A triple distinction of cerebellar function for oculomotor learning and fatigue compensation

Jana Masselink[1*], Alexis Cheviet[2,3], Denis Pélisson[2] & Markus Lappe[1]

[1] Institute for Psychology & Otto Creutzfeldt Center for Cognitive and Behavioral Neuroscience, University of Münster, Fliednerstrasse 21, 48149 Münster, Germany

[2] IMPACT Team, Lyon Neuroscience Research Center, INSERM U1028, CNRS UMR 5292, University Claude Bernard Lyon 1, Bron cedex 69676, France

[3] Department of Psychology, Durham University, South Road, Durham DH1 3LE, United Kingdom

* corresponding author: jana.masselink@uni-muenster.de, +49 251 8334175

1 Abstract

The cerebellum implements error-based motor learning via synaptic gain adaptation of an inverse model, i.e. the mapping of a spatial movement goal onto a motor command. Recently, we modeled the motor and perceptual changes during learning of saccadic eye movements, showing that learning is actually a threefold process (Masselink & Lappe, 2021). Besides motor recalibration of the inverse model (1), learning also comprises perceptual recalibration of the visuospatial target map (2) and of a forward dynamics model that estimates the saccade size from corollary discharge (3). Yet, the site of perceptual recalibration remains unclear. Here we dissociate cerebellar contributions to the three stages of learning by modeling the learning data of eight cerebellar patients and eight healthy controls. Results showed that cerebellar pathology restrains short-term recalibration of the visuospatial target map and of the inverse model while the forward dynamics model is well informed about the reduced saccade change. Moreover, patients showed uncompensated oculomotor fatigue caused by insufficient upregulation of saccade duration. According to our model, this could induce long-term perceptual compensation, consistent with the overestimation of target eccentricity found in the patients' baseline data. We conclude that the cerebellum mediates short-term adaptation of the visuospatial target map and of the inverse model, especially by control of saccade duration. The forward dynamics model and long-term perceptual learning are computed outside of the cerebellum.

Introduction

The cerebellum modulates supervised error-based learning (Marr, 1969; Albus, 1971; Herzfeld, Kojima, Soetedjo, & Shadmehr, 2015). If a movement is inaccurate, an error signal adapts the synaptic gains of cerebellar Purkinje cells (Bays & Wolpert, 2007; Herzfeld, Kojima, Soetedjo, & Shadmehr, 2018; Raymond & Medina, 2018; Markanday, Inoue, Dicke, & Thier, 2021) that implement an inverse model, i.e. the mapping of the visuospatial movement goal onto a motor command (Kawato, 1999; Bays & Wolpert, 2007; Franklin & Wolpert, 2011). If e.g. the eye muscles fatigue, the synaptic gains are modulated such that the saccade does not fall short of the target (McLaughlin, 1967; Havermann & Lappe, 2010; Pelisson, Alahyane, Panouilleres, & Tilikete, 2010). To compensate for continuous fluctuations of muscle dynamics, the cerebellum is constantly recalibrating

the saccadic circuitry (Srimal, Diedrichsen, Ryklin, & Curtis, 2008; Shadmehr, Smith, & Krakauer, 2010; Wolpert, Diedrichsen, & Flanagan, 2011).

However, the traditional view on the cerebellum as a pure motor hub has changed. The cerebellum is interconnected with almost the entire cortex (Middleton & Strick, 2001; Hoshi, Tremblay, Féger, Carras, & Strick, 2005; Bostan, Dum, & Strick, 2010), including retinotopic areas (Buckner, Krienen, Castellanos, Diaz, & Yeo, 2011; Brissenden, Levin, Osher, Halko, & Somers, 2016; Marek et al., 2018), and holds at least five visuospatial maps itself (van Es, van der Zwaag, & Knapen, 2019). Moreover, it has been shown that saccadic motor learning also comprises changes in visuospatial representations. These changes occur, firstly, in the visuospatial target map when errors are assigned to an internal failure of spatial target representation (Moidell & Bedell, 1988; Collins, Dore-Mazars, & Lappe, 2007; Schnier, Zimmermann, & Lappe, 2010; Zimmermann & Lappe, 2010; Gremmler, Bosco, Fattori, & Lappe, 2014). Secondly, these changes occur in the internal representation of saccade size as measured by trans-saccadic target localizations (Bahcall & Kowler, 1999; Zimmermann & Lappe, 2009; Schnier et al., 2010).

Changes in the internal saccade representation affect the forward dynamics model that transforms the corollary discharge, i.e. a copy of the motor command (CD_M; Duhamel, Colby, & Goldberg, 1992; Umeno & Goldberg, 1997; Crapse & Sommer, 2009) into a visuospatial representation of saccade size (CD_V; Bays & Wolpert, 2007; Sommer & Wurtz, 2008; Crapse & Sommer, 2008). Intact CD_V information is necessary to correctly bridge the spatial gap between pre- and post-saccadic visual input that supports our perception of a stable world (Sperry, 1950; von Holst & Mittelstaedt, 1950; Wurtz, 2008). In Masselink and Lappe (2021), we implemented the action-perception entanglement during learning in a computational model that collectively adapts the visuospatial target map, the inverse model and the forward dynamics model in response to postdictive motor error, i.e. motor error with respect to a postdicted target position.

Cerebellar perturbations restrain saccade changes during learning, as shown e.g. in lesioned monkeys (Takagi, Zee, & Tamargo, 1998; Barash et al., 1999), in cerebellar patients (Alahyane et al., 2008; Golla et al., 2008; Xu-Wilson, Chen-Harris, Zee, & Shadmehr, 2009) and in healthy subjects with non-invasive cerebellar stimulation (Panouilleres et al., 2012; Avila et al., 2015; Jenkinson & Miall, 2010). Because of its circular learning architecture, its visuospatial maps and its CD projection pathway to frontal cortex (Middleton

& Strick, 2000), the cerebellum is an ideal candidate to also recalibrate the visuospatial target map and the forward dynamics model. In Cheviet et al. (2022), we found first evidence that changes in visuospatial representations during saccadic motor learning are impaired in cerebellar patients.

Here we use an expanded version of the visuomotor learning model of Masselink and Lappe (2021) to quantify the recalibration of the visuospatial target map, of the inverse model and of the forward dynamics model of eight patients with a neurodegenerative cerebellar disease. Data were taken from Cheviet et al. (2022), including eight healthy control subjects. To achieve a deeper understanding of which control processes are perturbed, we expanded the model of Masselink and Lappe (2021) with (1) how changes in the motor command are transposed to saccade kinematics (i.e. saccade peak velocity and saccade duration), and (2) how the visuomotor system compensates for a fatigue-induced decline in saccade peak velocity. Conditions comprise (1) learning from peri-saccadic inward and (2) from peri-saccadic outward target steps, and (3) compensation of neural oculomotor fatigue, i.e. without target step. Our results reveal that cerebellar pathology reduces short-term learning of the visuospatial target map and of the inverse model, especially when controlled by upregulation of saccade duration. Notably, the forward dynamics model and thus, the CD_V signal, seemed correctly informed about the reduced saccade change. Moreover, we show that cerebellar pathology is accompanied by an overestimation of target eccentricity that, according to our model, could stem from error reduction to counteract oculomotor fatigue on a long timescale. We conclude that intact recalibration of the visuospatial target map and of the inverse model, particularly via control of saccade duration, depend on cerebellar integrity. The forward dynamics model, at least for learning from post-saccadic errors, may be adapted upstream of the cerebellum. Long-term learning at perceptual level may partially compensate for cerebellar motor deficits.

Results

To reveal how adaptation of the visuospatial target map, of the inverse model and of the forward dynamics model for saccade motor learning relies on cerebellar integrity, we expanded the visuomotor learning model of Masselink and Lappe (2021) and fitted it to the saccade and visual target localization data of eight cerebellar patients and eight

healthy control subjects.

Experimental data

Each subject participated in three conditions requiring saccades to a 20° rightward target as well as pre- and post-saccadic visual localizations of a shortly flashed bar presented around the usual target position (Figure 1A). In the pre-saccadic localization trials, subjects localized the flash with a mouse cursor while holding gaze at the fixation point. In the post-saccadic localization trials, subjects performed a saccade to a 20° rightward target and then localized the pre-saccadic flash that had appeared before target onset. The pre- and the post-exposure phase (phase 1 and 3) measured subjects' state of saccade vector, pre- and post-saccadic visual localizations before and after exposure. The exposure phase (phase 2) induced either saccade shortening in response to (1) a 6° peri-saccadic inward target step (inward condition), (2) saccade lengthening in response to a 6° peri-saccadic outward target step (outward condition), or (3) tested the ability to maintain the saccade vector during repetitive, stereotyped saccades to a non-stepping target (no step condition). This task is known to induce oculomotor fatigue, i.e. a decline in saccade peak velocity, that is usually counteracted by upregulation of saccade duration.

Figure 2 shows the inward learning data of an example control subject (A) and of an example patient (B). Besides the higher variability of saccade endpoints (that has been reported before as a side-effect of cerebellar dysfunction, Barash et al., 1999; Golla et al., 2008; Xu-Wilson, Chen-Harris, et al., 2009; Thier & Markanday, 2019), the data show the impairment in amplitude adaptation of cerebellar patients compared to healthy controls.

Model fits

Figure 1B presents the framework of the expanded visuomotor learning model based on Masselink and Lappe (2021) that we fitted to the saccade vectors and pre- and post-saccadic visual localizations, separately for each group (controls, patients) and each condition (inward, no step, outward). The visual pre-saccadic target V_1 (fitted to the pre-saccadic visual localizations) is represented on the visuospatial map with the visual gain ω_v (Figure 1B-1). An inverse model transforms V_1 into a motor command M (fitted to the saccade vectors) with the motor gain ω_m (Figure 1B-2). Before saccade execution, a copy of the motor command is routed into the CD pathway where a forward dynamics

model estimates the visuospatial size CD_V of the upcoming saccade based on the CD gain ω_{cd} (Figure 1B-3). A forward outcome model then shifts retinal coordinates by CD_V to predict the retinal position of the post-saccadic target $\hat{V}_2$ (fitted to the post-saccadic visual localizations; Figure 1B-4). For saccade execution, the motor command is transposed to saccade peak velocity κ and saccade duration λ (Figure 1B-5). After the saccade is performed (Figure 1B-6), the actual post-saccadic target appears at retinal position V_2 (Figure 1B-7). A backward outcome model then postdicts the visual post-saccadic target back to pre-saccadic space $\hat{V}_1$ (Figure 1B-8). The postdictive motor error E_{post} evaluates the accuracy of the motor command with respect to the postdicted target position in order to adapt its gains ω_v, ω_m and ω_{cd} (Figure 1B-9). A decrease of ω_m (inward learning) is controlled by downregulating saccade peak velocity while an increase of ω_m (outward learning) is controlled by upregulation of saccade duration (Figure 1B-5).

The no step condition in which saccades are performed repetitively to the same, non-stepping target should lead to oculomotor fatigue, i.e. a decline in saccade peak velocity which is usually compensated by an increase of saccade duration. We captured peak velocity and duration changes in the no step condition by fitting a peak velocity decay rate $\gamma_\kappa \geq 0$ and a duration compensation rate γ_λ. The latter describes the within-trial percentage by which saccade duration compensates for the peak velocity loss ($0 \leq \gamma_\lambda \leq 1$).

