**Effects of sensorineural hearing loss on formant-frequency discrimination: Measurements**

**and models**

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**ABSTRACT**

This study concerns the effect of hearing loss on discrimination of formant frequencies in vowels. In the

response of the healthy ear to a harmonic sound, auditory-nerve (AN) rate functions fluctuate at the

fundamental frequency, F0. Responses of inner-hair-cells (IHCs) tuned near spectral peaks are captured

(or dominated) by a single harmonic, resulting in lower fluctuation depths than responses of IHCs tuned

between spectral peaks. Therefore, the depth of neural fluctuations (NFs) varies along the tonotopic axis

and encodes spectral peaks, including formant frequencies of vowels. This NF code is robust across a

wide range of sound levels and in background noise. The NF profile is converted into a rate-place

representation in the auditory midbrain, wherein neurons are sensitive to low-frequency fluctuations.

The NF code is vulnerable to sensorineural hearing loss (SNHL) because capture depends upon

saturation of IHCs, and thus the interaction of cochlear gain with IHC transduction. In this study,

formant-frequency discrimination limens ($DL_{FF}$s) were estimated for listeners with normal hearing or

mild to moderate SNHL. The F0 was fixed at 100 Hz, and formant peaks were either aligned with

harmonic frequencies or placed between harmonics. Formant peak frequencies were 600 and 2000 Hz,

in the range of first and second formants of several vowels. The difficulty of the task was varied by

changing formant bandwidth to modulate the contrast in the NF profile. Results were compared to

predictions from model auditory-nerve and inferior colliculus (IC) neurons, with listeners' audiograms

used to individualize the AN model. Correlations between $DL_{FF}$s, audiometric thresholds near the

formant frequencies, age, and scores on the Quick speech-in-noise test are reported. SNHL had a strong

effect on $DL_{FF}$ for the second formant frequency (F2), but relatively small effect on $DL_{FF}$ for the first

formant (F1). The IC model appropriately predicted substantial threshold elevations for changes in F2 as

a function of SNHL and little effect of SNHL on thresholds for changes in F1.

**INTRODUCTION**

The importance of speech as a communication signal motivates studies of its neural encoding.  In

listeners with normal hearing, speech intelligibility is robust across a wide range of sound levels and

background noise, and in the presence of temporal and spectral distortions. In contrast, listeners with

even relatively small amounts of hearing loss have difficulty understanding speech in noise. A better

understanding of neural speech coding would illuminate this difficulty and improve signal-processing

strategies designed to aid these listeners. This study focused on perception of vowel-like sounds in

listeners with normal hearing or with a range of sensorineural hearing loss (SNHL) to test the hypothesis

that discrimination of spectral peaks, or formants, is consistent with a code based on the profile of

neural fluctuations (NFs) in auditory-nerve (AN) responses.

In response to voiced sounds, including vowels, most AN responses are dominated by temporal phase-

locking to either the fundamental frequency, F0, or to harmonic frequencies near the fiber's

characteristic frequency (CF, the frequency at which a fiber is most sensitive) (Young and Sachs, 1979;

Delgutte and Kiang, 1984). The dominance of F0 wanes for fibers tuned near spectral peaks, for which

responses are "captured," or dominated, by phase-locking to the harmonic closest to CF (Deng and

Geisler, 1987; Delgutte and Kiang, 1984; Young and Sachs, 1979; Zilany and Bruce, 2007). Early studies

focused on the possibility that phase-locking to the temporal fine structure (TFS) of the harmonics could

provide a code for spectral peaks, yet identification of neural mechanisms that decode TFS phase-

locking has been elusive. The NF model focuses instead on the amplitude of the F0-related fluctuations

in the AN responses (Carney et al., 2015; Carney et al., 2016; Carney and McDonough, 2019; Carney,

2018). These low-frequency fluctuations are important for driving responses at the level of the auditory

midbrain, or inferior colliculus (IC), where nearly all neurons are sensitive to low-frequency fluctuations

of their inputs (Krishna and Semple, 2000; Nelson and Carney, 2007; review: Joris et al., 2004). Most IC

neurons are either are suppressed or excited by a band of modulation frequencies, referred to as band-

suppressed (BS) or band-enhanced (BE) neurons (Kim et al., 2020). The decoding of the NF profile is thus

straightforward: average discharge rates across the population of IC neurons represent the NF profile

across the population of AN fibers. These AN-response characteristics and the rate code at the level of

the midbrain are illustrated in Fig. 1 for models with normal hearing (Fig. 1A) and with SNHL (Fig. 1B).

