A New Method to Quantify the Causal Effects of Reinforcement in Terms of Behavioral Selection

Matthias Borgstede*, Patrick Anselme**

*Corresponding author:

University of Bamberg

Markusplatz 3

D-96047 Bamberg

matthias.borgstede@uni-bamberg.de

**Ruhr-University Bochum

D-44780 Bochum, Germany

patrick.anselme@rub.de

A New Method to Quantify the Causal Effects of

Reinforcement in Terms of Behavioral Selection

Abstract

We present a new methodology to partition different sources of learning within a selectionist framework based on the Price equation – the Multilevel Model of Behavioral Selection (MLBS). The MLBS provides a theoretical and formal background to disentangle behavior changes due to selection effects ("reinforcement") from behavior changes due to non-selection effects (e.g., "effort" or "skill"). The model allows to quantify the causal effect of reinforcement even in the presence of opposing sources of behavior change and to test whether the reinforcement effect is statistically significant for a given subject.

We demonstrate our method using training data from a reinforcement experiment with nine pigeons (*Columba livia*). The pigeons were trained to search for food in small holes on the ground of a special cage. In each session, the holes in only one half of the cage were filled with food (reinforced region), while the holes in the other half of the cage remained empty (nonreinforced region). Although the total time spent in the reinforced region between training sessions tends to decrease between training sessions, our method reveals positive behavioral selection (reinforcement effect) in most of the pigeons. However, this selection effect is masked by a strong non-selection component that consists in pigeons becoming more efficient foragers (skill effect) and in an increased peck frequency (effort effect).

The partitioning of behavior change into selection and non-selection components allows to identify the causal effects of reinforcement even if they cannot be isolated experimentally. Our method is especially useful in the context of non-equilibrium behavior analysis (such as the change between training sessions), and in the context of behavior observations in naturalistic settings.

38 **Keywords:** *reinforcement, behavioral selection, Price equation, covariance based law of effect,*

39 *multilevel model of behavioral selection, causal inference*

1 Introduction

The quantitative analysis of behavior traditionally focuses on establishing functional relations

between behavior and the contextual factors in which the observed behavior occurs, such that one

or more behavioral measures (e.g., time spent doing an activity, or lever press rate) is expressed as a

mathematical function of one or more independent variables (e.g., delay of reinforcement or the

amount of reinforcement). For example, in matching analysis, the ratio between two observed

behavioral measures, such as the time spent engaging in two mutually exclusive activities (e.g.,

pressing one of two different levers), is described as a function of the ratio between the amount of

reinforcement received during the different activities (e.g., food pellets) (Herrnstein, 1961).

Functional relations may help structure observed data, predict future behavior and advance new

ways to influence behavior. Furthermore, given all other factors are held constant in an experiment,

a functional relation between an independent and a dependent variable allows us to infer a causal

effect of the independent variable (Menzies & Price, 1993). The experimental method has revealed

many consistent qualitative findings in the field of behavior analysis, such as the causal effects of

different schedules of reinforcement (Ferster & Skinner, 1957), exposure to stressful stimuli (Lemos

et al., 2012), and drug consumption (Berridge & Robinson, 2016), on behavior change.

However, when reinforcement is studied on a quantitative level, causal inference is not quite as

straightforward. The problem with reinforcement is that, in order to be effective, it needs to be

contingent on behavior. Therefore, the received amount of reinforcement in a behavioral experiment

does not only depend on the experimenter, but also on the behavior of the individual under study.

Consequently, it is impossible to isolate reinforcement as an independent variable. For example, as

pointed out by Staddon (2020), the matching law is a functional relation between two *dependent*

variables – a behavior ratio and a reinforcement ratio. Therefore, one cannot interpret the

parameters of the fitted matching equation in terms of causal effects of reinforcement. Since

reinforcement always depends on behavior, this problem persists even if the data come from the

most controlled experiments.

The situation becomes even more difficult when behavior is studied under non-equilibrium

conditions, such as when the dynamics of behavior change over time due to gradual depletion in

reinforcers from trial to trial. As long as behavior changes dynamically, the experimenter has little

control over the amount of received reinforcement. In fact, conditional on the schedule of

reinforcement, the amount of received reinforcement solely depends on the behavior of the

individual under study, making it impossible to isolate the causal effect of reinforcement

experimentally.

Although the above methodological problems are well known, they are hardly ever considered in the

analysis of behavioral experiments. From a pragmatic point of view, focusing on functional, rather

than causal, relations may seem reasonable. However, even if one is "only" interested in the

prediction and control of behavior, it is difficult to adhere to a purely functional account. In fact, the

very idea of controlling behavior implies that the experimentally identified determinants of behavior

must be effective *causes* of behavior. Moreover, if there is one thing that behavior analysts can agree

upon, it is certainly that behavior changes *because* of reinforcement.

But in which sense can reinforcement be said to be a cause of behavior? Following Skinner's three-

term contingency, reinforcement requires the occurrence of an event (such as the administration of

food) contingent on a specific behavior (such as lever pressing), given specific contextual stimuli

(such as a flashing light in an operant chamber) (Skinner, 1965). If we observe a quantitative behavior

change in the presence of the contextual stimuli, we call the contingent event a reinforcer and

attribute the observed change in behavior to reinforcement. Applied to experimental data, the three-

term contingency yields an operational definition of reinforcement. All other things being equal, we

could say that behavior changed *because* of reinforcement, since all other potential causes of

behavior change were held constant and could therefore be ruled out. In other words, if we want to

give a causal interpretation to reinforcement, we need to treat it as an independent variable and

hold all confounding variables constant. However, as argued above, it is impossible to isolate the

amount of reinforcement as an independent variable in an experiment because reinforcement is

necessarily contingent on behavior. Therefore, although the three-term contingency provides a

coherent conceptual framework for the analysis of behavior, is not sufficient to justify a causal

interpretation of reinforcement.

To give an example, imagine a pigeon searching for food in an unfamiliar environment. We may

quantify its foraging behavior by measuring the time spent at various food patches over several

successive time intervals. Say that one food patch contains significantly more food than the other

patches. If reinforcement was effective, we would expect the pigeon to eventually spend more time

in the food patch that contains more food. However, other factors may also be effective in altering

behavior. For example, the pigeon may follow a very simple, fixed decision rule like this one: "As long

as you keep finding food, stay close; else, move to another location" (cf. McNamara & Houston,

2009). Such a rule does not require any kind of reinforcement or long-term learning. However, it will

naturally produce a quantitative change in behavior over successive observation intervals, such that

the pigeon will end up spending most of its foraging time in the region with the largest amount of

food. Accordingly, pigeons prefer to forage in patches with a higher food density, especially if the

food items can be detected visually (Anselme et al., 2018; Anselme et al., in press). Even if all

external factors were held constant, we could not be sure whether the observed change was actually

caused by reinforcement, or by a simple local decision rule that mimics reinforcement but is in fact

something completely different. Reinforcement could be effective but remain undetectable because

other sources of behavior change may mask its causal effect on behavior. For example, the pigeon

may not only learn where the food is, but also increase its foraging effort by means of a higher

pecking rate. It may also acquire skills that facilitate food retrieval over time. Both factors will result

in the pigeon spending less time in the rich food patch because they enable the pigeon to be a more

efficient forager. If the effects of effort and skill are strong enough, they may actually mask the effect

of reinforcement or even result in a "negative" overall behavior change—i.e., a lower investment in

the task. If we attributed this negative change to reinforcement effects, we would have to conclude

that the obtained food acts as a punisher, due to the pigeon eventually spending less time at the rich

food patch.