Figure 3 presents the model fits to the mean data of control subjects (A) and patients (B) for the three conditions (inward, no step, outward). Dots with errorbars show the mean data of the pre- and post-exposure phases, respectively, jagged blue lines show the trial-by-trial saccade data (A-1,B-1: saccade vectors; A-5,B-5: saccade peak velocities; A-6,B-6: saccade durations) and smooth lines show the trial-by-trial model fit to the data. Figure 4 depicts the baseline state as well as pre- to post-exposure changes for each condition, compared between patients and control subjects. Table 1 gives an overview on the fitted parameters and residual standard errors of model fits.

Cerebellar pathology suspends short-term learning of the visuospatial target map

The fit of the visual pre-saccadic target position V_1 to the pre-saccadic target localizations (Figure 3A-1,B-1, green) captures how the visuospatial target map, i.e. the visual

gain ω_v (Figure 3A-3,B-3, green), adapts on a short time-scale when errors are credited to an internal failure of visuospatial target representation. Consistent with previous studies (Moidell & Bedell, 1988; Collins et al., 2007; Hernandez, Levitan, Banks, & Schor, 2008; Schnier et al., 2010; Zimmermann & Lappe, 2010; Gremmler et al., 2014; Masselink & Lappe, 2021), we found a small change of V_1 in learning direction for control subjects (inward -0.7 $\pm$ 2.0°, $t_7 = -1.00$, $p = .351$; outward 1.2 $\pm$ 1.8°, $t_7 = 1.86$, $p = .105$; Figure 3A-1). Please note that in the analysis of Cheviet et al. (2022) (which comprised more trials including those in which the flash was presented with a small distance to the 20° target position), these changes were subtly significant. Accordingly, the visual gain ω_v of control subjects adapted by -0.04 $\pm$ 0.10 ($t_7 = -1.00$, $p = .351$; Figure 4B) in the inward condition and 0.06 $\pm$ 0.09 ($t_7 = 1.86$, $p = .105$; Figure 4D) in the outward condition.

By contrast, the visual pre-saccadic target position V_1 of cerebellar patients did not show learning from target steps. Small changes were observed in the opposite direction (inward 0.6 $\pm$ 1.3°, $t_7 = 1.35$, $p = .218$; outward -0.9 $\pm$ 1.1°, $t_7 = -2.28$, $p = .057$; Figure 4B,D) but were also not significant in the analysis of Cheviet et al. (2022). Adding a mechanism that allows the model to learn in the opposite direction of error reduction seemed not justified in the context. Accordingly, we fitted a stable V_1 and a stable ω_v to the patients' data (Figure 3B-1,B-3, green). In sum, patients did not show short-term learning of the visual pre-saccadic target position V_1 as compared to control subjects (significant difference of V_1 change between patients and control subjects in the outward condition, $t_{14} = 2.78$, $p = .015$, Figure 4D). This shows that cerebellar integrity is crucial to adapt the visuospatial target map. Neurophysiologically, the cerebellum may mediate visuospatial adaptation through feedback projections to cortical retinotopic areas (Buckner et al., 2011; Brissenden et al., 2016; Marek et al., 2018).

Cerebellar pathology reduces short-term learning of the inverse model

The fit of the motor command M to the saccade vectors (Figure 3A-1,B-1, blue) quantifies how the inverse model, i.e. the motor gain ω_m (Figure 3A-3,B-3, blue), adapts when errors are assigned to false computation of the motor command to bring the eyes to the visuospatial target position. In accordance with previous studies (McLaughlin, 1967; Miller, Anstis, & Templeton, 1981; Wallman & Fuchs, 1998; Bahcall & Kowler, 1999; Panouilleres et al., 2008; Ethier, Zee, & Shadmehr, 2008; Havermann & Lappe, 2010;

Masselink & Lappe, 2021), the motor command M of control subjects decreased by -3.9 $\pm$ 1.8° during inward learning ($t_7 = -6.06$, $p < .001$; Figure 4B) and increased by 3.6 $\pm$ 2.0° during outward learning ($t_7 = 5.10$, $p = .001$; Figure 4D). Accordingly, the inverse model, i.e. the motor gain ω_m, adapted significantly in both learning conditions (inward -0.17 $\pm$ 0.13, $t_7 = -3.71$, $p = .008$; outward 0.12 $\pm$ 0.13, $t_7 = 2.5$, $p = .041$). As expected by the model, the motor command changes during inward learning were transposed to saccade kinematics by downregulation of saccadic peak velocity (-94.9 $\pm$ 46.2$\frac{\circ}{s}$, $t_7 = -5.81$, $p = .001$; Figure 3A-5) while saccade duration stayed constant (-2.6 $\pm$ 7.3 ms, $t_7 = -1.01$, $p = .346$; Figure 3A-6). By contrast, the motor command increase during outward learning was controlled by upregulation of saccade duration (10.4 $\pm$ 3.1 ms, $t_7 = 9.37$, $p < .001$) while saccade peak velocity stayed constant (-11.0 $\pm$ 35.3$\frac{\circ}{s}$, $t_7 = -0.89$, $p = .405$). The saccade changes brought control subjects' eyes significantly closer to the post-saccadic target (V_2 change by 3.9 $\pm$ 1.8° during inward learning, $t_7 = 6.06$, $p < .001$; -3.6 $\pm$ 2.0° during outward learning, $t_7 = -5.1$, $p = .001$; Figure 3A-2). Thus, control subjects successfully reduced the postdictive motor error E_{post} in both learning paradigms (inward 3.8 $\pm$ 2.4°, $t_7 = 4.53$, $p = .003$; outward -3.3 $\pm$ 2.2°, $t_7 = -4.16$, $p = .004$, Figure 3A-4). This corresponds to 64.1 $\pm$ 53.0% error reduction in the inward condition ($t_6 = 3.2$, $p = .019$; Figure 4B) and 50.1 $\pm$ 36.3% error reduction in the outward condition ($t_7 = 3.9$, $p = .006$; Figure 4D).

Compared to control subjects, motor command changes were largely reduced in cerebellar patients. During inward learning, the motor command M decreased by -1.2 $\pm$ 2.1° ($t_7 = -1.65$, $p = .143$) and increased during outward learning by 0.8 $\pm$ 2.6° ($t_7 = 0.83$, $p = .433$; Figure 3B-1), which was significantly less than in control subjects (inward $t_{14} = -2.75$, $p = .016$; outward $t_{14} = 2.43$, $p = .029$; Figure 4B,D). Accordingly, inverse model adaptation was not significant in patients (ω_m change inward -0.08 $\pm$ 0.14, $t_7 = -1.73$, $p = .127$, outward 0.07 $\pm$ 0.13, $t_7 = 1.58$, $p = .158$). Saccade peak velocity was significantly decreased in the inward condition (-55.9 $\pm$ 55.4$\frac{\circ}{s}$, $t_7 = -2.85$, $p = .025$; Figure 3B-5) but saccade duration was not significantly increased in the outward condition (4.1 $\pm$ 13.7 ms, $t_7 = 0.84$, $p = .427$; Figure 3B-6). Hence, reduction of postdictive motor error was less effective than in the control subjects, i.e. only 5.5 $\pm$ 78.8% during inward learning ($z = 0.84$, $p = .401$; Figure 4B) and 24.5 $\pm$ 33.4% during outward learning ($t_7 = 2.07$, $p = .077$; Figure 4D). Reduction of E_{post} in the inward condition was significantly less in patients

than in controls ($t_{14} = 2.15$, $p = .05$).

Forward dynamics model is correctly informed about the reduced saccade change

Quantification of CD_V in our model (Figure 3A-1,B-1, red) relies on the difference between pre- and post-saccadic localization, hence capturing CD_V-based integration between the pre- and the post-saccadic visual scene (see Figure 3A-2,B-2 for changes of the post-saccadic target localization with respect to saccade landing, i.e. $\hat{V}_2$). Hence, the CD gain ω_{cd} captures how the forward dynamics model is calibrated when errors are credited to a false internal representation of the saccade. In control subjects, the CD_V signal declined by -4.1 $\pm$ 2.1° during inward learning ($t_7 = -5.54$, $p < .001$; Figure 4B) and increased by 3.9 $\pm$ 2.4° during outward learning ($z = 2.38$, $p = .017$; Figure 4D). Figure 3A-1 shows that CD_V well reflects the actual saccade changes in both learning paradigms. Thus, the initial CD gain ($\omega_{cd} = 1.03 \pm 0.02$, averaged as the baseline of all three conditions, Figure 4A) stayed stable throughout learning (inward 0.01 $\pm$ 0.08, $t_7 = 0.39$, $p = .707$, Figure 4B; outward 0.01 $\pm$ 0.06, $z = -0.42$, $p = .674$, Figure 4D). This means that the forward dynamics model is well informed about the actual saccade changes in control subjects.

Surprisingly, this picture was similar in cerebellar patients. During inward learning, CD_V of patients was reduced by -1.3 $\pm$ 2.9° ($t_7 = -1.28$, $p = .241$, Figure 4B), thus well reflecting the actual saccade changes that were less than in control subjects (Figure 3B-1). In the outward condition, CD_V of patients stayed roughly constant (change of -0.4 $\pm$ 3.5°, $t_7 = -0.35$, $p = .737$, Figure 4D). Accordingly, the initial CD gain ($\omega_{cd} = 1.04 \pm 0.04$, averaged as the baseline of all three conditions, Figure 4A) was not modified during inward learning (-0.01 $\pm$ 0.1, $t_7 = -0.19$, $p = .856$) and only slightly modified during outward learning (-0.07 $\pm$ 0.07, $t_7 = -2.67$, $p = .032$). In sum, the forward dynamics model seemed correctly informed about the ongoing motor changes, similar in controls and patients (no difference in ω_{cd} change between patients and controls, inward $t_{14} = 0.39$, $p = .704$, outward $t_{14} = 0.39$, $p = .704$).

Cerebellar pathology is accompanied by overestimation of target eccentricity

Figure 4A presents the baseline state of control subjects and patients, averaged across the three conditions. While control subjects accurately localize the pre-saccadic target on the visual map ($V_1 = 20.3 \pm 0.8°$, t-test against $P_1 = 20°$, $t_7 = 1.18$, $p = .276$), patients showed a significant overestimation of target eccentricity by around 1.5° ($V_1 = 21.5 \pm 1.3°$, t-test against $P_1 = 20°$, $t_7 = 3.13$, $p = .017$). Hence, the visual gain ω_v overestimated the actual target distance already when patients entered the laboratory ($\omega_v = 1.07 \pm 0.07$, t-test against 1, $t_7 = 3.13$, $p = .017$). This was consistent across all three conditions (Figure 3B-1). Still, patients exhibited a quite accurate baseline saccade ($M = 19.5 \pm 1.6°$, t-test against $P_1 = 20°$, $t_7 = -0.92$, $p = .389$), i.e. the motor gain ω_m was downregulated such that the saccade was not hypermetric as expected from the overestimated target eccentricity (0.91 ± 0.1, t-test against 1, $t_7 = -2.66$, $p = .033$). Interestingly, target overestimation despite a quite accurate saccade was observed before in a patient with a thalamic lesion (right posterior ventrolateral and right ventromedial, Zimmermann, Ostendorf, Ploner, & Lappe, 2015). In spite of the visuospatial hypermetria, the patients' visuomotor system seemed to be at a steady state as the postdictive motor error E_{post} did not significantly differ from zero ($t_7 = 2.11$, $p = .073$ in patients, $t_7 = 1.73$, $p = .127$ in control subjects, Figure 4A).

