Quantitative analysis of surface wave patterns of Min proteins

Sabrina Meindlhumer [1], **Jacob Kerssemakers** [1] **and Cees Dekker** [1,*]

[1] *Department of Bionanoscience, Kavli Institute of Nanoscience Delft, Delft University of Technology, Delft, The Netherlands*

2 ABSTRACT

The Min protein system is arguably the best-studied model systems for biological
pattern formation. It exhibits pole-to-pole oscillations in *E. coli* bacteria as well
as a variety of surface wave patterns in *in vitro* reconstitutions. Such Min surface
wave patterns pose particular challenges to quantification as they are typically only
semi-periodic and non-stationary. Here, we present a methodology for quantitatively
analyzing such Min patterns, aiming for reproducibility, user-independence, and
easy usage. After introducing pattern-feature definitions and image-processing
concepts, we present an analysis pipeline where we use autocorrelation analysis to
extract global parameters such as the average spatial wavelength and oscillation
period. Subsequently, we describe a method that uses flow-field analysis to extract
local properties such as the wave propagation velocity. We provide descriptions on
how to practically implement these quantification tools and provide Python code
that can directly be used to perform analysis of Min patterns.

Keywords: Min proteins, pattern formation, image analysis, surface protein waves, quantification, python

1   INTRODUCTION

Pattern formation is a fascinating basic phenomenon that occurs across many scales, from
galaxy formation all the way down to embryology and beyond. In chemistry and biology,
self-organizing patterns emerge from the combination of specific intermolecular interactions
and molecular transport processes.(1) Acting together, reaction and diffusion can result
in inhomogeneous concentrations of molecules that constitute spatiotemporal patterns.(2)
Such patterns provide useful functions as they impose directional or positional preferences
on processes in cells and tissues.(3, 4, 5) Indeed, pattern formation is of vital importance
for the description of a multitude of biological phenomena, ranging from bacterial and
eukaryotic cell division(4), to embryonic development of multicellular organisms(3, 5), up
to entire ecosystems(6).

For example, in *E. coli* bacteria, a pattern-forming mechanism acts to determine the
central position of the rod-shaped cell, ensuring that the required protein-machinery is
guided to the correct location to start a fully symmetric division into daughter cells. This
particular pattern-forming system, formed by the Min proteins, relies on a reaction-diffusion
mechanism and is widely considered to be the best-studied model system for intracellular
pattern formation.(4, 7) As the moment of cell division approaches, Min proteins will
periodically bind and unbind the inner membrane at the poles of the bacterium. When
visualized by fluorescent labelling, the Min proteins are observed to oscillate from pole
to pole with a period of approximately one minute. As a result, their temporally averaged
concentration is minimized at the mid-cell location. One component of the Min system,

MinC, exerts an inhibitory effect on a component of the cell division machinery. As the
lowest concentration of MinC is found at mid-cell, the proteins that facilitate cell division
will preferably bind there, and the cell gets divided evenly.(8)

While MinC is important for this downstream process, the pattern as such is formed by
only two proteins, MinD and MinE. MinD is an ATPase that upon binding ATP can attach
to the membrane, while MinE is its ATPase activator. MinE can bind to the membrane upon
recruitment by membrane-bound MinD and subsequently facilitate MinD's ATP-consuming
membrane detachment.(9, 10, 11, 7) The Min proteins thus constitute a pattern-forming
model system with only 2 essential components, which is appealingly simple for both
theoretical and experimental studies. A wide range of experiments have been reported
that explore particular features of the Min system.(12, 9, 13) A multitude of Min protein
models(14, 15) have been proposed, and continue to be developed as new molecular details
are discovered.(16, 17, 10, 18)

Arguably, the most iconic images of Min protein patterns present themselves in *in vitro*
studies of these proteins. Such experiments typically reconstitute Min proteins on supported
lipid bilayers on a glass slide, with a fraction of Min proteins carrying a fluorescent label.(9)
Min proteins exhibit mesmerizing dynamic membrane patterns in such an artificial *in vitro*
environment: Over a wide range of concentrations, one encounters characteristic patterns
such as rotating spirals or travelling planar wave fronts, with typical wavelengths in the
order of tens of micrometers.(9, 12) An example is given in Fig. 1A, showing a snapshot
image for labelled MinE. Examination of this image reveals various features that are typical
for Min patterns. For example, Min proteins exhibit planar waves, but these occur only
locally and become less correlated on longer length scales. Min patterns thus organize in
surface domains with one dominating type of pattern, such as spiral or planar wave fronts
traveling in a certain direction. Boundaries between domains are recognizable by phase
shifts.