The above example illustrates that the causal effect of reinforcement cannot easily be inferred from

observed behavior change. Other sources of behavior change may mimic reinforcement, even if the

individual is never actually reinforced, or mask existing reinforcement effects. Such non-

reinforcement factors may be difficult to control because: a) they may be unobservable, such as local

decision rules, b) they may be dynamic in nature and thus change in the course of the experiment,

such as skills, or c) they lie outside the influence of the experimenter, such as increased effort. Since

reinforcement itself cannot be isolated experimentally, non-reinforcement sources of behavior

change may occur in the most controlled experiments, and will probably be even more important in

the wild. Indeed, some findings indicate that animals often spend time and effort seeking uncertain

food despite the availability of large amounts of free food (Inglis et al., 1997), accept to pay a cost for

an information about a future outcome that is independent of this request for information (Wang &

Hayden, 2019), and sometimes develop various pathologies in captivity when the opportunity to

exert the actions leading to reward procurement in nature is not possible, despite the absence of

food deprivation (Eilam et al., 2006). These phenomena suggest that reinforcement is not all in

animal behavior.

In this paper, we address the issue of causal inference in the context of reinforcement. First, we

provide a coherent theoretical background for reinforcement that builds on the concept of selection

by consequences (Skinner, 1981). Second, we use the selectionist theory of reinforcement to develop

a new methodology that allows for the quantification of the causal effects of reinforcement by

means of counterfactual reasoning (Lewis, 1973). Third, we apply our methodology to quantify the

causal effects of reinforcement in the presence of other sources of behavior change using training

data from a pigeon experiment.

The remainder of this article starts with an introduction to the selectionist account of reinforcement,

and its formalization within the Multilevel Model of Behavioral Selection (MLBS), in particular

(Borgstede & Eggert, 2021). We then apply the rationale of counterfactual reasoning to derive a new

method for the quantification of the causal effects of reinforcement on behavior change between

experimental trials. The method also allows for the calculation of p-values to test the selection effect

for statistical significance on the level of single subjects, which can then be aggregated to the group-

level using a meta-analytic approach (cf. Dugard et al., 2012). Finally, we apply our method to an

empirical data set, showing that reinforcement may be causally effective even if it is masked by other

factors, and discuss the implications with regard to the selectionist theory of reinforcement and

potential practical applications of the method.

151   2   Behavioral Selection Theory

Reinforcement has repeatedly been characterized as a process that works analogous to natural

selection (Broadbent, 1961; D. T. Campbell, 1956; Gilbert, 1970; Herrnstein, 1964; Palmer &

Donahoe, 1992; Pringle, 1951; Skinner, 1966; Thorndike, 1900). Whereas in natural selection, species

adapt to the environment as a result of the fitness consequences of inheritable traits, reinforcement

consists of individuals adapting to specific contexts as a result of the reinforcing consequences of

repeatable actions. Skinner (1981) proposed that both processes should be subsumed under the

common explanatory mode of "selection by consequences."

The idea that reinforcement may be a selection process was later formalized by Baum (2017) and

further developed by Borgstede and Eggert (2021), who integrated individual level behavioral

selection with population level natural selection within a Multilevel Model of Behavioral Selection

(MLBS). The MLBS builds on the abstract description of selection processes by means of the Price

equation (Price, 1970, 1972). The Price equation describes selection by means of the covariance

between the individual values of a quantitative character (e.g., an inheritable trait such as size) and

individual evolutionary fitness (i.e., the contribution of an individual to the future population). A

positive covariance is associated with a positive change in mean character value (i.e., selection

results in a higher average value), whereas a negative covariance indicates a negative change (i.e.,

selection results in a lower average value). In other words, those character values that coincide with

higher evolutionary fitness, are selected and thus alter the population average. The Price equation

provides a mathematically exact description of this process that is independent of the specific

mechanisms of variation, selection, and transmission (Luque, 2017).

In the Price equation, all other sources of change (those that do not refer to selection) are subsumed

in a residual term. This term has different interpretations depending on the context. For example,

when applied to the evolutionary change of gene frequencies, the residual term captures the effects

of imperfect transmission (i.e., mutation and recombination). When applied to phenotypic change

over generations (e.g., body weight or behavioral traits), the term may also capture environmental

factors influencing the phenotype (Luque & Baravalle, 2021).

In the MLBS, the Price equation framework is applied to a population of individuals that vary in a

certain quantitative behavior (such as average time spent doing a certain activity). In this case, the

covariance term refers to natural selection on average behavior tendencies of the population, and

the residual term captures the average change within individuals. The MLBS is mainly concerned with

this latter within-individuals change. Following the rationale that individual changes in behavior can

be explained through selection by consequences, the MLBS extends the Price equation by applying

the same covariance principle on the within-individuals level. Here, the population average in

behavior is not calculated over different individuals, but over recurring instances of the same context

(e.g., experimental trials). Behavior change, such as an increase or decrease in time spent doing a

certain activity averaged over a longer period, is described according to the covariance partitioning

from the Price equation. However, the criterion of selection is not individual fitness itself (in terms of

a direct contribution to the future population), but statistical predictors of individual fitness. In other

words, on the within-individual level, behavior is not selected by means of reproduction or survival

(in fact, if the individual dies, all of its behavior immediately ceases), but by events that predict

expected change in evolutionary fitness (Borgstede, 2020). For example, food is generally a positive

predictor of evolutionary fitness because it raises the probability of survival and, thus, future

reproduction. Conversely, physical threat is a negative predictor of evolutionary fitness because it

lowers the chances of survival and future reproduction. The concept of a fitness predictor is largely

equivalent to what Baum (2012) calls a "phylogenetically important event (PIE)". The only difference

is that, in the MLBS, fitness predictors are defined on purely statistical grounds, whereas Baum

emphasizes the causal effects of PIEs on evolutionary fitness.

The conceptual framework of the MLBS allows us to describe behavioral selection on the individual

level by means of a within-individuals covariance between behavior in recurring contexts and its

consequences in terms of statistical fitness predictors. A positive covariance corresponds to an

increase in behavior due to reinforcement, whereas a negative covariance implies a decrease in

behavior due to punishment (cf. Baum, 2012). Similar to the process of natural selection, those

behaviors that coincide with events that signal a gain in expected evolutionary fitness are selected,

which in turn changes the average behavior of the individual. Following the MLBS, the amount of

change due to selection corresponds to the covariance between behavior and fitness predictor,

weighted by the slope of the fitness predictor (its "reinforcing power"). Formally, the amount of

behavior change due to within-individual selection can be expressed by the following equation

(Borgstede & Eggert, 2021):

$$\Delta_S b = \beta_{wp} \, \text{Cov}(b,p) \tag{1.}$$

Here, b designates a quantitative behavior (such as time spent doing a certain activity) and $\Delta_S b$

corresponds to the within-individual change in average behavior due to selection. The value p is a

quantitative fitness predictor and $\text{Cov}(b,p)$ is the covariance between the behavior and the fitness

predictor. Finally, β_{wp} is the slope of the fitness function of the predictor p (i.e., its reinforcing

power).

