Fractions strategy differences in those born extremely preterm

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Abstract

Introduction: For those with weak cognitive skills, certain mathematical problem-solving strategies may be more difficult than others. Tailored mathematical instruction that recognizes cognitive load and incorporates ways to reduce this may help to overcome mathematical difficulties. To investigate the effects of different strategies and cognitive load we explored brain

47 hemodynamic responses associated with the use of different strategies to solve subtraction of
48 fractions. We focused on those born extremely preterm (EPT; <28 weeks' gestation) as they are
49 known to have cognitive challenges and struggle with mathematics in particular. We also included
50 a group of full-term (FT) peers for comparison.
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Methods: Functional MRI was acquired while the participants mentally solved fraction equations
using either an improper fractions strategy, where whole numbers are converted to improper
fractions before solving, or a mixed fractions strategy, where computations are carried out
separately for the whole numbers and fraction components. Different fraction item types were
given, which affected respective required cognitive loads per strategy. Diffusion and T1-weighted
structural images were also acquired. All imaging modalities were compared between the two
groups.
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Results: The EPT and FT groups differed in terms of task-related hemodynamic responses,
regional volumes, and white matter connectivity. Functional group differences varied with strategy
and item type. These differences were greatest when the mixed fractions strategy was prompted
for an item type that required relatively greater cognitive load and involved borrowing. Other
findings showed reduced white and grey matter volume and reduced white matter connectivity in
widespread areas in the EPT group compared to the FT group.
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67 Conclusion: Changes in the brain related to preterm birth are complex. The understanding of
68 function and structure presented here may help inform pedagogical practices by allowing for
69 tailoring of mathematical education through identifying suitable strategy adoption that depends on
70 problem type, to circumvent weaknesses in cognitive skills.
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1.0 Introduction

Extremely preterm (EPT) birth is defined as birth before 28 completed weeks of gestation. The
incidence of preterm birth (gestational age (GA) < 37 weeks) in the US is about one in ten births
[1] and globally, 2-5 births in 1000 are EPT [2]. Survival rates among those born EPT are around
33% at 23 weeks' GA, 65% at 24 weeks, 81% at 25 weeks and 94% at 27 weeks [3]. Children born
EPT often have deficits in working memory, executive function, inhibition, and processing speed
when compared to full-term (FT) control subjects [4, 5]. Children born EPT are known to have
cognitive difficulties through adolescence and by early adulthood they are likely to have lower IQ
and impaired visuomotor, prospective memory, language and executive functioning skills [6].
Therefore, EPT individuals are vulnerable to experience impairments in a range of neurocognitive
skills that are crucial for learning, problem solving and effective communication, which are likely
to exert a negative impact on their overall academic achievement (with up to 50% needing extra
educational help at mainstream schools) [7]. In particular, EPT individuals experience
mathematics learning difficulties to a greater extent than other academic and cognitive deficits [7].
Mathematics difficulties have been associated with poor performance on working memory and
visuo-spatial processing tasks, rather than impairments in numerical representation [4], suggesting
that the nature of mathematics difficulties of preterm children is different from that of individuals
with developmental dyscalculia. In middle childhood, among those born EPT, 44% had serious
difficulty with mathematics compared to 1.3% of FT peers. In contrast, 30% of EPT children had
serious difficulty with reading compared to 2% of FT children [7].
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In FT individuals, multiple brain regions have been implicated in the neurobiology of computation,
including in the frontal, parietal, and temporal cortices, as well as subcortically, in the thalamus,
basal ganglia, and hippocampus [8, 9]. There are much data supporting the intraparietal sulcus
(IPS) in the inferolateral parietal lobe as the primary locus of numerical processing, although IPS
lesions have been associated with a variety of other deficits of motor, sensory, and associative
function, suggesting that the information processing it supports is critical to mathematical
reasoning but not necessarily specific [10]. Nevertheless, the IPS is considered as part of a "core"
visual-spatial number system, along with the fusiform gyrus [10, 11]. Research studies have
investigated white matter associated with mathematics in typically developing children and adults.
Tract-specific white matter microstructural characteristics, such as fractional anisotropy (FA),
have been associated with mathematical skill. These tracks are the superior longitudinal fasciculus
(connecting fronto-parietal cortices) [12-14], inferior longitudinal fasciculus (fronto-occipito-
temporal areas) [12, 15] and arcurate fasciculus (inferior fronto-occipito-temporal, connecting
Wernicke's and Broca's areas) [16]. The processing and maintenance of both visual and verbal
information is also often central to mathematical performance [17-19].
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Few functional imaging studies have investigated the neural correlates associated with performing
mathematics in preterm-born individuals. Functional magnetic resonance imaging (fMRI) studies,
involving tasks such as the Stroop and number estimation, have shown an association between
longer gestation and more pronounced hemodynamic responses in parietal brain regions. Shorter
GA has also been associated with more prefrontal cortex activity in young adults born < 37 weeks'
gestation when completing a magnitude comparison task [20], in 6- to 7-year-old children born
between 27-32 weeks with a numerical distance effect task [21, 22] and 11-year-old youth born <
28 weeks' gestation with a working memory/selective attention task [23]. As FT children mature,
areas of the brain associated with performing mathematics change from mostly frontal to less
frontal and more parietal areas, possibly due to procedural changes in how mathematics is
performed [24, 25]. Individuals born EPT may thus have a more 'immature' mathematical network
[20].
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A study of functional connectivity and performance on mathematical tests showed patterns of
association unique to preterm individuals born between 25-36 weeks' gestation. Functional
connectivity derived from resting state fMRI in adulthood (26 years old) showed associations with
mathematical ability in childhood in bilateral fronto-parietal networks in preterm adults that were
different to FT adults [26]. Specifically, in the right fronto-parietal network, math abilities were
correlated with left lateral occipital/middle temporal cortex intrinsic functional connectivity in
preterm but not FT individuals. In the left fronto-parietal network a similar pattern was observed,
with math abilities being correlated with right angular gyrus/middle temporal cortex intrinsic
functional connectivity in preterm but not FT individuals. Also, mathematical abilities recorded in
childhood (8 years old) were more positively associated with adult IQ for preterm than for FT
individuals.
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134 A study of mathematics and regional brain volumes found an association between reduced grey
135 matter volume in left parietal lobe and poor mathematics performance in EPT teenagers [27].
136 Diffusion weighted imaging studies assessing white matter characteristics have shown that EPT
137 infants scanned at 38 weeks' post-conceptual age have alterations in white matter microstructure
138 (reduced FA and increased radial diffusivity) in widespread areas associated with early

myelination (such as sensorimotor areas) [28] and frontal and occipital areas [29] compared with FT babies. In older EPT children, 9-16 years of age, lower FA values in the corpus callosum, forceps minor and major, cingulate gyrus, inferior fronto-occipital fasciculus, inferior and superior longitudinal fasciculi and corticospinal tract have been associated with impaired executive functioning [30]. In EPT infants scanned between birth and 4 years of age, changes in mean diffusivity values in the internal and external capsules have been associated with intelligence and language [31]. The long-range connections between frontal, temporal and parietal lobes serve to integrate and control complex brain processes involved in cognition and skills. The authors are not aware of any research investigating mathematics and white matter connectivity in individuals who were born EPT. In summary, the EPT population has a multitude of structural and functional brain changes that affect both their ability to do mathematics and domain-general functions such as attention and working memory.