Thorough quantitative analysis of Min patterns is nontrivial. While visual inspection
is often sufficient to deduce the basic Min pattern, quantitative information is required
to extract trends in the patterns' characteristic parameters, such as the average or local
wavelength, oscillation period, or propagation velocity. For perfectly periodic Min patterns
with only one type of pattern with a set orientation over the entire imaged surface, analysis
can easily be achieved by Fourier analysis. However, this is most often not possible due to
the fact that real Min patterns are usually a patchwork of domains separated by phase-shift
boundaries. The semi-periodic nature of Min patterns makes image analysis challenging,
and so far there are no clear guidelines or standards on how to realise this without user
bias. Extraction of quantitative parameters is typically performed by manual selection of
individual surface positions,(19) line traces(20), or rectangular regions-of-interest(21, 12).
Plotting of fluorescence intensity along a defined axis allows to determine the pattern's
local wavelength. Similarly, the temporal characteristics such as its oscillation period and
wave propagation velocity can be measured by monitoring the intensity versus time at one
spot,(19) see Fig. 1A for an illustration of these possible practices.

While these approaches are widely used, such manual selection is cumbersome, prone
to user bias, and it underuses the vast amount of data in videos of Min patterns that could
improve data accuracy. In the example given in Fig. 1A, the intensity profile of denoted

line trace (magenta) shows approximately equidistant peaks that indicate the wavelength.
However, selection of another spot or a slightly different trace that is not perpendicular to
the wave fronts would have led to a deviating result. Furthermore, note how extending the
trace over the region of the spiral domain would erroneously lead to the inclusion of shorter
or longer wavelengths. Notably, these domain boundaries do not always remain stationary
over the time of acquisition, and hence line traces would have to be carefully adapted for
every single frame so as to adapt to possible reorientations of wave fronts (compare for
example the domain variation over time in Fig. S1A). In view of all these limitations, we
conclude that an automated user-independent analysis of large regions is preferable, as it
allows to obtain solid statistics on the patterns' characteristic features.

In this paper, we present a methodology for analyzing Min patterns that aims for thorough
quantitation, easy usage, reproducibility, and user independence. We start by briefly
proposing strategies for image cleaning. After that, we proceed to presenting strategies for
global and local analysis of Min protein surface patterns. For extracting global parameters,
we rely on calculating autocorrelation maps to examine the average periodic features of
Min patterns, following other groups(16) as well as our own.(18) We treat a Min pattern
acquisition stack as a threedimensional matrix containing information in space and time (x,
y, t), and we propose strategies on how to efficiently access this information. Subsequently,
we introduce an analysis pipeline which allows to quantify local properties of Min patterns,
such as the wave propagation speed and direction of propagation. The approach we present
here relies on the identification of individual wave crest points and their movement from one
frame to the next. While other tools have been used to extract the directional preferences
of Min surface wave propagation(22), our approach allows not only for obtaining large
distributions of parameters, but also for accessing multiple parameters at the same time.
For both global and local analysis, we offer guidance to researchers who would like to
implement similar strategies for their own applications. Code is openly available and
provided in Python 3(23).

2 IMAGE PROCESSING METHODOLOGY

Min patterns are phenomena that occur at lipid membranes. Accordingly, the most suitable
forms of microscopy for *in vitro* experiments are those that acquire an imaging slab along
the membrane-coated surface. Examples are total internal reflection fluorescence (TIRF)
microscopy,(19, 12, 16, 24) laser scanning confocal microscopy(21, 22, 20, 25) or spinning
disc confocal microscopy(18, 26). Epifluorescence microscopy(27) is generally not suitable
as it leads to high background signal from the fluorescent molecules in the bulk, significantly
reducing the pattern's quality or even making it unrecognizable.

"Image cleaning" includes procedures and operations performed on microscope data
that improve the overall quality of the image by making the features of interest better
recognizable, while not distorting or removing essential components. Good image cleaning,
where background and spurious contributions are removed, is important for successful
quantitative analysis of Min protein patterns, as insufficient cleaning can lead the algorithms
to fail to recognize the pattern as such. There are multiple imaging artefacts that need to
be corrected. For example, local fluorescent impurities such as protein aggregates may
give a static signal that is not part of the Min pattern. And depending on the microscope,

illumination is typically inhomogeneous across the field-of-view. In many cases, researchers
are interested in the time-dependent behavior of Min patterns, and for this, they acquire
images at the same spatial positions at regular time intervals ranging from seconds to
minutes. Consequently, Min proteins may bleach due to prolonged imaging.(18) Flow-cell
setups with constant bulk flow may pose additional challenges in the form of objects entering
and passing through the field-of-view or adhering to and spontaneously detaching from
the surface.(26) We empirically found that the occurrence of imaging artefacts can vary
strongly, depending on the experimental setup (specifically, the type of sample chamber and
the surface preparation), protein concentration (higher concentrations may result in more
aggregates), and experiment duration (the longer, the more aggregates occur).

