

1 **The nervous system leverages the non-linear properties of the Achilles tendon to regulate**
2 **ankle impedance during postural control**

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23 final version.

24 **ABSTRACT**

25 Regulating ankle impedance is essential for controlled interactions with the environment and
26 rejecting unexpected disturbances. Ankle impedance in the sagittal plane depends strongly on the
27 triceps surae and Achilles tendon, but their relative contributions remain unknown. It is commonly
28 assumed that ankle impedance is controlled by changing muscle activation and, thereby, muscle
29 impedance, but this ignores the fact that tendon impedance also changes with loading caused by
30 increases in muscle activation. Thus, we sought to determine the relative contributions from the
31 triceps surae and Achilles tendon during conditions relevant to postural control. We used a novel
32 technique that combines B-mode ultrasound imaging with joint-level perturbations to quantify
33 ankle, muscle, and tendon impedance simultaneously across activation levels from 0 – 30% of
34 maximum voluntary contraction. We found that muscle and tendon stiffness, the static component
35 of impedance, increased with voluntary plantarflexion contractions, but that muscle stiffness
36 exceeded tendon stiffness at very low loads (21 ± 7 N). Above these loads, corresponding to 1.3%
37 of maximal strength for an average participant in our study, ankle stiffness was determined
38 predominately by Achilles tendon stiffness. Hence, the nervous system leverages the non-linear
39 properties of the Achilles tendon to increase ankle stiffness during postural conditions.

40

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44 Muscle, tendon, ankle, impedance, stiffness, ultrasound imaging

45 **BACKGROUND**

46 The ability to adapt the mechanical properties of the ankle is essential for seamlessly
47 transitioning across different terrains when walking and for maintaining postural stability when
48 unexpectedly perturbed [1, 2]. The triceps surae muscles and the Achilles tendon are the primary
49 determinants of ankle mechanics in the sagittal plane, but their relative contributions remain
50 largely unknown. It is commonly assumed that changes in ankle mechanics during active
51 contractions are largely determined by the activation-dependent properties of muscle [3-5], but
52 there have been limited *in vivo* measurements validating this presumption. Determining how the
53 triceps surae and Achilles tendon mechanics contribute to ankle mechanics across a broad range
54 of physiological conditions would provide fundamental insight into the mechanisms underlying
55 humans' ability to navigate their physical world. Such knowledge could also aid in developing
56 targeted interventions when musculotendon mechanics are altered due to neuromuscular
57 pathologies, or biomimetic assistive devices [4, 6]. As such, we sought to determine the relative
58 contribution from the triceps surae and Achilles tendon to the mechanics of the ankle.

59 The assumed primary role of muscle in determining the mechanical properties of the ankle is
60 based on two assumptions. The first is that muscle impedance is substantially lower than tendon
61 impedance for most physiological conditions. Impedance—a quantitative measure of mechanics—
62 describes the dynamic relationship between an imposed displacement and the evoked forces or
63 torques [7]. Due to the serial connection between the muscle and tendon, ankle impedance will be
64 determined mainly by the component with the lowest impedance when the impedance of each
65 component differs substantially. The Achilles tendon is long and compliant [8, 9], and its
66 impedance relative to that of the triceps surae is unknown. Therefore, muscle impedance may not
67 be substantially lower than tendon impedance during physiologically relevant conditions.

68 The second assumption is that tendon impedance is constant across loads and that changes in
69 joint impedance must therefore be due to changes in muscle impedance. Nearly all experimental
70 studies quantifying muscle and tendon mechanics have focused on stiffness, the static component
71 of impedance. It is well known from *in vivo* experiments that muscle stiffness changes with the
72 activation-dependent changes in muscle force [10, 11]. Several studies have measured tendon
73 stiffness *in vivo*, but often relying on the assumption that it remains constant across loads [12-15].
74 While this is a reasonable assumption at high loads (above approximately 30% of maximum force)
75 [16, 17], tendons have a non-linear stress-strain relationship that results in load-dependent stiffness

76 properties in the lower load regime within the “toe-region” [16, 17]. Ultimately, accounting for the
77 non-linear properties of the tendon could impact the relative contributions from the muscle and
78 tendon to the stiffness of the joint.

79 There is conflicting experimental evidence on how triceps surae and Achilles tendon stiffness
80 vary with respect to each other and their relative contributions to ankle stiffness. This stems from
81 the fact that few studies have examined muscle and tendon stiffness over a wide range of loads
82 relevant to common functional tasks. Previously, it has been observed that tendon stiffness is
83 greater than muscle in experiments that only considered activation levels above approximately
84 30% of the maximum voluntary contraction (MVC) [12]. In contrast, others have observed that
85 the Achilles tendon is more compliant than the triceps surae during standing [18], which typically
86 occurs around 15% MVC [19]. These conflicting results may be due partly to differences in the
87 tested range of muscle activations. To our knowledge, no one has bridged the gap between these
88 estimates and quantified the relative contribution from the muscle and tendon across a range of
89 activations that are relevant to many functional tasks.