Here, we investigate functional and structural brain differences associated with mathematical problem-solving in adolescents born EPT and FT control participants. We focus on fraction problem-solving, as this mathematics domain poses demands on multiple computational abilities, requires more advanced skills than arithmetic problem-solving, and is a key mathematical subject area. Another benefit of focusing on fractions is that the same fraction problems can be solved using either an improper fractions or mixed fractions strategy approach. Depending on the item, the two strategies can impose different cognitive loads (e.g., more or fewer mental operations, or interim steps requiring working memory for problem-solving). We illustrate this further below.

The present study represents an initial effort to identify individual differences in brain structure and function as a means for developing more targeted approaches to mathematical instruction. We focused on adolescents as they adapt well as an age group to fMRI experimentation and are mathematically advanced enough to have already had instruction in solving fraction problems. fMRI was used to examine hemodynamic response differences between adolescents born EPT and FT control subjects during tasks that required different strategies of fraction problem-solving. The goal was to investigate group differences in hemodynamic response patterns during processing of same types of test items invoking different strategies that varied in cognitive load. We also aimed to explore between group differences in brain structure. We hypothesized that there would be differences between FT and EPT groups in hemodynamic response patterns, particularly for the math problem and strategy combinations that require relatively higher cognitive loads. Discovery of group differences could suggest the need for stronger emphasis on flexible strategy adoption for adolescents born EPT that would allow for reductions in cognitive load.

2.0 Methods

2.1 Participants

The participants made two visits to University Hospitals Cleveland Medical Center (UHCMC) on separate days. The first visit was to undertake neuropsychological testing and training in fractions, (lasting 3 - 4 hours). The second visit was to the MRI department, lasting around 2 hours. Duration between visits ranged from 7 to 364 days with the median duration being 22 days (SD 81.2 days). In total 50 subjects attended for neuropsychological training and a subset was selected for MRI based on: 1) the subject's willingness to participate in an MRI, 2) the lack of physical

contraindications to MRI (e.g., claustrophobia, the presence of cardiac pacemakers or other
medical devices, metallic fragments such as shrapnel, etc.), and 3) competency in doing fractions
without pen and paper. A total of 30 subjects underwent MRI, including 14 EPT adolescents, all
with either GA <28 weeks and/or birth weight < 1000 g. EPT participants were 15-17 years of age
and included 12 females. The 16 FT adolescences were aged 15-17 years old and included 8 males.
The FT youth were recruited from the same regular classrooms as the children born extremely
preterm and were thus representative of children attending regular education classes. Eleven EPT
and 15 FT participants were right-handed, 2 EPT and 1 FT participants were left-handed and 1
EPT participant was ambidextrous. Participant characteristics are summarized in Table 1.
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195 The Institutional Review Board office at UHCMC granted ethics approval prior to the study. The
196 ethical considerations complied with the Declaration of Helsinki for human subject research.
197 Subjects and their parents gave informed consent prior to taking part.
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199 2.2 Neuropsychological testing
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Neuropsychological testing was performed using the NIH toolbox -
https://www.healthmeasures.net/explore-measurement-systems/nih-toolbox. It includes a range of
tests to assess cognition, emotion, sensory and motor function. The cognition tests assessed
executive function, working memory, verbal fluency, attention, processing speed and episodic
memory. In the interests of brevity, the reader is directed to [32] for full details of the tests. Test
score summaries of working memory as assessed by WRAML2 (Wide Range Assessment of
Memory and Learning, second edition), by birth group, are also reported in Table 1.
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209 2.3 Fractions strategies
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We have developed a set of problems assessing subtraction of mixed fractions for administration
in the scanner that are similar to a diagnostic subtraction of mixed fractions test developed by K.
Tatsuoka [33, 34]. This test and its item-skill specifications have been widely studied and
validated, with data available at the Royal Statistical Society website (https://rss.org.uk) [35]. The
problems are solved using mental arithmetic. Each item can be solved with one of two strategies,
with the required strategy prompted during the fMRI session. Item types are described as:
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$$\text{Item Type I:} \quad X\left(\frac{x}{z}\right) - Y\left(\frac{y}{z}\right), \quad where \; x > y \; and \; X > Y \tag{Eq. 1}$$

$$\text{Item Type II:} \quad X\left(\frac{x}{z}\right) - \left(\frac{y}{z}\right), \quad where \; y > x \tag{Eq. 2}$$

218 Solving strategies include "mixed" and "improper" methods. Consider $1\frac{3}{4} - \frac{1}{4}$, an Item Type I
219 problem. The "mixed" method involves separate computations on whole number and fraction
220 components, e.g.,

$$1\frac{3}{4} - \frac{1}{4} = (1 - 0) + \left(\frac{3}{4} - \frac{1}{4}\right) = 1\frac{2}{4} \tag{Eq. 3}$$

223 while the "improper" strategy involves solving using improper fractions by converting a whole
224 number to fraction, e.g.,

$$225 \qquad 1\frac{3}{4} - \frac{1}{4} = \left(\frac{4}{4} + \frac{3}{4}\right) - \frac{1}{4} = \frac{7}{4} - \frac{1}{4} = \frac{6}{4}$$

$$\text{(Eq. 4)}$$

226   (Eq. 4)

Note that in solving an item of this type, the improper strategy requires higher cognitive load,
specifically in working memory. However, the relative cognitive demands or difficulty levels
imposed by the two strategies (easier vs. harder) vary by the type of problem. For an Item Type I
problem, the mixed method requires fewer steps, and thus a lower cognitive load, than does the
improper fraction method. However, for an Item Type II problem, the improper fraction approach
is more efficient than the mixed fraction method. A problem of this type would be: $2\frac{1}{4} - 1\frac{3}{4}$,
which is an Item Type II.

$$2\frac{1}{4} - 1\frac{3}{4} = (2-1) + \left(\frac{1}{4} + \frac{4}{4}\right) - 1\frac{3}{4} = 1\frac{5}{4} - 1\frac{3}{4} = (1-1) + \left(\frac{5}{4} - \frac{3}{4}\right) = \frac{2}{4} \qquad \text{(Eq. 5)}$$

$$2\frac{1}{4} - 1\frac{3}{4} = \left(\frac{1}{4} + \frac{8}{4}\right) - \left(\frac{3}{4} + \frac{4}{4}\right) = \frac{9}{4} - \frac{7}{4} = \frac{2}{4} \qquad \text{(Eq. 6)}$$

In this problem the mixed fractions strategy requires borrowing from a whole number, i.e. 1 or $\frac{4}{4}$
from the 2 on the left-hand side of the problem, yielding $1\frac{5}{4}$. In this case, and more generally for
items of Type II, converting both numbers to improper fractions before subtracting places similar
or even fewer demands on working memory. This can be made more explicit by listing out the
computations and steps and numbers that must be held in memory during the problem-solving
process. In general, cognitive load varies depending on strategy and item type. Depending on item
type, one strategy can impose a higher demand on working memory than the other. See Figure 1.

