

Interpreting Inverse Correlation Time: from Blood flow to Vascular Network

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Abstract

1 The inverse correlation time (ICT) is a key quantity in laser speckle contrast
2 imaging (LSCI) measurements. Traditionally, ICT is regarded as a metric
3 of blood flow, such as speed or perfusion. However, we highlight that ICT
4 not only contains important information about blood flow, but also reflects
5 the underlying structure of the vascular network. In the past, ICT has been
6 found to be correlated with vessel diameter. Here, we further report that ICT
7 exhibits a different sensitivity to blood flow depending on vessel orientation.
8 Specifically, ICT is more sensitive to blood flow speed changes in vessels de-
9 scending from or arising to the tissue surface, compared with those laying
10 parallel to the surface. Those findings shift our understanding of ICT from
11 purely blood flow to a combination of blood flow and vascular network struc-
12 ture. We also develop theories to facilitate the study of vascular network's
13 impact on ICT.

Keywords: dynamic light scattering, laser speckle contrast imaging, inverse
correlation time, blood flow, vascular network

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14 1. Introduction

15 Laser speckle contrast imaging (LSCI) has gained attention in recent years
16 for the quantification of blood flow in biomedical imaging applications¹⁻³. It

17 is non-invasive, non-ionizing and label free. In general, the higher the blood
18 flow speed, the more rapidly the speckle patterns will vary in time, leading to
19 a lower speckle contrast when integrated over the camera exposure time^{4,5}.
20 Valuable information about blood flow perfusion in regions of interest can be
21 extracted in real time from the continuous and wide-field 2-dimensional (2D)
22 monitoring of speckle contrast^{6,7}. Nevertheless, the speckle contrast only
23 provides qualitative measurements of the underlying blood flow⁸. Numerous
24 efforts have been put into advancing LSCI from qualitative to a quantitative
25 imaging modality⁹⁻¹⁵.

26 One promising path is to relate speckle contrast to the autocorrelation
27 function of detected electric field, $g_1(\tau)$ and extract the inverse correlation
28 time (ICT) as the index of blood flow. Within a limited set of conditions, ICT
29 is proportional to the typical speed of blood flow within a certain range^{16,17},
30 and it has demonstrated great potential in quantifying cerebral blood flow
31 and facilitating intraoperative flow monitoring¹⁸⁻²¹.

32 In view of the promise of ICT in transforming LSCI to a quantitative
33 imaging modality, the strategy to extract ICT from measured speckle dy-
34 namics is gaining the significant attention. Initially this was done with
35 single-exposure LSCI^{16,17}, and more recently, multi-exposure speckle imaging
36 (MESI) was developed to extract ICT more accurately from the confounding
37 effects of static scattering, instrumentation noise and loss of correlation due
38 to speckle averaging²²⁻²⁴. Recently, dynamic light scattering imaging (DLSI)
39 was proposed to reduce the ICT estimating error owing to an inaccurate
40 model of electric field autocorrelation function²⁵.

41 Though ICT has been mainly interpreted as a metric of blood flow, such
42 as speed, or perfusion, there is increasing evidence that ICT is subject to the
43 structure of the vascular network. Kazmi et al.'s experimental results showed
44 that ICT might be quantifying neither volumetric flux nor flow speed but the
45 product of the flow speed and vessel diameter²⁶. Fredriksson et al. reported
46 the vessel packaging effect in which the confinement of blood to vessels with
47 an average diameter of $40\ \mu\text{m}$ could lead to a 50% reduction in perfusion
48 estimation by LSCI compared with homogeneous blood distribution inside
49 the tissue²⁷. Jafari et al. found that ICT could be shifted over 10 times
50 under the homogeneous assumption compared with using the actual vascular
51 geometry, highlighting the significant impact of vascular geometry on ICT²⁸.

52 The impact of vessel orientation on ICT has not been fully investigated
53 yet. In this work, we conducted Monte Carlo simulations and found that ICT
54 of vessels perpendicular to the tissue surface, i.e. descending from/arising to

55 the surface, exhibits a higher sensitivity to blood flow changes than that
56 of vessels laying on the surface. Such finding is confirmed by experimental
57 validation *in vivo* combining MESI and 2-Photon (2P) imaging. Those results
58 suggest that the structure of the underlying vascular network deserves more
59 attention than it currently receives in the interpretation of ICT. We also
60 develop a generalized theory to facilitate the study on the impact of vascular
61 network structure. It is compatible with all extant $g_1(\tau)$ models and free of
62 assumptions about groundtruth blood flow speeds.

63 2. Theory and Methods

64 2.1. A unified theoretical framework for ICT interpretation

65 According to the traditional dynamic light scattering (DLS) and diffusing
66 wave spectroscopy (DWS) theories, in different scattering regimes (single vs.
67 multiple) and flow conditions (ordered vs. unordered), different assumptions
68 should be made about the form of the electric field autocorrelation function
69 $g_1(\tau)$ [29–33], as shown in **Fig. 1A** [25]. τ_c is the correlation time and ICT
70 is defined as $1/\tau_c$. The modulation number n is the main differentiating factor
71 among those models.

72 In this paper, we first introduce a unified theoretical framework that is
73 compatible with all extant $g_1(\tau)$ models. After Monte Carlo simulation of
74 photon migration inside the tissue, the electric field auto-correlation function
75 $g_1(\tau)$ can be calculated according to Eq. 1 (ref. [34])

$$|g_1(\tau)| = \left| \int_{-\infty}^{\infty} P(Y) e^{jY\tau} dY \right| \quad (1)$$

76 where $Y = \sum_{i=1}^N \vec{q}_i \cdot \vec{v}_i$ and $\vec{q} = \vec{k}_o - \vec{k}_i$. N is the number of dynamic scattering
77 events experienced by a single photon. N can be larger than 1 hence Eq. 1
78 accommodates both single and multiple scatter regimes. \vec{q} is the momentum
79 transfer vector defined as the difference between the scattering wave vector
80 \vec{k}_o and the incident wave vector \vec{k}_i [35]. The direction of \vec{k}_o and \vec{k}_i is the
81 propagating direction of the scattered light and incident light, respectively.
82 The amplitudes are both equal to k_0 , the wavenumber. Finally, \vec{v}_i is velocity
83 of the scattering particle in the i -th dynamic scattering event experienced
84 by the photon. For clarity sake, speed refers to scalars while velocity corre-
85 sponds to vectors in this paper. Note that since the instantaneous velocity
86 of Brownian particles is physically measurable³⁶, we expand the definition of

