Front Matter

Full Title:
Asymmetric Signaling Across the Hierarchy of Cytoarchitecture within the Human Connectome

Short Title:
Asymmetric signaling over the cortical hierarchy

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Abstract

Cortical variations in cytoarchitecture form a sensory-fugal axis that shapes regional profiles of extrinsic connectivity and is thought to guide signal propagation and integration across the cortical hierarchy. While neuroimaging work has shown that this axis constrains local properties of the human connectome, it remains unclear whether it also shapes the asymmetric signaling that arises from higher-order topology. Here, we used network control theory to examine the amount of energy required to propagate dynamics across the sensory-fugal axis. Our results revealed an asymmetry in this energy indicating that bottom-up transitions were easier to complete compared to top-down. Supporting analyses demonstrated that asymmetries were underpinned by a connectome topology that is wired to support efficient bottom-up signaling. Finally, we found that asymmetries correlated with differences in communicability and intrinsic neuronal timescales, and lessened throughout youth. Our results show that cortical variation in cytoarchitecture may guide the formation of macroscopic connectome topology.

Teaser

We link microstructure to the connectome and show that activity propagates more efficiently up the cortical hierarchy than down.
MAIN TEXT

Introduction
Multiple lines of evidence suggest that the brain’s extrinsic structural connectivity is predicted from its cytoarchitecture\(^1\)-\(^4\). This structural model suggests that the degree to which two regions share similar cytoarchitectural features predicts the distribution of their laminar projections. Critically, inter-regional similarity in cytoarchitecture varies gradually across the cortex, creating a sensory-fugal (S-F) axis\(^5\),\(^6\) that predicts regions’ profiles of extrinsic connectivity to the rest of the brain. This gradient positions contiguous visual and sensorimotor cortex at one end and distributed heteromodal association and paralimbic cortices at the other, and is correlated with other macroscopic gradients of brain structure and function\(^7\)-\(^15\). Together, these multi-modal gradients form a hierarchy of brain organization that is thought to govern extrinsic connectivity\(^3\) and support the efficient propagation and integration of signals across the cortex\(^16\)-\(^18\). However, the extent to which cytoarchitecture’s governance over connectivity manifests in the topology of the macroscopic structural connectome remains a key open question. Here, we examine whether the S-F axis constrains signal propagation across macroscopic connectome topology.

Convergent evidence spanning the past three decades supports the premise that neuronal signaling is shaped and constrained by a globally ordered cortical hierarchy\(^16\),\(^17\),\(^19\),\(^20\). External stimuli arrive at functionally specialized sensory cortices before propagating up modality-specific hierarchies to then apex at association and paralimbic regions responsible for functional integration. This convergent bottom-up signal propagation is complemented by far-reaching modulatory top-down signals\(^21\)-\(^24\) that operate on longer timescales\(^25\) and that bind incoming sensory signals together to update predictive inferences about our environment and to complete goal-directed action\(^26\),\(^27\). Critically, these cooperative patterns of bottom-up and top-down signaling, and the asymmetries between them\(^25\), may be underpinned by graded variations in cortical cytoarchitecture\(^2\),\(^3\),\(^28\). Specifically, regions’ cytoarchitecture robustly predicts their extrinsic connectivity profiles\(^1\), including the strength\(^29\), distance\(^29\), and layer origination and termination\(^29\),\(^30\) of feedforward and feedback projections\(^23\). Further, inter-regional similarity in cytoarchitecture follows a clear S-F axis\(^5\),\(^6\), suggesting that where a region is situated along the cortical hierarchy characterizes its bottom-up and top-down connectivity with the rest of the brain, and thus explains its capacity to support signal propagation across the hierarchy. Consistent with this notion, regional variation in the depth-wise T1w/T2w ratio—an in vivo neuroimaging measurement that correlates with the S-F axis of cytoarchitecture\(^5\),\(^31\)—couples with regions’ intrinsic timescales of neuronal activity\(^10\), demonstrating that cytoarchitecture tracks the progressive lengthening of neuronal oscillations associated with hierarchical information integration\(^25\). Additionally, the S-F axis also correlates with regional weighted degree from diffusion-weighted structural networks\(^32\), demonstrating that cytoarchitecture tracks local properties of macroscopic connectome topology.

Regional variations to cytoarchitecture are, in part, rooted in neurodevelopment\(^1\)-\(^3\),\(^33\)-\(^37\). During prenatal development, differences in the developmental timing of neurogenesis leads to highly eulaminate regions—such as the primary visual cortex—developing more slowly than agranular regions\(^38\), suggesting that prenatal development lays the foundation for the S-F axis. Once laid, the S-F axis scaffolds the formation of extrinsic feedforward and feedback connections that traverse up and down the hierarchy\(^3\). This connectivity formation also appears to track the S-F axis in a developmentally-staged manner, with synaptogenesis peaking earlier in lower-order primary visual areas than in higher-order frontal cortex\(^39\)-\(^41\). Furthermore, neuroimaging research
shows that macroscopic proxies of the S-F axis (e.g., T1-weighted features), as well as structural connectivity, continue to change throughout postnatal development\textsuperscript{15,42–48}, suggesting that the S-F axis continues to shape connectome topology.

As the above literature demonstrates, the processes that govern patterns of extrinsic connectivity across the cortex are encoded by regional variations in cytoarchitecture, and this regional variation provides a blueprint for the refinement of connectivity throughout development. However, the extent to which the topology of the structural connectome can be leveraged to model bottom-up and top-down signal propagation across the S-F axis remains unknown. The literature reviewed above leads us to four predictions. First, if differences in extrinsic projections encoded by cytoarchitecture are reflected in connectome topology\textsuperscript{32}, then we should be able to model asymmetries between bottom-up and top-down signal propagation across the S-F axis in humans \textit{in vivo}. Notably, recent work has shown that the topology of the undirected structural connectome generates spatially varied patterns of signal propagation\textsuperscript{49} and asymmetric signaling\textsuperscript{50}, suggesting that such asymmetry may be assessable using non-invasive neuroimaging. Second, if asymmetric signal propagation is produced specifically by the cytoarchitectonic hierarchy, then asymmetries may not generalize to different definitions of the cortical hierarchy that only partially correlate with the S-F axis, such as those derived from the T1w/T2w ratio\textsuperscript{31} and functional connectivity\textsuperscript{12}. Third, since signals propagating across the S-F axis will traverse through changing temporal receptive windows\textsuperscript{10}, we expect asymmetries to correlate with differences in intrinsic neuronal timescales. Fourth, if signal propagation continues to be refined throughout development, then asymmetries should vary systematically as a function of age in youth.

To evaluate evidence for the above reasoning, we turned to the minimum control energy framework from network control theory (NCT)\textsuperscript{51,52}. Using a linear model of dynamics, NCT estimates the amount of input energy—delivered to a set of control nodes (brain regions)—that is required to drive the brain to transition between pairs of activity states. In this context, we consider binary states in which one set of regions are active while the rest of the brain is inactive. Here, we sought to estimate the transition energy associated with trans-hierarchical state transitions. We found that bottom-up state transitions were more efficient (required less energy) compared to top-down transitions. We also observed that the hierarchical distance separating brain states correlated with the size of these energy asymmetries, suggesting that states with different underlying cytoarchitecture display the most pronounced asymmetries. In addition to these primary findings, we examined (i) whether our findings generalized to the T1w/T2w ratio\textsuperscript{31} and the principal gradient of functional connectivity\textsuperscript{12}; (ii) whether our transition energies correlated with between-state differences in intrinsic timescales; (iii) whether brain regions’ position along the S-F axis explained their role in facilitating state transitions; and (iv) whether energy asymmetries correlated with age in a developing sample of youths. Our work extends the field's understanding of connectome topology by showing that the neuroanatomical processes that give rise to extrinsic connectivity constrain the directional flow of macroscopic dynamics over the cortex.
Results

Mapping trans-hierarchical state transitions
We characterized the energy required to complete trans-hierarchical state transitions. Here, we set our brain states to actuate patches of cortex with relatively homogenous profiles of cytoarchitecture. Briefly, we defined the cortical hierarchy as the sensory-fugal (S-F) axis of cytoarchitectonic similarity (Fig. S1A) developed in previous work\textsuperscript{5,53} and disseminated as part of the BigBrainWarp toolbox\textsuperscript{6} (see Methods). We selected this S-F axis as it represents the current state-of-the-art proxy of continuously varying profiles of cytoarchitecture in the human brain. Next, we defined brain states by splitting the S-F axis into $k$ equally sized non-overlapping groups of regions that spanned the gradient (Fig. 1A; see Methods). Then, using a group-averaged structural connectome, $A$, taken from the Philadelphia Neurodevelopmental Cohort\textsuperscript{54} (see Methods; N=793 [458 females], mean age = 15.66±3.3 years), we modeled the transition energy between all $k$ pairs of brain states, generating a $k \times k$ matrix of energy values, $T_E$ (Fig. 1B, C). Critically, the hierarchically ordered nature of our brain states meant that bottom-up transition energies were naturally stored in the upper triangle of $T_E$ while top-down transition energies were stored in the lower triangle. We computed energy asymmetries by subtracting top-down energy from bottom-up energy (Fig. 1D; $T_{EA} = T_E - T_E^T$). In the upper triangle of $T_{EA}$, positive values indicate bottom-up energy being greater than top-down energy whereas negative values indicate bottom-up energy being lower than top-down energy.

\textbf{Fig. 1. Estimating trans-hierarchical signal propagation.} Using the Schaefer atlas, we sampled 20 non-overlapping groups of regions ($n=10$ per state) traversing up the S-F gradient of cytoarchitectonic similarity\textsuperscript{6}. These groups formed brain states spanning the cortical hierarchy. By definition, regions within each state had relatively similar profiles of cytoarchitecture. Accordingly, pairs of states separated by long hierarchical distances have different underlying cytoarchitecture. (A). An example pair of brain states $(x_i, x_j)$ at different locations along the S-F axis. (B). For a given pair of states $(x_i, x_j)$, we calculated the minimum control energy ($E$) required to complete the transition from $x_i$ to $x_j$ and from $x_j$ to $x_i$. (C), Minimum control energy between all pairs of states was assembled into a transition energy matrix, $T_E$. Owing to the ordered nature of our brain states, transition energies were trivially grouped into bottom-up (transitions moving up the hierarchy; $T_E$, upper triangle) and top-down (transitions moving down the hierarchy; $T_E$, lower triangle). (D), Given this grouping, we subtracted top-down energy from bottom-up energy to create an energy asymmetry matrix ($T_{EA}$). In the upper triangle of this asymmetry matrix, positive values represented state transitions where bottom-up energy was higher than top-down energy, whereas negative values represented the opposite. Note that, apart from the sign of the $\Delta$ value, $T_{EA}$ is symmetric; hence, all analyses of asymmetries focused on the upper triangle of this matrix.
We found that bottom-up energy was significantly lower than top-down energy (Fig. 2A, left; mean energy asymmetry=-0.60, bootstrapped 95% CI=[-0.62, -0.59]), demonstrating that state transitions moving up the cytoarchitectonic S-F axis required less energy (i.e., were easier to complete; see Methods) compared to those moving down the same axis (see Fig. S2 for first-order statistical features of the bootstrapped connectomes). Furthermore, in support of our hypothesis, we found that the hierarchical distance between brain states was negatively correlated with $T_{E\Delta}$ (Fig. 2B, left; Spearman’s $\rho$=-0.32, bootstrapped 95% CI=[-0.33, -0.31]). That is, as states’ cytoarchitecture became more dissimilar from one another (greater hierarchical distance), energy asymmetries became more negative. Thus, asymmetries between bottom-up and top-down transition energies were largest when brain states had differing cytoarchitecture, with bottom-up transitions becoming progressively easier to complete than top-down. These findings were highly robust to the choice of normalization constant, $c$, and time horizon, $T$, in our model (Fig. S3; see Methods). Additionally, we found convergent results when we (i) generated a new group-averaged connectome using only individuals who were at least 20 years old (N=69; mean energy asymmetry=-0.55; correlation with hierarchical distance, $\rho$=0.29); and (ii) ran new analyses on a single hemisphere, thereby excluding inter-hemispheric connections (mean energy asymmetry=-0.64; correlation with hierarchical distance, $\rho$=-0.30).

