Damage dynamics in single *E. coli* and the role of chance in the timing of cell death

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Genetically identical cells in the same stressful condition die at different times. The origin of this stochasticity is unclear; it may arise from different initial conditions that affect the time of demise, or from a stochastic damage accumulation mechanism that erases the initial conditions and instead amplifies noise to generate different lifespans. To address this requires measuring damage dynamics in individual cells over the lifespan, but this has rarely been achieved. Here, we used a microfluidic device to measure membrane damage in 648 carbon-starved *E. coli* cells at high temporal resolution. We find that initial conditions of damage, size or cell-cycle phase do not explain most of the lifespan variation. Instead, the data points to a stochastic mechanism in which noise is amplified by a rising production of damage that saturates its own removal. Surprisingly, the relative variation in damage drops with age: cells become more similar to each other in terms of relative damage, indicating increasing determinism with age. Thus, chance erases initial conditions and then gives way to increasingly deterministic dynamics that dominate the lifespan distribution.

Introduction

Genetically identical organisms placed in the same conditions die at different times [1–5]. This non-genetic variation is shared also by single celled organisms, such as starving *E. coli* [4] and aging yeast [6].

Two possibilities have been raised to understand this stochasticity of death times [1,2,7,8]. The first is that the initial states of individuals are different and affect the eventual time of demise [2,8]. The second is that initial conditions are rapidly erased by stochastic accumulation of damage over time, and stochasticity further accumulates to cause the different lifespans [7]. The nature of this stochastic accumulation is unclear.

To understand the role of chance and initial conditions in the timing of cell death, it is essential
to measure the damage that causes death over time in individual cells. This, however, has rarely
been done.
Here we use carbon-starved *E. coli* in microfluidic chambers to study the role of stochasticity
and initial conditions in the time of cell death. The cells have a risk of death that rises
exponentially with age [4], known as the Gompertz law, which also characterizes mortality in other
microorganisms and animals [9]. We use the well-established bacterial viability marker propidium
iodide [10] to measure membrane damage in individual cells in the microfluidic device. We find
that initial conditions of damage or cell-cycle phase do not strongly correlate with time of death.
Instead, the data suggests a specific mechanistic model for the stochastic dynamics of the
damage that causes death. In this model, damage-producing units such as unfolded protein
complexes rise at a constant rate and produce damage, whose removal processes saturate at high
damage levels. This saturation amplifies noise and leads to different individual dynamics,
explaining the majority of variation in lifespan. Surprisingly, the relative damage variation
between cells drops with age, indicating that stochasticity erases initial conditions, but then
becomes less dominant and damage dynamics becomes increasingly deterministic with age.
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55 # Results

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57 *E. coli* **damage dynamics in individual cells**

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We tracked individually starved *E. coli* cells by time-lapse microscopy using a microfluidic
system called the mother machine [11] (Fig. 1A, Fig. S1, Movie S1). Individual cells from the same
clone were loaded onto an array of dead-end micro-channels (6μm long and 1.1μm high and
wide) that open onto a main channel [12]. The micro-channels exposed the individual cells to a
homogenous medium refreshed by flow in the main channel in which the cells were starved for
carbon.
The device prevented cells from interacting. This bypasses the effects of feeding on the remains
of perished cells that occur in batch culture starvation and lead to an exponential survival curve
with a constant risk of death[13] rather than the Gompertz law observed in the microfluidic device[4].
To allow different initial cell-cycle phases and cell sizes, we loaded the cells onto the chip from a
culture in exponential growth. Thus, some cells have recently divided whereas others are about
to divide. The chip was then thoroughly washed to eliminate traces of carbon nutrient [4].
To follow the physiological deterioration process of each cell, we focused on membrane integrity
as an indicator of damage. Membrane integrity is critical to a cell's survival [14–16] and is affected
by many physiological parameters, including pH, redox balance, energy metabolism and
translation fidelity [17].
We measured membrane integrity with propidium iodide (PI), a well-established non-toxic dye
for bacterial viability [4]. PI becomes fluorescent only when it penetrates the cell membrane and