87 \vec{v}_i from the velocity of ordered motion as defined in ref. [34] to include both
 88 ordered and diffusive motions. $P(Y)$ is the probability density function of Y .
 89 When some photons generate the same Y value, their weights will be added
 90 together to give rise to $P(Y)$. Y can be interpreted as the accumulation of
 91 frequency shifts induced by dynamic scattering (see Supplemental Material
 92 section 1 for a more concise proof than ref. [37]).

$$g_1(\tau) = \int_{-\infty}^{\infty} \Omega(\omega) e^{j\omega\tau} d\omega \quad (2)$$

93 With $g_1(\tau)$ rewritten in terms of Y , we notice that $g_1(\tau)$ is the Fourier
 94 transform of $P(Y)$. Considering the Wiener-Khintchine theorem, if $\Omega(\omega)$
 95 is the normalized power spectral density of the detected electric field, then
 96 $g_1(\tau)$ would be the Fourier transform of $\Omega(\omega)$ (Eq. 2) (ref. [38]). Therefore,
 97 we arrive at Eq. 3 that $P(Y)$ is a shifted version of $\Omega(\omega)$

$$\Omega(\bar{\omega}) = P(Y) \quad (3)$$

98 where $\bar{\omega} = Y + \omega_0$ and ω_0 is the center frequency of the electric field.

99 Substituting $P(Y)$ for $\Omega(\omega)$ is advantageous in that $P(Y)$ reveals the
 100 mechanism of spectrum broadening in LSCI since Y is the accumulation of
 101 frequency shifts induced by dynamic scattering. $P(Y)$ and specific forms of
 102 $g_1(\tau)$ can be bridged by Eq. 4 and 5. For $g_1(\tau) = e^{-|\tau|/\tau_c}$,

$$\frac{1}{\tau_c} = \Gamma \quad (4)$$

103 where Γ is the half width at half maximum of the Lorentzian $P(Y) =$
 104 $\frac{1}{\pi\Gamma} \left(\frac{1}{1 + \frac{Y^2}{\Gamma^2}} \right)$. For $g_1(\tau) = e^{-(\tau/\tau_c)^2}$,

$$\frac{1}{\tau_c} = \frac{1}{\sqrt{2}}\sigma \quad (5)$$

105 where σ is the standard deviation of the Gaussian $P(Y) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{Y^2}{2\sigma^2}}$. See
 106 proof in Supplemental Material section 2.

107 These two equations (Eq. 4 and 5) provide new interpretations of ICT
 108 (i.e., $\frac{1}{\tau_c}$) from the point of view of $P(Y)$. For Lorentzian $P(Y)$, ICT deter-
 109 mines the half width at half maximum while in Gaussian $P(Y)$, ICT is a
 110 scaled version of the standard deviation. Note that in both cases, ICT serves
 111 as a kind of measure of the broadening of the spectrum of Y . In fact, as long

112 as the spectrum of detected light is both bandwidth- and amplitude-limited,
113 a more general linear relationship

$$114 \quad \left(\frac{1}{\tau_c}\right)^2 \propto \text{Var}(Y)$$

115 can be shown to hold for any electric field auto-correlation functions taking
116 the form of $g_1(\tau) = e^{-(|\tau|/\tau_c)^n}$ (see Supplemental Material section 3 for proof).
117 This suggests that ICT in the various $g_1(\tau)$ models shown in Fig. 1a can be
118 unified as the reduced case of the standard deviation of Y . Since $P(Y)$
119 is essentially the same as the power spectral density of the electric field of
120 detected light (Eq. 3), ICT can be interpreted as the scaling factor of the
121 variance of the detected optical spectrum as well. Since $\text{Var}(Y)$ measures
122 the variance of frequency shifts in the dynamics scattering process, we call it
123 the variance of dynamic scattering.

124 2.2. Characterizing the inherent properties of vascular network to produce 125 ICT

126 In this section, we aim to decouple the effects of blood flow speeds and
127 vascular structure on ICT and develop tools to study the vascular network
128 individually. Further analyzing the structure of Y and separate the contri-
129 butions to Y by the blood flow and others, we arrive at Eq. 6

$$Y = Y_s + Y_f = Y_s + k\tilde{v} \quad (6)$$

130 where Y_f represents the contributions to Y by motions induced by blood flow
131 while Y_s denotes the component in Y that is independent of the blood flow.
132 Y_f can be expressed as the product of k and \tilde{v} where $k = \sum_{i=1}^N |\vec{q}_i| \cos \alpha_i$,
133 $\tilde{v} = \frac{\sum_{i=1}^N |\vec{q}_i| \cos \alpha_i \cdot |\vec{v}_i|}{\sum_{i=1}^N |\vec{q}_i| \cos \alpha_i}$ and α_i is the angle between \vec{q}_i and \vec{v}_i . The \vec{q}_i , \vec{v}_i and N
134 follow same definition as in Eq. 1.

135 Note that \tilde{v} represents the weighted average of absolute blood flow speeds
136 and the weighting is determined by the photon's scattering geometry, i.e., the
137 scattering angle and the angle between the momentum transfer vector \vec{q}_i and
138 velocity vector \vec{v}_i . k is the sum of weights and equal to Y_f when blood flow
139 speeds are all unit speeds.

140 Also notice that k and \tilde{v} are well de-correlated from each other. To under-
141 stand this, it is helpful to view k as the sum of weights and \tilde{v} as the weighted
142 average of blood flow speeds. When the sum of weights changes, we would
143 not be able to predict how the weighted average will change if little is known
144 about how the individual weight changes. The weighted average can increase

145 or decrease. It can also remain invariant if the weights increase/decrease by
146 the same ratio.

