The evolution of manipulative cheating

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Abstract

A social cheat is typically assumed to be an individual that does not perform a cooperative behaviour, or performs less of it, but can still exploit the cooperative behaviour of others. However, empirical data suggests that cheating can be more subtle, involving evolutionary arms races over the ability to both exploit and resist exploitation. These complications have not been captured by evolutionary theory, which lags behind empirical studies in this area. We bridge this gap with a mixture of game-theoretical models and individual-based simulations, examining what conditions favour more elaborate patterns of cheating. We found that as well as adjusting their own behaviour, individuals can be selected to manipulate the behaviour of others, which we term 'manipulative cheating'. Further, we found that manipulative cheating can lead to dynamic oscillations (arms races), between selfishness, manipulation, and suppression of manipulation. Our results can help explain both variation in the level of cheating, and genetic variation in the extent to which individuals can be exploited by cheats.

Keywords: phenotypic diversity, tragedy of the commons, social evolution, public goods, dynamic oscillation.

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Introduction

Many social interactions involve a trade-off between investing in behaviours or traits that increase the productivity of the group, versus those that increase an individual's share of group productivity (Frank 1998; Bourke 2011; Queller & Strassmann 2018)(Fig. 1a). A female social insect larva could become a queen or a worker (Hamilton 1972). A slime mould cell could become a stalk or a spore within a fruiting body (Strassmann *et al.* 2000). A bacterial cell could invest costly resources into producing some 'public good' that benefits the local group of cells, such as iron scavenging siderophore molecules (Griffin *et al.* 2004).

A standard assumption is that individuals can behave more selfishly by investing less in cooperative behaviours that benefit the group, and by taking a larger share of the available resources (Ghoul *et al.* 2014). For example, a slime mould lineage could 'cheat' by having a larger proportion of its cells develop into spore cells, or a bacterial cell could cheat by producing fewer siderophores (Strassmann *et al.* 2000; Jiricny *et al.* 2010). When cheats can invade, theory predicts that this will lead to either uniform cooperation at a lower level or the coexistence of cheats and cooperators (Queller 1984; Frank 1994, 1998; West & Buckling 2003; MacLean & Gudelj 2006; Ross-Gillespie *et al.* 2007; Gore *et al.* 2009; Frank 2010c; Frank 2010a, b; Patel *et al.* 2019). Coexistence is only expected when some factor leads to the fitness of cheats being higher when they are less common (frequency-dependent selection).

In contrast, the empirical data suggests that there can be more complex forms of cheating and resistance to cheating within social groups. For example, in the slime *Dictyostelium discoideum*: (i) lineages appear to be able to evolve resistance to cheating, where they prevent other lineages from obtaining a higher proportion of spore cells (Buttery *et al.* 2009; Khare *et al.* 2009; Levin *et al.* 2015); (ii) genomic data suggests an ongoing evolutionary arms race, and not just selection towards an optimal level of cooperation (Ostrowski *et al.* 2015; Noh *et al.* 2018; Ostrowski 2019). In some ant species, genetic variation appears to be maintained in the extent to which different patrilines contribute to the production of workers in a colony, a phenomenon termed 'royal cheating' (Hughes *et al.* 2003; Linksvayer 2006; Anderson *et al.* 2008; Hughes & Boomsma 2008; Mitchell *et al.* 2012; Stürup *et al.* 2014). In *Pseudomonas* bacteria, strains appear to vary in both the extent to which they can cheat by exploiting the siderophores produced by other strains and the extent to which they can be cheated by other strains (Kümmerli *et al.* 2009; Bruce *et al.* 2017; Butaitè *et al.* 2017). In all of these cases, cheating appears to involve doing more

68 than just cooperating at a lower level. Other examples of more complex forms of
69 cheating can be found in bacteria, viruses, and replicator RNA (Pollak *et al.* 2016;
70 Furubayashi *et al.* 2020; Bruce *et al.* 2021; Mizuuchi *et al.* 2022).
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Our aim is to explain how these more complex forms of cheating can be
maintained in a population. As mentioned above, most evolutionary models assume
that an individual can control their own investment into selfish and cooperative
behaviours – put simply, an individual cheats by investing less in cooperation (Queller
1984; MacLean & Gudelj 2006; Ross-Gillespie *et al.* 2007; Gore *et al.* 2009; Frank
2010c; Patel *et al.* 2019). We investigate another possibility, that individuals can
manipulate the behaviour of others. For example, an ant patriline may increase the
likelihood that its own larvae are raised as queens, while reducing the likelihood that
the larvae of other patrilines are reared. Or a bacteria cell lineage could increase the
public goods produced by another lineage. Such 'manipulative cheating' could
involve a variety of mechanisms, ranging from coercive communication to more
direct influencing. In addition, we explore how once manipulation has evolved, there
could be selection to evolve resistance or suppression of that cheating.
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We develop a series of models to examine whether manipulative cheating can
be favoured, and if it will lead to variation in the extent to which individuals can
exploit others. We use a mixture of game theory and simulation, to examine
scenarios where resistance can evolve relatively simply, or where there are multiple
mechanisms of manipulative cheating that each require a different form of
resistance. We find that natural selection can maintain a variety of strategies at
equilibrium, as well as the possibility for ongoing oscillating dynamics, such as
evolutionary arms races. While our focus is on 'manipulation', our more general aim
is to investigate scenarios where cheating is more than just 'cooperate less'.
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Modelling overview
Our aim is to investigate the general feasibility of manipulation, in a way that could
be applicable across a range of species, and does not rely on the specifics of any
single species. Consequently, we have chosen a deliberately simple approach to
maintain tractability. We use a combination of modelling approaches to examine the
evolutionary stability and dynamics of manipulative cheating.
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First, we use an equilibrium game theoretical approach to examine under what
conditions manipulative cheating could be favoured. Our model is based on the
classic tragedy of the commons model, where individuals can invest in their own

selfish reproduction, or the productivity of the group (Fig. 1a; appendix 1.2). We
extend this model by assuming that: (i) individuals can invest effort into manipulating
the behaviour of others to make them cooperate at a higher rate (behave less
selfishly; Fig. 1b); and (ii) individuals can also invest effort into suppressing (blocking)
the extent to which they are manipulated by others (Fig. 1c). We then test the
robustness of our game-theoretical results by comparing them with individual-based
simulations.
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Second, we examine the consequence of manipulative cheating when multiple
different mechanisms of manipulation can evolve, which each requires a different
mechanism to suppress. We consider cases where traits are introduced at the same
time point or different time points (mutation) and focus on the temporal trait
dynamics. As multiple mechanisms could generate complications between traits
which cannot be easily presented by equilibrium analysis, we focus on dynamic
results from individual-based simulations.
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Our general aim is to investigate scenarios where cheating can be more than
just 'cooperate less'. We do this by developing models focused on the special case of
manipulation and its suppression. Other possibilities would include developing
coevolutionary genetic models to look at genotype-specific cheating-resistance,
analogous to gene-for-gene or matching alleles models of host-parasite coevolution,
or to model a different form of coercion (Sasaki 2000; Agrawal & Lively 2002).
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Manipulative cheating and its suppression
Model design
We assume a haploid population inhabiting an infinite number of identical habitat
patches, where each patch supports a single social group and lets social interactions
take place. We also assume the fitness of each individual is proportional to the
productivity of the social group multiplied by the individual's share of group
productivity, and all offspring compete globally for patches in the next generation.
Within each social group, each individual divides its effort into cooperation with
group members, which aids group productivity or selfishly reproducing (gaining a
greater share of the group productivity). We consider three coevolving traits:
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(a) Selfishness (z)   (b) Manipulative cheating (x)   (c) Suppression of manipulation (u)

Cooperation

Selfishness

Manipulation

Suppression

Figure 1. Schematic view of the three evolving traits in our model. Each individual (indexed by i) can put effort into three actions: (a) invest resources into reproduction (z_i) or group productivity (average cooperation; $1 - \bar{z}$); (b) manipulate others (x_i; represented by the grid texture), to make them invest more into group productivity; and (c) suppress (block) the manipulation from others (u_i; represented by horizontal dashed texture).

Selfishness (z): We assume that when individuals put more effort into reproduction (z), they: (i) obtain a larger share of the group productivity; (ii) put less effort into cooperation, which reduces group productivity. Specifically, if a focal individual i invests z_i, into reproduction, and the group average of all individuals in the group is $\bar{z}$ ($0 < z < 1$). In other words, the parameter z measures the level of 'selfishness' (Fig. 1a)(Frank 1994, 1996, 1998; Dionisio & Gordo 2006; Frank 2010a, b).