binds to DNA. Due to its relatively large size and charge, PI can not cross the membrane when
the membrane is functionally intact. We therefore used the rate of PI uptake to quantify the
integrity of bacterial membranes (Fig. 1B). PI uptake rate was calculated from the image time-
series of each bacterium at resolution of 1 hour (Methods). Experimental noise of the
fluorescence image time-series is estimated at about 6% (Fig. S2). PI-base viability in the assay
compared well with another viability stain which has a distinct, protein based mechanism
(Supplementary Information S3, Fig. S3).
According to the Arrhenius equation, PI uptake rate is inversely proportional to the exponential
of the potential barrier that the PI molecule has to cross to enter the cell. We therefore define
membrane damage X(t) as the log of the PI uptake rate normalized to the mean uptake rate of the
initial population (Methods). Cell death was determined by damage levels exceeding a threshold,
X_c. The value of X_c is determined by the maximal X(t) observed before cells reach previously
established lifespans [4].
Cells survived for an average of 82h (Fig. 1C), and showed an exponentially rising risk of death
(Fig. 1E), namely the Gompertz law [4]. Cells rarely die in the first 40 hours, and then begin to die
more and more frequently, leading to a sigmoidal survival curve well described by a Weibull
function (Methods). The relative variation of death times was 24%, where 5% of the cells died
by 42h, and 95% died by 106h.
From the time-series of PI fluorescence we measured the damage X(t) in 648 individual bacterial
cells at 8 time points, which correspond to 8 non-overlapping windows of 7 hours each between
20h and 80h. We do not consider the initial 20h period since it is a time over which cells adapt to
the starvation conditions in the device, nor the data after 80 hours since most cells are dead.
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Figure 1. Damage dynamics in starving *E. coli* cells. (**A**) Individual *E. coli* cells were placed in
microfluidic channels with medium flow. Propidium iodide (PI) added to the medium crosses the
membrane and stains DNA when membrane integrity is compromised. (**B**) Membrane damage
was measured by the temporal derivative of PI fluorescence, as shown for two individual
bacteria. Top: fluorescence signal, bottom: derivative (uptake rate) in 7h time windows. (**C**)
Colormaps of normalized fluorescence time-series, with individual cells ranked by lifespan. (**D**)
Colormaps of membrane damage computed from the PI rate of change, with individual cells

ranked by lifespan. (**E**) Cumulative risk of death as a function of age shows an exponential
regime. Cumulative risk of death is defined as negative natural logarithm of survivorship and is
equal to the integral of the hazard function. The blue region corresponds to 95% confidence
intervals. Death conditions are as previously defined [4]. (**F**) Cellular damage fluctuates around a
rising trajectory, subsampled to 7h time windows. Trajectories are color coded by the time
window of cell death, circles indicate the last time window before death. Data shown here are the
same as those in (**D**). (**G**) PI uptake rate distributions and best-fit to a type-2 generalized beta
distribution with the ratio between shape parameters $p/(p+q)$, plotted versus age in (**H**), see
Methods.
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119 **Initial damage and cell-cycle phase do not correlate with lifespan in most cells**
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We asked whether initial conditions, namely the cell state when loaded onto the chip, might
explain the variations in lifespan (Fig 2A). There was a negative correlation between initial
damage and lifespan (Spearman r=-0.41, p<0.001). This correlation was primarily due to a subset
of 3% of the cells that had high initial damage (PI uptake rate>4/h, compared to the mean uptake
rate of 0.87/h in the remaining cells). These initially damaged cells had a short lifespan,
averaging 48h.
We therefore divided the cells into two populations, with initial uptake rate above and below 4
(Fig. 2 B-C), which we call the high damage and low damage groups. The high damage group
showed a strong correlation between initial damage and lifespan (Spearman r=-0.70, n=17,
p=0.002). The low damage group, which comprised 97% of the cells, showed low correlation
(Spearman r=-0.15, n=503, p=0.001).
We also investigated the effect of cell-cycle phases by noting the initial size of the cell and
number and timing of reductive divisions on the chip[18]. We find that cell size has only weak
correlations with lifespan (Spearman r=-0.09) (Fig. 2D), as did the time of last division
(Spearman r=-0.11) (Fig. 2E) and number of divisions (Spearman r=-0.06).
Multiple regression shows that initial conditions explain a total of 27% of the variation for all
cells, and 10% of the variation for the majority -- 97% of the cells -- with low initial damage
(Fig. 2F). We conclude that in the traits measurable in this experiment, the initial conditions
explain only a minority of the variation in lifespan.
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Figure 2. Initial conditions do not account for most of the variations in lifespan. (**A**) Initial
damage levels (PI uptake rate) and lifespan of all cells in the experiment; (**B**) For cells with high
initial damage (PI uptake rate>4, n=18), initial damage correlates with lifespan; (**C**) For cells
with low initial damage (<4, n=589), the correlation between initial damage and lifespan is
weak; (**D**) Initial cell size and lifespan of all cells in the experiment; (**E**) Time of last division
and lifespan for all cells in the experiment; (**F**) Fraction of lifespan variation explained by initial

conditions according to multiple regression. Left are all cells, right are cells with low (<4) initial

damage.

Damage dynamics rise and fall suggesting a stochastic mechanism

We next sought to characterize the stochastic dynamics of damage, defined as PI uptake rate,

over time. Damage in each cell did not accumulate monotonically. Instead, damage rose and fell

in each cell, with fluctuations larger than can be explained by experimental noise (Fig. 1F). This

indicates that damage is produced and removed on the timescale of hours. These fluctuations

occurred around a mean trajectory that accelerated with age on the scale of tens of hours. This

suggests two timescales: in addition to the fast timescales of hours, a slower timescale of tens of

hours over which damage production and removal rates change.