Cerebellar pathology is accompanied by insufficient upregulation of saccade duration causing uncompensated oculomotor fatigue

The no step condition tested subjects' ability to maintain a stable saccade vector when saccades were repetitively performed to the same, non-stepping target. Figure 3A-5 shows that control subjects underwent oculomotor fatigue, as revealed by the significant decline in saccade peak velocity by $-45.7 \pm 33.4\frac{°}{s}$ ($t_7 = -3.87$, $p = .006$, $\gamma_\kappa = 0.003$). However, peak velocity decline was counteracted by a significant upregulation of saccade duration (5.6 ± 5.4 ms, $t_7 = 2.90$, $p = .023$) such that the saccade vector was maintained (M remained stable with $t_7 = 0.30$, $p = .775$). With a duration compensation rate of $\gamma_\lambda = 0.964$, saccade duration compensated for 96.4% of the within-trial velocity loss. Thus, control subjects successfully kept the visuomotor system calibrated and the error nullified (Figure 3A-4).

The cerebellar patients experienced an even greater loss of peak velocity by -68.2 $\pm$ 102.2$\frac{°}{s}$ (that did not reach significance, through, probably due higher variability in patients and small sample size, t_7 = -1.89, p = .101; γ_κ = 0.008). By contrast, upregulation of saccade duration could compensate only partially (7.7 $\pm$ 14.9 ms, t_7 = 1.46, p = .187) such that the saccade vector declined by -0.8 $\pm$ 1.5°(t_7 = -1.52, p = .172). Figure 4C shows that the saccade clearly fell short in five of eight patients. Overall, saccade duration could compensate for only 45.7% (γ_λ = 0.457) for the within-trial velocity loss, resulting in uncompensated oculomotor fatigue (Figure 3B-1). The deficit in saccade duration control of cerebellar patients during oculomotor fatigue appears consistent with the greater impairment during outward learning in which changes of the inverse model are usually transposed to an increase of saccade duration (Figure 3B-1 outward condition).

Overestimation of target eccentricity may be a result of error reduction to counteract uncompensated oculomotor fatigue

We wondered how the patients' tendency for uncompensated oculomotor fatigue affected their natural visuomotor behavior on the long run. Saccade kinematics underlie continuous fluctuations and if saccade duration cannot sufficiently compensate for regular declines of saccade peak velocity, the visuomotor system will inevitably tend to be hypometric. Saccade hypometry has been observed as a consequence of vermal cerebellar lesion in monkeys (Takagi et al., 1998; Barash et al., 1999; Ignashchenkova et al., 2009; Ohki et al., 2009) and in humans (Vahedi, Rivaud, Amarenco, & Pierrot-Deseilligny, 1995). However, Takagi et al. (1998) and Barash et al. (1999) reported that saccade vectors recovered within weeks to months. Notably, baseline saccades of cerebellar patients in our experiments were not hypometric (19.5 $\pm$ 1.6°, t_7 = -0.92, p = .389) and not different from those of control subjects (t_{14} = 0.30, p = .767). Thus, if hypothetically, saccade hypometria occurred in the early phase of the disease, the visuomotor system would necessarily have experienced significant motor errors due to the saccade vector decline. Even if short-term error reduction is reduced in cerebellar patients, a certain ability for long-term learning is assumed to be preserved (Barash et al., 1999; Tseng, Diedrichsen, Krakauer, Shadmehr, & Bastian, 2007; Xu-Wilson, Chen-Harris, et al., 2009; Thier & Markanday, 2019). Hence, using the peak velocity decay rate and the duration compensation rate of the patients' model fit (γ_κ = 0.008, γ_λ = 0.457), we simulated how the visuomotor system will behave

on a long time course if, simultaneously, preserved learning counteracts the saccade decline. Figure 5 shows a simulation for 7000 saccades directed towards a $10°$ goal. We chose the initial visuomotor gains ω_v, ω_m and ω_{cd} measured for similarly sized saccades in 35 healthy subjects by Masselink and Lappe (2021) because the larger sample size provides a more faithful picture than the initial gains of the healthy group of Cheviet et al. (2022). The simulation shows that a loss in saccade peak velocity (that is only partially compensated with $\gamma_\lambda = 0.457$) leads to an immediate decline of the motor command M, hence shortening the saccade vector from $9.8°$ to $8.4°$. In turn, the visuomotor system starts to counteract the growing motor error E_{post}, inducing outward learning at perceptual (ω_v) and motor level (ω_m). Consequently, learning to counteract oculomotor fatigue leads to an outward shift of the visual pre-saccadic target localization and simultaneous recovery from saccade hypometry. The steady state at which the visuomotor system arrives is consistent with the baseline gains that we measured when patients came to the laboratory (Figure 5). In the natural situation, this time course must be longer as saccades are performed to goals of different directions and eccentricities. However, we assume that intertemporal oculomotor fatigue of multiple occurrence may lead to gradual changes of the visuomotor system similar to our simulation on the long run. In sum, the overestimation of target eccentricity in cerebellar patients may be a consequence of long-term perceptual learning to reduce motor errors.

Discussion

To dissociate cerebellar contributions to three stages of error-based learning, we modeled the visuomotor learning data of eight patients with a neurodegenerative cerebellar disease and eight healthy control subjects. The model, based on Masselink and Lappe (2021), captures recalibration (1) of the visuospatial target map, (2) of an inverse model that transforms the visuospatial movement goal into a motor command, and (3) of a forward dynamics model that estimates the saccade size from corollary discharge. The model learns from postdictive motor error, i.e. motor error with respect to a postdictive update of the pre-saccadic target position. In patients, short-term learning was reduced in the inverse model and abolished in the visuospatial target map while the forward dynamics model seemed correctly informed about the reduced saccade change. Moreover, cerebellar

pathology impaired the ability to upregulate saccade duration in response to oculomotor fatigue. Modeling suggests that long-term error reduction at perceptual level may have counteracted, explaining the overestimation of target eccentricity in the patients' baseline data. We conclude that the cerebellum recalibrates the visuospatial target map and the inverse model on a short time-scale, particularly via control of saccade duration, while the forward dynamics model is computed outside of the cerebellum. Long-term perceptual learning may partially compensate for cerebellar motor deficits.

Cerebellum implements short-term learning of the inverse model

Our results confirmed that the inverse model is adapted within the cerebellar microcircuit. Motor gain adaptation was largely restrained in cerebellar patients for both inward and outward errors. Similar impairments have been shown in lesioned monkeys (Takagi et al., 1998; Barash et al., 1999), in cerebellar patients (Alahyane et al., 2008; Golla et al., 2008; Xu-Wilson, Chen-Harris, et al., 2009) and in healthy subjects with cerebellar tDCS or magnetic stimulation (Panouillères, Miall, & Jenkinson, 2015; Avila et al., 2015; Jenkinson & Miall, 2010). In the patients of Golla et al. (2008), learning from outward target steps was completely suspended while in our study, a small saccade change was preserved. This difference may arise because the patients' lesion of Golla et al. (2008) was specifically located in the oculomotor vermis, i.e. the particular region assumed to process inverse model adaptation for oculomotor commands (Hopp & Fuchs, 2004; Dean, Porrill, Ekerot, & Jörntell, 2010; Thier & Markanday, 2019).

Cerebellum mediates short-term learning of the visuospatial target map

After visuomotor learning has initially been seen through a pure motor lens, numerous studies have revealed changes in the visuospatial perception of the movement goal (Collins et al., 2007; Schnier et al., 2010; Gremmler et al., 2014). Hence, motor learning is not simply a change of the motor command directed to the same goal location on every trial. Instead, learning underlies recalibration of both the visuospatial goal representation and the motor command required to bring the eyes to that location. This makes sense since motor errors cannot only be due to erroneous computation of the motor command but can also stem from a deficient goal representation. To our knowledge, these data are the first to demonstrate that the cerebellum is a neural substrate for visuospatial recalibration during

motor learning. Neurophysiologically, the cerebellum is an ideal candidate to modulate visuospatial plasticity because of its inner circular organization (Dean et al., 2010; Tanaka, Ishikawa, Lee, & Kakei, 2020), its homogenous output organization (Sultan, Mock, & Thier, 2000; Hoshi et al., 2005; Bostan et al., 2010), and its functional interconnections with cerebral retinotopic areas (Buckner et al., 2011; Brissenden et al., 2016; Marek et al., 2018).

The forward dynamics model is computed outside of the cerebellum

Consistent with previous work (Bahcall & Kowler, 1999; Collins et al., 2007; Schnier et al., 2010; Masselink & Lappe, 2021), in our study, healthy subjects' localizations shifted pre- and post-saccadically while both changes remained absent in patients. Thus, CD_V seemed to correctly reflect the saccade changes in healthy controls and in patients. This result has two major implications. First, it proposes that the efference copy that is routed into the forward dynamics model reflects the actual adapted motor command and not some kind of initial motor command prior to adaptive changes. Second, it suggests that also in patients, the forward dynamics model accurately captures the actual changes of the inverse model such that the saccade vector is neither over- nor underestimated. This means that the forward dynamics model involved in trans-saccadic spatial integration and feedback motor learning is computed outside of the cerebellum. Indeed, the cerebellum computes forward models for object motion (Nowak, Hermsdörfer, Rost, Timmann, & Topka, 2004; Miall, Christensen, Cain, & Stanley, 2007; Roth, Synofzik, & Lindner, 2013) and feed-forward motor control (movement adjustments during execution; Chen-Harris, Joiner, Ethier, Zee, & Shadmehr, 2008; Ethier et al., 2008; Albert & Shadmehr, 2018). However, the forward dynamics model measured in our task is one involved in trans-saccadic perception and feedback motor learning, i.e. from errors after movement completion. That this forward dynamics model is computed outside of the cerebellum is supported by studies showing that a disruption of the CD pathway from SC via MD thalamus to the FEF provokes a bias in visual space updating (Ostendorf, Liebermann, & Ploner, 2010; Prime, Vesia, & Crawford, 2010; Ostendorf, Kilias, & Ploner, 2012; Cavanaugh, Berman, Joiner, & Wurtz, 2016). The forward dynamics model could also be computed along other CD pathways, e.g. from SC via the thalamic pulvinar to parietal and occipital cortex (Wurtz, Joiner, & Berman, 2011; Berman, Cavanaugh, McAlonan, & Wurtz, 2017). The role

³⁹⁷ of parietal cortex in CD processing was recently demonstrated by Cheviet, Pisella, and

³⁹⁸ Pélisson (2021). At least, saccadic learning involves a distributed network across cerebral

³⁹⁹ cortex (Blurton, Raabe, & Greenlee, 2012; Gerardin, Miquée, Urquizar, & Pélisson, 2012;

⁴⁰⁰ Guillaume, Fuller, Srimal, & Curtis, 2018).

Cerebellum counteracts oculomotor fatigue by upregulating saccade duration

⁴⁰³ Our results disclosed that cerebellar integrity is crucial for counteracting oculomotor

⁴⁰⁴ fatigue by saccade duration adjustment. While healthy subjects compensated peak veloc-

⁴⁰⁵ ity loss by 96% within a trial, patients achieved only 46%, resulting in gradual saccade

⁴⁰⁶ hypometry. This is in line with results of, firstly, Golla et al. (2008) who observed re-

⁴⁰⁷ duced oculomotor fatigue compensation, and, secondly, Xu-Wilson, Chen-Harris, et al.

⁴⁰⁸ (2009) who observed reduced within-saccade compensation for peak velocity fluctuations

⁴⁰⁹ in cerebellar patients. Hence, it seems that saccade lengthening, within-saccade (due to

⁴¹⁰ oculomotor fatigue) or after saccade (due to post-saccadic motor error), is operated by

⁴¹¹ cerebellar-dependent saccade duration control. The cerebellum adjusts movement dura-

⁴¹² tion in response to velocity variations also for smooth pursuit (Dash & Thier, 2013) and

⁴¹³ hand pointing movements (Markanday, Messner, & Thier, 2018). Neurophysiologically, it

⁴¹⁴ remains to be examined how duration control is implemented. For manual movements,

⁴¹⁵ there is first evidence that the simple spikes of Purkinje cells also code movement velocity

⁴¹⁶ and duration (Roitman, Pasalar, Johnson, & Ebner, 2005; Pasalar, Roitman, Durfee, &

⁴¹⁷ Ebner, 2006; Ebner & Pasalar, 2008).

