Title

Estimating clade-specific diversification rates and palaeodiversity dynamics from

reconstructed phylogenies

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Abstract

One of the central goals of macroevolution is to understand palaeodiversity dynamics through time

and space, and its potential drivers. Estimating palaeodiversity dynamics has been historically

addressed with the fossil record because it directly reflects the past variations of biodiversity.

Unfortunately, some groups or regions lack a good fossil record, and dated phylogenies can be

useful to estimate deep-time diversification dynamics. Recent methodological developments have

unlocked the possibility to investigate palaeodiversity dynamics with dated phylogenies by using

birth-death models with non-homogeneous rates through time and across clades. One of them,

which models rate heterogeneity as a local clock, seems particularly promising to detect clades

whose diversity has declined through time. However, empirical applications of the method have

been hampered by its lack of automation. Here we propose an automation with additional features

accounting for recent developments and we implement it in the R package RPANDA. We also test

the approach with simulations focusing on its ability to detect shifts of diversification and to infer

palaeodiversity dynamics. Finally, we illustrate the automation by investigating the palaeodiversity

dynamics of Cetacea, Vangidae, Parnassiinae, and Cycadales. Simulations showed that we

accurately detected shifts of diversification although false positive errors are higher for complex

models. The median global error of palaeodiversity dynamics estimated with the automated model

is low showing that the method is able to capture diversity declines. We detected shifts of

diversification for three of the four empirical examples considered (Cetacea, Parnassiinae and

Cycadales). These heterogeneities of diversification rates unveil a waxing-and-waning pattern due

to a phase of negative net diversification rate embedded in the trees after isolating recent radiations.

Our work allows to easily apply non-homogeneous models of diversification in which rates can

vary through time and across clades to reconstruct palaeodiversity dynamics. By doing so, we

detected palaeodiversity declines among three of the four groups tested, highlighting that such

periods of negative net diversification might be common. We discuss the extent to which this

approach might provide reliable estimates of extinction rates and we provide guidelines for users.

Keywords

Birth-death model, macroevolution, palaeodiversity, rate heterogeneity, RPANDA.

1 | Introduction

Estimating palaeodiversity dynamics over geological timescales is a thrilling goal of macroevolution (Alroy et al. 2008; Quental and Marshall 2010; Morlon et al. 2011). This question is generally addressed with paleontological data because fossil records are direct witnesses of past diversity dynamics (Marx and Uhen 2010; Ezard et al. 2011). Unfortunately, the fossil record is not homogeneous over time, space and groups (Close et al. 2020). Consequently, investigating evolutionary history of poorly fossilised groups relies on diversification analyses based on dated phylogenies (timetrees) mainly composed of extant species. Methodological developments in the field have focused on estimating the speciation rate (λ) and extinction rate (μ), which represent the pace at which lineages appear and go extinct, respectively, as well as the net diversification rate (noted r) defined as the difference between them (Ricklefs 2007; Stadler 2013; Morlon 2014). A large variety of phylogenetic models allows testing evolutionary hypotheses on whether diversification rates are constant, vary over time (Rabosky and Lovette 2008; Morlon et al. 2010), across clades (Morlon et al. 2011; Rabosky et al. 2013; Maliet et al. 2019) or in association with species' traits (Maddison et al. 2007; FitzJohn 2012; Beaulieu and O'Meara 2016) or with environmental changes (Condamine et al. 2013, Condamine, Rolland & Morlon 2019). However, early studies have shown that reconstructed dated phylogenies can display heterogeneity of diversification rates across clades (Rabosky et al. 2007, Esquerré et al. 2019).

Among the methods developed to detect this heterogeneity (Alfaro et al. 2009; Bokma and Stadler 2013; Rabosky et al. 2013; Maliet et al. 2019; Barido-Sottani et al. 2020; Maliet & Morlon 2022), the model developed by Morlon et al. (2011) takes into account heterogeneity in diversification rate by testing for shifts in rates of diversification at specific branching points in the

phylogeny. The diversification of subclades identified *a priori* based on taxonomy or ecological

traits, and the diversification of the ancestral group leading to these clades, hereafter called the

backbone, can be analysed separately. The main advantage of this method is that each part of a

phylogeny (subclades and backbone) can follow a different birth-death model, offering the

opportunity to test biological hypotheses that create heterogeneity of diversification rate and thus

reconstruct palaeodiversity dynamics for each part of the tree (Nee et al. 1992; Morlon et al. 2011;

Morlon 2014). Doing so for Cetacea, Morlon et al. (2011) showed a good consistency in the trend

of the palaeodiversity dynamics between the molecular phylogeny and the fossil record. Recent

advances have improved palaeodiversity estimation with a probabilistic approach providing

confidence intervals of palaeodiversity values (Billaud et al. 2020). Subclades might experience

recent adaptive radiations due to the acquisition of key innovations (Jønsson et al. 2012; Drummond

et al. 2012) while the backbone tree might display a different dynamic such as a waxing-waning

pattern of diversification. The resulting heterogeneity of diversification rates cannot be detected in

clade-homogeneous birth-death models because recently radiating clades can overshadow the

estimation of extinction in other parts of the tree, and likely hamper the inference of a negative net

diversification rate ($r < 0$, $\mu > \lambda$) that may explain such a period of diversity decline (Morlon et al.