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Figure 1. Neural fluctuations in model AN responses result in rate code for spectral peaks in the auditory midbrain.
(A) Simulations of AN and IC BS responses in model with normal hearing. AN frequency channels tuned near
spectral peaks have relatively shallow NFs, due to capture of IHC responses, resulting in higher rates in IC BS
neurons, which are suppressed by fluctuations. (B) Simulations for model with SNHL. In the impaired ear, capture
of IHC responses for channels tuned near spectral peaks is weaker, resulting in larger AN NFs, and thus lower IC BS
responses. Hearing loss included in the model corresponded to 12 dB HL at 600 Hz and 18 dB loss at 2000 Hz (AN
model parameters: $C_{IHC}$=0.5, $C_{OHC}$ = 0.5). The effect of relatively mild hearing loss has a much greater impact on the
encoding of F2 in model IC responses.

AN fibers tuned away from spectral peaks have large amplitude NFs at F0, due to beating between

harmonics in the inner ear that is transduced by inner hair cells (IHCs). However, near spectral peaks,

IHC responses saturate, and as a result the F0-related fluctuations are "flattened," reducing the

amplitude of the NFs in responses of AN fibers tuned near spectral peaks (Fig 1, middle)). The profile of

NF amplitudes along the tonotopic axis thus encodes the locations of spectral peaks (Carney et al., 2015)

(Fig. 1, bottom). Information about the frequencies of the spectral peaks, or formant frequencies, allow

identification of vowels. Although NFs are particularly salient for voiced, or harmonic sounds, they also

encode spectral shapes in unvoiced speech sounds (e.g., fricative consonants, Hamza et al., in review).

NFs depend on IHC sensitivity and saturation, and thus are directly influenced by cochlear gain. As a

result, the reduced cochlear gain associated with SNHL affects any neural code based upon NFs. Here we

tested the hypothesis that NFs encode the spectral peaks of vowel-like sounds. The bandwidths of

formants were varied to increase or reduce the contrast in the NF profiles. We also estimated formant-

frequency discrimination thresholds in listeners with a wide range of hearing sensitivity. We

hypothesized that thresholds for all listeners would increase (worsen) as formant bandwidth was

increased, and that thresholds would increase proportionally to hearing loss due to SNHL-dependent

reduction in the contrast of NF profiles. Lastly, for all listeners and formant bandwidths, we varied the

frequency of the formant peak with respect to the harmonic frequencies, a manipulation previously

shown to affect formant-frequency discrimination (Lyzenga and Horst, 1995, 1997, 1998; Tan and

Carney, 2006; Henry et al., 2017).

Our findings suggest that discrimination of F2 is quite vulnerable to hearing loss, whereas discrimination

of F1 is affected very little, even by substantial hearing loss. Predicted discrimination thresholds based

on the NF model were consistent with these psychophysical results. This finding has implications for the

effect of hearing loss on speech understanding. The role of formant-frequency discrimination for F1 and

F2 in determining the systematic patterns of vowel contrasts cross-linguistically will be discussed.

**METHODS**

Listeners.  Thirty-four participants (ages 18-79 years, 26 female, 8 male) were recruited and tested using

procedures approved by the University of Rochester Institutional Review Board. All participants were

initially screened with a standard audiogram (0.25 – 8 kHz; Fig. 2) and were excluded if hearing loss (HL)

was asymmetric ( > 15 dB difference in HL between the two ears) or if HL was greater than 80 dB.

Audiometric thresholds were used as input parameters for the computational models (see below), and

thresholds at 500 Hz and 2 kHz were used in analyses of formant-frequency discrimination thresholds.

All native English-speaking subjects (*n* = 31) were screened with the Quick Speech-in-Noise test (QSIN;

Killion et al., 2004). Individual test sessions were one or two hours in durati

Figure 2. Subject audiograms.  Audiograms (mean of both ears) for each subject. Age ranges are indicated by line
color (see Fig. 7 for individual subject ages).

Stimuli.  Vowel-like stimuli were synthesized based on Klatt (1980), using the glottal pulse of Rosenberg

(1971) and a radiation impedance implemented using a 1$^{st}$-order highpass Butterworth filter with a

corner frequency of 10 Hz. Stimuli had F0 of 100 Hz, duration of 300 ms, 25-ms cos$^2$ on/off ramps, and

were presented at 75 dB SPL. DL$_{FF}$s were estimated for synthetic vowels with two formant

configurations; the formants were either aligned with harmonics (designated ON; F1=600 Hz, F2 = 2000

Hz) or midway between harmonics (designated BTW; F1 = 650 Hz, F2 = 2050 Hz) (Fig. 3). DL$_{FF}$s were also

estimated for three formant bandwidths (50, 100, and 200 Hz; Fig. 3). The 12 stimulus conditions were

tested in blocks that were randomly ordered for each subject.