![Fig. 2.](https://example.com/fig2.jpg)

**Fig. 2.** The topology of the structural connectome is sensitive to asymmetries between top-down and bottom-up signal propagation across the sensory-fugal axis of cytoarchitecture. (A). Bottom-up energy was significantly lower than top-down energy (left), demonstrating that bottom-up state transitions were easier for our network control model to complete. 1,000 bootstrapped resamples of the group-averaged connectome (see Methods) revealed that the 95% confidence interval of this asymmetry did not overlap 0. Additionally, this mean asymmetry was...
larger than expected under a pair of null network models (right), including one that preserved the spatial embedding and the edge weight distribution of the network and another that preserved the spatial embedding and the strength distribution. (B). The distance along the cytoarchitectonic gradient separating initial and target states was negatively correlated with energy asymmetries, demonstrating that high cytoarchitectonic dissimilarity between states was linked to greater negative energy asymmetries (left). This finding shows that when cytoarchitecture differs between brain states, bottom-up transitions required lower energy to complete compared to their top-down counterparts. The same bootstrap test described above revealed that the 95% confidence interval of this correlation did not overlap 0. Additionally, this correlation with hierarchy distance was larger than expected under the same pair of null network models described above (right). Taken together, these observations suggest that trans-hierarchical transition energy may be supported by higher-order topology of the structural connectome.

Next, to examine whether the above energy asymmetries depended on topology, we recomputed $T_{E\Delta}$ under two null network models. Specifically, we randomly rewired the underlying group-averaged structural connectome 10,000 times using a spatially embedded permutation model that preserved either the edge distribution or the strength distribution of the network$^{55}$ (see Methods). Then, for every rewired connectome, we re-estimated $T_{E\Delta}$ as well as the correlation with hierarchical distance. We found that both the mean energy asymmetry (Fig. 2A, right) and the hierarchy distance correlation (Fig. 2B, right) were stronger than expected under both null distributions. These results demonstrate that energy asymmetries, as well as the negative correlation with hierarchical distance, were not explained by a combination of the network’s spatial embedding and edge (or strength) distribution. In turn, these effects may be explained by variations in cytoarchitectonic profiles.

Having demonstrated that energy asymmetries were not explained by lower-order topology of the human connectome, we next sought to characterize potential higher-order features that may explain these effects. To achieve this goal, we leveraged two metrics of inter-nodal communication that are sensitive to the asymmetric signaling embedded in connectome topology: diffusion efficiency ($de$) and search information ($si$)$^{50}$ (see Methods). The metric $de$ quantifies the efficiency of signal propagation from node $i$ to node $j$ under a diffusion model$^{56}$. The metric $si$ quantifies the probability that a random walker will arrive at node $j$ by following the shortest path from node $i$$^{57}$; lower $si$ indicates a higher probability of finding the shortest path. We subtracted $de_{ij}$ from $de_{ij}$, and $si_{ij}$ from $si_{ij}$, to create $de_{\Delta}$ and $si_{\Delta}$. Additionally, to provide deeper intuition, we developed a modified version of path transitivity ($pt$)$^{58}$ that was sensitive to asymmetry (see Methods). Given a shortest path between a pair of nodes, path transitivity measures the extent to which activity deviates from, but then returns to, the shortest path (Fig. 3A); high $pt$ indicates the presence of paths wherein detours return to the path, whereas low $pt$ indicates the presence of detours that do not return. The standard implementation of $pt$ is symmetric$^{58}$. To introduce asymmetry, we examined the cumulative $pt$ ($pt_c$; see Methods) of a given shortest path. Specifically, $pt_c$ was obtained by calculating $pt$ separately for successively longer segments of the shortest path in both directions (Fig. 3B). This approach created a pair of transitivity curves (Fig. 3C)—one for each direction—that both culminated in the same full-path $pt$ value (see Fig. S4 for plots of these curves for a subset of the longest paths in A). Subtracting these curves and summing the differences yielded a difference score, $pt_{c\Delta}$, that encoded the extent to which returning detours were encountered sooner or later when traveling one direction along the path compared to the other.
We quantified each of these asymmetric communicability metrics ($d_{\Delta}, s_{\Delta}, p_{\Delta}$) between all pair of nodes in $A$ and then averaged over the values that connected our brain states (see Fig. S5 for correlations between the S-F axis and node-averaged communicability metrics). We found that $T_{(F)}$ correlated negatively with $d_{\Delta}$ (Fig. 3D) and positively with $s_{\Delta}$ (Fig. 3E) and $p_{\Delta}$ (Fig. 3F). These results indicate that state transitions with lower bottom-up energy (relative to top-down) are also associated with (i) higher bottom-up diffusion efficiency; (ii) lower bottom-up search information; and (iii) lower bottom-up cumulative path transitivity. In turn, these results suggest bottom-up signaling is more efficient than top-down (higher bottom-up $d_{\Delta}$) in part because it is more likely to find the shortest paths (lower bottom-up $s_{\Delta}$). Additionally, returning detours are encountered sooner for top-down signaling (lower bottom-up $p_{\Delta}$ / higher top-down $p_{\Delta}$), which indicates that the early occurrence of these detours may inhibit top-down signaling.

Fig. 3. Asymmetries in transition energy are explained by asymmetries in communicability.
We examined how our energy asymmetries correlated with asymmetries in diffusion efficiency, search information, and path transitivity. While diffusion efficiency and search information represent asymmetric communicability metrics, path transitivity is symmetric. Thus, we defined a modified version of path transitivity that was sensitive to asymmetries in the human connectome. (A), Path transitivity measures the occurrence of returning detours (i.e., triangles) along a given shortest path. Path transitivity is typically estimated along the entire length of the shortest path and is symmetric. (B), We modified path transitivity by estimating it separately for each segment of the shortest path starting from nodes located at either end. (C), Doing so allowed us to estimate a pair of cumulative path transitivity curves: one for each direction along the shortest path. These curves allowed us to probe whether returning detours were encountered sooner in one direction or the other, which we quantified by subtracting the curves and summing the differences. (D), Energy
asymmetries correlated negatively with asymmetries in diffusion efficiency. Thus, lower bottom-up energy corresponds to higher bottom-up diffusion efficiency. (E) Energy asymmetries correlated positively with asymmetries in search information. Thus, lower bottom-up energy corresponds to lower bottom-up search information. (F) Energy asymmetries correlated positively with asymmetries in cumulative path transitivity. Thus, lower bottom-up energy corresponds to lower bottom-up path transitivity; in turn, returning detours are encountered sooner for top-down signaling.

Finally, to test whether our results were specific to the S-F axis of cytoarchitecture, we repeated all of the above analyses using the T1w/T2w ratio\(^{31}\) (Fig. 1B) as well as the principal gradient of functional connectivity\(^{12}\) (Fig. 1C) to define brain states. This is a relatively strong test of specificity as the gradient of cytoarchitecture was correlated with both the T1w/T2w ratio \((r=-0.68)\) and the gradient of functional connectivity \((r=0.56)\). Using the T1w/T2w ratio, we found that neither the mean energy asymmetry (Fig. S6A; \(-0.11, p_{edge}=0.699, p_{strength}=0.707\)) nor the correlation with hierarchical distance (Fig. S6B; \(\rho=0.14, p_{edge}=0.958, p_{strength}=0.934\)) were larger than expected under our null network models. Additionally, while energy asymmetries correlated significantly with diffusion efficiency asymmetry (Fig. S6C; \(r=0.31, p_{FDR}=4\times10^{-5}\)) and search information asymmetry (Fig. S6D; \(r=0.23, p_{FDR}=2\times10^{-3}\)), they no longer correlated significantly with our asymmetric measure of path transitivity (Fig. S6E; \(r=0.06, p_{FDR}=0.420\)). A similar pattern of results was found for the functional connectivity gradient. Neither the mean energy asymmetry (Fig. S7A; \(0.15, p_{edge}=0.943, p_{strength}=0.900\)) nor the correlation with hierarchical distance (Fig. S7B; \(\rho=0.11, p_{edge}=0.906, p_{strength}=0.844\)) were larger than expected under our null network models. Regarding the communicability metrics, energy asymmetries were significantly correlated with diffusion efficiency asymmetry (Fig. S7C; \(r=-0.58, p_{FDR}=3\times10^{-18}\)) and search information asymmetry (Fig. S7D; \(r=0.55, p_{FDR}=4\times10^{-16}\)), but not transitivity (Fig. S7E; \(r=0.09, p_{FDR}=0.215\))

These results indicate that asymmetries between bottom-up and top-down transition energies were stronger for the S-F axis of cytoarchitecture compared to both the T1w/T2w ratio and the principal gradient of functional connectivity. Specifically, only energy asymmetries for the S-F axis revealed a clear hierarchy distance effect as well as a correlation with cumulative path transitivity. This result may be explained by the fact that these axes diverge at their apexes\(^{5,59}\). For example, the top of the S-F axis comprises paralimbic regions while the top of the functional connectivity axis comprises transmodal cortex. Previous work has suggested that this (relative) untethering of functional connectivity from cytoarchiteconic constraints may support the functional diversity of the transmodal cortex\(^5\). This untethering is also consistent with evidence that macroscopic structural and functional connectivity are relatively uncoupled in transmodal cortex compared to unimodal cortex\(^{60,61}\). Thus, our findings converge on the idea that while cytoarchitecture and structural connectivity are tightly intertwined, functional connectivity dearts from both in a spatially patterned way. Additionally, our results indicate that even though the S-F axis and T1w/T2w ratio are correlated, they show marked differences that may be critical to capturing how brain structure constrains connectivity.