With image cleaning, we aim to tackle all of these issues. Here, we propose a sequence of
standard actions that we found to yield overall good results for a time series (several frames
of the same sample position saved sequentially in an image stack) of images I_{movie} of *in
vitro* Min surface patterns. Our protocol involves the following steps:

− Correct for fluorescence bleaching by normalizing each frame to its mean intensity
value.
− Create an 'illumination correction map' I_{illum} by smoothing and averaging all movie
images, and normalizing the images to their maximum intensity.
− Create a static background image I_{stat} by averaging over all the moving (surface
pattern) features of all images in the stack. This background image then only contains
static fluorescent features such as local specks, holes, and scratches.
− Correct each image via the following image operation: $I_{cor} = (I_{movie} - I_{stat})/I_{illum}$.
− At this point, there may still be some artefacts left, for example, those that appeared
during the acquisition time and might thus not have been included in the static
background image. Therefore, remaining bright or dark artefacts can be removed
manually or by thresholding.
− Images can finally be slightly smoothed to diminish effect of sharp edges and artefacts
from the latter cropping.

In cases where it is required to explore Min patterns across very large areas, it may
furthermore be of interest to stitch multiple fields-of-view of Min patterns into larger
images.(28, 26) If the microscope's software does not offer an automatized solution for this,
stitching can be achieved by good bookkeeping and a few lines of code. When planning
to stitch images, it can be helpful to choose individual field-of-views in such a way that
there is a bit of an overlap (e.g. 5% of the width) between adjacent areas, as this makes
it easier to correctly reassemble the full image afterwards. Note that in general, adjoining
areas may not have exactly the same median intensity. Therefore, differences in median
intensity levels between individual field-of-views need to be corrected for when assembling
the stitched image. This way, the resulting large image will appear more homogeneous in
brightness and stitching borders will be less visible.

3   PATTERN ANALYSIS STRATEGIES

3.1   Global parameters

In many cases, researchers are interested in quantifying parameters such as the average
spatial wavelength and oscillation period of a Min pattern. For this purpose, they acquire
image stacks of Min patterns at a certain surface region (x, y in pixel or distance units)
and at regular time-intervals (t in time units or frames). However, the existence of domains
within and dynamics of patterns make manual extraction of these parameters a laborsome
task, and the results of such analyses (cf. Fig. 1A) may suffer from poor statistics and user
bias. Here, it is important to realize that what we are interested in are essentially global,
image-averaged parameters. In this section, we describe how quantification of such global
parameters can be achieved by performing autocorrelation analysis(29) for different slices
along time or space coordinates (x-y frames such as in Fig. 1B, t-x slices such as in Fig. 1C
or t-y slices as in Fig. 1D). We start with spatial autocorrelation, aiming to quantify the
wavelength, and then continue to present how temporal autocorrelation can be used to
quantify the oscillation period of a pattern.

3.1.1   Global wavelength

Spatial autocorrelation analysis of an image essentially compares each pixel to other
pixels around it, quantifying their (dis)similarity as a function of distance.(29) Starting
from a single image frame as shown in Fig. 2A, an autocorrelation map can be calculated
using routines from scientific libraries provided for most programming languages. Before
performing these operations, the image should be normalized by a series of actions
(subtraction of minimum intensity, division by summed-up total intensity and subtraction
of mean intensity). Using standard functions supplied within most environments, a
twodimensional autocorrelation map *crmx* can be calculated for an image frame *image* by
the transformation

$$crmx = \text{real}(\text{ifft2}(\text{fft2}(image) \cdot \text{conj}(\text{fft2}(image)))) \tag{1}$$

with *fft2* calculating a two-dimensional discrete Fourier Transformation, *ifft2* calculating
its inverse and *real* and *conj* returning the real part and complex conjugate of the input,
respectively. The four quadrants of the autocorrelation map can be re-arranged so as to place
the position ($\Delta x = 0$, $\Delta y = 0$) in the center of the image, rather than having four partial
peaks in the corners.

Close examination of the autocorrelation map in Fig. 2B reveals a general speckled pattern
as well as a ring-shaped feature that is present around the center, which is characterized by
a peak in intensity. As this central peak corresponds to a distance of zero, its high intensity
is a consequence of the self-correlation of each pixel with itself. Moving radially outward
from the center, one observes a decrease in intensity (negative autocorrelation) followed by
a peak (positive autocorrelation). An easy way to extract the pattern's dominant wavelength
is to perform an angular averaging of the profile around the central peak, where the radial
line profiles are averaged over all angles, as illustrated by the red arrow in panel Fig. 2B.
This leads to a profile as shown in Fig. 2C. The first minimum corresponds to the dark
value from the autocorrelation map. Here, the first peak after the central peak identifies

the pattern's global wavelength λ (magenta dashed line). The valley in fact corresponds to $\sim \lambda/2$ (black dashed line). Note that this value is not exactly half the wavelength, since Min profiles are typically somewhat asymmetrical (cf. Fig. 1A).

If, as often is the case, Min patterns display steady-state dynamics, then multiple time frames can be used to provide better statistics in estimating the global wavelength. Min patterns are routinely acquired at constant time intervals, which provides a series of sequential image frames, as represented in Fig. 1B. Calculating and analysing autocorrelation maps for several frames within such an image stack allows to collect a distribution of wavelengths, such as the histogram shown in the inset in Fig. 2C, summarising results for 20 consecutive frames. Indeed, for dynamic patterns, we recommend performing this analysis strategy for multiple (e.g. 10) frames and averaging the results to obtain a reliable value for the pattern's spatial wavelength. As Min patterns are typically dynamic, it is also possible that their wavelength changes over time, e.g., due to changes in external parameters. The spatial autocorrelation analysis presented here is however equally applicable to static patterns.