For the two item types that we considered for fMRI, there are thus harder and easier difficulty
levels for each of the two strategies. For the items considered, when one strategy is at the harder
level, the other strategy is at the easier level, as illustrated above. This suggests that more difficult
levels of specific strategies can be avoided through flexibility in adopting alternative strategies.
The present study examines associations of different problem-solving strategies that have been
taught and practiced to mastery by the participants with patterns of neural activation on fMRI.

2.4 Fraction Strategy Training

Training in subtraction of mixed fractions was carried out as part of the initial visit, through a
multi-step program that began with review of basic concepts followed by (1) instruction and
practice in converting whole and mixed numbers to proper and improper fractions, subtraction of
simple proper fractions, and written subtraction problems, using each of the two strategies in order
of increasing difficulty; 2) practice and review in mental problem solving, using two strategies (the
"improper fraction" and "mixed fraction" approach) for solving problems that are easier or harder
depending on whether the items are Type I or Type II ; and 3) computer administration of similar
sets of problems to prepare participants to solve fraction problems in the same format that was
used for subsequent in-scanner presentations. During training with written problems, the examiner
taught each of the two problem solving strategies explicitly and had the subject verbalize the
strategy after solving each problem. Practice in doing the problems mentally also included the

requirement that subjects verbalize the strategy used after giving their answers. For the computer
administrations, subjects were first presented with a problem on the screen and asked to provide
the answer verbally as soon as they could while pressing the space bar to indicate their time to
solve the problem. They were then asked to verbalize the strategy used to solve that problem.
Problems were limited to those with common denominators and subtraction of relatively simple
fractions to ensure that subjects could be taught the problem-solving strategies to a high level of
accuracy and that in-scanner mental calculations would be feasible. The majority of subjects from
both the EPT and FT groups were able to achieve a high level of accuracy on the computer
administration, median values for EPT - 32.5 out of 35 (IQR 4.5) and FT - 34 out of 35 (IQR 1.0).
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275 2.5 fMRI Stimulus protocols
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277 Respective blocks of items requiring the two fraction solving strategies were presented separately
278 in the scanner. An example sequence is shown in Figure 2. Which strategy to use was prompted
279 through instructions printed on a screen at the beginning of each scan and with the presentation of
280 each equation. Colored Xs were used to prompt the format of the expected solution, e.g.:
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$$1\frac{3}{4} - \frac{1}{4} = \frac{X}{X} \quad or \quad 1\frac{3}{4} - \frac{1}{4} = X\frac{X}{X}$$

283
Correct strategy adoption was validated by high correctness rates. See Figure 2 for further details.
For each strategy, Item Types I and II were presented within each scan in an interleaved fashion.
For the improper fractions strategy, the Item Type II involves 3 steps, while Item Type I involves
5 steps. For mixed fractions, Item Type I is only 2 steps, while Item Type II is 4 steps. A fraction
was displayed on the screen for 12-18 seconds, depending on difficulty level. Difficulty was
determined by the cognitive load/number of steps required to solve the equation. In the response
phase of solving an item, another screen was then displayed with two possible answers to choose
from. The answers were displayed in the format related to the strategy in use, and displayed for
only 6 seconds. There was thus insufficient time for subjects to convert their answer if they had
used the incorrect strategy, which encouraged correct adoption. Subjects indicated their answer
choice by pressing a button on a response box held in the right hand. Finally, the presentation of
each fraction item was separated by a 'rest' condition. A black dot was displayed in the center of
the screen and subjects were instructed before the scan to look at the dot for the duration.
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The visual stimulus was presented using an in-house custom written program that was developed
using Python (Python Software Foundation, https://www.python.org/) and libraries from
PsychoPy - an open source visual presentation program [36-38]. The Cedrus Lumina controller
was used to integrate all the signals. The program connected to the controller box which received
the subject responses as well as a trigger pulse from the MRI scanner. The trigger pulse was
outputted every scan (every 3 seconds) and was used to synchronize the stimulus to the scan
acquisition. On the experimenter's computer screen was displayed a Supervisor Window that
tracked the current block number being presented, how many remaining blocks there were and
when the subject responded. The software has been made available from the Bitbucket repository:
https://bitbucket.org//tatsuoka-lab/fmri-presentation.
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309 2.6 MR Imaging Parameters
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Scans were acquired using a Philips Ingenuity 3T PET/MR scanner at UHCMC. Subjects were positioned supine on the scanner bed. The head was fixed in position using inflatable pads and an 8-channel head coil was used for data acquisition. Echo planar imaging scans were acquired with the following parameters: TR = 3.0 s, TE = 35 ms, voxel resolution = 1.797 x 1.797 x 4 mm (matrix 128 x 128), 36 slices in total provided full brain coverage, and flip angle was 90°. A SENSE P reduction factor of 2 was implemented and scans were acquired in an ascending interleaved fashion. Two fMRI scan sessions were run, one for each fraction solving strategy. They consisted of 200 scans each. A high-resolution T1-weighted anatomical image was also acquired using a magnetic preparation gradient-echo sequence (3D IR TFE) with the parameters: TR = 7.5 ms, TE = 3.7 ms, voxel resolution = 1 x 1 x 1 mm, number of slices = 200 slices and flip angle = 8°. A 64-direction diffusion weighted image with a FOV of 224 x 224 producing a final in-plane resolution of 1.75 x 1.75 mm^2 and 2 mm slices. A TR of 7415 ms was used. Full-brain coverage was achieved with 60 slices. One B$_0$ image was acquired, and the b factor was 1000.

2.7 fMRI Individual-level Analysis

FSL FEAT [39] was used to perform motion correction, spatial smoothing and apply a high pass filter to preprocess the raw data. A rigid body transform with 6 degrees of freedom was used for motion correction. Spatial smoothing was performed with a full-width-at-half-maximum Gaussian kernel of 6 mm, a high pass temporal filter of 90 s was used. All scans were then co-registered to a standard space template (MNI) and an individual level general linear model (GLM) analysis was run. The fractions were presented in a block design and a hemodynamic response double gamma function was convolved with a boxcar function to model the expected signal. We were most interested in the neural correlates of calculation so only scans during the computation time were modelled as active, not the scans during the response phase. The scans related to the response phase recorded the process of reading the possible answers and indicating their choice via a button press. The allowed response duration was kept short to ensure that calculations could not continue into this phase. Recorded response times were related to the time taken by participants to indicate their choice, not the time to do the mental calculation. Response times were not included as regressors in the GLM.

