Sequence analysis

Lokatt: A hybrid DNA nanopore basecaller with an explicit duration hidden Markov model and a residual LSTM network

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Abstract

Motivation: Basecalling long DNA sequences is a crucial step in nanopore-based DNA sequencing protocols. In recent years, the CTC-RNN model has become the leading basecalling model and has replaced prior hidden Markov models (HMMs) based on pre-segmentation of the ion current measurements. However, CTC-RNN relies on the neural network to make basecalling decisions while prior knowledge of the biological and physical processes is not involved. We believe that there are undiscovered potentials in using this prior knowledge that can benefit the basecalling performances and that HMMs can indeed be used to leverage this information if combined with an RNN in an end-to-end algorithm.

Results: We present the basecaller named **Lokatt**: explicit duration Markov model and residual-LSTM network. It is a novel basecaller structure based on an Explicit Duration HMM (EDHMM), designed to model the nanopore sequencing processes. Trained on a new library created with free-methylation Ecoli genome with MinION R9.4.1 chemistry, the Lokatt basecaller achieves basecalling performances with a median single read identity score of 92%, a genome coverage ratio of 99.750%, on par with existing state-of-the-art.

Availability: https://github.com/chunxxc/lokatt; Data is held on Zenodo, DOI:10.5281/zenodo.7970716.

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1 Introduction

The concept of nanopore-sequencing was first drafted in 1989 as a hand-sketched illustration by David Deamer on a page of a notebook [1]. 30 years later, the technology is now commercially available from Oxford Nanopore Technologies (ONT) [2]. Nanopore sequencing works by threading a single-strand DNA (ssDNA) through a protein-formed pore in a membrane, where the sequence of nucleotides along the ssDNA can be indirectly recorded through their effect on an ion current flowing through the pore. However, transforming the current measurements into a sequence of nucleotide bases, i.e., basecalling, is challenging for several reasons [3]. Firstly, multiple nucleotides along the ssDNA, also known as the k-mer where k is the number of nucleotides, simultaneously affect the noisy current measurements at any given time. Secondly, the ssDNA's

translocation speed through the pore is fast and unstable, leading to a random and apriori unknown number of current samples per nucleotide base in the measurements. Further, the short-term average translocation speed and the noise level are also variable across a long sequencing run due to slowly changing experimental conditions. These challenges made early nanopore sequencing unusable for most clinical and research applications. Although these problems have now been mitigated by, e.g., selecting and modifying various protein pores with narrower constriction, using improved DNA ratcheting enzymes to control the ssDNA's translocation speed, and better basecalling algorithms, the technology is still limited for many applications due to high error rates, amounts of material, and costs [4, 5, 6].

Early basecalling algorithms worked by first segmenting the current measurements into a sequence of probabilistic events [7]. These events were then treated as observations in a graphical model, usually in the form

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of a Hidden Markov model (HMM) with latent states representing the dominating k-mers [1, 8]. The representation of observation probabilities in HMMs went from simple Gaussian distributions parameterized by the mean and variance of the ionic current during an event [9, 10] to more elaborate models such as hierarchical Dirichlet processes [11]. With the probabilistic model in place, the final basecalling step could be completed using standard inference algorithms for HMMs, such as the Viterbi and the beam search (BS) algorithms. However, the performance of the HMM remained severely limited by the quality of the segmentation step and the choice of features used to model the distribution of the events.

To avoid the limitations of the HMM basecallers, most modern basecallers are based on deep neural networks (DNN) and now end-to-end, following the pioneering work that led to the Chiron basecaller [12]. Specifically, Chiron applied a recurrent neural network (RNN) to process the current measurements, and a connectionist temporal classification (CTC) layer from natural language processing (NLP) to replace the event-based HMM for data alignment and trained the resulting network end-to-end. The previously used event features have thus been replaced by neural networks, which obviate the need for explicit feature engineering. The ONT open-source software Bonito [13], which also uses a CTC-RNN structure and end-to-end training, performs on par with the current state-of-art commercial software Guppy, which presumably also uses a deep learning solution.

Inspired by the pioneering projects, recent research into basecallers has mainly explored variations in the neural network structure. Networks with recurrent units such as long-short term memory (LSTM) networks and RNNs, temporal convolution networks (TCNs), and attention/transformer networks such as the convolution-augmented transformer have all showed acceptable basecalling accuracy when combined with a CTC layer [14, 15, 16]. The attention structure could also be used without the CTC layer, which has shown superior performance in NLP applications [17]. Basecallers built solely with attention have, however, not yet demonstrated higher accuracy for basecalling [18], unlike in NLP applications. Natural differences between DNA and speech are likely the reason for this. Nanopore signals have vague transitions between nucleotides, especially within homopolymers or repeated sequences of purines or pyrimidines, and no clear rules of order. On the other hand, speech signals have frequency domain information that separates phonemes, word-separated sentences, and linguistic rules.

This said, the lack of linguistic rules for DNA sequences does not mean there is no prior knowledge about the process that generated the nanopore data. For example, some studies model the ratcheting enzyme, e.g., a helicase, as finite state space machines with well-defined state transition probabilities driven by ATP concentration [19]. However, it is not straightforward to incorporate such knowledge in basecallers solely built with deep learning. However, we believe that incorporating such prior knowledge could provide a pledge of in-depth understanding of nanopore sequencing and a new direction for future developments.

With this in mind, we wanted to revisit HMMs for basecalling while explicitly addressing some of the shortcomings of prior HMM basecallers. To this end, we propose a new hybrid basecaller called **Lokatt** that uses an explicit duration HMM (EDHMM) model with an additional duration state that models the dwell time of the dominating k-mer. The duration state allows the basecaller to be applied directly to the raw current measurements by circumventing the need to pre-segment the data, which was problematic in previous HMM basecallers. It also allows us to explicitly model the probability distribution of k-mer dwell times within the pore, e.g., based on a physical understanding of the ratcheting enzyme [19]. However, we

still use a neural network to estimate the individual k-mer probabilities, and we train our basecaller using end-to-end training.

We evaluate Lokatt on a methylation-free Ecoli-dataset sequence obtained with an ONT MinION device and Guppy. Benchmarked against the Guppy basecaller, a locally trained Bonito basecaller, and the default Bonito basecaller, the Lokatt provides comparable performance in raw read accuracy and consensus assembly quality. All data and code are available at https://github.com/chunxxc/lokatt.