Figure 3. Stimulus spectra. Discrimination thresholds were measured using a standard pair of identical
sounds and a target pair with a change in (A) F2 or (B) F1.  Spectral peaks were either centered (C, D) on
(ON) a harmonic, or (E, F) between (BTW) harmonics. Formant bandwidths were 50 (purple), 100 (black),
or 200 (orange) Hz.

<u>Procedure</u>.  A two-interval, forced choice, two-down one-up tracking procedure was used, as follows.

Each trial contained two pairs of sounds; the standard pair had identical sounds, and the target pair had

sounds that differed in either F1 or F2. For each track the formant-frequency difference ($\Delta F$) started at

40%. The formant-frequency difference was reduced by a factor of two following every two correct

responses, or increased after incorrect responses, until two reversals occurred. $\Delta F$ was then reduced or

increased by a factor of 1.26 until four reversals occurred, then reduced or increased by a factor of 1.12

until a total of ten track reversals were attained. Individual tracks were retained for analysis if a criterion

of (standard deviation of $\Delta F$ / track threshold) < 0.3 was achieved. The $DL_{FF}$ for each 10-reversal track

was estimated as the average $\Delta F$ of the final six reversals. Overall threshold for a particular stimulus

condition was based on the average of at least three individual track thresholds. If the ratio of the

standard deviation of the threshold estimates to the mean threshold was > 0.3, additional tracks were

collected until the criterion (< 0.3) was achieved. Statistical analyses were based on ANOVA analyses of

linear mixed-effects models, focusing on the bandwidth factor and its interaction with the factors of HL,

QSIN score, and Age.

<u>Computational Modeling Methods.</u>  Model thresholds were estimated as follows: auditory-nerve (AN)

responses were simulated for 11 high-spontaneous-rate fibers with log-spaced CFs spanning 1/3-octave,

centered at the formant frequency being tested. A single model AN fiber was simulated for each

frequency channel. Thresholds based on individual audiograms for each listener were included in the AN

model (Zilany et al., 2014).

Model $DL_{FF}$s were based on Band-Suppressed (BS) IC model neurons (Fig. 4; Carney and McDonough,

2019). Midbrain neurons were either excited or suppressed by temporal fluctuations on their inputs.

The BS population rate-profile peaks at frequencies near formants, where fluctuations are reduced by

capture (Fig. 1). Fluctuations were minimal near formant peaks, due to capture of the IHC responses by

a single harmonic near CF (Deng and Geisler, 1987; Zilany and Bruce, 2007). BS models had modulation

transfer functions with a trough frequency at 64 Hz, the median observed in a population of rabbit IC

neurons (Kim et al., 2020).

Figure 4.  Schematic illustration of models for band-enhanced (BE) and band-suppressed (BS) IC neurons. Model IC
BS neurons were used in this study. (From Carney et al., 2015)

The stimulus interval with model population rate-profiles having the largest mean squared difference

across the pair of stimuli was chosen as the target interval. Rate profiles were based on the mean rates

of model IC BS neurons, omitting the first 25 ms that includes the onset response. Thirty trials were run

for each ΔF in every stimulus condition, i.e., for variation of F1 or F2, for standard stimuli with formants

on or between harmonics, and for the three formant bandwidths. Half of the simulated trials had the

test stimulus as the first interval of the test pair, and half had this stimulus as the second interval, in

order to counterbalance any effects of neural adaptation in the model. Simulations were done for %ΔF =

0.01, 0.02, 0.05, 0.1, 0.2, .5, 1, 2, 5, 10, 20, and 50 to cover the wide range of thresholds for the entire

group of listeners. Each $DL_{FF}$ estimate was based on a logistic function fitted to %-Correct vs. %ΔF. Model

threshold was estimated as the %ΔF that resulted in 70.7% correct performance. Data files and Matlab

code used for simulations and figure preparation will be made available on an OSF website.