Note, one EPT subject was unable to complete the fMRI tests and a technical issue prevented one FT subject from taking the fMRI tests, hence the fMRI data reported at both individual and group level contains 13 EPT and 15 FT subjects. However, structural data (DTI and T1 images) were obtained for all 30 subjects. Also note, due to the anatomical heterogeneity reported in EPT individuals, we considered the use of a custom structural brain template created from a group average instead of using the MNI standard template. There were differences in the size of the brain between the MNI and custom templates with the custom template being comparatively smaller (228,453 and 177,110 voxels respectively, custom template was 22 % smaller). The fMRI results were largely in the same anatomical locations. However, peak t-scores and total number of active voxels differed with the fraction solving strategy. The MNI template was kept through all analyses for ease of reporting and interpreting results, as well as minimizing the number of transformation steps. Also note, in the Supplement section S2, activation status of specific regions are compared by birth group.

2.8 fMRI Group Analysis

The statistical output from the individual analyses were used to perform the group level statistics using fixed effects modelling in a factorial design involving group and strategy/item type combination. Below, we focus on comparing birth group (EPT and FT) by strategy (mixed or improper), birth group by item type (Type I or Item Type II), and 3-way interaction effects. The latter consisted of within group comparisons of activations to Item Types I vs. II using the same strategy (mixed or improper), and of activations associated with the same item types (Types I and II) using different strategies. Note that strategy by item type interactions were purposely designed so that differences in difficulty levels associated with the two item types would depend on the strategy used to solve the problems. The inclusion of sex as a covariate was considered. However, given that the EPT group consisted of predominantly females (11 out of 13), the sex results were confounded with birth status and so are not reported. To reflect multiple hypotheses at least to some degree, a result was considered significant if the resulting p-value was < 0.001 which equates to a t-score > 3.1.

2.9 Linear SVM Classification

To further explore the activation differences between birth groups and strategy adoption, a linear support vector machine (SVM) analysis was performed. The aim was to determine if it was possible to systematically distinguish activation patterns in each of the item types in an automated way. Preprocessing of BOLD signal were performed using FEAT, as described above. Additional preprocessing steps via PyMVPA toolbox [40] included detrending, normalization, and ANOVA-based feature selection (using top 5% of active voxels) as described in [40]. Rest volumes were excluded from analysis. The linear SVM was implemented using a leave-one-out cross validation approach. For the group level analyses, a single subject's mean activation for all conditions related to a specific strategy type (or strategy-item type combination) was used in classification to perform a leave-one-(subject)-out cross validation. As a result, the SVM would be trained on all strategy conditions from n-1 subjects prior to testing on the subject left out. Overall classification accuracies were determined using the PyMVPA toolbox built-in statistics.

2.10 Volumetrics and DWI analysis

MRI-based volumetrics and DWI analyses are described in the Supplement sections S3 and S4. This includes group comparisons of regional volumes and white matter connectivity.

3.0   Results

3.1 Accuracy of responses by strategy/item type

We first establish the accuracy of the performance on the fraction subtraction problems. The accuracy rates by strategy, item type (difficulty level), and strategy/item type combination are given for both the FT and EPT groups in Table 2. Note that in general accuracy is quite high, which supports the effectiveness of the training protocol, and the correct adoption of prompted strategy per item. A Wilcoxon rank sum test was used to compare the differences in accuracy rate between groups for each strategy/item type combination. Within birth groups, item types for same strategy were compared, as well as strategies for a same item type. Most comparisons were not statistically

significant. Still, it was found that for both EPT and FT subjects, when using the mixed strategy, Item Type II (harder) problems had significantly lower accuracy rates compared to Item Type I ($p = 0.007$ and $p = 0.002$). Performance using different strategies on same item types were compared as well. For Item Type II, both EPT and FT had lower correctness rates ($p = 0.049$ and $p = 0.005$) for the mixed fractions strategy compared to improper fractions strategy. No significant difference was found for other item type and strategy combinations. When using the mixed strategy to solve Item Type II problems, EPT subjects had lower correctness rates compared to FT subjects (85.7 versus 71.4%, $p = 0.050$), though even the EPT had relatively high accuracy rates.

3.2 Main effects of strategy and their interaction with item type

The main effect of strategy was investigated. The data were modelled as task (Item Type I and II) versus rest and both EPT and FT groups were included. The improper fraction strategy was associated with hemodynamic response in the left superior and inferior frontal gyri, paracentral lobule, precuneus and middle temporal gyrus; and right cingulate gyrus. Modelling the mixed fractions strategy in a similar way revealed hemodynamic response in left medial frontal gyrus, inferior parietal lobule and thalamus; right superior parietal lobule, superior frontal gyrus, precuneus, precentral gyrus and caudate nucleus.

The interaction of item type and strategy was also investigated. Improper fractions strategy for Item Type II (easier to solve problems) was associated with hemodynamic response in left superior and medial frontal gyri, paracentral lobule and middle temporal gyrus. Item Type I problems solved by this strategy was associated with hemodynamic response in left superior frontal gyrus and right posterior cingulate. For the mixed fractions strategy, Item Type I (easier to solve problems) showed hemodynamic response in left medial frontal gyrus, insula and fusiform gyrus; right cingulate, superior frontal gyrus, precuneus, precentral gyrus and caudate; and bilateral lingual gyrus. Hemodynamic response associated with Item Type II of mixed fractions strategy were widespread and included in left medial frontal gyrus, lingual gyrus, inferior parietal lobule, cingulate, thalamus and caudate; right superior frontal gyrus, superior parietal lobule and precuneus; bilateral precentral gyrus and posterior cingulate gyrus.

A conjunction analysis for each strategy and item types shows that much of the functional activation that differs between item types appears around the edges of the overlapping clusters. Statistical contrasts of improper strategy Item Type I versus II and Item Type II versus I were not significant. The contrast of Item Type I versus II for mixed fractions strategy showed statistical differences in left paracentral lobule, insula and precentral gyrus; right lingual and postcentral gyri. The contrast of Item Type II versus I showed greater hemodynamic response mainly in left brain areas including the precuneus, middle frontal gyrus, precentral gyrus and bilateral cingulate gyrus.

3.3 Between birth group differences by strategy and difficulty level

Table 3 shows between group differences in hemodynamic response for the easy and hard levels for each fraction strategy.