Notably, we find that cells become more similar in relative terms as they age. Although the mean

damage and its standard deviation both rise with age (Fig. 3 A,B,F), the standard deviation rises

more slowly than the mean. As a result, the relative variation drops with age, as measured by the

coefficient of variation CV=SD/mean (Fig. 3C). 1/CV rose approximately linearly with age

above 50h.

The increasing relative similarity between cells with age is seen also in the damage distributions

at each timepoint. At early ages the distribution is skewed to the right, but skewness reduces with

age (Fig. 3D), as the distribution becomes more symmetric,

The longitudinal nature of the data allowed us to calculate the autocorrelation of damage.

Correlation time increased with age. This means that a cell with damage above or below the

population average remained so for a longer at old ages (Fig. 3E). Plotting damage as a function

of remaining lifetime shows that X=log(normalized PI uptake) becomes less dispersed the closer

the cell is to death (Fig. 3G).

These findings indicate that the damage dynamics has aspects that become more deterministic

with age.

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Figure 3. Damage dynamics show increasing determinism with age. Statistics of *E. coli*
membrane damage for all cells alive at a given age: Mean (**A**) and standard deviation (**B**)
increase with age; but coefficient of variation (**C**) decreases, indicating reduced relative
heterogeneity in the damage distribution. (**D**) Skewness drops with age. (**E**) Autocorrelation of
damage increases with age, showing increasing persistence. (**F**) Probability distribution of
damage in younger (52.5h blue dashed line) versus older (72.5h yellow solid line) cells. (**G**) Log
PI uptake rate as a function of remaining lifespan becomes less variable close to death.

Damage dynamics indicate a saturated-repair stochastic model

To elucidate the stochastic mechanism that can give rise to these damage statistics, we modeled
damage production and removal with noise. We exploited the separation of timescales in the
data, namely the rapid fluctuations of damage around a slowly rising mean trajectory. Therefore,
we explored models in which damage is produced and repaired quickly compared to the lifespan,
whereas the rates of damage production and removal change slowly with age t (See Table S3 for
relevant timescales). Damage removal and production were also allowed to depend on the
amount of damage to include the possibility of feedback and saturation effects.
We use as a damage variable X=log(normalized PI uptake) to represent the loss of the free-
energy barrier posed by the membrane in units of $k_B T$. We consider a general stochastic model
dX/dt = production - removal + noise, or mathematically $dX/dt = G(X,t) + \sqrt{2\sigma}\xi$, where ξ is
white noise of amplitude σ.
To define the production and removal terms that make up G(X,t), we used timescale separation,
by assuming that at each time point the damage distribution among cells P(X,t) is a steady-state
solution of the equation. The analytical solution for the steady-state is $P(X, t) = e^{-U(X,t)/\sigma}$,
where U(X,t) is a potential function defined by $\partial U/\partial X = -G(X,t)$. This is analogous to the
Boltzmann distribution in statistical mechanics.
Using the measured distribution of damage at different timepoints, P(X,t), we estimated U,
integrated it to provide G(X,t) and hence the production-removal terms in the model.

To facilitate this process, we characterized the experimental damage distributions P(X,t) by
comparing them to 15 commonly-used distribution functions with 3-4 parameters (Fig. S4, Table
S1). The best fit for the PI uptake distribution was a type-2 generalized beta distribution[19] with
shape parameters whose ratio, p/(p+q), rises approximately linearly with age (Fig. 1H). The
stochastic process which gives rise to this distribution is (see Methods):

$$(1)\ dX/dt = \eta t - \beta f(X) + \sqrt{2\sigma}\xi$$

In this inferred mechanism (Fig. 4A) damage production rises linearly with age as ηt, and
damage removal is a saturating function of damage, $\beta f(X) = \beta e^{aX}/(e^{aX} + e^{a\kappa})$, (Fig. 4B-C).
The parameters are a production slope $\eta = (6.1 \pm 0.8) \times 10^{-3}\ k_B T h^{-2}$ and removal parameters
$a = 0.27 \pm 0.06\ (k_B T)^{-1}$, $\beta = 2.0 \pm 0.3\ k_B T h^{-1}$ and $\kappa = 2.1 \pm 0.5\ k_B T$ The white noise
amplitude is $\sigma = 0.106 \pm 0.008 (k_B T)^2\ h^{-1}$.

Notably, this model is in the same class as the saturated repair (SR) model established for aging
in mice [20], in the sense that the production rate of damage rises linearly with age and damage
inhibits or saturates its own removal. The only difference is that the mouse SR model used a
different saturating removal function, $f(X) = X/(\kappa + X)$. Hence we call the model of Eq. 1 the
membrane-potential-SR model or MP-SR model. We note that the MP-SR removal function
$f(X) = e^{aX}/(e^{aX} + e^{a\kappa})$ can be interpreted as a two-state partition function that senses the loss
of membrane potential X.