Manipulative cheating (x): We assume that a focal individual can invest x in manipulation, which causes other individuals to invest fewer resources into their own reproduction, and instead invest those resources into the reproduction of the focal individual (manipulator; $0 < x < 1$; Fig. 1b). This manipulation requires effort and so reduces the resources that the manipulator contributes to group productivity (by $\bar{x}$). Manipulation x therefore takes reproduction from others, whereas selfishness z shifts an individual's allocation between cooperation and reproduction. Consequently, manipulation is redistributing the share of all individual's reproduction while z is changing the effort spent in reproduction. For simplicity, we have assumed there is no 'loss' in reproductive effort during the process of manipulation, but we found similar results when manipulation also leads to a personal reproduction cost (appendix 3).

Suppression of manipulative cheating (u): We add the possibility for individuals to suppress (block) manipulation ($0 < u < 1$; Fig. 1c). When suppression exists, a manipulator can only take a proportion $1 - u^b$ of reproduction, where *b* is a shape parameter (see below). Like the other two traits, suppression takes effort and reduces the effort put into group productivity (by $\bar{u}$).

174   Combining the effects of all three traits lead to:

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$$w_i = \frac{z_i + \left(1 - u_{-i}^b\right)x_i^a z_{-i} - \left(1 - u_i^b\right)x_{-i}^a z_i}{\bar{z}}(1 - \bar{z} - \bar{x} - \bar{u}),$$

177   (1)

where z_i is the selfishness of the focal individual, $\left(1 - u_{-i}^b\right)x_i^a z_{-i}$ is the gain from

manipulating others, $\left(1 - u_i^b\right)x_{-i}^a z_i$ is the loss from being manipulated, and $1 -$

$\bar{z} - \bar{x} - \bar{u}$ is the group productivity. Because the sum of gain and loss across all

individuals in the group is zero, the average effort in reproduction is just $\bar{z}$. Thus, the

first term is the relative share of group productivity of the focal individual (i.e.,

$\frac{z_i + \left(1 - u_{-i}^b\right)x_i^a z_{-i} - \left(1 - u_i^b\right)x_{-i}^a z_i}{\bar{z}}$). We provide a more detailed derivation of equation 1 in

appendix 1.1. In the special case of no manipulation or suppression, equation 1

simplifies to the classic tragedy of the commons model (Frank 1994, 1996, 1998;

Dionisio & Gordo 2006; Frank 2010a, b).

We allow the effects of manipulation and suppression to be nonlinear by the

shape parameters, a and b. Nonlinearities can arise for a number of reasons, such

as mechanisms of molecular diffusion, or interference between the behaviour of

different individuals (Müller *et al.* 2006; Wiley 2013; Rogers *et al.* 2017). The

parameter a determines whether the benefit from increased investment into

manipulation is decelerating ($a < 1$), linear ($a = 1$) or accelerating ($a > 1$). Similarly,

the shape parameter b determines the shape of the benefit of increased

investment into suppression. We have focused on the decelerating forms because

this will often be the case for biological traits (appendix 5.1).

We find it useful to think about manipulation, suppression, and equation 1 with

a lottery-ticket metaphor. Imagine reproduction as the buying of a lottery ticket –

producing an offspring, that has some chance of 'winning' (reproducing) in the next

generation. Individuals can either invest resources into buying the lottery tickets

produced by the group (z; selfish), or invest resources into helping the group

produce more lottery tickets ($1 - z$; cooperation). Each group produces its own

lottery tickets and more tickets means a higher chance for the focal group to win.

Being more selfish (higher z) means obtaining a larger fraction of the lottery tickets

produced by the group, but also putting fewer resources into producing tickets (and

so the group procures fewer tickets). In contrast, manipulation (higher x) allows

individuals to steal lottery tickets from others within their group. Suppression would

involve blocking lottery tickets from being stolen. We consider biological examples of

manipulation and suppression in the discussion section.

Model analysis

We seek the evolutionarily stable strategy (ESS), which is the individual strategy that

cannot be invaded by any other rare strategy. Using the neighbour-modulated fitness

approach of Taylor & Frank (1996), we find:

$$
\begin{cases}
\Delta W_z = \left(\bar{R}_{-i} \dfrac{-(\frac{n-1}{n}-x^a(1-u^b))}{z} + \dfrac{\frac{n-1}{n}-x^a(1-u^b)}{z} \right)(1-z-x-u) - \bar{R} \\
\Delta W_x = (\bar{R}_{-i}(-ax^{a-1})(1-u^b) + ax^{a-1}(1-u^b))(1-z-x-u) - \bar{R} \\
\quad\quad \Delta W_u = (\bar{R}_{-i}(-x^a)bu^{b-1} + x^a bu^{b-1})(1-z-x-u) - \bar{R}
\end{cases}
$$

(2)

where traits are analysed one at a time, where ΔW_z means the change in fitness

due to a slight increase in selfishness in the focal individual, and analogous for ΔW_x

and ΔW_u. In addition, $\bar{R}_{-i}$ denotes the relatedness of focal individual to all other

group members, $\bar{R}$ indicate the whole-group relatedness (Pepper 2000)(appendix

1.2). The two relatedness terms can be linked— for example, if the group size is n,

then $\bar{R} = 1/n + ((n-1)/n)\,\bar{R}_{-i}$. For simplicity, we assume all traits only operate

within the group so that $\bar{R}_{-i}$ does not differ between traits. More general form

allowing for cases when different traits are at different social scales is considered in

the derivation in appendix 1. We also assume each trait evolves independently and

there is no allele-level interaction between each trait.

Each of the three equations in (2) represents the change to the inclusive fitness

of an individual that occurs when the individual increases the level at which it

expresses the focal trait (Hamilton 1964a, b). Because all three expressions share

similar structure, we can simplify them into

$\Delta W_{trait} = (\bar{R}_{-i}(-A) + A)(1-z-x-u) - \bar{R},$

(3)

where A is different for each trait and subscript 'trait' means the type of trait we

are analysing, which could be z, x, or u. The first term on the right, $-A$,

represents the relatedness-weighted reduction in neighbours' share of group

productivity due to an individual's selfishness or manipulation (an inclusive-fitness

cost; e.g., $\dfrac{-(\frac{n-1}{n}-x^a(1-u^b))}{z}$ for selfishness). The second term, A, represents the

increase in personal share of group productivity made by a selfish or manipulative

individual (an inclusive-fitness benefit; $\dfrac{\frac{n-1}{n}-x^a(1-u^b)}{z}$ for selfishness). The third

term, group productivity, represents a relatedness-weighted reduction in fitness of

the average group member, self-included, owing to selfishness, manipulation, or

suppression (i.e., $1 - z - x - u$). The cost in group productivity is spread equally

among all individuals in the group, including the actor. The last term, $\bar{R}$, represents

the indirect cost of reducing the share of group productivity obtained by relatives.

Expression 2 could not be solved analytically, and so we found solutions with an

iterative numerical method (Fig. 2; appendix 6.2). We tested the robustness of our

solutions with an individual-based simulation, which includes mutation and drift. Our

simulations and numerical predictions arising showed close agreement (Fig. 2;

appendix 7).

Figure 2. Selfishness, manipulation, and suppression of manipulation. The panels show the ESS
predictions and simulation results for our three-trait model. The solid lines show the ESS
predictions, and the dots show the results of our individual-based simulations ($a = b = 0.5$).
The black segments within each dot show the standard deviation of trait values of the last 10%
duration of 10 repeated simulations (appendix 7).

We found that the ESS selfishness, manipulation, and suppression are all

predicted to show negative relationships with relatedness (Fig. 2). At a lower

relatedness, individuals are predicted to: (i) selfishly keep a higher fraction of their

resources for themselves (as predicted by the classic tragedy of the commons

model); (ii) invest more heavily in manipulating others to help them (as also

predicted in a model without suppression; appendix 2); (iii) invest more heavily in

suppressing manipulation perpetrated by others (when manipulation is at higher

levels). These predictions qualitatively hold for a broad range of parameter space,

with linear or non-linear returns on increased investment in manipulation and

suppression, and show that manipulative cheating as well as its suppression can be
favoured by natural selection.
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The quantitative ESS predictions depend upon the shape parameters (Fig. 3).
When the shape parameter of manipulation, a, is more decelerating, selfishness
becomes lower, suppression becomes higher, and manipulation becomes higher until
suppression evolved (Fig. 3a-c). When the shape parameter of suppression, b, is
more decelerating, selfishness becomes higher, manipulation becomes lower, and
suppression becomes higher until there is no manipulation to suppress (Fig. 3g-i).
Lastly, when the two shape parameters covary together, the impact on ESS trait
values is a combination of the two forementioned effects (Fig. 3d-f). Both
manipulation and suppression can be favoured across a wide range of parameter
values.
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Figure 3. Nonlinear returns of manipulative cheating and its suppression. Panels (a), (b), and
(c) show the predicted ESS level of selfishness (z^*), manipulation (x^*), and suppression (u^*)
respectively, for different values of relatedness (R, x-axis). From top to bottom, each row of

panels presents varying different parameters on y-axis: the shape parameter for manipulative
cheating (a-c; a), both parameters (d-f; a and b), and the shape parameter for suppression
(g-i; b). The black triangle indicates the horizontal row where the parameter settings are
identical to each other and to Fig. 2. We have focused on decelerating function for shape
parameters because it resembles the nature of communication (appendix 6.1).
295

Multiple mechanisms for manipulative cheating and suppressing

In our above model, we have focused on evolutionary equilibrium, assuming there is

only a single mechanism to manipulate others. In nature, manipulation could take

many forms, and each requires a different form of suppression. This could lead to

complicated dynamics, such as a genetic arms race, where different forms of

manipulation arise and are then suppressed over time. Because the rise and fall of

trait values are potentially transient, we move away from game-theoretical analysis

and focus on non-equilibrium scenarios through individual-based simulations. We

present two different cases here: one with multiple mechanisms where all are

introduced at the same time, and the other with multiple mechanisms where new

mechanisms are introduced to the population at different time points (via mutation).