2011). The waxing-waning pattern detected by Morlon et al. (2011) was promising, yet the

approach developed in that paper, part of which was made accessible in the R package RPANDA

(Morlon et al. 2016), has been applied to only a few empirical cases since it was proposed (Bacon et

al. 2013; Legendre and Condamine 2018; Billaud et al. 2020; Chazot et al. 2021) because of the

lack of automation.

In addition to making this method more automatic and user-friendly, several aspects of its

performance remain to be tested. It was shown that the method recovers unbiased rates of

diversification and is able to detect periods of diversity decline (Morlon et al. 2011), but its ability

to detect clade-specific shifts of diversification remains untested and can make the palaeodiversity

dynamic challenging to recover (Burin et al. 2019). More generally, several studies have questioned

our ability to estimate extinction rate from molecular phylogenies (Rabosky 2010, 2016; Louca and

Pennell 2020; but see Nee et al. 1994; Morlon 2014; Beaulieu and O'Meara 2015). Historically,

Nee et al. (1994) have demonstrated how to estimate constant extinction rate from molecular-dated

phylogenies with extant species only. Some studies relaxed the assumption of constant rates

(Rabosky and Lovette 2008, Stadler 2011a), but these models are homogeneous across clades. By

being non-homogeneous across clades, the model of Morlon et al. (2011) brings better extinction

rate estimates by revealing ancient periods of palaeodiversity decline (Stadler 2011b) in line with

the fossil record (Marx et Uhen 2010). This model opens investigating palaeodiversity dynamics for

groups without good fossil records.

In this study, we automatize the approach developed by Morlon el al. (2011) and implement

it in the R package RPANDA (Morlon et al. 2016). In addition, we provide several advances

compared to the original method. In particular, we implement the possibility to test for a shift at the

crown age of subclades, including the stems into the backbone analysis, whereas the original

version of the method tested shifts at the stem age of subclades (Morlon et al. 2011; Billaud et al.

2020). We provide functions to calculate rates and diversity dynamics through time, including

recent developments from Billaud et al. (2020) with new functions using automation outputs. Using

simulations, we assess the performance of the approach to detect shifts and to infer palaeodiversity

dynamics under various diversification scenarios. We further illustrate the approach empirically by

investigating the evolutionary history of four groups with well-sampled molecular-dated

phylogenies (Cetacea, Vangidae, Parnassiinae and Cycadales), which have been previously

analysed with other methods. We finally discussed both simulations and empirical cases to provide

guidelines and recommendations when using this approach.

2 | Methods

2.1 | The clade-dependent time-dependent diversification model of Morlon et al. (2011)

Morlon et al. (2011) developed an exact analytical expression of a birth-death model of

cladogenesis that estimates rate variation through time while accounting for undersampling thanks

to a sampling fraction (denoted f, f=1 if all described species are included in the phylogeny). The

expression is defined backward in time such as values for λ and μ for time-dependent models

correspond to rate values at present (t=0) with α and β their dependency parameters, respectively.

Then, they assumed changes of diversification rates to occur at specific branching points (nodes) of

the phylogeny. Under such assumptions, their analytical expression holds and in particular their

expressions of the probability that a lineage alive at time t has no descendant in the sample at t=0

($\Phi(t)$), and the probability that a lineage alive at time t leaves exactly one descendant lineage at time

$s < t$ ($\Psi(s, t)$, *i.e.* the probability of survival from t to s, see Appendix S8 and S9 from Morlon et al.

2011). These two expressions allow expressing the likelihood of backbone by including the

speciation event corresponding to the subclade. The probability $1 - \Phi(t_1^{cl})$ that the subclade

survives from this branch point t_1^{cl} is then included in the likelihood of the subclade expressed with

the same formula. Finally, the product of the likelihood of the subtree and the backbone gives the

global likelihood of the phylogeny while accounting for heterogeneity of diversification rates across

clades. This global likelihood can be compared to the likelihood of a diversification model with an

homogeneous model of diversification to see if the shift of diversification rate is supported. This

can be extended to a phylogeny with multiple subclades following their own diversification rates

and even shifts of diversification rates inside the backbone creating multiple backbones.

