral and contralateral channels and then

subtracted the resulting time series from one another (i.e., contralateral minus ipsilateral).

This process resulted in three averaged time series that we used for decoding, akin to the

procedure above. Each bin contained 32 trials. Again, we separated trials in the double

cueing condition into trials where both cues pointed to the same direction and trials where
cues pointed in opposite directions

For target-related EEG, we decoded cueing conditions (i.e., single versus double
cueing) based on exogenous cue-validity ERPs. We performed this analysis across
contralateral and ipsilateral channels separately and split trials in the double cueing
condition into trials where the cues pointed to the same or opposite direction. We
averaged trial bins separately for cue valid and invalid trials and subtracted these
waveforms (i.e., exogenous cue valid minus exogenous cue invalid) before training and
testing the data. This analysis yielded three averaged time series for our decoding
analysis per condition akin to the approach described above. Each bin used to compute
the average time series contained 14 trials.

Applying principal component analysis to the cue-related exogenous orienting of
attention. We aimed to isolate the effects of endogenous attention over the exogenous
cue-related processes based on the encoding model. For this analysis, we trained SVM
classifiers to decode the exogenous orientation of attention (i.e., left versus right) using
the three-fold cross-validation approach we described previously over cue-related ERPs.
Decoding of exogenous orienting was trained and tested separately for single exogenous
cueing, double cueing when both cues indicate the same location, and lastly double
cueing when both cues indicate opposite locations. We therefore divided trials into
separate bins for all three conditions – 16 trials per bin. For all three conditions, we
evaluated decoding performance against chance-level using cluster-corrected one-
sample t-tests. Next, we examined the encoding model using an established procedure,
whereby we extracted the beta weights from each classifier at each time point and then
we multiplied them by the covariance of the corresponding ERP data (Haufe et al., 2014).
For each participant, we then averaged the encoding model from all the iterations, which
resulted into variations of the SVM beta weights across the time series. Next, we
averaged these time series of SVM beta weights across all participants for each condition
separately. We applied principal component analysis (PCA) to the averaged SVM beta
weights from single cueing, double cueing when cues indicate the same location and

double cueing when cues indicate opposite locations. Next, we rotated the loadings using
varimax rotation and kept the first two components, which explained 84.5% of the total
variance. We plotted the topography from both components. We then projected the
averaged SVM weights from each participant and cueing conditions onto both
dimensions. Lastly, we compared all three cueing conditions using cluster-corrected one-
sample t-tests across the time series of SVM weights and PCA components separately.

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SUPPLEMENTARY MATERIAL

We present the tables from all hierarchical linear regression models for predicting correct response times. We performed the comparison and selection of models using chi-square goodness-of-fit tests and Bayesian Information Criterion (BIC). The best fitting model is highlighted in bold.

Table 1. Single cueing task. Hierarchical linear regression models for predicting RTs as a function of exogenous cue validity.

Models	X^2	p-value	BIC
RTs ~ β0 + S0 [*Subject*] + ε			148220
RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + ε	**210.91**	**p < .001**	**147990**

Table 2. Single cueing task. Hierarchical linear regression parameters of the best model for predicting RTs as a function exogenous cue validity.

Model: RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + ε

Variables	Coefficient	Std. Error	95% C.I.
Intercept	630.19	14.62	[601.53, 658.85]
Exo Cue Validity	-41.28	2.82	[-46.83, -35.74]

Table 3. Double cueing task. Hierarchical linear regression models for predicting RTs as a function of exogenous and endogenous cue validity.

Models	X^2	p-value	BIC
RTs ~ β0 + S0 [*Subject*] + ε			14530
RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + ε	166.27	p < .001	145150
RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + β2[*Endo.CueValidity*] + ε	**48.37**	**p < .001**	**145110**
RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + β2[*Endo.CueValidity*] + β3[*Exo.CueValidity* × *Endo.CueValidity*] + ε	< .1	p = .98	145120

Table 4. Double cueing task. Hierarchical linear regression parameters of the best fitting model for predicting RTs as a function exogenous and endogenous cue validity.