Just like the original Price equation, the MLBS introduces a residual term that captures all other

sources of behavior change that are not selection. Designating the overall change in average

behavior, Δb is the within-individuals behavior change which can now be expressed as the sum of a

selection term and a residual term δ:

$$\Delta b = \Delta_S b + \delta \tag{2.}$$

This equation is called the covariance based law of effect (CLOE). The CLOE can be regarded as a

fundamental principle of behavior analysis in that it captures the essence of behavioral selection by

partitioning the overall change in behavior into a selection component and a residual component

(Borgstede & Luque, 2021). The selection component corresponds to what is traditionally called

"reinforcement", whereas the residual term subsumes all other sources of behavior change that are

not reinforcement. In the following section, we use the MLBS as a starting point for a theory-based

approach to measuring the effects of reinforcement (cf. Borgstede & Eggert, in press).

3   Causal Analysis and Counterfactual Reasoning

On a theoretical level, the MLBS accounts for a great range of behavioral phenomena that are

difficult to explain using traditional stimulus-response theories (cf. Borgstede, 2021; Borgstede &

Eggert, 2021; Borgstede & Luque, 2021), such as the blocking effect (Kamin, 1969), reinforcing effects

of rare behavior (Premack & Premack, 1963), reinforcing effects of response deprivation (Timberlake

& Allison, 1974), information seeking (Berlyne, 1957; Hendry, 1965), and various deviations from

matching (Davison & McCarthy, 2016).

However, quantitative estimates of behavioral selection from empirical data can be difficult to obtain

(cf. Strand et al., 2021). As mentioned before, selection effects may be masked by other sources of

behavior change, which is why a direct correspondence between observed behavior change and

behavioral selection is not guaranteed. Moreover, observed behavior may differ between trials due

to random fluctuations, rather than selection. Therefore, estimates of behavioral selection from

empirical covariances between behavior and reinforcement are only reliable for large amounts of

data. However, as long as selection is present, behavior is not in an equilibrium state and thus is

subject to ongoing change, which in turn biases covariance estimates.

The above challenges are not unique to the theory of behavioral selection, but also occur in

biological applications of the Price equation. Although the partitioning of change into selection and

non-selection components is always possible on a theoretical level, empirical applications require

specific models about the causes of change (Okasha & Otsuka, 2020). Okasha and Otsuka (2020)

propose to use such models for causal inference using counterfactual reasoning (Lewis, 1973, 2000).

Given a specific model, counterfactual analysis yields empirical estimates of the causal effects of the

selection and non-selection components in the Price equation. In the domain of behavioral selection,

a causal interpretation of the selection term in the CLOE would provide a quantitative estimate of the

causal effect of reinforcement. Therefore, a method based on counterfactual reasoning might

provide a tractable method to infer the causal effects of reinforcement from observed behavioral

change.

The general idea behind counterfactual reasoning is that we attribute a causal effect to an event if

we have reason to believe that, all other things being equal, the effect would not have occurred in

the absence of the event (Pearl, 2013). Given this interpretation of causality, conducting a controlled

experiment is an attempt to produce two exchangeable scenarios that are identical in every relevant

respect except for the event that we assume to be the cause of what we expect to observe. In

between-subject experiments, we may ensure exchangeability by randomly assigning the individuals

to the experimental conditions. In within-subject experiments, we may ensure exchangeability by

randomly choosing the temporal order of the experimental condition for each subject (Edgington &

Onghena, 2007). Applying counterfactual reasoning, a properly designed experiment shows us, what

would have happened to an individual in condition A, if it had been assigned to condition B, instead

(and vice versa).

As mentioned in section 1, it is sometimes difficult or even impossible to realize experimental

conditions that are equal in every relevant respect except for the independent variable.

Nevertheless, we may still apply the method of counterfactual reasoning to justify causal inference,

as long as we make our inference conditional on a specific model. In other words, given a theoretical

model, we may use empirical observations to estimate what would have happened if certain

parameters had been equal. In this sense we may justify a claim like "the gravitational field of the sun

causes the earth to move on its observed trajectory", although it is technically, if not physically,

impossible to change the gravitational field of the sun in a controlled experiment to verify our causal

claim. We may, however, justify this causal claim based on a theoretical model that describes the

trajectory of planets in different gravitational fields (e.g., classical mechanics). We can apply the

model to empirical observations regarding the movement of the earth and the other planets in our

solar system and use these data to estimate the gravitational pull of the sun on the earth, as well as

the earth's momentum. Together, these empirical estimates yield a very accurate description of the

earth's trajectory. A causal interpretation can now be justified by leaving the parameterized model

unchanged, except for the parameters that corresponds to the gravitational field of the sun. If we set

the sun's gravitation equal to zero (in our model!), we may then calculate what would have

happened if the sun had not kept the earth in orbit with its gravitational field. The difference of these

two trajectories – the actually observed one and the counterfactual one – quantifies the causal effect

of the sun's gravitational field.

Similar to the above physical example, we can justify theory-based causal inference using

counterfactual reasoning in behavior analysis. Such a theory-based approach would be especially

helpful in situations where it is difficult or impossible to justify a causal interpretation on

experimental grounds. Therefore, here we propose theory-based approach to infer the causal effects

of reinforcement from observed behavior change by means of the above described Multilevel Model

of Behavioral Selection (MLBS) and the Covariance Based Law of Effect (CLOE).

The CLOE describes change due to reinforcement by means of a covariance term, such that a higher

covariance between behavior and reinforcement yields a higher selection and a lower covariance

yields smaller selection. To apply the counterfactual method outlined above, we need to use the

MLBS in the specific conditions that generated the observed data. For example, the theoretical

covariance between a quantitative behavior and the amount of received reinforcement can generally

be obtained from the feedback function of a reinforcement schedule (cf. Borgstede & Luque, 2021).

Similarly, the quantitative behavior itself (and, consequently, behavioral change) can be observed

over several repeated experimental trials. We can then use these empirically derived parameters to

calculate what would have happened in the absence of reinforcement, conditional on the specified

model. In other words, assuming that reinforcement can be described as a behavioral selection

process and that this process is formally captured by the MLBS, we can calculate the counterfactual

behavior by leaving everything in the model unchanged, except for the part that is responsible for

selection to occur (cf. Okasha & Otsuka, 2020). Practically, this means to apply a minimal change to

the model parameters, such that the covariance term becomes zero (because a zero covariance

implies zero selection and hence, no reinforcement effect).

Mathematically, there are several ways to ensure that the covariance term in the CLOE is zero.

However, the most plausible candidate for our counterfactual model is certainly that reinforcement

is set equal across trials, i.e., we set reinforcement equal to the average reinforcement of all

observed trials. For example, if we conduct an experiment with two subsequent trials, we may

observe behavior that yields 10 food items in trial one and 20 food items in trial two. The

counterfactual model would use the actual feedback functions from the two trials, respectively, to

calculate the behavior that would have resulted in the two trials given the individual had continued

doing what it was doing, until average reinforcement (i.e., 15 food items) had been received.