3.3.1 Improper strategy. Comparison of the EPT vs FT groups on the less difficult items (Item Type II) for the improper strategy vs rest revealed greater hemodynamic response in right

precuneus in the EPT group compared to the FT group (contrast EPT vs FT). The FT group showed greater hemodynamic response in the left middle and superior frontal gyri, superior parietal lobule and right paracentral lobule (contrast FT vs EPT). For Item Type I (hard) vs rest, we observed no areas displaying greater hemodynamic response in the EPT group compared to the FT group. For the more difficult Item Type I, the FT group showed greater hemodynamic response in left cingulate gyrus, middle and superior frontal gyri, caudate and thalamus, and bilateral superior and inferior parietal lobules compared to the EPT group. Locations for each contrast are shown in Figure 3 and listed in Table 3. A conjunction analysis of EPT and FT group activity is shown in Figure 4. These results are suggestive of the EPT group demonstrating either widespread under-activation during the task compared to FT subjects or it may be due to more variability in brain responses across subjects. Closer inspection of the variance between the groups showed that the EPT group variance is almost twice as much as the FT group – for example FT improper Item Type I: mean voxel level variance = 222.6 (SD 151.6) and EPT improper Item Type I: mean voxel level variance = 428.2 (SD 327.2). Across all strategies and item types, the variance in the EPT group remains consistently around twice the variance in the FT group.

3.3.2 Mixed strategy. In group comparisons of the less difficult items (Item Type I) versus rest for the mixed strategy data, the EPT group compared to the FT group showed greater hemodynamic response in left insula, middle and medial frontal gyri; right superior frontal gyrus, cingulate, superior parietal lobule and precuneus. In contrast, the FT group compared to the EPT group showed greater hemodynamic response in left cingulate, middle and superior frontal gyri; right precentral gyrus, inferior parietal lobule, caudate nucleus; bilateral medial frontal and postcentral gyri. For Item Type II (hard) versus rest, the EPT group compared to the FT group showed greater hemodynamic response in left medial frontal gyrus and parahippocampal gyrus; right middle frontal and precentral gyri; bilateral precuneus. For the easier Item Type II, the FT group had greater hemodynamic response in left middle, medial and superior frontal gyri, pre- and post-central gyri; right inferior parietal lobule, cingulate, paracentral lobule and thalamus compared to the EPT group. The conjunction analysis for mixed fractions Item Types I and II in Figure 5 shows that much of the activity that is different between the groups appears around the edges of the overlapping clusters where statistical certainty is the lowest. These areas coincide with those listed above.

3.4 SVM classification

The purposes of these analyses were to determine if 1) birth group membership can be distinguished from hemodynamic response patterns from each strategy and item type, 2) difficulty level within a birth group and for a given strategy, and 3) strategy adoption within each birth group and for each of the item types. Discriminability with SVM corroborates findings of activation differences with the GLM-based analyses.

Classification of difficulty level (i.e., distinguishing item types) for the mixed fractions strategy demonstrated accuracies of 56.67% and 71.43% for FT and EPT groups, respectively (Figure 6a). Difficulty level classification for the improper fractions strategy demonstrated accuracies of 63.33% and 61.54% for FT and EPT groups, respectively. A similar analysis was performed to classify different strategies within the same item type. Classification of mixed versus improper strategies for Item Type II (improper easy vs mixed fractions hard) demonstrated accuracies of

495 86.67% and 80.77% for FT and EPT groups, respectively (Figure 6b). Strategy classification for
496 Item Type I (improper hard vs mixed fractions easy) demonstrated accuracies of 70% and 69.23%
497 for FT and EPT groups, respectively.
498
A further goal was to determine if the task-related BOLD signal measured here could be used by
the SVM to identify specific traits about a subject, or more specifically, if the SVM could
distinguish between birth status. BOLD signal data from a specific strategy and an item type (e.g.,
harder level of mixed fractions) was used with the goal of classifying untested BOLD signal data
as belonging to an EPT versus FT subject. This was conducted over multiple cross validation
iterations. The resulting classification accuracies and confusion matrices for each strategy-
difficulty combination are detailed in Table 4. The strategy-difficulty combinations with the
hardest difficulty produced the highest classification accuracies (67.86% and 64.29% for mixed
and improper fractions, respectively).
508
509 4.0 Discussion
510
511 This study explored differences in hemodynamic response between extremely preterm and FT born
512 teens associated with using two strategies to solve fractions, where cognitive loads varied by item
513 type and strategy. A main hypothesis of the study was that among the specific strategy and item
514 type combinations, activation differences between birth groups would be particularly pronounced
515 for the harder versus easier difficulty levels of a given strategy.
516
Overall, the estimated main effects of strategy indicated hemodynamic responses across
widespread areas of the brain associated with mathematical processing. Mixed fractions strategy
was associated with the highest number of active voxels and with a pattern of functional activation
that was distinct from the improper fractions strategy. Mixed fractions related hemodynamic
responses were located in fronto-parietal areas, while improper fractions hemodynamic responses
were centered around the precuneus and temporal gyrus. The hemodynamic response of the mixed
fractions strategy is consistent with that reported in the literature for mathematics tasks [8, 9].
524
In terms of group differences, the interaction between strategy and item type showed areas of
greater hemodynamic response specific to each group for each condition, with the exception of
Item Type I improper fractions strategy, where the EPT did not show greater functional activation
compared to the FT group. The areas of increased hemodynamic response for all other conditions
were widespread in fronto-parietal areas and along the midline and temporal gyri and by birth
group, strategy and item type. Efforts to solve both item types (I and II) using the mixed fractions
produced similar patterns of activity for both groups (see Supplement section S1, within group
analyses). In comparison, functional activations for this strategy in the EPT group compared to the
FT group were greater in bilateral insulae and middle frontal gyri. The different networks for each
strategy may be due to the different processes involved with the calculations (see Figure 1). The
mixed fraction strategy can have a greater cognitive load attributable to a higher demand for
number memorization necessary to achieve the answer (i.e., the separate answers for the whole
number and fractions must both be remembered and one must be kept in memory while the other
is calculated), particularly for Type II items (harder level). This finding may also reflect a relatively
higher level of demand on executive function. In contrast, when using the improper fractions
strategy, each calculation at a given step is used in the next step until the final result is obtained.