The MP-SR model captures the statistics of the observed PI uptake dynamics (Fig. 4D-G). It
shows a reduction in the relative variation, CV=SD/mean (Fig. 4F), despite a super-linear rise in
both mean and SD (Fig. 4D-E). The inverse CV, 1/CV, rises linearly with age as in the data.
The model also captures the reducing skewness with age (Fig. 4G). Hence, the MP-SR model
captures the dynamics of damage in the experiment.
To compute the distribution of lifespans in the MP-SR model, we modeled death as damage X
exceeding a threshold X_c [20]. Death is therefore modeled as a first passage time process, which we
computed numerically and analytically (Supplementary Information S6) using Kramer's
approximation [21,22]. The model provides an exponential increase in the risk of death that slows at
very old ages, namely the Gompertz law (Fig. 4H), and a Weibull-like sigmoidal survival curve
(Fig. 4I), as experimentally observed. This Gompertzian exponential increase is due in the model
to the linear rise in damage production, which causes the potential U to drop linearly with time;
since crossing this barrier goes exponentially in U, the risk of death rises exponentially with
time.
The differences in lifespan between individuals in the inferred stochastic mechanism is due to the
fact that noise is effectively amplified by the saturation of damage removal. The slope of
production minus removal becomes flat at old ages; fluctuations are not pulled back strongly

towards equilibrium by the effective potential U (Fig. 4C). This is at the heart of how noise can
generate different lifespans for cells with identical physiological parameters.
We conclude that PI-uptake trajectories and their reducing relative variation are well-explained
by an SR-type model in which damage production (loss of membrane barrier function) rate rises
linearly with age whereas damage removal saturates.
The SR and MP-SR models make a further prediction that may be called 'shortening twilight'
[23,24]. Twilight is the remaining lifespan after a given damage threshold is crossed, and the model
predicts that twilight shortens with age. This shortening twilight prediction is borne out by the *E.*
coli damage data (SI Fig. S5).
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Figure 4. The staurating-removal model captures damage dynamics. (**A**) Schematic of the
MP-SR model. (B) rate plot showing linearly increasing production with age and a removal rate
that saturates with damage, causing the fixed point to accelerate to high damage levels. (**C**) The
potential function of the MP-SR model and its evolution with age. Simulations of the MP-SR
model for PI uptake rate (e^x) show rising mean (**D**) and standard deviation (**E**), reducing CV (**F**)
and reducing skewness (**G**). The model provides a death hazard that rises exponentially with age

(**H**) and a Weibull-like survival function (**I**). Blue regions are 95% confidence intervals from
simulation of N=645 cells.
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271   **Dynamics in a strain deleted for stress-response regulation agrees with model**
272   **predictions**
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We repeated the experiment with an *E coli* strain deleted for a master regulator of the stress
response, RpoS [25]. Since this strain has reduced stress-response, the model makes specific
predictions. Reduced stress response should increase the rate of damage production η and/or
decrease the rate of damage removal β. These changes in parameters are predicted to result in a
shorter lifespan, higher Gompertz slope and, to the extent that β is decreased, a shallower
survival curve (changes in η do not affect survival curve steepness [20]). The model further
predicts that damage mean and SD should be higher than the wildtype strain whereas damage
CV and skewness should be lower than the wildtype strain.
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We tested these predictions using damage measurements from n=138 *ΔrpoS* cells in the
microfluidic assay (Fig. 5AB). The data agrees with the model predictions. Lifetime was reduced
by 54% (CI: 51%-58%) (Fig. 5A), and the Gompertz slope was higher by 67% (CI: 38%-102%)
(Fig. 5C). The survival curve was only mildly shallower (Fig. 5D), indicating that the parameter
β was not strongly affected by the RpoS deletion. Damage mean and SD were higher (Fig 5EF),
and CV and skewness were lower than the wildtype strain (Fig. 5GH) as predicted. The findings
indicate that the main effect of the RpoS deletion is an increase in the damage accumulation rate
parameter η. The model dynamics with increased η and capture the observed dynamics as shown
in Fig 5 I-L. We conclude that the model can explain damage dynamics in a strain with reduced
stress response.
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Figure 5. Damage dynamics in a strain that has reduced stress response (*ΔrpoS*) agree with
model predictions. (**A**) Colormaps of normalized fluorescence time-series of *ΔrpoS* cells, with
individuals ranked by lifespan. (**B**) Colormaps of estimated PI uptake rates of *ΔrpoS* cells ranked
by lifespan. C) Cumulative hazard shows increased Gompertz slope, D) Survivorship shows
reduced lifespan (inset), and survivorship versus normalized age shows a mildly shallower
survival curve. Measured damage statistics include E) CV F) mean, G) SD and H) skewness.
Model simulations with increased η show similar dynamics for the I) CV, J) mean, K) SD and L)
Skewness.
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Discussion

We studied the role of chance and initial conditions on lifespan by measuring membrane damage over time in starved *E. coli* cells in a microfluidic device. Initial conditions in each cell, such as initial damage, cell size or cell-cycle phase, did not strongly correlate with time of death in most cells. Instead, damage fluctuated in each cell around a rising mean trajectory. Unexpectedly, the relative variation in damage dropped with age. This indicates an increasing determinism with age, where damage levels become more similar in relative terms the older the cells are. Correlation times increased and distributions became less skewed, further indicating rising determinism. The model correctly predicted dynamics in an *E coli* strain deleted for the stress response regulator RpoS.

