PhysiCOOL: A generalized framework for model Calibration and Optimization Of modeLing projects

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Data availability: PhysiCOOL is available as a Python library distributed through PyPi. The source code is available on GitHub. All the examples presented here can be run online through interactive Jupyter Notebooks

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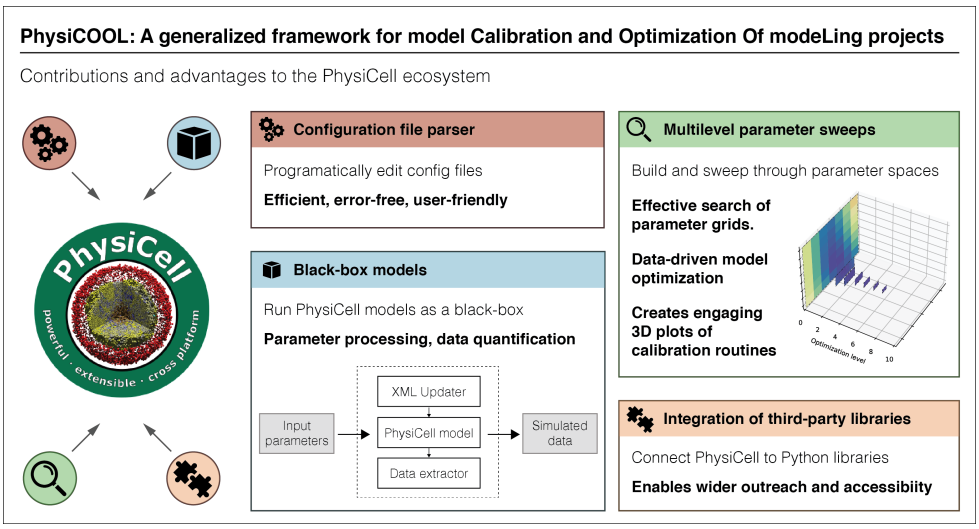
Abstract

In silico models of biological systems are usually very complex and rely on a large number of parameters describing physical and biological properties that require validation. As such, exploration of parameter space is an essential component of computational model development to fully characterize and validate simulation results. Experimental data may also be used to constrain parameter space (or enable model calibration) to enhance the biological relevance to model parameters. One widely used computational platform in the mathematical biology community is *PhysiCell* which provides a standardized approach to agent-based models of biological phenomena at different time and spatial scales. One limitation of *PhysiCell*, however, is that there has not been a generalized approach for parameter space exploration and calibration that can be run without high-performance computing access. Taking this into account, we present *PhysiCOOL*, an open-source Python library tailored to create standardized calibration and optimization routines of *PhysiCell* models.

Graphical abstract



Introduction

Mathematical biology is a field of study that aims to represent biological systems through the language of mathematics as a set of mathematical rules which can be used to test hypotheses and make predictions (Clermont and Zenker, 2015). There are several types of mathematical models that can be used to simulate biological systems at varying complexity levels. Agent-based models are one of the most popular implementations to develop models that consider the cellular and subcellular scales. Currently, multiple computational frameworks are available to facilitate the creation of agent-based models based on previously built templates, making mathematical biology more accessible to researchers from different backgrounds (Metzcar et al., 2019). Among these platforms, *PhysiCell* (Ghaffarizadeh et al., 2018) is an open-source hybrid framework that is able to simulate cells as discrete agents and model the reaction-diffusion dynamics of the substances present in the surrounding microenvironment through a continuous approach. Furthermore, recent add-ons have been developed to introduce new biological processes into the *PhysiCell* ecosystem (Letort et al., 2018; Bergman et al., 2022; Gonçalves and Garcia-Aznar, 2021).

Despite the recent advances in the development of additional *PhysiCell* plugins, the new modules are mostly centred around model extensions. Nevertheless, model exploration can be as important as model development to validate results and evaluate whether the model predictions about the underlying biological mechanisms are plausible (Hasenauer et al., 2015). Furthermore, experimental data could be used to provide biological and/or physical constraints on model parameters to validate whether the model captures the range of expected biological behaviors (Kazerouni et al., 2020), they can be used in computational biology to understand which model parameters maximize the similarity between the model results and a target data set, for example experimentally measured data. Subsequently, model developers may take these optimal solutions into account to identify which biological mechanisms captured by the computational model may explain the experimental data.

