

10 **ABSTRACT**

11 Hyperparasites (species which parasitise other parasites) are common in natural populations and
12 affect many parasitic taxa, including: eukaryotic parasites; bacterial and fungal pathogens; and insect
13 parasitoids. Hyperparasitism is therefore likely to shape the ecology and evolution of many host-
14 parasite systems, and represents a promising method for biocontrol (e.g. treating antimicrobial
15 resistant infections). However, the eco-evolutionary consequences of hyperparasitism have received
16 little attention. We use a host-parasite-hyperparasite model to explore how introducing a
17 hyperparasite drives the evolution of parasite virulence, and how this affects host population
18 dynamics. We show when the introduction of a hyperparasite selects for higher or lower parasite
19 virulence, and how this changes the disease burden for the host population. Crucially, we show that
20 variation in the virulence and infectivity of hyperparasites, along with the probability of co-
21 transmission, can lead to a previously unseen hysteresis effect, whereby small shifts in hyperparasite
22 characteristics can lead to sudden shifts in parasite virulence. We show that hyperparasites can
23 induce diversification in parasite virulence, leading to the coexistence of high and low virulence
24 strains. Our results show hyperparasites can have dramatic effects on the evolution of parasite
25 virulence, and that the use of hyperparasites in biocontrol should therefore be approached with
26 caution.

27 INTRODUCTION

28 Hyperparasitism, wherein parasitic organisms are themselves parasitised by another species, is
29 ubiquitous in the natural world. Hyperparasitism has been observed across many taxa, including
30 bacterial (Greer 2005; Ashelford, Day, and Fry 2003) and fungal (Mikhailov, Simdyanov, and Aleoshin
31 2016) pathogens, parasitic worms (Mohan et al. 2020) and other eukaryotic parasites (Wendling et
32 al. 2017), and among insect parasitoids (Haelewaters, Page, and Pfister 2018). For example, many
33 human bacterial pathogens are parasitised by bacteriophages, including *E. Coli* (e.g. phage O157:H7
34 (Munns et al. 2015)); *Salmonella typhimurium* (e.g. phage ϕ AB2 (Berchieri, Lovell, and Barrow
35 1991)); and *Klebsiella pneumoniae* (e.g. phage B5055 (Chhibber, Kaur, and Kumari 2008)).
36 Hyperparasitism is also common among fungal plant pathogens, such as the powdery mildew fungus
37 *Podosphaera plantaginis* with the hyperparasitic fungus *Ampelomyces* spp. (Parratt and Laine 2018),
38 or the chestnut blight fungus *Cryphonectria parasitica* (Nuss 2005) which can be infected by
39 *Cryphonectria hypovirus 1* (Parratt and Laine 2016).

40

41 Hyperparasites are understood to play a major role in the ecology of parasites, and have been
42 shown to influence both the early epidemic dynamics and the overwintering success (Parratt and
43 Laine 2018) of plant pathogens. They have also been implicated as a driver of seasonal epidemics of
44 cholera (Faruque et al. 2005). In addition to ecological effects on the parasite, hyperparasites can
45 have significant effects on virulence, either inducing hypovirulence (a reduction in the virulence
46 experienced by the host, e.g. by reducing the population size of the parasite) or hypervirulence (an
47 increase in the virulence experienced by the host, e.g. by causing the parasite to release toxins or by
48 introducing virulence factors). Hyperparasite-induced changes in virulence have been observed in
49 many bacterial pathogens. For example, a phage protein enhances motility (and hence virulence) of
50 *E. coli* (Kakkanat et al. 2017); the temperate phage PHB09 reduces the virulence of *Bordetella*
51 *bronchiseptica* both *in vivo* and *in vitro* (Chen et al. 2020); the phage CTX ϕ encodes the cholera toxin

52 within *Vibrio cholerae* (Waldor and Mekalanos 1996); and the phage ϕ CDHM1 interferes with
53 quorum sensing in *Clostridium difficile* (Hargreaves, Kropinski, and Clokie 2014).

54

55 Due to their ecological and virulence-mediating effects, hyperparasites long have been considered as
56 possible sources of biological control (biocontrol) for many infectious diseases (Holtappels et al.
57 2021; Obradovic et al. 2004), including in the agricultural and food industries and in the treatment of
58 chronic or antimicrobial resistant infections in humans (Gordillo Altamirano and Barr 2019). Indeed,
59 phage therapy has long been used as an alternative to antibiotics in some countries (Schooley et al.
60 2017; Ferriol-González and Domingo-Calap 2021). However, little is known about the evolutionary
61 implications of hyperparasitism for parasites, and so their use as agents of biocontrol in novel
62 settings could lead to unexpected outcomes for important traits such as parasite infectivity and
63 virulence. For instance, (Prospero et al. 2021) speculated that the introduction of hyperparasites
64 which reduce parasite virulence (hypovirulence) might select for higher virulence in chestnut blight
65 fungus, which has been observed experimentally (Bryner and Rigling 2012).