We used our dynamical damage measurements to infer a stochastic mechanism that provides the dynamics and survival curves. In this mechanism, damage is produced at a rate that rises linearly with age, and damage-removal saturates at high damage levels. We called the mechanism the membrane-potential saturating repair (MP-SR) model. The MP-SR model predicts well the effects on damage dynamics of deleting the stress regulator RpoS. Our findings suggest that chance fluctuations, amplified by saturating removal of damage, play a major role in explaining why genetically identical bacterial cells in the same conditions die at different times.

The damage dynamics measured here have statistical features that differ from random walks and from most previously suggested models of aging [26–28]. The mean rises faster than the standard deviation, so that the relative heterogeneity between cells at a given age declines. This can be quantitated as a drop in the coefficient of variation, CV=SD/mean, such that 1/CV rises roughly linearly with age. This is an unusual feature in stochastic processes in general, and in previous theoretical models of aging including network models [26,27], the Strehler-Mildvan model [28], the cascading failure model [7], fixed frailty model [8] and Ornstein-Uhlenbeck type models which do not provide a drop in damage CV with age but instead have a constant CV.

The present MP-SR mechanism has two main features that require biological explanations. The first feature is the linear rise with age of the damage production rate, ηt. This linear rise can be explained by assuming that damage arises from 'damage-producing units', such as unfolded-protein complexes, that are added at a constant rate and cannot be resolved or removed [29–35]. If these complexes assimilate new unfolded proteins at a constant rate, and cannot be removed, their total mass should rise linearly with time. Such unfolded protein complexes are known to be toxic to cells [32]; they cause damage such as dysregulated proteostasis [36], which can lead to membrane damage [37,38].

Mathematically, if cells accumulate damage-producing units P at a constant rate v, and these units cannot be removed, their number rises linearly with age, $P = v\,t$. Each unit produces damage at rate b, so that total damage production rate rises linearly with time as ηt with $\eta = v\,b$

Organisms that manage to dilute such damage-producing units P, such as organisms with
indefinite growth, are predicted to have different damage dynamics, in which P does not rise
indefinitely. Such dilution occurs in growing and dividing bacterial cells [32,33], but not in the non-
growing starved cells studied here. Other examples of damage dilution may occur in eukaryotic
cells with symmetric division such as fission yeast; in contrast, budding yeast with asymmetric
divisions show aging and eventual death of the mother cell which retains damage rather than
passing it to daughter cells.
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353   The second feature of the MP-SR model is the saturation of damage removal, which is crucial for
354   the present dynamical hallmarks. The relevant removal mechanisms in *E coli* include chaperones
355   and proteases [36], as well as enzymatic systems that repair proton leakage [39], oxidative damage [40]
356   and maintain membrane structural integrity [41]. Such enzymatic repair mechanisms should
357   naturally saturate at high damage levels.
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The inferred stochastic mechanism in *E. coli* is similar to a mechanism inferred in the context of
mice aging by Karin *et al*. Karin *et al* used stochastic trajectories of senescent cells in mice, cells
which are growth arrested cells that cause inflammation, to infer a mechanism for senescent-cell
accumulation [20]. This mechanism, called the saturating removal (SR) model, is a stochastic
differential equation with a production rate that rises linearly with age and a removal rate that
saturates, so that high senescent cell levels slow their own removal. The removal terms in the SR
and MP-SR models both saturate; the difference between them may stem from the type of
damage: X is senescent cell abundance in the SR model, an extensive variable, whereas X is
membrane integrity in the MP-SR model in units of potential, which is intensive and can enter
the dynamics in terms of Boltzmann-like factors.
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Karin *et al* experimentally confirmed a prediction of the SR model, that senescent cell turnover
slows with age [20]. The SR model was generalized to other forms of damage, and explains
observations on aging such as the Gompertz law, heterochronic parabiosis [42], age-related disease
incidence in humans [43] and the scaling of survival curves in *C. elegans* [5,20]. Interestingly, the
human frailty index shows similar dynamical features, including a reduction in CV with age [44].
Both the SR and MP-SR model provide shortening twilight [24], in which remaining lifespan after
a threshold damage is crossed is reduced with the age that the threshold was crossed.
The similarity between the present study on *E. coli* cells and the model of Karin *et al* on
mammalian aging hints at a possible universality in mechanisms of aging, in which chance plays
a large role in the differing lifespans of genetically identical organisms. Although the molecular
forms of damage and lifespan timescales are different between *E. coli* and mice, the features of
linearly rising production and saturating removal may be more general and give rise to similar
damage dynamics, with reducing relative heterogeneity with age.
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It would be interesting to measure longitudinal damage trajectories in other organisms to explore whether linear-production-and-saturating-removal models might apply more generally. In the context of bacteria, it would be important to explore the dynamics of damage in cells challenged with antibiotics, in order to better understand the role of chance in the function of these drugs.