90 The objective of this study was to determine how the triceps surae and Achilles tendon
91 contribute to the impedance of the ankle during conditions relevant to postural control. We used
92 an innovative technique that combines joint-level perturbations with B-mode ultrasound to
93 quantify ankle, muscle, and tendon impedance [20]. Given the limited and conflicting experimental
94 data reported in the literature, we tested the null hypothesis that the muscle and tendon contribute
95 equally to ankle impedance to determine which structure was most dominant over contraction
96 levels ranging from 0 to 30% MVC. Our results help determine the mechanisms contributing to
97 the regulation of human ankle impedance, as needed for seamless interactions with the
98 environment. As a secondary objective, we quantified the frequency ranges over which muscles
99 and tendons behave elastically. Though there are conditions for which muscles and tendons exhibit
100 spring-like behavior, both structures are viscoelastic [21, 22]. Until recently [20], it has not been
101 possible to quantify muscle and tendon impedance *in vivo* in humans. As such, it is unknown under
102 which conditions it is reasonable to assume that muscles and tendons behave as simple springs
103 with only a stiffness component and when they exhibit more complex mechanical properties. We,
104 therefore, quantified these regimes in this study.

105

106 **METHODS**

107 *Participants*

108 Seventeen healthy young adults (age = 27 ± 3 years (mean \pm standard deviation); height = 1.7
109 ± 0.1 m; body mass = 73 ± 15 kg, 8 males and 9 females) participated in this experiment. All
110 participants were right leg dominant and had no history of neuromuscular or musculoskeletal
111 injuries to their right leg. All participants provided informed consent prior to participation. The
112 Northwestern University Institutional Review Board approved the study, and all methods were
113 carried out according to the approved protocols (STU00009204 & STU00213839).

114

115 *Experimental setup*

116 Participants were seated in an adjustable chair (Biodex Medical Systems, Inc. Shirley, NY),
117 with their trunk and torso stabilized with safety straps (Fig 1). Participants' right leg was extended
118 in front of them with their knee flexed at 15° . A knee brace (Innovator DLX, Ossur, Reykjavik,
119 Iceland) stabilized the knee in this position. The participant's right foot was attached rigidly to an
120 electric rotary motor (BSM90N-3150AF, Baldor, Fort Smith, AR) via a custom-made fiberglass
121 cast at an ankle angle of 90° . The cast encased the entire foot, extending distally from the medial
122 and lateral malleoli to the toes, thus preserving the full range-of-motion of the ankle but preventing
123 any movement of the foot or toes. The axis of rotation of the motor was aligned with the ankle
124 center of rotation in the sagittal plane, restricting all movement to the plantarflexion/dorsiflexion
125 direction. Electrical and mechanical safety stops limited the rotation of the motor within the
126 participant's range of motion. A 24-bit quadrature encoder integrated with the motor measured
127 ankle angle (24-bit, PCI-QUAD04, Measurement Computing, Norton, MA), while a 6-degree-of-
128 freedom load cell (45E15A4, JR3, Woodland, CA) measured all ankle forces and torques.
129 Throughout the experiment, the motor was controlled in real-time via xPC target (MATLAB,
130 Mathworks, Natick, MA).

131 Single differential bipolar surface electrodes (Bagnoli, Delsys Inc, Boston, MA) measured
132 muscle activity from the medial and lateral gastrocnemius and soleus (ankle plantarflexors) and
133 the tibialis anterior (ankle dorsiflexor). Standard skin preparation methods were performed prior
134 to electrode placement [23], and electrodes were placed on the belly of the muscle.
135 Electromyography (EMG) signals were amplified to maximize the signal resolution in each
136 channel. EMG data were collected for visual feedback provided to the subjects. All analog data

137 were passed through an antialiasing filter (500 Hz using a 5-pole Bessel filter) and sampled at 2.5
138 kHz (PCI-DAS1602/16, Measurement Computing, Norton, MA, USA).

139 A B-mode ultrasound system using a linear transducer (LV7.5/60/128Z-2, LS128, CExt,
140 Telemed, Lithuania) recorded images of the medial gastrocnemius muscle-tendon junction (MTJ).
141 A custom-made probe holder and elastic adhesive wrap (Coban™, 3M, St. Paul, MN) secured the
142 probe to the leg. We positioned the ultrasound probe to center the MTJ on the image. At the start
143 of ultrasound data collection, a trigger signal was used to synchronize the ultrasound data
144 collection with all other measurements. Ultrasound images were acquired with a mean frame rate
145 of 124 Hz. All ultrasound data were saved for processing offline.

146

147 *Protocol*

148 At the start of each experiment, we collected three 10-second isometric maximum voluntary
149 contractions (MVC) trials in both the plantarflexion and dorsiflexion directions. These data were
150 used to scale the visual feedback provided to the participants.

151 Our primary objective was to determine how muscle, tendon, and ankle impedance vary across
152 various levels of plantarflexion torque. This was accomplished by instructing participants to
153 produce different levels of isometric plantarflexion torque while the rotary motor applied small
154 rotational perturbations in the sagittal plane. We used pseudo-random binary sequence (PRBS)
155 perturbations with an amplitude of 0.175 radians, a maximum velocity of 1.75 radians per second,
156 and a switching time of 153 ms. We tested seven isometric plantarflexion torque levels from 0%
157 to 30% MVC in 5% increments. Participants were provided real-time visual feedback of their
158 normalized plantarflexion torque. Tibialis anterior EMG was also provided to prevent co-
159 contraction. Rectified EMG and torque signals were low pass filtered at 1 Hz to remove high-
160 frequency components from the applied perturbations (2nd order Butterworth). Subjects completed
161 three trials at each level of plantarflexion torque in a randomized fashion. Each trial lasted 65
162 seconds. Rest breaks were provided as needed between trials to prevent fatigue.