2 The Lokatt Model

An HMM is a generative Bayesian model used to represent the relationship between a sequence of latent states, which are assumed to be generated according to a Markov process, and a corresponding sequence of observations. For the basecalling task at hand we focus on building a hierarchical HMM structure to encode the temporal dependencies between a k-mer sequence of length M, denoted by $\boldsymbol{K} \triangleq \{K_1, K_2, \ldots, K_M\}$ where $K_m \in \mathbb{K} \triangleq \{1, \ldots, 4^k\}$, and a current measurement sequence of length N, denoted by $\{X_1, X_2, \ldots, X_N\}$, where typically $M \ll N$.

The duration of any state with a self-transition in a Bayesian state-space model is always geometrically distributed. This is inconsistent with the dwell times reported for both polymers and helicases [20, 21], two popular candidates for ratcheting enzymes. This inconsistency causes basecalling errors in regions rich in homopolymers since current variations are relatively small here, implying that the basecaller can only rely on the statistical modeling of the translocation speed. We address this problem via the introduction of M explicit duration variables [22], denoted by $\boldsymbol{D} \triangleq \{D_1, D_2, \ldots, D_M\}$ where $D_m \in \mathbb{N}$. This provides flexibility in terms of assigning an arbitrary dwell-time distribution. Each pair (K_m, D_m) for $m = 1, \ldots, M$ thus encodes the mth k-mer and its dwell time. However, to encode potentially very long dwell times using a limited number of states, we will allow self-transitions between the states encoding the distribution of D_m for $m = 1, \ldots, M$.

In the following two subsections, we formalize the hybrid data model on which Lokatt is based, beginning with the EDHMM and continuing with the DNN observation model.

2.1 The EDHMM structure

We consider a hierarchical and generative Bayesian EDHMM for the nanopore data, constructed as follows. We first draw the number of k-mers, $M \in \mathbb{N}$, from some distribution $\zeta(M)$ Then, we draw the first-order Markov sequence of k-mers $\boldsymbol{K}$ starting with K_1 from a distribution $\xi_0(K_1)$ followed by recursive draws of K_m from K_{m-1} according to a conditional distribution $\xi(K_m|K_{m-1})$ for $m = 2, \ldots, M$. At the same time, we draw the sequence of dwell-times $\boldsymbol{D}$ by drawing each D_m independently from some distribution $\eta(D)$ for $m = 1, \ldots, M$. Finally, D_m measurements $X_{(m,d)}$ for $d = 1, \ldots, D_m$ are drawn for each k-mer K_m for $m = 1, \ldots, M$, from a conditional distribution $\varphi(X_{(m,d)}|K_m)$. Here the state variable d acts as a counter that counts down to the next draw of a k-mer. For notational convenience, we let $\boldsymbol{X}$ denote the sequence of measurements in the order of which they would be obtained, i.e.,

$$\boldsymbol{X} \triangleq \left\{ X_{(1,D_1)}, \ldots, X_{(1,1)}, X_{(2,D_2)}, \ldots, X_{(M,D_M)}, \ldots, X_{(M,1)} \right\},$$

and use simply X_n for $n = 1, \ldots, N$, where $N = \sum_{m=1}^{M} D_m$, when speaking of the nth consecutive measurement. The joint probability distribution of the model is given in Eq. (1).

$$p(\boldsymbol{X}, \boldsymbol{K}, \boldsymbol{D}) = \zeta(M) \times \underbrace{\xi_0(K_1) \prod_{m=2}^{M} \xi(K_m|K_{m-1})}_{\text{Transition model}} \times \underbrace{\prod_{m=1}^{M} \eta(D_m)}_{\text{Duration model}} \times \underbrace{\prod_{m=1}^{M} \prod_{d=1}^{D_m} \varphi(X_{(m,d)}|K_m)}_{\text{Observation model}} \tag{1}$$

Fig. 1. Illustration of EDHMM structure, with example of $\mathbf{K}_3 = \{K_1, K_2, K_3\}$ and $\mathbf{X}_5 = \{X_1, \ldots, X_5\}$, hence $M = 3$, $\bar{D} = 2$ and $N = 5$. States in the upper half represent $(K_m, d = 1)$ while states in lower half represent $(K_m, d = 2)$. The blue path goes through five states $(K_1, d = 2)$, $(K_1, d = 1)$, $(K_2, d = 2)$, $(K_2, d = 1)$, $(K_3, d = 1)$, representing the sequence of pairs $(K_1, D_1 = 2)$, $(K_2, D_2 = 2)$, $(K_3, D_3 = 1)$; The yellow path goes through $(K_1, d = 1)$, $(K_2, d = 1)$, $(K_3, d = 2)$, $(K_3, d = 1)$, representing the sequence of pairs $(K_1, D_1 = 1)$, $(K_2, D_2 = 1)$, $(K_3, D_3 = 3)$.

To allow for computationally efficient inference using the model, we make two additional assumptions on the model: First, we assume that the sequence length is geometrically distributed such that $\zeta(M) = (1 - \alpha)\alpha^M$ for some $\alpha \in [0, 1)$; Second, we assume the duration distribution has a geometric tail such that $\eta(D + 1) = \gamma\eta(D)$ for all $D \geq \bar{D}$ for some $\gamma \in [0, 1)$ for an arbitrary $\bar{D} \in \mathbb{N}$. The value of these assumptions is that they are inherently encoded in a *finite* state-space model using self-transitions between states. The generative model can, with these assumptions, be encoded as a state model with a start state A, an end state B, and $|\mathbb{K}| \times \bar{D}$ intermediate state pairs (K, d) representing joint k-mer and duration states. The intermediate states are stochastically reset according to the explicit duration probability η upon drawing new k-mers. The set of paths from A to B is isomorphic with the set of pairs $(\boldsymbol{K}, \boldsymbol{D})$, and a pair can be drawn from $p(\boldsymbol{K}, \boldsymbol{D})$ by a random walk from A to B with the following state transition rules:

1. State A transitions into state (K_1, d) with probability $\alpha\xi_0(K_1)\eta(D = d)$ for any $d = 1, \ldots, \bar{D} - 1$, into state $(K_1, \bar{D})$ with probability $\alpha(1 - \gamma)^{-1}\xi_0(K_1)\eta(\bar{D})$, and directly into state B with probability $1 - \alpha$.