Model: RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + β2[*Endo.CueValidity*] + ε

Variables	Coefficient	Std. Error	95% C.I.
Intercept	670.72	16.36	[638.66, 702.78]
Exo Cue Validity	-39.27	3.04	[-45.22, -33.32]
Endo Cue Validity	-22.41	3.21	[-28.73, -16.11]

Table 5. Comparing single to double cueing – same cueing location. Hierarchical linear regression models for predicting RTs as a function of exogenous cue validity and task.

Models	X^2	p-value	BIC
RTs ~ β0 + S0 [*Subject*] + ε			221920
RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + ε	315.65	p < .001	221610
RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + β2[*Task*] + ε	114.18	p < .001	221540
RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + β2[*Task*] + β3[*Exo.CueValidity × Task*] + ε	**14.01**	**p < .001**	**221490**

Table 6. Exogenous cueing effect across single and double cueing – same cueing location. Hierarchical linear regression parameters of the best fitting model for predicting RTs as a function exogenous cue validity and task.

Model: RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + β2[*Task*] + β3[*Exo.CueValidity × Task*] + ε

Variables	Coefficient	Std. Error	95% C.I.
Intercept	630.3	14.83	[602.7, 657.91]
Exo Cue Validity	-41.28	2.93	[-47.02, -35.55]
Task	39.98	4.18	[31.78, 48.18]

Exo.CueValidity × Task	-19.91	5.31	[-30.33, -9.49]

Table 7. Exogenous cueing effect across single and double cueing – opposite cueing locations. Hierarchical linear regression models for predicting RTs as a function of exogenous cue validity and task.

Models	X^2	p-value	BIC
RTs ~ β0 + S0 [*Subject*] + ε			221030
RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + ε	241.58	p < .001	220820
RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + β2[*Task*] + ε	110.89	p < .001	220680
RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + β2[*Task*] + β3[*Exo.CueValidity × Task*] + ε	**20.82**	**p < .001**	**220660**

Table 8. Exogenous cueing effect across single and double cueing – opposite cueing locations. Hierarchical linear regression parameters of the best fitting model for predicting RTs as a function exogenous cue validity and task.

Model: RTs ~ β0 + S0[*Subject*] + β1[*Exo.CueValidity*] + β2[*Task*] + β3[*Exo.CueValidity × Task*] + ε

Variables	Coefficient	Std. Error	95% C.I.
Intercept	630.32	14.44	[602.01, 658.62]
Exo Cue Validity	-41.31	2.94	[-47.08, -35.54]
Task	18.13	3.34	[11.59, 24.69]
Exo.CueValidity × Task	24.48	5.37	[13.98, 35.07]

Next, we used multivariate pattern classification to examine the effects of exogenous orienting on cue-related and target-related neural dynamics across single and double cueing. We used a three-fold cross-validation approach described in the method section across two separate decoding challenges. Supplementary Figure 1 provides a description of the pipeline we used.

A. decoding pipeline applied to each participant and timepoint seperately

repeat 3x for all combinations

EEG data of participant i	divide EEG trials into three equal bins	average trials within bins	train SVM at timepoint i	validation SVM at timepoint i

bin 1
bin 2
bin 3

repeat 50x for each timepoint and particiapnt

B. decoding challenges

Challenge I: Generalization of decoding

Challenge II: Decoding cueing conditions

train on single cueing

validation single cueing

validation double cueing

train SVM

validation SVM

Supplementary Figure 1. Decoding pipeline that we applied at the subject-level (**A**). For each participant, across all channels, we randomly separated epoched EEG time series from each trial in three separate bins. We then averaged the time series from each bin separately. We used SVM to decode the effects of exogenous attention. For each time point, we trained the classifier using two data points and then validated it on the remaining one. We iterated this process three times so that each averaged epoched was used twice for training and once for validation. We applied this strategy across two decoding challenges (**B**). In the first challenge, we focused on classifiers trained and validated during single cueing and examined how well they performed in the context of double cueing. For the second challenge, we validated whether SVM classifiers could decode the cueing condition: Single versus double cueing.