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Methods

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508 **Experimental and analytical methods**

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Microfluidic chip fabrication. The negative master mould for the modified mother machines
was fabricated on top of silicon wafers in two steps. First, arrays of dead-end channels (2000x 6
μm long) were fabricated via electron-beam lithography (EBL) in a specialized micro-fabrication
facility. It was necessary to use EBL for these channels due to the high precision requirements
for the cross-section dimensions (both height and width have to be between 1.1 and 1.2 μm).
They had to be large enough to allow single cells to enter yet narrow enough so that multiple
cells could not be squeezed in the same channel. In the second step, using standard
photolithography methods, the negative mould for the main channel was overlaid perpendicular
to the dead-end channels. The main channel is 10mm long, 50μm wide and 10μm deep.
For each run of the bacterial starvation experiment, microfluidic chips were fabricated by casting
PDMS structures out of negative master moulds. Uncured PDMS mixes (RTV-615, Momentive
Performance Materials) were poured to a thickness of 3mm onto the silicon wafer carrying the
master moulds, and then de-gassed under vacuuming and spread out via gravity for about 2
hours. The PDMS was then partially heat cured at 80°C for about an hour to form solid yet
flexible PDMS blocks with patterned surfaces. After drilling inlets and outlets through the flow
channel, the PDMS blocks were bound to cover glasses suitable for microscopy, using oxygen
plasma (90 s, 1000 mTorr). Lastly, the assemblies were cured fully at 80°C overnight and so that
the PDMS structure was sealed permanently to the glass cover slide.
On the day of the experiment, the microfluidic chip was again treated by oxygen plasma for 90s
so that its surfaces were activated, and then injected with 20% (v/v) polyethylene glycol 400
solution for at least 1h to prevent bacterial adhesion.

531
Material and equipment. During the process of media preparation, sterilization, cell culture and
fluidic infusion, we generally avoided disposable lab plasticware in favor of glass or equipment
whose wetted surfaces are coated with fluoropolymer such as polytetrafluoroethylene (PTFE).
This step avoided a pitfall in which trace concentrations of carbon and energy-rich chemicals
leached into the media, such as phthalate plasticisers commonly used in PVC tubings. Such
compounds can serve as carbon sources and allow the cells to grow, circumventing the goal of
our experiments [4]. Medium was filter-sterilized (0.2 μm) to avoid contamination by volatiles
during autoclaving, and glassware was sterilized by dry heat. In the mother machine chips we
subjected a relatively small number of cells (<10,000) to constantly refreshing volumes (5 μl per
hour) of media.

Bacterial growth and loading. Bacterial cultures were loaded into the microfluidic chip via
centrifugation. All culture media were filter-sterilized before use to remove dust particles, which
might otherwise block the microfluidic channels. *E. coli* wildtype strain MG1655 with a
chromosomal-inserted constitutively CFP-expressing cassette (PrrnB2) was grown overnight in
M9 minimal media (supplemented by 2mM MgSO4, and 0.1 mM CaCl2) at 37°C with 40mM
succinate as carbon source, and diluted 250-fold into 50ml of the same media in 250-ml
Erlenmeyer flasks. This subculture was grown to exponential phase (OD600 ~ 0.1) at 37°C and
then transferred to glass centrifugation tubes and harvested by centrifugation at 4000rpm for
15min. The bacterial pellet was resuspended, washed with fresh carbon-free M9 media and
centrifuged 3 more times. The resulting pellet was resuspended a final time with 20µl M9 media.
This final suspension was manually injected into the main channel of the microfluidic chip, and
forced into the dead-end channels by centrifugation at 1000rpm for 15min. After centrifugation,
the main channel is washed thoroughly by carbon-free M9 media to remove all cells that remain
there.
557
Microfluidic and microscopy setup. After the microfluidic chip was loaded with cells, it was
connected to a linear, flow-controlled fluidic system driven by a high-precision syringe pump
(Harvard Apparatus PHD 2000 Programmable) and GC-grade glass/PTFE syringes (Hamilton
Gaslight 1000 series). As mentioned previously, PTFE tubing and glass syringes are used to
avoid leaching of plasticizers into the media. This is critical for this type of microfluidic
starvation experiments, as *E. coli* are able to uptake as carbon sources the trace concentrations of
plasticizers in the media when it is constantly refreshed by the microfluidic flow. The syringes
are preloaded with filter-sterilized M9 minimal media without carbon source, supplemented with
propidium iodide (PI, 5 µg/ml). The chip was first washed at 100µl per hour for 30 min and then
the flow rate was halved every 15 min to a final flow rate of 5µl per hour. In the meantime, the
chip was mounted and stabilized onto the objective stage of an inverted microscope (Nikon
ECLIPSE Ti2, 100× oil-immersion objective, controlled with MetaMorph software) with
temperature controlled at 37°C. Phase-contrast and fluorescence (PI signal excitation, 546/12
nm; emission, 605/75 nm; CFP excitation 436/20nm; emission 480/40nm) images were
automatically taken for up to 90 imaging positions every hour for up to 120 hours. Focus was
maintained by the hardware-based Perfect Focus System (PFS) from Nikon.
574
Image analysis. We used a published image analysis method specifically designed for mother
machines [12]. The regions in the time-lapse images of each dead-end channel were detected and
cut out of the image stacks and displayed chronologically from left to right on the same image
(Fig. S1B). Cells were segmented using the CFP (constitutively expressed) fluorescent image.
The segmentation approach was semi-automatic and consisted of automatic segmentation,
lineage assignment and manual correction. First, the central region of the cells was detected
using statistical p-value thresholding, assuming that the observed intensities are spatially
distributed as Gaussian functions. Then these central regions were used as seeds to add