**RESULTS**

Thresholds vs. HL at formant frequencies

Subject thresholds for the F2 and F1 conditions, as a function of HL and stimulus bandwidth, are

presented in Fig. 5; results from ANOVA analysis of linear mixed-effects models for the same data are

presented in Table 1. For the F2 condition there was a strong, positive, linear correlation between

threshold and HL. These correlations were similar for all three tested bandwidths, and also for both ON

and BTW stimuli (see Fig. 5 legend for linear regression $R^2$ values). A significant bandwidth-dependent

increase in threshold was also observed for both ON and BTW, being particularly evident for subjects

with HL < 15 dB (*cf.* Fig. 5 top row panels), and confirmed with ANOVA analysis (Table 1). For the F1

condition there was little evidence for positive correlation between threshold and HL for any of the

tested bandwidths (Fig. 5, bottom row; Table 1). Similar to the F2 condition, a significant bandwidth-

dependent increase in threshold was observed in the F1 condition for both ON and BTW, particularly

evident for subjects with HL <15 dB, and was confirmed by ANOVA analysis (Table 1). These results are

consistent with a statistically significant, positive, bandwidth- and mid-to-high frequency HL-dependent

difficulty in discriminating differences in F2, a difficulty that is comparatively absent for F1

Figure 5.  F2 and F1 threshold as a function of HL and stimulus bandwidth. For each plot the aggregate data for ON
(solid symbols) and BTW (open symbols) are fitted with linear regressions (solid and dotted lines, respectively);
data points are color- and symbol-type-coded by age range as indicated (see also Fig. 7), plotted as $\log_{10}$(%F). For
the F2 condition (top row), thresholds for both ON and BTW stimuli increased significantly with increasing HL at
2000 Hz (linear regression $R^2$ values: ON, 0.72 (50 Hz), 0.74 (100 Hz), 0.75 (200 Hz); BTW, 0.70 (50 Hz), 0.72 (100
Hz), 0.71 (200 Hz)). For the F1 condition (bottom row) there was little evidence for correlation between threshold
and HL at 500 Hz (linear regression $R^2$ values: ON, 0.02 (50 Hz), 0.06 (100 Hz), 0.01 (200 Hz); BTW, 0.08 (50 Hz),
0.11 (100 Hz), 0.11 (200 Hz)). In both the F2 and F1 conditions, for HL < 10 dB discrimination thresholds were
elevated for both ON and BTW for BW 200 Hz compared to the narrower bandwidths. See Table 1 for ANOVA
analyses of the plotted data. Note the age-dependence of BTW thresholds for F1 discrimination, as indicated in
Table 1, is highlighted by the red arrows, which point to the relatively low thresholds for F1 BTW for younger
listeners with normal hearing (NH).

Ratiometric comparison of ON and BTW thresholds as a function of HL and stimulus bandwidth are

presented in Fig. 6. For subjects with HL less than 10 dB at either 2000 or 500 Hz, thresholds for ON

were typically higher than BTW for both the F2 and F1 conditions, particularly for subjects with age less

than 40 yrs (black symbols, Fig. 6). This trend was reduced for all subjects, and for both the F2 and F1

conditions, as a function of increasing stimulus bandwidth. These results indicate that most subjects had

higher thresholds for the ON condition (i.e., threshold ratios > 1) as compared to the BTW condition, for

both the F2 and F1.

Figure 6. Ratio of ON and BTW thresholds as a function of HL and bandwidth. For F2 (top row), normal-hearing
subjects (<15 dB HL) tend to have greater thresholds for ON than BTW at 50 Hz bandwidth, a trend that is absent
at greater bandwidths; subjects with mild-to-moderate HL tend to have greater threshold for ON compared to
BTW as a function of increasing bandwidth. For F1 (bottom row), normal-hearing subjects have a consistently
higher threshold for ON than BTW, independent of HL and bandwidth; the thresholds for ON and BTW are similar
with increases in HL and bandwidth.

QSIN scores as a function of subject age and HL are presented in Fig. 7. The strongest linear correlation

(i.e., regression $R^2$ value) was observed for HL at 2000 Hz (Fig. 7, right panel). This result was supported

by ANOVA analysis (Table 1). Outlier QSIN scores > 10 for two subjects suppressed these correlations,

particularly with respect to HL; when those two data points were excluded the $R^2$ values were 0.17 (age),

0.38 (HL 500 Hz), and 0.50 (HL 2000 Hz). These results indicate a general, positive correlation between

QSIN score and HL, and further indicate that formant-frequency discrimination tasks, such as those used

in this study, could be used as non-cognitive surrogates to the QSIN test to assess HL and vowel-sound

discrimination.

Figure 7.  QSIN scores as a function of age and HL. Linear regressions and $R^2$ values are indicated; color and symbol-
type (left panel) match that of Figs. 5 and 6. QSIN scores were correlated with age and HL, particularly for HL at
2000 Hz (right panel). See Table 1 for ANOVA analyses of these data.