Some degree of working memory is thus needed to apply the improper fractions strategy,
particularly for Type I items (harder level). However, this approach may not require the same
magnitude of retention and manipulation as the mixed fractions strategy. The difference between
the strategies may also be due to more familiarity with the improper fractions strategy which is
often taught in schools. In support of this possibility, Tenison and colleagues found that unfamiliar
mathematics problems, compared to more familiar ones, took longer to solve and were
accompanied by increased brain activity in the intraparietal sulcus [41].
548
Group differences in patterns of functional activation may be associated with several factors. The
EPT subjects generally had lower working memory function (see WRAML2 scores in Table 1)
and they may have adopted different cognitive strategies to compensate for this weakness,
resulting in different areas of neural recruitment. An alternative explanation is that there may be
alterations in brain structure. Consistent with the group differences in brain structure observed in
this study (discussed below), past research has revealed alterations in grey and white matter
volumes and altered folding patterns of the cortical gyri in individuals born EPT [42, 43]. The
pattern of functional activity observed here may also be reflective of compensation for reduced
capacity or neural efficiency in the areas typically used by FT control subjects. A previous study
found evidence for neural compensation in adults with preterm birth on a visual learning task [44].
Further evidence in support of compensatory processes, as manifest in "cognitive reserve," is
provided by findings indicating age differences between younger and older adults in the level of
task difficulty at which patterns of neural activation change from those observed while doing less
difficult problems [45]. Greater variability in brain response at the individual level may also have
contributed to activation differences between the EPT and FT groups. Greater variability in
functional brain activity has been found among those with developmental dyscalculia [46] and
those born EPT [47]. The source of the greater variability may arise from differences in the brain
structure associated with preterm birth [42, 43], but may also reflect different developmental
trajectories related to atypical patterns of maturation and neuronal pruning [48, 49]. One study
found evidence of accelerated brain maturation and earlier neuronal pruning in individuals with
EPT compared to those born FT [50].
570
The SVM-based classifications with the highest accuracies were observed for strategy
classification based on item type (i.e., difficulty level). This higher classification accuracy (> 80%)
is seen for both groups. These findings suggest BOLD signals that differentiate strategy may be
shared across groups and are consistent with the group-level GLM activation pattern results, which
indicate different neural activation patterns by strategy. Classification rates for distinguishing
difficulty levels were higher for the EPT group than for the FT participants, particularly for the
mixed fractions strategy (71.43% versus 56.67%). This finding provides further evidence that the
EPT participants may be straining to solve the more difficult Type II items with this strategy. These
results are consistent with other findings from this study, including group differences in accuracy,
GLM-based activation patterns, and DWI-based connectivity, indicating that group differences
were most pronounced when participants were solving more difficult problems.
582
The above-noted group differences in patterns of brain functional activations and structure suggest
that some youth with EPT birth may engage different brain networks than FT youth in solving
fraction problems. These findings suggest a need to tailor instructions in fraction problem-solving,
and perhaps other aspects of mathematics, to individual differences. In solving problems relying

on brain networks similar to those engaged by FT youth, similar approaches may be justified.
However, the present findings indicate that at least some EPT adolescents may engage different
brain networks, depending on the strategy employed in solving a problem, the type of item, and
the cognitive competencies of the learner. One implication of these findings for mathematics
instruction is the support they provide for adapting problem-solving strategies in ways that are
biologically informed. Although procedures for making these modifications are to be determined,
the present results suggest the need for the student to recognize both their individual cognitive
competencies and the characteristics of the mathematics problems, such as their cognitive load and
the corresponding respective efficiencies of problem-solving strategies. Alternatively, efforts
could be made to strengthen some of the processes that contribute to problem-solving. An example
of these efforts as applies to fraction problem-solving would be to increase the automaticity of
retrieval of arithmetic facts as a means for compensating for weaknesses in working memory. In
the Supplement section S2, it was found that several areas were more likely to be functionally
active in the EPT group than the FT group, including the left parahippocampal and bilateral medial
frontal gyri, as well as a lack of functional activation in the precuneus. The precuneus has been
studied as a functional hub between multiple interacting brain networks and supports visuospatial
imagery and attention activation [51], skills necessary for mathematical calculations.
604
We also compared the EPT and FT groups on measures of brain structure using volumetrics and
DTI analysis (see Supplement sections S3 and S4). Volumetric analysis revealed reduced volume
in the left lingual and parahippocampal gyri in the EPT compared to the FT group. DTI analysis
revealed several altered connections for these youth, particularly involving the left
parahippocampal gyrus, left visual area and right superior parietal lobule. The findings indicating
alterations in the EPT group in brain volumes and connectivity are in line with other studies in
very preterm individuals (GA < 33 weeks) [42, 43, 52, 53]. Increased volumes and abnormal
patterns of structural connectivity may reflect alterations in brain growth that occur in response to,
or in compensation for, the above-noted decreases in brain volumes. For example, stronger
connectivity between some brain regions may compensate for weaker connectivity between other
regions. The overlap we found between the volumetric and DTI analyses suggests structural
changes in the left parahippocampal gyrus and right superior parietal lobule. Both regions had
reduced white matter volume and structural connectivity. The superior parietal lobule is involved
with action processes and visuomotor functions, attention, reasoning, spatial perception, visual
perception and working memory [54]. The function of the parahippocampal gyrus has been linked
to retrieval fluency in 7- to 9-year-old children [55]. Reduced grey and white matter volume in this
area may impact fluency in retrieval of math facts and suggests that EPT individuals may need to
invest more effort in making mental computations. The volumetric analysis also suggested that the
EPT group had reduced grey and white matter volume in the left lingual gyrus. The left lingual
gyrus has been linked to abilities in visual memory [56], a component of the working memory
system [57]. Reduced volume in both the grey and white matter of the lingual gyrus areas raises
the possibility of deficits in aspects of the working memory system supported by that region.
627
Major study limitations are the small sample size and questions regarding sample
representativeness. Participants were recruited from a larger sample of youth assessed several
years prior to this study. Many of the families could not be located. Although the EPT and FT
groups did not differ in age, most youth in the EPT group were female; thus, the sample was not
representative of the broader regional or national population of EPT youth. Further MRI studies

with larger and more representative samples are needed to confirm our results, and to continue to
explore how heterogeneity in cognitive outcomes of EPT birth may be associated with variability
in neural activations that we observed at the group level.
636
637 5.0 Conclusion
638
The effects of being born EPT on the brain are multifactorial and complex. The present study
explored brain function and structure in those born EPT through the lens of mathematical strategies
used in performing mental computation of fraction problems. We found both group and strategy-
dependent differences in neural activations to fraction problem-solving. The findings offer support
for considering individual differences among EPT in neural structure and function, along with the
specific demand characteristics or mathematics problems, in developing more targeted approaches
to mathematics instruction. This information may inform pedagogical practices and allow
educators to tailor mathematical approaches adapted to the cognitive and neural profiles of EPT
individuals. Particularly, hemodynamic response patterns associated with different problem-
solving strategies in youth born EPT compared to FT youth could serve as potential biomarkers of
approaches to mathematics instruction that may be most appropriate for youth born EPT. The
present findings suggest consideration of instructional approaches that focus on strategies with
relatively lower cognitive loads and on emphasizing flexibility in strategy adoption.
652
653 Declaration of conflicts of interest: All authors declare no conflicts of interest.
654
SC – Study design, analysis and interpretation of data, drafting of manuscript
MB – Study design, analysis and interpretation of data, review of manuscript
AI – Study design, analysis and interpretation of data, review of manuscript
BM-D – Study design, analysis and interpretation of data, review of manuscript
GW – analysis and interpretation of data, review of manuscript
WC – Study design, analysis and interpretation of data, software development, review of
manuscript
JF – Study design and software development, review of manuscript
JZ – Study design, analysis and interpretation of data, review of manuscript
MW – analysis and interpretation of data, review of manuscript
SYY – analysis and interpretation of data, review of manuscript
AB – Study design, data collection, review of manuscript
ER – Study design, analysis and interpretation of data, review of manuscript
CG – Study design, analysis and interpretation of data, review of manuscript
NM – Study design, analysis and interpretation of data, review of manuscript
LT – Study design, analysis and interpretation of data, review of manuscript
WHK - Study design, analysis and interpretation of data, review of manuscript
YS – study design, interpretation of data, review of manuscript
CN – interpretation of data, review of manuscript
HGT – Study design, analysis and interpretation of data, drafting of manuscript
CT – Study design, analysis and interpretation of data, drafting of manuscript
676