2. State (K_m, d) deterministically transitions into state $(K_m, d - 1)$ with the same k-mer for any $K_m \in \mathbb{K}$, $d = 2, \ldots, \bar{D} - 1$, and $m \geq 1$.

3. State $(K_m, \bar{D})$ self transition into state $(K_m, \bar{D})$ with the same k-mer with probability γ for any $K_m \in \mathbb{K}$, and transitions into state $(K_m, \bar{D} - 1)$ with probability $1 - \gamma$.

4. State $(K_{m-1}, 1)$ transitions into state (K_m, d) with new drawn k-mer with probability $\alpha\xi(K_m|K_{m-1})\eta(d)$ for any $(K_{m-1}, K_m) \in \mathbb{K} \times \mathbb{K}$ and $d = 1, \ldots, \bar{D} - 1$, transitions into state $(K_m, \bar{D})$ with probability $\alpha(1 - \gamma)^{-1}\xi_0(K_m|K_{m-1})\eta(\bar{D})$, and transitions into state B with probability $1 - \alpha$.

The state-space model is a standard implementation of an EDHMM [22]. The mth time the process returns to a state of the form $(K_m, 1)$ for $K_m \in \mathbb{K}$ marks the end of k-mer K_m in the data. Each measurement, $X_n = X_{(m,d)}$, can also be drawn directly based on the value of state

(K_m, d), although we, in our particular implementation, assume that the observations are independent of d.

The value of the state-space representation is that it allows for efficient inference while maintaining model interpretability [23]. From the specific model presented above, the EDHMM can be constructed into a graph with size $(M \times \bar{D}) \times N$, as illustrated in Fig. 1. The joint data likelihood and k-mer sequence $p(\mathbf{K}, \mathbf{X})$ can, using this graph, be efficiently computed with Eq. (1) by applying the forward algorithm [24, 25]. The data likelihood $p(\mathbf{X})$ can, similarly, be efficiently computed by applying the forward algorithm to a slightly altered graph, where $K_m \in \mathbb{K}$ can be arbitrary. The two graphs are sometimes referred to as the *clamped* and *free-running* models, respectively [24, 25], and allow us to efficiently compute the posterior sequence likelihood as $p(\mathbf{K}|\mathbf{X}) = p(\mathbf{K}, \mathbf{X})/p(\mathbf{X})$. The conditionally most likely sequence of states and dwell-times $(\boldsymbol{K}, \boldsymbol{D})$ can be computed using the Viterbi algorithm, and the conditionally most likely sequence of states $\boldsymbol{K}$ can be approximately obtained using any of our recently introduced marginalized BS algorithms [26].

Choosing the exact distributions in the model are also rather straightforward. The k-mer transition probabilities $\xi(K_m|K_{m-1})$ can, for example, be estimated with a maximum likelihood (frequency counting) estimator from a reference genome; or by using uniform probabilities for k-mers K_m that originate from K_{m-1}, e.g., set to $\frac{1}{4}$ for each possible one-base transition and zero for any other combination, in order not to bias the model towards any particular genome. The value of α needs to be set very close to 1 for the model to plausibly generate reads on the order of hundreds of thousands of bases, and for all intents and purposes, one can set $\alpha = 1$ in the implementation of the inference algorithms which we also do, although this does, strictly speaking, lead to an ill-defined prior distribution. The dwell-time distribution $\eta(D_m)$ can be estimated from sequences realigned at the sample-to-k-mer level. In the particular realization of Lokatt studied herein, we use a log-logistic distribution for η with parameters estimated using linear regression from the average number of large changes in the signal amplitude per sample. At the same time, we choose the tail factor γ so that $\eta(D)$ provides a representative mean dwell time. We also perform a read-specific duration estimation during training and inference in our implementation since the average duration is longer for reads obtained later during the sequencing run due to ATP depletion. Finally, we replaced $\varphi(X_{(m,d)}|K_m)$ with

scores obtained from a match network $\varphi_{n,K}^{\theta}(\mathbf{X})$, where $K \in \mathbb{K}$, $n = 1, \ldots, N$ and where θ are the trainable weights of the (match) DNN described next.

2.2 The DNN structure

Lokatt relies on a neural network to dynamically extract the features from the current signal, then map them into scores associated with each k-mer, i.e., $\varphi_{n,K}^{\theta}(\mathbf{X})$. As we want the basecaller to be capable of handling various lengths of inputs, we construct a network with convolution kernels and recurrent units. In particular, we use two types of blocks: i) two residual-convolution blocks consisting of three convolution layers, with $32, 64, 32$ features respectively, and a skip connection [27]; and ii) two bi-directional LSTM blocks [28], with 256 features in the first block on each direction and 1024 for the second block. In the end, a dense layer is applied to map the $2 \times 1024 = 2048$ features into $|\mathbb{K}| = 4^k$ dimensions, which in Lokatt is 1024 with $k = 5$. Lokatt contains two of each block types, resulting in a total of 15.3 million weights. The complete network is shown in Fig. 2 with a decomposition of the residual-convolution block and the bi-directional LSTM block. We used Swish activation, which nonlinearly interpolates between a linear function and the ReLU function [29, 30] between each layer in the network.

2.3 Model training

The weights in Lokatt's DNN are trained end-to-end with (semi)-supervised learning using a modified conditional maximum likelihood (CML) approach. The vanilla CML objective maximizes the conditional log-likelihood, i.e. $\log p(\mathbf{K}|\mathbf{X})$, which is often decomposed as $\log p(\mathbf{K}|\mathbf{X}) = \log p(\mathbf{K}, \mathbf{X}) - \log p(\mathbf{X})$. Then the clamped model is used to compute $\log p(\mathbf{K}, \mathbf{X})$ and the free-running model is used to compute $\log p(\mathbf{X})$, respectively, the former with latent states representing the particular target k-mer sequence and the latter with latent state from $\mathbb{K}$ representing all possible sequences. Through the two graphs, the gradients can be computed with respect to $\varphi_{n,K}^{\theta}(\mathbf{X})$ and passed down to update the weights in the DNN with back-propagation [25].