recursively neighboring points with similar intensities to form labeled regions. The result of this
automatic process is an accurately segmented image with occasional over segmentation errors.
Then labeled regions from different time points in the same dead-end channels were assigned
together with arrows to track the same cell through time. These automatically segmented and
tracked cells are then manually corrected to account for over-segmentation errors and mis-
assignment due to sudden movements of the cells. For more details see [12]. For each segmented
and tracked cell through time, we used the segmented CFP contours to extract the average PI
fluorescence signal.
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592 **Modeling and statistical methods**
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Measurements of membrane damage. Our general approach is to use the time derivative of
fluorescence to calculate the rate constant of PI uptake, which in turn is a proxy for membrane
damage.
We model the PI fluorescence time series with one slow and one fast chemical reaction. The
slow reaction is PI uptake $PI_{ext} \rightarrow PI_{in}$ with rate constant r, and the fast reaction is PI binding to
DNA once inside the cell $[PI]_{in} + [DNA] \Leftrightarrow [PI:DNA]$, assumed reversible and at equilibrium
with equilibrium constant K, so that $K[DNA][PI]_{in} = [PI:DNA]$.
First, we focus on the rate of PI uptake. The Arrhenius equation states that the logarithm of the
rate constant scales linearly with activation energy, in this case, an energetic barrier representing
the integrity of the cell membrane. Thus, we defined membrane damage X(t) as the reduction of
this energy barrier compared to a healthy baseline. X(t) has the unit of $k_B T$, where T is the
experimental temperature 310K and k_B is the Boltzmann constant. We can choose the unit
appropriately, i.e. to be $k_B T$, X(t) can be made unitless. Under these definitions, the rate constant
is $r = A_0 e^{X(t)}$, where T is the experimental temperature 310K and k_B is the Boltzmann constant.
Then the PI uptake rate is $A_0 e^{X(t)}([PI]_{ext} - [PI]_{in})$.
Having defined the relation between membrane damage and PI uptake rate, our task is the
estimation of the latter using fluorescence time-series. Since PI only becomes fluorescent when
bound to DNA, average fluorescence intensity is proportional to the bound form of PI: $[Fluo] =$
$J_F[PI:DNA]$. Since the binding of PI to DNA is assumed to be at equilibrium, we have
$[PI:DNA] = ([PI]_{in} + [PI:DNA])\frac{K[DNA]}{1+K[DNA]}$. Thus, the time derivative of fluorescence should
be proportional to the PI uptake rate:
$$\frac{d[Fluo]}{dt} = A_0 e^{X(t)}([PI]_{ext} - [PI]_{in})\frac{J_F K[DNA]}{1+K[DNA]}.$$
To obtain relative fluorescence time-series we normalize for each cell its fluorescence signal
$[Fluo]$ by its observed maximum $[Fluo]_{max} = J_F K[DNA][PI]_{ext}$. The relative time series is
thus $s(t) = [Fluo]/[Fluo]_{max} = [PI]_{in}/[PI]_{ext}$. Membrane damage can be calculated from the
experimentally observed relative fluorescence $s(t)$:
$$\frac{ds(t)}{dt} = \frac{d[Fluo]}{dt}/[Fluo]_{max} = \frac{A_0 e^{X(t)}}{1 + K[DNA]}[1 - s(t)]$$

and thus we obtain the formula used in our analysis

$$A_1 e^{X(t)} = \frac{ds(t)/dt}{1-s(t)},$$

where $A_1 = A_0/(1 + K[DNA])$.