2.2 | Automation

2.2.1 | Implementation in RPANDA

Few empirical studies have applied the approach using a manual and sequential approach

(Morlon et al. 2011; Bacon et al. 2013; Billaud et al. 2020; Chazot et al. 2021). Each shift was

selected one by one among subclades defined *a priori* until either the inclusion of a new shift was

no longer statistically supported, or shifts at all nodes were supported. Instead of this sequential

approach, the automation compares a large number of combinations of shifts at the same time. The

simplest way to select clades is to follow the approach of Morlon et al. (2011) by choosing

taxonomic subclades such as families. Birth-death models require to know the sampling fraction

from a taxonomic database. The tested subclades can also correspond to clades of species sharing

key-innovations or colonisation events to test the role of these biological events on the clade's

diversification. Once subclades have been chosen *a priori,* the whole analysis is divided in four

steps: (1) calculating sampling fractions for the subclades from the taxonomic database, (2)

calculating all potential combinations of subclade(s) and corresponding backbone(s) from the set of

preselected subclades, (3) applying a set of diversification models (see section 2.2.2) to each part

(subclades and backbone) of each combination to calculate global likelihoods and the corrected

Akaike Information Criterion (AICc) for each combination and comparing their statistical support,

and (4) computing the palaeodiversity dynamics with deterministic or probabilistic approaches. The

four steps of the whole analysis are illustrated in **Figure 1**. By default, three constraints are applied:

(1) λ and μ must be strictly positive, (2) r (λ - μ) must be positive at the beginning of the

diversification history for all models, and also (3) during all the diversification history for the

constant birth-death model.

Figure 1. Conceptualization of the analytical pipeline for the automation of the method presented in Morlon et al. (2011). A) Step 1 calculates sampling fractions (*f*) from a database that contains all described species of the clade of interest and monophyletic subgroups (based on taxonomy or ecology); B) Step 2 calculates all the possible combinations of shifts; C) Step 3 applies a model comparison to select the best model for each part (sublades and backbone) of each combination. Then, it computes the likelihood and AICc of each combination, when using the best models. Finally, it selects the best supported combination. The final result is a list containing four elements: the model comparison for (1) the phylogeny analysed as a whole, (2) all subclades apart, (3) all backbones apart, and (4) the comparison of all combinations of heterogeneous diversification models based on their global AICc (see Appendix S3 for example). D) Step 4 computes palaeodiversity dynamics either with the deterministic (function *paleodiv*) or probabilistic approach (function *apply_prob_dtt*).

2.2.2 | Set of diversification models

Several features have been implemented to perform different analyses. The minimum clade size for applying diversification can be defined at each step and should be the same during the application of the whole pipeline (argument clade.size, default is 5 tips). The set of diversification

models applied by default in the model comparison corresponds to the six following birth-death

models: (1) constant pure-birth model (BCST), (2) constant birth-death model (BCST_DCST), (3)

pure-birth model with exponential time-dependency (BVAR), (4) birth-death model with

exponential time-dependency for speciation rate and constant extinction rate (BVAR_DCST), (5)

birth-death model with constant extinction rate and exponential time-dependency for speciation rate

(BCST_DVAR), and (6) birth-death model with exponential time-dependency for both speciation

rate and extinction rate (BVAR_DVAR). A subset of these models can be used for all parts

(subclades and backbones) with the argument models or only for subclades if, for example,

extinction is not expected in subclades but only in the backbone(s) (see help files in RPANDA).

2.2.3 | Testing shifts at crown or stem age

Originally, the probability of the speciation event at the stem age was included in the

likelihood of the backbone, while the probability that the stem of the subclade survives to the crown

age was included in the likelihood of the subclade. Therefore, changes in diversification rate are

tested at the stem age of the subclades. However, adaptive radiations are expected to be related to

ecological opportunities (Yoder et al. 2010) creating a long stem branch at the crown of the

subclade. We implemented the possibility to test for shifts at crown ages of subclades by including

the probability that the stem of the subclade survives to the crown age in the likelihood of the

backbone. Users can choose to test for a shift at the stem age (backbone.option="stem.shift") as in

Morlon et al. (2011), or at the crown age of the subclade (backbone.option="crown.shift").

2.2.4 | Multiple backbones

Shifts of diversification can also be nested creating combinations of shifts with more than one backbone (multiple backbones) in the phylogeny (Figure 1B, combination 3). We recommend to start analysing combinations with a simple backbone to first capture the main tendency of the backbone with the option multi.backbone=F, especially if there are a lot of combinations with multiple backbone. Then, combinations with multiple backbones can be analysed using the option multi.backbone=T or all combinations can be analysed at once with the option multi.backbone="all".