Conditional on the model, the difference between these two counterfactual values for the behavior

in trial one and two corresponds to the behavior change that we would have observed if there had been no behavioral selection (i.e., no reinforcement). Comparing the change with and without selection, we may calculate an empirical estimate of the causal effect of reinforcement by taking the difference between the counterfactual change and the actually observed change.

The proposed method can thus be summarized by the following steps. First, describing the experimental scenario in terms of behavioral selection using the MLBS. Second, using the model to calculate the amount of behavior change that would have occurred in the absence of selection. Third, subtracting this non-selection component of behavior change from the total behavior change observed between trials to obtain the selection component of behavior change. This latter step corresponds to the causal effect of reinforcement on observed behavior change given the specified model.

The counterfactual methodology provides a new way to infer causal effects of reinforcement from observed behavior change, even if reinforcement is confounded with other causes of behavior change. In the following section, we will fully develop the method by applying it to an actual empirical data set. We will show how empirical estimates of the causal effects of reinforcement can be obtained at the level of individual learning, and how these individual causal effects can be tested for statistical significance using a Monte-Carlo simulation approach.

4 Empirical Application: Behavioral Selection Between Learning Trials

We demonstrate how the counterfactual analysis of selection effects described above can be implemented in an empirical study. Our method is applied to the data from two training trials (first and last days) of a behavioral experiment involving nine naïve pigeons. The focus of the main experiment was to investigate the effects of signals for the availability of food items in the holes of a board on foraging behavior (Anselme et al., in press). Here, we focus on the training trials administered prior to the main experiment, consisting of two conditions only ("no reinforcement" vs. "guaranteed reinforcement" at the beginning of a trial). The question we address is, whether the

pigeons actually learned to distinguish between the reinforcement and the non-reinforcement

condition between training trials (i.e., if behavioral selection was effective), or if they primarily relied

on non-associative mechanisms like conditional rules to exploit the available food sources.

Additionally, we investigate the potential contribution of non-selection sources of behavioral change,

such as increased skill and effort.

4.1   Experimental Apparatus and Data Acquisition

4.1.1   Housing

Nine naïve pigeons (4 males and 5 females; age: 5.42±1.15 years) obtained from local breeders were

housed in individual cages under a 12h light/dark cycle (lights on at 7:30 am). The pigeons had ad

libitum access to water in their home cage but were maintained at 85-90% of their free-feeding body

weight for the duration of the experiment, to motivate them for food in the task. They did not

receive any additional food besides the supply to the amounts consumed during a training session.

All procedures were approved by the Ruhr-University and followed the German guidelines for the

care and use of animals in science, and were in accordance with the European Communities Council

Directive 86/609/EEC concerning the care and use of animals for experimentation.

4.1.2   Apparatus

The experimental apparatus consisted of a rectangular wooden box with a net on top to prevent the

pigeons from flying away. The floor was a horizontally removable brown plate of wood (120 cm

length × 70 cm width × 2 cm height), adjusted to the box's size and perforated with holes (1.5 cm

diameter and 2 cm depth). The foraging board contained 60 holes organized as 6 rows of 10 holes

regularly spaced. The board was covered with a black plastic tape with a cross cut above each hole to

create an opening, which allowed the pigeons to access the food items while being unable to visually

detect their presence from a distance (Fig. 1a). An entrance compartment (28.7 cm length × 20.4 cm

width × 36 cm height) was located in the middle of one long side of the box, which was of the same

height. This compartment had two vertical doors on each side, one allowing the experimenter to

introduce the pigeon in the compartment and another giving the pigeon access to the board. Specific

stimuli (green and red; 21 cm length × 14.5 cm width) were used to signal the consistent presence or

absence of food in one area. The two areas were separated by means of a blue-white strip glued on

the plastic tape, dividing the board in two equal left and right areas of 30 holes each from the

entrance compartment. Each session was recorded with an external camera (GoPro – Hero7), placed

above the apparatus.

4.1.3   Procedure

Before using the board with covered holes (see above), the pigeons had to learn that food items

could be found in the board's holes. To this end, the board was initially not covered for 3-4 days,

such that the food items could immediately be detected. At this stage, each of the 60 holes was

baited with one food item (corn, green pea, yellow pea, or sunflower). No discriminative stimuli and

no blue-white strip were used. Following this phase, the covered board was used in association with

the discriminative stimuli and the demarcation strip. In each of the 30 holes of one area (left or right,

counterbalanced within the same individuals), we positioned one food item and this area was

associated with one stimulus (red or green, counterbalanced across individuals) placed on each wall.

The 30 holes of the adjacent area remained empty and associated with the other stimulus placed on

each wall. The pigeons were trained for four days to learn and inspect the covered holes properly.

Practically, a pigeon was placed in the entrance compartment via an external vertical door, which

remained closed during each 10-min daily trial. An internal vertical door giving the pigeon access to

the board was then immediately removed from top and the compartment remained accessible

during the trial—this removal started the trial, during which the pigeon could move on the board,

consume grains in the rewarded area, or spend time in the entrance compartment. After a trial, the

pigeon was picked up by means of a fishing net from the entrance compartment and the number of

food items consumed was manually counted. The board was cleaned and prepared for the next

pigeon. After positioning a food item in a hole, the corners of the cut tape covering the hole were

realigned with a tweezer in order to minimize the risk that the food item was detected. Body weight

was controlled daily.

4.1.4 Data extraction

Data were collected on manual counting (food items consumed, time spent per area, and number of

pecks per area). Determining whether a peck at a hole was successful (food item grasped) or not was

mostly impossible from the videos, so that peck is not synonymous with item consumed. A peck

simply meant a vertical downshift of the pigeon's head above a hole. We considered a pigeon to be

positioned in a given area if its head was in this area—because its body could be in one area and yet

pecking in the adjacent one. A crossing between the two areas was not counted if the pigeon came

from one area, had a quick look of a few seconds above another area, and then went back to the first

one. Sometimes, the pigeon missed a grain (picked it up and lost it), so that it rolled on the board. In

the attempt to get it, the pigeon could cross the demarcation line between two areas. The time spent

pursuing a missed grain in another area was attributed to the area from which the pigeon came in

case it returned to this area after catching the grain. A peck given outside of a hole, even to get a

missed grain, was not counted. A pigeon might flap its wings while on the board, often traveling from

one area to another. No crossing was counted if the pigeon stopped flapping its wings in the same

area as before executing this behavior.

a) Experimental chamber with pigeon (P91)

reinforced   not reinforced

0cm   60cm   120cm

b) Distribution of position over time (day 1)

reinforced   not reinforced

0cm   60cm   120cm

c) Distribution of position over time (day 4)

reinforced   not reinforced

0cm   60cm   120cm

Figure 1: Experimental setup and data collection. (a) Pigeons were put in a 70cmx120cm experimental chamber with 60 covered holes. In the reinforced region, the holes contained food (grains). In the non-reinforced region, the holes were empty. (b, c) Heatmaps show spatial distributions of the pigeon during a 10-minute session for day 1 and day 4, respectively. Duration of visits is indicated by a color gradient ranging from blue (short) over yellow (medium) to red (high). Heatmaps were generated using the ezTrack software (Pennington et al., 2019).