147 Furthermore, if we assume that blood flow speeds are uncorrelated with
148 the photon's scattering geometry (i.e., the scattering angle and the angle
149 between \vec{q}_i and \vec{v}_i are uncorrelated with the magnitude of the flow vector), \tilde{v}
150 and k would be uncorrelated (see proof in Supplemental Material section 4).
151 With this uncorrelated relationship, we arrive at Eq. 7 and 8

$$E(Y) = E(Y_s) + E(k) E(\tilde{v}) \quad (7)$$

152

$$\text{Var}(Y) = \text{Var}(Y_s) + \text{Var}(k) E(\tilde{v}^2) + E^2(k) \text{Var}(\tilde{v}) \quad (8)$$

153 where $E(X)$ and $\text{Var}(X)$ give the expectation and variance of the random
154 variable X , respectively.

155 Eq. 7 and 8 points out the relationship between statistical properties of
156 Y and those of k and \tilde{v} . Further approximations to Eq. 8 can be made to ac-
157 commodate blood flow quantification. Either of the following two conditions
158 is sufficient for Eq. 9 to be applied with good accuracy. First, the vascular
159 structure sampled by detected photons is dominated by a single vessel, i.e.,
160 $\text{Var}(\tilde{v})$ is approximately 0. This is true for major surface vessels where dy-
161 namic scattering events of detected photons are strongly localized within that
162 vessel^{8,21,33}. Second, the scattering of collected photons is fully randomized,
163 i.e., $E(k)$ is 0. This is true for parenchyma regions where dynamic scattering
164 is dominated by micro-vessels whose orientation is randomized. Our simula-
165 tion results of $E(k)$ on parenchyma regions also support that as section 3.1
166 will show.

$$\text{Var}(Y) = \text{Var}(Y_s) + \text{Var}(k) E(\tilde{v}^2) \quad (9)$$

167 With Eq. 9, we define the characteristic variance of dynamic scattering
168 as $\text{Var}(k)$. If we plot Eq. 9 (Fig. 2), the physical implications of $\text{Var}(k)$ are
169 evident as the slope. $\text{Var}(k)$ can be defined for each detection point (i.e.,
170 a pixel on the camera) in LSCI and it characterizes the ability of the sam-
171 pled vascular network to decrease speckle contrast or increase ICT under the
172 specified illumination/detection setup at the detection point. The larger the
173 $\text{Var}(k)$, the stronger the ability of the vascular network to decrease speckle
174 contrast or increase ICT under the same blood flow speed, at the detection
175 point. In addition, $\text{Var}(k)$ is independent of the blood flow speed since it

176 is defined with unit speeds. Hence, it reveals the inherent properties of the
 177 vascular network under the specified illumination/detection setup.

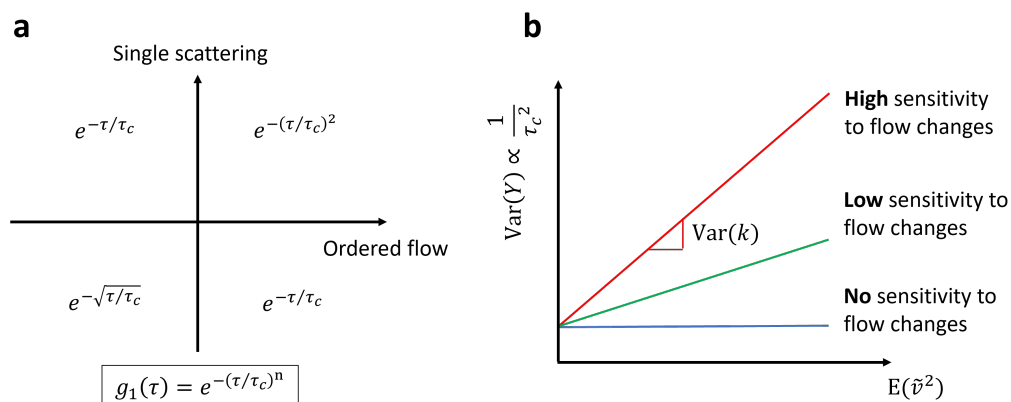


Figure 1: **A unified theoretical framework for ICT interpretation.** **a** The various $g_1(\tau)$ models proposed in treatment of the complex vascular network in LSCI. Extant models of the electric field auto-correlation function in various cases of scattering regimes and flow conditions. τ_c is the correlation time and ICT is defined as $1/\tau_c$. On the quadrant plot, the opposite of the order motion is unordered motion (also known as diffusive motion) and that of single scattering is multiple scattering. **b** Physical meaning of the characteristic variance of dynamic scattering. The vertical axis depicts the variance of dynamic scattering $\text{Var}(Y)$ which is proportional to the square of ICT. The horizontal axis is the weighted average of blood flow speeds sampled by the photon scattering process. The slope of the plot is $\text{Var}(k)$. A steeper slope indicates a vascular network of higher sensitivity to flow changes.

178 2.3. Monte Carlo simulation

179 The simulation algorithm is based on ref. [28]. The uniform flat beam
 180 profile is used for simulation. The effects of ordered motion of the RBCs
 181 along the direction of vessels are investigated in this study. Though the
 182 diffusive motion of RBCs has been recently suggested as dominating the
 183 correlation decay in diffuse correlation spectroscopy (DCS) measurements³⁹,
 184 it is unclear whether the effects are due to the radially diffusive motion of
 185 RBCs within vessels or axially ordered motion of RBCs along the vessel but
 186 within a diffusive vascular network where vessels are curved and direction-
 187 randomized. Nor it is clear whether the observation holds in LSCI. Jafari et
 188 al. found that the axially ordered motion of RBCs along the vessel adequately
 189 describes the particle dynamics in LSCI given the strong agreement between

190 experimental and simulated speckle contrast values²⁸. Hence, the effects of
191 radially diffusive motion of RBCs within vessels might be negligible in LSCI.
192 The potential impact of radially diffusive motion of RBCs within vessels to
193 findings of this study is also discussed in section 4.1.

194 The simple vascular geometry for simulation is made of parallel and
195 equally spaced vessels (similar to ref. [39]). Vessels in the first geometry
196 are parallel to y axis, and parallel to z -axis in the second geometry (Fig. 2a).
197 Some of the major settings are as follows: geometry size: $1 \times 1 \times 1 \text{ mm}^3$,
198 the radius of vessels: 0.01 mm, space between vessels: 0.1 mm, radius of
199 the incident beam: 0.25 mm, radius of the detector: 0.01 mm, NA of the
200 detector: 0.2. The detector is placed in the center of the field of view and
201 right above the vessels. The optical properties of vessels and tissue are the
202 same as in ref. [39].