We highlight that previous works have developed model exploration routines with *PhysiCell* (Duggan, Metzcar, and Macklin, 2021; Ozik et al., 2018), but these were specifically designed for high-performance computing (HPC) and distributed systems. Hence, currently, general *PhysiCell* users without access to such resources, or whose needs do not require them, must develop their own scripts to process simulation results and perform model exploration studies. As well as introducing a barrier to scientific progress depending on the researchers' programming knowledge level and computing resources, bespoke HPC work flows lack standardization that may enable a widespread use in the mathematical biology community (Banga, 2008).

Taking into account that there is still a need in the *PhysiCell* community for a standardized tool that implements calibration and optimization routines, we present *PhysiCOOL*, a generalized framework for model calibration and optimization of modeling projects written in *PhysiCell*. *PhysiCOOL* aims to be model agnostic, in the sense that models are treated as a black-box that can be executed through Python, making it suitable to several kinds of biological problems. Moreover, our library includes a built-in multilevel optimization routine for parameter estimation that is constrained by target output (experimental or otherwise). We also provide two practical examples of how *PhysiCOOL* can be used, showcasing *PhysiCOOL*'s optimization routine at two distinct complexity levels. Furthermore, we show how *PhysiCOOL* black-boxes can be used to couple *PhysiCell* with other publicly-available Python libraries for model optimization.

Implementation

PhysiCOOL is a Python library that requires Python 3.8 or higher. This package was created to work specifically with *PhysiCell* models and it fully supports *PhysiCell* v.1.10.2 and lower, and has partial support for *PhysiCell* v1.10.3 and higher. Furthermore, *PhysiCOOL* has been tested extensively and

includes several unit tests to assure that its modules are working as expected and that it can be used in different platforms.

Configuration file parser

As for many several computational modelling frameworks, *PhysiCell* models are initialized with values stored in a text-based configuration file, namely an Extensible Markup Language (XML) file (Ghaffarizadeh et al., 2018). Thus, in parameter sweeps and sensitivity analysis studies it is necessary to open these files and modify the parameter values to be studied every time a new simulation is run. This process can be done manually, either by editing the XML file directly or using GUI tools such as *xml2jupyter* (Heiland et al., 2019). However, it becomes unfeasible to repeat this action several times in large scale studies. Henceforth, it is crucial to automate this process to run optimization and calibration workflows. Although it is possible to create Python scripts that will edit these files automatically with a standard module such as *ElementTree* (*Xml.etree.ElementTree - the elementtree XML API* n.d.), doing so requires users to identify the values to be updated with long strings that reflect the structure of the XML file, as shown in the code snippet below.

```python
from xml.etree import ElementTree

# Read cell data
file_path = "config/PhysiCell_settings.xml"
tree = ElementTree.parse(file_path)

# Define where to find the motility parameters
stem = "cell_definitions/cell_definition[@name='default']/phenotype/motility"
# Define the name and value of the parameter to be updated
key = "migration_bias"
value = 0.9
# Update the migration_bias value (no validation)
tree.find(f"{stem}/{key}").text = str(value)
tree.write(file_path)
```

Here, we aimed to develop a Python class that enables users to read the data from these configuration files in a more efficient manner, making this process less prone to errors. We implemented a *ConfigurationFileParser* class that reads the data from the configuration file into custom Python objects that follow the expected structure and data requirements defined in the XML file. A more detailed description of this implementation is presented in the documentation. Variable types and numerical constraints are validated when new instances of these data classes are created and when their values are updated. To achieve this, we implemented our classes using *Pydantic* (Colvin, n.d.) which improves data validation in Python. An example of how the task described in the code snippet presented previously may be implemented in a more user-friendly way with *PhysiCOOL* can be found below.

```python
from physicool.config import ConfigFileParser

# Read cell data into custom Python objects
file_path = "config/PhysiCell_settings.xml"
parser = ConfigFileParser(file_path)
cell_data = parser.read_cell_data(name="default")

# Update the migration_bias value (values will be validated before writing)
cell_data.motility.migration_bias = 0.9
```

```
parser.write_cell_params(cell_data)
```

Black-box models

In complex and large computational models, it may be challenging or even impossible to estimate the model outputs analytically. Consequently, it is common to conduct calibration and optimization studies by running several simulations and performing sensitivity analysis studies to identify how model outputs change in response to different input parameter values. This process is recognized as simulation-based optimization or black-box optimization (Alarie et al., 2021). *PhysiCell* models are written in C++ and should be compiled to produce an executable file that can be run to produce simulation results. In order to test and characterize the response of these models, it is generally necessary to conduct three tasks:

1. Update the *PhysiCell* configuration file with input parameters values;
2. Run the *PhysiCell* model;
3. Read the model outputs and compute a desired output metric.