The gradient of cytoarchitecture constrains the flow of activity over the cortex

The above findings demonstrate that the energy asymmetries associated with trans-hierarchical state transitions may result from a topology wired to propagate activity up the cytoarchitectonic gradient more efficiently compared to down. To illustrate this phenomenon intuitively, we examined whether the flow of uncontrolled activity followed the S-F axis as it spread throughout
the cortex over time (see Methods). Briefly, seeding from each brain state, we examined the spread of natural dynamics across the whole brain as they unfolded over time. This amounted to re-simulating our dynamical model for each initial state in the absence of both a target state and a control set. Below, we used this approach to show that the activity in our diffusive model preferentially propagates up the S-F axis.

For each seed brain state and time point, $t$, we calculated the Spearman’s rank correlation between the pattern of simulated activity at each node and the S-F axis (Fig. 4A). Note that this correlation was computed excluding the regions that made up a given seed state (i.e., where activity was propagating from). Thus, correlations were not driven by activity leaving a given brain state. For a given time step, negative correlations indicated that brain activity was higher at the bottom of the hierarchy than at the top, while positive correlations indicated the opposite. Fig. 4B shows that states lower on the hierarchy tend to show negative correlations between the S-F axis and early activity propagation (Fig. 4B, blue arrow), while states higher on the hierarchy tend to show positive correlations (Fig. 4B, peach arrow). This pattern demonstrates that early signal propagation tends to activate regions near to a state’s location on the hierarchy. That is, activity propagating from low positions on the hierarchy reaches other low-hierarchy regions first, driving a negative correlation, while activity propagating from high on the hierarchy reaches other high-hierarchy regions first, driving a positive correlation. Critically, Fig. 4B also shows that the negative correlations low on the hierarchy diminish (i.e., become less negative) more quickly compared to the positive correlations for the high-hierarchy states. This effect is quantified and recapitulated in Fig. 4C, which shows the differences in correlations between neighboring time points ($\rho^{t+1} - \rho^t$). We found that differences in correlations between timepoints were greater when activity was seeded from the bottom of the hierarchy (Fig. 4C, blue arrow) compared to the top (Fig. 4C, peach arrow). These results suggest that activity propagates more readily in the bottom-up direction than in the top-down direction. Furthermore, these results are consistent with our observation of lower bottom-up energy compared to top-down (see Fig. 2); a topology that is organized to facilitate bottom-up activity flow will require less energy to complete controlled bottom-up state transitions compared to top-down.
**Energy asymmetries in trans-hierarchical state transitions are correlated with differences in intrinsic timescales and asymmetries in effective connectivity**

Our observations thus far are consistent with the notion that regional cytoarchitectonic similarity influences the difference between bottom-up and top-down signal propagation across the cortical hierarchy. Specifically, our results suggest that how patterns of brain activity spread across the hierarchy varies as a function of the direction of flow. However, the results presented thus far were only derived from linear dynamics simulated upon the structural connectome. We reasoned that if our results for simulated dynamics were neurobiologically meaningful, then we would observe two findings.
First, we expected that energy asymmetries would correlate with changes in the intrinsic neuronal timescales of our brain states. Specifically, we predicted that transitions where bottom-up energy was lower than top-down would correspond to a lengthening of neuronal timescales between the initial and target states. In turn, this finding would suggest that the topology of the structural connectome is wired to support the integration of information that is thought to be occurring as activity traverses up the hierarchy. Second, we expected that energy asymmetries would be consistent with asymmetries derived from dynamical models trained on functional neuroimaging data. To test the former prediction, we used open-access human electrocorticography (ECoG) data\textsuperscript{62,63} to index regions’ intrinsic timescales. Specifically, following Gao et al.\textsuperscript{10}, we quantified timescales using the time constant, $\tau$, of an exponential decay function fitted to the autocorrelation function of the ECoG timeseries (Fig. 5A; see Methods). Larger $\tau$ values correspond to longer (slower) fluctuations in a region’s intrinsic timescales.

Subsequently, we averaged $\tau$ within each of our brain states and then subtracted mean $\tau$ between pairs of brain states, $\tau_\Delta$. Thus, positive $\tau_\Delta$ represented larger $\tau$ in state $j$ compared to state $i$. Finally, we correlated $T_{E\Delta}$ with $\tau_\Delta$ and found that they were negatively correlated (Fig. 5B). This result indicates that state transitions where bottom-up energy is lower than top-down (i.e., negative $T_{E\Delta}$) are also characterized by a slowing of intrinsic timescales going from state $i$ to state $j$ and vice versa. Thus, state transitions that are (relatively) easy to complete are coincident with a lengthening of the timescales of resting-state electrophysiological fluctuations.

**Fig. 5. Energy asymmetries correlate with differences between brain states’ intrinsic neuronal timescales.** (A), We used resting-state electrocorticography data to examine differences between brain states’ intrinsic neuronal timescales (as per methods described in Gao et al.\textsuperscript{10}) between our cytoarchitectonic brain states. (B), Energy asymmetries between brain states were negatively correlated with differences between brain states’ intrinsic timescales. This result shows that state transitions where bottom-up energy is lower than top-down (negative energy asymmetry) are also characterized by a slowing of intrinsic timescales going from state $i$ to state $j$ and vice versa.

Next, we turned from an evaluation of differences between brain states’ intrinsic neuronal timescales to an evaluation of asymmetries derived from effective connectivity. Specifically, we computed the effective connectivity (EC) between brain states using a spectral version of dynamic causal modeling\textsuperscript{64,65} applied to participants’ resting-state functional magnetic resonance imaging (rs-fMRI) data (see Methods). We subsequently computed EC asymmetries by subtracting top-down EC from bottom-up EC ($EC_\Delta = |EC| - |EC|^\top$). We found that $T_{E\Delta}$ was positively correlated with $EC_\Delta$ (Fig. S8; $r=0.24, p=1\times10^{-3}$), indicating that for state transitions where bottom-up energy
was lower than top-down the same was true for EC and *vice versa*. This result extends prior work\(^{50}\) by demonstrating that the topology of the undirected structural connectome supports directed signal propagation along the cortical gradient of cytoarchitectonic similarity.

**Optimized control weights track the sensory-fugal axis of cytoarchitecture and increase energy asymmetries**

The preceding sections demonstrated that brain network topology may be wired to facilitate more efficient bottom-up trans-hierarchical state transitions compared to top-down, and that this effect (i) is not better explained by spatial embedding or lower-order topology, (ii) may be specific to cytoarchitecture, and (iii) is consistent with asymmetries in intrinsic timescales and effective connectivity. These findings were also supported by results from inter-nodal communicability metrics, suggesting that how patterns of brain activity spread across the hierarchy varies as a function of the direction of flow. However, while convergence with communicability provides deeper insight into our results, a relative strength of NCT lies in its capacity to not only simulate dynamics, but to control them as well. In this section, we sought to leverage this strength by studying whether regions’ position along the S-F axis informed their capacity to facilitate trans-hierarchical state transitions.

To achieve the above goal, we optimized state transitions by introducing a variable set of control weights using a data-driven approach (see Methods). Briefly, for each state transition, we systematically perturbed the system to generate a set of control weights that minimized transition energy (Fig. 6A). Rather than assuming all regions have equal influence over dynamics, these weights tune the control assigned to different brain regions with the goal of reducing transition energy (i.e., improving the efficiency of state transitions). For each state transition, we examined the correlation between these optimized control weights and the hierarchical distance separating nodes from the associated initial/target state (see Methods). We assigned \( p \)-values using BrainSMASH\(^{66}\) and corrected for multiple comparisons via the Benjamini and Hochberg false discovery rate (FDR, \( q = 0.05 \)) procedure\(^{67}\). Here, any observed correlation implies that optimizing control weights uncovers a spatial mode of control variation that tracks the gradient of cytoarchitecture. Finally, we examined how optimized control weights influenced energy asymmetries. Here, we computed absolute mean \( T_{EA} \) for both uniform and optimized control weights using 1,000 bootstrapped resamples of the group-averaged connectome (see Methods).

We found that optimized weights correlated negatively with nodes’ hierarchical distance from the initial/target states (Fig. 6B). This result shows that optimized control weights reduce as nodes traverse along the S-F axis away from the initial/target states. Thus, optimized weights track the gradient of cytoarchitecture, and this tracking exceeds that which would be expected based on the spatial autocorrelation embedded in the data. Next, we found that mean energy asymmetry \( (T_{EA}) \) was significantly larger for optimized control weights compared to uniform control weights (Fig. 6C). Note, optimized weights were only designed to minimize transition energy, including both bottom-up and top-down energies. Thus, this observed increase in mean energy asymmetry suggests that our data-driven optimized control weights minimized bottom-up energy to a greater extent than top-down. Together, these results illustrate that a region’s position along the S-F axis explains its role in facilitating trans-hierarchical state transitions, and that imbuing our model with knowledge of these roles optimizes the efficiency of bottom-up signal propagation across the hierarchy.
Fig. 6. Optimized control weights track the cortical gradient of cytoarchitecture and maximize energy asymmetries. (A), For each trans-hierarchical state transition, we adopted the following procedure to generate optimized control weights that minimized transition energy. First, for a given state transition, we calculated uniformly weighted transition energy; nodes of the system were provided the same degree of control over system dynamics. Note, results for uniformly weighted transition energy have been reported in all figures prior to this one. Second, we re-estimated the transition energy n times, each time providing one node with additional control over the system. This approach generated a vector of perturbed transition energies (purple vector). Third, we subtracted the uniformly weighted energy from each of the perturbed energies to generate a vector of perturbed energy deltas (blue vector), the magnitude of which encoded regions’ importance to the state transition. Fourth, we re-estimated transition energy one more time using the perturbed energy deltas as optimized control weights. (B), Correlations between optimized control weights for each state transition and the S-F axis. For each state transition, we estimated the Spearman rank correlation between nodes’ optimized weights and their distance along the S-F axis from the initial and target state, and retained whichever correlation was strongest (see Methods). BrainSMASH p-values were corrected for multiple comparisons using the Benjamini-Hochberg False Discovery Rate. Significance was determined as \( p_{FDR} < 0.05 \). We found that optimized weights correlated negatively with hierarchical distance, indicating that they decayed as a function of distance from the initial/target state. (C), Mean energy asymmetries (\(|T_{EA}|\)) for uniform (light gray) compared to optimized (dark gray) control weights under 1,000 bootstraps (see Methods). Mean \(|T_{EA}|\) was larger for optimized control weights compared to uniform control weights. Thus, optimizing control weights maximized energy asymmetries.
Asymmetries in trans-hierarchical state transitions are refined throughout development