203 For the realistic vascular geometry (shown in Fig. 2b), the simulation flow
204 for generating the photon trajectories through the 3D geometry is detailed by
205 Jafari et al.²⁸. Briefly, parallelized Dynamic Light Scattering Monte Carlo
206 (DLS-MC) simulations were launched on the Stampede2 Skylake compute
207 nodes on Texas Advanced Computing Center (TACC) using the Message
208 Passing Interface (MPI) protocol to simulate 80×10^9 photon trajectories
209 through the geometry.

210 The realistic vascular geometry was obtained through 2P imaging, fol-
211 lowed by vectorization of the vascular structure⁴⁰. The vectorized geometry
212 was voxelized into a three-dimensional matrix of the size $277 \times 277 \times 303$
213 voxels in the X, Y, and Z directions, respectively. The voxel size was a cubic
214 $2 \times 2 \times 2 \mu\text{m}^3$, yielding a total geometry size of $554 \times 554 \times 606 \mu\text{m}^3$. A
215 circular collimated wide-field beam with a flat profile was set to illuminate
216 95% of the top surface of the geometry. A NA of 0.25 and detector size of
217 $9.8 \times 9.8 \mu\text{m}^2$ were used in the simulation settings to reflect the typical con-
218 figuration of LSCI experimental setup. For detected photons, both entry and
219 exit locations as well as the photon trajectories through the volume and pho-
220 ton weights were recorded. The optical properties of capillaries, non-capillary
221 vessels and extra-vascular tissue as used in ref. [28] are adopted.

222 2.4. *In vivo* experimental validation

223 The MESI imaging system detailed in ref. [21, 22] is used for microfluidics
224 and *in vivo* speckle imaging experiments. The laser wavelength is 785 nm and
225 the magnification of the system is 2x. 56 MESI sequences with each sequence
226 containing 15 speckle contrast images corresponding to 15 exposure times are

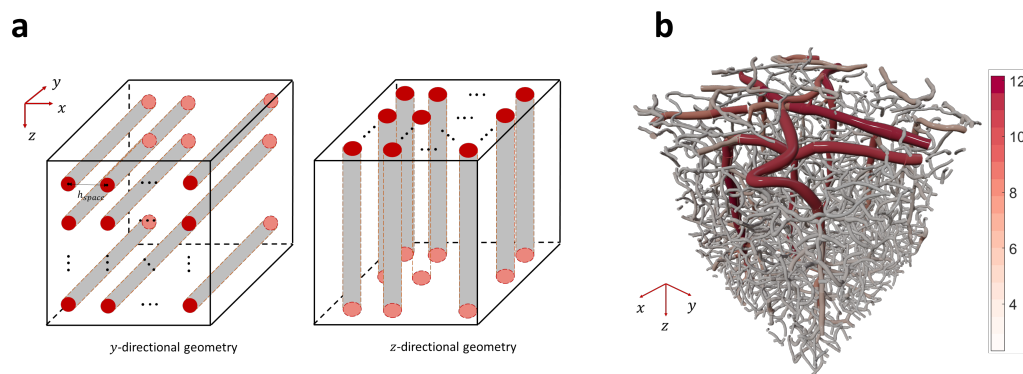


Figure 2: **Vascular geometry in Monte Carlo simulation.** **a** The diagram of simple y - and z -directional vascular geometry. **b** The realistic vascular geometry scanned from a mouse's cerebral cortex. The geometry size is $554 \times 554 \times 606 \mu\text{m}^3$. 3D rendering by Blender 2.81 (ref. [41]). Color coded by vessel radius (unit: μm).

227 acquired. The K^2 curves are calculated by averaging speckle contrast values
228 over multiple MESI sequences and then squaring it. ICT values are then
229 extracted by fitting the K^2 curves based on the MESI model²².

230 The mouse cranial window preparation procedures were detailed by Kazmi
231 et al.²⁶. During imaging sessions, the mouse (C57BL/6, Charles River Lab-
232 oratories Inc.) was anesthetized with medical grade O_2 vaporized isoflurane
233 (3% induction, 1.5% maintenance).

234 For 2P imaging, images were acquired with a custom microscope and
235 laser system^{42,43}. The same anesthesia procedure as above-mentioned was
236 used. In addition, 100 μL of 70 kDa dextran-conjugated Texas Red diluted
237 in saline at a 5% w/v ratio was added to the blood plasma through retro-
238 orbital injection prior to imaging. The dye was then excited by an Yb fiber
239 amplifier ($\lambda = 1060 \text{ nm}$). 30 frames acquired with a resonant scanner were
240 averaged at each depth to produce images.

241 All animal procedures in this study were approved by The University of
242 Texas at Austin Institutional Animal Care and Use Committee (IACUC).

243 3. Results

244 3.1. Monte Carlo Simulation

245 The simulation results on the realistic vascular network under normal il-
246 lumination are shown in Fig. 3. Figure 3a-e shows the map of the number of

247 detected dynamic photons (i.e., photons experiencing dynamic scattering at
 248 least once), $\text{Var}(k)$, $E(k)$, and $\text{Var}(Y)$, respectively. To counter the effects of
 249 wavelength, the $\text{Var}(Y)$, $\text{Var}(k)$ and $E(k)$ are normalized by the wavenum-
 250 ber, i.e. $\text{Var}(Y/k_0)$, $\text{Var}(k/k_0)$ and $E(k/k_0)$, unless specified otherwise.