66

67 Understanding the interplay of host, parasite and hyperparasite ecological and evolutionary
68 dynamics is crucial not only to the development of novel agents of biocontrol, but also for
69 understanding their role in natural ecosystems. Theoretical studies of hyperparasites are rare and
70 have in the past mainly focussed on their ecological consequences (Taylor et al. 1998; Morozov,
71 Robin, and Franc 2007). Yet recently there has been renewed theoretical interest in hyperparasitism
72 in an evolutionary context, in the form of theoretical models of hyperparasite evolution (Northrup et
73 al. 2021) and parasite-hyperparasite coevolution (Sandhu et al. 2021). Two findings are of particular
74 interest. First, Sandhu et al. (2021), who considered parasite-hyperparasite coevolution, observed
75 that the introduction of hyperparasites typically increases parasite virulence, but in almost all
76 scenarios decreases average host mortality. Second, Northrup et al. (2021) observed that when

77 hyperparasites are more readily co-transmitted with evolutionarily static parasites, this selects for
78 less harm by the hyperparasite due to an increased link between its fitness and parasite transmission
79 (similar to virulence evolution in vertically transmitted parasites). These findings highlight the
80 importance of understanding hyperparasitism in both an ecological and an evolutionary context.

81

82 Here, we further investigate the eco-evolutionary consequences of introducing of a hyperparasite
83 for parasite virulence and the resulting net impact on the host population. We show how the
84 introduction of hyperparasites can cause an increase in evolved virulence but may cause an increase
85 or decrease in disease burden depending on the relative infectivity and virulence of hyperparasitised
86 parasites. We also show how small changes in the effects of the hyperparasite on parasite
87 transmission and virulence can lead to large shifts in the evolution of virulence due to hysteresis.
88 Finally, we show that the hyperparasite can induce diversification in parasite virulence, leading to
89 the coexistence of a relatively high and low virulence strains.

90

91 METHODS

92 *MODEL DESCRIPTION*

93 We consider a well-mixed population of asexual hosts, parasites, and hyperparasites, where S is the
94 density of uninfected (susceptible) hosts, I is the density of hosts only infected by the parasite
95 (parasitised) and H is the density of hosts infected by both the parasite and the hyperparasite
96 (hyperparasitised). Hosts reproduce at a baseline per-capita rate b , subject to density-dependent
97 crowding qN , with $q > 0$ and $N = S + I + H$. Parasite transmission is density-dependent, with
98 parasitised and hyperparasitised hosts having parasite transmission rates of β and $\eta\beta$ to susceptible
99 hosts, respectively, where β is the baseline transmission rate, $\eta > 1$ implies “hypertransmission”
100 (the hyperparasite increases parasite transmissibility) and $\eta < 1$ implies “hypotransmission” (the

101 hyperparasite decreases parasite transmissibility). Hyperparasites are co-transmitted with parasites
 102 to susceptible hosts with probability ρ . Hyperparasite infection of parasitised hosts is also density-
 103 dependent, with transmission rate σ . All hosts experience a natural mortality rate d , with parasitised
 104 and hyperparasitised hosts experiencing additional mortality due to disease at rates α and $\lambda\alpha$,
 105 respectively. Thus, when $\lambda < 1$ the hyperparasite induces hypovirulence (the hyperparasite
 106 decreases the disease-associated mortality rate) and when $\lambda > 1$ the hyperparasite induces
 107 hypervirulence (the hyperparasite increases the disease-associated mortality rate). Both parasitised
 108 and hyperparasitised hosts recover from infection at rate γ , with no lasting immunity (see Table 1
 109 for a full summary of model parameters and their default values for the analysis).