These tasks can be performed manually. Nonetheless, it is not feasible or productive to do so in large computational studies, specifically when trying to characterize the model's response to a large number of input parameter values that can be inside a large range and require multiple simulation runs. Hence, *PhysiCOOL* allows users to create black-box models using the *PhysiCellBlackBox* class and automatically perform the aforementioned tasks through Python.

These black-box models are modular in the sense that the users can select what functions to use to update the configuration file (i) and to process the results (iii). For instance, users can decide to change the cells' motility parameters and evaluate the effect on the distance traveled by cells over time. Alternatively, the cell cycling rates could be varied to analyze the evolution of the number of cells. Furthermore, it is not essential that both (i) and (iii) are defined in the black-box. In fact, users can also create black-box models composed only of the *PhysiCell* executable and use our approach to run multiple simulation replicates.

PhysiCOOL offers some built-in data quantification methods that can be used to extract and process data in step (iii). For example, functions are provided to obtain the final number of cells in a simulation, the final coordinates of the cells and the concentration of a given substance over the simulation domain. Furthermore, these methods can be employed by users to process simulation results and generate 2D and 3D plots of the cells and the microenvironment.

Multilevel parameter sweeps

Parameter optimization studies require the definition of a search space, which defines the range of the parameter values that will be studied. There are multiple approaches to defining this space and how to explore it. For example, random search algorithms can be employed to randomly sampling points within a defined bounded parameter space. Alternatively, a grid search, while a more computationally expensive option, systematically samples every point within a defined parameter grid space providing a more comprehensive overview of the model's response than that offered by random search.

PhysiCOOL implements a multilevel parameter sweep class (*MultiLevelSweep*) that is aimed at identifying the parameters that best fit a target data set through a grid search. In this example, the parameter sweep considers two *PhysiCell* parameters for which the user should provide initial values. At each level, *MultiLevelSweep* creates a search grid based on these two values, the number of points per direction and the percentage per direction. These values should be configured by the user.

The results for each simulation are compared to the target data and the error between both datasets is computed and stored. At the end of the level, the parameters that provided the minimum error value are selected as the center of the parameter exploration grid for the next level