Statistical Analysis

Statistical evaluation ($p$-values of ANOVA analysis of linear mixed-effects models) of the human-derived

thresholds is summarized in Table 1. For both F1 and F2, and in both the ON and BTW conditions,

bandwidth had a significant effect upon $DL_{FF}$, with no significant interaction between bandwidth and

age. There was a significant effect of age (green box, Table 1) and hearing loss upon the F1 BTW

condition, for which some young subjects with low audiometric thresholds had especially low thresholds

(presented graphically below). For F2, but not F1, QSIN score, age, and hearing loss at 2 kHz all had

significant effects on $DL_{FF}$s for both the ON and BTW conditions. Interactions between bandwidth and

hearing loss, and between bandwidth and QSIN score, were significant only for the F2 BTW condition.

The effects of hearing loss near the formant frequency, QSIN score, and age were always significant for

the F2 thresholds, the only significant interaction for the F1 BTW condition being that between age and

bandwidth. These statistical analyses indicated that all interactions between a factor (age, QSIN score,

and hearing loss) and bandwidth were significant for the F2 BTW condition.

| Factors and Interactions | F1 ON | F1 BTW | F2 ON | F2 BTW |
|---|---|---|---|---|
| Bandwidth | $p < 0.001*$ | $p < 0.001*$ | $p < 0.001*$ | $p < 0.001*$ |
| HL @ 500 (F1) or 2000 (F2) (N = 34) | 0.20 | 0.02* | $p < 0.001*$ | $p < 0.001*$ |
| Bandwidth | $p < 0.001*$ | $p < 0.001*$ | $p < 0.001*$ | $p < 0.001*$ |
| HL:Bandwidth | 0.68 | 0.75 | 0.08 | 0.004* |
| QSIN scores (N = 31) | 0.48 | 0.18 | 0.013* | 0.009* |
| Bandwidth | $p < 0.001*$ | $p < 0.001*$ | $p < 0.001*$ | $p < 0.001*$ |
| QSIN:Bandwidth | 0.16 | 0.34 | 0.64 | 0.015* |
| Age (N=34) | 0.14 | 0.007*† | 0.001* | p<0.001 |
| Bandwidth | $p < 0.001*$ | $p < 0.001*$ | $p < 0.001*$ | p<0.001 |
| Age:Bandwidth | 0.47 | 0.02* | 0.20 | 0.02 |

241    Table 1. P-values of ANOVA analysis of Linear Mixed-Effects Models, focusing on the bandwidth factor and its
242    interaction with the factors of hearing loss (HL), QSIN score, and age. The * symbol indicates statistical significance
243    (p < 0.05); the † symbol highlights the age-dependence of threshold for the F1 BTW condition (see arrows in Fig. 5).
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Listeners' formant-frequency discrimination thresholds were estimated based on AN and IC BS

computational-model responses. Predictions based on AN rate profiles quantify the ability to predict

responses based on AN rate-based coding of differences in the stimulus spectra. These results can be

compared to the predictions presented below that were based on model IC BS neurons, which quantify

the ability of neural fluctuation-based coding of the spectra.

The rate profiles for 1/3-octave CF ranges of AN fibers are shown in Fig. 8, for stimuli that differed in F1

(bottom row) or F2 (top row) conditions, ON (on-peak) or BTW (between-peak) conditions, and formant

bandwidth (colors). Responses to the standard stimuli, with spectral peaks at 600 or 2000 Hz for the ON

condition, or 550 or 1950 Hz, for the BTW condition, are shown in dark lines, with line color indicating

formant bandwidth. Responses to target stimuli that were shifted down in frequency by 5% of the

formant frequency are shown in light lines, for all three bandwidth conditions. Stimuli were presented

to the model in two pairs, one with identical standard stimuli, and one with a formant-frequency

difference. The sum of the squared differences across the 11 CF channels was used to estimate the

stimulus pair that differed on each trial. Percent-correct scores were tallied across 30 trials for each

stimulus condition, for a range of formant-frequency differences. A logistic function fit to the percent-

correct results was used to estimate the formant-frequency differences corresponding to threshold, or

70.7% correct.

Figure 8. AN model rate profiles for models with (A) NH and (B) SNHL corresponding to 12 dB loss at 600 Hz and 18 dB loss at 2000 Hz (AN model parameters: $C_{IHC}$=0.5, $C_{OHC}$ = 0.5). AN model rate profiles are illustrated for stimuli that differed by ΔF = 5%, which is above threshold for either NH or listeners with the degree of SNHL included in (B) (cf., Fig. 5, note $\log_{10}(5\%) \approx 0.7$). Model rate profiles are shown for the three formant bandwidths using line colors matched to Fig. 3: 50-Hz BW, purple; 100-Hz, black; 200-Hz, orange. For each BW, the darker line corresponds to the standard stimulus, and the lighter line is the response to a formant shifted down by 5% of the standard formant frequency (2000 Hz or 600 Hz). Each AN model profile is for 11 frequency channels spanning 1/3-octave centered at the formant frequency. Model threshold estimates were based on the sum of squared errors between rate profiles. The rate profiles illustrated here are based on averages of 10 trials.