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679
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682
683 Data availability
684
685 The raw data supporting the conclusions of this article will be made available by the authors,
686 without undue reservation.
687

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Figure 1: Strategy/Item Type calculation steps demonstrating the cognitive load for each
combination.

825
826
827   **Figure 2:** Sample fraction protocol demonstrating the two strategies.

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830

Figure 3: Hemodynamic responses associated with improper and mixed fractions for both groups. Contrasts are easy EPT vs FT, easy FT vs EPT, hard EPT vs FT, and hard FT vs EPT. Improper fractions (A) and mixed fractions (B) locations are shown separately. L = Left, R = Right, A = Anterior, P = Posterior. Regions include - left side: precuneus, superior, medial and middle frontal gyri, superior and inferior parietal lobule, pre- and post-central gyri, insula, cingulate gyrus, parahippocampal gyrus, caudate nucleus and thalamus. Right side: paracentral lobule, precuneus, pre- and post-central gyri, inferior and superior parietal lobule, superior, medial and middle frontal gyri, cingulate, caudate nucleus and thalamus.

A)

843 **Figure 4:** Conjunction analysis of EPT and FT group results for improper and mixed fractions.
844 The EPT (red) and FT (blue) results have been overlaid. Shared voxels between EPT and FT are
845 shown in yellow. Improper fractions and mixed fractions include both Item types I and II. The
846 brain activity is overlaid on the MNI template brain. L = left, R = right, A = anterior.

847
848
849 **Figure 5:** Conjunction analysis of Item Types I and II for FT and EPT for mixed fractions. The
850 EPT (red) and FT (blue) results have been overlaid for each Item Type. Shared voxels are shown
851 in yellow. The brain activity is overlaid on the MNI template brain. L = left, R = right, A = anterior.

852
853
854 **Figure 6:** Accuracies of group-level SVM classification of difficulty level (A) and strategy (B)
855 from both FT and EPT groups. A leave-one-out cross validation approach was used for all SVM
856 analyses.
857 A)

B)

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Table 1: Summary of all subjects recruited for neuropsychological assessment. A subset of 30
subjects received MRI. Normally distributed continuous variables are described using mean (SD)
and tested using a t-test. Not normally distributed continuous variables are described using median
[IQR, interquartile range] and tested using a Wilcoxon test. Categorical variables are described
using percentages and tested using the Chi-squared test or Fisher's exact test (for variables with
small values). SD = Standard deviation, ZSES = a composite (mean of sample z scores) of maternal
education level, a measure of social advantage based on parent occupation, and medium income
of the family. HS = high school, GED = general education degree certificate, NDI =
neurodevelopment impairment (CP, Hearing, Vision and/or MDI<70), NeoRisk = number of

neonatal risk factors, SepsisNecMeningitis = sepsis, necrotising enterocolitis or menigitis present,
HUS = Head UltraSound, ROP = Retinopathy of prematurity, KTEA3 = Kaufman Test of
Educations Achievement third edition, WIAT3 = Wechsler Individual Achievement Test third
edition.WRAML2 = Wide Range Assessment of Memory and Learning, second edition.

	Level	EPT	FT	P-value	Stat test
Total		**14**	**16**		
SEX (%)	**Female**	**12 (85.7)**	**8 (50.0)**	**0.058**	**Fisher's exact**
	Male	**2 (14.3)**	**8 (50.0)**		
Age (mean (SD))		**16.60 (0.61)**	**16.00 (0.56)**	**0.009**	**T-test**
Age by year (%)	**14**	**0 (0.0)**	**2 (12.5)**	**0.304**	**Fisher's exact**
	15	**2 (14.3)**	**4 (25.0)**		
	16	**10 (71.4)**	**10 (62.5)**		
	17	**2 (14.3)**	**0 (0.0)**		
Ethnicity (%)	**Black or African American**	**7 (50.0)**	**7 (43.8)**	**1.000**	**Fisher's exact**
	Mixed	**0 (0.0)**	**1 (6.2)**		
	White	**7 (50.0)**	**8 (50.0)**		
Handedness (%)	**Left**	**3 (21.4)**	**0 (0.0)**	**0.090**	**Fisher's exact**
	Right	**11 (78.6)**	**16 (100.0)**		
Grade completed (%)	**8th**	**1 (7.1)**	**2 (12.5)**	**0.046**	**Fisher's exact**
	9th	**1 (7.1)**	**7 (43.8)**		
	10th	**11 (78.6)**	**7 (43.8)**		
	11th	**1 (7.1)**	**0 (0.0)**		
ZSES (median [IQR])		**0.07 [-0.32, 1.01]**	**0.50 [-0.16, 1.39]**	**0.467**	**Wilcoxon**
Maternal type of education (%)	**<HS**	**2 (14.3)**	**1 (6.2)**	**0.785**	**Fisher's exact**
	>HS	**11 (78.6)**	**14 (87.5)**		
	HS/GED	**1 (7.1)**	**1 (6.2)**		
Duration in years of Mothers Education (median [IQR])		**14.00 [12.00, 16.00]**	**15.00 [13.75, 18.00]**	**0.187**	**Wilcoxon**
Multiple Birth (%)	**Multiple Birth**	**2 (14.3)**	**0 (0.0)**	**0.209**	**Fisher's exact**
	Single Birth	**12 (85.7)**	**16 (100.0)**		