163 The measured ankle torque included the gravitational and inertial contributions from the
164 apparatus connecting the foot to the motor. A single trial was collected with only the cast attached
165 to the rotary motor enabling us to remove these contributions from the net torque measured in each
166 trial.

167

168 *Data processing and analysis*

169 All data were processed and analyzed using custom-written software in MATLAB. The same
170 individual manually digitized the MTJ within each frame of the ultrasound videos [20]. All
171 ultrasound data were resampled using linear interpolation to match the sampling rate of the other
172 experimental signals (2.5 kHz).

173 We computed ankle, muscle, and tendon impedance as described previously [20]. Briefly, we
174 used non-parametric system identification to estimate ankle, muscle, and tendon impedance from
175 the experimental measures of ankle angle, ankle torque, and displacement of the MTJ (Fig 2). We
176 quantified ankle impedance as the relationship between the imposed ankle rotations and the
177 resultant ankle torque [7]. Measurement of the MTJ motion allowed us to estimate muscle and
178 tendon impedance under the assumption that the muscle and tendon are connected in series [24],
179 and that the displacement of the muscle-tendon unit is determined by the angular rotation of the
180 ankle multiplied by the Achilles tendon moment arm. We refer to the relationship between MTJ
181 displacement and the angular rotations of the ankle as the translation ratio. Specifically, to
182 characterize ankle, muscle, and tendon impedance, we estimated ankle impedance and the
183 translation ratio, and used these quantities to compute muscle and tendon impedance [20]. We
184 previously demonstrated that the magnitude of the frequency response functions was nearly
185 constant from 1 to 3 Hz, indicating that stiffness was the dominant contributor to impedance over
186 this frequency range [20]. As such, we computed the stiffness component of ankle, muscle, and
187 tendon impedance by averaging the magnitude of the respective frequency response functions from
188 1 to 3 Hz. Our primary analysis will focus on the stiffness component of impedance due to its
189 relevance in the control of posture and movement at the ankle [25].

190 A single approximation of the Achilles tendon moment arm (51.4 mm) was used for all
191 analyses. This was estimated as the mean across subjects from Clarke et al. [26] with an ankle
192 angle of 90°. It has been demonstrated that the Achilles tendon moment arm does not scale with
193 anthropometric data [26, 27]. Additionally, system identification is a quasi-linear approximation
194 about a single operating point, which, in our study, was 90°. Therefore, we approximated the
195 moment arm as a single value.

196 Ankle and tendon stiffness varied non-linearly with plantarflexion torque (or musculotendon
197 force). Therefore, the ankle and tendon stiffness experimental data were fit with non-linear models

198 to synthesize our results. The model used to characterize torque-dependent changes in ankle
199 stiffness was:

$$200 \quad K_A = \frac{\beta \cdot Torque \cdot K_{A1}}{\beta \cdot Torque + K_{A1}} + K_{A0} \quad (1)$$

201 in which K_A represents the modeled ankle stiffness, $Torque$ was the input to the model, β , K_{A1} and
202 K_{A0} are the optimized parameters. A similar model has been used to characterize load-dependent
203 changes in the stiffness of a muscle-tendon unit [28].

204 Tendon stiffness was modeled by an exponential function:

$$205 \quad K_T = K_{Tmax} + a \cdot \exp(-b \cdot force) \quad (2)$$

206 in which K_T represents the modeled tendon stiffness, musculotendon $force$ was the input to the
207 model, and K_{Tmax} , a , and b are the optimized parameters. This model was chosen since exponential
208 models have been used previously to characterize the non-linear toe-region of the tendon stress-
209 strain curve [29]. We computed musculotendon force by dividing the measured ankle torque by
210 the Achilles tendon moment arm.

211
212 *Sensitivity analyses*

213 We evaluated the sensitivity of ankle stiffness to changes in muscle and tendon stiffness at
214 different levels of force. We first consider that ankle stiffness (K_A) is determined by the serial
215 connection of the muscle and tendon and can be described as a function of these stiffnesses [20],
216 such that:

$$217 \quad K_A = \frac{K_M \cdot K_T}{K_M + K_T} r^2 \quad (3)$$

218 where r represents the Achilles tendon moment arm in the sagittal plane, K_M represents muscle
219 stiffness, and K_T represents tendon stiffness. This relationship was used to derive the sensitivity of
220 ankle stiffness to muscle and tendon stiffness using Eq 4, where S_x is the relative sensitivity to a
221 given parameter x (either muscle or tendon stiffness).

$$222 \quad S_x = \frac{\partial K_A / \partial K_x}{K_A / K_x} \quad (4)$$

223 The average values of muscle and tendon stiffness estimated from our experiment were used to
224 compute numerical values for the sensitivity of ankle stiffness.