2.2.5 | Constraints and palaeodiversity dynamic estimation

Two optional constraints are embedded in the optimisation process: rate value and maximum number estimates can be constrained with a maximum value (argument rate.max and n.max) for each part of the combinations. The constraint on palaeodiversity uses the deterministic approach. The automation also includes recent developments on diversity through time estimates (Billaud et al. 2020), an approach to better estimates palaeodiversity dynamics by relying on a probabilistic approach to infer a confidence interval of diversity values. Functions that are already included in the R package RPANDA 2.0 (Morlon et al. 2016) have been slightly modified to be used with outputs of the shift.estimates() through a new function called apply_prob_dtt().

2.3 | Simulations

We used simulations to test whether the approach successfully detects diversification shifts and correctly estimates palaeodiversity dynamics (**Figure 2**). We simulated four diversification scenarios following Billaud et al. (2020). All trees were simulated forward in time over 100

millions years (Myrs, T_{max}=100) with the R package TESS 2.1.0 (Höhna et al. 2016). Rate values

were selected such as they respect the following conditions to test the performance of the approach:

1. Expanding diversity: constant pure-birth model (BCST) with $\lambda \in [0.05; 0.25]$ and μ=0

(**Figure 2A**).

2. Saturing diversity: pure-birth model with exponential time-dependency (BVAR) with

$\lambda_{(t)}=\lambda_0\exp(-\alpha t)$ with $\lambda_0 \in [0.05; 0.25]$ and α such that T_{eq} satisfies $\exp(-\alpha T_{eq})$=0.5 is in

$[T_{max}2/3; T_{max}3/4]$ and μ=0 (**Figure 2B**).

3. Waxing-waning (with decreasing speciation): birth-death model with exponential time-

dependency for speciation rate and constant extinction rate (BVAR_DCST) with $\lambda_{(t)}=\lambda_0\exp(-$

$\alpha t)$ with $\lambda_0 \in [0.2; 0.4]$ and $\mu=\lambda_0/2$ and α such that T_{eq} satisfies $\exp(\alpha T_{eq})=\mu/\lambda$ in $[T_{max}2/3;$

$T_{max}3/4]$ (**Figure 2C**).

4. Waxing-waning (with increasing extinction): birth-death model with constant extinction rate

and exponential time-dependency for speciation rate (BCST_DVAR) $\lambda \in [0.2; 0.4]$ and

$\mu(t)=\mu_0\exp(\beta t)$ with $\mu_0=\lambda/2$ and β such that T_{eq} satisfies $\exp(\beta T_{eq})=\lambda/\mu$ in $[T_{max} 2/3; T_{max}3/4]$

(**Figure 2D**).

For both waxing-waning models, α and β values are defined such that the diversity decline

starts between the last third and the last quarter of the phylogenetic tree (*i.e.* between 33 and 25

Myrs ago in our case). We retained the simulated trees containing at least 40 species. We simulated

the diversification shift by grafting a new simulated tree at a specific node defined as the more

recent node among nodes between 33 and 25 Myrs ago (**Figure 2F**). This node must have a

minimum of five extant species to avoid applying diversification models on a species-poor clade

when testing for the detection of a shift on raw phylogenies. For trees with a shift of diversification,

the grafted tree follows a pure-birth model (BCST) with $\lambda=0.1$ (**Figure 2E**). This tree was grafted at

its crown age and must contain at least 15 species. Because the shift was simulated at the crown

age, the search for shift was also conducted at crown ages.

We quantified whether the model detected a shift of diversification while no shift was

simulated (*i.e.* false positive error), following Billaud et al. (2020), we also calculated the global

error *D* between the estimated and the expected diversity curves. Simulations were set up with

Snakemake 5.2.4 and R 3.6.3 using the R packages ape 5.5 (Paradis et al. 2019), phytools 0.7-80

(Revell 2012), TESS 2.1.0 (Höhna et al. 2016), phangorn 2.7.0 (Schliep 2011), and RPANDA 2.0

(Morlon et al. 2016, see Appendix S2 for more details).

Figure 2. Simulation pipeline. A) to D) Diversification rates through time for the models used to simulate the backbone (grey). E) Diversification model used for the subclade (orange). F) Example of a simulated phylogeny with a rate shift shown in orange (the backbone is simulated with the Model 1).

2.4 | Applications to empirical phylogenies

We tested the automated pipeline on four clades representing a large diversity of taxa to illustrate the potential of the approach. First, we applied the approach to the original example of Morlon et al. (2011), the cetacean phylogeny published by Steeman et al. (2009). To compare with previous results, we used the same taxonomy as in Morlon et al. (2011) with a global sampling fraction of 98% (87/89 species). We looked for diversification shifts for the four main families (Balaenopteridae, Delphinidae, Phocoenidae and Ziphiidae) and for the two parvorders (Odontoceti and Mysticeti). We tested shifts at the crown age (backbone.option="crown.shift") of subclades but also at the stem age (backbone.option="stem.shift" see Appendix S1) as in Morlon et al. (2011) to compare both approaches.