A_1 is an Arrhenius-type pre-exponential factor with a unit of inverse time. It is assumed to be
constant, because DNA concentration should be constant among the non-growing cells in our
experiment. The value of A_1 is not relevant to the dynamics of damage, thus we used $A_1=1/600$
so that initial timepoints start close to PI uptake rates of 1.

Time-series analysis and numerical differentiation. The fluorescence series was zeroed by the
background and then divided by the maximum fluorescence for each cell to arrive at $s(t)$ defined
above. To arrive at estimates for PI uptake rate, $\frac{ds(t)/dt}{1-s(t)}$, we performed numerical differentiation
of $s(t)$ in a fashion that reduces the impact of experimental noise. In the present time-lapse
microscopy experiments where single cells inside microfluidic chambers are imaged,
experimental noise is driven by fluctuations in focus on the z-axis. This type of noise is
approximately multiplicative and non-correlated in neighboring 1h time points (see Fig. S2). We
therefore smoothed the log-transformed data $ln[s(t)]$ in time windows of 7h with a Wiener filter.
Then $dln[s(t)]/dt$ were estimated using linear regression in non-overlapping 7h windows. The
resulting time derivatives are multiplied by the $s(t)/[1-s(t)]$ to arrive at $A_1 e^{X(t)}$.
The typical values of X(t) during the lifetime of the bacteria begin around 0.01Xc and rise to
cross Xc at 80-100h.

Marginal damage distributions. We searched for an analytical form for the probability
distribution function that can fit the damage distributions at various ages with age-dependent
parameters. We tested 15 commonly used probability distributions. Each distribution has a
probability density function f(Z/σ; Θ), where Z is the value of the random variable, Θ is the
vector for the shape parameters and σ is the scaling parameter. We fit this to the empirical
damage distribution Z_{it} of cell i at age t, by maximizing the likelihood $\Sigma_i f(Z_{it}/\sigma_t; \Theta_t)$ as a
function of parameters σ_t, Θ_t, using the scipy.stats package of python. The goodness of fit was
evaluated by the one-sample Kolmogorov-Smirnov (K-S) test. The tested distributions, the K-S
test statistics and associated p-value are shown in Table S1 and Fig. S4.
The three distribution functions that best fit the marginal damage distributions, Burr, Burr12 and
Fisk, are all special cases of the generalized beta distribution of the second kind (GB2) [19], whose
probability density function is:

$$f_{GB2}(Z) = a\, b^{aq}\, Z^{ap-1}(b^a + Z^a)^{-p-q} \; /Beta(p,q),$$

where p and q are dimensionless shape parameters, and a and b describe the cooperativity and
scale of the observed damage proxy Z, the PI uptake rate. GB2 becomes a Burr (Burr Type III)

distribution when q=1 and a Burr12 distribution when p=1, and the Fisk distribution when
p=q=1. Since the damage we seek is X=ln(Z), we transform to obtain:

$$(2)\ P(X) = f_{GB2}(Z)\ dZ/dX \sim\ e^{apX}(b^a + e^{aX})^{-p-q}\quad.$$

Derivation of the MP-SR model. We model the dynamics with a stochastic differential equation
(SDE) in the form of

$$(3)\ dX/dt = G(X,t) + \sqrt{2\sigma}\xi = production - removal + \sqrt{2\sigma}\xi,$$

where both production and removal rates of damage can depend on damage level X and age t.
We assume that the production and removal of damage happen much faster than the age-related
change in parameters. Thus we can make the approximation that the observed damage
distributions in the previous section are quasi-steady-state distributions of the SDE. The quasi-
steady-state distribution can be written as the Boltzmann distribution $P(X) \sim e^{-U(X,t)/\sigma}$, where
the potential function U is defined by $G(X,t) = -\partial U/\partial X$.
Using the best-fit GB2 distribution P(X) of Eq (2), we find the potential up to an irrelevant
constant:
$$U(X,t) = \sigma(p+q)ln(b^a + e^{aX}) - \sigma apX\quad.$$
The two terms of this potential function naturally relate to damage production and removal
terms. Thus, via differentiation of U with respect to X we find:
$$production = \sigma ap, removal = \sigma a(p+q)\ e^{ax}/(e^{ax} + e^{a\kappa}).$$
By redefining the GB2 parameters $b = e^{\kappa}, p = \eta_t/a\sigma, q = (\beta_t - \eta_t)/a\sigma$, the MP-SR model for
damage dynamics in *E. coli* is given by:
$$dX/dt = \eta_t - \beta_t\ e^{aX}/(e^{aX} + e^{a\kappa}) + \sqrt{2\sigma}\xi.$$
The GB2 parameters that best fit the experimental data show that p/(p+q) rises approximately
linearly with time (Fig. 1H) and that *b* and *a* remain approximately constant. We conclude that
the observed damage distributions are well-described by an SR-type process with $\eta_t = \eta t$ and
$\beta_t=\beta$, as in Eq 1.