225

226 *Statistical analysis*

227 We sought to determine how the triceps surae and Achilles tendon contribute to the impedance
228 of the ankle over a range of activation levels. Non-linear mixed-effects models were used to
229 characterize the ankle stiffness–torque relationship and the tendon stiffness–force relationship (Eq
230 1 & 2). A linear mixed-effects model was used to describe the muscle stiffness–musculotendon
231 force relationship. For all models, subject was treated as a random factor, and plantarflexion torque
232 or musculotendon force was a continuous factor. A restricted maximum likelihood method was
233 used to estimate all models [30]. The model fit for ankle, muscle, and tendon stiffness was assessed
234 by quantifying the coefficient of determination (R^2) for each participant from the respective mixed-
235 effects model. We tested the null hypothesis that the muscle and tendon contribute equally to ankle
236 stiffness. We used a bootstrapping procedure to determine the range of musculotendon forces when
237 muscle and tendon stiffness were not significantly different from each other to a level of $p > 0.05$.
238 The bootstrapping involved randomly resampling the data from each subject with replacement to
239 create a new dataset for the entire pool of subjects. This process was repeated 200 times. Each
240 synthesized dataset was analyzed as described above to create a distribution of estimates for which
241 muscle and tendon stiffnesses were the same. Our null hypothesis—that muscle and tendon
242 stiffness contribute equally to the stiffness of the ankle—was accepted within the 95% confidence
243 intervals of this distribution and rejected elsewhere. All metrics reported are mean \pm 95%
244 confidence intervals unless otherwise noted.

245

246 **RESULTS**

247 *Muscle stiffness exceeded tendon stiffness at low loads*

248 At all levels of activation, the magnitudes of the frequency response functions for muscle and
249 tendon impedance were nearly constant from 1 – 6.5 Hz (Fig 3), indicating that stiffness is the
250 primary contributor to impedance at these frequencies. Therefore, it is reasonable to assume that
251 muscle and tendon behave as simple springs during the conditions tested and over this frequency
252 range, which is not impacted by changes in load.

253 Muscle and tendon stiffness increased with increases in musculotendon force (Fig 4). Figure
254 4A displays the experimental measures and model fits from an individual subject. The muscle and
255 tendon stiffness models fit the data well for the representative subject (muscle: $R^2 = 0.94$; tendon:
256 $R^2 = 0.91$), and across the entire group (muscle: $R^2 = 0.94 \pm 0.01$; tendon: $R^2 = 0.94 \pm 0.01$).

257 We found that muscle stiffness increased at a greater rate with increases in force than tendon
258 stiffness. A representative participant shown in Fig 4A, illustrates that muscle stiffness was greater
259 than tendon stiffness at 21 N (solid line). This trend was consistent across all subjects. We observed
260 that muscle stiffness exceeded tendon stiffness at 21 ± 7 N (Fig 4B). The musculotendon force
261 where muscle stiffness exceeded tendon stiffness (21 N) occurred at a very low contraction level,
262 corresponding to $1.5 \pm 0.2\%$ of the maximum voluntary torque across all subjects. At the highest
263 force tested in this study, ~ 830 N, the muscle was approximately 6.6 times stiffer than the tendon.

264

265 *Ankle stiffness was most sensitive to changes in tendon stiffness*

266 A unique feature of our measurement technique is that we were able to quantify ankle, muscle,
267 and tendon stiffness simultaneously, enabling us to quantify the relative contributions from the
268 muscle and tendon to the stiffness of the joint. As others have reported [3, 7, 31], we found that
269 ankle stiffness increased with voluntary contraction (Fig. 5). This increase was non-linear and
270 described well by Eq. 1 for individual subjects (Fig. 5A; $R^2 = 0.99$), and the full population of
271 tested subjects (Fig. 5B; $R^2 = 0.98 \pm 0.007$). Our values of ankle stiffness are consistent with
272 previous reports using a similar experimental protocol [32].

273 We completed a sensitivity analysis to quantify how changes in muscle and tendon stiffness
274 influence ankle stiffness across the range of tested forces (Fig 6). As expected, ankle stiffness was
275 most sensitive to the tendon for forces above 21 N, where tendon stiffness became lower than
276 muscle stiffness. For forces above 350 N, corresponding to approximately 20% MVC in our
277 population of subjects, ankle stiffness was nearly 4 times more sensitive to changes in tendon
278 stiffness than to changes in muscle stiffness. The importance of tendon stiffness for determining
279 ankle stiffness increased at further contraction levels. These results provide additional evidence
280 that the mechanical properties of the human ankle are determined primarily by the non-linear
281 mechanical properties of the Achilles tendon.

282

283 **DISCUSSION**

284 Regulating ankle impedance is critical when adapting to varying environmental conditions and
285 responding to postural disturbances. This study sought to determine how the triceps surae and
286 Achilles tendon contribute to the sagittal plane impedance of the ankle over a range of activation
287 levels. We used our novel technique to quantify ankle, muscle, and tendon impedance

288 simultaneously [20]. We found that both muscle and tendon impedance increased with activation,
289 and that both had spring-like properties for frequencies below approximately 6.5 Hz. Muscle
290 stiffness exceeded tendon stiffness beyond the lowest forces and levels of activation (~ 21 N or
291 $\sim 1.5 \pm 0.2\%$ MVC). The stiffness of the human ankle during plantarflexion is determined largely
292 by the net stiffness of the serially connected Achilles tendon and triceps surae muscles. Because
293 springs connected in series have a net stiffness that is limited by the most compliant (least stiff)
294 element, our results indicate that the mechanical properties of the Achilles tendon, a passive
295 structure, have a substantial impact on the activation-dependent increases in ankle stiffness at
296 almost all levels of muscle activation. This finding is in contrast to the common assumption that
297 the regulation of ankle stiffness is directly linked to activation-dependent changes in muscle
298 stiffness [3-5]. Instead, our results suggest that the nervous system leverages the non-linear
299 properties of the Achilles tendon to increase ankle stiffness during postural conditions. This is a
300 fundamental shift in the assumed roles of the muscle and tendon and our current understanding of
301 how muscle and tendon impedance contribute to the impedance of the ankle.