Assuming there are k mechanisms to manipulate and suppress, fitness is given

by

$$w_i = \left(z_i + \left(1 - u_{1,-i}^b\right)z_{-i}x_{1,i}^a - \left(1 - u_{1,i}^b\right)z_i x_{1,-i}^a + \left(1 - u_{2,-i}^b\right)z_{-i}x_{2,i}^a -$$

$$\left(1 - u_{2i}^b\right)z_i x_{2,-i}^a + \cdots + \left(1 - u_{k,-i}^b\right)z_{-i}x_{k,i}^a - \left(1 - u_{k,i}^b\right)z_i x_{k,-i}^a\right)\bar{z}^{-1}\left(1 - \bar{z} - \right.$$

$$\left. \bar{x}_1 - \bar{u}_1 - \bar{x}_2 - \bar{u}_2 - \cdots - \bar{x}_k - \bar{u}_k\right).$$

314   (4)

where $x_1, x_2, \ldots, x_n$ denote the n mechanisms of manipulation and $u_1, u_2, \ldots, u_n$

represent suppression. Additional terms of gain and loss from manipulation and

being manipulated are added to the first parenthesis, and group productivity can

potentially be decreased by all of the $2k + 1$ traits.

We first examine this potentially non-equilibrium scenario by assuming all

mechanisms are present from the beginning and consider the simplest case of two

mechanisms ($k = 2$). By simulating various combinations of shape parameters and

relatedness, we found that levels of selfishness and manipulation do not always tend

to a single equilibrium. Instead, they can oscillate in a periodic style (Fig. 4a). Though

the oscillation in suppression is less profound, it also fluctuates in a smaller

amplitude in response to the changes in levels of manipulation. We used harmonic

regression to test for periodic oscillations, as opposed to random noise (Fig. 4b and

appendix 4.2).

We found oscillations occur when relatedness is relatively low ($R < 1/6$) and

when shape parameters are intermediate decelerating ($0.6 < a, b < 0.85$). In these

intermediate settings, the optimal levels of manipulation and selfishness are similar,

which could lead to a similar pay-off between investing in them. Thus, any small

perturbation in trait values could disturb the dynamics and generate oscillation. In

support of the hypothesis that oscillation is a consequence of interactions between

selfishness and manipulation, we found that oscillation can be prevented when

selfishness cannot mutate (appendix 4.3) or when there is no linkage between traits

(appendix 4.4). We also found that oscillations can occur when there are more than

two mechanisms to manipulate and supress (appendix 4.5), becomes slower when

mutation rate is smaller (appendix 4.6), and less likely when there is a personal

reproduction cost to manipulation and suppression (appendix 4.7).

Figure 4. Selfishness and manipulative cheating traits can oscillate when there are two
mechanisms for manipulation and suppression. (a) An example of oscillating dynamics when
shape parameters are intermediate, and relatedness is relatively low ($R = 1/8$; $a = b = 0.7$).
Broader analysis and more details are provided in appendix 4. (b) The estimated amplitude of
the time series of selfishness by harmonic regression. Harmonic regression is an analysis of
time series to show the significance of periodic oscillation, where low period means frequent
recurrent pattern, and high period means recurrence ager a long span. Here, 10 repeated
simulations were used and only the last 75% of the 3000 generations was analysed, after
selfishness is roughly stabilised. The analysis shows maximal amplitude is found at period of
815 generations with p-value of 1.8035×10^{-5}. Mean estimation is shown in black curve whereas
the 95% confidence interval is illustrated as the grey area (F-test; $\mu \pm 2\sigma$).

We now consider a slightly different scenario. In the above analysis, we

assumed that all manipulation and suppression mechanisms were available at the

start of the simulation. An alternative possibility is that different mechanisms can

arise over time, by mutation. When a manipulation trait arises, it could be selected

for. Furthermore, once a form of manipulation becomes sufficiently common, then a

mutation that allows suppression of that manipulation could be selected for. These

different forms of manipulation could involve very different traits, or new forms of an

old trait, that would require a different suppression mechanism. This scenario could
potentially lead to an evolutionary arms race where new forms of manipulation
evolve and are then suppressed. We modelled this scenario by introducing mutations
for new manipulative traits at random time points, and then mutations for the
suppression of manipulation 400 generations afterwards for illustrative purpose.
367

We found that this scenario also leads to a form of arms race (Fig. 5). When a
new form of manipulation arises, it initially spreads. This spread of manipulation
favours lower levels of selfishness, because the manipulation reduces the benefit of
selfishly investing in reproduction. In addition, once a manipulation is common, any
mutation that allows suppression of that manipulation will be favoured, and hence
increase in frequency. As suppression spreads, this selects for reduced investment in
manipulation (which would just be blocked), and hence also increased selfish
investment in reproduction (which won't be manipulated anymore) (Fig. 5). Overall,
this leads to a pattern of recurring dynamics whenever a new manipulative trait
arises, and where individuals can show variable levels of selfishness, manipulation
and suppression. For illustrative purposes, our example in Figure 5 shows the gradual
evolution of 10 different manipulation mechanisms and focuses on the parameter
space where suppression can almost completely block manipulation in a very
effective way ($a = 0.5, b = 0.01$)(Scott & West 2019). We examine other scenarios in
appendix 5 (Fig. A13 & A14).
383

Altogether, our results from the multiple mechanisms of manipulation suggest
that: (i) multiple types of manipulation can arise and / or be maintained in a
population; (ii) the manipulation traits and their suppression can sometimes show
oscillating dynamics, where the levels of selfishness, manipulation, and/ or
suppression oscillate. The oscillation originates either from interactions between
coevolving traits (endogenous; Fig 4) or from the introduction of new mechanisms
(exogenous; Fig. 5). These results provide possible explanations for cases where
there appears to be genetic variation for the extent or form of cheating and / or
cheating suppression.
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Figure 5. Time series of trait dynamics of the simulations when new mechanisms for manipulation and suppression are introduced at different time points. Selfishness is shown in the upper panel, the ten manipulative traits are shown in the middle panel, and the ten suppressive traits are shown in the bottom panel. The y-axis is scaled differently across the panels, to match the levels of variation. Each manipulative and suppressive trait are mutated to non-zero values in arbitrary time points for better visualisation. The shape parameters are set to $a = 0.5$ for manipulation and $b = 0.01$ for suppression, and the relatedness is $R = 1/3$. All data are from a single representative simulation.

Discussion

We found that: (1) manipulative cheating can be favoured across a wide variety of

conditions; (2) manipulation is more likely to be favoured when relatedness is

relatively low; (3) suppression of manipulation can also be favoured. In addition,

when we allowed for multiple mechanisms (types) of manipulation, we found that
non-equilibrium dynamics could occur, such as oscillations. Oscillations could be
generated in either (i) a coevolutionary interaction between selfishness and
manipulation; or (ii) a genetic arms race between different forms of manipulative
cheating and their specific suppressors. These non-equilibrium dynamics could help
explain the genetic diversity that has been observed for both cheating and the
response to cheating across the biological world (Hughes *et al.* 2003; Linksvayer
2006; Anderson *et al.* 2008; Hughes & Boomsma 2008; Buttery *et al.* 2009; Khare *et*
al. 2009; Kümmerli *et al.* 2009; Mitchell *et al.* 2012; Stürup *et al.* 2014; Levin *et al.*
2015; Ostrowski *et al.* 2015; Pollak *et al.* 2016; Bruce *et al.* 2017; Butaitė *et al.* 2017;
Noh *et al.* 2018; Ostrowski 2019; Furubayashi *et al.* 2020; Bruce *et al.* 2021; Mizuuchi
et al. 2022).