4.2 Statistical Analyses

Pigeons' peck frequency, pecking success and the time spent at the reinforced and non-reinforced region were compared between training trials 1 and 4 using descriptive statistics (mean and standard deviation). Change in average peck frequency and average pecking success were tested for significant deviations from zero ("no change") using one-sided exact permutation tests for paired data to compute p-values for increases in skill and effort, respectively (Edgington & Onghena, 2007). Change in average time spent at the reinforced region was tested for significant deviations from zero ("no change") using two-sided exact permutation tests for paired data.

In order to estimate the causal effect of selection between trials, we parameterized the MLBS under

the assumption that reinforcement was absent using the feedback function of the realized schedule

of reinforcement and the observed behavior of the pigeons. Since the holes in the experimental

chamber were not rebaited during the trials, the probability of finding additional food items

decreased over time spent at the reinforced region, depending on how many food items had already

been consumed. The rate of decrease in reinforcement probability depends on the pigeon's peck

frequency (pecks per time) and the corresponding success rate (probability of retrieving food from a

hole, given the hole contains food). Assuming constant peck frequency and constant pecking success

within trials, the average feedback function at the reinforced region is:

$$R = N - N(1 - \lambda)^t \tag{3.}$$

with R being the expected total amount of reinforcement received until time t, N being the number

of food items in the reinforced region at the beginning of the trial, and λ being a free parameter to

be calculated from the observed behavior for each experimental trial, separately (see Appendix for

mathematical details). Figure 2 depicts the graph of the feedback function for pigeon 91 during the

first experimental trial.

Figure 2: Feedback function in reinforced region given constant effort (pecks/time) and constant skill (consumption/pecks)
for Pigeon 91 on the first day of the experiment. Reinforcement at time t is given by $R = N - N(1 - \lambda)^t$, with a given

number of 30 food items at the beginning (N = 30) and an estimated steepness parameter λ = 0.00242 (which refers to
time measured in seconds).

The individually parameterized feedback functions for the first and the last experimental trials were

then used to construct the counterfactual models for each pigeon. Instead of calculating the

expected amount of reinforcement from time spent in the reinforced region, the inverse of the

feedback function was used to obtain the time it would have taken the pigeon in the respective trial

to obtain average reinforcement (i.e., the arithmetic mean between the actually obtained

reinforcements during the first and last experimental trials). If the calculated value exceeded the trial

length (600 s), the maximum possible value (i.e., 600 s) was used. The difference between these

counterfactual values of the time spent at the reinforced region yields the amount of behavior

change we would have observed if there had been no behavioral selection. This difference

corresponds to the residual term, δ, in the CLOE. Given the actually observed change in time spent in

the reinforced region, Δb, and the residual change, δ, from the counterfactual model, behavioral

selection, $\Delta_S b$, can be calculated for each pigeon separately using Equation 2.

To test whether the individual selection terms, $\Delta_S b$, are significantly different from zero, the

parameterized counterfactual model was simulated for 10000 pairs of trials for each pigeon,

separately. In every iteration of the simulation, the time needed to reach average reinforcement in

the first and the last training trial was used to calculate the corresponding behavior change. Under

the null hypothesis that there is no selection, the distribution of the simulated behavioral change

values from the counterfactual model resembles the sampling distribution, from which the actually

observed behavior change was drawn. The quantiles of this sampling distribution were used to

calculate one-sided p-values for each pigeon (compare Figure 3 and Appendix for technical details). If

a p-value yielded a significant result at the 5%-level, the null hypothesis was rejected in favor of the

alternative, that the observed change was at least partly caused by selection. The p-values from the

individual-level significance tests were further combined multiplicatively using Fisher's method to

obtain a meta-analytic result for the significance at a group level (Fisher, 1938). The overall p-value

tests against the null hypothesis that there is no selection effect in the population. All statistical

analyses and simulations were conducted using the software R, version 4.0.3 (R Core Team, 2020).

Figure 3: Sampling distribution to test for significant change due to selection between trials (Pigeon 91) obtained from
10000 runs of a Monte-Carlo-Simulation using the counterfactual model (without selection) as the generating model. The
expectation of the sampling distribution corresponds to the analytically derived value for $\delta = -426$ s. The gray shading
indicates the region of rejection for a one-sided significance test with $H_0: \Delta_S b = 0$. The red star indicates the observed
difference in behavior between trials ($\Delta b = -251$ s). Despite this negative change in behavior, the counterfactual model
implies that there is in fact a considerable positive selection ($\Delta_S b = 175$ s), which is statistically significant at $\alpha = .05$ (p =
.0087).

4.3   Results

Table 1 summarizes the pigeons' behavior during the first and the last trial of training, respectively.

The main behavioral metric was the time spent at the reinforced region per trial (measured in s). The

average time spent at the reinforced region during the first trial was 429 s (*SD* = 99 s), which makes

up 72% of the total time (600 s). In other words, pigeons prefer the reinforced region right from the

beginning. The average time spent at the reinforced region during the last trial was 305 s (*SD* = 159

s), which makes up only 51% of the total time (600 s). Thus, average time at the reinforced region

decreased over training trials (*p* = .027). Average foraging effort, as given by peck frequency while in

the reinforced region (pecks per second, measured in s^{-1}), increased from the first trial (*M* = 0.53 s^{-1},

SD = 0.27 s^{-1}) to the last trial (*M* = 71 s^{-1}, *SD* = 0.28 s^{-1}). Hence, average effort increased over trials (*p* =

.015). Average skill, as given by the number of consumed food items per peck (food items per peck,

dimensionless number), also increased from the first trial ($M = 0.07$, $SD = 0.05$) to the last trial ($M =$

0.13, $SD = 0.07$), indicating an average increase in skill across trials ($p = .016$). The observed changes

in effort and skill are illustrated by Figure 4a and 4b, respectively.

Table 1: Comparison of first and last training trial (day 1 and day 4) with respect to the time spent at the reinforced region,
the pecks performed per second (peck frequency) and the grains consumed per peck while in the reinforced region (success
rate).

	Time at reinforced region[a]		Peck frequency[b]		Success rate[c]	
	first trial	last trial	first trial	last trial	first trial	last trial
P17	586 (95 %)	585 (96 %)	0.40	0.15	0.09	0.26
P73	483 (84 %)	382 (63 %)	0.67	0.89	0.04	0.05
P91	544 (89 %)	293 (48 %)	0.84	0.91	0.05	0.11
P96	293 (74 %)	105 (80 %)	0.81	1.11	0.05	0.15
P97	407 (83 %)	187 (76 %)	0.52	0.80	0.05	0.13
P103	413 (72 %)	437 (78 %)	0.11	0.77	0.02	0.06
P118	298 (70 %)	165 (79 %)	0.39	0.63	0.07	0.07
P519	399 (73 %)	410 (74 %)	0.22	0.49	0.2	0.14
P534	441 (79%)	182 (91 %)	0.82	0.64	0.05	0.15
Mean	429	305	0.53	0.71	0.07	0.13
SD	99	159	0.27	0.28	0.05	0.07

488   [a]measured in s, percentage in brackets refers to the total time spent in the reinforced and the nonreinforced region;
489   [b]measured in 1/s; [c] dimensionless number

Figure 4: Changes in a) effort (peck frequency measured in pecks per second) and b) skill (success rate measured in consumed food items per peck) from the first day of training to the last day of training.