302

303 *Characteristics of triceps surae and Achilles tendon impedance*

304 We found that muscle and tendon have spring-like properties below approximately 6.5 Hz, as
305 indicated by the nearly constant-valued impedance frequency response functions (Fig 3). This
306 result implies that viscous and inertial properties of the muscle and tendon are small relative to
307 stiffness over this frequency range. This result is consistent with testing in excised tendons, where
308 it has been found that the estimated tendon mechanical properties are invariant with respect to the
309 frequency of the applied stretch up to 11 Hz [33, 34]. It is also consistent with previous findings
310 within feline muscle, where the muscle behaves elastically in response to small stochastic
311 perturbations over a similar frequency range to what we tested [35]. Our measured response in
312 muscle suggests that our measurements remained within its short-range stiffness region [10].
313 Muscle short-range stiffness describes the initial response to small, fast displacements prior to
314 reflexive or volitional muscle activation and is critical in the control of posture and limb stability
315 [35, 36]. This finding is consistent with our previous results that demonstrated that our muscle
316 stiffness estimates are similar to measurements of muscle short-range stiffness scaled to the triceps
317 surae [20]. We do note, however, that if the stretch within the muscle or tendon was larger or
318 slower, we would expect to observe more complex viscoelastic behavior. For example, when a

319 larger stretch is applied to a muscle, the response is no longer purely elastic [10]. Similarly, within
320 tendon, when stretch velocity is slower, the mechanical properties of the tendon decrease [37].

321 Our estimated values of muscle stiffness were larger than the few previous reports that
322 attempted to quantify the stiffness of the human triceps surae muscle *in vivo*. This is likely due to
323 the small size of our perturbations compared to earlier studies. All previous estimates of human
324 triceps surae muscle stiffness used perturbations at least twice as large as those we applied (20° or
325 larger) [12, 38]. Previously, Hauraix et al. [12] reported a triceps surae muscle stiffness value of
326 218 N/mm at 40% MVC, while Clark et al. [38] reported a muscle stiffness of 118 N/mm at 25%
327 MVC. For comparison, we estimate muscle stiffness to be 261 N/mm at 25% MVC for an average
328 participant in our study. Muscle stiffness varies based on the size of the applied perturbation [10].
329 Therefore, given the difference in perturbation size, it was expected that the previously reported
330 muscle stiffness values would be lower than our results. Our novel *in vivo* estimates of muscle
331 stiffness may be especially pertinent for stability and the response to unexpected postural
332 disturbances when the short-range stiffness of the muscle is important.

333 The observed increase in tendon stiffness with increases in musculotendon force suggests that
334 the Achilles tendon was within the non-linear toe-region of its stress-strain curve during our
335 experiments (Fig 4). Tendons exhibit a strain-dependent increase in stiffness at low strains (e.g.,
336 the toe-region of the stress-strain curve) [16]. While Achilles tendon stiffness has been
337 characterized before [12-15], previous studies have only estimated its stiffness above 30% MVC
338 to satisfy the methodological assumption that tendon stiffness is constant. Our approach is not
339 constrained by this assumption, allowing measurements to be made at lower forces corresponding
340 to activation levels that occur during everyday activities like standing and walking [19].

341

342 *Limitations*

343 Our technique for estimating muscle and tendon stiffness assumes that all plantarflexion torque
344 is transmitted through the Achilles tendon to the triceps surae, omitting contributions from other
345 structures that span the joint (e.g., the joint capsule and other musculotendon units) [20]. This
346 assumption is valid during plantarflexion contractions, when the musculotendon force from the
347 triceps surae is significantly greater than contributions from other sources. However, other
348 structures can have a substantial effect relative to Achilles tendon force when the ankle is passively
349 dorsiflexed. To mitigate their contributions, we positioned the ankle in a neutral position where

350 passive torque is minimal [39]. We may still be overestimating muscle and tendon stiffness during
351 passive conditions, but this limitation will have a negligible impact on our main conclusions when
352 the triceps surae are active.

353

354 *Functional implications and Conclusions*

355 While the data presented was during isometric conditions, our findings may explain an
356 underlying physiological mechanism of previous estimates of ankle impedance during walking.
357 Rouse et al. [40] observed that ankle stiffness estimated using perturbations of ankle posture during
358 the stance phase of walking was similar to that estimated by the slope of the ankle torque – ankle
359 angle relationship, also known as quasi-stiffness. This was surprising since these two estimation
360 approaches can only yield the same results if the system is purely elastic and passive [41].
361 However, it is well documented that the triceps surae are active during the stance phase of
362 locomotion [8, 40]. One possible explanation for the Rouse et al. [40] findings is that ankle
363 stiffness was determined primarily by the Achilles tendon—a passive elastic structure—during the
364 stance phase of walking, where it has been shown that muscle fascicle length changes are modest
365 [8, 9], as in our postural experiment.