Second, we tested a group without expected diversity decline, and studied the phylogeny of Vangidae (Jønsson et al. 2012), which is a small but fully sampled group (32/32 species). In their study, the authors detected two diversification shifts and concluded that this group has experienced adaptive radiation involving changes in beak size and body mass. We thus tested these hypotheses.

Third, we applied the approach to Parnassiinae, a subfamily of swallowtail butterflies (Condamine et al. 2018) with a good sampling fraction (96.6%, 85/88 species). Shifts of diversification can also come from ecological changes such as colonisation of new environments (Yoder et al. 2010) or host-plant shifts (Ehrlich and Raven 1964). We tested hypotheses related to host-plant shifts, Himalayan mountain colonisations, and taxonomic groups.

Finally, we investigated the diversification history of Cycadales (Nagalingum et al. 2011). The sampling fraction of this group is equal to 72.5% (231/327 species, IUCN 2021). This group originated 275 Myr ago and almost all extant species emerge from recent radiations during the

Miocene (Condamine et al. 2015). We tested shifts for all genera with more than five species

described except *Dioon*, which is the poorest sampled (8/13 species). To account for uncertainty in

divergence time estimates, we applied the approach to posterior trees and calculated the

corresponding range of the palaeodiversity dynamics with the deterministic approach. This allows

measuring variation of palaeodiversity estimates on a large panel of posterior trees and therefore

accounting for uncertainties on divergence time estimates. We also calculated the palaeodiversity

dynamics with the probabilistic approach to account for uncertainty of diversity estimates (Billaud

et al. 2020).

For all empirical cases, we did not use the BVAR_DVAR model because it often produced

unrealistic estimates and has already been discussed as problematic (Burin et al. 2019).

297   3 | Results

298   3.1 | Simulations

The simulation plan has been set up to test both shift detections and palaeodiversity dynamic

estimates. The analyses of the simulations initially revealed high proportions of false positives

(>11%, **Figure 3**, light orange). These false positives led us to look at what they would be without

the model selection procedure, *i.e.* if we fitted only the true (simulated) models rather than selecting

the best model from the set of models applied to subclades, backbones and the whole phylogeny. By

doing this, proportions of false positives dropped below 10% (**Figure 3**, light blue). This finding

sheds light on two problems: (1) the model selection, and (2) even with the simulated models,

proportions of false positives are higher than 5%. This latter problem shows that when an

homogeneous model is simulated, splitting the optimisation of this model into a subclade and a

backbone provides a gain of likelihood at the subclade level that is not penalised enough to avoid

selecting a shift. This can be solved by adding a parameter for the shift location in the AICc

calculation as in previous methods such as MEDUSA (Alfaro et al. 2009). With this additional

parameter and when fitting the models that were simulated, proportions of false positives decreased

below 5% (**Figure 3**, dark blue). If we use this additional parameter but used models that were

selected rather than those that were simulated, proportions of false positives are equal to 3.3% for

BCST, 2.4% for BVAR, 13.8% for BVAR_DCST, and 22.7% for BCST_BVAR (**Figure 3**, dark

orange). These results are convenient for simpler models (BCST and BVAR) but false positives are

still important for more complex models. Accordingly, we warrant careful interpretation of results

and to cross-validate with other methods when possible.

Figure 3. Proportions of false positives by models used to simulate the backbone depending on
the method. Values for best-fitting models (in shades of orange) include the step of model selection
for each part (subclade and backbone) while values for simulated models (in shades of blue) are
calculated using the simulated models (no model selection). "Old version" corresponds to the AICc
calculation from Morlon et al. (2011) and "+1 parameter" corresponds to the addition of one
parameter for the location of the shift**.**
324

Concerning palaeodiversity dynamics, the main tendency (decline or not) is well recovered

(BCST=97.35%, BVAR=84.6%, BVAR_DCST=89.5%, BCST_DVAR=92.65%). More precisely,

we compared palaeodiversity curves from simulated rate values with palaeodiversity curves from

estimated rate values. We found rather low global median errors *D* for simpler models with 0.146

for the BCST model and 0.176 for the BVAR model (**Figure 4**). More complex models have

slightly higher median values of *D* with 0.295 for the BVAR_DCST model and 0.315 for the

BCST_DVAR model (**Figure 4**). The mean of median values of the different models is equal to

0.233. First and third quartiles follow the same variations across models than the median with

higher values of *D* for more complex models.

Figure 4. Comparison of inferred versus simulated palaeodiversity dynamics for the three
quartiles of global error *D* by model. Purple: inferred palaeodiversity. Green: simulated
palaeodiversity. Note that the inferred palaeodiversity with the BVAR model (median) corresponds
to a false positive with a BVAR DCST model for the backbone creating this decline.