Our general aim was to investigate scenarios where cheating is characterised by
more than just 'cooperate less'. We did this by developing a theoretical model where
individuals could manipulate others, to make them cooperate more. There is a range
of other possibilities for more complex forms of cheating, such as obtaining a
disproportionate share of some public good, where we suggest that a similar logic
would apply (i.e., the evolution of 'more efficient' cheating). A key distinction here is
that we are not modelling some evolutionarily stable signalling system which
benefits the signaller and receiver (Maynard Smith & Harper 2003). We have instead
modelled coercion, which provides no benefit to the recipient of that coercion.
Consequently, the response would be to evolve to suppress or ignore that coercion,
rather than evolve to some evolutionarily stable mutually beneficial response.

Manipulative cheating could take many different forms in different species. In
bacteria and other microorganisms, individuals could produce coercive molecules
that make other cells invest more into the production of public goods, and invest less
into reproduction. In species that form fruiting bodies, manipulation could cause the
cells of other lineages to be more likely to become stalk cells (Buttery *et al.* 2009;
Khare *et al.* 2009; Levin *et al.* 2015). In organisms such as social insects, the method
of manipulation would depend upon how caste is determined (Schwander *et al.*
2010). In species where workers control the caste of offspring, manipulation could
cause workers from other lineages (different queens or patrilines) to be less likely to
rear their own offspring as reproductive, and be more likely to rear the offspring of
the manipulating lineage as reproductive (Hamilton 1972). In species where larvae
control their own caste, manipulation could decrease the likelihood that other
individuals develop as reproductive (Wenseleers & Ratnieks 2004). Alternatively,

manipulation could occur through more direct approaches, such as selectively killing the eggs from other lineages. These mechanisms all share the same concept that the 'more manipulative' lineage gains a greater share of group productivity.

Similarly, suppression could involve a variety of different mechanisms, from evolving to ignore coercion, to blocking behaviours that steal resources or kill individuals, to making fewer public goods. Experiments on slime moulds have found that strains can evolve to become more resistant to cheats (Levin *et al.* 2015). Bacteria appear to be able to produce more specific and less exploitable public goods (Kümmerli *et al.* 2009; Bruce *et al.* 2017; Butaitė *et al.* 2017). Different lineages of cooperative RNA replicators can survive better against different cheating replicators (Mizuuchi *et al.* 2022). These cases share the same concept that cooperators can somewhat defend against or suppress the cheats. Other possible mechanisms are discussed elsewhere, for bacteria and viruses.

Previous theoretical work has focused on conflict suppression and hence how the tragedy of the commons could be avoided (Frank 1995; West *et al.* 2002; Frank 2003; Wenseleers *et al.* 2003; Wenseleers *et al.* 2004; Ratnieks *et al.* 2006). In these previous papers, selfishness could be selected against, by mechanisms such as policing, sanctions, and social reputation (Frank 1995; Milinski *et al.* 2002; Dionisio & Gordo 2006, 2007; El Mouden *et al.* 2010). In contrast, we have examined a different route to increased selfish behaviour – the manipulation of others via manipulative cheating. Furthermore, we have shown that if there are multiple manipulation traits, then genotypic diversity can be maintained for selfishness, manipulative cheating, and/or its suppression. This diversity result links to previous work on quorum sensing in bacteria, which has shown how cycles of 'cheating' and 'cheating immunity' can arise (Eldar 2011; Pollak *et al.* 2016). More generally, manipulation and counteradaptations to prevent elimination can arise in many forms of communication (Dawkins *et al.* 1979; Maynard Smith & Harper 2003).

To conclude, we have shown how cheating can take more complex forms than just lower levels of cooperation. We have shown that individuals can also be selected to manipulate the behaviour of others, for their own selfish gain. Furthermore, this can lead to evolutionary arms races between attempts to manipulate and to suppress that manipulation. A major task for the future is to determine the extent to which more complex forms of cheating occur in the natural world (Pollak *et al.* 2016; Meir *et al.* 2020; Leeks *et al.* 2021). In many cases, this would require elucidation of the underlying mechanisms, which could be completely different across different

484   species. The potential for manipulation and its suppression could arise at all levels of
485   life, from RNA replicators to complex animal societies.
486

487   **Code and data availability**
488   All results are generated using C and Python. The codes and data used for this study
489   are available at: https://github.com/mingpapilio/Codes_Manipulative_Cheat
490

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Appendix

Our appendix contains seven sections. In section 1, we formally analyse our model with single mechanisms to manipulate and suppress manipulation. Section 2 contains the non-suppression model, which is a reduced model without suppressive traits. This model bridges the gap between the single-mechanism model and the classic tragedy of the commons (Frank 1994, 1996; Taylor & Frank 1996; Frank 1998; Dionisio & Gordo 2006; Frank 2010a, b). Further, the non-suppression model also illustrates a biologically possible case where manipulation cannot be suppressed. We consider the effects of personal cost in manipulation and suppression in section 3. Section 4 provides additional analyses for the scenario with two mechanisms to manipulate and suppress, where we found oscillations in selfishness and manipulation (Fig. 4). We examine the origin of the oscillation dynamics and compare the results with game-theoretical analysis. We subsequently present similar arms race dynamics in section 5 for the scenario with multiple mechanisms introduced at different time points (Fig. 5), with different biological settings assumed in each case. In section 6, we discuss some modelling details and justification. Lastly, section 7 has the details for the individual-based simulations.

1. Formal analysis of the scenario with a single mechanism to manipulate and
   suppress manipulation

1.1 Derivation of the fitness equation

We track a population of haploid asexual individuals by observing it at discrete points spaced evenly in time. The model population itself is subdivided into groups of size n. Groups are re-constituted at the very end of a given time step, through among group competition. Individuals compete within their own group for their share of the group's productivity.

We use y_i to denote the (absolute) competitive effort realised by focal individual i. We build up the fitness expression by assuming that the focal individual initially commits to a within-group level of competition equal to z_i. Likewise, each non-focal individual $k \neq i$ commits to a within-group level of competitive effort equal to z_k.

Once each group member has committed to an initial level of competitive effort, the group enters a phase in which members can manipulate effort (i.e., investment) from one another. We model the manipulation phase by assuming that the focal group member is assigned a non-self partner, uniformly at random with replacement. The assumption is equivalent to letting the focal individual manipulate

every neighbour to the same degree and we use a probabilistic sampling narrative

for the ease of explaining each process (Wild 2011). When manipulation takes place,

the focal individual attempts to manipulate a fraction x_i^a of the competitive effort

z_k committed to by the partner. Here, we are treating x_i as a new trait (i.e., effort

devoted to manipulation), and a as a constant that modulates the efficacy of the

trait (i.e., determines how effective the effort is). The partner individual can also

suppress manipulation. Specifically, we assume that the partner individual prevents a

fraction $(1 - u_k^b)$ of manipulation that would have otherwise occurred. Here, we are

thinking of u_k as a trait, and b as a constant that modulates the efficacy of the

trait.

The focal individual is not only a manipulator, it can also be a the target of

manipulation. In keeping with the description above, the focal individual is chosen to

be manipulated by each of its non-self neighbours with probability $1/(n-1)$. When

chosen, the focal individual loses $x_k^a(1 - u_i^b)$ of the competitive effort z_i

committed to by itself.

Putting the details together, we arrive at the following expression for the

competitive effort realised by focal individual i:

$$y_i = z_i + x_i^a \frac{1}{n-1}\sum_{k \neq i}(1 - u_k^b)z_k - (1 - u_i^b)z_i \frac{1}{n-1}\sum_{k \neq i}x_k$$

$$= z_i + x_i^a(1 - \bar{u}_{-i}^b)\bar{z}_{-i} - \bar{x}_{-i}(1 - u_i^b)z_i$$

731   (A1)

where a bar paired with a $-i$ subscript denotes the arithmetic mean of non-focal

individuals in the focal group. It is important to note that the share of group

productivity of the average non-focal individual can be expressed as

$$\bar{y}_{-i} = \frac{1}{n-1}\sum_{k \neq i}\left(z_k + x_k^a \frac{1}{n-1}(1 - u_i^b)z_i - \frac{1}{n-1}x_i^a(1 - u_k^b)z_k + \right.$$

$$\left. x_k^a \frac{1}{n-1}\sum_{j \neq i,k}(1 - u_j^b)z_j - \frac{1}{n-1}(1 - u_k^b)z_k \sum_{j \neq i,k}x_j^a\right)$$

$$= \bar{z}_{-i} + \frac{1}{n-1}\bar{x}_{-i}(1 - u_i^b)z_i - \frac{1}{n-1}x_i^a(1 - \bar{u}_{-i}^b)\bar{z}_{-i} + \frac{1}{(n-1)^2}\left(\sum_{k \neq i}\sum_{j \neq i,k}x_k^a(1 - \right.$$

$$\left. u_j^b)z_j - \sum_{k \neq i}\sum_{j \neq i,k}x_j^a(1 - u_k^b)z_k\right)$$

740   (A2)

Further simplification can be achieved by recognising that the term contained in

parenthesis immediately above is zero. To see this let $\delta_{kj} = \delta_{jk}$ take a value of 1 if

$k = j$ and a value of 0 otherwise. Then,

$\left(\sum_{k\neq i,}\sum_{j\neq i,k} x_k^a\left(1 - u_j^b\right)z_j - \sum_{k\neq i,}\sum_{j\neq i,k}\left(1 - u_k^b\right)z_k x_j^a\right) = \left(\sum_{k,j\neq i} x_k^a\left(1 - \right.\right.$

$\left.\left. u_j^b\right)z_j\left(1 - \delta_{kj}\right) - \sum_{k,j\neq i} x_j^a\left(1 - u_k^b\right)z_k\left(1 - \delta_{jk}\right)\right) = 0.$

(A3)

In words, the term in question simplifies to zero because the double sums both

represent the total sum of all entries of the same $(n - 1) \times (n - 1)$ matrix.