Identifying the peaks shown in Fig. 2C (and 2F, see following section) is trivial to the human eye, but not necessarily straightforward to automate. For our data, we achieved this via a simple algorithm that identifies the second local maximum of the trace. In doing so, we implicitly assume that the trace is fine enough to achieve sufficient accuracy and upsampling is not required. While a curve such as shown in Fig. 2C looks smooth to the eye, the original image data had a finite resolution, and accordingly, this curve contains small rags which an algorithm may erroneously detect as a local maximum. In many cases, this issue can be solved by smoothing the curve slightly before subjecting it to peak analysis. This can be achieved by applying a smoothing kernel stretching over a few pixels, for example a small fraction of the image dimension.

To avoid erroneous results, it is recommendable to plot at least one example trace (for one frame) and inspect whether the detected (averaged) wavelength position correctly co-localizes with the valley position. If no clear valley can be identified (characterized by a small or even vanishing intensity difference between the local minimum and maximum), the pattern may lack a recognizable periodicity, which could be an intrinsic property of the given pattern. Alternatively, this issue can also be encountered if insufficient image cleaning has been applied to the stack before analysis and the pattern is superimposed with too many artefacts, resulting in low autocorrelation. However, we find that this method is generally quite robust towards noise, as shown in Fig. S2B.

Further, the ratio between image size and spatial wavelength is of importance. In Fig. S3, a large-scale image stack is sequentially cropped to smaller sizes and global autocorrelation analysis as presented here is performed on randomly selected areas. Based on these results, we find that the standard deviation increases as the image sizes gets smaller, and estimate that the image dimension should be large enough to contain at least 5-10 full wavelengths for the presented algorithm to provide reliable results.

3.1.2 Global oscillation period

Another global property of interest is the average oscillation period. This parameter describes how at any given point within the imaged region, the membrane protein density

(which is proportional to the fluorescence intensity) can be expected to change over time.
We quantify the global oscillation period of a Min pattern following a strategy that closely
resembles the one presented for obtaining the global wavelength in the preceding section.

To obtain quantitative information on the temporal dynamics of Min patterns, Min patterns
are typically acquired as time series. A time series such as the one shown in Fig. 1B
is essentially a threedimensional (x, y, t) matrix, containing information on fluorescence
intensity as a function of space and time. Notably, for temporal analysis to be reliable, image
data has to be acquired at a rate above the Nyquist rate. Min patterns are characterized by
point-wise temporal periodicity (compare the time evolution at a random sample position in
Fig. 1A). Hence, when acquiring a time series, intervals have to be chosen short enough to
ensure the acquisition of enough data to adequately depict the pattern's temporal dynamics.
If consecutive acquisition times in a series are chosen very far apart, the pattern may
even appear to travel towards the opposite direction. According to Nyquist theorem, for
patterns of an oscillation period τ, consecutive images in a series have to be acquired at
intervals spaced no longer than $\tau/2$ apart. In principle, the shorter these intervals are, the
better the temporal dynamics can be characterized. Min protein patterns in lipid bilayer
reconstitutions will typically exhibit wave propagation velocities of several $100\,\mathrm{nm\,s}^{-1}$(12)
and wavelengths around $50\,\mu\mathrm{m}$(9). This leads to an expected oscillation period in the order
of minutes. Acquiring sufficient images to fulfill Nyquist theorem should therefore not be an
issue in most microscope setups. In practice, finding the optimal imaging rate is a trade-off
between achieving a high temporal resolution and minimizing fluorescence bleaching.

Upon analysing a given Min pattern stack with respect to its temporal characteristics,
we found that reslicing the stack along fixed spatial coordinates simplifies data processing
and makes it more straightforward to access the temporal information contained within the
stack. Fig. 2D shows a (t, y) slice through our example image stack at fixed pixel position x.
These t-x or t-y slices are collections of kymographs for all points along the cross-section
at the fixed spatial coordinate. In Fig. 2E, we show example traces of these kymographs
along selected y positions, which then correspond to individual surface locations (x, y)
on the field-of-view shown in Fig. 2A. Analogous to the strategy presented for spatial
global analysis, Eq. (1) can be used to obtain an autocorrelation map for this slice (cf.
Supplementary Appendix *DEMO_MinDE_global_analysis*). To extract the pattern's global
oscillation period, we consider the autocorrelation map's trace at $\Delta y = 0$ for $\Delta t \geq 0$,
plotted in Fig. 2F. Including the $\Delta t \leq 0$ trace (going back in time) of the curve would not
yield additional resolution, as it contains the same information as the positive trace (going
back in time). This profile then immediately provides the averaged temporal autocorrelation
trace for all points along one fixed spatial coordinate (as indicated for fixed x by the vertical
line in Fig. 2A). If the line-averaged autocorrelation trace does not provide sufficiently high
resolution to identify a minimum indicative of the oscillation period, imaging over a longer
time and/or at shorter intervals could be necessary.