Table 2 shows the results from the counterfactual analysis. In accordance with the descriptive data, the observed change in time spent at the reinforced region, Δb, was negative for all but two individuals (pigeons 103 and 519), with an average value of -124 s (SD = 114 s). The counterfactual model revealed that this negative behavior change is the result of non-selection factors, δ, that were even stronger in the absence of behavioral selection (M = -303 s, SD = 143 s). Thus, the observed negative change is what remains of these non-selection factors after the effect of behavioral selection has been accounted for. The corresponding selection effects, $\Delta_S b$, were positive for all but one pigeon (pigeon 118). Hence, although the observed change between training trials was generally negative, there was actually positive change due to selection (M = 179 s, SD = 158 s). The individual-level statistical analyses were significant in four of the nine pigeons, indicating that the data was only conclusive in about half the individuals. However, the meta-analytically combined p-value across all individuals yielded a significant overall selection effect (p < .0001). The results from the counterfactual analysis are illustrated in Figure 5, which shows that behavioral selection was generally positive, despite a negative overall change in behavior.

Table 2: Partitioning of total behavioral change in time spent at reinforced region from first to last training day. Total behavioral change (Δb) is expressed as the sum of change due to selection ($\Delta_S b$) and residual change (δ). P-values were calculated using a Monte-Carlo approximation to the sampling distribution under the null hypothesis ($H_0: \Delta_S b = 0$).

	Behavior Change (Δb)	Selection ($\Delta_S b$)	Residual (δ)	Significance[a] (p)
P17	-1	68	-69	.310
P73	-101	136	-237	.240
P91	-251	175	-426	.009*
P96	-188	118	-306	.130
P97	-220	262	-482	.013*
P103	24	442	-418	.0001*
P118	-133	-28	-105	.619
P519	11	391	-380	.0003*
P534	-259	42	-301	.411
Mean[b]	-124	179	-303	< .0001*
SD	114	158	143	–

Δb, $\Delta_S b$ and δ measured in s; [a]approximated p-values obtained from Monte-Carlo simulation; [b]combined p-value calculated using Fisher's method; *statistically significant selection term ($\alpha = .05$)

Partitioning of behavior change

Figure 5: Partitioning of behavior change (time spent at reinforced region) into selection and non-selection (i.e., residual) components using the Covariance Based Law of Effect (CLOE).

5 Discussion

In this paper, we proposed a new method to estimate the causal effects of reinforcement in terms of behavioral selection by means of counterfactual reasoning. The method builds on a formal theory of reinforcement, the Multilevel Model of Behavioral Selection (MLBS), that allows to partition observed changes in average behavior into a behavioral selection component and a non-selection component. Applying the MLBS to empirical data, we showed how the causal effects of reinforcement can be inferred from empirical data, even if reinforcement is masked by other factors. The rationale was to use the MLBS to simulate what would have happened if selection had been absent. The difference between this (counterfactual) behavior change and the observed (actual) behavior change yields an estimate for the causal effect of reinforcement. We further proposed a Monte-Carlo simulation framework to statistically test against the null hypothesis that reinforcement was absent at the level of single individuals. These individual p-values can then be combined using meta-analytic methods.

A first application of the method to the training data from a reinforcement experiment with pigeons revealed that the proposed method is indeed capable to separate selection effects (i.e., behavior change due to reinforcement) from non-selection effects (such as changes due to increasing effort and skill). Although the observed change between training trials was negative (i.e., individuals tended to spend less time at the reinforced region), there was in fact strong evidence for positive behavioral selection. However, these selection effects were masked by significant increases in skill and effort. In other words, the pigeons did not only learn where the food was, but also became more efficient in retrieving the food from the apparatus. Thus, the decrease in time spent in the reinforced region did not result from food acting as a punisher (which would be highly implausible in this context), but from pigeons spending less time foraging due to increased skills. In fact, during the last training trial, several pigeons only engaged in foraging behavior for a rather short time period and spent the rest of the trial with other activities, such as wing flapping or preening. These results indicate that reinforcement, skill and effort all contribute to the observed behavior. Moreover, since all pigeons

showed a strong bias towards the reinforced region even in the first trial, it seems likely that the

adaptive response of the individuals is at least partly caused by non-associative mechanisms. This

conclusion is supported by the qualitative aspects of the pigeons' behavior during the first trial.

Pigeons seemed to randomly move through the experimental chamber and occasionally peck, until

they encountered food. Subsequently, they would move much less and more slowly, which in turn

might have resulted in an increased probability of obtaining more food and an increased amount of

time spent at the region where they found food. As mentioned in the introduction, such a behavior

might be caused by a local decision rule ("If you find food, move less!"), rather than reinforcement.

The existence of such a rule is compatible with the marginal value theorem from optimal foraging

theory (Charnov, 1976). It predicts that a patch will be abandoned when its resources deplete to the

point that the next expected reward falls below the average reward in the patch. It also predicts that

a longer transit time between two patches will maintain the forager longer in the depleting patch.

Here, the transit time between the two adjacent areas was short but one of them contained no food

at all, giving a signal to the pigeons that there was no patch of interest around. This is likely to have

kept the pigeons in the reinforced area. A similar propensity to spend time, peck, and visit the food-

richest area compared to poorer areas was also shown (Anselme et al., in press). Furthermore, in the

presence of a single patch type, pigeons visit adjacent holes more often when food density is higher

at the beginning of a trial (Wittek et al., 2022). The rule "If you find food, move less!" would explain

these results, even if it was hardwired in the pigeon's brain and thus independent of individual

experiences. However, the rule itself does not tell us how individual pigeons convert it into action.

Reinforcement could be a second-order process based on this rule, capable of influencing behavior at

an individual level. Indeed, our findings suggest considerable inter-individual variation in both the

selection and non-selection effects, which might be related to distinct "temperaments" among the

individuals.

We present the first empirical application of the MLBS in the context of a reinforcement experiment.

The results show that the MLBS provides a feasible theoretical foundation for the experimental

analysis of behavior and thereby demonstrate the strength of the selectionist approach to

reinforcement. Future work may extend the method to further disentangle non-selection effects

such as skill and effort, alongside with other potential sources of behavioral change.

The proposed selection framework acknowledges that reinforcement cannot be isolated as an

independent variable. The resulting methodology allows to infer causal effects of reinforcement even

if behavior is in a non-equilibrium state. Shifting the focus away from steady-state analysis (such as

the application of the generalized matching law), the proposed method specifically applies to

behavior that is currently changing, such as the adaptive dynamics during operant training. In

general, data from training trials are rather messy due to various uncontrollable factors affecting

behavior simultaneously. We think that the counterfactual analysis of behavioral selection provides

the necessary tools to deal with these data. However, it should not be concluded that non-selection

effects necessarily operate against predictors of reinforcement such as food. Among them, indirect

predictors of reinforcement could exist, such as information about the consistency of cue-food

pairings. For example, in a free-choice task, pigeons often prefer an option in which a consistent cue-

food pairing occurs rarely (e.g., red probability = 20% but if red $\rightarrow$ 100% chance of one food item) to

another option in which more food is delivered but the cue-food pairing is inconsistent (e.g., blue

and yellow probability = 50% and whether blue or yellow $\rightarrow$ 50% chance of three food items)

(Anselme, 2022; Fortes et al., 2016; McDevitt et al., 2016; Zentall, 2016). Parameters that control

information seeking might be relevant predictors of reinforcement even if their influence may be less

direct and possibly independent from food (e.g., Inglis et al., 1997).