110

111 The ecological dynamics for a monomorphic population are described by the following three
 112 ordinary differential equations:

$$\begin{aligned}\dot{S} &= (b - qN)N - (\beta I + \eta\beta H + d)S + \gamma(I + H) \\ \dot{I} &= (\beta S - \sigma H - (d + \alpha + \gamma))I + (1 - \rho)\eta\beta SH \\ \dot{H} &= (\rho\eta\beta S + \sigma I - (d + \lambda\alpha + \gamma))H\end{aligned}\tag{1}$$

113

Parameter	Description	Default value
b	Natural birth rate of hosts	2.0
d	Natural mortality rate of hosts	0.5
q	Strength of density dependent competition	0.1
α_{max}	Maximum parasite virulence	5.0
β_0	Scale factor in parasite virulence-infectivity trade-off	$\sqrt{5}$
γ	Host recovery rate	0.5
η	Hyperparasite infectivity modifier	n/a

λ	Hyperparasite virulence modifier	n/a
ρ	Probability of hyperparasite co-transmission	0.5
σ	Hyperparasite transmission rate	4.0

114

Table 1: Model parameters and default values

115 We explore the evolution of parasite virulence under a standard transmission-virulence trade-off
 116 with diminishing returns, such that $\beta = \beta(\alpha)$ and $\beta''(\alpha) < 0$. For simplicity, we consider a trade-off
 117 of the form,

$$\beta(\alpha) = \beta_{max} \sqrt{\frac{\alpha}{\alpha_{max}}} = \beta_0 \sqrt{\alpha} \quad (2)$$

118

119 We assume that mutations are sufficiently rare so that the ecological dynamics in Equation 1 reach a
 120 stable endemic equilibrium (with either the host and parasite, or all three species present; see
 121 *Supplementary materials*) before a new mutant arises, and that mutations have small phenotypic
 122 effects. The invasion dynamics of a rare mutant parasite with transmission rate β_m and virulence α_m
 123 are then,

$$\begin{aligned} \dot{I}_m &= (\beta_m S^* - \sigma H^* - (d + \alpha_m + \gamma)) I_m + (1 - \rho) \eta \beta_m S^* H_m, \\ \dot{H}_m &= (\rho \eta \beta_m S^* - (d + \lambda \alpha_m + \gamma)) H_m + \sigma I_m H^*. \end{aligned} \quad (3)$$

124

125 where asterisks indicate the equilibrium population densities for the resident parasite. The invasion
 126 fitness $w(\alpha_m)$ is given by the largest eigenvalue of the next generation matrix (Hurford, Cownden,
 127 and Day 2010) (see *Supplementary materials*),

$$\begin{bmatrix} \frac{\beta_m S^*}{\sigma H^* + d + \alpha_m + \gamma} + \frac{(1 - \rho) \eta \sigma \beta_m S^* H^*}{(\sigma H^* + d + \alpha_m + \gamma)(d + \lambda \alpha_m + \gamma)} & \frac{(1 - \rho) \eta \beta_m S^*}{d + \lambda \alpha + \gamma} \\ \frac{\rho \eta \sigma \beta_m S^* H^*}{(\sigma H^* + d + \alpha_m + \gamma)(d + \lambda \alpha_m + \gamma)} & \frac{\rho \eta \beta_m S^*}{d + \lambda \alpha + \gamma} \end{bmatrix}$$

128

129 which we omit here for the sake of brevity. We derive the fitness gradient $F(\alpha) = \left. \frac{\partial w}{\partial \alpha_m} \right|_{\alpha_m = \alpha}$ and

130 hence calculate singular strategies, α^* , that satisfy $F(\alpha^*) = 0$. We determine the evolutionary

131 stability of a singular strategy by the sign of $E(\alpha^*) = \left. \frac{\partial^2 w}{\partial \alpha_m^2} \right|_{\alpha_m = \alpha = \alpha^*}$ (negative values indicate

132 evolutionary stability), and convergence stability by numerically approximating the derivative

133 $M(\alpha^*) = \left. \frac{\partial^2 w}{\partial \alpha_m \partial \alpha} \right|_{\alpha_m = \alpha = \alpha^*}$ and checking if the inequality $E(\alpha^*) + M(\alpha^*) < 0$ holds.

134

135 *SIMULATIONS*

136 We complement our numerical analysis with simulations of the evolutionary dynamics of our

137 system, which relax the adaptive dynamics assumptions of continuous traits and separate ecological

138 and evolutionary timescales. To perform our simulations, we first create a discretised trait space for

139 the parasite. We then initialise the hyperparasite-free system at its eco-evolutionary attractor, and

140 introduce hyperparasites at an arbitrarily low population density. We use a fourth order Runge-Kutta

141 method to solve the ordinary differential equations over a long time period, stopping when the

142 populations have relatively small changes in size, or the time threshold has been reached.