Having illustrated that a region’s position along the S-F axis explains its role in facilitating state transitions, in this final section, we sought to characterize the developmental trajectories of transition energies. Based on previous literature, we expected that ongoing developmental refinement of structural connectivity would result in age-related changes to bottom-up and top-down energy. To test this expectation, we estimated the correlation between participant-specific transition energies and age, while controlling for sex, total brain volume, edge density, and in-scanner motion (Fig. 7A). Here, energy was estimated using participant-specific optimized weights (see Methods and previous section). Next, for each participant, we averaged transition energies over bottom-up and top-down transitions separately and subtracted the mean values to get participant-specific energy asymmetries. We found that age correlated positively with these energy asymmetries (Fig. 7B). This effect was driven by the fact that the correlation between age and top-down energy (Fig. S9A; $r=-0.24$, $p_{FDR}=7\times10^{-12}$) was stronger than that observed for bottom-up energy (Fig. S9B; $r=-0.09$, $p_{FDR}=1\times10^{-2}$). Thus, while top-down and bottom-up energy both decreased throughout development, top-down energy did so more quickly. In turn, energy asymmetries weakened as a function of age. These results suggest that neurodevelopmental refinement of the connectome may involve converging toward a balance between bottom-up and top-down signal propagation. We also found that the age effects for individual transitions (from Fig. 7A) were negatively correlated with the energy asymmetries taken from the group-average connectome (Fig. 7C). This result demonstrates that state transitions with stronger energy asymmetries in the group-averaged connectome also showed the strongest age effects. Lastly, using a cross-validated penalized regression model (Fig. 7D; see Methods), we found that energy asymmetries were able to robustly predict participants’ age in out-of-sample testing (Fig. 7E; see also Fig. S10 which shows that optimized energies better predicted participants’ age compared to non-optimized energies derived from uniform control weights). Consistent with our expectations, these results show that development plays a critical role in refining trans-hierarchical transition energies, and that this refinement is concentrated in state transitions with divergent cytoarchitecture.
Fig. 7. Energy asymmetries in trans-hierarchical state transitions vary systematically over development. We estimated correlations between age and trans-hierarchical transition energy in 793 individuals, while controlling for sex, total brain volume, edge density, and in-scanner motion. (A), Correlations between age and transition energy for all state transitions. We observed widespread negative correlations between age and transition energy, suggesting that state transitions became easier to complete as individuals got older. (B), Correlation between age and participant-specific energy asymmetries averaged over bottom-up and top-down state transitions. We found a positive correlation between age and energy asymmetries indicating that the energy asymmetries between bottom-up and top-down closed throughout youth. (C), Correlation between age effects for individual state transitions (from panel A) and the energy asymmetries derived from the group-averaged structural connectome \( T_{E_A} \); see Fig. 2). We found that the age effects (Pearson’s \( r \)) were negatively correlated with \( T_{E_A} \), demonstrating that the strongest age effects were concentrated in the state transitions with the largest energy asymmetries. (D), Schematic illustration of a cross-validated regression model that was used to assess out-of-sample prediction of participants’ age. (E), Results from out-of-sample prediction of participants’ age. Energy asymmetries robustly predicted participants’ age in out-of-sample testing when scored using the correlation between true and predicted \( y \) (top, left), negative root mean square error (middle, left), and negative mean absolute error (bottom, left). As both error metrics represent the original units of \( y \), these results show that our model was able to predict age to within 2.64 to 3.18 years. Note, these prediction effects were replicated when using both a higher resolution version of our
parcellation that included 400 parcels (Schaefer 400; correlation($y_{true}$, $y_{predicted}$)=0.30; negative[RMSE]=-3.15; negative[MAE]=-2.60) as well as a 360-parcel multi-modal parcellation developed in the Human Connectome Project (correlation($y_{true}$, $y_{predicted}$)=0.30; negative[RMSE]=-3.15; negative[MAE]=-2.61). Taken together, these results show clearly that asymmetries in trans-hierarchical signal propagation and neurodevelopment are intimately intertwined.
Discussion

Here, we investigated how the relationship between cytoarchitecture and connectivity constrains the dynamics supported by the structural connectome. Using NCT\textsuperscript{51,52,68,69}, we modeled the amount of control energy that was required to propagate linear dynamics up and down the S-F axis of cytoarchitecture. We reported several key findings. First, we found that the energy required to complete bottom-up state transitions was lower compared to their top-down counterparts, indicating that bottom-up transitions were easier for our model to complete. Additionally, through a combination of null network models, as well as analyses of communicability and uncontrolled dynamics, we found that this energy asymmetry was underpinned by a network topology that is wired to enable efficient bottom-up signaling across the cortical hierarchy. Second, we found that energy asymmetries correlated with differences in intrinsic neuronal timescales estimated from ECoG as well as asymmetries in effective connectivity estimated from resting-state fMRI. The former finding demonstrates that efficient bottom-up signaling across the structural connectome is coincident with a lengthening of regions’ temporal receptive windows, while the latter shows that our model of dynamics is consistent with those drawn from functional data. Third, we found that regions’ position along the S-F axis was correlated with their importance in facilitating state transitions, demonstrating that the spatial modes of control embedded in our model were coupled to the cortical hierarchy. Finally, we found that asymmetries between bottom-up and top-down energy decreased as a function of age in a sample of developing youths. Overall, our results demonstrate that the higher-order topology of the human connectome may be wired to support asymmetric signaling across the cortical hierarchy, and that this signaling is rooted in the spatial patterning of cytoarchitecture that is itself guiding the ongoing refinement of connectivity throughout youth.

Cytoarchitecture shapes the connectome

Understanding how cytoarchitecture shapes connectivity is a central goal of neuroscience\textsuperscript{70}. In humans, recent research has shown a clear link between cortical cytoarchitecture and local properties of structural connectivity\textsuperscript{32,53,71}. Using graph theory, Wei \textit{et al.}\textsuperscript{32} found that several indices of regions’ local network importance correlated moderately with regions’ cytoarchitectonic similarity to the rest of the brain, demonstrating that regions with similar cytoarchitecture were more strongly, and more globally, connected to the rest of the network. Paquola \textit{et al.}\textsuperscript{53} defined a regional embedding space that fused together edge-level structural connectivity, geodesic distance, and cytoarchitectonic similarity\textsuperscript{5}. Paquola \textit{et al.}\textsuperscript{53} found that their wiring diagram explained variance in regional externopyramidization—which tracks the laminar origin of neuronal projections\textsuperscript{70}—supporting the notion that variance in the laminar origin of feedback and feedforward connections is intertwined with variance in cytoarchitecture and macroscopic connectivity. Our findings extend these prior studies by showing that cytoarchitecture shapes not only the local connectivity but also the higher-order topology of the structural connectome. Specifically, our findings suggest that cytoarchitecture may constrain the traversal of structural pathways to engender efficient bottom-up signal routing over the hierarchy. Thus, it appears that cytoarchitecture not only predicts which pairs of regions are connected (i.e., “like connects with like” cf. the \textit{structural model}\textsuperscript{1–4}), but also the spatial embedding of senders and receivers in the brain\textsuperscript{50,72,73}.

To probe potential explanations for how cytoarchitecture constrains higher-order topology, we examined three asymmetric communicability metrics\textsuperscript{50,56–58}: diffusion efficiency, search information, and cumulate path transitivity. We found that lower bottom-up transition energy was
associated with higher bottom-up diffusion efficiency, lower bottom-up search information, and lower bottom-up cumulative path transitivity. The first two correlations indicate the intuitive result that bottom-up energy may be lower because bottom-up diffusion of activity is more efficient—a conclusion that is also supported by our analysis of uncontrolled dynamics—and because it is more likely to track the shortest paths. The correlation with cumulative path transitivity indicates that top-down signaling encounters a greater number of returning detours nearer to the top of the S-F axis. In our model, the presence of local detours creates cycles that may give rise to sustained activity patterns74. In turn, the early occurrence of these detours may result in the earlier onset of sustained activity patterns for top-down state transitions. Thus, higher top-down energy may reflect the increased effort required to propagate these recurrent activity patterns down the S-F axis. This interpretation is consistent with the idea that the apex of the S-F axis forms a limbic workspace, wherein sustained activity patterns support ongoing prediction and integration of sensory signals in a predictive coding framework75.

Energy asymmetries link to changes in intrinsic neuronal timescales and effective connectivity
Recent work has shown that the spatial patterning of regions’ intrinsic neuronal timescales correlate with the patterning of the T1w/T2w ratio10, suggesting that the brain’s timescale hierarchy reflects its cytoarchitectonic hierarchy. Here, we found that the asymmetries in trans-hierarchical state transitions were coupled to differences in state-level intrinsic neuronal timescales. Specifically, the easier a bottom-up state was to complete (compared to its top-down counterpart) the more the timescale of the target state lengthened compared to the initial state. Lengthening timescales are thought to be associated with progressive changes to longer temporal receptive windows, which in turn is thought to underpin shifts from segregated to integrated functional processing76. Thus, convergent with our communicability results, these findings show that the topology of the structural connectome may be wired to support the progressive integration of lower-order properties of our environment into higher-order percepts and cognitions. Our findings also serve as a functional validation of our network control model; we observed a positive correlation between energy asymmetries and asymmetries in effective connectivity, which is consistent with past literature50. Thus, our findings contribute to a growing body of evidence demonstrating that asymmetric signal routing is measurable from the topology of the connectome, despite being derived from an undirected description of brain connectivity.

Energy asymmetries refine systematically throughout youth
The effects of development on connectome topology are increasingly well studied42,77–79, including with network control theory where the amount of control energy required to activate the executive function system (from baseline) has been shown to decrease throughout youth80. This observation is consistent with the current study, wherein the energy associated with trans-hierarchical state transitions also reduced throughout youth. Here, we provide a key extension to prior work that deepens our understanding of these developmental energy effects; we observed that energy asymmetries diminished as a function of age in our sample, and that this effect was driven by stronger age effects for top-down energy compared to bottom-up. These findings suggest that maturation throughout youth alters the balance between bottom-up and top-down signal propagation, refining the connectome towards an equilibrium between the two. This interpretation is consistent with a staging account of neurodevelopment that suggests that lower-order connections are refined earlier in development compared to their higher-order counterparts3,39–41. That is, the energy asymmetry we observed might reflect the relatively advanced refinement of
lower-order connections that is already well underway by 8 years of age (the youngest in our sample). In turn, the stronger age effect observed for top-down energy might reflect the relatively delayed onset of refinement of higher-order connections that may be occurring within the age range of our sample. Examining how our results present on either side of the age range of the PNC, as well as whether they are supported by longitudinal data, will be a critical avenue for future research.