The general methodology of model-based counterfactual analysis can be applied to many other

experimental setups that involve behavioral change over time – probably, there are already

thousands of unused training data sets only awaiting to be analyzed. The partitioning of behavior

change into selection and non-selection components may equally be applied in naturalistic settings,

such as actual foraging behavior. Moreover, the method provides a promising framework to analyze

the complexities of human behavior, such as the relation between reinforcement and competence

gain in students' learning behavior or the interaction between reinforcement and verbal instruction

in the formation of rule-governed behavior. We hope that this article contributes to the foundations

of behavioral selection as a general theory of behavior, and encourages other researchers to put the

behavioral selection perspective into practice.

6   Author Contributions

600 XX developed the modeling framework and the statistical methodology, analyzed the data and wrote

601 the original draft. XY planned and conducted the experiments, collected the data and contributed to

602 the theoretical background and the interpretation of the results. Both authors contributed to the

603 final version of the manuscript.

7   Competing Interests

605 The authors declare no competing interests.

8   Data and Code Availability

607 The original data and R-code used in this study will be made publicly available on publication.

9   Funding

609 This research was supported by the Deutsche Forschungsgemeinschaft through An1067/3-1 (PA).

10 Appendix

10.1 Derivation of Feedback Function

612 At each time step, there are $N(t)$ food items present in the reinforced region. Given that a single

613 food item is consumed with probability λ, the expected value of reinforcement at each time step is

614 $N(t)\lambda$. We can thus express the expected change in reinforcement from one time step (t) to the next

615 time step ($t + 1$) by the following difference equation:

616
$$\Delta R(t) = N(t)\lambda$$

617   The corresponding recursion equation is:

618
$$R(t+1) = R(t) + N(t)\lambda$$

619   Since $R(t) = N - N(t)$, by substitution we obtain:

620
$$R(t+1) = N - N(t) + N(t)\lambda = N - N(t)(1-\lambda)$$

621   The general solution of this dynamic equation is:

622
$$R(t) = N - N(1-\lambda)^t$$

This corresponds to the feedback function of expected reinforcement given constant peck rate and

constant pecking success.

10.2 Calculation of individual p-values

Assuming that time steps are small enough, such that an individual can never consume more than

one food item per time step, the probability of being reinforced in a given time step equals the

probability of at least one success, which is given by $1 - (1-\lambda)^{N(t)}$.

We can thus simulate the pigeon's behavior as a series of random reinforcement events with a

reinforcement probability of $1 - (1-\lambda)^{N(t)}$ at each time step. The parameter λ is estimated from

the observed data using the feedback function. $N(t)$ is calculated as the result of the previous

reinforcement events, i.e., starting at the total number of available food items, $N(t)$ is reduced by 1

in every time step that yields reinforcement. The simulation is run for the first and last training trial

(with λ being estimated from the observed behavior in the corresponding trial), until average

reinforcement (i.e., the arithmetic mean of the observed reinforcement over both trials) or the

maximum possible time (i.e., the length of one experimental trial) are reached.

The simulation was repeated 10000 times to approximate the sampling distribution, from which the

actually observed behavior has been drawn. The quantiles of this sampling distribution yield a critical

value for the region of rejection, as well as the approximate p-value of the observed data, given the

data was generated by the specified model.

11 References

Anselme, P. (2022). The optimality of "suboptimal" choice: A psycho-evolutionary perspective. In M.

Krause, K. L. Hollis, & M. R. Papini (Eds.), *Evolution of Learning and Memory Mechanisms*

(pp. 193–209). Cambridge University Press.

Anselme, P., Dreher, T., & Güntürkün, O. (2018). Pigeons consistently prefer easy over harder access

to food: No reversal after direct dopaminergic stimulation. *Behavioral Neuroscience*, *132*(4),

293–301. https://doi.org/10.1037/bne0000249

Anselme, P., Wittek, N., Oeksuez, F., & Güntürkün, O. (in press). Overmatching under food

uncertainty in foraging pigeons. *Behavioural Processes*.

Baum, W. M. (2012). Rethinking reinforcement: Allocation, induction, and contingency. *Journal of the*

Experimental Analysis of Behavior, *97*(1), 101–124. https://doi.org/10.1901/jeab.2012.97-

101

Baum, W. M. (2017). Selection by consequences, behavioral evolution, and the price equation.

Journal of the Experimental Analysis of Behavior, *107*(3), 321–342.

https://doi.org/10.1002/jeab.256

Berlyne, D. E. (1957). Uncertainty and conflict: A point of contact between information-theory and

behavior-theory concepts. *Psychological Review*, *64, Part 1*(6), 329–339.

https://doi.org/10.1037/h0041135

Berridge, K. C., & Robinson, T. E. (2016). Liking, wanting, and the incentive-sensitization theory of

addiction. *The American Psychologist*, *71*(8), 670–679. https://doi.org/10.1037/amp0000059

Borgstede, M. (2020). An evolutionary model of reinforcer value. *Behavioural Processes*, 104109.

https://doi.org/10.1016/j.beproc.2020.104109

Borgstede, M. (2021). Why do individuals seek information? A selectionist perspective. *Frontiers in*

Psychology. https://doi.org/10.3389/fpsyg.2021.684544

Borgstede, M., & Eggert, F. (in press). Squaring the Circle: From Latent Variables to Theory Based

Measurement. *Theory & Psychology*.

Borgstede, M., & Eggert, F. (2021). The formal foundation of an evolutionary theory of

reinforcement. *Behavioural Processes*, *186*, 104370.

https://doi.org/10.1016/j.beproc.2021.104370

Borgstede, M., & Luque, V. J. (2021). The covariance based law of effect: A fundamental principle of

behavior. *Behavior and Philosophy*, *49*, 63–81. https://behavior.org/wp-

content/uploads/2022/01/BP-v49-Borgstede2.pdf

Broadbent, D. E. (1961). *Behaviour*. Methuen.

Campbell, D. T. (1956). Adaptive behavior from random response. *Behavioral Science*, *1*(2), 105–110.

https://doi.org/10.1002/bs.3830010204

Charnov, E. L. (1976). Optimal foraging, the marginal value theorem. *Theoretical Population Biology*,

9(2), 129–136. https://doi.org/10.1016/0040-5809(76)90040-X

Davison, M., & McCarthy, D. (2016). *The Matching Law*. Routledge.

https://doi.org/10.4324/9781315638911

Dugard, P., File, P., & Todman, J. B. (2012). *Single-case and small-n experimental designs: A practical*

guide to randomization tests (2. ed.). Routledge.

Edgington, E., & Onghena, P. (2007). *Randomization Tests, Fourth Edition* (4th ed.). *Statistics*. CRC

Press.

Eilam, D., Zor, R., Szechtman, H., & Hermesh, H. (2006). Rituals, stereotypy and compulsive behavior

in animals and humans. *Neuroscience and Biobehavioral Reviews*, *30*(4), 456–471.

https://doi.org/10.1016/j.neubiorev.2005.08.003

Ferster, C. B., & Skinner, B. F. (1957). *Schedules of reinforcement*. Appleton-Century-Crofts.

https://doi.org/10.1037/10627-000

Fisher, R. A. (1938). *Statistical methods for research workers* (7. ed., rev. and enl). *Biological*

monographs and manuals. Oliver & Boyd.

