Hearing elliptic movements reveals the imprint of action on prototypical geometries

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Abstract

Within certain categories of geometric shapes, prototypical exemplars that best characterize the category have been evidenced. These geometric prototypes are classically identified through the visual and haptic perception or motor production and are usually characterized by their spatial dimension. However, whether prototypes can be recalled through the auditory channel has not been formally investigated. Here we address this question by using auditory cues issued from timbre-modulated friction sounds evoking human drawing elliptic movements. Since non-spatial auditory cues were previously found useful for discriminating distinct geometric shapes such as circles or ellipses, it is hypothesized that sound dynamics alone can evoke shapes such as an exemplary ellipse. Four experiments were conducted and altogether revealed that a common elliptic prototype emerges from auditory, visual, and motor modalities. This finding supports the hypothesis of a common coding of geometric shapes according to biological rules with a prominent role of sensory-motor contingencies in the emergence of such prototypical geometry.

Introduction

Our perceptual system stores and categorizes objects from our surroundings around canonical items, called prototypes, that are the most representative of their category. Geometric prototypes have been viewed as mainly emerging from visual experiences (Rosch, 1973; Rosch & Mervis, 1975; Feldman, 2000; Kalénine et al. 2011; Theurel et al. 2012), via the haptic sensory channel (Theurel et al., 2012; Kalénine et al. 2011) and via a motor restitution (Feldman, 2000; Kalénine et al., 2013). Alternatively, the possibility to recall prototypes through visual and haptic modalities or motor output may suggest common processing of these specific shapes. Whether such prototypes only rely on spatial cues that are present in the visual, haptic, and kinetic domains is still questioned. Could such geometric prototypes also be recalled through auditory stimuli that are solely based on dynamic cues? Answering this question is fundamental to understanding the influence of the motor system on human learning, memory, and cognition. It is essential both for the language sciences (Sablé-Meyer et al., 2021) and for cognitive neuroscience as this is a cornerstone question in these fields (Dehaene et al., 2006).

Interestingly, studies revealed the proficient role of the auditory modality to perceive movements and shapes through timbre variations of monophonic sounds (Merer et al. 2008; 2013). More strikingly, Thoret et al. (2014) demonstrated that auditors listening to synthesized monophonic friction sounds corresponding to those produced by the pencil of someone drawing on a paper, were able to recognize specific kinematics characterizing biological motion, in particular the 1/3 power law linking the tangential velocity of the hand movement to the curvature of the drawn shape (Lacquaniti et al., 1983). In addition, they were even able to discriminate geometric shapes, such as a circle, an ellipse, and a line, simply by listening to synthetic friction sounds in which timbre variations revealed the velocity profile of the drawing movement. In follow-up studies, we demonstrated that these acoustic variations may even distort the visuomotor coupling of biological motions (Thoret et al, 2016a, 2016b). Taken

together, these studies suggest that simple geometric shapes can be evoked through the auditory

channel and that the auditory modality may play a significant role in the perception and

production of geometric shapes.

Here we investigated the hypothesis that geometrical prototypes can be recalled through

the auditory modality employing timbre variations of friction sounds evoking the velocity of

biological movements. We focused on a particular shape category, ellipses, that encompass any

closed shape of a conic section contained between a line and a circle. From a geometric point

of view, an ellipse is principally described by its eccentricity representing its flatness. The

eccentricity is a number comprised between 0 and 1: the flatter the ellipse, the higher the

eccentricity. The line and the circle are two specific cases which eccentricities equal 1 and 0

respectively. From a dynamic point of view and concerning the 1/3 power law, the accelerations

of an elliptic movement increase as the distance between the focal points of the ellipse increases

(i.e., when the ellipse tends towards a line). Ellipses can be distinguished by ear from circles

and lines and do not involve discontinuity movements. Hence, this geometric shape has been

chosen for the present study.

Based on the dynamic model of biological motion described below, four experiments

were designed to examine how participants assessed the prototypical ellipse through different

modalities. The first three experiments aimed at highlighting the geometric prototype from

visual and motor restitutions. The fourth experiment was the cornerstone of this series of

experiments and focused on sounds' ability to evoke an elliptic prototype based on the

kinematics underlying the drawn ellipse. Consistency between this auditory prototypical ellipse

and the visual and motor prototypes would support a common encoding of prototypical shapes.

Before presenting the four experiments, the dynamic model of elliptic motions used in

the four experiments will be described in the following section. The results of these experiments

are presented together.