**Limitations**

Similar to our recent work\(^8\), a limitation of this study is the use of a linear model of neuronal dynamics to estimate signal propagation across the S-F axis. While this assumption is an oversimplification of brain dynamics, linear models explain variance in the slow fluctuations in brain activity recorded by fMRI\(^8\),\(^8\), suggesting that they successfully approximate the kinds of data commonly used to examine brain function. An additional limitation is the use of a single map of cytoarchitecture to define brain states, which precluded us from defining participant-specific states. This limitation may be compounded by the fact that the S-F axis we used was obtained from an adult brain, whereas our structural connectomes were estimated in a developing sample. As mentioned above, previous work contends that the T1w/T2w ratio forms a reasonable proxy of the S-F axis that is measurable in vivo\(^5\). However, while the PNC includes T1-weighted imaging, it does not include T2-weighted imaging\(^5\), which prevented us from estimating the T1w/T2w ratio in our sample. Replication of our findings using participants’ T1w/T2w maps is warranted given well-known individual variability in the spatial patterning of cortical structural features. However, this approach must be weighed against the fact the T1w/T2w ratio is imperfectly correlated with the S-F axis. Thus, such replication efforts must consider the trade-off between the value of capturing individual variability and the cost of potentially disconnecting from the relevant underlying neurobiology (i.e., cytoarchitecture). Indeed, our results showing that energy asymmetries did not replicate using the T1w/T2w ratio taken from the HCP data support this interpretation. Finally, our use of a developmental sample limits the generalizability of our findings beyond the age range of the PNC. Future work may consider replicating our effects in lifespan data to examine the extent to which energy asymmetries are a general feature of connectome organization. This is particularly pertinent given recent work showing protracted changes to the rich club of the connectome across 5 to 80 years of age\(^8\).

**Conclusions**

Our results demonstrate that cytoarchitecture may constrain network topology in such a way as to induce asymmetries in signal propagation across the cortical hierarchy. Specifically, we found that bottom-up trans-hierarchical state transitions were easier to complete than their top-down counterparts, that energy asymmetries correlated with asymmetries in communicability metrics and changes to neuronal timescales, that control signals tracked the sensory-fugal axis, and that asymmetries reduced with age in youth. Collectively, our work highlights that variation in the properties of cortical microstructure that govern extrinsic connectivity may guide the formation of macroscopic connectome topology.
Materials and Methods

Participants
Participants included 793 individuals from the Philadelphia Neurodevelopmental Cohort\textsuperscript{85,86}, a community-based study of brain development in youths aged 8 to 22 years\textsuperscript{87,88}. The institutional review boards of both the University of Pennsylvania and the Children’s Hospital of Philadelphia approved all study procedures. The neuroimaging sample of the PNC consists of 1,601 participants\textsuperscript{85}. From this original sample, 156 were excluded due to the presence of gross radiological abnormalities distorting brain anatomy or due to a medical history that might impact brain function. Next, a further 159 participants were excluded because they were taking psychoactive medication at the time of study. An additional 466 individuals were excluded because they did not pass rigorous manual and automated quality assurance for their T1-weighted scan\textsuperscript{89}, their diffusion scan\textsuperscript{90}, or their resting-state functional magnetic resonance imaging (rs-fMRI) scan\textsuperscript{91,92}. Finally, 27 participants were excluded owing to the presence of disconnected regions in their structural connectivity matrix (see section entitled Structural connectome construction below). This process left a final sample of 793 participants.

Imaging data acquisition
MRI data were acquired on a 3 Tesla Siemens Tim Trio scanner with a 32-channel head coil at the Hospital of the University of Pennsylvania. Diffusion weighted imaging (DWI) scans were acquired via a twice-refocused spin-echo (TRSE) single-shot echo-planar imaging (EPI) sequence (TR=8100 ms, TE=82 ms, FOV=240\text{mm}^2/240\text{mm}^2; Matrix=RL: 128, AP: 128, Slices: 70, in-plane resolution of 1.875 mm\text{2}; slice thickness=2 mm, gap=0; flip angle=90°/180°/180°, 71 volumes, GRAPPA factor=3, bandwidth=2170 Hz/pixel, PE direction=AP). The sequence utilized a four-lobed diffusion encoding gradient scheme combined with a 90-180-180 spin-echo sequence designed to minimize eddy-current artifacts\textsuperscript{54}. The sequence consisted of 64 diffusion-weighted directions with \(b=1000 \text{s/mm}^2\) and 7 interspersed scans where \(b=0 \text{s/mm}^2\). The imaging volume was prescribed in axial orientation and covered the entire brain.

In addition to the DWI scan, a B0 map of the main magnetic field was derived from a double-echo, gradient-recalled echo (GRE) sequence, allowing for the estimation and correction of field distortions. Prior to DWI acquisition, a 5-min magnetization-prepared, rapid acquisition gradient-echo T1-weighted (MPRAGE) image (TR=1810 ms, TE=3.51 ms, FOV=180 x 240 mm, matrix 256 x 192, effective voxel resolution of 0.94 x 0.94 x 1 mm) was acquired for each participant.

Finally, approximately 6 minutes of rs-fMRI data was acquired using a blood oxygen level-dependent (BOLD-weighted) sequence (TR=3000 ms; TE=32 ms; FoV=192 x 192 mm; resolution 3 mm isotropic; 124 volumes). These data were used primarily to generate the principal cortical gradient of functional connectivity discussed in the main text\textsuperscript{12} (see section entitled Principal gradient of functional connectivity below).

Imaging data quality control
All DWI and T1-weighted images underwent rigorous quality control by highly trained image analysts (see Roalf et al. (2016) and Rosen et al. (2018) for details on DTI and T1-weighted imaging, respectively). Regarding the DWI acquisition, all 71 volumes were visually inspected and evaluated for the presence of artifacts. Every volume with an artifact was marked as contaminated and the fraction of contaminated volumes was taken as an index of scan quality.
Scans were marked as ‘poor’ if more than 20% of volumes were contaminated, ‘good’ if more than 0% but less than 20% of volumes were contaminated, and ‘great’ if 0% of volumes were contaminated. Regarding the T1-weighted acquisition, images with gross artifacts were considered ‘unusable’; images with some artifacts were flagged as ‘usable’; and images free of artifact were marked as ‘superior’. As mentioned above in the section entitled Participants, 466 individuals were removed due to quality. Of these, 318 individuals were removed due to either ‘poor’ DWIs or ‘unusable’ T1-weighted images. In the final sample of 793 participants, a total of 535 participants had diffusion tensor images identified as ‘great’, with the remaining identified as ‘good’, and 701 participants had T1-weighted images identified as ‘superior’, with the remaining identified as ‘usable’. Regarding the rs-fMRI data, as in prior work\textsuperscript{91,92}, the remaining 148 of 466 excluded participants were removed either because their mean relative root mean square (RMS) framewise displacement was higher than 0.2 mm or their scan included more than 20 frames with motion exceeding 0.25 mm.

**Structural image processing**

Structural image processing was carried out using tools included in ANTs\textsuperscript{93}. The \texttt{buildtemplateparallel} pipeline from ANTs\textsuperscript{94} was used to create a study-specific T1-weighted structural template with 120 participants that were balanced on sex, race, and age. Structural images were processed in participants’ native space using the following procedure: brain extraction, N4 bias field correction\textsuperscript{95}, Atropos tissue segmentation\textsuperscript{96}, and SyN diffeomorphic registration\textsuperscript{94,97}.

**Diffusion image processing**

For each participant, a binary mask was created by registering the standard fractional anisotropy mask provided by FSL (FMRIB58 FA) to the participant’s mean \(b=0\) reference image using FLIRT\textsuperscript{98}. To correct for eddy currents and head motion, this mask and the participant’s diffusion acquisition was passed to FSL’s \texttt{eddy}\textsuperscript{99} (version 5.0.5). Diffusion gradient vectors were subsequently rotated to adjust for the motion estimated by \texttt{eddy}. Distortion correction was conducted via FSL’s FUGUE\textsuperscript{100} using the participant’s field map, estimated from the B0 map.

**rs-fMRI processing**

State-of-the-art processing of functional data is critical for valid inference\textsuperscript{101}. Thus, functional images were processed using a top-performing preprocessing pipeline implemented using the eXtensible Connectivity Pipeline (XCP) Engine\textsuperscript{91}, which includes tools from FSL\textsuperscript{100,102} and AFNI\textsuperscript{103}. This pipeline included (1) correction for distortions induced by magnetic field inhomogeneity using FSL’s FUGUE utility, (2) removal of 4 initial volumes, (3) realignment of all volumes to a selected reference volume using FSL’s MCFLIRT, (4) interpolation of intensity outliers in each voxel’s time series using AFNI’s 3dDespike utility, (5) demeaning and removal of any linear or quadratic trends, and (6) co-registration of functional data to the high-resolution structural image using boundary-based registration. Images were de-noised using a 36-parameter confound regression model that has been shown to minimize associations with motion artifact while retaining signals of interest in distinct sub-networks\textsuperscript{91,104}. This model included the six framewise estimates of motion, the mean signal extracted from eroded white matter and cerebrospinal fluid compartments, the mean signal extracted from the entire brain, the derivatives of each of these nine parameters, and quadratic terms of each of the nine parameters and their
derivatives. Both the BOLD-weighted time series and the artificial model time series were temporally filtered using a first-order Butterworth filter with a passband of 0.01–0.08 Hz.\(^{105}\)

**Imaging-derived nuisance covariates**

In our analyses of individual differences, we used total brain volume, edge density, and mean in-scanner motion as imaging-derived nuisance covariates. Total brain volume was generated from the T1-weighted images using ANTs. In-scanner head motion was estimated for each participant from their DWI sequence as relative framewise displacement.\(^{90}\) Specifically, rigid-body motion correction was applied to the seven high quality \(b=0\) images interspersed throughout the diffusion acquisition. Once estimated, framewise displacement was averaged across time to create a single measure for each participant. Edge density was estimated from each participant’s adjacency matrix (see section entitled *Structural connectome construction* below) as the fraction of present connections to all possible connections.

**Structural connectome construction**

For each participant, whole-brain deterministic fiber tracking was conducted using DSI Studio\(^{106}\) with a modified fiber assessment by continuous tracking (FACT) algorithm with Euler interpolation. A total of 1,000,000 streamlines were generated for each participant that were between 10mm and 400mm long. Fiber tracking was performed with an angular threshold of 45° and step size of 0.9375 mm. Next, following our previous work\(^{81}\), the number of streamlines intersecting region \(i\) and region \(j\) in a 200-parcel cortical parcellation\(^{107}\) was used to weight the edges of an undirected adjacency matrix, \(A\) (see Fig. S11 for sensitivity analyses covering different parcellation resolutions and definitions\(^{108}\)). Note that \(A_{ij} = 0\) for \(i = j\). This process yielded 793 subject-specific \(A\) matrices that were used in subject-level analyses reported in the main text (i.e., Fig. 6). Our primary analyses, however, were based on a group-averaged \(A\) matrix. To obtain this \(A\) matrix, we averaged over the entries of the individuals’ \(A\) matrices and thresholded using an edge consistency-based approach.\(^{109}\) Specifically, edges in the group-averaged \(A\) matrix were only retained if non-zero edge weights were present in at least 60% of participants’ \(A\) matrices.\(^{110}\) If not, edges were set to zero. This process yielded a group-averaged structural connectome with a sparsity value of approximately 8%. This group-averaged structural connectome was used for analyses reported in Figs. 2, 3, 4, 5, and 6. See Fig. S12 for sensitivity analyses spanning a range of consistency thresholds and corresponding sparsity values.