366 We observed that the Achilles tendon is less stiff than the triceps surae at almost all loads, but
367 these results may not apply to other muscle-tendon units. For the Achilles tendon, the compliance
368 of the tendon is essential for the storage and return of elastic energy, increasing the economy of
369 locomotion [8, 9, 42, 43]. However, the mechanical properties of the muscle relative to the tendon
370 will depend upon the functional role of each muscle-tendon unit and its corresponding architecture
371 [44]. For example, muscles that have a similar fascicle length and tendon slack length have been
372 termed “stiff”, while muscles where the fascicles are much shorter than the tendon—like the triceps
373 surae—have been termed “compliant” [16]. It is almost certain that muscles in the former category
374 will contribute more to the stiffness of the joint that they cross.

375 Finally, our results have implications for targeted rehabilitation. Changes in Achilles tendon
376 stiffness that occur as a result of injury [45], or healthy aging [46] will impact ankle stiffness. For
377 example, our results suggest that the previously reported age-related decrease in Achilles tendon
378 stiffness will decrease the stiffness of the ankle for a fixed level of contraction [47]. This decrease
379 could impair the control of posture and movement. To improve balance during tasks that require
380 effective ankle stabilization, altering muscle stiffness through strength training might be less

381 effective than increasing tendon stiffness through high magnitude loading [48, 49]. Ultimately,
382 understanding the relative contributions from the muscle and tendon advances our fundamental
383 understanding of how ankle stiffness is varied for an individual's interactions with their physical
384 world, and aids in developing targeted interventions when musculotendon mechanics are altered
385 as a result of neuromuscular pathologies or aging.

386

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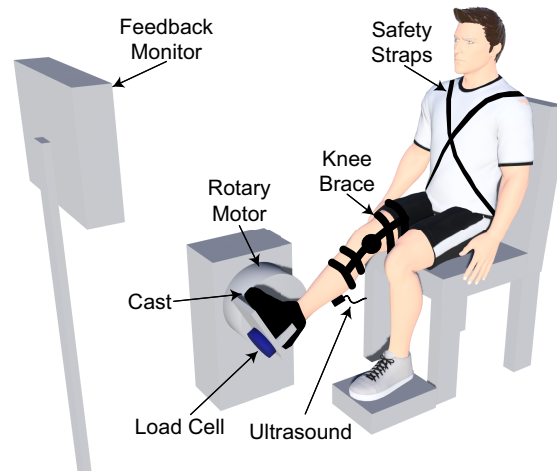
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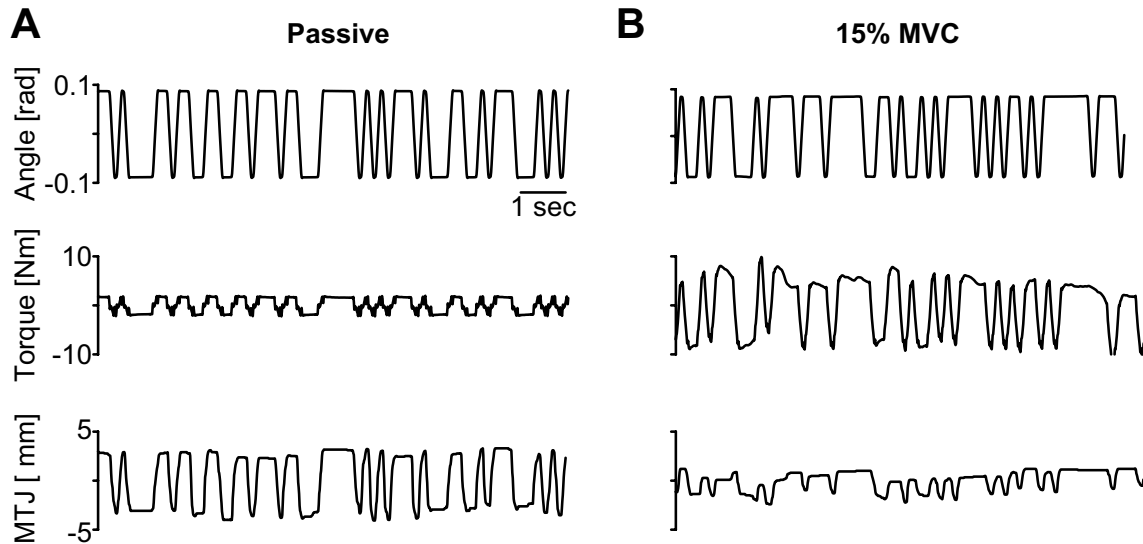
535 **FIGURES**