3.2 | Empirical evidence of extinction from phylogenies

3.2.1 | Cetacea

As in Morlon et al. (2011), we tested the presence of shifts in diversification at the base of

the four main and recently diverged families (Balaenopteridae, Delphinidae, Phocoenidae and

Ziphiidae) and the two parvorders (Mysteceti and Odotonceti) of Cetacea. This selection of

subclades creates 25 combinations of shifts with a single backbone and 47 combinations of shifts if

we add combinations with multiple backbones. When testing the shifts at the crown of subclades,

we detected a single best combination with shifts for the four families tested (Table S1,

ΔAICc=8.50). All the subclades follow a model with a decreasing speciation rate through time (see

Appendix S3 for details). The simple backbone of this combination follows a model of

diversification with a constant speciation rate and an increasing extinction rate leading to a phase of

decline starting at 10 Ma before present, with a peak of palaeodiversity at 596 species (**Figure 5**).

The same analysis with shifts tested at stem ages provides a best combination with a lower global

AICc (Appendix S1, Table S5).

Figure 5. Diversification shifts and palaeodiversity dynamics estimated for Cetacea with shifts tested at crown ages. A) The phylogeny of Cetacea with shifts highlighted in colours and best models in parenthesis. Red dots correspond to all tested nodes. B) The evolution of diversification rates through time. C) The palaeodiversity dynamic estimated with the probabilistic approach. Dotted line represents the confidence interval of diversity estimates for the backbone at 95% calculated with the probabilistic approach. For the sake of clarity, confidence intervals of diversity estimates for subclades are not represented.

3.2.2 | Vangidae

We tested shifts at three nodes in the Vangidae phylogeny corresponding to the Malagasy Vangidae clade and two nodes where shifts of morphological evolution have been detected in a previous study (Jønsson et al. 2012). Because these nodes are nested and there are only 32 species, only five

combinations result from this initial selection of subclades. We did not detect any shift of

diversification, and a model for the phylogeny without shift remains better (Table S2, ΔAICc=3.38)

than other combinations. The whole phylogeny follows a model with a decreasing speciation rate

resulting in a palaeodiversity increase through time, which slows down to present and reaches the

current diversity of 32 species (**Figure 6**).

Figure 6. Diversification shifts and palaeodiversity dynamics estimated for Vangidae with
stems included in backbone analysis. A) The phylogeny of Vangidae without shift detected
(crown shifts). B) The evolution of diversification rates through time. C) The palaeodiversity
dynamic estimated with the probabilistic approach. Dotted line represents the confidence interval of
diversity estimates for the backbone at 95% calculated with the probabilistic approach. For the sake
of clarity, confidence intervals of diversity estimates for subclades are not represented.

3.2.3 | Parnassiinae

We tested 11 shifts corresponding to tribes (Luehdorfiini, Parnassiini, Zerynthiini), genera (*Allancastria, Parnassius*), subgenera (*Driopa, Tadumia, Kailasius, Koralius, Parnassius*), of which some match with host-plant shifts (genus *Parnassius*) or colonisation of Himalayan mountains (*Kailasius, Koramius*). This selection creates 392 combinations to compare with a single backbone and 1079 by adding combinations with multiple backbones. First results showed unrealistically high rates of diversification leading to unlikely palaeodiversity curves highlighting limits from some models (see Appendix S3 for details). We then repeated the analysis by constraining the rate to a maximum value of 10 and found one best combination among the 1079 combinations (Table S3, ΔAICc=3.50). Among the tested shifts, seven shifts compose the best combination with tribes (Luehdorfiini, Zerynthiini) and subgenera (*Driopa, Tadumia, Koramius, Kailasius* and *Parnassius,* **Figure 7**). The tribes Luehdorfiini, Zerynthiini and both subgenera *Parnassius* and *Tadumia* follow a model with a constant speciation rate while subgenera *Driopa, Kaliasius* and *Koramius* follow a model with a decreasing speciation rate through time. The backbone follows a model with a decreasing speciation rate through time and a constant extinction rate (**Figure 7b**), leading to a period of negative net diversification rate from the beginning of the Miocene (22 Myrs ago) from the peak of the palaeodiversity of 748 species to the diversity of 88 extant species. This creates a palaeodiversity decline at the beginning of the Miocene. All combinations with multiple backbones yield a lower global AICc than the best combination with a single backbone.

Figure 7. Diversification shifts and palaeodiversity dynamics estimated for Parnassiinae with stems included in backbone analysis. A) The phylogeny of Vangidae with shifts highlighted (crown shifts) in colours and best models in parenthesis. B) Red dots correspond to all tested nodes. The evolution of diversification rates through time. C) The palaeodiversity dynamic estimated with the probabilistic approach. Dotted line represents the confidence interval of diversity estimates for the backbone at 95% calculated with the probabilistic approach. For the sake of clarity, confidence intervals of diversity estimates for subclades are not represented.