The AN-model threshold estimates as a function of subject thresholds are presented in Fig. 9. In the F2

condition, for bandwidths of 100 and 200 Hz, the model-derived thresholds were positively correlated

with subject thresholds and roughly captured the human threshold values ($R^2$ range of 0.28-0.36 for ON

and BTW). For the F1 condition, for all three bandwidths, the AN model consistently returned elevated

thresholds (points above the unity line on Fig. 9) that were negatively correlated with the human

threshold values plotted as a function of SNHL. These model results suggest that the AN model captures

some aspects of human F2 and F1 thresholds, but that absolute AN-model threshold values were

consistently higher than human thresholds for the F1 conditions and for the 50-Hz F2 condition. The

relatively small AN rate differences observed in the F1 condition responses, for both NH and SNHL

models (Fig. 8A, B, bottom row) are consistent with the elevated threshold estimates in Fig. 9.

Differences in AN rate profiles for stimuli that differed in F2 (Fig. 8A, B, top row) were large enough to

estimate thresholds similar to some listeners' thresholds, but the trends with SNHL and BW in the

listeners' threshold were not well predicted by AN model responses.

Figure 9.  AN-model thresholds as a function of subject thresholds. Symbol types and colors as in Fig. 5, with the gray line indicating unity. Bold lines correspond to linear regressions of the displayed ON (black) and BTW (red) data sets, with the $R^2$ values indicated in each panel. The AN model captured some of the F2 data trends for 100 and 200 Hz bandwidths, but less so for the 50-Hz bandwidth (cf. the respective panels in Fig. 5). For F1 conditions, AN-model thresholds were consistently elevated with respect to human thresholds (points above the unity line) and were negatively correlated with the listeners' thresholds. Model thresholds were based on 30 repetitions of single-trial responses that were used to estimate logistic functions (see Methods).

Figure 10 shows examples of IC BS model rate profiles for a NH model (Fig. 10A) and a model with SNHL

(Fig. 10B). The AN inputs used for the example IC BS model responses shown in Fig. 10 were the exact

responses shown in Fig. 8. Thus, direct comparison of Figs. 8 and 10 provides a qualitative illustration of

the difference in information between AN rate profiles and AN NF profiles, which are mapped into IC

rate profiles.

Figure 10. IC BS model rate profiles for inputs with (A) NH, and (B) SNHL corresponding to 12 dB loss at 600 Hz and 18 dB loss at 2000 Hz (AN model parameters: $C_{IHC}$=0.5, $C_{OHC}$ = 0.5). IC model rate profiles are illustrated for stimuli that differed by ΔF = 5%, which is above threshold for either NH or listeners with the degree of SNHL included in (B) (cf., Fig. 5, note $\log_{10}(5\%) \approx 0.7$). Model rate profiles are shown for the three formant bandwidths using line colors matched to Fig. 3: 50-Hz BW, purple; 100-Hz, black; 200-Hz, orange. For each BW, the darker line corresponds to the standard stimulus, and the lighter line is the response to a formant shifted down by 5% of the standard formant frequency (2000 Hz or 600 Hz). Each IC model profile is for 11 frequency channels spanning 1/3-octave centered at the formant frequency. Model threshold estimates in Fig. 11 were based on the sum of squared errors between rate profiles. The rate profiles illustrated here are based on averages of 10 trials.

Examples of model IC BS population responses to stimulus pairs for different conditions (F1 and F2, ON

and BTW) and for different formant bandwidths (colors) are illustrated in Fig. 10. Figure 10A shows NH

models responses, and Fig. 10B shows responses for a model that received inputs from an AN model

with SNHL (see caption, Fig. 8B). Squared differences between the IC rate profiles for the standard

formant frequencies (dark lines, either F1 = 600 H or F2 = 2000 Hz) and for the target formants that

were shifted down (light lines, shifted by 5% of the formant frequency in the examples shown) were

used as the decision variable to estimate model thresholds. The same 2-pair (i.e., 4-interval) stimuli

were used for the model responses for each trial as were used in listening tests, and the pair of model

responses with the larger squared rate difference was selected as the target interval. Note that for the

model with NH (Fig. 10A), the model IC BS rate profiles in response to F2 (top row) shifted  to the left

when the formant frequency shifted to a lower frequency (lighter lines), as compared to the standard

formant frequency of 2000 Hz (darker lines). The sharper IC BS rate profiles in response to the BTW

condition with respect to the ON condition were due to differences in the nature of the stimulus

fluctuations when the formant was aligned with a harmonic, as opposed to when it fell between two

harmonics (Lyzenga and Horst, 1997; Tan and Carney, 2006; Henry et al., 2017).