Long-term perceptual learning may compensate for cerebellar deficiencies in saccade duration control

⁴²⁰ On the long run, insufficient velocity compensation in cerebellar patients will lead to

⁴²¹ hypometric saccades. Indeed, saccade hypometry and reduced saccade velocity were ob-

⁴²² served in cerebellar patients (Golla et al., 2008; Vahedi et al., 1995) and lesioned monkeys

⁴²³ (Takagi et al., 1998; Barash et al., 1999; Ignashchenkova et al., 2009; Ohki et al., 2009).

⁴²⁴ Our model simulation for long-term behavior of a cerebellar-deficient visuomotor system

⁴²⁵ shows that initially, the saccade will become hypometric. Yet, with the gradual increase

⁴²⁶ of motor errors, learning will counteract at perceptual and motor level. Firstly, the sim-

ulation can explain the significant overestimation of target eccentricity in the patients' baseline data. Secondly, the simulation depicts a recovery from saccade hypometry as found in lesioned monkeys (Takagi et al., 1998; Barash et al., 1999). Yet, in these studies, recovery concerned saccade accuracy but not saccade precision, like in our patients who exhibited non-hypometric saccades despite high endpoint variability. Hence, a tendency for saccade dysmetria due to deficiencies in saccade duration control may induce long-term perceptual and motor learning, probably upstream of the cerebellum. This may enable the visuomotor system to stay calibrated despite cerebellar short-term adaptation deficits.

Neurophysiologically, the visual overestimation of target eccentricity is interesting when put together with Zimmermann et al. (2015) who found a similar result in a patient with a right posterior ventrolateral and ventromedial thalamic lesion. If, in both cases, this visual peculiarity is a consequence of motor adaptation deficits, these results underline the critical role of the cerebellar projection pathway via VL thalamus to frontal cortex for intact motor learning (Middleton & Strick, 2000; Gaymard, Rivaud-Péchoux, Yelnik, Pidoux, & Ploner, 2001).

Conclusion

We suggest an expanded view on the cerebellar circuit function for oculomotor learning and fatigue compensation. Accordingly, the cerebellum does not only adapt the inverse model at the Purkinje cell synapse, but additionally mediates the recalibration of the visuospatial goal representation on a short-time scale. The forward dynamics model for trans-saccadic space perception and feedback motor learning is computed outside of the cerebellum. Future research needs to examine which cerebellar structures could mediate visuospatial recalibration, and where the forward dynamics model is computed, e.g. in the thalamus, in the frontal eye fields or in other cerebral areas.

Methods

Subjects

Our study is based on the dataset of Cheviet et al. (2022) which includes eight healthy control subjects (49.25 ± 7.67 years, four male, four female) and eight patients with a neurodegenerative disorder of the cerebellum (55.5 ± 9.61 years, four male, four female).

Three patients suffered from spinocerebellar ataxia, two patients from Friedreich ataxia, one patient from unknown autosomal dominant inherited cerebellar ataxia, one patient from fragile X–associated tremor/ataxia syndrome and one patient from late onset sporadic ataxia. Each patient was clinically examined at the Neurological Hospital Pierre Wertheimer (Bron, France) to verify a chronic progressive cerebellar ataxia, normal or corrected-to-normal vision, the ability to concentrate and to remain seated for at least 30 min as well as to maintain a stable hand position for at least 30 s. Patients with another neurological disease, unstable medical condition, psychotropic medication intake, pronounced nystagmus or ocular instability were excluded from study participation.

All subjects gave informed consent to participation. The experiment was performed in accordance with the ethical standards of the 1964 Helsinki Declaration and was approved by the ethics committee (CPP Est-III; ID-RCB: 2017–00942-51; 17.05.09).

Setup

Subjects were seated in a completely dark room in front of a CRT monitor (19 inches, 1280×1024 pixels, 85 Hz, 57 cm viewing distance) that was covered with a neural density filter to prevent visibility of monitor background light and contrast to the surrounding (ND4, 25% transmittance).

Movements of the right eye were recorded by an Eyelink 1000 (remote configuration; SR Research, Ontario, Canada) at 1000 Hz with a five-point calibration before each session and drift correction after each session break. Online detection of saccade onset was determined by a 5° position threshold, a $22\frac{\circ}{s}$ velocity threshold and $4000\frac{\circ}{s^2}$ acceleration threshold. Online fixation control was based on a 5° position threshold (horizontally and vertically). The procedure was controlled with Experiment Builder (SR Research, Ontario, Canada).

Experimental design

Each subject participated in three experimental conditions recorded in randomized order with at least one week in between. Each condition measured reactive saccades to a 20° rightward target as well as visuospatial localizations of a flashed bar that varied horizontally around the target position by -4, -2, 0, +2 and +4 ° (Figure 1A). Localization was performed during fixation (pre-saccadic localization trials) and after saccade landing (post-saccadic localization trials).

The pre-exposure phase measured subjects' baseline state, comprising four repetitions of five pre-saccadic localization trials and five post-saccadic localization trials, followed by a block of 20 saccade trials with peri-saccadic target offset (4*(5+5) + 20 = 60 trials; for an overview of the trial sequence see Figure 2A-B). The exposure phase measured 120 saccade trials with either a 6° peri-saccadic target step opposite to saccade direction (inward condition), or a 6° peri-saccadic target step in saccade direction (outward condition), or without any peri-saccadic target step (no step condition). The latter condition required subjects to maintain the saccade vector, which is usually achieved by upregulating saccade duration to counteract peak velocity decline in the course of repetitive, stereotyped saccades, known as oculomotor fatigue. A break was performed after the 50th and the 100th trial. The post-exposure phase measured localizations after exposure (four repetitions of five pre-saccadic localization trials and five post-saccadic localization trials), interleaved with three blocks of each 20 saccade refresh trials (including the respective target step) to maintain the achieved saccade vector of the exposure phase (4*(5+5) + 3*20 = 100 trials; Figure 2A-B). Each session began with a 10 min dark adaptation phase. During session breaks (before each change of trial type and after the 50th and 100th trial of the exposure phase), the room was dimly illuminated to keep the level of dark adaptation constant.

All stimuli (target, flash and pointer) were presented with respect to the average horizontal gaze position of a 50 ms fixation reference period at trial start (fixation reference, see trial descriptions below). A trial was repeated if fixation criteria were violated. Inter-trial interval was a 800 ms black screen.

Saccade trials. A red fixation circle of 1° diameter appeared for a random time interval between 800 and 1400 ms (5° to the right of the left screen border, vertically randomized between -1.5, 0 and 1.5° to the horizontal meridian, Figure 1A). If fixation criteria were

met during this period, a red target circle was displayed 20° to the right with respect to the fixation reference determined during the last 50 ms of the fixation period. As soon as saccade onset was detected, the target switched off in the pre-exposure phase, and, in the exposure and post-exposure phase, stepped either 6° inward (inward condition), 6° outward (outward condition) or stayed at its position (no step condition). In the exposure and post-exposure phase, the target stayed visible for 100 ms.

Post-saccadic localization trials. A red fixation circle of 1° diameter was presented 5° to the right of the left screen border on the horizontal meridian (Figure 1A). Subjects were instructed to fixate the circle and to indicate when ready to begin the trial via mouse press. If, after a 450 ms black screen, fixation criteria were met for 50 ms, a blue vertical line was flashed with counterbalanced horizontal distance of 16, 18, 20, 22 or 24° with respect to the fixation reference determined during the 50 ms fixation check period (12 ms, 0.2° width, 29° height). After a 400 ms black screen, a red target circle of 1° diameter appeared 20° to the right of the fixation reference. As soon as saccade onset was detected, the target was extinguished, followed by a 100 ms black screen. A blue line pointer was displayed on the right screen bottom (0.2° width, 10° height, 10° below the horizontal meridian, randomly 17, 19, 21 or 23° to the right of the fixation reference). As soon as subjects started moving the mouse, the pointer was blocked to the horizontal meridian. The subject had to move the pointer to the perceived horizontal flash position, confirming the judgement with a mouse press.

Pre-saccadic localization trials. A red prohibited direction sign served as a fixation stimulus (with the same spatial parameters as in the post-saccadic localization trials, Figure 1A). The subject had to continuously fixate it from the first mouse press (to indicate she/he is ready to start the trial) to the second mouse press (to confirm the localization judgement). The flash was presented with the same latency and spatial parameters as in the post-saccadic localization trials. The pointer appeared 750 ms after flash offset to roughly match the respective interval of the post-saccadic localization trials, and with the same latency and spatial parameters as in the post-saccadic localization trials. As soon as the subject started moving the mouse, the pointer was blocked to the horizontal meridian and the subject had to move the pointer to the perceived horizontal flash position and press the mouse.

 Training phase. Before each session, subjects practiced a minimum of 5 pre- and 5

 post-saccadic localization trials. In case of difficulties, online gaze position and a fixation

 box around the fixation circle were displayed to help subjects to familiarize with the task

 requirements.

Model

 To quantify the adaptive changes in the visuomotor circuitry of patients and control

 subjects, we used the model of Masselink and Lappe (2021) and expanded it with (1)

 how changes in the motor command are transposed to saccade peak velocity and saccade

 duration and (2) how the visuomotor system compensates for a fatigue-induced decline in

 saccade peak velocity (Figure 1B). The model describes the saccadic circuitry based on

 three sensorimotor transformations, i.e. synaptic gains (Shadmehr et al., 2010; Wolpert

 et al., 2011), that learn to reduce postdictive motor error, an error of the motor command

 with respect to a postdictive update of the pre-saccadic target position. These plastic gains

 are, first, a visual gain ω_v to transform retinal input into target position on a visuospatial

 map, second, a motor gain ω_m to transform spatial target position into a motor command

 (inverse model), and, third, a CD gain ω_{cd} to transform the corollary discharge CD_M of

 the motor command into CD_V, i.e. the computed displacement of visual space due to the

 saccade (forward dynamics model).

 Pre-saccadic calculations. The pre-saccadic target position $V_1^{(n)}$ on the visuospatial

 map is scaled by the visual gain $\omega_v^{(n)}$:

$$V_1^{(n)} = P_1 \omega_v^{(n)} \tag{1}$$

 with the trial number n and physical target eccentricity P_1 (Figure 1B-1). If $\omega_v^{(n)} = 1$,

 the target is accurately localized on the visuospatial map. If a postdictive motor error is

 assigned to an internal failure of visuospatial target representation, $\omega_v^{(n)}$ is adapted to

 reduce the error for future movements (see equation 14).

 The inverse model (Figure 1B-2) transforms the pre-saccadic target position into a

 motor command with the motor gain $\omega_m^{(n)}$:

$$M^{(n)} = V_1^{(n)} \omega_m^{(n)} = P_1 \omega_v^{(n)} \omega_m^{(n)} \tag{2}$$

Thus, the inverse model transforms the movement goal from visuospatial to motor coordinates based on the assumed state of muscle dynamics. If $\omega_m^{(n)} = 1$, the saccade lands at the spatial position $V_1^{(n)}$. If a postdictive motor error is assigned to a change in muscle dynamics, $\omega_m^{(n)}$ is adapted to reduce the error for future movements (see equation 14). The quantification of changes to the visual gain ω_v, on the one hand, and the motor gain ω_m, on the other hand, dissociates the contribution of the two processes to behavioral output, i.e. saccade vector change.