A model of biological elliptic motor dynamics

Biomechanical mechanisms involved in graphical production as handwriting have been extensively investigated. It has been shown that dynamic and geometric properties of elliptic motions can be modeled by explicit equations. The dynamic approach of movement production supports the idea that planar hand movements can be modeled by two harmonic oscillators $(x(t), y(t))$ whose frequencies, amplitudes and phases evolve over time (Hollerbach, 1981) with the following system:

$$\begin{cases} x(t) = A_x(t)\cos\big(\omega_x(t) + \phi_x(t)\big) \\ y(t) = A_y(t)\cos\big(\omega_y(t) + \phi_y(t)\big) \end{cases}$$

where A_x and A_y are the amplitudes, and ω_x and ω_y the frequencies, and ϕ_x and ϕ_y the phases of the two oscillators. In the case of periodic elliptic motions, this model can be simplified by equaling the amplitudes and frequencies of the oscillators $(A(t) = A_x = A_y = A$ and $\omega(t) = \omega_x = \omega_y = \omega)$:

$$\begin{cases} x(t) = A\cos(\omega t) \\ y(t) = A\cos(\omega t + RP) \end{cases} \tag{1}$$

where A is the amplitude, $\omega = \dfrac{2\pi}{T}$ the frequency with T the period of the motion, and $RP = \phi_x - \phi_y$ the relative phase between the oscillators $x(t)$ and $y(t)$.

Hence, this system co-defines the motion dynamics and the geometry, but may also be used to parameterize only the geometry of the entire ellipse whether or not the ellipse is considered dynamically. Practically, the eccentricity e of the ellipse and the relative phase RP are linked by the following relations demonstrated in Appendix A:

$$\begin{cases} RP = 2\arctan\sqrt{1 - e^2} \\ e = \sqrt{1 - \tan^2\left(\dfrac{RP}{2}\right)} \end{cases} \tag{2}$$

It should be noted that this model complies with the biological rules, namely the 1/3 power law

100   (Lacquaniti et al., 1983), as demonstrated in Appendix A.

101   This model then enables the generation of biological elliptic motions whose trajectory

102   can be continuously morphed from a line (RP = 0°) to a circle (RP = 90°) by simply acting on

103   RP (see Figure 1). It will be used in the four following experiments in order to generate visual

104   and auditory stimuli complying with biological motion. Motor productions of Experiment 2

105   will also be analyzed regarding this model.

106   Finally, the tangential velocity profile was generated according to the equations (1) and

107   can be explicitly written as follows:

108
$$v(t) = A\frac{2\pi}{T}\sqrt{\sin^2\left(\frac{2\pi}{T}t\right) + \sin^2\left(\frac{2\pi}{T}t + RP\right)} \quad (3)$$

109   Although the mapping was arbitrarily fixed during the experiment, it is noticeable that it also

110   varied according to the period T and the amplitude A of the motion.

RP	0°	15°	30°	45°	60°	75°	90°
e	1	.99	.96	.91	.82	.64	0

Figure 1. Continuum of different ellipse shapes from a line (left) to a circle (right) with the

corresponding relative phases RP and eccentricities e.

Experiment 1 – Static Visual Output

The first experiment aimed to evaluate the prototype of the ellipse from visual restitution (i.e.,

visual output). To that aim, an adjustment protocol was established. Participants were asked to

adjust the eccentricity of static ellipses on a screen to evoke the most representative shape of

this geometric category.

Methods

Participants. Twenty right-handed participants (8 women) with an average age of 30.6

years (SD = 12.8) voluntarily took part in the experiment. All the participants were naive to the

purpose of the experiment. As in all the following experiments, participants gave their informed

consent before the study, and the experiment was approved by the Aix-Marseille University

ethical committee.

Stimuli. The visual stimuli were white static ellipses displayed on a black background

with different sizes and eccentricities according to the dynamic model previously introduced

(equations (1)). Three sizes defined by the amplitudes $A_1 = 3cm$, $A_2 = 5cm$, $A_3 = 10cm$ were

chosen. The ellipses were rotated counterclockwise by 45° to conform to the preferential

drawing inclination of an ellipse for right-handed persons (Danna et al., 2011).

Apparatus. The participants sat in front a computer screen (DELL 1907fp) with a

resolution of 1280 x 1024 pixels and a frame rate of 60 Hz. The ellipses were displayed at the

center of the screen and the interface was programmed with Max/MSP software

(http://cycling74.com/). Participants modified the ellipse eccentricities by using a MIDI AKAY

MPK keyboard. The experiment took place in a lighted room.