Therefore, the average competitive effort in the focal group is:

$\bar{y} = \frac{1}{n}y_i + \frac{n-1}{n}\bar{y}_{-i}$

$= \frac{1}{n}z_i + \frac{n-1}{n}\bar{z}_{-i} + \frac{1}{n}x_i^a(1 - \bar{u}_{-i}^b)\bar{z}_{-i} - \frac{n-1}{n}\frac{1}{n-1}x_i^a(1 - \bar{u}_{-i}^b)\bar{z}_{-i} -$

$\frac{1}{n}\bar{x}_{-i}\left(1 - u_i^b\right)z_i + \frac{n-1}{n}\frac{1}{n-1}\bar{x}_{-i}\left(1 - u_i^b\right)z_i$

$= \bar{z}$

(A4)

Where bars with no subscript denote an arithmetic mean taken over the entire group

of n individuals. The average competitive effort in the group is not changed by the

manipulation phase. Manipulation only serves to redistribute the initial commitment

to competitive effort within a given group. It follows that the relative share of group

productivity of the focal individual can be expressed as $y_i/\bar{z}$.

We next assume, for simplicity, that all traits impose a cost on group performance at

the same rate, and we propose that group productivity is proportional to $1 - \bar{z} -$

$\bar{x} - \bar{u}$. Thus, we express fitness of the focal individual as

$w_i = \frac{y_i}{\bar{z}}(1 - \bar{z} - \bar{x} - \bar{u}).$

(A5)

Technically, w_i in the previous line is more accurately described as an inclusive-

fitness-generating function, because differentiating it following the steps outline in

(Taylor & Frank 1996) will lead to the correct generalisation of Hamilton's rule

(Hamilton 1964a, b).

1.2 Kin selection analysis

Following Taylor& Frank (1996), we assume that traits z, x, and u are controlled by

a separate locus. We use, g_z, g_x, and g_u, respectively, to denote the genotypic

value of the focal individual at the z, x, and u loci.

To capture the effect of competition on an individual's inclusive fitness we treat

the traits z_i, $\bar{z}_{-i}$, and $\bar{z}$ as a function of g_z. We then differentiate w_i with respect

to g_z and evaluate the result at a point where all individuals in the population have

the same genotypic value at every locus. Evaluating at such a point allows us to

assert that $z_i = \bar{z}_{-i} = \bar{z} = z$, $x_i = \bar{x}_{-i} = \bar{x} = x$, and $u_i = \bar{u}_{-i} = \bar{u} = u$. It also

justifies us replacing dz_i/dg_z with relatedness between the focal individual and

itself (= 1), replacing $d\bar{z}_{-i}/dg_z$ with relatedness between the focal individual and

its average non-self group mate (= $\bar{R}_{-i,z}$, where the subscript reminds us that

relatedness is assessed at the z locus), and replacing $d\bar{z}/dg_z$ with relatedness

between the focal individual and the average member of its group, self-included (=

$\bar{R}_z$). Following through this entire multi-step procedure, we arrive at

791
$$\Delta W_z = \left(\bar{R}_{-i,z} \frac{-\left(\frac{n-1}{n} - x^a\left(1-u^b\right)\right)}{z} + \frac{\frac{n-1}{n} - x^a\left(1-u^b\right)}{z} \right)(1 - z - x - u) - \bar{R}_z$$

792   (A6)

793   as the inclusive fitness effect of a small increase in selfishness, z. When ΔW_z is

794   zero, z is at equilibrium with respect to the action of selection (ESS).

796   Treating traits x_i, $\bar{x}_{-i}$, and $\bar{x}$ as a function of g_x we can go through

797   analogous steps to obtain

799
$$\Delta W_x = (\bar{R}_{-i,x}(-ax^{a-1})(1 - u^b) + ax^{a-1}(1 - u^b))(1 - z - x - u) - \bar{R}_x$$

800   (A7)

801   where the subscript reminds us that relatedness is now assessed at the x locus.

802   Treating traits u_i, $\bar{u}_{-i}$, and $\bar{u}$ as a function of g_u, we get

804
$$\Delta W_u = (\bar{R}_{-i,u}(-x^a)bu^{b-1} + x^a bu^{b-1})(1 - z - x - u) - \bar{R}_u$$

805   (A8)

as the inclusive fitness effect of suppression, where relatedness is assessed at the u

locus.

2. The non-suppression model: model with only selfishness and one mechanism for

manipulation

We assume suppression is absent in this model, but manipulation can occur.

Consequently, this gives:

$$w_i = \frac{z_i + z_{-i}x_i^a - z_i x_{-i}^a}{\bar{z}}(1 - \bar{z} - \bar{x}),$$

815
<div align="right">(A9)</div>

where x_i is the level of manipulative cheating of the focal individual, z_{-i} is the

average level of selfishness (excluding the focal individual), a is the shape

parameter for manipulative cheating, and $1 - \bar{z} - \bar{x}$ is the group's productivity. As

above, the parameter a determines whether the benefit from increased investment

into manipulation is decelerating ($a < 1$), linear ($a = 1$) or accelerating ($a > 1$).

To facilitate comparison with previous work, the relations between the classic

tragedy of the commons, the non-suppression model, and the model with

suppression are illustrated in Fig. A1. The first model is the classic tragedy of the

commons model, which predicts a single optimal level of investment into

cooperation / selfish reproduction (Fig. A1a)(Frank 2010a). The next model is the

non-suppression model, which allows for manipulative cheating, where individuals

increase their own investment into reproduction, by reducing that of others (Fig.

A1b). Lastly, in the model with suppression, we allow suppression as a defensive

mechanism against manipulative cheating (Fig. A1c).

$$w_i = \frac{z_i + z_{-i}x_i^a - z_i x_{-i}^a}{\bar{z}}(1 - \bar{z} - \bar{x}),$$

(a) Classic tragedy of the commons

(b) The non-suppression model: tragedy+ manipulation

(c) The model with suppression (main model): tragedy+ manipulation+ suppression

	Classic tragedy of the commons	Non-suppression model	The model with suppression
Group productivity	$1 - \bar{z}$	$1 - \bar{z} - \bar{x}$	$1 - \bar{z} - \bar{x} - \bar{u}$
Individual share of group productivity	$\dfrac{z_i}{\bar{z}}$	$\dfrac{z_i + x_i^a z_{-i} - x_{-i}^a z_i}{\bar{z}}$	$\dfrac{(z_i + (1-u_{-i}^b)x_i^a z_{-i} - (1-u_i^b)x_{-i}^a z_i)}{\bar{z}}$

Figure A1. Comparison between the classic tragedy of the commons, the non-suppression model, and the model with suppression. Here, we illustrate three models with gradually increasing complexity. (a) In the classic tragedy of the commons, individuals can choose to invest resources into reproduction (z_i) or group productivity (cooperation; $1 - \bar{z}$). (b) In the non-suppression model, individuals can also manipulate others (x_i), to make them invest more in group productivity. (c) In the model with suppression, individuals can also suppress (block) the manipulation by others (u_i). Within each model, arrows indicate manipulation, the blockings indicate suppression, and the outcome of the two actions are expressed below the arrows. The fitness of an individual is divided into two components: group productivity and share of group productivity, both shown at the bottom of the figure.

We find the change of inclusive fitness effect for selfishness, and manipulation:

$$\begin{cases} \Delta W_z = \left(\bar{R}_{-i,z} \dfrac{-(\frac{n-1}{n} - x^a)}{z} + \dfrac{\frac{n-1}{n} - x^a}{z} \right)(1 - z - x - u) - \bar{R}_z \\ \Delta W_x = (\bar{R}_{-i,x}(-ax^{a-1}) + ax^{a-1})(1 - z - x - u) - \bar{R}_x \end{cases}.$$

(A10)

Expression A10 could not be solved analytically, and so we found solutions with an iterative numerical analysis. We also tested the predictions of our analytical model with an individual-based simulation, which showed close agreement (Fig. A2b).