The motor command $M^{(n)}$ is copied into $CD_M^{(n)}$:

$$CD_M^{(n)} = M^{(n)} \tag{3}$$

and directed into the CD pathway.

Before saccade start, the forward dynamics model (Figure 1B-3) transforms the corollary discharge of the motor command $CD_M^{(n)}$ into the $CD_V^{(n)}$ signal, i.e. the computed displacement of visual space, to inform the visual system about the upcoming saccade:

$$CD_V^{(n)} = CD_M^{(n)}\omega_{cd}^{(n)} = P_1\omega_v^{(n)}\omega_m^{(n)}\omega_{cd}^{(n)} \tag{4}$$

If $\omega_{cd}^{(n)} = 1$, $CD_V^{(n)}$ matches the actual saccade vector. If a postdictive motor error is assigned to an internal failure of CD_V representation, $\omega_{cd}^{(n)}$ is adapted to reduce the error for future movements (see equation 14).

Based on $CD_V^{(n)}$, the forward outcome model (Figure 1B-4) shifts the coordinates of the visual pre-saccadic target position $V_1^{(n)}$ to predict the visual post-saccadic target position:

$$\hat{V}_2^{(n)} = V_1^{(n)} - CD_V^{(n)} = P_1\omega_v^{(n)}(1 - \omega_m^{(n)}\omega_{cd}^{(n)}) \tag{5}$$

Saccade kinematics. Saccadic motor learning has been shown to be differently transposed to saccade kinematics, i.e. to saccade peak velocity and saccade duration, depending on the error direction (Golla et al., 2008; Thier & Markanday, 2019). Moreover, there is evidence that cerebellar patients are more impaired in learning from outward than from inward errors (Golla et al., 2008). Thus, capturing the learning effect on the patients' saccade kinematics may provide a deeper understanding of how the cerebellum operates the recalibration of motor commands. Hence, we expanded the model of Masselink and

Lappe (2021) with how the motor command is transposed to saccade peak velocity and saccade duration. Accordingly, the saccade is executed with the saccade peak velocity $\kappa^{(n)}$ and the saccade duration $\lambda^{(n)}$ that are specific for the motor command (Figure 1B-5, see equations 16, 18 and 20 for how the motor command is transposed to saccade peak velocity and saccade duration depending on the paradigm). This specificity relies on a linear relationship between a saccade's amplitude, its peak velocity and its duration, known as the saccadic main sequence (Bahill, Clark, & Stark, 1975; Harris & Wolpert, 2006; Collins, Semroud, Orriols, & Doré-Mazars, 2008). Hence, we specify the relationship between the motor command $M^{(n)}$, the saccade peak velocity $\kappa^{(n)}$ and the saccade duration $\lambda^{(n)}$ by the following equation:

$$M^{(n)} = \beta_0 + \beta_\kappa \kappa^{(n)} + \beta_\lambda \lambda^{(n)} \tag{6}$$

For the modeling, we derive β_0, β_κ and β_λ from fitting the equation to the saccade vectors, saccade peak velocities and saccade durations of patients and healthy controls.

Saccade execution. The execution of the motor command produces the physical saccade vector (Figure 1B-6):

$$P_M{}^{(n)} = M^{(n)} + \epsilon_m{}^{(n)} = P_1 \omega_v{}^{(n)} \omega_m{}^{(n)} + \epsilon_m{}^{(n)} \tag{7}$$

with random motor noise $\epsilon_m{}^{(n)}$.

In the inward and outward learning paradigms, the target is shifted during saccade execution. The peri-saccadic target displacement due to the target shift P_s and the motor execution noise ϵ_m is described by:

$$P_d{}^{(n)} = P_s - \epsilon_m{}^{(n)} \tag{8}$$

Post-saccadic calculations. After saccade offset, the post-saccadic target is localized on the visuospatial map (Figure 1B-7):

$$V_2{}^{(n)} = P_1 + P_d{}^{(n)} + \epsilon_m{}^{(n)} - P_M{}^{(n)} = P_1(1 - \omega_v{}^{(n)} \omega_m{}^{(n)}) + P_d{}^{(n)} \tag{9}$$

The backward outcome model integrates the visual post-saccadic target position $V_2{}^{(n)}$ with $CD_V{}^{(n)}$ to from a postdictive update of the target position in a pre-saccadic reference

frame (Figure 1B-8):

$$\hat{V}_1^{(n)} = V_2^{(n)} + CD_V^{(n)} = P_1(1 + \omega_v^{(n)}\omega_m^{(n)}(\omega_{cd}^{(n)} - 1)) + P_d^{(n)} \tag{10}$$

We refer to this process as the backward outcome model as it performs a postdictive trans-

formation from post- to pre-saccadic space, analogously to the forward outcome model that

performs a predictive transformation, i.e. from pre- to post-saccadic space.

Learning of visuomotor gains and its transposition to saccade kinematics. In

the inward and outward learning paradigms, the visuomotor system experiences a signifi-

cant motor error due to the peri-saccadic target step. This error, termed the postdictive

motor error $E_{post}^{(n)}$, is calculated as the error of the motor command with respect to the

postdicted pre-saccadic target position (Figure 1A-9):

$$E_{post}^{(n)} = \hat{V}_1^{(n)} - M^{(n)} = P_1(1 + \omega_v^{(n)}\omega_m^{(n)}(\omega_{cd}^{(n)} - 2)) + P_d^{(n)} \tag{11}$$

To reduce $E_{post}^{(n)}$ on the next trial, the visuomotor system adapts its gains following

an internal estimate of the $E_{post}^{(n)}$ gradient (Doya, 1999; Wolpert et al., 2011; Taylor &

Ivry, 2014). We express this principle by the delta rule (Widrow & Hoff, 1960; Widrow &

Stearns, 1985):

$$\boldsymbol{\omega}^{(n+1)} = \boldsymbol{\omega}^{(n)} - \boldsymbol{\alpha}\frac{\partial|E_{post}^{(n)}|^2}{\partial\boldsymbol{\omega}^{(n)}} \tag{12}$$

$$= \boldsymbol{\omega}^{(n)} - 2\boldsymbol{\alpha}E_{post}^{(n)}\frac{\partial E_{post}^{(n)}}{\partial\boldsymbol{\omega}^{(n)}} \tag{13}$$

$$= \boldsymbol{\omega}^{(n)} - 2\boldsymbol{\alpha}E_{post}^{(n)}\begin{pmatrix} P_1\omega_m^{(n)}(\omega_{cd}^{(n)} - 2) \\ P_1\omega_v^{(n)}(\omega_{cd}^{(n)} - 2) \\ P_1\omega_v^{(n)}\omega_m^{(n)} \end{pmatrix} \tag{14}$$

The learning rates $\boldsymbol{\alpha} = \begin{pmatrix} \alpha_v & 0 & 0 \\ 0 & \alpha_m & 0 \\ 0 & 0 & \alpha_{cd} \end{pmatrix} \geq 0$ specify the speed of learning.

The changes in the visual gain ω_v and in the motor gain ω_m result in a changed motor

command $M^{(n+1)}$ on the next trial. The transposition of the changed motor command

to saccade peak velocity and saccade duration needs to take into account whether the

motor command was decreased or increased, i.e. whether changes occurred during inward or during outward learning (Golla et al., 2008; Thier & Markanday, 2019). Saccade shortening during inward learning is usually characterized by a decline of peak velocity while saccade duration stays constant. Accordingly, during inward learning in our model ($P_s < 0$), saccade duration λ stays constant while saccade peak velocity κ is downregulated on the next trial according to the changed motor command (Figure 1B-6):

$$
\begin{aligned}
\lambda^{(n+1)} &= \lambda^{(n)} & (15) \\
\kappa^{(n+1)} &= \frac{M^{(n+1)} - \beta_0 - \beta_\lambda \lambda^{(n+1)}}{\beta_\kappa} & (16)
\end{aligned}
$$

By contrast, saccade lengthening during outward learning is usually characterized by an increase of saccade duration while saccade peak velocity stays constant (Golla et al., 2008; Thier & Markanday, 2019). Accordingly, during outward learning in our model ($P_s > 0$), saccade peak velocity κ stays constant while saccade duration λ is upregulated on the next trial according to the changed motor command (Figure 1B-6):

$$
\begin{aligned}
\kappa^{(n+1)} &= \kappa^{(n)} & (17) \\
\lambda^{(n+1)} &= \frac{M^{(n+1)} - \beta_0 - \beta_\kappa \kappa^{(n+1)}}{\beta_\lambda} & (18)
\end{aligned}
$$

The visuomotor system reaches a steady state, i.e. learning comes to an end, if the saccade lands at the postdicted pre-saccadic target position such that $E_{post}^{(n)} = 0$.

Oculomotor fatigue and its compensation by saccade duration. For a deeper understanding of which calibration processes are perturbed due to cerebellar disease, we also modeled the experimental condition without any target step, i.e. without learning. Although target localizations and saccade vectors should stay roughly constant in healthy subjects, the repetitive execution of saccades to the same target position is usually accompanied by a decline in saccade peak velocity, a sign of oculomotor fatigue. Compared to learning in response to an assumed fatigue of the eyes muscles, oculomotor fatigue is of neural origin and perhaps due to a loss of motivation or attention (Prsa, Dicke, & Thier, 2010). Usually, it is compensated by an increase in saccade duration such that saccade endpoint accuracy is maintained (Schmidt, Abel, DellOsso, & Daroff, 1979; Fuchs & Binder, 1983; Bahill et al., 1975; Straube, Robinson, & Fuchs, 1997; Chen-Harris et al.,

2008; Xu-Wilson, Zee, & Shadmehr, 2009; Prsa et al., 2010). However, this compensating mechanism has been shown to be impaired in patients with vermal cerebellar lesion (Golla et al., 2008). Accordingly, in the no step condition of our model ($P_s = 0$), saccade peak velocity κ declines while saccade duration λ compensates by a certain percentage on the next trial (Figure 1B-6):

$$\kappa^{(n+1)} = \kappa^{(n)} - \gamma_\kappa \left(\kappa^{(n)} - \kappa_{end} \right) \tag{19}$$

$$\lambda^{(n+1)} = \lambda^{(n)} - \gamma_\lambda \left(\lambda^{(n)} - \frac{(M^{(n+1)} - \beta_0 - \beta_\kappa \kappa^{(n+1)}}{\beta_\lambda} \right) \tag{20}$$

Here, $\gamma_\kappa \geq 0$ describes the decay rate of peak velocity, κ_{end} limits peak velocity loss and γ_λ describes the percentage by which saccade duration compensates for the peak velocity loss ($0 \leq \gamma_\lambda \leq 1$). According to the changes of peak velocity κ and duration λ in the no step condition ($P_s = 0$), the motor gain $\omega_m{}^{(n+1)}$ of the next trial is:

$$\omega_m{}^{(n+1)} = \frac{\beta_0 + \beta_\kappa \kappa^{(n+1)} + \beta_\lambda \lambda^{(n+1)}}{P_1 \omega_v{}^{(n+1)}} \tag{21}$$

Hence, during expected oculomotor fatigue in the no step condition, we model changes in saccade peak velocity and saccade duration that are reflected in the motor gain ω_m while ω_v and ω_{cd} are assumed to stay stable.