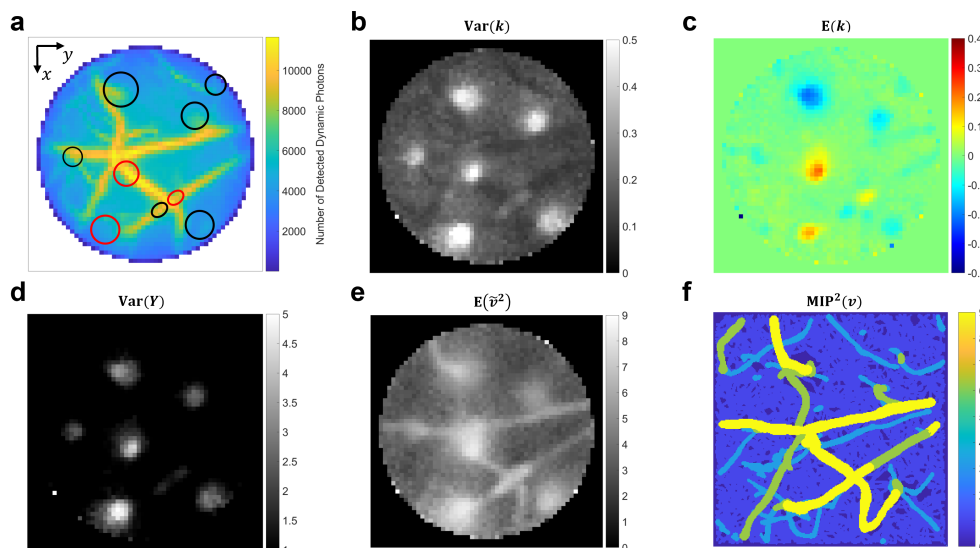


Figure 3: **Simulation results on the realistic vascular network under normal illumination.** **a** The map of the number of detected dynamic photons at each camera pixel. The dynamic photons refer to photons which experience at least one dynamic scattering event before exiting and being detected. **b-f** The map of $\text{Var}(k)$, $\text{Mean}(k)$, $\text{Var}(Y)$, $E(\tilde{v}^2)$, and $\text{MIP}^2(v)$, respectively. $\text{MIP}^2(v)$ represents the square of maximum intensity projection of flow speeds assigned in simulation. The position of bright spots in (b), (c) and (d) is circled out correspondingly in (a).

251 There are several interesting observations. First, note the bright blobs in
 252 Fig. 3b, d and blue/orange blobs in Fig. 3c whose positions are circled in Fig.
 253 3a. The reason that those blobs appear in those places instead of elsewhere
 254 is suspected to be correlated with the underlying vascular structure and we
 255 find that there is always a major descending/ascending vessel in those spots
 256 (Fig. 2b and Supplemental Material section 5).

257 Second, the major surface vessels extending in the x - y plane shown in Fig.
 258 3a appear even darker than surrounding parenchyma regions in the $\text{Var}(k)$
 259 map (Fig. 3b). This suggests that $\text{Var}(k)$ might be sensitive to the orien-
 260 tation of vessels, namely, small for x - y plane surface vessels while large for

261 z -directional descending vessels under normal illumination. This hypothesis
262 is verified by simulation results on the simple vascular geometries consist-
263 ing of parallel and equally-spaced vessels. $\text{Var}(k)$ of z -directional vessels is
264 observed to increase by 7 times compared with that of y -directional vessels
265 under normal illumination (Supplemental Material section 6).

266 Third, among those blobs, some are blue while others appear orange in
267 Fig. 3c. Further analysis on the flow vector assignment in simulation reveals
268 that this is dependent on whether the flow vector is z -positive or z -negative
269 (Supplemental Material section 7).

270 Finally, $E(k)$ of parenchyma regions is 0 (Fig. 3c). Hence, Eq. 9 can be
271 applied with good accuracy. With $\text{Var}(Y_s)$ being 0 in simulation, we could
272 calculate $E(\tilde{v}^2)$ by dividing $\text{Var}(Y)$ with $\text{Var}(k)$. As Fig. 3e shows, the $E(\tilde{v}^2)$
273 map reveals a clearer structure of surface vessels than $\text{Var}(Y)$ (Fig. 3d). To
274 evaluate accuracy of the absolute blood flow speed estimation given in Fig.
275 3e, the square of the maximum intensity projection (MIP) of blood flow
276 speeds assigned in simulation is mapped in Fig. 3f. In terms of the resolved
277 vessels, the shape of x - y plane surface vessels is well preserved in Fig. 3e and
278 the intensity value also shows a good match with that in Fig. 3f. However,
279 for z -directional descending vessels, the vessel boundary is expanded and
280 there is no clear border, which highlights their distinct properties in LSCI
281 from x - y plane surface vessels.

282 3.2. Experimental validation

283 The enhanced sensitivity of speckle contrast to blood flow speed in z -
284 directional vessels compared with x - y plane vessels is also observed *in vivo*.
285 As highlighted by white arrows in Fig. 4a and b, the orthogonal X-Y and
286 X-Z cross-sections of 2P imaging data clearly reveal an inverted “L” shaped
287 vessel. At the end of its surface strand, it develops into a descending strand
288 into the tissue. ROI of the two strands is shown by the white boxes in Fig.
289 4d. Notice that there is no other major vessel branch on this “L” shape
290 and vessel diameters of the two strands are approximately the same. Thus,
291 based on blood flow conservation²⁶, the flow speed should be approximately
292 the same in these two strands. Nevertheless, we see a lower speckle contrast
293 in areas corresponding to the descending strand as pointed out by the white
294 arrow in Fig. 4c. It indicates an enhancement of the sensitivity of speckle
295 contrast to blood flow speed in the descending strand compared with surface
296 strand. More specifically, the average ICT squared of the descending strand
297 is $\sim 78\%$ larger than that of its surface counterpart, as highlighted by white