Fortes, I., Vasconcelos, M., & Machado, A. (2016). Testing the boundaries of "paradoxical"

predictions: Pigeons do disregard bad news. *Journal of Experimental Psychology. Animal*

Learning and Cognition, *42*(4), 336–346. https://doi.org/10.1037/xan0000114

Gilbert, R. M. (1970). Psychology and biology. *Canadian Psychologist/Psychologie Canadienne*, *11*(3),

221–238. https://doi.org/10.1037/h0082574

Hendry, D. P. (1965). *Reinforcing Value of Information: NASA Technical Report No. 65-1.* University of

Maryland.

Herrnstein, R. J. (1961). Relative and absolute strength of response as a function of frequency of

reinforcement. *Journal of the Experimental Analysis of Behavior*, *4*, 267–272.

https://doi.org/10.1901/jeab.1961.4-267

Herrnstein, R. J. (1964). Will. *Proceedings of the American Philosophical Society,*, *108*(6), 455–458.

Inglis, Forkman, & Lazarus (1997). Free food or earned food? A review and fuzzy model of

contrafreeloading. *Animal Behaviour*, *53*(6), 1171–1191.

https://doi.org/10.1006/anbe.1996.0320

Kamin, L. J. (1969). Predictability, surprise, attention and conditioning. In B. A. Campbell & R. M.

Church (Eds.), *Punishment and aversive behavior* (pp. 279–296).

Lemos, J. C., Wanat, M. J., Smith, J. S., Reyes, B. A. S., Hollon, N. G., van Bockstaele, E. J., Chavkin, C.,

& Phillips, P. E. M. (2012). Severe stress switches CRF action in the nucleus accumbens from

appetitive to aversive. *Nature*, *490*(7420), 402–406. https://doi.org/10.1038/nature11436

Lewis, D. (1973). Causation. *The Journal of Philosophy*, *70*(17), 556. https://doi.org/10.2307/2025310

Lewis, D. (2000). Causation as Influence. *The Journal of Philosophy*, *97*(4), 182.

https://doi.org/10.2307/2678389

Luque, V. J. (2017). One equation to rule them all: a philosophical analysis of the Price equation.

Biology & Philosophy, *32*(1), 97–125. https://doi.org/10.1007/s10539-016-9538-y

Luque, V. J., & Baravalle, L. (2021). The mirror of physics: on how the Price equation can unify

evolutionary biology. *Synthese*, *199*, 12439–12462. https://doi.org/10.1007/s11229-021-

03339-6

McDevitt, M. A., Dunn, R. M., Spetch, M. L., & Ludvig, E. A. (2016). When good news leads to bad

choices. *Journal of the Experimental Analysis of Behavior*, *105*(1), 23–40.

https://doi.org/10.1002/jeab.192

McNamara, J. M., & Houston, A. I. (2009). Integrating function and mechanism. *Trends in Ecology &*

Evolution, *24*(12), 670–675. https://doi.org/10.1016/j.tree.2009.05.011

Menzies, P., & Price, H. (1993). Causation as a Secondary Quality. *The British Journal for the*

Philosophy of Science, *44*(2), 187–203. https://doi.org/10.1093/bjps/44.2.187

Okasha, S., & Otsuka, J. (2020). The Price equation and the causal analysis of evolutionary change.

Philosophical Transactions of the Royal Society of London. Series B, Biological Sciences,

375(1797), 20190365. https://doi.org/10.1098/rstb.2019.0365

Palmer, D. C., & Donahoe, J. W. (1992). Essentialism and selectionism in cognitive science and

behavior analysis. *The American Psychologist*, *47*(11), 1344–1358.

https://doi.org/10.1037/0003-066X.47.11.1344

Pearl, J. (2013). *Causality: Models, reasoning, and inference* (Second edition, reprinted with

corrections). Cambridge Univ. Press.

Pennington, Z. T., Dong, Z., Feng, Y., Vetere, L. M., Page-Harley, L., Shuman, T., & Cai, D. J. (2019).

Eztrack: An open-source video analysis pipeline for the investigation of animal behavior.

Scientific Reports, *9*(1), 19979. https://doi.org/10.1038/s41598-019-56408-9

Premack, D., & Premack, A. J. (1963). Increased eating in rats deprived of running. *Journal of the*

Experimental Analysis of Behavior, *6*, 209–212. https://doi.org/10.1901/jeab.1963.6-209

Price, G. R. (1970). Selection and Covariance. *Nature*, *227*(5257), 520–521.

https://doi.org/10.1038/227520a0

Price, G. R. (1972). Extension of covariance selection mathematics. *Annals of Human Genetics*, *35*(4),

485–490. https://doi.org/10.1111/j.1469-1809.1957.tb01874.x

Pringle, J. (1951). On the Parallel Between Learning and Evolution. *Behaviour*, *3*(1), 174–214.

https://doi.org/10.1163/156853951X00269

R Core Team. (2020). *R: A Language and Environment for Statistical Computing*. https://www.R-

project.org/

Skinner, B. F. (1965). *Science and Human Behavior*. Free Press.

https://ebookcentral.proquest.com/lib/gbv/detail.action?docID=4934291

Skinner, B. F. (1966). The phylogeny and ontogeny of behavior. Contingencies of reinforcement

throw light on contingencies of survival in the evolution of behavior. *Science (New York,*

N.Y.), *153*(3741), 1205–1213. https://doi.org/10.1126/science.153.3741.1205

Skinner, B. F. (1981). Selection by consequences. *Science (New York, N.Y.)*, *213*(4507), 501–504.

Staddon, J. E. R. (2020). The Role of Theory in Behavior Analysis: A Response to Unfinished Business,

Travis Thompson's Review of Staddon's New Behaviorism (2nd edition). *The Psychological*

Record, 1–7. https://doi.org/10.1007/s40732-020-00409-y

Strand, P. S., Robinson, M. J. F., Fiedler, K. R., Learn, R., & Anselme, P. (2021). Quantifying the

instrumental and noninstrumental underpinnings of Pavlovian responding with the Price

equation. *Psychonomic Bulletin & Review.* Advance online publication.

https://doi.org/10.3758/s13423-021-02047-z

Thorndike, E. L. (1900). The associative processes in animals. *Biological Lectures from the Marine*

Biological Laboratory of Woods Holl, 1899, 69–91.

Timberlake, W., & Allison, J. (1974). Response deprivation: An empirical approach to instrumental

performance. *Psychological Review*, *81*(2), 146–164. https://doi.org/10.1037/h0036101

Wang, M. Z., & Hayden, B. Y. (2019). Monkeys are curious about counterfactual outcomes. *Cognition*,

189, 1–10. https://doi.org/10.1016/j.cognition.2019.03.009

Wittek, N., Oeksuez, F., Güntürkün, O., & Anselme, P. (2022). More opportunities to peck for

identical food availability increases foraging efficiency in pigeons. *Behaviour*, 1–24.

https://doi.org/10.1163/1568539X-bja10173

Zentall, T. R. (2016). Resolving the paradox of suboptimal choice. *Journal of Experimental Psychology.*

Animal Learning and Cognition, *42*(1), 1–14. https://doi.org/10.1037/xan0000085