3.2.4 | Cycadales

We tested five shifts with the genera *Cycas*, *Ceratozamia*, *Zamia*, *Macrozamia*, and *Encephalartos*.

This selection creates 32 combinations with a simple backbone and none with multiple backbones.

The best combination is composed of all the tested subclades (Table S4, ΔAICc=11.96). The genera

Cycas, *Ceratozamia* and *Macrozamia* follow pure-birth models with a constant speciation rate,

while *Zamia* and *Encephalartos* follow models with a decreasing speciation rate (**Figure 8a,**

Appendix S3). The diversification model of the backbone has a constant speciation rate and an

increasing extinction rate, creating a negative net diversification rate starting 130 Myrs ago during

the Early Cretaceous (**Figure 8b**). The global palaeodiversity increased again and reached the

extant diversity thanks to the radiations of extant genera during the Miocene. The peak of

palaeodiversity calculated with the deterministic approach reaches 200 species and ranges on

posterior trees from 500 to 100 species (**Figure 8c**). The probabilistic approach estimates 150

species at the palaeodiversity with a confidence interval ranging from 400 to 0 species (**Figure 8d**).

Figure 8. Diversification shifts and palaeodiversity dynamics estimated for Cycadales with stems included in backbone analysis. A) The phylogeny of cycads with shifts highlighted (crown shifts) in colours and best models in parenthesis. Red dots correspond to all tested nodes. B) The evolution of diversification rates through time. C) The palaeodiversity estimated with the deterministic approach. The red area represents the range of palaeodiversity estimates calculated on posterior trees. D) The palaeodiversity dynamic estimated with the probabilistic approach. Dotted line represents the confidence interval of diversity estimates for the backbone at 95% calculated with the probabilistic approach. For the sake of clarity, confidence intervals of diversity estimates for subclades and species names are not represented.

4 | Discussion

In this study, we automated in RPANDA, tested with simulations and illustrated with empirical cases the approach developed by Morlon et al. (2011) that allows detecting shifts of diversification and estimating palaeodiversity dynamics through time from dated phylogenies.

Several options and functions have been added to make this approach largely accessible to address

an array of questions about heterogeneity of diversification rates and palaeodiversity dynamics by

consolidating the challenging field of macroevolution in adopting hypothesis-driven approaches

(Morlon et al. 2022). This emphasises the importance of additional information from biological

knowledge on the focal groups to compare scenarios motivated by biological hypotheses (*e.g.*

Legendre et Condamine 2018). In this sense, integrative taxonomic work is fundamental as it

summarises broad morphological, ecological and geographical divergences without neglecting

historical divergence of clades thanks to phylogenetic analyses. Beyond taxonomy, ecological data

or other analyses such as ancestral state estimations can ground hypotheses for selecting subclades

if the sampling fraction is known.

From a biological point of view, phylogenies are more complex objects than what birth-

death models estimate. For instance, speciation might not be instantaneous (Etienne and Rosindell

2012). Accordingly, one should keep in mind that underlying assumptions of models influence the

results. Among time- and clade-heterogeneous approaches, the most popular model, BAMM,

investigates shifts along branches and does not allow periods of decline of diversity (Rabosky et al.

2013). The Multi-Type Birth-Death model developed by Barido-Sottani et al. (2020) provides a

Bayesian framework that investigates shifts thanks to type-specific birth and death rate without

defining location of the type changes. ClaDS models rate heterogeneity with small but frequent

shifts (Maliet & Morlon 2022). These alternative approaches can be used in a complementary way

to study heterogeneity of diversification but will not necessarily provide similar results because of

their underlying assumptions on diversification rates. In our case, rates of birth-death models are

either constant or exponentially variable over time and shifts occur at specific branch points. The

main advantage of our approach is to provide inference of palaeodiversity dynamics by better

estimating deep periods of palaeodiversity decline (see also Maliet and Morlon 2022).

Previous studies on Vangidae (Jønsson et al. 2012), on Cetacea (Rabosky 2014), on

Parnassiinae (Condamine et al. 2018), and on Cycadales (Condamine et al. 2015) have investigated

heterogeneity of diversification with other methods. The cladogenesis test used for the Vangidae

found one significant and one marginal shift among the nodes we tested. Contrary to the

cladogenesis test, our method implies birth-death models. Finding no shift can then come from the

small size of the phylogeny but might also highlight that our approach is more conservative in

detecting shifts in small phylogenies. Interestingly, BAMM analyses on the three other empirical

cases estimated less diversification shifts (one in Cetacea vs. four here, one in Parnassiinae vs.

seven here, and four in Cycadales vs. five here), suggesting that BAMM might be more

conservative in rate shift detection. Moreover, BAMM did not detect palaeodiversity decline

contrary to our inferences. For instance in Parnassiinae, we found a decline starting at 22 Ma from a

peak at 748 species to the current diversity of the backbone (8 species). This is consistent with

Condamine et al. (2018) who applied models assuming instantaneous drops of diversity through

time at specific time points (Stadler 2011a; May et al. 2016). This study found a sudden extinction

around 15 Ma, 7 Myrs later, with a loss of 89% of the diversity (from 90 species to 10). Both

methods recover a decline of diversity, although different assumptions behind each model (mass

extinction vs. exponential dependency to time) influence the inferred timing and the scale of the

decline.