143 After removing phenotypes that fall below an arbitrary threshold, we choose one of the extant

144 parasite phenotypes (using a weighted probability based on parasite density) and introduce a rare

145 mutant a small phenotypic distance away at a low frequency. We then use this new population as

146 the initial condition for our ordinary differential equation system, which we again evaluate using a

147 fourth order Runge-Kutta method. All code used to produce the figures within this paper is available

148 within the Supplementary Material and on GitHub ([GitHub - JasonRWood/Wood Ashby 2023](#)).

149

150 *MEASURING THE IMPACT OF THE HYPERPARASITE ON THE HOST POPULATION*

151 We assume that the hyperparasite is introduced into a well-established host-parasite system, such
152 that the parasite is initially at its continuously stable strategy α_0 (see *Supplementary materials*) and
153 the system is at equilibrium. In addition to exploring the evolutionary implications for parasite
154 virulence we also consider the ecological implications for the host. Specifically, we consider multiple
155 metrics to encapsulate relative disease burden following the introduction of the hyperparasite,
156 namely impacts on: host population size, disease prevalence (proportion of hosts infected), and
157 mortality rates of infected individuals and the overall host population. These measures are
158 formulated below, where S_0 , I_0 and N_0 correspond to the steady state of the population before the
159 introduction of the hyperparasite, and asterisks indicate the population with the hyperparasite
160 present (usually evaluated at a continuously stable strategy, α^*).

161

162 We measure the relative host population size following the introduction of the hyperparasite as

163 $\Delta_N = \frac{N^*}{N_0}$ and the relative disease-associated mortality rate of infected hosts (Δ_M) is,

164
$$\Delta_M = \frac{\frac{\alpha^* I^* + \lambda \alpha^* H^*}{I^* + H^*}}{\frac{\alpha_0 I_0}{I_0}} = \frac{\alpha^* (I^* + \lambda H^*)}{\alpha_0}$$

165 **RESULTS**

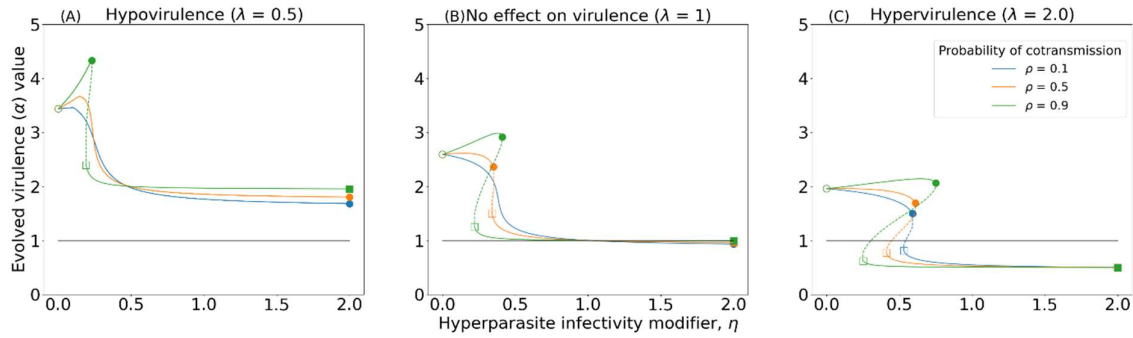
166 *HYPERPARASITE-INDUCED SHIFTS IN VIRULENCE EVOLUTION*

167 Following the introduction of the hyperparasite, we see pronounced shifts in the evolution of
168 virulence depending on the extent to which hyperparasites modify parasite infectivity (η) and/or
169 virulence (λ), and the extent to which co-transmission of the hyperparasite (ρ) occurs. When the
170 hyperparasite causes hypovirulence (a reduction in the disease-associated mortality rate, $\lambda < 1$), the
171 parasite always experiences selection for higher baseline virulence (Fig. 1a). However, the picture is

172 more complicated when the hyperparasite either causes no change to virulence ($\lambda = 1$; Fig. 1b) or
173 induces hypervirulence ($\lambda > 1$; Fig. 1c). Specifically, when the hyperparasite strongly reduces
174 parasite transmission ($\eta \ll 1$), the parasite evolves higher virulence, and when the hyperparasite
175 increases transmission ($\eta > 1$), virulence either remains virtually unchanged ($\lambda = 1$; Fig. 1b) or
176 evolves to lower levels ($\lambda > 1$; Fig. 1c). Yet at intermediate values, there is a hysteresis effect which
177 becomes more prominent as the virulence modifier (λ) or probability of co-transmission (ρ)
178 increase (Fig. 1b-c).