**Trans-hierarchical state transitions**

**Cortical hierarchies**

Below we describe three definitions of the cortical hierarchy that were used in the present study to examine trans-hierarchical state transitions.

**Sensory-fugal axis of cytoarchitecture**

We primarily characterized the cortical hierarchy using the gradient of cytoarchitectonic similarity developed in previous work\(^{5,53}\) and disseminated as part of the BigBrainWarp toolbox.\(^{6}\) Specifically, from BigBrainWarp, we retrieved the histological gradient (‘Hist-G2’) corresponding to the sensory-fugal (S-F) axis of cytoarchitecture stored in \(fsaverage\) space. Next, we averaged over the vertex values within each of our 200 cortical parcels (see section entitled *Structural connectome construction* below) as the fraction of present connections to all possible connections.
connectome construction above). This process resulted in a $200 \times 1$ vector describing regions’ positions along the S-F axis of cytoarchitectonic similarity.

Alternative hierarchies: T1w/T2w ratio and the gradient of functional connectivity
As stated above and in the main text, our primary constituent of the cortical hierarchy was the S-F axis of cytoarchitectonic similarity. To test the specificity of our primary results, we also examined two other definitions of the cortical hierarchy: the T1w/T2w ratio\textsuperscript{31} and the principal gradient of functional connectivity\textsuperscript{12}.

The T1w/T2w ratio is thought to index cortical microstructure and myelin content \textit{in vivo}\textsuperscript{5,7,31}. As above, we retrieved this definition of the cortical hierarchy gradient from BigBrainWarp (‘Micro-G1’) stored in \textit{fsaverage} space and averaged over the vertex values within each of our 200 cortical parcels. This process resulted in a $200 \times 1$ vector describing regions’ positions along the MRI proxy of the S-F axis.

The gradient of functional connectivity situates unimodal sensorimotor cortex at one end and transmodal association cortex at the other. Deriving this definition of the cortical hierarchy involves projecting functional connectivity data to a low-dimensional manifold that positions regions with similar functional connectivity profiles near to one another and regions with dissimilar functional connectivity profiles distant from one another. Here, as in our previous work\textsuperscript{81}, we generated this gradient using whole-brain resting-state functional connectivity obtained from the PNC data (see section entitled \textit{rs-fMRI processing} above). Specifically, for each participant, processed rs-fMRI timeseries were averaged regionally and a Pearson correlation coefficient was estimated between each pair of regional timeseries to generate a functional connectome. Correlation coefficients were normalized using Fisher’s \textit{r}-to-\textit{z} transform, and then connectomes were averaged over participants. The principal gradient of functional connectivity was generated from this group-average functional connectome using diffusion map embedding implemented in the \textit{BrainSpace} toolbox\textsuperscript{111}. We selected the first gradient output from this approach, which was closely aligned to that observed previously\textsuperscript{12}. Note that this gradient is the same as that reported in our previous work\textsuperscript{81}. This process resulted in a $200 \times 1$ vector that describes regions’ positions along the unimodal-to-transmodal (U-T) axis of functional connectivity.

Hierarchical brain states
As discussed in the main text and illustrated in \textbf{Fig. 1}, we divided our $200 \times 1$ S-F axis of cytoarchitecture—as well as the T1w/T2w ratio and U-T axis of functional connectivity—into 20 evenly sized ($n=10$) and non-overlapping sets of brain regions that traversed up the cortical hierarchy. This procedure yielded 20 groups of cortical regions that differed based on their position along the cortical hierarchy. Thus, regions within each group had similar profiles of cytoarchitecture while regions between groups had dissimilar profiles of cytoarchitecture. Moreover, this dissimilarity increased with greater distance between pairs of groups along the S-F axis. These 20 groups of regions formed the brain states that we used in the network control theory analysis (see section entitled \textit{Network control theory} below), thus allowing us to model transitions between states moving up and down the cortical hierarchy. See \textbf{Fig. S13} for sensitivity analyses covering different set sizes for brain states.
Network control theory
To model trans-hierarchical state transitions, we employed tools from network control theory. Given an $A$ matrix as input (either group-averaged or individual; see section entitled Structural connectome construction above), we first apply the following normalization:

$$A = \frac{A}{\lambda(A)_{max} + c} - I.$$  

Eq. 1

Here, $\lambda(A)_{max}$ is the largest eigenvalue of $A$, $c = 1$ to ensure system stability, and $I$ denotes the identity matrix of size $N \times N$. In our analyses, $N$ is equal to the number of brain regions, which is 200. Within this normalized $A$ matrix, we allow each node of the network to carry a real value representing that node’s activity. These values are represented in $x$ and collectively describe the pattern of whole-brain activity as it changes over time. Next, we use a simplified noise-free linear continuous-time and time-invariant model of network dynamics:

$$\dot{x} = Ax(t) + B_k u_k(t),$$  

Eq. 2

where $x(t)$ is a $N \times 1$ vector that represents the state of the system at time $t$. The matrix $B_k$ identifies the control input weights, which by default we set to the $N \times N$ identity matrix to compute unweighted energy (see section entitled Minimizing transition energy through optimized control weights below for the weighted case).

Given the above model of the dynamics (Eq. 2), we compute the control inputs, $u_k(t)$, that drive the system from some initial state, $x_0$, to some target state, $x^*$, in a finite amount of time, $T = 1$. Here, initial and target states were constructed using the 20 non-overlapping groups of 10 brain regions spanning the S-F axis (see above section entitled Hierarchical brain states). That is, each initial or target state was defined as an $N \times 1$ vector within which 10 elements that represented cytoarchitecturally similar areas contained a 1, and the remaining elements contained a 0. Among the many possible inputs, we chose the minimum energy input which minimizes a quadratic cost on the inputs, such that

$$E_{min} = \min \int_0^T u_k^T(t)u_k(t)dt,$$  

Eq. 3

subject to Eq. 2. To compute the minimum energy, we construct a useful mathematical object called the controllability Gramian, given by

$$W_c = \int_0^T e^{At}BB^Te^{A^Tt}dt,$$  

Eq. 4

where $e^{At}$ is the time-dependent matrix exponential of the matrix $A$, and is also the impulse response of the system that governs the natural evolution of system dynamics. Then, the minimum energy is given by

$$E_{min} = (e^{At}x_0 - x^*)^T W_c^{-1}(e^{At}x_0 - x^*).$$  

Eq. 5
Intuitively, the quantity in the parentheses measures the difference between the natural evolution of the system from the initial condition, $e^{A t} x_0$, and the target state, $x^*$. This difference is precisely the difference for which the control input $u_k(t)$ needs to compensate, and the projection of this difference onto $W_c^{-1}$ yields the minimum energy for providing such compensation.

**Transition energy and energy asymmetries**

We used the above derivation of minimum control energy to compute a $k \times k$ transition energy matrix, $T_E$. Elements of $T_E$ quantified the minimum energy ($E$) required to transition between all possible pairs of $k = 20$ brain states, where brain states were based on the subsets of regions sampled along the S-F axis of cytoarchitecture outlined above (see section entitled Cortical hierarchies). Following from the above equations, we interpret transition energy as the amount of effort the control signals had to exert to compensate for the difference between the natural (i.e., uncontrolled) and the desired (i.e., controlled) evolutions of the system. In this way, lower transition energy corresponds to less need for control input, which in turn confers a transition that is easier for the model to complete. Thus, we interpret differences in transition energy as differences in the ease with which dynamics can be controlled to propagate across the S-F axis of cytoarchitecture.

As mentioned in the main text and above, the hierarchically ordered nature of our brain states endowed $T_E$ with a distinction between transitions moving up the hierarchy (bottom-up energy) from those moving down the hierarchy (top-down energy). Further, these bottom-up and top-down transition energies were naturally compartmentalized into the upper and lower triangles of $T_E$, respectively. Hence, asymmetries between bottom-up and top-down energy for all state pairs were calculated as $T_{E\Delta} = T_E - T_E^T$. Note that unlike $T_E$, $T_{E\Delta}$ is symmetrical; thus, only the upper triangle was carried forward for asymmetry analysis.

**Bootstrap test for energy asymmetries**

In Fig. 2 in the main text, we showed that bottom-up energy was lower than top-down (negative mean $T_{E\Delta}$) and that $T_{E\Delta}$ was negatively correlated with the distance that separated states along the hierarchy. To examine whether these effects were robust to sampling variability, we calculated $T_{E\Delta}$ in each of 1,000 bootstrapped versions of our group-averaged structural connectome. Specifically, we reproduced our group-averaged structural connectome for each of 1,000 bootstrapped samples comprising 50% of our 793 participant connectomes ($n=396$). Then, we re-estimated $T_{E\Delta}$ in each of these 1,000 bootstrapped connectomes. This procedure allowed us to estimate 95% confidence intervals on mean $T_{E\Delta}$ and the correlation with hierarchical distance (see Fig. 2A and Fig. 2B).

**Null network models**

In addition to our above bootstrap test, we compared both mean $T_{E\Delta}$ and the correlation with hierarchical distance to null distributions generated using two different spatially embedded null network models. Alongside preserving the spatial embedding of network nodes, these null network models randomly rewired the network while preserving either the edge distribution or the strength distribution of the network. For each of these null models, we produced 10,000 rewired networks derived from the group-averaged structural connectome (see section entitled Structural connectome construction above). Then, to generate empirical null distributions, upon each rewired network we recomputed $T_{E\Delta}$ and the corresponding hierarchy distance correlation. Finally, $p$-
values were estimated as the probability that the magnitude of the observed values occurred under a given null.

Comparison with measures of communicability

As mentioned in the main text, we compared our energy asymmetries ($T_{EA}$) to asymmetric measures of network communicability taken from past literature, namely, diffusion efficiency ($de$), search information ($si$), and a modified version of path transitivity ($pt$). We implemented $de$ and $si$ following past literature, as such we refer readers to $^{50,56–58}$ as well as the Brain Connectivity Toolbox (https://sites.google.com/site/bctnet/; diffusion_efficiency.m and search_information.m) for details. For path transitivity, we developed a modified version that incorporated asymmetries by examining the cumulative $pt$ over successively longer segments of the shortest path. Below, we describe the original definition of path transitivity before describing our modification.