The first maximum of this curve beyond the central peak again identifies the predominant
global oscillation period τ (magenta dashed line), while the first minimum is located at
approximately $\tau/2$ (black dashed line). Statistics on τ can be collected by performing
the analysis pipeline illustrated in Fig. 2D-F for multiple cross-sections at fixed y or x,
that is, for multiple resliced frames as shown in Fig. 1C and 1D. Compared to the traces

obtained from spatial autocorrelation, which are calculated via radial averaging, these
temporal autocorrelation traces may appear rather coarse. A more advanced peak detection
can be obtained with cubic-spline fitting and subsequent extreme point analysis. Further,
the presented method for temporal autocorrelation analysis is less robust towards noise than
spatial autocorrelation, as shown in Fig. S2C. Adequate image preprocessing and cleaning
is again of high importance. Image smoothing was found to slightly increase the detected
oscillation period, albeit not above the error margins obtained for unsmoothed images, as
shown in Fig. S4.

Note furthermore that the propagation speed of a pattern may depend on the concentrations
of all components, and may change over time. Therefore, for very long time series, it can
make sense to split the stack up into multiple stacks of shorter total duration and perform
analysis for subsequent sub-stacks (compare Fig. S8). However, we estimate that an image
stack needs to span the duration of a minimum length of 3 oscillation periods for the
presented method to yield reliable results (cf. Fig. S4).

3.2 Local parameters

In this section, we present an analysis strategy that aims to quantify local parameters of
Min patterns. These parameters include the local wave propagation velocity or characteristic
local distances such as the distance between MinD and MinE wave crests. As we will
describe in more detail, local parameters can be quantified by implementing two steps: (i)
identification of wave crests for each frame within an image stack, and (ii) comparison of
intensities at and around the identified crest points from one frame to the next.

3.2.1 Local wave propagation velocity

The local wave propagation velocity is determined as the shift of individual crest points
from one frame to the next. To calculate the local velocity, we first need to identify these
crest points, and then determine their positional difference. We achieve this by applying
optical flow analysis. Optical flow is defined by how brightness patterns move from one
image to another(30, 31). For our Min patterns, we estimate an optical flow vector field using
Horn-Schunck algorithm(30, 32). This algorithm works on a pair of sequential image frames
(see Fig. 3A for example data, recorded for MinE) and returns a vector field, describing
the estimated optical flow for each pixel from the first to the second frame. Fig. 3B shows
the magnitude (indicated by image brightness) of the optical flow vectors obtained for
our example image pair from Fig. 3A. Note that the collected optical flow vectors do not
necessarily represent the local wave propagation velocities. The relation between the two
measures will depend on the wave shape, making it hard to generalize.

As a first step to identifying the positions of the wave crests within the first frame, we
use the information obtained from optical flow analysis to create a phase image. This
phase image is essentially a binary map over the whole image, which indicates whether
at any given point we are at the "front" ('ahead of the wave') or "wake" region of the
wave ('behind the wave'). These regions are characterized by a decrease or increase in
fluorescence intensity, respectively, along the direction of movement. If we consider any
specific surface location and its corresponding vector obtained from optical flow, we can
follow the direction of that vector over a short distance (say 3 pixels) within the same frame,

and determine whether the fluorescence intensity is decreasing or increasing. The outcome
of this procedure for our example frames is shown in Fig. 3C. Using this phase image, we
can identify those positions in the image that make up the wave crests – which form the
backbone structure of the pattern. Wave crests are identified by the positions at which a
transition from the front to a wake region occurs. Fig. 3D shows the wave crests identified for
the first frame in red. Subsequently, we need to determine the direction of wave propagation
for these individual crest points. While we have a set of vectors available for distinct (x, y)
positions from optical flow analysis, their directions will in general not be exactly normal
to the wave crests due to noise. Therefore, we calculate vectors which are perpendicular
to the lines of wave crests, and determine their correct directionality (pointing towards the
front of the wave) using the information already present in the phase image. In Fig. 3D the
direction of propagation is indicated by vectors at distinct crest points throughout the image
for illustration. Following the procedure outlined here and in Fig. 3A-D, we thus effectively
obtained (i) a list of positions, identifying the wave crest point positions, and (ii) a list of
vectors, describing their direction of movement from the current to the next frame.