The non-suppression model predicts that manipulation can be favoured, and
that greater levels of manipulation will be favoured when relatedness is lower (Fig.
A2b). This prediction arises because there is an indirect fitness cost to manipulating
relatives and reducing group productivity. Further, since a function with smaller
shape parameter means the manipulative effective is higher for a given trait value, as
shown in the three panels on the left of Fig. A2, we find greater intermediate values
of manipulation when the shape is more decelerating (smaller a have more shaded
area, Fig. A3b).

This model also predicts a very different relationship between selfishness and
relatedness, compared with the classic tragedy of the commons model and the
model with suppression (compare Fig. A2b with other panels). Specifically, rather
than selfishness increasing as relatedness decreases, the non-suppression model
predicts that selfishness shows a non-monotonic (domed) pattern, peaking at
intermediate relatedness (Fig. A2b). The difference in the non-suppression model is
that, relative to tragedy of the commons, selfishness is not as advantageous when
relatedness is low. At low relatedness, there is selection for high levels of
manipulation – this dilutes the benefit of selfish reproduction because that effort will
be taken away by manipulation. Within our lottery ticket metaphor in the main text,
the benefit of buying tickets is reduced if those tickets are just going to be stolen.

Comparing the non-suppression model and the model with suppression, a
consequence of adding in suppression is that lower levels of manipulation are
selected for, because the benefit of increased manipulation is reduced if it will be
suppressed (compare Fig. A2b & A2c). This lower level of manipulation, and the fact
that some of it is suppressed, lead to selfishness being beneficial at low relatedness,
as in the classic tragedy of the commons model (compare Fig. A2a & A2c), and in
contrast to when there is no suppression (Fig. A2b).

By comparing all three models, we also found the group productivity did not
vary depending upon whether or not manipulation and suppression were included in
our model, compared to the classic tragedy of the commons model (Fig. A2). This is
because adding manipulation and suppression does not change the basic structure of
the model: share of productivity multiplied by group productivity. Thus, the relation
between relatedness and group productivity is not affected: the two additional traits
are sharing the 'loss' in group productivity with selfishness, where the sum of loss is
the same for a given relatedness. In other words, manipulation and suppression do
not change the degree of cooperation across the group and this finding confirms the

design in expression A4.

Figure A2. Selfishness, manipulation, and suppression of manipulation. The panels show the
ESS predictions and simulation results for: (a) tragedy of the commons (only selfishness
evolves); (b) the non-suppression model (selfishness and manipulation evolve); (c) the model
with suppression (selfishness, manipulation, and suppression of manipulation evolve). The
solid lines show the ESS predictions, and the dots show the results of our individual-based
simulations ($a = b = 0.5$).

900
Figure A3. Nonlinear returns in the non-suppression model. Panels (a) and (b) show the
predicted ESS level of selfishness (z^*) and manipulation (x^*) respectively, for different values
of relatedness (R) and the shape parameter (a). The black triangle indicates the horizontal row
where the parameter settings are identical to each other and to Fig. A2b.

3. The models with personal costs: adding cost to relative shares of group
productivity

In the main model, investment in manipulation or suppression led to reduced

investment in group productivity. As an alternative, we also investigated a scenario

where manipulation and selfishness have a personal cost, reducing the share that an

individual obtains of the group productivity, but not influencing the overall success of

the group. In this case, manipulative cheating and suppression of cheating now have

impacts on the average level of competition, and they are not just redistributing the

share of productivity. We first consider the case where suppression is absent and
manipulation has a personal cost, and then we move on to the case where both
manipulation and suppression are allowed.
917

3.1 The non-suppression model with personal costs
The personal cost of manipulation can be added in many ways, and one easy way is
to multiply the benefit of selfishness by $(1 - x)$, where x is the level of
manipulation. For simplicity, we assume cost is multiplicative and there is no
coefficient before x. This modification changes the competitive effort through
selfishness from z_i to $(1 - x_i)z_i$, and changes the competitive effort gained
through manipulation from $z_{-i}x_i^a$ to $(1 - x_{-i})z_{-i}x_i^a$. Similarly, the average effort
of the group is $(1 - \bar{x})\bar{z}$, making the fitness of the focal individual,
926

927   $$w_i = \frac{(1-x_i)z_i + (1-x_{-i})z_{-i}x_i^a - (1-x_i)z_i x_{-i}^a}{(1-\bar{x})\bar{z}}(1 - \bar{z} - \bar{x}),$$

928   (A11)
where $(1 - \bar{z} - \bar{x})$ is the group productivity and the terms before it is the relative
share of group productivity. By comparing expressions A11 and A9, it is apparent that
we are multiplying $(1 - x)$ for both the numerator and denominator in A11.
However, it is meaningful because each term is multiplied by different x: some are
the level of manipulation of the focal individual, while others are the average of the
social neighbours or the average across the entire group.
935

We found that adding a personal cost of manipulation leads to a reduced level
of manipulation, especially when $R < 0.1$ (compare Fig. A2b& A4b). Furthermore,
because both selfishness and manipulation have a personal cost, the net benefit
obtained from investing in manipulation is reduced, and so we found no dramatic
increase in the predicted level of manipulation when $R < 0.1$ (Fig. A4b). In contrast,
when manipulation is cost-free at the individual level, the predicted strategy is to put
all selfish effort into manipulation when relatedness of the population is very low
(Fig. A2b).
944

945   *3.2 The model with suppression and personal cost*
946   We then allow suppression, with a personal cost, that reduces the share of group
947   productivity obtained. We multiply each term in the relative share of productivity in
948   expression (1) with $(1 - x - u)$, where x and u are the ones with same identity
949   as z they are multiplying (e.g., z_i multiplied by $(1 - x_i - u_i)$). This gives:
950

$$w_i = \frac{(1-x_i-u_i)z_i+\left(1-u_{-i}^b\right)(1-x_{-i}-u_{-i})z_{-i}x_i^a-\left(1-u_i^b\right)(1-x_i-u_i)z_ix_{-i}^a}{(1-\bar{x}-\bar{u})\bar{z}}(1-\bar{z}-\bar{x}-\bar{u}).$$

$$(A12)$$

We found the predicted level of suppression is lower when a personal cost of

suppression is also included to the model (compare Fig. A2c& Fig. A4c). Because

there is (i) a lower need for suppression from a lower predicted level of

manipulation, and (ii) a more costly design of suppression, we only find small levels

of suppression when relatedness is low (Fig. A4c). In addition, given the presence of

suppression, the predicted level of manipulation is lower than the model without

suppression (compare Fig. A4b& A4c). Despite the lower predicted ESS values, these

models with personal cost for manipulation and suppression still predict both traits

can be favoured, especially when relatedness is low.

Figure A4. Selfishness, manipulation, and suppression of manipulation. The panels show the
ESS predictions and simulation results for: (a) tragedy of the commons (only selfishness
evolves); (b) the non-suppression model with personal cost (both selfishness and manipulation
evolve); (c) the model with suppression and personal cost (selfishness, manipulation, and
suppression evolve). All results are generated with the same shape parameters as other figures
($a = b = 0.5$).

4. Additional analysis of the scenario with two mechanisms where all traits are

simultaneously introduced

4.1 The relation between ESS and relatedness

In order to understand the oscillating dynamics (Fig. 4) better, we perform game-

theoretical analysis for the two-mechanisms case and examine when do the two

approaches disagree with each other. We begin by analysing the model along

relatedness and found it gives very similar predictions to the scenario with only one

mechanism to manipulate (compare Fig. 2 & Fig. A5). Selfishness, manipulation, and

suppression are all greater when relatedness is lower. Both the two manipulative

traits, and the two suppression traits converge to the same ESS values. Notably,

because of the constraints on group productivity, where the sum of traits cannot

exceed 1, a lower level of selfishness is selected in the scenario with two

mechanisms while the levels of manipulation and suppression is roughly the same

between the scenario with single mechanism and two mechanisms. In other words,

because the additional manipulative mechanism is the same worthy to invest as the

other one, we find a lower level of selfishness in the scenario with two mechanisms.

Figure A5. Selfishness, manipulations, and suppressions of manipulation in the scenario with
two mechanisms to manipulate and suppress manipulation, where all traits are introduced at the
same time point. Solid lines show the ESS predictions, and dots show the results of our
individual-based simulations ($a = b = 0.5$).