The NH model rate profiles in response to F1 (Fig. 10A, bottom row) had relatively small differences over

the 1/3-octave range of CFs that were included in the simulations, yet the squared differences between

responses across this limited CF range explained listener thresholds (Fig. 11). Interestingly, the

differences in NH model rate profiles for the F1 BTW condition were only slightly larger than those for

the ON condition, but this greater difference predicted the lower thresholds for the BTW condition that

were observed for the youngest listeners with good thresholds (Fig. 11, and Fig. 5, red arrows). Note

that the model IC BS rate profiles in response to F1 (Fig. 10, bottom row) do not show simple leftward

shifts when the formant frequency was shifted lower (compare light to dark lines for each bandwidth, or

color, in Fig. 10). Instead, the reduced IC rates in response to the shifted formants (lighter lines) reflect

the larger fluctuations that occur in AN responses when F1 was shifted away from a harmonic (see Fig.

1), and the subsequent suppression of the model IC BS responses by fluctuations on their inputs.

The IC model results as a function of subject thresholds are presented in Fig. 11. Compared to the AN

model, the IC-model threshold estimates better matched human thresholds for the F2 condition, and

were well correlated for the 100- and 200-Hz bandwidth conditions (with correspondingly greater $R^2$

regression values; top row, Fig. 11). IC-model F2 threshold estimates were slightly lower than subject

thresholds (i.e., regression lines were below the unity line), suggesting that the IC model was sufficient

to explain listeners' F2 thresholds, whereas the AN-model thresholds were not (Fig. 9). The IC model

also performed better than the AN model in estimating the subjects' F1 thresholds (cf. linear regressions

in the bottom rows of Figs. 9 and 11). For the F1 ON condition the IC model correctly predicted the

listeners' threshold values, whereas for the F1 BTW condition, with the exception of subjects with the

lowest thresholds, IC-model thresholds were substantially lower than the corresponding listeners'

thresholds (i.e., points and red regression lines fell below the gray unity line in Fig. 11, bottom row), a

trend that decreased with increasing bandwidth. These results indicate that detection cues available to

the IC model might also be used by human subjects, especially for the F2 condition at 100 and 200 Hz

(both ON and BTW). For the F1 condition, the model apparently takes advantage of enhanced

fluctuation cues present in the BTW condition, but only the most sensitive human subjects apparently

used those cues.

Figure 11. IC-model thresholds as a function of subject thresholds. Symbol types, colors, and lines as in Fig. 9.
Compared to the AN model, the IC model better represented ON and BTW human subject data for the F2 condition
at all three bandwidths (*cf.* corresponding panels in Fig. 9). For F1, the IC model generally matched the values of
the ON subject data at all three bandwidths, but consistently had lower thresholds than the human data for the
BTW condition (open symbols, bottom row). Model thresholds were based on 30 repetitions of single-trial
responses that were used to estimate logistic functions (see Methods).

## DISCUSSION

The goal of this study was to test the hypothesis that NF cues support encoding of formant frequencies

in vowels. Two factors that affect NF coding in computational models of midbrain responses to vowels

are formant bandwidth and SNHL. The results of manipulating the bandwidth of formants in synthetic

vowel-like sounds and by testing listeners with a range of SNHL generally supported the hypothesis.

Furthermore, these results showed a surprising insensitivity of F1 discrimination to SNHL and a

surprising sensitivity of F2 discrimination to SNHL. The NF-based IC-level model was largely able to

capture the trends in these results, although the IC model predicted lower thresholds for most listeners

to the BTW condition. The BTW condition has been explored in previous studies of NH subjects

(humans: Lyzenga and Horst, 1995; budgerigars: Henry et al., 2017). Model thresholds were consistent

with those of young listeners with NH who perform better in the BTW condition as compared to the ON

condition, as expected due to stronger fluctuation cues in response to BTW stimuli (Tan and Carney,

2006). However, most other listeners in our test group, especially those who were not in the youngest

group or had any measurable elevation of audiometric thresholds, did not seem to take advantage of

these fluctuation cues, based on the fact that they did not have improved performance for the BTW

condition.