Path transitivity is sensitive to the number of local detours (i.e., those that traverse only two edges) that are present along the shortest path connecting two nodes, source and target. To estimate path transitivity, the matching index between all possible pairs of nodes is first estimated as follows:

$$m_{ij} = \frac{\sum_{k \in I} (w_{ik} + w_{jk}) \theta(w_{ik}) \theta(w_{jk})}{\sum_{k \in J} w_{ik} + \sum_{k \in J} w_{jk}}$$  \hspace{1cm} Eq. 6

where $w_{ij}$ is the weight of the edge between nodes $i$ and $j$, and $k$ denotes the node along a detour between nodes $i$ and $j$. The quantity $\theta(w_{ik}) = 1$ if $w_{ik} > 0$ and 0 otherwise, and the quantity $\theta(w_{jk}) = 1$ if $w_{jk} > 0$ and 0 otherwise. Then, assuming a sequence of nodes, $\Omega_{s\rightarrow t} = \{s, a, b, c, d, t\}$, that comprise a shortest path, path transitivity is calculated by summing the matching index for each pair of nodes as follows:

$$pt(\Omega_{s\rightarrow t}) = \frac{2 \sum_{i \in \Omega} \sum_{j \in \Omega} m_{ij}}{|\Omega_{s\rightarrow t}|(|\Omega_{s\rightarrow t}| - 1)}$$  \hspace{1cm} Eq. 7

where $|\Omega_{s\rightarrow t}|$ denotes the number of nodes in $\Omega_{s\rightarrow t}$, and hence $|\Omega_{s\rightarrow t}|(|\Omega_{s\rightarrow t}| - 1)$ is the total number of pairs of nodes comprising $\Omega_{s\rightarrow t}$. Since $A$ is weighted in our study, a higher $pt$ confers a path with higher strength of local returning detours.

To endow path transitivity with asymmetry, we performed the follow modification. We calculated $pt$ separately for each segment of $\Omega_{s\rightarrow t}$ that began at the source node (Fig. 3B); $\Omega_{s \rightarrow a} = \{s, a\}$, $\Omega_{s \rightarrow b} = \{s, a, b\}$, $\Omega_{s \rightarrow c} = \{s, a, b, c\}$, $\Omega_{s \rightarrow d} = \{s, a, b, c, d\}$, and $\Omega_{s \rightarrow t} = \{s, a, b, c, d, t\}$. Critically, for each of these segments, the denominator in Eq. 7 remained fixed as $|\Omega_{s\rightarrow t}|(|\Omega_{s\rightarrow t}| - 1)$. This choice resulted in the $pt$ of each segment being normalized by the full shortest path, which guaranteed that the transitivity of each segment approached the transitivity of the full shortest path. The $pt$ of each segment was assembled as a $n \times 1$ vector, $pt_c$, where $n$ is the number of segments, which in turn is equal to the length of the shortest path. We refer to this vector as cumulative path transitivity. Next, we re-estimated cumulative path transitivity for segments starting from the target node, thus obtaining $pt_c$ for both directions along the shortest path, $pt_{c, s \rightarrow t}$ and $pt_{c, t \rightarrow s}$ (Fig. 3C). Finally, we subtracted these vectors elementwise and summed the differences, $pt_{c\Delta} = \sum (pt_{c, s \rightarrow t} - pt_{c, t \rightarrow s})$. A positive $pt_{c\Delta}$ states that path transitivity accumulated more quickly when traversing from source to target compared to target to source. Intuitively, this means that high-
strength local detours were encountered sooner while traversing source to target compared to the reverse. Thus, $p_{t_{\Delta}}$ is asymmetric.

**Uncontrolled dynamics**

In addition to examining the energy required to complete state transitions between specific state-pairs, we also examined how uncontrolled dynamics spread naturally across the cortex from each of our cytoarchitectonic brain states. Specifically, for each brain state, we set the constituent regions’ activity to 1 and all other regions’ activity to 0. Then, we allowed the activity to diffuse in an uncontrolled manner along the networks’ edges over time according to $\dot{x} = Ax(t)$. This approach stands in contrast to the approach that we have discussed thus far of guiding activity to flow from one state to another via a set of control signals. As mentioned in the main text, for each seed brain state and time point, $t$, we correlated the pattern of simulated activity with the sensory-fugal axis of cytoarchitecture. Results of this analysis are shown in Fig. 4B and 4C.

**Intrinsic neuronal timescales**

As mentioned in the main text, we sought to validate our transition energy analysis in functional data using intrinsic neuronal timescales derived from electrocorticography (ECoG) data. Thus, we compared energy asymmetries from our NCT analysis with differences between brain states’ intrinsic timescales. Following previous work, we estimated regions’ intrinsic timescales using the time constant, $\tau$, of an exponential decay function fitted to the autocorrelation function of ECoG timeseries. Specifically, we downloaded sensor-level $\tau$ data processed by Gao et al. (https://github.com/rdgao/field-echos/data/df_human.csv) and, using the provided MNI coordinates, matched each sensor to our parcellation (200 Schaefer parcels); matching was done by finding the smallest Euclidean distance between each sensor and the centroid of each parcel. We then averaged $\tau$ over sensors within each parcel as well as over regions within each cytoarchitectonic brain state. This process generated state-level $\tau$ values that were then subtracted to produce $\tau_{\Delta}$, a matrix of change in $\tau$ between all pairs of brain states.

**Effective connectivity**

As mentioned in the main text, we sought to validate our transition energy analysis in functional data using effective connectivity derived from rs-fMRI data. Thus, we compared energy asymmetries from our NCT analysis with asymmetries in effective connectivity. As per our previous work, effective connectivity was estimated using a spectral version of dynamic causal modeling (spDCM) implemented in SPM12 (Wellcome Trust Centre for Neuroimaging, London, UK). To generate timeseries for modeling effectivity connectivity, we first averaged participants’ processed rs-fMRI data across the regions that comprised each cytoarchitectonic brain state. This process yielded one timeseries of 120 volumes per subject per brain state. Next, owing to the low number of volumes in our rs-fMRI acquisition, we deployed an averaging and concatenation approach that yielded a single group-averaged timeseries of 1200 volumes for each brain state. This process proceeded as follows. First, we randomly excluded 3 participants from our sample to retain 790 participants. Second, we divided our sample of 790 participants into 10 equally sized groups ($n=79$) and averaged the state-level rs-fMRI timeseries across participants within each group separately. Finally, we concatenated these group-averaged timeseries end-to-end across the 10 groups. This process yielded resting-state timeseries for each brain state with 1200 volumes that represented averages over distinct subsets of participants taken from our sample. These timeseries were used as inputs to the spDCM algorithm, together with a fully
connected model of coupling strengths, enabling the estimation of effective connectivity between all cytoarchitectonic brain states spanning the S-F axis. As per our primary analysis of transition energies, effective connectivity estimates were trivially grouped into bottom-up and top-down, and were then subtracted to create an effective connectivity asymmetry matrix.

**Minimizing transition energy through optimized control weights**

Our primary analyses involved examining uniformly weighted transition energies, where all nodes of the dynamical system were assigned control weights equal to 1 (i.e., setting the diagonal entries of $B_k$ in Eq. 2 to the $N \times N$ identity matrix). This uniform weighting meant that all brain regions were endowed with the same degree of control over all $k \times k$ state transitions. However, as discussed in the main text (see section entitled Optimized control weights track the sensory-fugal axis of cytoarchitecture and increase energy asymmetries), we were also interested in examining regional variation in facilitating trans-hierarchical state transitions.

To achieve this goal, we systematically perturbed each region’s degree of control over the system and measured the corresponding change in transition energies. Specifically, for each brain region, $i$, we recomputed $T_E$ after adding a constant amount of additional control to the corresponding diagonal element of $B_k$ (the remaining diagonal entries were left equal to 1). This process generated a $k \times k \times 200$ matrix of perturbed transition energies, $P_E$. Next, for each perturbed region (dimension 3 of $P_E$), we subtracted the perturbed transition energies from the uniformly weighted energies ($T_E$) to create $P_{EA}$, a $k \times k \times 200$ matrix of perturbed transition energy deltas. For each state transition, this subtraction yielded a $200 \times 1$ vector that quantified how perturbing each node of the system one at a time—by a constant arbitrary amount—impacted transition energy. Note that increasing the influence of a single node’s control necessarily reduces energy; the task of completing a state transition is easier for the model when any node in $B_k$ is granted a greater degree of control over the system, leading to lower energy. Accordingly, all values in $P_{EA}$ were positive and the magnitude of these deltas encoded the relative importance of each region to completing a specific state transition, with regions with larger deltas being more important.

To assess correspondence with the S-F axis, we calculated the Spearman rank correlation between perturbed deltas for each state transition and the S-F axis. The spatial embedding of perturbed deltas varied as a function of the location of the initial and target states on the S-F axis. To account for this, instead of correlating deltas with the S-F axis directly, we correlated them with the distance separating nodes from the initial and target state separately and retained the strongest correlation coefficient. In this way, any observed correlation captures the extent to which deltas vary as a function of hierarchical distance from the states that comprise a given transition. Note, nodes that were within the initial and target states were excluded when calculating correlations. Thus, coupling between the deltas and the S-F axis was only assessed in the remaining bystander regions. We assigned $p$-values using BrainSMASH (Brain Surrogate Maps with Autocorrelated Spatial Heterogeneity; https://brainsmash.readthedocs.io/) and corrected for multiple comparisons via the Benjamini and Hochberg false discovery rate (FDR, $q = 0.05$) procedure. The spatial autocorrelation embedded in neuroimaging data can lead to inflated $p$-values in spatial correlation analyses and must be accounted for in the creation of null models. BrainSMASH addresses this by generating null brain maps that match the spatial autocorrelation properties of the input data. We used BrainSMASH to generate 10,000 spatial autocorrelation–preserving null maps of the S-F axis, generating a null distribution of Spearman rank correlations.
Finally, we re-estimated $T_E$ (and $T_{EA}$) one more time using each state transition’s vector of perturbed deltas as optimized control weights. This process yielded optimized trans-hierarchical transition energies and energy asymmetries. Finally, to assess whether the size of the mean $T_{EA}$ was significantly different for optimized weights compared to uniform weights, we derived $T_{EA}$ for both weight sets using bootstrapped group-averaged connectomes (see section entitled Bootstrap test for energy asymmetries above) and assigned 95% confidence intervals to the mean $T_{EA}$.

**Age effects**

As mentioned in the main text, we sought to link participant-specific energy asymmetries with age to examine developmental effects. To achieve this goal, we derived $T_E$ and $T_{EA}$ from each participant’s $A$ matrix (see section entitled Structural connectome construction above) using optimized control weights. Note that the process of computing optimized transition energies was performed on a subject-specific basis using subject-specific optimized control weights; this was done by applying the above perturbation procedure (see section entitled Minimizing transition energy through optimized control weights) to each participant’s $A$ matrix separately (see Fig. S14 for correlations between participant-specific optimized weights and the gradient of cytoarchitecture). Next, for each state transition, we calculated the Pearson’s correlation between $T_E$ and age, while controlling for sex, total brain volume, edge density, and in-scanner motion (see section entitled Imaging-derived nuisance covariates above). We repeated this process for energy asymmetries averaged over bottom-up and top-down energy, where energy was averaged over the upper and lower triangles of each participant’s $T_E$ matrix, respectively, before being subtracted.