Birthweight in grams (mean (SD))		**780.00 (191.65)**	**3348.79 (537.28)**	**<0.001**	**T-test**
Gestational age (mean (SD))		**25.21 (1.42)**			
NDI (%)	**Impaired**	**5 (35.7)**			
	Not Impaired	**9 (64.3)**			
NeoRisk (%)	**0**	**6 (46.2)**			
	1	**3 (23.1)**			
	2	**2 (15.4)**			
	3	**1 (7.7)**			
	4	**1 (7.7)**			
Oxygen At 36wks (%)	**Not on O2@36wksCA**	**9 (69.2)**			
	On O2@36wksCA	**4 (30.8)**			
SepsisNecMeningitis (%)	**No**	**9 (64.3)**			
	Yes	**5 (35.7)**			
Severe HUS Abnormality (%)	**No**	**12 (85.7)**			
	Yes	**2 (14.3)**			
ROP (%)	**No**	**10 (76.9)**			
	Yes	**3 (23.1)**			
KTEA3					
Math Computation (mean (SD))		**92.21 (19.53)**	**101.94 (17.99)**	**0.167**	**T-test**
Math Concepts and Applications (mean (SD))		**92.57 (15.28)**	**103.25 (18.99)**	**0.104**	**T-test**
WIAT3					
Addition (mean (SD))		**87.50 (11.63)**	**96.88 (17.95)**	**0.106**	**T-test**
Subtraction (mean (SD))		**92.71 (11.47)**	**98.81 (16.60)**	**0.258**	**T-test**
Multiplication (mean (SD))		**86.93 (13.82)**	**92.81 (11.93)**	**0.221**	**T-test**

WRAML2				
Number Letter Scaled Score (mean (SD))	**10.21 (3.31)**	**11.00 (3.06)**	**0.505**	**T-test**
Finger Windows Scaled Score (mean (SD))	**8.29 (3.45)**	**11.81 (2.43)**	**0.003**	**T-test**

877 **Table 2**: Median accuracy rates for the mixed and improper fractions tasks performed during
878 fMRI. Easy and Hard is the overall rates for the improper or mixed fractions. SD = standard
879 deviation.

	Improper Median accuracy rate (%)(IQR)	Mixed Median accuracy rate (%)(IQR)
FT		
Easy	100 (17.6)	100 (14.3)
Hard	100 (17.6)	85.7 (17.9)
EPT		
Easy	100 (28.6)	85.7 (0.0)
Hard	100 (14.3)	71.4 (25.0)

881 **Table 3:** Between group differences in hemodynamic responses for Item Types for each fraction
882 strategy. P = 0.001, minimum cluster extent = 10 voxels.

Group	Strategy/ Level	Cluster No.	Coordinates (MNI)	No. of Voxels	Peak t-score	Side	Location
EPT >FT	Improper/ Item Type II	1	8 -38 52	21	3.50	Right	Precuneus
FT > EPT	Improper/ Item Type II	1	-30 8 54	43	4.36	Left	Middle Frontal Gyrus
		2	14 -28 58	36	3.74	Right	Paracentral Lobule
		3	-2 14 54	25	4.01	Left	Superior Frontal Gyrus
		4	-28 -48 64	12	3.95	Left	Superior Parietal Lobule
	Improper/ Item Type I	1	0 22 36	313	4.56	Left	Cingulate Gyrus
		2	-10 -64 64	33	4.66	Left	Superior Parietal Lobule
		3	-28 44 26	25	3.81	Left	Middle Frontal Gyrus
		4	0 12 54	25	3.62	Left	Superior Frontal Gyrus
		5	-32 -42 42	22	4.00	Left	Inferior Parietal Lobule
		6	-12 6 20	21	3.50	Left	Caudate
		7	-40 4 54	16	3.56	Left	Middle Frontal Gyrus
		8	16 -58 64	15	3.67	Right	Superior Parietal Lobule
		9	42 -34 40	13	3.48	Right	Inferior Parietal Lobule
		10	-34 56 16	11	3.76	Left	Superior Frontal Gyrus
		11	-8 -26 16	10	3.28	Left	Thalamus

EPT >FT	Mixed/ Item Type II	1	2 14 42	1258	7.74	Left	Medial Frontal Gyrus
		2	2 -60 52	817	7.02	Left	Precuneus
		3	34 0 54	315	6.03	Right	Middle Frontal Gyrus
		4	58 0 36	15	4.34	Right	Precentral Gyrus
		5	4 -70 48	13	5,15	Right	Precuneus
		6	-30 -30 -22	12	3.34	Left	Parahippocampal Gyrus
FT > EPT	Mixed/ Item Type I	1	-8 -14 38	653	5.17	Left	Cingulate Gyrus
		2	-46 6 38	221	4.44	Left	Middle Frontal Gyrus
		3	-20 48 38	159	5.81	Left	Superior Frontal Gyrus
		4	-16 -38 40	113	4.33	Left	Cingulate Gyrus
		5	0 50 20	69	5.26	Left	Medial Frontal Gyrus
		6	50 -14 40	60	4.17	Right	Precentral Gyrus
		7	56 -30 38	45	6.42	Right	Inferior Parietal Lobule
		8	30 -26 66	39	3.99	Right	Postcentral Gyrus
		9	-20 -32 70	35	3.93	Left	Postcentral Gyrus
		10	48 -50 42	21	3.92	Right	Inferior Parietal Lobule
		11	18 -8 28	21	3.59	Right	Caudate
		12	2 46 34	12	4.87	Left	Medial Frontal Gyrus
		13	4 -14 60	11	3.34	Right	Medial Frontal Gyrus
	Mixed/ Item Type II	1	-46 6 38	187	6.86	Left	Middle Frontal Gyrus
		2	-32 -26 66	115	6.14	Left	Postcentral Gyrus
		3	-36 -16 42	106	5.1	Left	Precentral Gyrus
		4	58 -30 38	56	7.35	Right	Inferior Parietal Lobule
		5	22 -34 12	40	3.88	Right	Thalamus
		6	14 -40 68	27	4.06	Right	Paracentral Lobule
		7	4 4 26	25	3.71	Right	Cingulate Gyrus
		8	-4 -10 66	23	3.65	Left	Medial Frontal Gyrus
		9	-6 42 48	16	3.68	Left	Superior Frontal Gyrus
		10	-42 -14 54	15	4.09	Left	Postcentral Gyrus
		11	-32 44 14	10	4.11	Left	Middle Frontal Gyrus

883
884 **Table 4.** Accuracies and confusion matrices from SVM classification of birth status.

	Classifier Accuracy (%)	Confusion Matrix (Prediction – Target)			
		EPT-EPT	EPT-FT	FT-EPT	FT-FT
Mixed, Item Type I (Easy)	60.71	7	5	6	10
Mixed, , Item Type II (Hard)	67.86	6	2	7	13
Improper, , Item Type II (Easy)	28.57	1	8	12	7
Improper, Item Type I (Hard)	64.29	7	4	6	11
Item Type I (Mixed Easy, Improper Hard)	53.57	6	6	7	9
Item Type II (Mixed Hard, Improper Easy)	50.00	3	4	10	11