Analysis

Data processing. Data analysis was performed in Matlab R2017a (Mathworks, Natick, MA). Saccades with a latency of less than 100 ms, an amplitude below 10° or above 30° as well as localizations with more than ±7° localization error were excluded from the analysis. Moreover, as our modeling approach explicitly relies on the localization judgement of target eccentricity, we chose only the pre- and post-saccadic localization trials in which the flash position matched the saccade target position, i.e. 20° eccentricity. Thus, we ensured that our modeling approach quantifies perceptual changes exactly at the spatial position of the target and is not disturbed by the process of learning transfer to nearby locations, known as the saccadic adaptation field (Deubel, 1987; Miller et al., 1981; Frens & Van Opstal, 1994; Straube et al., 1997; Hopp & Fuchs, 2004; Collins et al., 2007; Schnier et al., 2010; Pelisson et al., 2010).

For each condition of each subject, we calculated the mean saccade vector, mean saccade peak velocity and mean saccade duration of the 20 pre-exposure saccade trials and the last 20 exposure saccade trials, respectively. For the pre- and the post-saccadic flash localizations we extracted the mean of the pre-exposure and the post-exposure phase. In addition, we quantified a cross-condition baseline state for each subject, averaging the mean saccade vectors, saccade peak velocities, saccade durations and pre- and post-saccadic localizations across the three conditions. Outliers with more than three standard deviations from the mean were excluded. We averaged the saccade vectors, pre- and post-saccadic localizations at group level, i.e. separately for patients and control subjects and condition. Moreover, we calculated the mean trial-by-trial saccade vectors, saccade peak velocities and saccade durations of the 120 exposure trials, separately for patients and control subjects.

Model-based analysis. We calculated the state of the CD_V signal, the visuomotor gains $\boldsymbol{\omega}$ and the E_{post} error of each subject's pre-exposure and post-exposure phase. Based on the pre-saccadic target localization (V_1), the saccade vector (M) and the post-saccadic target localization with respect to the saccade landing position ($\hat{V}_2$), we derive:

$$CD_V = V_1 - \hat{V}_2 \tag{22}$$

$$\omega_v = \frac{V_1}{P_1} \tag{23}$$

$$\omega_m = \frac{M}{V_1} \tag{24}$$

$$\omega_{cd} = \frac{CD_V}{CD_M} \tag{25}$$

$$E_{post} = P_1(1 + \omega_v\omega_m(\omega_{cd} - 2)) + P_d \tag{26}$$

with $P_1 = 20°$ and $P_d = 0°$ for the pre-exposure phase and the post-exposure phase of the no step condition, $P_d = $ -6° for the post-exposure phase of the inward condition and $P_d = 6°$ for the post-exposure phase of the outward condition. Additionally, we derived the change of each variable from the pre- to the post-exposure phase.

Before fitting the model to the trial-by-trial data, we performed a regression of the saccade vectors on saccade peak velocities and saccade durations of the exposure phase, separately for each group (controls, patients) and each condition (inward, no step, out-

 ward). See Table 1 for the fitted regression weights.

 Starting from the pre-exposure mean of pre-saccadic localization ($V_1^{(1)}$), post-saccadic

 localization (with respect to the saccade landing point, $\hat{V}_2^{(1)}$), saccade vector ($M^{(1)}$),

 saccade peak velocity ($\kappa^{(1)}$) and saccade duration ($\lambda^{(1)}$) taken as values of trial $n = 1$,

 we fitted the model to the exposure phase, separately for each group (control subjects,

 patients) and each condition (inward, no step, outward). For the inward and the outward

 condition, we fitted the learning rates of the visuomotor gains ($\boldsymbol{\phi_{fit}} = \boldsymbol{\alpha}$), and for the no

 step condition, we fitted the peak velocity decay rate and the duration compensation rate

 ($\boldsymbol{\phi_{fit}} = (\gamma_\kappa, \gamma_\lambda)$). The fitting procedure minimized the weighted sum of squared errors

 (SSE):

$$
\begin{aligned}
\boldsymbol{\phi_{fit}} \quad = \quad &argmin\Bigg(\sum_{1,120} \Big(\eta_{V_1}(V_1^{(n)} - V_{1,predicted}^{(n)})^2 + \eta_{\hat{V}_2}(\hat{V}_2^{(n)} - \hat{V}_{2,predicted}^{(n)})^2 \Big) \\
&+ \sum_{1}^{120} \Big(\eta_M(M^{(n)} - M_{predicted}^{(n)})^2 + \eta_\kappa(\kappa^{(n)} - \kappa_{predicted}^{(n)})^2 + \eta_\lambda(\lambda^{(n)} - \lambda_{predicted}^{(n)})^2 \Big) \Bigg)
\end{aligned}
$$

 with the weights $\eta_{V_1} = \eta_{\hat{V}_2} = 90.090$, $\eta_M = 0.015$, $\eta_\kappa = 0.012$ and $\eta_\lambda = 0.003$ to

 account for the unequal number of data points the signals were fitted to (e.g. only two

 data points for V_1 and $\hat{V}_2$ but 120 data points for M, κ and λ) and for the unequal units

 (e.g. a saccade vector error of $3°$ should be weighted more than a peak velocity error of

 $3\frac{°}{s}$). In the inward and in the outward condition patients showed a small V_1 change in the

 opposite direction of learning. This effect was small, not significant and, thus, rather of

 random nature (see Figure 3B). In these two cases, we fitted a stable V_1 as the mean of

 the pre-saccadic target localizations between the pre- and the post-exposure phase. For

 all model fits, we set $\epsilon_m^{(n)} = 0$.

 Residual standard errors RSE were calculated, collectively for V_1, M and $\hat{V}_2$ (in $°$)

 and separately for κ (in $\frac{°}{s}$) and λ (in ms):

$$
RSE = \sqrt{\frac{SSE}{q-1}} \tag{27}
$$

 with q as the number of data points used for the respective RSE calculation.

Statistical analysis. To compare the data of one group against zero, we used two-sided one-sample t-tests or a Wilcoxon signed rank test in case normality distribution was violated. To compare data between groups, i.e. between patients and control subjects, two-sided two-sample t-tests, or, alternatively, Wilcoxon rank sum tests in case normality distribution was violated, were calculated. All tests were conducted with a significance level of 0.05.

Acknowledgements. We thank Pr. Caroline Froment-Tilikete for helping us in the recruitment and clinical evaluation of the patients, and Eric Koun and Roméo Salemme for their assistance with the technical implementation of the protocol and their advice about eye movements analysis tools.

Funding. This project has received funding from the German Research Foundation (LA952/8-1 to ML), from the French National Agency for Research (ANR-15-CE37-0014-01 to DP) and from the European Union's Horizon 2020 research and innovation programme under grant agreement No 951910. AC received a scholarship from Fondation de France Berthe Fouassier (2019, 00099566).

Competing interests. The authors declare no competing financial interests.

References

Alahyane, N., Fonteille, V., Urquizar, C., Salemme, R., Nighoghossian, N., Pelisson, D., & Tilikete, C. (2008). Separate neural substrates in the human cerebellum for sensory-motor adaptation of reactive and of scanning voluntary saccades. *The Cerebellum*, *7*(4), 595–601.

Albert, S. T., & Shadmehr, R. (2018). Estimating properties of the fast and slow adaptive processes during sensorimotor adaptation. *J. Neurophysiol.*, *119*(4), 1367–1393.

Albus, J. S. (1971). A theory of cerebellar function. *Math. Biosci.*, *10*(1-2), 25–61.

Avila, E., van der Geest, J. N., Kengne Kamga, S., Verhage, M. C., Donchin, O., & Frens, M. A. (2015). Cerebellar transcranial direct current stimulation effects on saccade adaptation. *Neural Plast.*, *2015*.

Bahcall, D. O., & Kowler, E. (1999). Illusory shifts in visual direction accompany adaptation of saccadic eye movements. *Nature*, *400*(6747), 864-866.

Bahill, A. T., Clark, M. R., & Stark, L. (1975). The main sequence, a tool for studying human eye movements. *Math. Biosci.*, *24*(3-4), 191–204.

Barash, S., Melikyan, A., Sivakov, A., Zhang, M., Glickstein, M., & Thier, P. (1999). Saccadic dysmetria and adaptation after lesions of the cerebellar cortex. *J. Neurosci.*, *19*(24), 10931–10939.

Bays, P. M., & Wolpert, D. M. (2007). Computational principles of sensorimotor control that minimize uncertainty and variability. *J. Physiol.*, *578*(2), 387–396.

Berman, R. A., Cavanaugh, J., McAlonan, K., & Wurtz, R. H. (2017). A circuit for saccadic suppression in the primate brain. *J. Neurophysiol.*, *117*(4), 1720–1735.

Blurton, S. P., Raabe, M., & Greenlee, M. W. (2012). Differential cortical activation during saccadic adaptation. *J. Neurophysiol.*, *107*(6), 1738–1747.

Bostan, A. C., Dum, R. P., & Strick, P. L. (2010). The basal ganglia communicate with the cerebellum. *PNAS*, *107*(18), 8452–8456.

Brissenden, J. A., Levin, E. J., Osher, D. E., Halko, M. A., & Somers, D. C. (2016). Functional evidence for a cerebellar node of the dorsal attention network. *J. Neurosci.*, *36*(22), 6083–6096.

Buckner, R. L., Krienen, F. M., Castellanos, A., Diaz, J. C., & Yeo, B. T. (2011). The organization of the human cerebellum estimated by intrinsic functional connectivity.

J. Neurophysiol., *106*(5), 2322–2345.

Cavanaugh, J., Berman, R. A., Joiner, W. M., & Wurtz, R. H. (2016). Saccadic corollary

discharge underlies stable visual perception. *J. Neurosci.*, *36*(1), 31–42.

Chen-Harris, H., Joiner, W. M., Ethier, V., Zee, D. S., & Shadmehr, R. (2008). Adaptive

control of saccades via internal feedback. *J. Neurosci.*, *28*(11), 2804-2813.

Cheviet, A., Masselink, J., Koun, E., Salemme, R., Lappe, M., Froment-Tilikete, C., &

Pélisson, D. (2022). Cerebellar signals drive motor adjustments and visual percep-

tual changes during forward and backward adaptation of reactive saccades. *Cereb.*

Cortex.

Cheviet, A., Pisella, L., & Pélisson, D. (2021). The posterior parietal cortex processes

visuo-spatial and extra-retinal information for saccadic remapping: A case study.

Cortex, *139*, 134–151.

Collins, T., Dore-Mazars, K., & Lappe, M. (2007). Motor space structures perceptual

space: Evidence from human saccadic adaptation. *Brain Res.*, *1172*, 32-39.

Collins, T., Semroud, A., Orriols, E., & Doré-Mazars, K. (2008). Saccade dynamics before,

during, and after saccadic adaptation in humans. *IOVS*, *49*(2), 604–612.

Crapse, T. B., & Sommer, M. A. (2008). Corollary discharge circuits in the primate brain.

Curr. Opin Neurobiol., *18*(6), 552-557.

Crapse, T. B., & Sommer, M. A. (2009). Frontal eye field neurons with spatial represen-

tations predicted by their subcortical input. *J. Neurosci.*, *29*(16), 5308–5318.

Dash, S., & Thier, P. (2013). Smooth pursuit adaptation (spa) exhibits features useful to

compensate changes in the properties of the smooth pursuit eye movement system

due to usage. *Front. Syst. Neurosci.*, *7*, 67.

Dean, P., Porrill, J., Ekerot, C.-F., & Jörntell, H. (2010). The cerebellar microcircuit as

an adaptive filter: experimental and computational evidence. *Nat. Rev. Neurosci.*,

11(1), 30–43.

Deubel, H. (1987). Adaptivity of gain and direction in oblique saccades. In *Eye movements*

from physiology to cognition (pp. 181–190). Elsevier.