4.2 The occurrence of oscillation is related to shape parameters

In contrast to the close agreement shown above, we found some disagreement

between simulation and game-theoretical analyses when we analyse along shape

parameters (Fig. A6). We used harmonic regression to test for oscillating dynamics in

our simulation data. In a harmonic regression, white noise (randomly time series)

would be a flat line because all frequencies have similar predicted amplitude; but an

oscillating pattern would lead to peak or peaks. For example, a harmonic regression

of sine wave would be mainly a single peak because it only consists of a wave at

single period. From the time series of selfishness, we found oscillating dynamics at

intermediate shape parameters ($a = b = 0.7$; Fig. A6c), but not at low and high

shape parameters (Fig. A6b& d; $a = b = $ 0.4 or 1.0). Specifically, a harmonic

regression of selfishness under low and high shape parameter values gave almost

horizontal lines, whereas intermediate values showed several peaks at periods

around 500-1500 generations (insets of Fig. A6). These peaks suggest that there is a

periodic component to the evolutionary dynamics, with stochastic cycle that repeats

about every 500-1500 generations, and the dynamic is not random fluctuations.

1010

The oscillations could occur because the benefits of manipulation and

selfishness become similar when shape parameters are at intermediate values, which

subsequently can be influenced by the interactions between traits. The decreased

difference in benefits is supported by a broader analysis, showing the discrepancy

between game-theoretical and simulative results only occurs when the former

predicts selfishness is lower than the level of manipulative cheating (Fig. A6a; $0.6 <$

$a, b < 0.8$). When shape parameters are at these intermediate values, the level of

selfishness in simulations does not go below the level of manipulation, as predicted

by game-theoretical analysis (Fig. 5a, dots& curves). Moreover, the simulated trait

values are a lot more variable as the error bars become visible (Fig. 5a; black vertical

lines over dots).

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1023

Figure A6. Oscillation dynamics of selfishness and manipulation occur in some ranges of shape
parameters in the scenario with two mechanisms when relatedness is low ($R = 1/8$). (a) ESS
predictions and simulation results from the model, where disagreement between two
approaches is found when shape parameters are between 0.6 and 0.8. (b-d) Time series of
simulations under various relatedness settings. Each panel shows the time series of traits, and
the analysis from harmonic regression is shown in the inset (same as Fig. 4). Harmonic
regression found the greatest amplitude in the period of 1385 generations and p-value of
1.5333×10^{-2} when shape parameters are 0.4; period of 815 generations and p-value of
1.8035×10^{-5} when shape parameters are 0.7; period of 1760 and p-value of 2.5202×10^{-3} when
shape parameters are 1.0.

1034

We can further examine the oscillations by checking the changes in maximal

amplitude along with shape parameters or evolved trait values (Fig. A7). In
agreement with our previous results (Fig. A6b-d), the maximal amplitude shows a
peak when shape parameters are at intermediate values and amplitude is low when
the shape is either high or low (> 0.8 or <0.6). We are interested in the difference in
evolved trait values because oscillation seems to take place when the evolved level
of selfishness is close to the level at which manipulation is expressed (Fig. A6a). After
we visualised the relationship between trait difference and the maximal amplitude of
oscillation, we found a consistent negative correlation between the difference and
amplitude. This finding suggests oscillation might have resulted from interactions
between traits when their evolved levels are similar.

1046

1047

1048 Figure A7. The relation of maximal amplitude from harmonic regression in response to (a)
1049 shape parameters, and (b) distance in evolved levels of selfishness and manipulation.
1050 Relatedness is set to 1/8 and the error bars are the 95% confidence intervals. Details of the
1051 analysis are described in appendix 7.5.

1052

4.3 Oscillating trait dynamics disappear when selfishness is not coevolving with

manipulation

In order to better understand the origin of oscillation, we reduce the complexity in
simulations by reducing the number of coevolving traits. In Fig. A6 and A7, there are
5 traits coevolving: selfishness, manipulation 1, suppression 1, manipulation 2, and
suppression 2. We make 1 of the 5 traits non-mutable at a time and analyse the
evolving traits through harmonic regression. We found oscillation disappears when
selfishness is held constant, while holding one of the two manipulative traits
constant can still produce oscillating dynamics (Fig. A8b& A8c). Moreover, the results
are consistent regardless of whether the traits are fixed at the average of coevolving
dynamics or the prediction from game-theoretical analysis (only the latter is plotted
in Fig. A7 to avoid redundancy).

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1066

Figure A8. Oscillation disappears when selfishness is controlled and fixed at a value. We use
harmonic regression to instead analyse the dynamics of manipulation 2 in this figure, because
selfishness and manipulation 1 are fixed in some panels. The level of fixed selfishness and
manipulation are determined by the ESS predicted in game-theoretical analysis, where
relatedness is 1/8 and shape parameters are 0.7. Harmonic regression found greatest amplitude
in the period of 825 generations and p-value of 2.1045×10^{-4} when all traits coevolve; period of
1450 generations and p-value of 2.5239×10^{-4} when selfishness is fixed; period of 1575 and p-
value of 5.5099×10^{-4} when manipulation 1 is fixed.

The above findings suggest the oscillation is likely to be an outcome from the

linkage (interaction) between selfishness and manipulation. That is, some

stochasticity may lead to deviations in trait values, for instance, increased selfishness

and decreased manipulation. This perturbation would generate selective forces that

favours decreased level of selfishness and increased level of manipulation. However,

because the optimal trait values of both traits are similar to each other, the selective

force would be weak, which allows trait values to fluctuate within a range of levels.

Finally, when the optimal trait values are more differed and selective forces are

strong, oscillation would only take place in a small range of parameter or even

disappear. Such effects of linkage (interactions) are not discovered in game-

theoretical analysis because inclusive fitness effects are estimated as independent

factor (i.e., no linkage between traits). Similar complication in coevolving traits have

also been observed in other studies involving individual-based simulations (Tibbetts

et al. 2020; Liu *et al.* 2021).

4.4 Oscillation also disappears when traits are independently inherited without linkage

To further test our linkage hypothesis for the oscillations, we examined an artificial

scenario where there could be no possible linkage. Specifically, we assumed that each

offspring inherits each trait independently, possibly from different individuals

(multiple asexual parents, a different one for each trait). In support of our hypothesis,

we found that when there can be no linkage, that oscillations do not occur (Figure

A9a& A9b). In addition, in this scenario, where there can be no linkage, the results of

the simulation where in quantitative agreement with the analytical prediction (Figure
A9c). This contrasts with our simulations results in Figure A6a, where oscillations
occurred, and there was a greater quantitative disagreement between our analytical
and simulation results. It also suggests that some disagreement between analytical
and simulation results were due to the simulation allows for correlation among
inherited traits to build over time.

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1105
1106 Figure A9. Oscillation does not occur when traits are inherited independently without linkage.
1107 (a) Time series of coevolving traits when shape parameters are intermediate, and relatedness is
1108 low ($R = 1/8$; $a = b = 0.7$). (b) The estimated amplitude of the time series of selfishness by
1109 harmonic regression. (c) analytical predictions and simulation results from the model without
1110 linkage of traits.

1111

4.5 Can oscillation happen when there are fewer or more mechanisms?

We then analyse whether oscillation can occur in cases with different number of

mechanisms. The idea is if the oscillation was caused by interacting selfishness and

manipulation, can oscillation still occur when there is only one mechanism to

manipulate, or when there are 3 mechanisms. As shown in Fig. A10, we found single-

mechanism simulation cannot generate oscillation while the three-mechanism

simulation still has oscillations. This makes sense because multiple mechanisms of

manipulation can amplify the initially small perturbations and help oscillation to be

maintained in the trait dynamics.

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Figure A10. Oscillation happens when there is more than one mechanism to manipulate and suppress. Here, relatedness is 1/8 and shape parameters are 0.75. Harmonic regression found greatest amplitude in the period of 1800 generations and p-value of 4.7899×10^{-3} in single-mechanism simulations; period of 1475 generations and p-value of 2.7475×10^{-5} in two-mechanism simulations; period of 390 and p-value of 1.4544×10^{-2} in three-mechanism simulations.

4.6 Does changing mutation rate lead to a different oscillation period?

In section 4.3 and 4.4 we have showed that the oscillation results from interactions and linkages between traits, consequently, we expect mutation rate should change the behaviour of oscillation. This is because mutation rate controls the speed of introducing new genotype to the population and the oscillation can be slower if mutation rate is lower. We verify this thought by running simulation with half of the original mutation rate (i.e., 5×10^{-3}, appendix 7). We found supporting evidence as the oscillation of traits last longer per each cycle and have the greatest amplitude at a larger period close to 1500 generations (compare Fig. A11 and Fig. 4).

1140

Figure A11. Selfishness and manipulative cheating traits oscillate slower when mutation rate is lower. In this figure, we set mutation rate is half the size of which in all other simulation ($R = 1/8$; $a = b = 0.7$).

4.7 Can we find oscillation in the personal cost model?

In section 3, we have discussed that implementing personal cost to manipulation and

suppression would not qualitatively change the predictions, but can we still get

oscillation in these models? We made a two-mechanism model with personal cost

and found out there is no oscillation (Fig. A12b). The underlying reason is the evolved

level of selfishness is much higher than the level of manipulation (Fig. A12a). Despite

the model design is different, the relation between maximal amplitude and trait

difference seems to remain unchanged by comparing Fig. A12c and Fig. A7b.