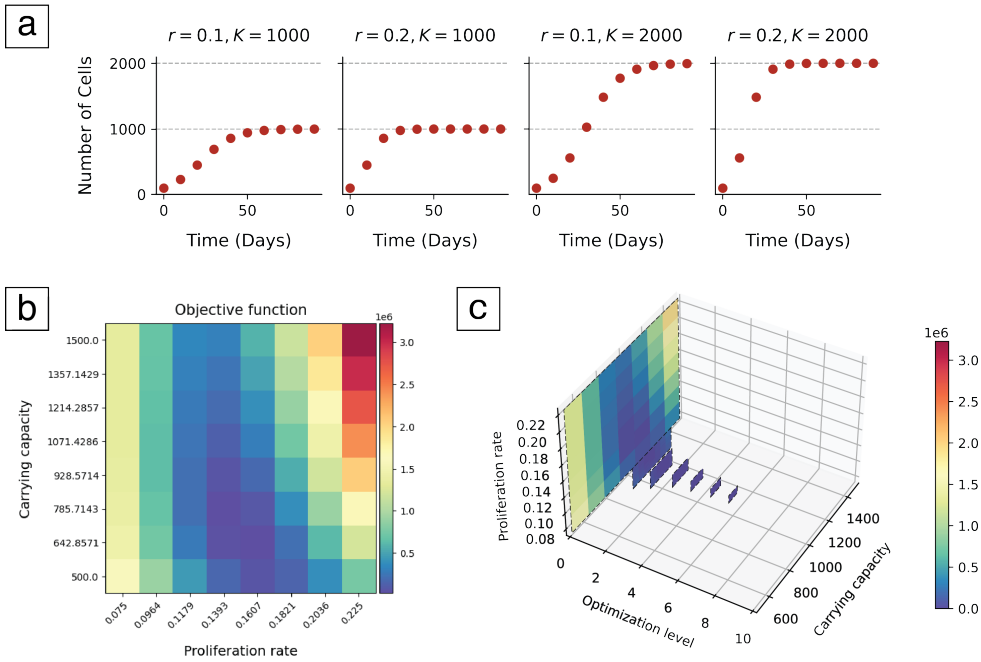


Figure 1. Model and optimization results for the logistic growth example. (a) Growth curves obtained for different parameter sets (carrying capacity, K, and proliferation rate, r). (b) Optimization results after the completion of the first level of the multilevel optimization algorithm. The heatmap shows the difference, as given by the summed squared error, between the target data and the data produced by each cell's input parameters. (c) Optimization results after 7 levels of the multilevel optimization algorithm. Results converged to the parameters that originated the target data.

and the parameter bounds are updated accordingly. The number of levels can be defined by the user.

Examples

Simple model of logistic growth

The first example was implemented to calibrate two parameters of a simple model of logistic growth based on some target data that defines a generated growth curve. Therefore, it serves as an introduction to this *PhysiCOOL* feature, as users are able to fully understand the behaviour of this simple model. We modelled the number of agents in a population, N, over a period of time t through a logistic function given by Eq 1:

$$N(t) = \frac{K N_0}{N_0 + (K - N_0)\exp(-rt)} \tag{1}$$

where K represents the carrying capacity, i.e., the maximum population size, N_0 represents the number of initial agents and r is the proliferation rate. In this study, we fixed the initial number of agents and evaluated how the carrying capacity and the proliferation rate regulated the growth curve of a population. An example of two growth curves obtained for different model parameters is shown in Fig 1(a).

We generated some target data using this model ($K = 1000, r = 0.1$) and, subsequently, we used *PhysiCOOL*'s multilevel sweep algorithm to evaluate if we could estimate these model parameters based on their resulting growth curve. To do so, we first created a search grid based on a set of user-defined values: an initial estimate for both parameters, the number of points to search in each direction of the search grid, the percentage to vary in each direction and the number of levels to search. These values can be found in Table 1.

Table 1. Parameter values used in the multilevel optimization examples.

Example	Initial point	Points	%	Levels	Estimated point	Target point
Logistic growth	[0.15, 1000.0]	8	50 %	7	[0.10, 994.7]	[0.10, 1000.0]
Chemotaxis	[3.0, 0.75]	6	50 %	4	[1.65, 0.85]	[2.0, 0.9]

Fig 1(b) shows the error between the target and simulated datasets for every cell of the parameter space after one level of the multilevel search. At this point, a new point estimate was calculated based on the parameter values that minimized the error between the two datasets. Likewise, the parameter space was adjusted to the area of interest and the process was repeated in the new parameter grid. This process was repeated for each level of the search and the results are shown in Fig 1(c).

PhysiCell chemotaxis model

The second example can be classified as a more complex problem, since it was developed to calibrate a chemotaxis model written in *PhysiCell*. In this modelling framework, the cells' chemotactic response, i.e., the ability to migrate along a substance gradient, is dictated by a bias value defined between 0 and 1 (Ghaffarizadeh et al., 2018). When cells have a migration bias of 0, they move according to a random walk. Conversely, if the value is set to 1, cells follow the substance gradient in a deterministic manner. Therefore, we developed a model to estimate the migration bias of the cells in response to an oxygen gradient, as well as their speed, based on their travelled distances.

We implemented a 2D simulation with an oxygen source on one of the domain walls, as defined by the model's boundary conditions, and a group of cells placed on the opposite wall, as shown in Fig 2(a). We expected that the cells' final position would be modulated by the cells' sensitivity to the oxygen chemotactic gradient. On the one hand, if a cell population had low sensitivity and, thus, moved randomly, they would likely remain close to their initial position as they would move around without following any specific direction. On the other hand, cells that followed oxygen would move towards the opposite wall, as seen in panel 2(b).