During the training of Lokatt, we realized that this strategy led to a network that did not generalize well and gave low final scores. In a sense, the model learned to maximize $\log p(\mathbf{K}|\mathbf{X})$ by minimizing $\log p(\mathbf{X})$ and hence did not provide a very good model of the data. This leads the neural network to output low values of the score $\varphi_{n,K}^{\theta}(\mathbf{X})$ overall. Therefore, we instead adopted a modified CML training strategy, where we maximized a weighted linear combination of $\log p(\mathbf{K}|\mathbf{X})$ and $\log p(\mathbf{X})$ to regularize the model to provide a balance between posterior decisions and modeling of the data. In particular, we explicitly used

$$\log p(\mathbf{K}|\mathbf{X}) + \lambda \log p(\mathbf{X}) = \log p(\mathbf{K}, \mathbf{X}) - (1 - \lambda) \log p(\mathbf{X})$$

with regularization factor $\lambda = \frac{1}{2}$ as the overall cost function. We also trained the network with a cost function where $p(\mathbf{X})$ was replaced by $p(\mathbf{K}_{\mathrm{BS}}, \mathbf{X})$, i.e, with

$$\log p(\mathbf{K}, \mathbf{X}) - (1 - \lambda) \log p(\mathbf{K}_{\mathrm{BS}}, \mathbf{X}), \tag{2}$$

again with $\lambda = \frac{1}{2}$, but where $\mathbf{K}_{\mathrm{BS}}$ is the output sequence of k-mers from the local focus BS (LFBS) decoder presented in Section 3.4 and discussed in detail in [26]. The intuition behind Eq. (2) is to make the training focus more on segments of the data where $\mathbf{K}_{\mathrm{BS}}$ differ from the (correct) reference sequence $\mathbf{K}$. The model trained with this approach showed higher final basecalling accuracy. Therefore, it was used to benchmark Lokatt with the other basecallers.

3 Methods

3.1 Data generation

To be able to evaluate Lokatt, we sequenced *E.coli* non-methylated genomic DNA (D5016, Zymo Research) at two dates using an ONT MinION device. The reason for the choice of DNA was that we initially thought that DNA methylation might play a more important role when basecalling than it did in the end. We also performed short-read Illumina sequencing on the same sample using the TruSeq PCR-free library preparation on the MiSeq sequencing platform (Illumina, USA). For the purpose of estimating the basecalling accuracy, coverage, and contiguity, we constructed a draft assembly from the Illumina sequencing results using SPAdes v3.6.0 [31] and used it as the reference genome.

The sequencing libraries were prepared by fragmenting the genomic DNA using Covaris g-TUBE and a Ligation sequencing kit (SQK-LSK109, Oxford Nanopore). The first sequencing run was performed in December 2019 using Flow Cell chemistry R9.4.1 and basecalled using Guppy 3.2.2. The second sequencing run was performed in November 2021 using Flow Cell chemistry R9.4.1 and basecalled with Guppy 5.0. The reason for performing the second sequencing run was to, first of all, obtain a more recent comparison to the state-of-the-art commercial software, as well as to provide separate data sets for training and evaluation.

The data were divided into training and testing batches based on their position on the genome. We divided the data from the 2019 sequencing run into batch 1.A and batch 1.B, by separating reads corresponding to the first and second half of the reference genome, respectively. The 2021 sequencing run was similarly divided into batch 2.A and batch 2.B. The data in batch 1.A was used as training data for the model, while the remaining batches were used for validation and performance evaluations. This allowed us to ensure that the model was not over-fitted to the underlying genome by comparing the performance on batch 2.A, where an obvious homology exists, with the performance on batch 1.B and 2.B where no clear homology between the training and test data should exist. Similar data division strategies have been used for human genome data sets, where the training and testing were based on different chromosomes [18].

3.2 Data preparation and DNN pre-training

We obtained a ground-truth nucleotide sequence for each raw read by mapping a tentative read from Guppy to the reference genome with `Minimap2` [32]. We next obtained a sample-to-k-mer level re-alignment using an early implementation of our EDHMM basecaller, which used an observation probability table obtained by applying the Baum-Welch algorithm [24, 25] instead of a dynamic output from a neural network. The Lokatt model, once in existence, could also be used for this purpose as alignment information is an inherent part of the model.

Based on the alignment, we divided the long reads into segments of 4096 samples with corresponding reference sequences to enable parallel computation with GPUs. A small portion of re-aligned training data was first used to pre-train the neural network structure to reduce the total training time of the computationally costly modified CML training. We trained the network to predict the corresponding k-mer per sample probabilities using a cross-entropy loss.

3.3 End to end training

As described in section 2.3, training with the regularized CML loss from Eq. (2) requires two graphs representing $p(\mathbf{K}, \mathbf{X})$ and $p(\mathbf{K}_{\mathrm{BS}}, \mathbf{X})$ to compute the gradients with respect to the output of the DNN, i.e., $\varphi_{n,K}^{\theta}(\mathbf{X})$, for $n = 1, \ldots, N$. Note here that while $p(\mathbf{X})$ is usually computed using the free running mode, we use the clamped model for both $p(\mathbf{K}, \mathbf{X})$ and $p(\mathbf{K}_{\mathrm{BS}}, \mathbf{X})$. In our implementation, the size of the

Fig. 2. The overall structure of the Basecaller: A. The main components of Lokatt, from the bottom up, are normalized input, the neural network, the EDHMM layer, and output. The neural network is expanded into main component layer blocks on the right side: two residual blocks, two bi-directional LSTM clocks, and a dense layer. B. The inner structure of the residual block consists of three layers of 1D convolution, followed by layer-normalization, and the Swish activation, of which the outputs are taken and added with the inputs of the residual block followed by cross-layer normalization. C. The inner structure of the bi-directional LSTM layer consists of two independent LSTM layers, one in the forward direction and the other in the backward direction. The outputs of the two LSTM layers are then concatenated along the feature dimension, making the output sequence the same length as the inputs.

two graphs are $\bar{D} \times M \times 4096$ and $\bar{D} \times M_{\text{BS}} \times 4096$, where the lengths of $\mathbf{K}$ and $\mathbf{K}_{\text{BS}}$, i.e., M and M_{BS}, are on the order of a few hundred bases of overlapping k-mers. To manage the complexity of the inference on these graphs, we rely on custom GPU implementations that can efficiently utilize the sparsity of the graphs. In particular, we implemented the gradient calculation for the EDHMM as custom CUDA kernels [33] and registered them as customized operations in Tensorflow2 [34]. The gradients are then back-propagated to the DNN to calculate weight updates using a standard batch-based Adam optimizer [35] from Tensorflow. We trained the whole DNN on the NSC Berzelius compute cluster using 8 Nvidia A100 GPUs [1], for which training on one epoch of data took 576 GPU hours. The CUDA kernel code is available in the Lokatt repository: https://github.com/chunxxc/lokatt.