Task. The participants were asked to adjust the eccentricity of the static ellipse displayed

on the screen so as to set the most representative geometric shape of this category. The notion

of the most representative ellipse was explained in French to the participants by the following

sentences (here translated in English): *Ellipses correspond to any closed shape between a line*

and a circle. When you imagine an ellipse, you may have one particular elliptic shape in mind.

You will adjust the ellipse on the screen to display the ellipse you think is the most prototypical.

The adjustment protocol was based on the one proposed by Carlyon et al. (2010). The ellipse

eccentricity was adjusted thanks to 6 different keys defined on the keyboard: "<<<" – "<<" –

"<" and ">" – ">>" – ">>>". Depending on the selected key, the ellipse eccentricity was

modified with different step sizes. The higher the number of arrows the greater the step size,

i.e. the modification of the eccentricity. To avoid a possible non-sensorial bias due to the

orientation of the arrows (right or left), the action of the keys on the eccentricity differed across

participants. Hence, for half of the participants, arrows that pointed to the right increased the

eccentricity and for the other half they had the opposite effect. In addition, the step sizes were

not the same in both directions. Hence, for a given participant, all the arrows in one direction

(right or left) increased for instance the eccentricity by steps of {.01; .02; .03} while the others

(left or right) decreased the eccentricity by steps of {-.1; -.001; -.005}. Finally, 11 repetitions

for each size starting from 11 different initial eccentricities equally distributed between 0 and

1 were executed. The experiment was then composed of 33 trials, i.e. 3 {Sizes} x 11

{repetitions}, presented according to two pseudo-random series counterbalanced across the

participants. The participants were prompted to explore the whole range of possibilities with

the large arrows and to refine their adjustment with the smaller ones. For each participant, 33

final eccentricities were collected and the median was computed.

Experiment 2 – Motor Output

The goal of this experiment was to evaluate whether a prototypical eccentricity of an

ellipse can be elicited by a motor output. A motor production task was set up during which the

participants were asked to draw the ellipse which best represents this geometric shape category.

Methods

Participants. Twenty participants (2 left-handed - 5 women) with an average age of 39.6

years (SD = 11.5) voluntary took part in the experiment and were naive to the purpose of the

study. None of them participated in Experiment 1.

Apparatus. The participants sat in front of a Wacom Intuos5 graphic tablet enabling to

record graphic movements with a spatial precision of 5.10^{-3}mm and a sample rate of 129 Hz.

The data were recorded and collected using an interface programmed with the Max/MSP

software. The experiment was conducted in a lighted room.

Task. The participants were asked to repeatedly and continuously draw the most

representative ellipse of this geometric shape category on the graphic tablet during 50 seconds.

The notion of the most representative ellipse was explained with the same sentence as in

Experiment 1. Participants saw their hands during the recording, but no trace was visible on the

graphic tablet. The experiment comprised three sessions of 50 seconds. The participants were

asked to draw *small*, *intermediate*, and *large* ellipses in two different orders counterbalanced

across participants: 1) small – 2) intermediate – 3) large, or conversely. No template of the

ellipses was presented, but the participants could train in advance by drawing the 3 different

ellipses on the graphic tablet during a session preceding the experiment.

Data analysis. For each participant, recordings of the sampled coordinates $(x(t), y(t))$ of

the stylus on the graphic tablet were collected. To eliminate the numerical noise, the raw data

were smoothed with a Savitsky-Golay filter (Savitsky and Golay, 1964) with a 43 samples

window and a 3rd-order interpolation. This is equivalent to a low-pass filter with a cutoff

frequency of 8 Hz. A high-pass filter (Butterworth) with a cutoff frequency of .2 Hz was also

applied to eliminate the spatial drift of the participants' hands during their movements.

The geometric characteristics of the drawn ellipses were analyzed according to the

relative phase. Computing the Hilbert transforms of $x(t)$ and $y(t)$ enabled to estimate the relative

phase RP between two oscillators (Panter, 1965; Smith and Mersereau, 1991) with the

following formula: $RP(t) = |\tilde{x}(t) - \tilde{y}(t)|$, where $\tilde{x}$ and $\tilde{y}$ are the unwrapped Hilbert transforms

of x and y. The median of the relative phases RP were then computed for each recording and

then transformed into eccentricity. For each participant, 3 final eccentricities were collected

and the median was computed.

Experiment 3 – Dynamic Visual Output

Here, the Experiment 1 was reproduced with dynamic visual stimuli. The participants were asked to calibrate the eccentricity of the elliptic trajectory of a moving spotlight to create the most representative ellipse.