179

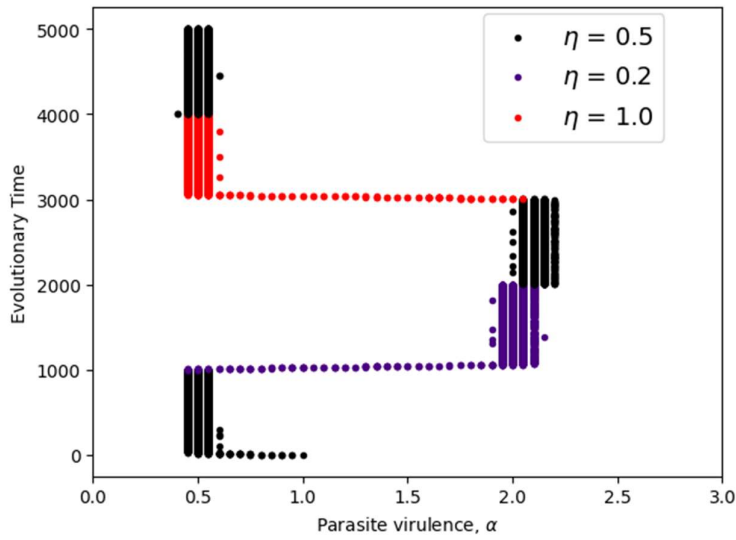
180 The hysteresis effect (the system demonstrates different behaviour as a parameter is smoothly
181 varied from high to low or from low to high) means that the system can have two evolutionary
182 attractors, and therefore small changes in the underlying ecology (e.g. effects of the hyperparasite
183 on parasite virulence or infectivity) may cause sudden shifts between high and low virulence states
184 that are difficult to reverse (Fig. 2). For example, suppose the hyperparasite causes an increase in
185 virulence ($\lambda > 1$; Fig. 1c), co-transmits with high probability ($\rho \approx 1$), and halves the transmissibility
186 of the parasite ($\eta = 0.5$). Selection would then favour a reduction in evolved virulence relative to
187 the absence of the hyperparasite ($\alpha^* < \alpha_0$) (Fig. 2). A small reduction in the infectivity modifier
188 below a critical threshold, η_c^1 , would suddenly shift selection for increased virulence ($\alpha^* > \alpha_0$), but
189 a reversion in the infectivity modifier to its initial value ($\eta > \eta_c^1$) would not lead to a drop in
190 virulence until a second critical threshold, $\eta > \eta_c^2 > \eta_c^1$ is breached (Fig. 2). Thus, relatively small
191 changes in the effects of the hyperparasite on parasite transmission can lead to large changes in the
192 evolution of virulence that may be difficult to reverse.



193

194 *Figure 1: Evolutionary consequences for parasite virulence (solid: attractors, dashed: repellers) as the effects of the*
195 *hyperparasite on parasite infectivity (hypoinfectivity: $\eta < 1$; hyperinfectivity: $\eta > 1$) and virulence (λ) vary. (A)*
196 *hypovirulence ($\lambda < 1$); (B) no effect on virulence ($\lambda = 1$); (C) hypervirulence ($\lambda > 1$). All panels contain three sets of curves*
197 *showing the evolved outcome as the probability of hyperparasite co-transmission varies: $\rho = 0.1$ (blue), $\rho = 0.5$ (orange),*
198 *$\rho = 0.9$ (green). The start and end of the hysteresis section are shown with empty and filled shapes. The black line indicates*
199 *the ancestral state prior to the introduction of the hyperparasite. (A-C) Evolved levels of virulence.*

200



201

202 *Figure 2: Evolutionary simulations showing the hysteresis affect observed in Figure 1 due to variation in the effects of the*
203 *hyperparasite on parasite infectivity, η . A relatively small shift (purple) from an initial value of η (black) leads to a sharp*
204 *increase in virulence. However, a reversion to the initial value of η (black) does not lead to a return to lower virulence.*
205 *Instead, virulence does not change significantly until a critical threshold is reached (red). Parameters as in Table 1 except*
206 *$\lambda = 2.0, \rho = 0.9$.*

207 *EFFECTS OF HYPERPARASITISM ON THE HOST POPULATION*

208 Although the parasite may evolve higher or lower baseline virulence following the introduction of
209 the hyperparasite, whether this has a net positive or negative effect for the host population depends
210 on not only the new level of virulence, but also the effects on parasite prevalence, the prevalence of
211 hyperparasites, and the effects of hyperparasitism on virulence. We therefore consider the
212 ecological consequences of the hyperparasite on the host following evolutionary shifts in parasite
213 virulence.