3.4 Decoding with the LFBS

The final task of basecalling, also known as *decoding*, is to find the sequence of k-mer with the highest posterior probability, i.e. $\mathbf{K} = \arg\max_{\mathbf{K}} p(\mathbf{K}|\mathbf{X})$). The optimal solution to this problem is intractable. It essentially requires an exhaustive search over all possible k-mer sequences of length $M \leq N$, which is infeasible. The Viterbi algorithm, popular for its low complexity, can not solve the target decoding problem using the EDHMM graph. It will instead find the *jointly* optimal sequence $(\mathbf{K}, \mathbf{D})$ that maximizes $p(\mathbf{K}, \mathbf{D}|\mathbf{X})$. However, decoding the optimal k-mer sequence requires marginalizing over the duration states, for which the Viterbi algorithm has no strategy.

We instead rely on our newly proposed marginalized BS algorithms [26], which approximates the maximum a posteriori solution

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[1] Berzelius: https://www.nsc.liu.se/support/systems/berzelius-getting-started/

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by recursively marginalizing the probabilities over a fixed-size list of k-mer sub-sequences $\mathbf{K}_m \triangleq (K_1, \ldots, K_m)$ for $m \leq n$, i.e., *beams*, with high posterior probability $p(\mathbf{K}_m|\mathbf{X}_n)$ for $\mathbf{X}_n \triangleq (X_1, \ldots, X_n)$ and $m \leq n$. Each beam also keeps track of the probability of $p(\mathbf{K}_m, D_m|X_n)$ from which it can compute the probability of new beams and marginalize over D_m as needed. From experimental experience, we know that the greedy marginalized BS (GMBS) algorithm performs similarly to the Viterbi algorithm on our particular EDHMM when we use at least 512 beams, which already have a significant memory footprint. The GMBS performances can be improved by increasing the number of beams, but the pruning and sorting operations inherent to the algorithm become prohibitively slow as sorting complexity scales up to, for a beam list size of B, $\mathcal{O}(B \log(B))$ in a sequential implementation and $\mathcal{O}(log^2 B)$ in a parallel implementation [36].

To alleviate these issues, we introduced the LFBS algorithm [26] based on the intuition that the correlation between decoding errors reduces quickly over time [26]. Since the sequence to be decoded is handled at the k-mer level, errors can be identified and corrected locally without significantly affecting other k-mers in the sequence. The difference to the GMBS algorithm is that LFBS discriminates between beams according to their ending k-mer at the current position during forward propagation and only sorts and prunes the leaf beams according to their end state, similar to the maximum forward propagation in the Viterbi algorithm. We have experimentally observed that the LFBS algorithm achieves the same performance as GMBS decoding.

The LFBS has obvious benefits in terms of complexity as it is computationally much simpler to in parallel sort the B groups of size (at most) 5 rather than finding the B globally best beams in a list of length $5B$. There is, however, also a more nuanced benefit to inference performance as the LFBS algorithm will keep a beam list with a much more diverse set of tail k-mers K_{m_b}.

In implementing the LFBS algorithm, we use a tree structure to store $\mathbf{K}_m$ in memory, where common ancestry represents common initial substrings of $\mathbf{K}_m$. Since this tree has at most $N \times B$ nodes, it can be efficiently implemented on the GPUs without needing dynamic memory allocation. Finally, to extract the final approximate maximum a posteriori k-mer sequence $\mathbf{K} = \mathbf{K}_M$, we can read this tree backwards from the highest-scoring leaf node to the root in a fashion similar to the backtracking step of the Viterbi algorithm. A detailed explanation of the LFBS algorithm is provided in [26].

4 Results

4.1 Benchmarking

We benchmark the Lokatt basecaller with ONT's Guppy and Bonito basecallers. Guppy 5.0 is ONT's current commercial basecaller, which we only had access to for the 2.A and 2.B data batches. The 1.A and 1.B batches were sequenced with Guppy 3.2.2, whose performance is $2\% - 5\%$ lower than Guppy 5.0 and therefore disregarded in the benchmark. Bonito is an open-source research tool released by ONT that has been actively updated recently. We take a model from Bonito release 0.5.0, choose $dna\_r9.4.1\_e8\_sup@v3.3$, and refer to this as 'Bonito Sup' in what follows as it is supposed to give 'super accuracy' [13] for the $r9.4.1$ pore used in this project. We also trained a Bonito model from scratch using the same basecaller model structure as Bonito Sup, but with the data used in Lokatt's training. We will refer to this as 'Bonito Local'. Bonito Local and Bonito Sup thus use the same decoding strategy. The only difference is that ONT trained Bonito Sup on a different, presumably larger, data set. Both Lokatt and Bonito Local were trained over 5 epochs of training data before they started to over-fit.

In the following section, we will discuss the basecalling quality in terms of raw read identities and assembly results.

4.2 Raw read accuracy

The evaluation of basecalling performance is measured in terms of sequence accuracy, output base length per read, the total number of mapped reads and bases. We define the sequence accuracy in terms of the identity score to be the ratio between the number of matches and the total alignment columns:

$$\text{identity} = \frac{\text{matches}}{\text{matches} + \text{mismatches} + \text{insertions} + \text{deletions}},$$

where the alignment columns are obtained by measuring the Levenshtein distance between the basecalled sequences of bases and the Illumina reference genome, i.e., the minimal number of single-state edits (insertions, deletions or substitutions) required to change the former to the latter [37]. The alignments are obtained with Minimap2 v.2.17-r941 using the default parameters [32]. The training performance with the 1.A data set is reported in Table. 1. The testing performances with 1.B, 2.A, 2.B are reported in Table. 2, Table. 3 and Table. 4 respectively. Results with Guppy 5.0 are included in the latter two tables.