Doya, K. (1999). What are the computations of the cerebellum, the basal ganglia and the

cerebral cortex? *Neural Netw.*, *12*(7-8), 961–974.

Duhamel, J. R., Colby, C. L., & Goldberg, M. E. (1992). The updating of the represen-

tation of visual space in parietal cortex by intended eye movements. *Science*, *255*,

90-92.

Ebner, T. J., & Pasalar, S. (2008). Cerebellum predicts the future motor state. *The Cerebellum*, *7*(4), 583–588.

Ethier, V., Zee, D. S., & Shadmehr, R. (2008). Changes in control of saccades during gain adaptation. *J. Neurosci.*, *28*(51), 13929–13937.

Franklin, D. W., & Wolpert, D. M. (2011). Computational mechanisms of sensorimotor control. *Neuron*, *72*(3), 425–442.

Frens, M., & Van Opstal, A. (1994). Transfer of short-term adaptation in human saccadic eye movements. *Exp. Brain Res.*, *100*(2), 293–306.

Fuchs, A. F., & Binder, M. D. (1983). Fatigue resistance of human extraocular muscles. *J. Neurophysiol.*, *49*(1), 28–34.

Gaymard, B., Rivaud-Péchoux, S., Yelnik, J., Pidoux, B., & Ploner, C. (2001). Involvement of the cerebellar thalamus in human saccade adaptation. *Eur. J. Neurosci.*, *14*(3), 554–560.

Gerardin, P., Miquée, A., Urquizar, C., & Pélisson, D. (2012). Functional activation of the cerebral cortex related to sensorimotor adaptation of reactive and voluntary saccades. *Neuroimage*, *61*(4), 1100–1112.

Golla, H., Tziridis, K., Haarmeier, T., Catz, N., Barash, S., & Thier, P. (2008). Reduced saccadic resilience and impaired saccadic adaptation due to cerebellar disease. *Eur. J. Neurosci.*, *27*(1), 132–144.

Gremmler, S., Bosco, A., Fattori, P., & Lappe, M. (2014). Saccadic adaptation shapes visual space in macaques. *J. Neurophysiol.*, *111*(9), 1846-1851.

Guillaume, A., Fuller, J. R., Srimal, R., & Curtis, C. E. (2018). Cortico-cerebellar network involved in saccade adaptation. *J. Neurophysiol.*, *120*(5), 2583–2594.

Harris, C. M., & Wolpert, D. M. (2006). The main sequence of saccades optimizes speed-accuracy trade-off. *Biol. Cybern.*, *95*(1), 21–29.

Havermann, K., & Lappe, M. (2010). The influence of the consistency of postsaccadic visual errors on saccadic adaptation. *J. Neurophysiol.*, *103*(6), 3302-3310.

Hernandez, T. D., Levitan, C. A., Banks, M. S., & Schor, C. M. (2008). How does saccade adaptation affect visual perception? *J. Vis.*, *8*(3), 1-16.

Herzfeld, D. J., Kojima, Y., Soetedjo, R., & Shadmehr, R. (2015). Encoding of action by the purkinje cells of the cerebellum. *Nature*, *526*(7573), 439–442.

Herzfeld, D. J., Kojima, Y., Soetedjo, R., & Shadmehr, R. (2018). Encoding of error and learning to correct that error by the purkinje cells of the cerebellum. *Nat. Neurosci.*, *21*(5), 736–743.

Hopp, J. J., & Fuchs, A. F. (2004). The characteristics and neuronal substrate of saccadic eye movement plasticity. *Prog. Neurobiol.*, *72*(1), 27-53.

Hoshi, E., Tremblay, L., Féger, J., Carras, P. L., & Strick, P. L. (2005). The cerebellum communicates with the basal ganglia. *Nat. Neurosci.*, *8*(11), 1491–1493.

Ignashchenkova, A., Dash, S., Dicke, P. W., Haarmeier, T., Glickstein, M., & Thier, P. (2009). Normal spatial attention but impaired saccades and visual motion perception after lesions of the monkey cerebellum. *J. Neurophysiol.*, *102*(6), 3156–3168.

Jenkinson, N., & Miall, R. C. (2010). Disruption of saccadic adaptation with repetitive transcranial magnetic stimulation of the posterior cerebellum in humans. *The Cerebellum*, *9*(4), 548–555.

Kawato, M. (1999). Internal models for motor control and trajectory planning. *Curr. Opin. Neurobiol.*, *9*(6), 718–727.

Marek, S., Siegel, J. S., Gordon, E. M., Raut, R. V., Gratton, C., Newbold, D. J., Ortega, M., Laumann, T. O., Adeyemo, B., Miller, D. B., et al. (2018). Spatial and temporal organization of the individual human cerebellum. *Neuron*, *100*(4), 977–993.

Markanday, A., Inoue, J., Dicke, P. W., & Thier, P. (2021). Cerebellar complex spikes multiplex complementary behavioral information. *PLoS Biol*, *19*(9), e3001400.

Markanday, A., Messner, J., & Thier, P. (2018). A loss of a velocity-duration trade-off impairs movement precision in patients with cerebellar degeneration. *Eur. J. Neurosci.*, *48*(4), 1976–1989.

Marr, D. (1969). A theory of cerebellar cortex. *J. Physiol.*, *202*, 437–470.

Masselink, J., & Lappe, M. (2021). Visuomotor learning from postdictive motor error. *eLife*, *10*, e64278.

McLaughlin, S. (1967). Parametric adjustment in saccadic eye movements. *Percept. Psychophys.*, *2*(8), 359-362.

Miall, R. C., Christensen, L. O. D., Cain, O., & Stanley, J. (2007). Disruption of state estimation in the human lateral cerebellum. *PLoS Biol.*, *5*(11), e316.

Middleton, F. A., & Strick, P. L. (2000). Basal ganglia and cerebellar loops: motor and cognitive circuits. *Brain Res. Rev.*, *31*(2-3), 236–250.

Middleton, F. A., & Strick, P. L. (2001). Cerebellar projections to the prefrontal cortex of the primate. *J. Neurosci.*, *21*(2), 700–712.

Miller, J. M., Anstis, T., & Templeton, W. B. (1981). Saccadic plasticity: Parametric adaptive control by retinal feedback. *J. Exp. Psychol. Hum. Percept. Perform.*, *7*(2), 356-366.

Moidell, B. G., & Bedell, H. E. (1988). Changes in oculocentric visual direction induced by the recalibration of saccades. *Vision Res.*, *28*(2), 329-336.

Nowak, D. A., Hermsdörfer, J., Rost, K., Timmann, D., & Topka, H. (2004). Predictive and reactive finger force control during catching in cerebellar degeneration. *The Cerebellum*, *3*(4), 227–235.

Ohki, M., Kitazawa, H., Hiramatsu, T., Kaga, K., Kitamura, T., Yamada, J., & Nagao, S. (2009). Role of primate cerebellar hemisphere in voluntary eye movement control revealed by lesion effects. *J. Neurophysiol.*, *101*(2), 934–947.

Ostendorf, F., Kilias, J., & Ploner, C. J. (2012). Theta-burst stimulation over human frontal cortex distorts perceptual stability across eye movements. *Cereb. Cortex*, *22*(4), 800–810.

Ostendorf, F., Liebermann, D., & Ploner, C. J. (2010). Human thalamus contributes to perceptual stability across eye movements. *PNAS*, *107*(3), 1229–1234.

Panouilleres, M., Neggers, S. F., Gutteling, T. P., Salemme, R., Stigchel, S. v. d., van der Geest, J. N., Frens, M. A., & Pelisson, D. (2012). Transcranial magnetic stimulation and motor plasticity in human lateral cerebellum: dual effect on saccadic adaptation. *Hum. Brain Mapp.*, *33*(7), 1512–1525.

Panouilleres, M., Weiss, T., Urquizar, C., Salemme, R., Munoz, D. P., & Pelisson, D. (2008). Behavioural evidence of separate adaptation mechanisms controlling saccade amplitude lengthening and shortening. *J. Neurophysiol.*, *101*(3), 1550 –1559.

Panouillères, M. T., Miall, R. C., & Jenkinson, N. (2015). The role of the posterior cerebellum in saccadic adaptation: a transcranial direct current stimulation study. *J. Neurosci.*, *35*(14), 5471–5479.

Pasalar, S., Roitman, A., Durfee, W., & Ebner, T. (2006). Force field effects on cerebellar purkinje cell discharge with implications for internal models. *Nat. Neurosci.*, *9*(11), 1404–1411.

Pelisson, D., Alahyane, N., Panouilleres, M., & Tilikete, C. (2010). Sensorimotor adapta-

tion of saccadic eye movements. *Neurosci. Biobehav. Rev.*, *34*(8), 1103-1120.

Prime, S. L., Vesia, M., & Crawford, J. D. (2010). TMS over human frontal eye fields

disrupts trans-saccadic memory of multiple objects. *Cereb. Cortex*, *20*(4), 759–772.

Prsa, M., Dicke, P. W., & Thier, P. (2010). The absence of eye muscle fatigue indicates that

the nervous system compensates for non-motor disturbances of oculomotor function.

J. Neurosci., *30*(47), 15834–15842.

Raymond, J. L., & Medina, J. F. (2018). Computational principles of supervised learning

in the cerebellum. *Annu. Rev. Neurosci.*, *41*, 233–253.

Roitman, A. V., Pasalar, S., Johnson, M. T., & Ebner, T. J. (2005). Position, direction

of movement, and speed tuning of cerebellar purkinje cells during circular manual

tracking in monkey. *J. Neurosci.*, *25*(40), 9244–9257.

Roth, M. J., Synofzik, M., & Lindner, A. (2013). The cerebellum optimizes perceptual

predictions about external sensory events. *Curr. Biol.*, *23*(10), 930–935.

Schmidt, D., Abel, L., DellOsso, L., & Daroff, R. (1979). Saccadic velocity characteristics-

intrinsic variability and fatigue. *ASEM*, *50*(4), 393–395.

Schnier, F., Zimmermann, E., & Lappe, M. (2010). Adaptation and mislocalization fields

for saccadic outward adaptation in humans. *J. Eye Mov. Res.*, *3*(4), 1-18.

Shadmehr, R., Smith, M. A., & Krakauer, J. W. (2010). Error correction, sensory predic-

tion, and adaptation in motor control. *Annu. Rev. Neurosci.*, *33*, 89–108.

Sommer, M. A., & Wurtz, R. H. (2008). Brain circuits for the internal monitoring of

movements. *Annu. Rev. Neurosci.*, *31*, 317-338.

Sperry, R. W. (1950). Neural basis of the spontaneous optokinetic response produced by

visual inversion. *J. Comp. Physiol. Psychol.*, *43*(6), 482-489.

Srimal, R., Diedrichsen, J., Ryklin, E. B., & Curtis, C. E. (2008). Obligatory adaptation

of saccade gains. *J. Neurophysiol.*, *99*(3), 1554–1558.

Straube, A., Robinson, F. R., & Fuchs, A. F. (1997). Decrease in saccadic performance

after many visually guided saccadic eye movements in monkeys. *Invest. Ophthalmol.*

Vis. Sci., *38*(13), 2810-2816.

Sultan, F., Mock, M., & Thier, P. (2000). Functional architecture of the cerebellar system.

Neurol. Dis. Therapy, *50*, 1–52.

Takagi, M., Zee, D. S., & Tamargo, R. J. (1998). Effects of lesions of the oculomotor

vermis on eye movements in primate: saccades. *J. Neurophysiol.*, *80*(4), 1911–1931.

Tanaka, H., Ishikawa, T., Lee, J., & Kakei, S. (2020). The cerebro-cerebellum as a locus of forward model: a review. *Front. Syst. Neurosci.*, *14*, 19.