536

537 **Figure 1. Schematic of the experimental setup.** A custom-made cast secured the subject's foot to the rotary motor.
538 The rotary motor rigidly controlled the ankle joint angle, while the load cell measured the resultant ankle torque. We
539 used B-mode ultrasound to image the muscle-tendon junction of the medial gastrocnemius. The knee brace secured
540 the knee in a stable position, preventing unwanted knee flexion or extension. The feedback monitor provided real-
541 time feedback on the magnitude of the plantarflexion torque and the tibialis anterior muscle activity.
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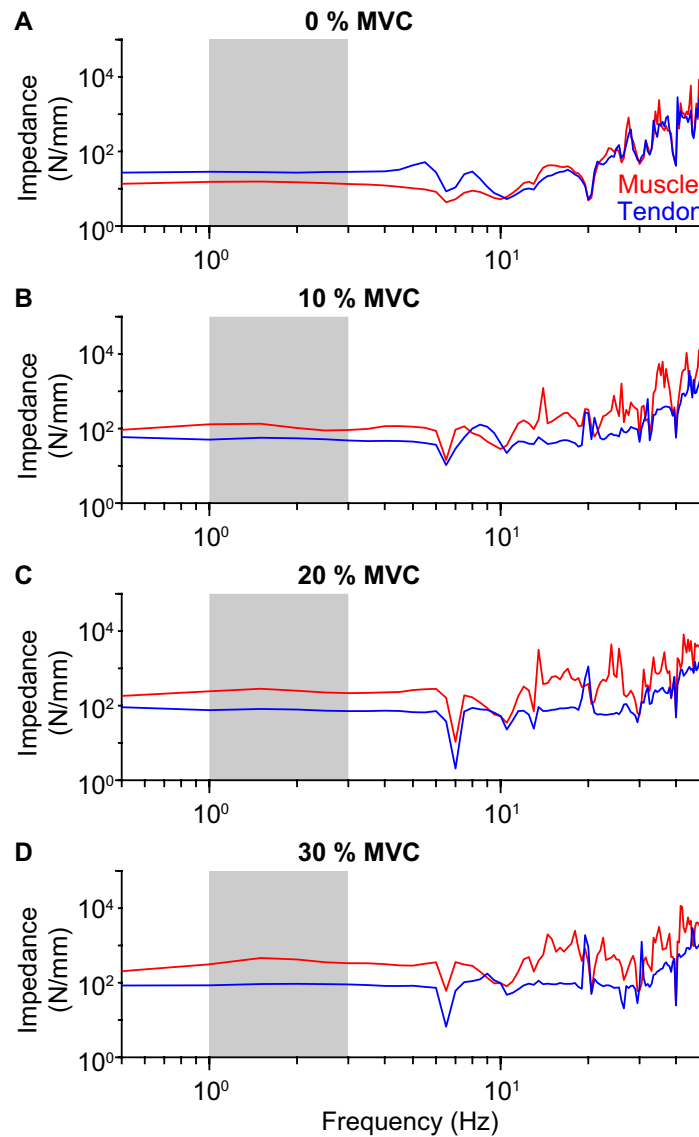
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544 **Figure 2. Representative data used to estimate ankle, muscle, and tendon impedance.** Representative data from
545 a passive trial (A) and a trial when the participant was instructed to maintain 15% of their maximum voluntary torque
546 (MVC) (B). The rotary motor rigidly controlled the position of the participant's ankle (angle) at all times. We measured
547 the resultant ankle torque and muscle-tendon junction (MTJ) displacement from the medial gastrocnemius resulting
548 from the applied random perturbations. Torque and MTJ displacement have been detrended.
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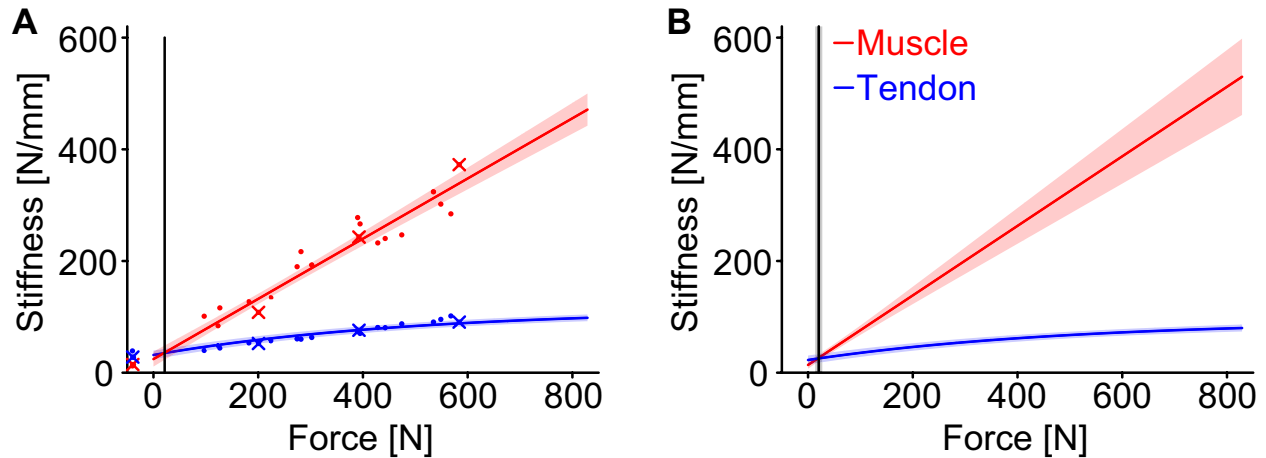
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551 **Figure 3. Stiffness is the dominant contributor to muscle and tendon impedance at low frequencies.** Muscle (red)
552 and tendon (blue) impedance frequency response functions from a representative participant at (A) 0% MVC, (B) 10%
553 MVC, (C) 20% MVC, and (D) 30% MVC. The magnitudes of the frequency response functions were nearly constant
554 from 1 – 6.5 Hz, indicating that stiffness is the primary contributor to impedance. Values between 1 – 3 Hz were used
555 to compute stiffness (shaded region).