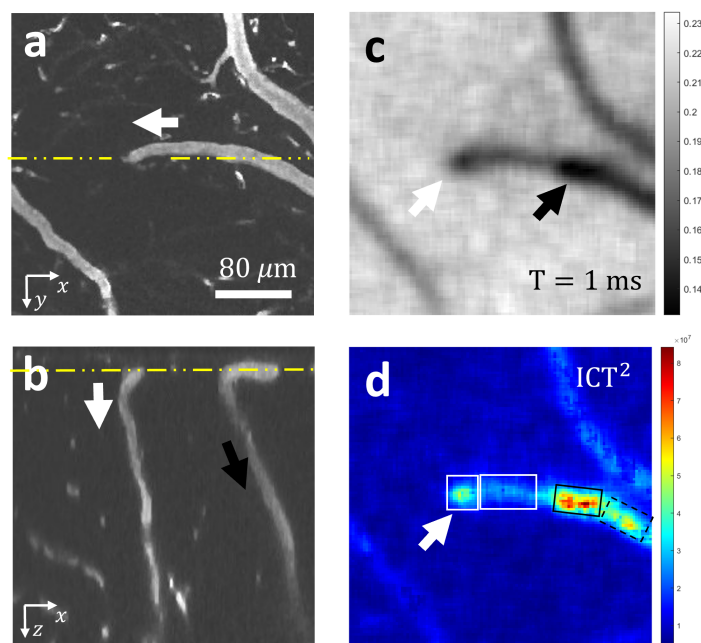


Figure 4: **One example of the z -directional descending vessel inducing a more significant decrease of speckle contrast and increase of ICT than its upstream x - y plane surface strand *in vivo*.** **a, b** Orthogonal cross-sections of the vascular structure acquired from 2P imaging. **(a)** X-Y cross-section (depth: $27\ \mu\text{m}$); **(b)** X-Z cross-section along the yellow dashed line in **(a)**. The yellow line in **(b)** indicates the z position of **(a)**. White arrows in **(a)** and **(b)** indicate the direction of an upside-down “L” shaped vessel which has a surface strand extending horizontally on the surface followed by a descending strand deep into the tissue. scale bar: $80\ \mu\text{m}$. The spatial scale along the x - and z -axis is the same in **(b)**. **c** Single-exposure speckle contrast image of the vascular network. Camera exposure time $T=1\ \text{ms}$. The white arrow indicates position of the descending vessel strand which shows a stronger decrease of speckle contrast than its connected x - y plane surface strand. **d** The map of ICT square. The two white boxes highlight the descending strand and surface strand, respectively. The white arrow indicates the position of the descending strand exhibiting a larger ICT value than its connected x - y plane counterpart. The black arrow in **b** highlights another descending vessel branch from the main vessel. The black arrow in **c** and black boxes in **d** indicate the compound effects of vascular structure and blood flow in modulating speckle contrast and ICT values.

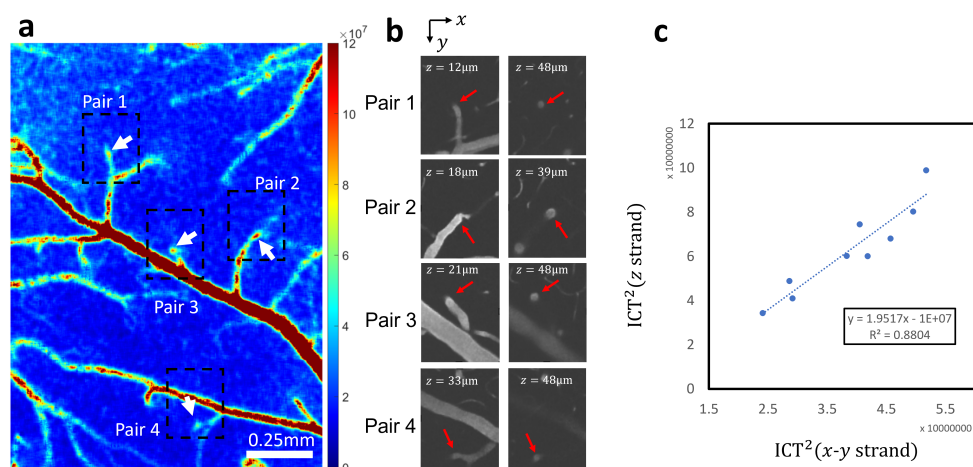


Figure 5: **Statistical comparison of ICTs between the z -directional descending vessel strand and its upstream x - y plane surface strand *in vivo*.** **a** Pairs of z strand and x - y strand in a typical mouse cerebral window whose position is highlighted by the dashed rectangle on the ICT squared image. The arrows point to the descending vessel in each pair. Scale bar: 0.25mm. **b** The corresponding 2P images showing the vascular structure of the four pairs of z strands and x - y strands. The first column shows the X-Y cross-section of the vascular structure near the surface while the second column shows the cross-section at the same location but in a deeper tissue. The red arrows point to the z strands in the pair. **c** The juxtaposing of ICT squared of the z strand and that of the contiguous x - y strand. The scatter plot shows the data of nine z and x - y strand pairs from three mice. The linear fitting is performed and the slope is around 2, larger than 1, which indicates that the ICT of z -directional vessels could be larger than that of x - y plane vessels even though they assume the same blood flow speed. The difference between ICT squared of the z strand and that of the paired x - y strand is statistically significant (paired t-test, $n=9$, $p < 0.001$).

298 boxes in Fig. 4d). If the impact of $\text{Var}(Y_s)$ is negligible, it implies that
299 $\text{Var}(k)$ of the descending strand would be more than 75% larger than that
300 of surface strand. Notably, similar border expansion is also observed here in
301 the position of the descending strand as in simulation (Fig. 3e).

302 To further evaluate the statistical significance of the enhanced sensitivity,
303 9 pairs of z -directional vessels and x - y plane vessels from 3 mice are analyzed.
304 Those vessel pairs are selected for analysis because their vascular structure
305 has the same properties as in the example mentioned above, i.e., the upside-
306 down L vessel shape and the approximately same diameter of the two strands.
307 The location of four z and x - y strand pairs in a typical mouse cerebral window
308 is shown in Fig. 5a and their vascular structure is acquired by 2P imaging
309 (Fig. 5b). ROI of the z and x - y strands in each pair is selected in the
310 similar way as shown by white boxes in Fig. 4d. The ICT squared of the z
311 strand in each pair is plotted against that of the x - y strand (Fig. 5c). The
312 linear fitting results in a slope of approximately 2. In addition, the difference
313 between ICT squared of z strand and that of its contiguous x - y strand is
314 statistically significant (paired t-test, $n=9$, $p < 0.001$). Those results provide
315 direct experimental evidence for the enhanced sensitivity of ICT to blood
316 flow changes in z -directional vessels compared with vessels extending in the
317 x - y plane.