Overall the two basecallers provided by ONT, Guppy 5.0 and Bonito Sup, give better performance than the two locally trained basecallers. Bonito Sup, with weights provided by ONT, gives the best basecalling performance for all tests, achieving identity 1.5%-2.7% higher than the rest of the basecallers and outputs 100 to 500 more bases per read. Bonito Sup is significantly better than Bonito Local, despite using the same model structure, and it is plausible that Lokatt would also benefit from training on a larger or different data set. However, since the training data and tuning strategy used for Bonito Sup is not publicly available, we could not assess this hypothesis.

Both Lokatt and Bonito Local are evaluated at the point before they overfit the training data set, which is illustrated by similar training and testing performances. Between the two basecaller trained with local data, Lokatt achieves higher raw read identity and more mapped bases than Bonito Local. For data set 1.A and 1.B Lokatt did, however, basecall fewer reads, although it achieved a longer average read length than Bonito Local.

We also observed that, during the training procedure of Lokatt, the pre-trained neural network could already achieve a median basecalling accuracy of around 90.5% when coupled with the EDHMM. The regularized CML training increased the median identity score by around 2.0%. Finally, by comparing Tables 1 and 3 with Tables 2 and 4, it is clear that the performance of the Lokatt base-caller is not due to it learning to repeat the reference genome.

Table 1. Training performances on data batch 1.A

Basecaller	identity	read length	total reads	bases (10^9)
Lokatt	0.909/0.925	6073/4738	453103	2.751
Bonito_Local	0.898/0.913	5901/4581	454202	2.680
Bonito_Sup	0.923/0.942	6067/4672	464310	2.817

*identity and read length are listed as 'mean/median'.

Table 2. Testing performances on data batch 1.B

Basecaller	identity	read length	total reads	bases (10^9)
Lokatt	0.910/0.925	6112/4823	376431	2.301
Bonito_Local	0.896/0.911	5928/4661	377161	2.235
Bonito_Sup	0.923/0.942	6105/4759	385767	2.355

*identity and read length are listed as 'mean/median'.

Table 3. Testing performances on data batch 2.A

Basecaller	identity	read length	total reads	bases (10^9)
Lokatt	0.904/0.933	5068/2810	1317777	6.679
Bonito_Local	0.904/0.928	4876/2474	1273413	6.209
Bonito_Sup	0.930/0.966	5107/2745	1370574	7.000
Guppy 5.0	0.908/0.936	5070/2781	1320641	6.696

*identity and read length are listed as 'mean/median'.

Table 4. Testing performances on data batch 2.B

Basecaller	identity	read length	total reads	bases (10^9)
Lokatt	0.904/0.932	5397/3175	1290218	6.964
Bonito_Local	0.902/0.925	5185/2833	1247460	6.469
Bonito_Sup	0.931/0.966	5422/3076	1346139	7.300
Guppy 5.0	0.908/0.935	5395/3138	1293809	6.981

*identity and read length are listed as 'mean/median'.

4.3 Basecaller complexity

Bonito utilizes the CTC-Conditional Random Field [38] structure on top of 3 convolution layers and 5 LSTM layers alternating in forward and reverse directions, totaling 26.9 million parameters. Despite being nearly twice large as Lokatt with 15.3 million parameters, Bonito is roughly 30 times faster than Lokatt in decoding speed. The high decoding speed results from a smaller CTC graph in Bonito and, thereby, a fast decoding algorithm. Firstly, Bonito's DNN runs with a stride of 5, reducing the costly recurrent computation and shortening the CTC graph size for decoding. Secondly, the CTC graph has only 5 states: blank and 1-mers, i.e., single nucleotides, while Lokatt uses 1024 5-mer states. Therefore, using the Viterbi algorithm in the CTC graph is sufficient, where it is equivalent to just taking the maximum output per sample.

We choose to proceed with k-mer instead of a single nucleotide as used in CTC to gain a high resolution per sample which will benefit the local-focus decoding algorithm. Using k-mer, however, requires a large-sized graph, i.e., a graph of size $4^k \times N$, leading to a computationally expensive and slow inference process. However, it is certainly within the capability of modern GPUs. We have observed that the main bottlenecks are, in fact, the N times recurrent calculation in the LSTM layer and the estimation of the duration distribution.

Theoretically, Lokatt could also adapt the striding structure and use a smaller k to reduce the graph size. However, we consider the main point of this project to be the introduction of a computational model which can explicitly leverage prior knowledge of the nanopore device. Thus, we did not spend further resources to improve the basecalling speed.

4.4 Consensus evaluation

The basecalled read sequences from Bonito Sup, Bonito Local, Guppy 5.0, and Lokatt were compiled into a single fasta file, respectively. The resulting four draft genome assemblies were produced using de novo assembly in Flye [39]. The assemblies were evaluated against the assembled reference Illumina *E.coli* genome using Quast [40]. The Lokatt assembly displayed a genome coverage of 99.750% (Fig. 3a) as compared to 99.757% in assemblies from other basecallers, with each basecaller exhibiting similar GC percentage (Fig. 3b). Fig. 3c shows the NGAx plot for assemblies from all the basecallers, where the NGA50 value for Bonito default was 106360, 106277 for Bonito local, 106101 for Lokatt and 106293 for Guppy 5.0 (Fig. 3d). Lokatt performed better at managing misassemblies (Fig. 3e) as it had lower values than the other basecaller performances. Lokatt also performed quite well in the Mismatches per 100 kilo base pair (kbp) metric (Fig. 3f) with a value of 8.22, which was close to Guppy's value of 8.14 and is the best in this metric.

5 Discussion

In this project, we have designed, trained, and tested a hybrid basecaller, **Lokatt,** with a performance that is at least as good as the CTC-CRF structured Bonito basecaller trained on the same data set and comparable to the ONT-trained Bonito and Guppy basecallers. Lokatt's consensus evaluation metrics were similar to the other three basecaller assemblies. In addition, Lokatt had a lower number of misassemblies and mismatches per 100 kbp, which makes it an attractive basecalling tool.

Lokatt and Bonito differ not just in model design but also in training strategy. Bonito utilizes the CTC loss, where a blank state is manually inserted between every nucleotide. Hence the reference sequence, including the problematic homopolymers, is divided into single bases. The CTC loss typically leads to a dominance of blank predictions in the output of the CTC trained RNN [12]. One interpretation is that the RNN has learned to detect the transition moment of the nucleotides and

treat everything else as blank, which is presumably a less complicated task compared with learning the complete characteristic of the measurements as given by the ion current through the nanopore and ratcheting enzyme. However, the dominance of blank predictions could limit the model design and make it more difficult to incorporate changes in the sequencing device.