In addition to estimating within-sample age effects, we also sought to test whether energy asymmetries could be used to predict participants’ ages in out-of-sample testing. To achieve this, we assembled the upper triangle of each subject’s $T_{EA}$ matrix into a $793 \times 190$ feature table, $X$. Then, we used a cross-validated ridge regression model implemented in scikit-learn with default parameters ($\alpha = 1$) to predict participants’ ages ($y$). Specifically, we assessed out-of-sample prediction performance using 10-fold cross-validation scored by root mean squared error (RMSE), mean absolute error (MAE), and the correlation between the true $y$ and predicted $y$. Note, as per scikit-learn defaults, to standardize the interpretation of all scoring metrics as higher scores represent better performance, we flipped the sign for RMSE and MAE.

Models were trained using all columns of $X$ as input features and scoring metrics were each averaged across folds. As above, we included sex, total brain volume, edge density, and in-scanner motion as nuisance covariates. Nuisance covariates were controlled for by regressing their effect out of $X$ before predicting $y$. Within each fold, nuisance covariates were fit to the training data and applied to the test data to prevent leakage. Subsequently, we applied principal component analysis (PCA) to reduce the dimensionality of $X$, retaining enough PCs to explain 80% of the variance in the data. Finally, owing to evidence that prediction performance can be biased by the arbitrariness of a single split of the data, we repeated 10-fold cross-validation 100 times, each time with a different random 10-fold split. This process yielded a distribution of 100 mean negative RMSE values, 100 mean negative MAE values, and 100 mean correlations between true $y$ and predicted $y$.

Our above prediction model generated robust estimates of prediction performance, but it did not examine whether prediction performance was itself significant. To test whether prediction performance was better than chance, we compared point estimates of each of our scoring metrics—taken as the mean over the 100 values—to the distribution of values obtained from permuted data.
Specifically, we subjected the point estimates of our scoring metrics to 10,000 random permutations, wherein the rows (i.e., participants) of y were randomly shuffled.
References


Citation diversity statement
Recent work in several fields of science has identified a bias in citation practices such that papers from women and other minority scholars are under-cited relative to the number of such papers in the field\textsuperscript{116–124}. Here we sought to proactively consider choosing references that reflect the diversity of the field in thought, form of contribution, gender, race, ethnicity, and other factors. First, we obtained the predicted gender of the first and last author of each reference by using databases that store the probability of a first name being carried by a woman\textsuperscript{120,125}. By this measure (and excluding self-citations to the first and last authors of our current paper), our references contain 7.82% woman(first)/woman(last), 12.25% man/woman, 16.98% woman/man, and 62.95% man/man. This method is limited in that a) names, pronouns, and social media profiles used to construct the databases may not, in every case, be indicative of gender identity and b) it cannot account for intersex, non-binary, or transgender people. Second, we obtained predicted racial/ethnic category of the first and last author of each reference by databases that store the probability of a first and last name being carried by an author of color\textsuperscript{126,127}. By this measure (and excluding self-citations), our references contain 6.03% author of color (first)/author of color (last), 19.77% white author/author of color, 20.93% author of color/white author, and 53.27% white author/white author. This method is limited in that a) names and Florida Voter Data to make the predictions may not be indicative of racial/ethnic identity, and b) it cannot account for Indigenous and mixed-race authors, or those who may face differential biases due to the ambiguous racialization or ethnicization of their names. We look forward to future work that could help us to better understand how to support equitable practices in science.

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Data availability

Code availability
All analysis code is available at https://github.com/lindenmp/nct_hierarchy
Supplementary Materials for

Asymmetric Signaling Across the Hierarchy of Cytoarchitecture within the Human Connectome

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This PDF file includes:

Figs. S1 to S14
Fig. S1. Brain maps used to define the cortical hierarchy. Brain states for network control theory analysis were define by sampling regions from each of these brain maps. Each brain map is shown for 200 parcels taken from the Schaefer atlas. (A), The sensory-fugal axis of cytoarchitecture. This brain map was used as our primary definition of the cortical hierarchy. (B), The T1w/T2w ratio. Note, this brain map was flipped before creating brain states, such that regions in the sensory and motor cortices were at the bottom of the hierarchy. This was done to standardize our interpretation of bottom-up and top-down with the other two brain maps. (C), The principal gradient of resting-state functional connectivity. This brain map was estimated in our own data using the BrainSpace toolbox.
Fig. S2. Statistical properties of bootstrapped group-averaged connectomes. The group-average connectome used in the main text was re-generated using 1,000 bootstrapped resamples each comprising 50% (n=396) of our 793 participant connectomes. For each bootstrapped group-average connectome, we calculated the mean (A), median (B), standard deviation (C), and sum (D) of the non-zero edge weights. Then, we plotted these distributions of 1,000 bootstrapped statistics alongside the 95% confidence interval (red vertical lines) and the corresponding observed value from the true group-averaged connectome (blue vertical line). In all cases, the 95% CI is narrow, illustrating that subject variability had only a small effect on our group-averaged connectome. This is partly due to the consistency-based thresholding we used that retained only the non-zero edges that were present in at least 60% of participants (see Methods).

Fig. S3. Energy asymmetries are robust to normalization constant, c, and time horizon, T, parameters in network control theory. (A), Mean energy asymmetry ($T_{EA}$) from Fig. 2A in the main text. (B), Hierarchy distance correlation from Fig. 2B in the main text. In both panels, the black box indicates parameters used in main analyses.
Fig. S4. Cumulative transitivity curves for the 32 longest shortest paths in our group-averaged adjacency matrix. Blue curves represent paths traversing source to target (see Fig. 3), while peach curves represent the reverse. Note, here source to target does not imply bottom-up.
**Fig. S5.** Correlations between the sensory-fugal axis and node-averaged communicability. Communicability metrics (top row) and their corresponding deltas (bottom row) were averaged over all nodes along one dimension of $A$, yielding a single estimate per node. These node-averaged metrics were then correlated with the sensory-fugal axis.
Fig. S6. Counterpart to Fig. 2 and Fig. 3 using the T1w/T2w ratio to define brain states instead of the sensory-fugal axis of cytoarchitecture.
A | bottom-up state transitions required lower energy compared to top-down

![Graph showing mean asymmetry and energy distribution](image)

B | cytoarchitectonic divergence correlates with larger energy asymmetries

![Graph showing Spearman's ρ and hierarchy distance correlation](image)

C | energy asymmetries correlate negatively with diffusion efficiency asymmetries

![Graph showing correlation between energy asymmetry and diffusion efficiency asymmetry](image)

D | energy asymmetries correlate positively with search information asymmetries

![Graph showing correlation between energy asymmetry and search information asymmetry](image)

E | energy asymmetries do not correlate with path transitivity asymmetries

![Graph showing correlation between energy asymmetry and path transitivity asymmetry](image)

Fig. S7. Counterpart to Fig. 2 and Fig. 3 using the principal gradient of functional connectivity to define brain states instead of the sensory-fugal axis of cytoarchitecture.
Fig. S8. Energy asymmetries correlate with asymmetries in effective connectivity measured from resting-state functional magnetic resonance imaging. (A), We used resting-state functional magnetic resonance imaging to examine asymmetries in effective connectivity (estimated using dynamic causal modeling) between our cytoarchitectonic brain states (see Methods). (B), Energy asymmetries between brain states correlated positively with asymmetries in effective connectivity between brain states. This result shows that for state transitions where bottom-up transition energy was lower than top-down (negative energy asymmetry) the same was true for effective connectivity and *vice versa*. 
**Fig. S9.** Bottom-up and top-down energy correlate negatively with age. (A), Correlation between age and average top-down energy. (B), Correlation between age and average bottom-up energy. We found that while both bottom-up and top-down energy reduced as a function of age, the age effect for top-down energy was larger than that observed for bottom-up.
Fig. S10. Optimized energy asymmetries improve the out-of-sample prediction of participants’ age. A cross-validated out-of-sample regression model revealed that optimized energy asymmetries (peach) better predicted participants’ age compared to uniform control weights (blue). Out-of-sample prediction was scored by root mean squared error (left), mean absolute error (middle), and the correlation between the true $y$ and predicted $y$ (right). The $p$-values comparing uniform and optimized prediction performance were calculated using an exact test of differences. That is, $p = 0.08$ means that 92% of the values in the optimized performance distribution exceeded their counterparts from the uniform performance distribution.
Fig. S11. Sensitivity analysis, connectome parcellation. In the main text, we reported network control theory results that were modeled on a connectome built from a parcellation with 200 regions. Here, we examined whether our primary findings were robust to our choice of parcellation by reproducing results from Fig. 2 twice, once using a higher resolution version of the same parcellation (Schaefer 400) and once using a parcellation with 360 regions defined according to different criteria (Glasser 360). For both Schaefer 400 and Glasser 360, we observed that bottom-up energy was lower than top-down energy and that hierarchical distance correlated negatively with energy asymmetry. However, compared to the original parcellation (Schaefer 200), we found that all effects were weaker for both Schaefer 400 and Glasser 360, suggesting that our results are somewhat scale/parcellation dependent.
Fig. S12. Sensitivity analysis, connectome sparsity. In the main text, we reported network control theory results derived from a group-averaged connectome that was thresholded to retain edges that were present in at least 60% of participants. This thresholding yielded a connectome with 8% sparsity. Here, we examined whether our primary findings were robust to that choice by reproducing results from Fig. 2 at a range of consistency thresholds (40%, 50%, 70%, and 80%). We observed that our results were highly consistent across this range of thresholds.
Fig. S13. Sensitivity analysis, number of regions per brain state. In the main text, we reported network control theory results for transitions between 20 cytoarchitectonic brain states, each comprising 10 regions. Here, we examined whether our primary findings were robust to that choice by reproducing results from Fig. 2 twice, once incrementing and once decrementing the size of brain states by one region. For both brain states of sizes 9 and 11, we observed that bottom-up energy was lower than top-down energy and that hierarchical distance correlated negatively with energy asymmetry. However, compared to the original state size of 10, we found that all effects were weaker for state sizes 9 and 11, suggesting that our results are somewhat scale dependent.
Fig. S14. Distributions of correlations between subject-specific optimized weights and the sensory-fugal axis of cytoarchitecture. For each subject, optimized control weights were generated for each state transition (see main text) and correlated with the sensory-fugal axis of cytoarchitecture using the same procedure as shown in Fig. 6B. Then, for each subject, correlations were averaged over all state transitions yielding a single correlation per subject; these summary correlations are plotted here including the mean and 95% confidence interval of the distribution.