Methods

Participants. Twenty participants (1 left-handed; 3 women) with an average age of 32 years (SD = 11.4) voluntary took part in the experiment. None of these participants took part in Experiments 1 & 2.

Stimuli. The visual stimuli were white spotlights displayed on a black background moving on elliptic paths of different sizes and with different periods according to the dynamic model defined in equation (1). As in Experiment 1, the elliptic paths were rotated counterclockwise by 45°. Three periods of the spotlight motion (T_1 = 1.2s, T_2 = 1.5s, T_3 = 1.8s) inducing different spotlight speeds were chosen.

Task. The adjustment protocol and the task were the same as in Experiment 1. For each (size) x (period) pair, 11 repetitions were performed starting from 11 different initial eccentricity values equally distributed between 0 and 1. The experiment was composed of 99 trials, i.e. 3 (sizes) x 3 (periods) x {11 repetitions}, presented according to two pseudo-random series counterbalanced across the participants. For each participant, 99 final eccentricities were collected and the median was computed.

Apparatus. The apparatus was the same as in Experiment 1.

Experiment 4 – Auditory Output

Here, participants were submitted to auditory stimuli generated with the dynamic characteristics of the motor performances recorded in experiment 2 and were asked to modify this dynamic to evoke a friction sound that conveys the the most representative elliptic

movement exclusively from the auditory modality. By using monophonic sounds, only dynamic

information was transmitted to the participants, as opposed to the visual cases in which both

spatial and dynamic cues were contained in the stimuli. Hence, this experiment intended to

show whether geometric prototypes could emerge from the auditory stimulations, which would

signify that spatial information is not strictly needed to evoke a prototype.

Methods

Participants. Twenty participants (9 women) with an average age of 32.1 years (SD =

9.56) voluntary took part in the experiment.

Stimuli. Stimuli were monophonic synthetic friction sounds simulating the motion of a

pencil on a rough surface, e.g., a piece of paper. A physically based model which simulates the

physical sound source as the result of successive impacts of a plectrum, here a pencil nail, on

the asperities of a surface, was used (Conan et al., 2014). The surface roughness is modeled by

a noise reflecting the different heights of the surface asperities. Movements on this surface is

then simulated processing this noise according to the velocity profile of the movement: the

faster the movement the more impacts there are. From a signal processing point of view, such

an operation is equivalent to a low-pass filter on the noise with a central frequency directly

linked to the movement velocity. The filtered noise is finally convolved with an impulse

response simulating the resonance of an object such as a table. To control the synthesis model,

we used the 60 motions (3 recordings x 20 participants) recorded in the motor experiment

(Experiment 2).

Task. The participants were asked to modify the sound to evoke an elliptic motion for

which the trajectory was the most representative of an ellipse. They were implicitly adjusting

the delay between the recorded oscillators which implicitly modify the ellipse's roundness. For

each of the 60 movements to adjust, 4 periods of the initial recording were used to generate the

stimuli. The participants were informed when they reached limits, i.e. 0 or 1 eccentricity, and

the adjustment protocol was inspired on one proposed by the on proposed Carlyon and

colleagues (Carlyon et al., 2010). The eccentricity of the ellipse could be modified either with

a large or a small modification of the actual eccentricity by using top-down and left-right-

arrows respectively, by steps of .10/.3 and .05/.2 respectively. In order to avoid an experimental

bias, for each opposite key, e.g., left/right, the roundness was modified with a different step so

that participants could not count the number of taps to adjust the friction sound. The participants

were prompted to explore the whole range of possibilities with the large arrows and to refine

their adjustment with the smaller ones.

Apparatus. Sounds were presented through Sennheiser HD650 headphones and the

sample rate of the soundcard was 44100 Hz with 16-bit resolution. The friction sounds were

real-time synthesized with MATLAB software. The experiment was carried out in a quiet room.

The sound was modified by the participants using the keyboard of the computer.

Data analysis. For each participant, 60 eccentricities values were collected and their

median was computed to characterize the prototypical ellipse.

Results

The results first revealed that an elliptical prototype can be determined in each modality.

More strikingly, a coherence between the motor, the visual - static and dynamic - and the

auditory prototypes was observed (Non-parametric Friedman test with modality as a factor:

df=3; $\chi^2 = 1.26$; p=.73) (Figure 2). They all converge toward a common eccentricity, each one

is not significantly different from .91 (t-test vs. .91: all not significant, Bonferroni corrections,

for each experiment, *df*=19) (motor: Mdn=.89, iqr=.067 – auditory: Mdn=.88, iqr=.049 – visual

static: Mdn=.91, iqr=.062 – visual dynamic: Mdn=.91, iqr=.121).