The next step is to quantify how far these crest points moved during the transition from the
current to the next frame. Upon quantifying this positional shift, the velocity magnitude is
given by this distance divided by the time that passed between the acquisition of subsequent
frames. The procedure is illustrated in Fig. 3E-F for three example crest points. For each
crest point, we considered the fluorescence intensity traces along the direction of movement
at the given position (i.e., perpendicular to the wave front). Starting from the crest position,
we plotted this trace up to a distance corresponding to roughly half the (global) wavelength
of the pattern. Choosing this distance should ensure that the next frame's peak is still within
the sampling range (provided that the time resolution of the acquisition stack is sufficiently
high, cf. section 3.1.2). In Fig. 3E, the example traces along which intensities are plotted
are highlighted in white. For sampling positions along this trace which are located off the
pixel grid, intensities can be estimated by interpolation. This yields an intensity trace at
sub-pixel resolution. This intensity trace will have a maximum located very close to the
center of the originally determined crest position, with a small offset that can be attributed
to the additional smoothing step performed before optical flow analysis, and is generally
not significant (cf. Fig. S5 and adjoined table).

Next, we performed exactly the same procedure at the same positions on the next frame.
As shown in Fig. 3E and Fig. 3F, these positions are now no longer centered around the
maximum of the intensity trace, but offset from them by a certain distance. This distance is
the positional shift that we need to obtain for quantification of the local wave propagation
velocity. Performing peak fitting allows to identify the two traces' peak values and measure
the shift d in crest peak position at sub-pixel resolution.

Performing this analysis for all identified crest points along all sequential pairs of frames
in an stack eventually yielded a list of velocity vectors with components (v_x, v_y) at frame n
for a wave crest at position (x, y). Image smoothing is an important technical aspect of the
local analysis presented here. We first perform a light image smoothing (with a limited initial
smoothing kernel) to de-noise the image and to simplify peak detection such as shown in
Fig. 3F. For optical flow analysis (Fig. 3B), we perform an additional smoothing step with a
more extensive secondary smoothing kernel. The effect of different initial smoothing kernels

is illustrated in Fig. S6, the effect of increasing image noise in Fig. S2D and E. Further,
applying Horn-Schunck algorithm(30) requires setting a few parameters, particularly the
regularization constant and the number of iterations. Here, we determined their values by
trial-and-error from evaluating simulated as well as real Min protein pattern data and kept
both constant from then on.

Depending on what kind of information is of interest, the obtained distribution of velocity
vectors can be represented in different ways. A representation that combines information on
the magnitude and directional preference is a 2D histogram such as the one shown in Fig. 3G
for an example image stack of MinE data. If the magnitude of the wave propagation velocity
is most important, the velocity magnitudes v can be plotted in a histogram to visualize their
distribution and peak value, as shown in Fig. 3H. In other cases, the directional information
may be of prime interest, for example, when studying the influence of an external bulk flow
(26) or physical environmental parameters on the pattern.(22) For each vector component, an
angle α can be calculated that corresponds to the wave crest point's direction of movement
with respect to the direction of applied flow. The occurrence of different directions can then
be plotted in a regular or polar histogram, as shown in Fig. 3I. As shown Fig. S7, the method
can be applied to a wide range of image sizes. Decreasing the area on which analysis is
performed generally leads to smaller standard deviation in velocity magnitude distribution,
which is linked to a loss in directional information.

393 3.2.2 Local MinD/MinE crest shift

When studying Min protein patterns, researchers routinely acquire data in two channels,
for fluorescently-labelled MinD and MinE, respectively. Both these proteins exhibit a peak
in their surface density, but these two peaks do not coincide in space and time (an example
is given in Fig. 4A).

To determine these differences, the analysis pipeline presented in section 3.2.1 for
obtaining wave propagation velocity between sequential frames can be slightly adapted
for measuring the difference in crest position between MinD and MinE waves. This can
be achieved by first performing crest detection (analysis pipeline shown in Fig. 3A to D)
for one stack, e.g. the MinD stack. The crest points attributed to the MinD stack can then
be compared to the corresponding frame of the MinE stack, analogous to the comparison
shown in Fig. 3E. The collected peak shifts d can be visualized in a histogram, such as
shown in Fig. 4B for our example data.

4 DISCUSSION

In this paper, we proposed protocols that can be applied to analyze data on *E. coli* Min protein
surface patterns with respect to quantitative parameters such as the spatial wavelength,
oscillation period, or wave crest propagation velocities. Our primary goal was to develop
user-independent and largely automatized strategies for pattern analysis in order to (i)
improve comparability of results obtained from different studies and research groups, and
(ii) provide tools for quantification of experimental data for comparing results to theoretical
studies. We presented global and local analysis methods which both can be valuable
depending on what kind of pattern information is of interest. All of the routines that we

suggested and described can be further modified to better fit the requirements posed by a
particular research question – thus providing a framework that others can build upon.

The methodology we describe can be combined with many of the aspects and practices
of Min pattern analysis which we did not cover here. For example, in studies investigating
absolute or relative local concentrations or concentration gradients of MinD and MinE on the
surface, fluorescence calibration can be important. Calibration allows to relate fluorescence
intensity to the local membrane protein density.(19, 21, 12, 16) However, in many cases the
patterns as such – their shapes, domains, wavelength, or dynamics – can be studied without
this step, using the acquired fluorescence intensity data in arbitrary units, and this is what
we focused on in this paper.