The approach we automated has already been recognized for its ability to better estimate

extinction rate (Stadler 2011b). Our simulations confirm the capacity of the model to recover non-

zero extinction rate in the backbone that can exceed speciation rate, resulting in a diversity decline.

Despite the high values of false positive errors for complex models, the difference between

observed and simulated palaeodiversity was not consequent with a mean of median global error

D=0.233 on average over models and close to the value found in Billaud et al. (2020) with a

D=0.22. This result shows that even with an error on the detection of shift, the model estimates a

trustworthy palaeodiversity dynamic (**Figure 4**). Moreover, our empirical analyses suggest diversity

declines are more widespread than previously considered. Cetacea, Parnassiinae, and Cycadales

show a common pattern with a single period of decline but we can address the question to what

extent patterns with many diversity declines might be detected. Indeed, the main limit of our

approach is that important levels of extinction are likely to erode both diversity and statistical

power. Splitting a phylogeny into backbones and subclades requires enough species to be shared in

different parts that will be analysed separately. Dated phylogenies with only a few extant species

cannot be investigated by our approach although we sometimes know from the fossil record that

they experienced extinction. The clade of Ginkgophyta is a caricatural example of this problem as it

only contains one lineage (*Ginkgo biloba*) besides 275 Ma of evolution, but certainly experienced a

lot of extinction events (Royer et al. 2003). An interesting perspective will be to simulate more

complex patterns of extinction with multiple backbones and multiple periods of decline to see

whether we can properly recover these patterns.

Given the difficulty to estimate extinction rates (Morlon 2014; Beaulieu and O'Meara 2015;

Rabosky 2016), studies have repeatedly raised debates about models in macroevolution (Kubo and

Iwasa 1995; Rabosky and Lovette 2008; Crisp and Cook 2009; Burin et al. 2019; Pannetier et al.

2021). Recently, Louca and Pennell (2020) argues that diversification rates should not be estimated

from birth-death models with clade-homogeneous rates because any reconstructed phylogeny can

be explained with an infinite number of alternative models. Although their limitations do not

directly apply to clade-heterogeneous diversification models such as the approach of Morlon et al.

(2011), the Louca and Pennell's study had the advantage of highlighting the importance of

hypothesis-testing (Helmstetter et al. 2021, Morlon et al. 2022) to limit confounding effects.

Methodological developments and collecting more data are required to investigate questions in such

a challenging field while keeping in mind that rates inferred from extant timetrees are tentative

estimates of a long past history and should be interpreted cautiously (Helmstetter et al. 2021).

In conclusion, the automated implementation of the approach originally developed by

Morlon et al. (2011) provides a user-friendly tool to investigate heterogeneity of diversification. We

improved this approach by (1) adding the possibility to test shifts at crown age that seems to

drastically improve the global likelihood of the approach (see Cetacea for example), (2) select a set

of constant or time-dependent diversification models, (3) easily set up multiple backbone

investigation, (4) make it possible to constrain rate estimates, and (5) infer palaeodiversity

dynamics while taking into account uncertainty both within rate estimation (probabilistic approach)

and across many trees that can differ in terms of topology or divergence times. Nonetheless, we

encourage users to adopt an hypothesis-driven approach and to be parsimonious concerning the

number of nodes to test. We also recommend being critical on results of inferred palaeodiversity of

the backbone in terms of raw number of species that results from rate values. We also caution that

the most complex model where both speciation and extinction rates vary exponentially is prone to

provide highly unrealistic patterns of palaeodiversity dynamics and should be avoided or

constrained echoing results from Burin et al. (2019). Keeping in mind these limitations, our study

highlights that signals of extinction and palaeodiversity declines can be investigated in groups

without species-level fossil records.

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Conflict of interest

None declared.

Authors' contributions

N.M. and F.L.C. designed the research with advice from P.-H.F.; N.M. performed the research and

analysed the data with advice from H.M. and F.L.C.; and N.M. wrote the paper and all authors

edited the text.

Data availability statement

This open source software is written entirely in the R language and is freely available through the

Comprehensive R Archive Network (CRAN) at:

https://cran.r-project.org/web/packages/RPANDA/index.html. The scripts used, simulation results,

model fits and case study data are available at: https://figshare.com/s/6e8924774165b5ed81ec

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