Figure 2. Averaged eccentricities obtained from the four experiments. The boxplot represents

the median (dot), the 25th and 75th percentiles (the bottom and top edges of the box). The

whiskers (vertical dashed line) extend to the most extreme data points below 1.5 the

interquartile range.. The dashed line indicates the value .91 corresponding to the elliptic

movement attractor. These results reveal a coherent averaged eccentricity close to .91.

General Discussion

In this study, we aimed at investigating whether common prototype of elliptic shapes elicited

across modalities, especially from auditory stimuli, could be identified. We compared the

restituted geometry through different outputs (visual, motor and auditory) across a series of four

experiments. A common elliptic prototype characterized by an eccentricity of .91 was

uncovered, hence demonstrating the common encoding of this prototype.

This complements knowledge from previous studies on the existence of prototypical

geometric shapes (Rosch, 1973, 1975; Feldman, 2000; Kalénine et al., 2013). This is also in

line with those from Wamain et al. (2011), who highlighted that the ellipse drawn

spontaneously has a relative phase close to 45°, i.e. an eccentricity of .91, and with those from

pure motor experiments aiming at revealing the preferentially drawn ellipse (Dounskaia et al.,

2000; Sallagoïty et al., 2004; Danna et al., 2011) corresponding to stable states, so-called motor

attractors (Kelso, 1986) (cf. Figure 2). Interestingly, when superimposing the prototypical

ellipse obtained in the present study with the prototypical rectangle highlighted by Kalénine et

al. (2013), common proportions can be observed. The length to width ratio for prototypical

rectangles and the semi-major to semi-minor axis ratio for prototypical ellipses are both close

to 2.3, which corresponds to .9 in term of eccentricity.

Above all, these results suggest a common coding of prototypical shape geometry and

more generally further support the role of the sensorimotor loop on our perceptual processes

(O'Regan and Noë, 2001; Varela et al., 1992; O'Regan, 2011). Interestingly,

neuropsychological studies demonstrated that motor schemes are re-activated during perceptual

processes through different sensory modalities (Chao and Martin, 2000; Creem-Regehr and

Lee, 2005; Grafton et al., 1997; Grèzes and Decety, 2002; Kohler et al., 2002; Bangert et al.,

2006; Zatorre et al., 2007), and through motor imagery (for a review see Jeannerod, 1995 or

Grosprêtre, Ruffino and Lebon, 2015). Concerning handwriting, it has been shown that seeing

a letter activates the cortical processes involved when producing the corresponding script

(Longcamp et al., 2003; James and Gauthier, 2006; Longcamp et al., 2006). Similarly,

perceiving a geometric shape may share processes involved when we are drawing it. In

Experiment 4, an elliptic prototype that did not differ from the visual and motor outputs was

elicited from monophonic sounds that only carried dynamic cues. This salient result shows that

the elliptic prototype is not only geometric but also can be transmitted through a dynamic

dimension. Hence without rejecting the necessity of visual experience in the emergence of

prototypical shapes (Theurel et al., 2011; Kalénine et al., 2011), our data suggest that the

prototypical shape is encoded through a common process based on the underlying covariation

between biological kinematics and shape geometry which characterizes the corresponding

drawing movement (Lacquaniti et al., 1983) and its perception through several sensory channels

(Viviani et al., 1992; Viviani and Stucchi, 1989; Viviani et al., 1987; Thoret et al., 2014). This

unified percept (Hommel et al., 2001) can then be recalled even through the auditory modality,

which does not provide any spatial cues. Further experiments with other geometric shapes are

needed to precisely assess the central role of the sensorimotor loop in the emergence of

prototypical shape geometries.

Authors contributions

Conceived and designed the experiments: ET MA LB SY RKM. Performed the experiments:

ET. Analyzed the data: ET MA LB SY RKM. Contributed reagents/materials/analysis tools:

ET. Wrote the paper: ET MA LB SY RKM

Declaration of interests

The authors declare no competing interests.

Acknowledgments

This work was funded by the French National Research Agency (ANR) under the MetaSon:

Métaphores Sonores (Sound Metaphors) project (ANR-10-CORD-0003) in the CONTINT

2010 framework and the SoniMove Project (ANR-14-CE24-0018). E.T. was funded through

an ILCB/BLRI grant no. ANR-16-CONV-0002 (ILCB), ANR-11-LABX-0036 (BLRI) and the

Excellence Initiative of Aix-Marseille University (A*MIDEX). The authors would like to thank

Thomas Bordonné and Joris Agator for their help running the experiments.

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