The global analysis that was presented here provides parameters averaged over entire
image frames (spatial analysis) or slices along fixed spatial coordinates (temporal analysis).
We found that for well-cleaned images, spatial autocorrelation robustly quantifies the
main dominant wavelength within an image frame, as identified by the distance at which
maximum self-correlation is present. This yielded results that are very comparable to those
obtained by manual quantification, albeit with higher statistical reliability (see Fig. S1 for
an example comparison of manual and automatic analysis). For temporal autocorrelation,
we recommend re-orienting the image stack into slices of fixed x- or y-coordinates and
calculating autocorrelation-maps along sets of kymographs, as described. We found this to
be an efficient way to access large parts of the information provided within the image stack.
Pixelwise analysis of intensity traces at distinct surface location, autocorrelation thereof and
subsequent averaging is a more straightforward approach. However, we found that taking
this detour via reslicing as presented in this paper reduces computational time by about two
orders of magnitude, and hence, allows for easier processing of large amounts of data (cf.
SI).

In many cases, parameters obtained from spatial and temporal analysis can be averaged for
several frames/slices. However, whether this is justified depends on the time evolution of the
pattern over the course of the acquisition. Fig. S8 shows the temporal autocorrelation results
for an example image stack which shows a decline in oscillation period over time. This is
visible from the spreading of peaks in the resliced image (cf. Fig. S8A) as well as in the
variation in the shape of the $\Delta x = 0$ traces (cf. Fig. S8B). In such a case, averaging is only
justified over the part of the stack that shows a constant temporal periodicity. If required,
the routines can be expanded to include peak analysis of single traces in the kymograph set
and automatically determine up to which point averaging is permitted.

Local analysis, in contrast to global analysis, directly provides large-number distributions
of parameters even when analysing only two consecutive images. Our approach to local
analysis relies on the identification of wave crests and quantification of the positional
shift thereof from one frame to the next. The first step can in principle be achieved by
various strategies. For example, one could implement an algorithm that relies on thresholds
of fluorescence intensity to identify peaks. Here, we presented a strategy that relies on
established algorithms for optical flow analysis, as it offers certain advantages, such as
direct access to the vector fields. We have already successfully used this local analysis
methodology to examine and quantify the response of Min protein patterns to hydrodynamic
bulk flow.(26) Numerous other applications can be imagined, in which a surface pattern is

either exposed to an external stimulus and responds to it, or in which the time evolution of
its characteristic properties is relevant. Using the local analysis pipeline presented here (or
modifications thereof) allows to systematically quantify properties of interest with proper
statistics rather than relying on qualitative description alone.

As our local analysis routine essentially offers a way to acquire a high number of intensity
traces that are locally perpendicular to the wave fronts, it opens up possibilities for further
in-depth analysis. Our brief illustration of a MinD-MinE crest distance detection is only
one example of a parameter that can be extracted using an optical-flow-based routine. For
example, it is imaginable to modify our local analysis pipeline such that it facilitates fast
visualization of local fluorescence intensity profiles for both MinD and MinE waves. Upon
fluorescence calibration, the fluorescence intensity can be converted to membrane protein
density, and hence the relative peak heights can be connected to the protein ratio at the
surface. Further, information obtained from local and global analysis can be combined, and
local velocity analysis can provide an alternative to global methods if their requirements are
not met. For example, while we found that a certain minimum number of entire oscillations
is required for global temporal analysis to yield results (cf. Fig. S4), local analysis can
already be performed on only two consecutive frames, and can be combined with global
spatial analysis to serve as an alternative route to determining the predominant oscillation
period.

Finally, we note that the general strategies presented within this paper are not restricted
to application to the analysis of *E. coli* Min protein surface patterns. Min protein patterns
have some properties that are very specific to them – such as their quasi-periodic nature,
dynamic oscillatory behavior, and their organization within domains – and our routines
are designed for these specific properties. However, the routines presented here may very
well be modifiable and applicable to quantify other types of semi-periodic surface patterns,
biological or not, for example to the fascinating reaction-diffusion patterns of chemical
systems like the BZ-AOT system(33). We hope that our analysis toolbox will help to further
disentangle the intriguing mechanisms that underlie pattern formation.

CONFLICT OF INTEREST STATEMENT

486 The authors declare that the research was conducted in the absence of any commercial or
487 financial relationships that could be construed as a potential conflict of interest.

AUTHOR CONTRIBUTIONS

488 S.M. contributed to the provided image analysis tools and their representation, created the
489 figures and co-wrote the paper. J.K. identified suitable image analysis methods, developed
490 the majority of the provided tools and co-wrote the paper. C.D. co-developed the underlying
491 methodology and co-wrote the paper.

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CODE AND DATA AVAILABILITY STATEMENT

The code created for this study as well as example data are openly available and can be found on GitHub at `https://github.com/M-Sabrina/MinDE_analysis_2022` and Zenodo at `https://zenodo.org/record/6724666` (second release). Please refer to Supplementary Material for further information.

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FIGURES

Figure 1. Min acquisition stacks contain spatial and temporal information on the pattern.