Taylor, J. A., & Ivry, R. B. (2014). Cerebellar and prefrontal cortex contributions to adaptation, strategies, and reinforcement learning. *Prog. Brain Res.*, *210*, 217–253.

Thier, P., & Markanday, A. (2019). Role of the vermal cerebellum in visually guided eye movements and visual motion perception. *Annu. Rev. Vis.*, *5*, 247–268.

Tseng, Y.-w., Diedrichsen, J., Krakauer, J. W., Shadmehr, R., & Bastian, A. J. (2007). Sensory prediction errors drive cerebellum-dependent adaptation of reaching. *J. Neurophysiol.*, *98*(1), 54–62.

Umeno, M. M., & Goldberg, M. E. (1997). Spatial processing in the monkey frontal eye field. I. predictive visual responses. *J. Neurophysiol.*, *78*(3), 1373-1383.

Vahedi, K., Rivaud, S., Amarenco, P., & Pierrot-Deseilligny, C. (1995). Horizontal eye movement disorders after posterior vermis infarctions. *J. Neurol. Neurosurg. Psychiatry*, *58*(1), 91–94.

van Es, D. M., van der Zwaag, W., & Knapen, T. (2019). Topographic maps of visual space in the human cerebellum. *Curr. Biol.*, *29*(10), 1689–1694.

von Holst, E., & Mittelstaedt, H. (1950). Das Reafferenzprinzip (Wechselwirkung zwischen Zentralnervensystem und Peripherie). *Naturwissenschaften*, *37*, 464-476.

Wallman, J., & Fuchs, A. F. (1998). Saccadic gain modification: visual error drives motor adaptation. *J. Neurophysiol.*, *80*(5), 2405-2416.

Widrow, B., & Hoff, M. (1960). Adaptive switching circuits, IRE WESCON Conv. *Rec., pt*, *4*, 96.

Widrow, B., & Stearns, S. D. (1985). Adaptive signal processing prentice-hall. *Englewood Cliffs, NJ*.

Wolpert, D. M., Diedrichsen, J., & Flanagan, J. R. (2011). Principles of sensorimotor learning. *Nature Rev. Neurosci.*, *12*(12), 739–751.

Wurtz, R. H. (2008). Neuronal mechanisms of visual stability. *Vision Res.*, *48*(20), 2070–2089.

Wurtz, R. H., Joiner, W. M., & Berman, R. A. (2011). Neuronal mechanisms for visual stability: progress and problems. *Philos. Trans. R. Soc. B: Biol. Sci.*, *366*(1564), 492–503.

Xu-Wilson, M., Chen-Harris, H., Zee, D. S., & Shadmehr, R. (2009). Cerebellar contribu-

tions to adaptive control of saccades in humans. *J. Neurosci.*, *29*(41), 12930-12939.

Xu-Wilson, M., Zee, D. S., & Shadmehr, R. (2009). The intrinsic value of visual informa-

tion affects saccade velocities. *Exp. Brain Res.*, *196*(4), 475–481.

Zimmermann, E., & Lappe, M. (2009). Mislocalization of flashed and stationary visual

stimuli after adaptation of reactive and scanning saccades. *J. Neurosci.*, *29*(35),

11055-11064.

Zimmermann, E., & Lappe, M. (2010). Motor signals in visual localization. *J. Vis.*, *10*(6),

1-11.

Zimmermann, E., Ostendorf, F., Ploner, C. J., & Lappe, M. (2015). Impairment of saccade

adaptation in a patient with a focal thalamic lesion. *J. Neurophysiol.*, *113*(7), 2351–

2359.

Table 1. Fitted parameters and residual standard errors.

Condition	Group	Fitted parameters	β_0	β_κ	β_λ	$RSE_{V_1,M,\hat{V}_2}$	RSE_κ	RSE_λ
inward	con	$\alpha_v = 2.6*10^{-6},\ \alpha_m = 2.1*10^{-5},\ \alpha_{cd} = 5.9*10^{-6}$	-9.995	0.034	0.230	0.8 °	25.0 $\frac{\circ}{s}$	3.0 ms
	pat	$\alpha_v = 0,\ \alpha_m = 3.8*10^{-6},\ \alpha_{cd} = 6.7*10^{-7}$	6.399	0.011	0.110	1.1 °	59.2 $\frac{\circ}{s}$	5.1 ms
no step	con	$\gamma_\kappa = 0.003,\ \gamma_\lambda = 0.964$	9.828	0.009	0.088	0.5 °	23.7 $\frac{\circ}{s}$	3.1 ms
	pat	$\gamma_\kappa = 0.008,\ \gamma_\lambda = 0.457$	8.917	0.009	0.092	1.1 °	56.1 $\frac{\circ}{s}$	6.4 ms
outward	con	$\alpha_v = 2.3*10^{-6},\ \alpha_m = 5.5*10^{-6},\ \alpha_{cd} = 5.3*10^{-13}$	-0.847	0.018	0.208	0.6 °	21.8 $\frac{\circ}{s}$	3.9 ms
	pat	$\alpha_v = 0,\ \alpha_m = 1.4*10^{-6},\ \alpha_{cd} = 5.1*10^{-7}$	8.360	0.006	0.131	1.1 °	50.8 $\frac{\circ}{s}$	5.7 ms

Here we report the fitted parameters and residual standard errors, separately for each group and condition. The learning rates α_v, α_m and α_{cd} were fitted to the data of the inward and the outward condition, respectively. The peak velocity decay rate γ_κ and the duration compensation rate γ_λ were fitted to the data of the no step condition. The parameters β_0, β_κ and β_λ are the weights of the regression from saccade vectors on saccade peak velocities and saccade durations. Residual standard errors are reported separately for saccade vectors and pre- and post-saccadic localizations ($RSE_{V_1,M,\hat{V}_2}$), as well as for saccade peak velocities (RSE_κ) and for saccade durations (RSE_λ).

Figure 1. Experimental tasks and model framework. **(A)** In the saccade trials, subjects executed a saccade to a 20° rightward target. In the pre-exposure phase, the target was extinguished at saccade onset. In the exposure and post-exposure phase, the target either stepped 6° inward (inward condition), 6° outward (outward condition) or stayed at its initial position (no step condition). In the pre-saccadic localization trials, subjects localized a 12 ms flash with a mouse cursor while holding gaze at the fixation point. In the post-saccadic localization trials, subjects performed a saccade to a 20° rightward target and then localized the 12 ms pre-saccadic flash with a mouse cursor. The mouse cursor was a blue line pointer. The yellow circle illustrates gaze location but was not present at the stimulus display. **(B)** The target with the physical distance P_1 is represented at the location V_1 on the visuospatial map. An inverse model maps V_1 onto a motor command M. Before saccade start, a forward dynamics model transforms a copy of the motor command CD_M into visuospatial coordinates, i.e. into the computed displacement of visual space CD_V. A forward outcome model then shifts retinal coordinates by CD_V to predict the visual location of the post-saccadic target $\hat{V}_2$. For saccade execution, the motor command is transposed to saccade peak velocity κ and saccade duration λ, producing the saccade vector P_M. The actual post-saccadic target appears at retinal position V_2. A backward outcome model then postdicts the visual post-saccadic target back to pre-saccadic space $\hat{V}_1$. The visuomotor system evaluates the accuracy of the motor command with respect to the postdicted target position (E_{post}) in order to adapt its gains ω_v, ω_m and ω_{cd}. A decrease of ω_m (inward learning) is controlled by downregulating saccade peak velocity while an increase of ω_m (outward learning) is controlled by upregulation of saccade duration. When saccades are performed repetitively to the same, non-stepping target, oculomotor fatigue occurs, i.e. peak velocity declines, which is usually compensated by an increase of saccade duration.

Figure 2. Example subject data for the inward condition. Saccade vectors, pre- and post-saccadic localizations for the inward condition of **(A)** an example control subject and **(B)** an example patient. The pre-exposure phase measured subjects' baseline state without target step. The exposure phase induced saccadic learning and the post-exposure phase measured adaptation-induced changes to the saccade vector, pre- and post-saccadic localizations. Similar to the pattern that we found at group level, the patient shows less learning in the saccade vector and higher saccade endpoint variability compared to the control subject.

Figure 3. Model fits to the group data. Pre- and post-exposure mean ± standard error (dots with error bars), trial-by-trial saccade data of the exposure phase (jagged blue lines) and model fits to the data (smooth lines) for **(A)** control subjects and **(B)** cerebellar patients, separately for each condition (inward, no step, outward). (1) Visual pre-saccadic target V_1 (fitted to pre-saccadic localizations), motor command M (fitted to saccade vectors), computed displacement of visual space CD_V, postdicted pre-saccadic target $\hat{V}_1$. (2) Predicted post-saccadic target $\hat{V}_2$ (fitted to post-saccadic localizations with respect to saccade landing), visual post-saccadic target V_2. (3) Visual gain ω_v, motor gain ω_m, CD gain ω_{cd}. (4) Postdictive motor error E_{post}. (5) Saccade peak velocity κ. (6) Saccade duration λ. Asterisks indicate significant difference between the pre- and post-exposure phase with *** $p < .001$, ** $p < .01$, * $p < .05$ and n.s. $p \geq .05$.

Figure 4. Baseline state and pre- to post-exposure changes. **(A)** Baseline state of the visuomotor system averaged across the pre-exposure phases of the three conditions (mean ± standard error), separately for control subjects and patients. Group-centered asterisks indicate significant difference from 20° (V_1, M, CD_V), from 1 (ω_v, ω_m, ω_{cd}) or from zero (E_{post}). **(B)** Pre- to post-exposure changes in the inward condition. **(C)** Pre- to post-exposure changes in the no step condition. **(D)** Pre- to post-exposure changes in the outward condition. For **B-D** group-centered asterisks indicate significant difference from zero. Panel-centered asterisks above a horizontal indicate significant difference between control subjects and patients with *** $p < .001$, ** $p < .01$, * $p < .05$ and n.s. $p \geq .05$.

Figure 5. Model simulation of the patients' baseline state. Oculomotor fatigue causes a loss of saccade peak velocity κ that can only be partially compensated by upregulation of saccade duration λ. Consequently, a decline of the saccadic motor command M leads to saccade hypometry, that, in turn, results in a rise of motor errors E_{post}. Preserved long-term learning at perceptual (ω_v) and motor level (ω_m) counteracts to keep saccadic behavior calibrated. Hence, the visuomotor system stabilizes with an overestimation of the pre-saccadic target eccentricity (V_1) and recovery from saccade hypometria (M), matching the baseline state measured in cerebellar patients (ω_v, ω_m, ω_{cd}). Simulations were performed for a target of $P_1 = 10°$ eccentricity, $\boldsymbol{\omega}^{(1)} = (0.958; 1.023; 0.980)$ (which are the baseline gains measured in healthy subjects of Masselink and Lappe (2021)), $\kappa^{(1)} = 300\frac{°}{s}$, $\lambda^{(1)} = 43.9$ ms, $\gamma_\kappa = 0.008$, $\gamma_\lambda = 0.457$ (derived from the patients' model fit to the no step condition), $\kappa_{end} = 200\frac{°}{s}$, $\alpha_v = 2.35*10^{-6}$, $\alpha_m = 5.53*10^{-6}$, $\alpha_{cd} = 5.31*10^{-13}$ (derived from control subjects' model fit to the outward condition to simulate preserved long-term learning), β_0 = -11.67, $\beta_\kappa = 0.03$, $\beta_\kappa = 0.27$ (derived from the saccade vectors, saccade peak velocities and saccade durations of control subjects across all three conditions to capture a minimum range of saccade vectors).