On top of the CTC loss, the training criteria share a similarity. Specifically, Bonito is trained with a conditional random field (CRF) loss [38], which is equivalent to the CML loss on an undirected graph model such as the CTC graph. In Lokatt's implementation, we have regularized the CML loss with the data likelihood. We have observed that the best regularization factor λ depends on the specific model, e.g., replacing our CNN-LSTM model with a U-net model requires a higher factor than $\lambda = \frac{1}{2}$. One plausible reason that the regularization is needed in the first place could be the mismatch between the model and the real device, like the assumption of independence between the duration distribution and the k-mer and between the duration state and the observations. In future versions of Lokatt, we would like to lift the constraints of the EDHMM design and replace it with a more dynamic structure based on more prior knowledge about the sequencing device and chemistry.

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References

[1] D. Deamer, M. Akeson, and D. Branton, "Three decades of nanopore sequencing," pp. 518–524, 5 2016.

[2] M. Jain, H. E. Olsen, B. Paten, and M. Akeson, "The Oxford Nanopore MinION: delivery of nanopore sequencing to the genomics community," *Genome Biology*, vol. 17, 12 2016.

[3] D. Branton, D. W. Deamer, A. Marziali, H. Bayley, S. A. Benner, T. Butler, M. D. Ventra, S. Garaj, A. Hibbs, X. Huang, S. B. Jovanovich, P. S. Krstic, S. Lindsay, X. S. Ling, C. H. Mastrangelo, A. Meller, J. S. Oliver, Y. V. Pershin, J. M. Ramsey, R. Riehn, G. V. Soni, V. Tabard-Cossa, M. Wanunu, M. Wiggin, and J. A. Schloss, "The potential and challenges of nanopore sequencing." *Nature biotechnology*, vol. 26, pp. 1146–53, 10 2008.

[4] D. Sheka, N. Alabi, and P. M. Gordon, "Oxford Nanopore sequencing in clinical microbiology and infection diagnostics," *Briefings in Bioinformatics*, vol. 22, 9 2021.

Fig. 3. Performance plots for basecallers: A. Genome coverage ratios. B. The number of windows for each GC percentage. C. NGAx plots for the different assemblies showing the aligned contig length distribution against the reference genome. D. The NGA50 plot. E. The misassemblies. F. The mismatches per 100 kbp.

[5] Y. Wang, Y. Zhao, A. Bollas, Y. Wang, and K. F. Au, "Nanopore sequencing technology, bioinformatics and applications," *Nature Biotechnology*, vol. 39, pp. 1348–1365, 11 2021.

[6] N. Sanderson, N. Kapel, G. Rodger, H. Webster, S. Lipworth, T. Street, T. Peto, D. Crook, and N. Stoesser, "Comparison of R9.4.1/Kit10 and R10/Kit12 Oxford Nanopore flowcells and chemistries in bacterial genome reconstruction," *Microbial genomics*, Jan 2023.

[7] F. Rang, W. Kloosterman, and J. De Ridder, "From squiggle to basepair: Computational approaches for improving nanopore sequencing read accuracy," *Genome Biology*, vol. 19, 07 2018.

[8] P. Goyal, P. V. Krasteva, N. V. Gerven, F. Gubellini, I. V. D. Broeck, A. Troupiotis-Tsaïlaki, W. Jonckheere, G. Péhau-Arnaudet, J. S. Pinkner, M. R. Chapman, S. J. Hultgren, S. Howorka, R. Fronzes, and H. Remaut, "Structural and mechanistic insights into the bacterial amyloid secretion channel CsgG," *Nature*, vol. 516, pp. 250–253, 12 2014.

[9] N. J. Loman, J. Quick, and J. T. Simpson, "A complete bacterial genome assembled de novo using only nanopore sequencing data," *Nature Methods*, vol. 12, pp. 733–735, 7 2015.

[10] C. L. C. Ip, M. Loose, J. R. Tyson, M. D. Cesare, B. L. Brown, M. Jain, R. M. Leggett, D. A. Eccles, V. Zalunin, J. M. Urban, P. Piazza, R. J. Bowden, B. Paten, S. Mwaigwisya, E. M. Batty, J. T. Simpson, T. P. Snutch, E. Birney, D. Buck, S. Goodwin, H. J. Jansen, J. O'grady, and H. E. Olsen, "MinION analysis and reference consortium: Phase 1 data release and analysis," *F1000Res.*, 2015.

[11] A. C. Rand, M. Jain, J. M. Eizenga, A. Musselman-Brown, H. E. Olsen, M. Akeson, and B. Paten, "Mapping dna methylation with high-throughput nanopore sequencing," *Nature Methods*, vol. 14, pp. 411–413, 2 2017.

[12] H. Teng, M. D. Cao, M. B. Hall, T. Duarte, S. Wang, and L. J. Coin, "Chiron: translating nanopore raw signal directly into nucleotide sequence using deep learning," *GigaScience*, 2018.

[13] O. N. T. plc., "Nanoporetech/bonito: A Pytorch basecaller for Oxford Nanopore reads." https://github.com/nanoporetech/bonito, Feb. 2020.

[14] J. Zeng, H. Cai, H. Peng, H. Wang, Y. Zhang, and T. Akutsu, "Causalcall: Nanopore basecalling using a temporal convolutional network," *Frontiers in Genetics*, vol. 10, 1 2020.

[15] X. Lv, Z. Chen, Y. Lu, and Y. Yang, "An end-to-end Oxford Nanopore basecaller using convolution-augmented transformer." Institute of Electrical and Electronics Engineers Inc., 12 2020, pp. 337–342.

[16] N. Huang, F. Nie, P. Ni, F. Luo, and J. Wang, "SACall: a neural network basecaller for Oxford Nanopore sequencing data based on self-attention mechanism," *IEEE/ACM Transactions on Computational Biology and Bioinformatics*, 2020.

[17] A. Vaswani, G. Brain, N. Shazeer, N. Parmar, J. Uszkoreit, L. Jones, A. N. Gomez, Łukasz Kaiser, and I. Polosukhin, "Attention is all you need," 2017.