1153

1154 Figure A12. (a) The simulated level of selfishness, manipulative cheating, and suppression, (b)
1155 the relation between maximal amplitude from harmonic regression and shape parameters ($a =$
1156 b), and (c) the relation between maximal amplitude and trait difference in evolved selfishness
1157 and evolved manipulation.

1158

5. Arms race under different biological settings

We construct two different scenarios to understand if alternative cost design can still

generate arms-race-like dynamics. In particular, we modified group productivity so

that the cost of suppression is closer to a switch-on/switch-off design. We assume

suppression becomes costly only when the group average is above 0.05, and the cost

is the same for all suppression above 0.05. This modification allows the share of

group productivity and group productivity, to disentangle with each other and relax

the linkage assumed in the main model. On top of whether the cost depends

continuously on the degree of suppression, the cost can be conditional and only

present when there are sufficient levels of manipulation. Thus, we assume the cost

of suppression is unconditional in one case, and conditional to the average level of

manipulation in the other case. For simplicity, we do not randomly introduce each

new mechanism but mutate them at fixed time points with equal intervals.

1172

We found the genetic arms race of manipulation and suppression still occur in

both cases, but with different dynamics of suppressive traits. When the cost is

unconditional and fixed, we found all of the suppressions go to almost 1 when the

shape parameter for manipulation and suppression are equal (a=b=0.5; Fig. A13).

This is because the effect of suppression is relatively linear and it does not cost extra

if suppression has higher values (compare Fig. A13c & Fig. 5c). When the cost is

conditional to manipulation, we found a drift-like dynamics for all suppressive traits

(a=0.5, b=0.01; Fig. A14). The underlying reason is suppressions are cost-free and no

longer under selection when manipulations are completely suppressed (Fig. A14b &

A14c). The cost-free suppressions are support by the dynamics of selfishness, which

is not gradually decreasing like other cases (compare Fig. A14a with Fig. 5a& Fig.

A13a). Nevertheless, the dynamics of manipulation are very similar in all cases, thus

suggesting genetic arms race is a robust result which can be found in different

biological settings (Fig. 5, Fig. A13, and Fig. A14).

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1188

1189   Figure A13. Arms race with an unconditional and fixed amount of cost for suppressing

1190 manipulative cheating. Suppression is costly in group productivity when it exceeds 0.05, and
1191 the cost is fixed at 0.01 regardless of the trait value of suppression. Shape parameters are equal
1192 for manipulation and suppression ($a = b = 0.5$) and relatedness is 1/3.
1193

1194

1195 Figure A14. Arms race with a conditional and fixed cost for suppression. Suppression is costly
1196 only when both manipulative cheating and suppression are above 0.05, and the cost of
1197 suppression is fixed at 0.05 regardless of the trait value. Shape parameters are the same as Fig.
1198 5 ($a = 0.5$ and $b = 0.01$) and relatedness is 1/3.
1199

6. Additional discussion

6.1 Decelerating return and the nature of communication

Contrary to the linear effects assumed in the classic tragedy of the commons,

empirical studies have shown that nonlinear effects might be common in
communications between cells and individuals. This is because the limitation of
diffusion in communicative molecules, making the benefit of increased production in
those molecules diminishes (Müller *et al.* 2006; Wiley 2013; Rogers *et al.* 2017);
same principle can be applied to social insects, as increased time in communicating
would also lead to increased possibility in encountering previously-interacted
individuals (Gill & Johnson 2002). As manipulation and suppression require such
short-distance interaction, we have considered the nonlinear impact of traits on
fitness to make the model more realistic. In particular, manipulative, and suppressive
traits may have larger gains when they evolved from absence to some intermediate
extent of effects, whereas the benefit of complete manipulation or suppression is
diminishing. Similar saturating property has been found in other social traits, such as
the benefit in increased stalk/spore ratio in slime moulds (Bonner 1982; Hudson *et*
al. 2002). Thus, we focus on cases where nonlinear effects have linear or diminishing
returns ($0 < a \leq 1$ and $0 < b \leq 1$). For simplicity, we only add nonlinearity effect
to individual reproduction component and not the group productivity component
(i.e., $1 - \bar{z} - \bar{x} - \bar{u}$).
1220
6.2 Methodological details of numerical analysis in game theory results
For a given number of iteration t, we update trait values by $\{z_{t+1}, x_{t+1}, u_{t+1}\} =$
$\{z_t + c_{scale}\Delta W_z, x_t + c_{scale}\Delta W_x, u_t + c_{scale}\Delta W_u\}$ and find the trait values that
converge to fixed values. All traits are initialised at 0.1. We set the scaling coefficient
c_{scale} to 2.5×10^{-3} for better precision. Finally, due to slow convergence when
relatedness is low, we iterated 4×10^6 times for $0.1 \geq R$ and 4×10^6 times for
the rest of relatedness values.
1228
7. Individual-based simulations
7.1 Overview
We use individual-based simulations following genetic algorithm to understand the
evolution of selfishness, manipulative cheating, and suppression of manipulation. In
contrast to the game-theoretical analysis, individual-based simulations allow us to
explicitly model mutations and trait dynamics under a continuous trait space.
Following the formal analysis (section 1), we employ similar assumptions that the
population size is constant, and generations do not overlap.
1237
After initialisation, the biological processes in each generation take place in the
following order: First, groups are formed from several (l) founders where the number
of founders determines the relatedness ($R = 1/l$). Each group has the same number

of founders, and it is a parameter for population structure. Second, the founders

expand the social group to a size that social interactions take place, where each

founder replicate the same number of times. Third, we calculate the group averages

of trait values and the relative fitness of each individual. Fourth, the new-born

founders are randomly drawn from the current population according to the relative

fitness. Each new-born founder inherits its parent's trait values with independent

chances of mutation for each of the three traits.

1248

1249   We use the design with founders and group growth to avoid the potential

1250 effects of small integers and small group sizes (i.e., demographic stochasticity in

1251 social groups). This simulation framework is known as haystack models (Maynard

1252 Smith 1964).

1253

7.2 Initialisation

We initialise the population by creating a population with uniform group size (n) and

uniform properties of no selfish traits (i.e., $z = x = u = 0$). In order to reduce the

effect of demographic stochasticity, we hold the size of the whole population and let

the number of groups change because group size (n) is explicitly modelled in the

model. Specifically, we set population size parameter (N) and obtain the number of

groups as $M = \lceil N/n \rceil$, the least integer larger than or equal to N/n. Thus, the

population size, Mn, is relatively constant while the number of groups increases as

the group size decreases.

1263

1264   Each individual has three variables: the degree of selfishly increase own fitness

1265 share at the cost of entire group (z), the degree of manipulative cheating (x) and the

1266 degree of suppressing manipulative cheating (u). Within one group, there are $m =$

1267 n/l individuals that have identical trait values because they are replicated from the

1268 same founder. Further, trait values could only be changed in *mutation* process.

1269

7.3 Fitness calculation and the coevolving traits

We perform two levels of selection to choose founders for the next generation: (i)

group selection according to group productivity from average trait values of all group

members, and (ii) individual selection according to each group members' relative

fitness (Fig. 1). In other words, the probability that a founder comes from a group

depends on the group's productivity, $1 - \bar{z} - \bar{x} - \bar{u}$, and the chance that it is an

offspring of the focal individual is determined by its relative fitness in the group (or

share or productivity), $\frac{z_i + (1 - u_{-i})z_{-i}x_i - (1 - u_i)z_i x_{-i}}{\bar{z}}$. Although the simulations calculate

fitness in the same way as the game-theoretical analysis, the process for each event

is explicitly modelled in the simulations and individuals can have any trait values,

whereas the game-theoretical analysis tracks on the trait dynamics of the entire

population under weak selection assumption.

1282

1283   *7.4 Mutation of the coevolving traits*

1284   We assumed the traits can mutate between generations. For each trait of a new

1285   founder, the mutation rate is $p_{mut} = 0.01$. If a mutation occurs, we perturb the

1286   parental trait value by a normally distributed deviation with mean of 0 and standard

1287   deviation of 0.1, constrained at the boundaries [0,1].

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7.5 Analysis of the simulations

In all cases, we repeated the simulation 10 times, and let social interactions take

place at the population around 10^5 individuals (i.e., $lm\lceil 10^5/lm \rceil$) to ensure that the

trait values converged to their evolutionary optima. We introduced mutation to

selfishness from the start of simulation, manipulative cheating from 100 generation,

and suppression from 200 generation to make sure the latter traits are not evolved in

the absence of selfishness. We tracked the trait dynamics for 3×10^3 generations

(unless specified elsewhere) and average over the last 10% to calculate the average

and standard deviation of trait values. Except for the ones with oscillation dynamics,

the coevolving traits usually stabilise within 500 generations (e.g., Fig. A6b& d).

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