Min protein surface patterns are dynamic in space and time. Min pattern acquisitions are
3D (x, y, t) matrices, containing the measured fluorescence intensity values for different
coordinates. The information contained within this matrix can be accessed and visualized
differently, dependent on what parameters are of interest. **A** Left: Example of a real MinE
protein surface pattern. Middle: Fluorescence intensity over time at the surface position
highlighted by orange cross in the image, for an image stack comprising 20 frames. Right:
Fluorescence intensity trace along surface cross-section highlighted in magenta in the image.
B 3D view of a Min protein acquisition stack with four example images (standard x-y slices)
shown for demonstration. **C** 3D view of slice from A, resliced along constant y-directions,
creating t-x slices. **D** 3D view of slice from A, resliced along constant x-directions, creating
t-y slices.

Figure 2. Overview of the autocorrelation analysis pipeline to obtain global parameters.

A Example of a Min protein surface pattern, single frame. Color brightness indicates
fluorescence intensity (a.u.). **B** Autocorrelation map of the frame shown in A. Color
brightness indicates intensity. Red dashed line indicates radial averaging. **C** Averaged
radial profile for the autocorrelation map shown in B. The first maximum after the central
peak at distance zero is a measure of the the patterns global characteristic wavelength.
The identified wavelength λ is highlighted by the magenta dashed line. The first valley
is positioned at approximately $\lambda/2$ (black dashed line). Inset: the analysis presented in
A-C can be performed for all individual frames within an image stack. Here, the collected
results for 20 consecutive frames (image stack also represented in Fig. 1B) are shown in
a histogram. A λ of 54 pixels is deduced. **D** Resliced image for fixed x; same as shown
in Fig. 1D. **E** Selected temporal traces for the y-positions indicated in D. All point-traces
shown in the kymograph in D will be included in the autocorrelation trace shown in F.
F Line-averaged autocorrelation trace from point-traces (such as shown in E) in blue, cubic
spline fit used for peak-detection in green. The first maximum after the central peak at
$\Delta t = 0$ measures the average characteristic oscillation period of the pattern. The identified
global oscillation of $\tau = 4$ frames is highlighted by the magenta dashed line. The first valley
is positioned approximately at $\tau/2$ (black dashed line). The analysis pipeline illustrated in
D-F can be performed for multiple slices (fixed x or y) of the image stack.

Figure 3. Overview of analysis pipeline for determining local wave propagation velocities.

A Local analysis relies on sequential pairwise comparison of frames within an image
stack. Example frames are here referred to as frame 1 and frame 2. **B** the Horn-Schunck
algorithms is used to compute optical flow of the image pair (from frame 1 to frame 2) These
return one vector per pixel, indicating the shift. Brightness indicates the vector magnitude.
C Phase image of frame 1. The phase is determined by whether the wave intensity goes
up ("front" of the wave, bright color) or down ("wake" of the wave, dark color) following
the direction of the vector obtained from the optical flow analysis. **D** Wave crests can be
identified by the transitions from front to wake as denoted in panel C. Red lines show the
identified wave crest locations. Selected arrows indicate the direction of movement of the
crests as determined from the optical flow. **E** Left: Zoom-in of frame 1 at the location
highlighted in panel D. Wave crest points are indicated by red dots; direction of movement
as identified by optical flow analysis are indicated by arrows. Right: Zoom-in of frame 2 at

the same location. Crest points of frame 1 are indicated by red dots. In both images, 3 crest
point positions are highlighted by white line traces parallel to the direction of propagation
at these points (i.e., normal to the wave fronts). **F** Intensities versus distance along the white
lines in panel E. Starting from the crests identified for frame 1 (red dots), intensities are
sampled at discrete sub-pixel positions perpendicular to the wave front. Smoothed intensity
traces are shown in red for frame 1 and in blue for frame 2. The translocation d of each
crest position is then determined from the peak shift, allowing to calculate a velocity vector
with magnitude v. Wave crest velocities can be calculated for each crest and each sequential
pair of frames in an image stack. **G** Velocity distribution of a pattern can be visualized as
a 2D histogram. **H** Velocity histogram that provides the average velocity magnitude v as
well as the distribution of velocities within a given pattern. **I** Histogram of angles of the
wave propagation vector (left) and an angular diagram denoting the occurrence of various
pattern velocities (right). From the list of velocity vectors, we have immediate access to the
propagation directions present within a pattern, the occurrence of which can be visualized
in a histogram (left). The information can be represented as a polar histogram (right).

Figure 4. Using the local analysis pipeline to determine local MinE-MinD crest positions shifts.

A MinD (magenta) and MinE (green) patterns. The pipeline for local analysis shown in
panels A-F can be used to quantify other properties of the pattern, such as the MinE-MinD
crest point distance in a simultaneous dual-channel acquisition. Here, crest point detection
was performed for each frame of the MinD stack. Subsequently, the intensity traces at
these positions were compared to those of the corresponding MinE frame. **B** Distribution of
MinE-MinD crest point distances.