[18] H. Konishi, R. Yamaguchi, K. Yamaguchi, Y. Furukawa, and S. Imoto, "Halcyon: An accurate basecaller exploiting an encoder–decoder model with monotonic attention," *Oxford Bioinformatics*, vol. 37, no. 9, pp. 1211–1217, 2020.

[19] J. M. Craig, A. H. Laszlo, H. Brinkerhoff, I. M. Derrington, M. T. Noakes, I. C. Nova, B. I. Tickman, K. Doering, N. F. D. Leeuw, and J. H. Gundlach, "Revealing dynamics of helicase translocation on single-stranded DNA using high-resolution nanopore tweezers," *PNAS*, vol. 114, pp. 11 932–11 937, 2017.

[20] P. Sarkozy, Jobbágy, and P. Antal, "Calling homopolymer stretches from raw nanopore reads by analyzing k-mer dwell times," *IFMBE Proceedings*, vol. 65, pp. 241–244, 2017.

[21] A. Fornili, A. N. Kapanidis, M. Meli, M. Sustarsic, T. D. Craggs, and G. Colombo, "Dna polymerase conformational dynamics and the role of fidelity-conferring residues: Insights from computational simulations," *Frontiers in Molecular Biosciences | www.frontiersin.org*, vol. 1, p. 20, 2016. [Online]. Available: www.frontiersin.org

[22] S. Yu and H. Kobayashi, "Practical implementation of an efficient forward-backward algorithm for an explicit-duration hmm," *Environment Protection Engineering*, 2007.

[23] M. J. Wainwright, M. I. Jordan *et al.*, "Graphical models, exponential families, and variational inference," *Foundations and Trends® in Machine Learning*, vol. 1, no. 1–2, pp. 1–305, 2008.

[24] A. Krogh, "Hidden Markov models for labeled sequences," in *Proceedings of the 12th IAPR International Conference on Pattern Recognition, Vol. 3-Conference C: Signal Processing (Cat. No. 94CH3440-5)*, vol. 2. IEEE, 1994, pp. 140–144.

[25] S. Riis, *Hidden Markov models and neural networks for speech recognition*. Technical University of Denmark [Department of Mathematical Modeling], 1998.

[26] X. Xu and J. Jaldén, "Marginalized beam search algorithms for hierarchical HMMs," *arXiv e-prints*, p. arXiv:2305.11752, May 2023.

[27] K. He, X. Zhang, S. Ren, and J. Sun, "Identity mappings in deep residual networks," *Lecture Notes in Computer Science (including subseries Lecture Notes in Artificial Intelligence and Lecture Notes in Bioinformatics)*, vol. 9908 LNCS, pp. 630–645, 2016.

[28] M. Schuster and K. K. Paliwal, "Bidirectional recurrent neural networks," *IEEE Transactions on Signal Processing*, vol. 45, pp. 2673–2681, 1997.

[29] P. Ramachandran, B. Zoph, and Q. V. L. G. Brain, "Searching for activation functions," *6th International Conference on Learning Representations, ICLR 2018 - Workshop Track Proceedings*, 10 2017. [Online]. Available: https://arxiv.org/abs/1710.05941v2

[30] S. Elfwing, E. Uchibe, and K. Doya, "Sigmoid-weighted linear units for neural network function approximation in reinforcement learning," *Neural Networks*, vol. 107, pp. 3–11, 2 2017. [Online]. Available: https://arxiv.org/abs/1702.03118v3

[31] A. Bankevich, S. Nurk, D. Antipov, A. A. Gurevich, M. Dvorkin, A. S. Kulikov, V. M. Lesin, S. I. Nikolenko, S. Pham, A. D. Prjibelski, A. V. Pyshkin, A. V. Sirotkin, N. Vyahhi, G. Tesler, M. A. Alekseyev, and P. A. Pevzner, "Spades: a new genome assembly algorithm and its applications to single-cell sequencing," *JOURNALOFCOMPUTATIONALBIOLOGY*, vol. 19, pp. 455–477, 2012.

[32] H. Li, "Minimap2: Pairwise alignment for nucleotide sequences," *Bioinformatics*, vol. 34, pp. 3094–3100, 9 2018.

[33] NVIDIA, P. Vingelmann, and F. H. Fitzek, "Cuda, release: 10.2.89," 2020. [Online]. Available: https://developer.nvidia.com/cuda-toolkit

[34] M. Abadi, A. Agarwal, P. Barham, E. Brevdo, Z. Chen, C. Citro, G. S. Corrado, A. Davis, J. Dean, M. Devin, S. Ghemawat, I. Goodfellow, A. Harp, G. Irving, M. Isard, Y. Jia, R. Jozefowicz, L. Kaiser, M. Kudlur, J. Levenberg, D. Mané, R. Monga, S. Moore, D. Murray, C. Olah, M. Schuster, J. Shlens,

B. Steiner, I. Sutskever, K. Talwar, P. Tucker, V. Vanhoucke, V. Vasudevan, F. Viégas, O. Vinyals, P. Warden, M. Wattenberg, M. Wicke, Y. Yu, and X. Zheng, "TensorFlow: Large-scale machine learning on heterogeneous systems," 2015, software available from tensorflow.org. [Online]. Available: https://www.tensorflow.org/

[35] D. P. Kingma and J. L. Ba, "Adam: A method for stochastic optimization," 2015.

[36] K. E. Batcher, "Sorting networks and their applications," in *Proceedings of the April 30–May 2, 1968, Spring Joint Computer Conference*, ser. AFIPS '68 (Spring).   New York, NY, USA: Association for Computing Machinery, 1968, p. 307–314. [Online]. Available: https://doi.org/10.1145/1468075.1468121

[37] G. Navarro, "A guided tour to approximate string matching," *ACM Computing Surveys*, vol. 33, 04 2000.

[38] L. John, M. Andrew, and P. F. C.N., "Conditional random fields: Probabilistic models for segmenting and labeling sequence," 2001.

[39] Y. L. . P. A. P. Mikhail Kolmogorov, Jeffrey Yuan, "Assembly of long, error-prone reads using repeat graphs," *Nature Biotechnology*, p. 540–546, 2019.

[40] A. Gurevich, V. Saveliev, N. Vyahhi, and G. Tesler, "Quast: Quality assessment tool for genome assemblies," *Bioinformatics*, vol. 29, p. 1072–1075, 2013.