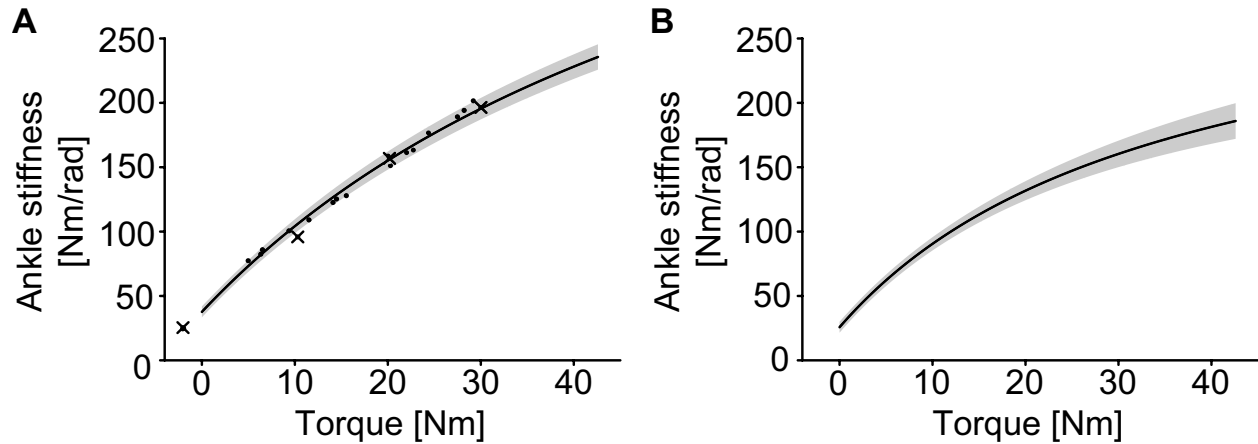
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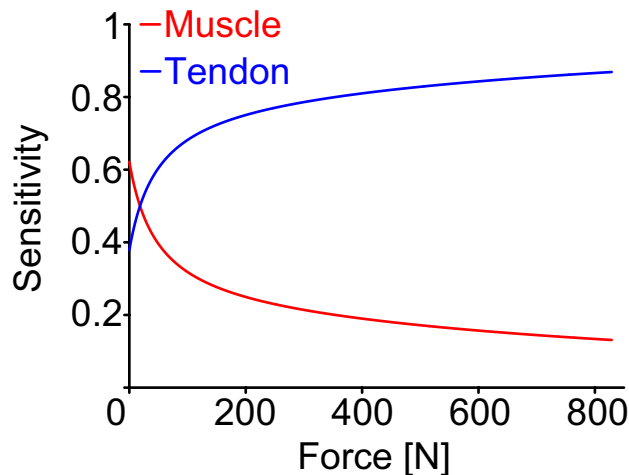
558 **Figure 4. Muscle stiffness exceeded tendon stiffness past the lowest levels of force.** (A) Muscle stiffness (red) and
559 tendon stiffness (blue) for an individual subject, illustrating that muscle stiffness exceeded tendon stiffness at low
560 levels of musculotendon force (21 N – solid black line). Each point represents an individual trial. The x's correspond
561 to the trials illustrated in Fig 3. (B) This trend was preserved across all subjects (n=17). Muscle stiffness exceeded
562 tendon stiffness at 21 ± 7 N (mean \pm 95% CI – solid line and shaded area). The tendon stiffness experimental data
563 were modeled using Eq 2, while the muscle stiffness experimental data were modeled linearly. Mixed-effects models
564 were used for muscle and tendon stiffness to account for random variability between subjects. The solid line indicates
565 the estimated muscle and tendon stiffness from the respective mixed-effects models, with the shaded region being the
566 95% confidence intervals. We evaluated the range of musculotendon forces when muscle and tendon stiffness were
567 not significantly different from each other to a level of $p > 0.05$ using a bootstrapping procedure. The solid black line
568 was the mean musculotendon force where muscle and tendon stiffness were equivalent within the set level of statistical
569 significance, with shading indicating the 95% confidence intervals across the bootstrapped samples.

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571
572 **Figure 5. Ankle stiffness increased with increased plantarflexion torque.** A) Ankle stiffness estimates for an
573 individual subject, illustrating the increase in stiffness with torque. Each point represents an individual trial. The x's
574 correspond to the trials illustrated in Fig 3. This trend was preserved in the group results (n=17) (B). The ankle stiffness
575 experimental data were modeled using Eq 1. A mixed-effects model was used to account for random variability
576 between subjects. For all plots, the solid line indicates the estimated stiffness from the respective fitted model, with
577 the shaded region being the 95% confidence intervals.

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581 **Figure 6. Sensitivity of ankle stiffness to changes in muscle (red) and tendon (blue) stiffness.** Beyond the lowest
582 levels of force, ankle stiffness was more sensitive to changes in tendon stiffness compared to changes in muscle
583 stiffness.