We generated some target data by running a simulation with a migration bias of 0.9 and a speed value of 2.0 μm/min and storing the final y coordinates of the cells. Subsequently, we ran our multilevel sweep pipeline to evaluate whether we could estimate the parameter values that originated this data with a set of initial points different from the target parameter values. The results for this study are shown in Fig 2(c).

Connecting to third-party libraries

Given that *PhysiCOOL* makes it possible for users to turn their *PhysiCell* models into black-box models that receive some input parameters and return an output metric, it is straightforward to couple them with third-party Python libraries that accept this kind of models. For example, *psweep* (Schmerler, 2022) is a Python library developed to run parameter studies that saves the input parameters values and the returned output metrics into a database. Users must define a set of parameters and, for each of the defined values, *psweep* will (i) run a given user-defined function that takes these parameters as input, and (ii) save the input and output values returned by this function into the database. Therefore, a *PhysiCOOL* black-box could seamlessly be integrated into step (i).

In addition, more sophisticated libraries could be considered to perform advanced optimization studies such as Approximate Bayesian Computation (ABC) and Bayesian Optimization for Likelihood-Free Inference (BOLFI) Lintusaari et al., 2018. Henceforth, although *PhysiCOOL* offers built-in optimization routines, it can be used in a modular way to take advantage of other libraries that may be more appropriate to a certain study or type of research, without the need to implement these optimization algorithms from scratch.

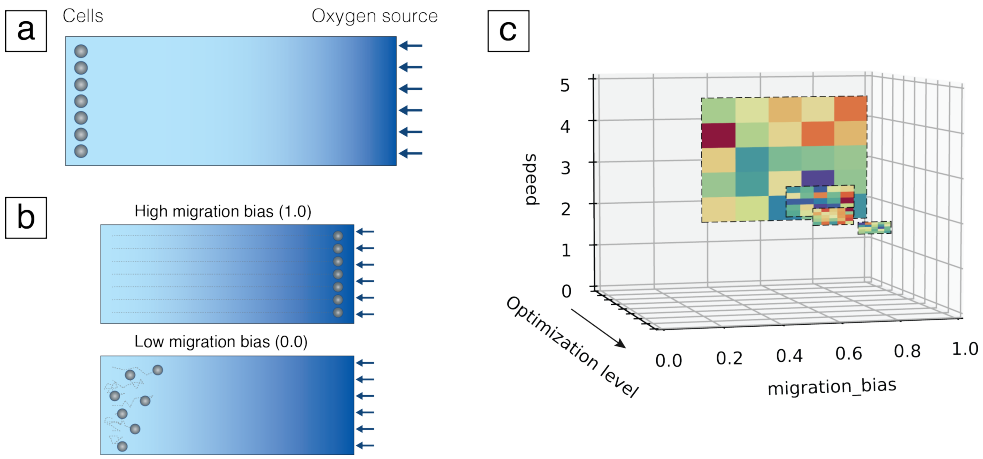


Figure 2. Model and optimization results for the chemotaxis example. (a) Initial model configuration design. Cells (represented as grey circles) were placed close to a domain wall and an oxygen source (represented by the blue arrows) was simulated on the opposite wall, creating a chemotactic gradient that cells could follow. This gradient is illustrated by the colour gradient shown in the figure. (b) Expected model results for cells with different migration bias values. High migration bias populations were expected to migrate in a deterministic manner and follow the oxygen gradient, crossing the domain and arriving at the opposite wall, as shown by their trajectories, shown as grey dashed lines. On the other hand, cells with low migration bias were expected to move randomly and, thus, present low net displacement values. (c) Optimization results after 4 levels of the multilevel optimization algorithm. Results converged to the parameters that originated the target data. The colormap was updated for each level, describing the minimum and maximum error values at the current level.

Future directions

At its current state of development, we believe that *PhysiCOOL* will already improve *PhysiCell*'s accessibility as it provides an intuitive interface to run studies in Python, which is more popular among biology researchers than C++, in which *PhysiCell* was originally written. Additionally, this standardized approach provides a straightforward workflow for integrating target data (defined from simulations or biological observations) to constrain parameter space for agent-based models. In the future, new features can be added to *PhysiCOOL*, such as the ability to generate non-linear parameter spaces and employ alternative optimization algorithms. Although future iterations of this library may include different optimization approaches, its modular design assures that advanced users are still able to build pipelines that suit their needs.

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