318 Finally, the compound effects of vascular structure and blood flow should
319 be noticed. As highlighted by the black arrow in Fig. 4b, there is another
320 descending vessel branch from the main vessel. The blood flow in the main
321 vessel splits into two portions: one goes into the above-mentioned inverted
322 “L” shaped vessel and the other goes into this second descending vessel.
323 Therefore, the speckle contrast and ICT in the solid black rectangle in Fig.
324 4d result from not only an underlying descending vessel but also the larger
325 blood flow in the main vessel. That is why they are not directly comparable
326 with those of the descending strand in the white square in Fig. 4d. Interest-
327 ingly, the enhanced sensitivity can be roughly examined if we compare the
328 ICT squared in the solid-line black rectangle with that in the dashed black
329 rectangle in Fig. 4d. Both areas cover the main vessel of the largest blood
330 flow but the solid rectangle assumes larger ICT squared, which indicates the
331 additional impact of the descending vessel in the solid square. Similarly, the
332 joint effects of vascular structure and blood flow are observed in the region
333 of vessel pair 2 in Fig. 5a where a second descending vessel is also present
334 (Fig. 5b).

335 4. Discussion

336 4.1. Bridging ICT to physiologically meaningful blood flow variables

337 Given the volume integrated nature of LSCI and the complexity of the
338 vascular network, it has been long hypothesized that if LSCI is measuring
339 some physiologically meaningful blood flow variable, it measures the weighted
340 average of that variable within the probed volume [22, 39]. However, it is
341 unclear how the weighting is determined. Our derivation in section 3.1 and
342 3.2 reveals that the weighting is determined by photons' dynamic scattering
343 process, according to the definition of \tilde{v} (Eq. 6). Note that \tilde{v} is physiologically
344 meaningful and represents the weighted average of blood flow speeds probed
345 by detected photons. In the case that all dynamic scattering events sample
346 the same blood flow speed v , \tilde{v} would be equal to v regardless the weighting.

347 Combining the results in section 2.1 and 2.2, a general relationship be-
348 tween ICT and physiologically meaningful blood flow variables, i.e. \tilde{v} , can
349 be established. In section 2.1, it has been shown that ICT squared is pro-
350 portional to the variance of Y , which accommodates all current $g_1(\tau)$ models
351 in LSCI. In section 2.2, Eq. 9 further points out that the variance of Y
352 assumes a linear relationship with the expectation of \tilde{v} squared. Hence, the
353 linear relationship between ICT squared and the expectation of \tilde{v} squared is
354 reached by our theoretical derivation.

355 Contrary to the frequently adopted notion that ICT is proportional to
356 blood flow speed, our theory concludes that the squares of the two that are
357 linear to each other. The difference between the two notions is centered on
358 whether $\text{Var}(Y_s)$ is zero or not. Pragmatically, the existence of $\text{Var}(Y_s)$ is
359 indispensable to tackling the "biological zero" problem which refers to the
360 non-zero residual signal even when no blood flow is present^{37,44}. A non-
361 zero $\text{Var}(Y_s)$ might reduce the difference of ICT values between descend-
362 ing/ascending vessels and surface vessels. As observed in simulation, the
363 $\text{Var}(k)$ of z -directional vessels is 7 times larger than that of y -directional
364 vessels in the simple vascular geometry, which is expected to generate a ICT
365 squared difference of 7 times according to Eq. 9 if $\text{Var}(Y_s)$ is zero. However,
366 ICT squared *in vivo* is only 60% larger on average in descending/ascending
367 vessels than vessels laying on the surface. A non-zero $\text{Var}(Y_s)$ *in vivo* could
368 play a significant role in accounting for such discrepancy. In addition, the
369 scatters' movement could be more diverse *in vivo* compared with our settings
370 in simulation. For example, the radially diffusive motion of RBCs in vessels
371 is not present in our simulation.

372 $\text{Var}(k)$ plays a major role in bridging ICT and the physiologically mean-
373 ingful blood flow variable, \tilde{v} , as Eq. 9 points out. It provides a theoretical
374 basis for extracting the physiologically meaningful blood flow variable \tilde{v} from
375 ICT. Given the $\text{Var}(k)$ already known of the vascular network, the estima-
376 tion of absolute statistical blood flow speeds could be made by dividing the
377 measured $\text{Var}(Y)$ by $\text{Var}(k)$ (Fig. 3e). Note that $\text{Var}(Y_s)$ is assumed 0 in
378 simulation.

379 Finally, our findings showed partial support for Briers et al.’s method of
380 converting measured ICT values to absolute blood flow speeds. Specifically,
381 the conversion is performed by $v_c = \lambda/(2\pi\tau_c)$ where v_c is named decorrelation
382 velocity, λ is wavelength and τ_c is correlation time^{16,17}. Our theory shows
383 that this is in fact acquired by assuming $\text{Var}(Y_s) = 0$ and approximating
384 $\text{Var}(k)$ with k_0^2 , the square of wavenumber (Eq. 9).

385 4.2. Interpretation and practical implications of $\text{Var}(k)$

386 $\text{Var}(k)$ can be interpreted at both the microscopic and macroscopic scales.
387 Microscopically, by definition (Eq. 6 and 8), it provides an essential char-
388 acterization for the variation of photons’ dynamic scattering process inside
389 the probed medium in terms of the accumulated frequency shift. Macro-
390 scopically, as revealed by Eq. 9, it reflects the ability of the probed vascular
391 network to induce a decrease of speckle contrast or increase of ICT for a given
392 illumination and detection setup. The micro and macro-scale interpretations
393 are connected due to the fact that photons’ dynamic scattering is mainly
394 constrained within the vascular network.

395 $\text{Var}(k)$ also illustrates that it is challenging, if not impossible, to do abso-
396 lute blood flow speed measurements through a generalized calibration since
397 $\text{Var}(k)$ is unique for a given vascular network. When the probed vasculature
398 changes, $\text{Var}(k)$ also changes.