Challenge I: Generalization of decoding

We first applied this decoding approach to cue-related and target-related waveforms. We evaluated classification performances using cluster-corrected one sample t-tests against chance-level (i.e., 50%). Here, the validation procedure shows that the classifiers were able to perform above chance level (i.e., 50%) in all conditions for single cueing (supplementary Figure 2A and 2B). Next, we examined how well these classifiers performed when they were tested in the context of double cueing. Again, the classifiers performed better than chance-level (supplementary Figure 2A and 2B).

Training and Validation
Single Cueing
Exogenous Attention Alone

Testing
Double Cueing
Exogenous and Endogenous Attention
are Oriented in the **SAME** Direction

Testing
Double Cueing
Exogenous and Endogenous Attention
are Oriented in **OPPOSITE** Directions

A. Decoding of Exogenous Orienting Using Event-Related Potentials

B. Decoding of Exogenous Cue Validity Using Event-Related Potentials

Supplementary Figure 2. Multivariate classification of exogenous orienting and cue validity where we trained and validated SVM linear classifiers in the context of single cueing and validated it in contexts of single and double cueing. We separated double cueing into trials where both cues were indicating the same location and trials where they indicated opposite locations. Classification was done at subject-level. We evaluated classification performances using cluster-corrected one sample t-tests against chance-level (i.e., 50%). Grey lines indicate significant clusters. Error bars indicate the SEM for each condition. **A.** Decoding the direction of exogenous orienting based on cue-locked ERPs. **B.** Decoding exogenous attention cue-validity based on target-locked ERPs.

We similarly examined the generalization of classifiers trained in the single cueing condition to the double cueing condition using the power and phase of alpha rhythms. First, we confirmed that validation was better than chance-level using cluster-corrected one sample t-tests against chance-level (i.e., 50%; supplementary Figure 3A and 3B). We then examined how well these classifiers would perform in the double cueing condition. Classification performance was above chance level when both cues indicated the same location. However, when both cues indicated opposite locations, classification performance dropped below chance level (supplementary Figure 3A and 3B).

A. Decoding of Exogenous Orienting Using Lateralized Alpha Index

B. Decoding of Exogenous Orienting Using ITPC for Alpha Oscillations

Supplementary Figure 3. Multivariate classification of exogenous orienting and cue validity where we trained and validated SVM linear classifiers in the context of single cueing and validated it in contexts of single and double cueing. We separated double cueing into trials where both cues were indicating the same location and trials where they indicated opposite locations. Classification was done at subject-level. We evaluated classification performances using cluster-corrected one sample t-tests against chance-level (i.e., 50%). Grey lines indicate significant clusters. Error bars indicate the SEM for each condition. **A.** Decoding the direction of exogenous orienting based on cue-locked lateralized alpha oscillations **B.** Decoding the direction of exogenous orienting based on cue-locked intertrial phase clustering of alpha oscillations.

Lastly, we aimed to explore the encoding model of cue-related processes of exogenous attention. We applied principal component analysis (PCA) to the classifiers' weights to uncover the underlying components to exogenous orienting. In this effort, we decoded the direction of exogenous attention across single cueing alone, double cueing when both cues indicate the same location and double cueing when both cues indicate opposite locations based on cue-related waveform. We validated these classifiers against chance level across all conditions (supplementary Figure 4A, 4B, 4C). We then extracted the beta weights from these conditions (supplementary Figure 4D, 4B, 4C). PCA was applied to these weights. See Method section for more details.

Supplementary Figure 4. Multivariate classification of exogenous orienting based on cue-related waveform across single cueing, double cueing when both cues indicate opposite locations, double cueing when both cues indicate the same location. We trained and validated SVM classifier based on our three-fold cross-validation across all conditions. Classification was done at subject-level. We evaluated classification performances using cluster-corrected one sample t-tests against chance-level (i.e., 50%) across single cueing (**A**), double cueing when both cues indicate the same location (**B**), and double cueing when both cues indicate opposite locations (**C**). Grey lines indicate significant clusters. Error bars indicate the SEM for each condition. Then, we extracted the beta weights of the SVM classifiers across the time series for single cueing (**D**), double cueing when both cues indicate the same location (**E**), and double cueing when both cues indicate opposite locations (**F**).