IC-model thresholds were particularly successful at predicting the strong dependence of F2-

discrimination thresholds on SNHL (Fig. 11). In contrast, a model based on AN rate profiles did not

predict the trends in threshold with SNHL and had thresholds that were generally elevated with respect

to listeners' thresholds (Fig. 9). The improved predictions of thresholds by the IC-model rate profile, as

compared to the AN model rate profile, suggests that NFs play an important role in coding of the vowel

spectra. AN rate profiles provide a representation of the "excitation pattern" associated with the

responses of the inner ear, but do not include the temporal patterns of the responses. In contrast, the

IC-model rate profile combines the representations of energy and low-frequency temporal fluctuations.

QSIN scores were correlated to thresholds for F2, most strongly for the F2 BTW condition (Fig. 7, Table

1). Thus, this condition may provide an alternative to intelligibility testing for quantifying sensitivity of

individual listeners to changes in speech sounds. A potential benefit of using the formant-frequency

discrimination task to predict speech intelligibility is that it likely to be less sensitive to cognitive factors

associated with speech testing, including a native English-speaking background. This result is consistent

with earlier studies, based on vowel similarity testing, which reported that F2 discrimination is an

important factor in multiple-regression analyses relating speech perception to psychophysical

thresholds in listeners with SNHL, and that F1 is weighted more strongly in listeners with SNHL

(Dreschler and Plomp, 1980, 1985).

Future studies will explore strategies for enhancing intelligibility by manipulating neural-fluctuation

profiles. The potential implication of elevated DL$_{FF}$s for F2 on intelligibility is illustrated by the loss of

resolution on the F2 axis of the English-language vowel space (Fig. 12). For our listeners, F1 DL$_{FF}$s were

not significantly elevated by HL at 500 Hz, thus one would expect that their resolution along the F1 axis

of a 2D vowel space would not be affected. However, F2 DL$_{FF}$s were significantly elevated by HL at 2 kHz,

Figure 12.  Vowel space (A) with 'dilation' corresponding to 35% increase in F2 range (±17% with respect to
Peterson and Barney, 1952) based on changes in DL$_{FF}$s for listeners with SNHL. Schematic visualization of the
implications of elevated FFDLs for vowel discrimination.  NOTE:  Threshold for listeners with most hearing loss in
F2, BW=100 Hz condition was 35% [log10(35%) = 1.54 on log axis] for both ON and BTW conditions. This listener
required a 35% difference in the frequency of F2 to reliably detect a change, in comparison to subjects with 0 dB
HL who required ~1% difference.  Diagram shows schematically the increase in overlap of the vowels in the vowel
space that might correspond to higher DL$_{FF}$s for F2.

by as much as 35% for the listeners in this study with the largest SNHL. Figure 11 shows the Peterson

and Barney (1952) vowel space for English to illustrate the effect of a 35% decrease in F2 resolution, i.e.,

a 35% increase in the size of vowel clusters. Considerable overlap between vowel clusters is consistent

with elevated QSIN scores for listeners with high F2 DL$_{FF}$s. The increase in overlap of spaces associated

with vowel contrasts depending on F2 is generally consistent with vowel confusions in listeners with

SNHL reported by Van Tasell et al. (1987) (e.g., the most common confusion reported was between /ʌ/

and /a/, with other common confusions being /ʌ/ and /æ/, /ɛ/ and /æ/, and /a/ and /æ/).

Our results shed new light on the structure of vowel contrasts and systems. In a well-documented,

cross-linguistic phenomenon, observed vowel contrasts pattern in consistent ways, dispersing

themselves within a space defined by the acoustic parameters of the vowels' first two formants, F1 and

F2, referred to as Dispersion Theory (Liljencrants and Lindblom, 1972; Lindblom 1986; Schwartz et. al.

1997a,b; Becker-Kristal, 2010). A given vowel space is defined by the highest front vowel [i] and the

lowest vowel [a] (Becker-Kristal, 2010), with larger systems occupying a larger space. However, the

larger vowel systems differ from smaller systems in the number of vowel contrasts, mainly along the F1

(height) parameter. Attempts at modeling the vowel space overpredict the number of vowel contrasts

that appear along the F2 (backness) parameter (Liljencrants and Lindblom, 1972; Schwartz et al., 1997a).

The acoustics of vowels sounds cannot explain these vowel-dispersion patterns, thus nearly every study

in this area has called on the need to understand the constraints of the auditory system on vowel

patterns. Our finding that formant-frequency discrimination in the F2 dimension is particularly

vulnerable to hearing loss, whereas discrimination in the F1 dimension is not, is consistent with the

relative importance of F1 in vowel contrasts in most languages. Additionally, the spectral magnitude of

F2 is inherently lower than that of F1 (Klatt, 1980), exacerbating the effect of hearing loss in the F2

frequency region.

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