399 4.3. Physical mechanism and practical implications of the directionality sus- 400 ceptibility

401 The different sensitivity of ICT to the blood flow speed in x - y plane vessels
402 and z -directional descending/ascending vessels is likely due to the different
403 flow direction in those vessels. One might argue that in descending/ascending
404 vessels, the ratio of blood volume in the overall volume sampled by detected
405 photons might be larger than that in the surface vessels. And it might be
406 the larger blood volume ratio in descending/ascending vessels that is caus-
407 ing the higher sensitivity of ICT to the blood flow. We exclude this theory

408 by manipulating the flow direction in simulation. If the blood volume ratio
 409 theory is true, then $\text{Var}(k)$ of z -directional vessels should remain larger than
 410 that of x - y plane vessels even if the direction of flow is changed since the
 411 blood volume ratio is invariant. However, it is observed that $\text{Var}(k)$ of the
 412 z -directional vascular geometry is smaller than that of y -direction vascular
 413 geometry after switching the flow direction in z -directional vascular geome-
 414 try to y -direction and that in y -directional vascular geometry to z -direction
 415 (Table S2). Validation on the realistic vascular geometry shows consistent
 416 results (Fig. 6). The bright blobs originally present in the $\text{Var}(k)$ map
 417 (Fig. 3b) are removed after the amplitudes of y and z component of the unit
 418 velocity vector of blood flow are swapped (Fig. 6a). Instead, the position
 419 of y -directional vessels is highlighted. However, such phenomena would not
 420 appear if it is the amplitudes of x and y component that are swapped (Fig.
 421 6b).

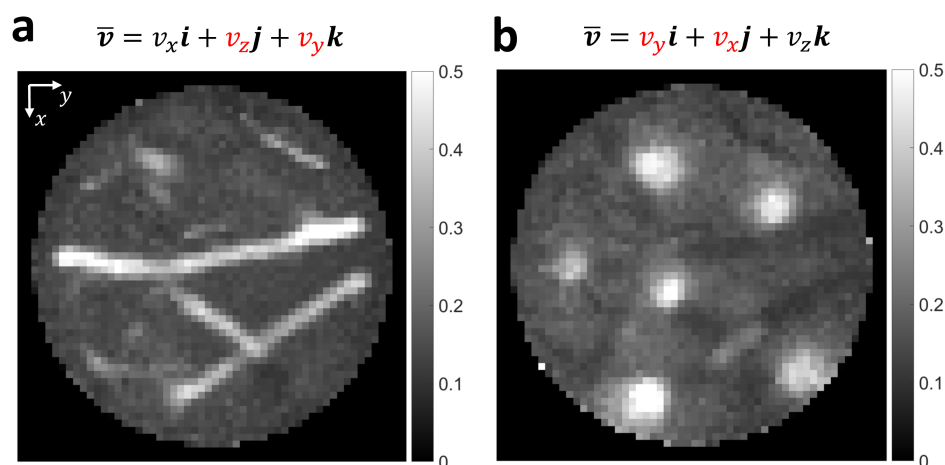


Figure 6: **Map of $\text{Var}(k)$ with the blood flow direction switched in realistic vascular geometry.** **a** The amplitudes of y and z components of the unit velocity vector of blood flow are swapped in simulation. **b** The amplitudes of x and y components of the unit velocity vector of blood flow are swapped in simulation.

422 $\text{Var}(k)$ not only quantifies and reveals the directionality susceptibility of
 423 LSCI to vessel orientation, but also helps explain such susceptibility. Since
 424 $\text{Var}(k)$ measures the overall variance of k of detected photons, it is suscep-
 425 tible to the range determined by the extreme values of k . Consider extreme
 426 values of k of singly scattered photons first where $k = |\vec{q}| \cos \alpha$. Under normal

427 illumination, $|\vec{q}| \approx 2k_0$ and \vec{q} is along the z -axis. Therefore, k would be max-
428 imized when $\cos \alpha$ is maximized. Since α is the angle between velocity vector
429 \vec{v} and momentum transfer vector \vec{q} which is along the z -axis, $\cos \alpha$ would be
430 maximized when \vec{v} is also along the z -axis. That explains why z -directional
431 vessels have larger $\text{Var}(k)$ values than x - y plane surface vessels. Finally, for
432 photons that are scattered multiple times, the randomized directions of \vec{q} and
433 \vec{v} make it difficult to generate extreme k values since the effects of multiple
434 scattering events can cancel out with each other. Hence, the directionality
435 susceptibility mainly originates from the directionality susceptibility retained
436 in single-scattering or few-scattering components of the detected light.

437 The directionality susceptibility of LSCI has several practical implica-
438 tions. First, direct comparison of ICT values in x - y plane vessels and in
439 ascending/descending vessels should be avoided. If a descending/ascending
440 vessel exhibits a larger ICT value, it does not necessarily imply a higher
441 blood flow than its surface counterpart. Second, the special property of z -
442 directional vessels, i.e., enhanced ability to induce the decrease of speckle
443 contrast and increase of ICT under the same blood flow speed, might be use-
444 ful in locating descending/ascending vessels. Note that those types of vessels
445 are particularly prevalent in cerebral cortex and play an important role in
446 the blood supply to deeper tissues.

447 5. Conclusion

448 The interpretation of ICT is a key topic in quantitative LSCI. Though
449 it has been mainly considered as a metric of blood flow, there is increasing
450 evidence that it is susceptible to the structure of vascular network. We build
451 a theoretical framework to facilitate the modeling of the vascular network's
452 impact on ICT and find that ICT is modulated by vessel orientation. In both
453 simulation and *in vivo* experimental validation, ICT of descending/ascending
454 vessels exhibits a higher sensitivity to blood flow changes than in surface-
455 extending vessels. The different sensitivity is shown due to the flow direction
456 instead of blood volume ratio by simulation. The single-scattering compo-
457 nent of the detected light might play a major role in ICT's susceptibility to
458 vessel orientation. Those results suggest that the impact of vascular network
459 structure warrants more attention and investigation in the interpretation of
460 ICT.

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470 **Author Contributions**

471 Q.F. and A.K.D. developed the theory and designed the experiments;
472 Q.F. and C.Z.J did the Monte Carlo simulation experiments; S.E. and A.T
473 performed the *in vivo* mice imaging experiments; Q.F., C.Z.J, A.T., S.E. and
474 A.K.D wrote the paper together.

475 **Conflicts of Interest**

476 The authors declared no conflicts of interest.

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