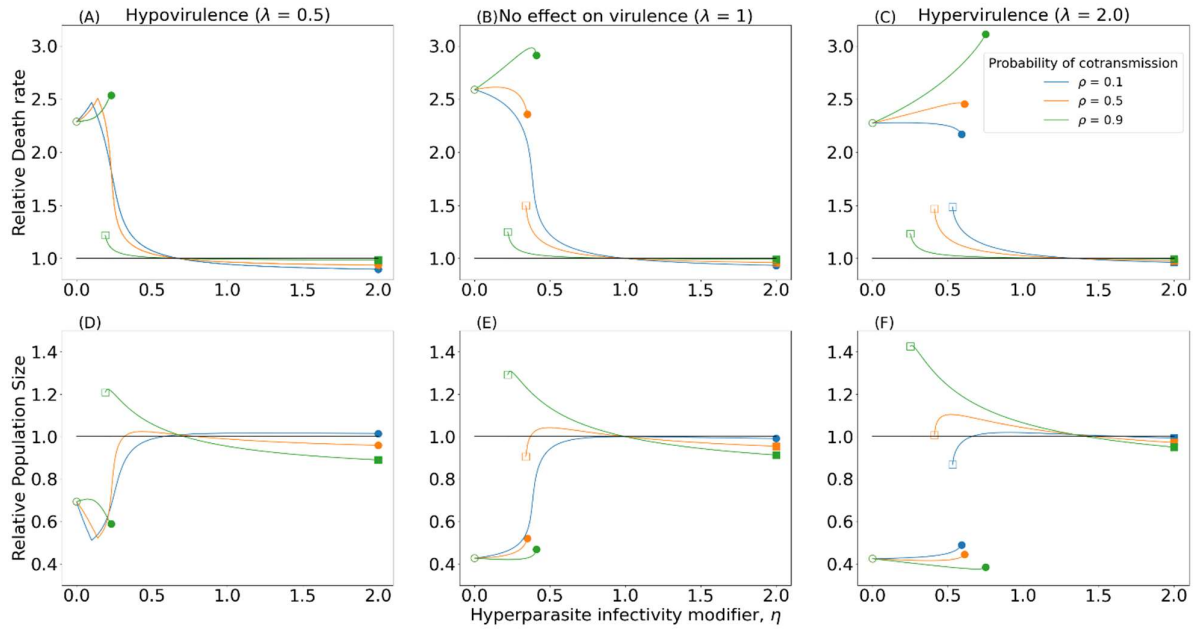
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215 Intuitively, when the hyperparasite causes an evolutionary increase in virulence while not inducing
216 hypovirulence, the burden on infected hosts (i.e. the average disease-associated mortality rate) is
217 always higher (Fig. 3B-C) and the resulting host population size is lower (Fig. 3E-F). This is especially
218 pronounced when the hyperparasite strongly reduces transmission ($\eta \ll 1$). However, the burden
219 on hosts is less straightforward when the hyperparasite induces hypovirulence while selecting for
220 higher virulence (Fig. 3A,D), or induces hypervirulence while selecting for lower virulence (Fig. 3C,F).
221 For example, the latter scenario can lead to little effect on the mortality rate of infected hosts (Fig.
222 3C) but a marked increase in the host population size (Fig. 3F).

223

224 Crucially, the hysteresis effect in the evolution of virulence has a striking effect on the host
225 population, with relatively small shifts in the effects of hyperparasites on transmission (η) or on the
226 probability of co-transmission (ρ) causing substantial changes in the relative mortality rate of
227 infected hosts (Fig. 3B-C) and the host population size (Fig. 3E-F). While the hysteresis effect
228 separates a region of lower host population size from a region of higher host population size (Fig.
229 3D-F), this does not hold for the burden on infected hosts (Fig. 3A-C). Typically, infected hosts either
230 experience a significant increase in average disease burden (for sufficiently low values of η), or there

231 is little effect. This suggests that the introduction of a hyperparasite rarely improves the outcome of
232 infection on average, even if it is beneficial at the population level by reducing the proportion of the
233 population that is infected. We also see that as the probability of coinfections (ρ) increases, the
234 effect of introducing the hyperparasites on the average disease burden for infected hosts and on the
235 host population size typically grows stronger.



236

237 *Figure 3: Ecological consequences of hyperparasitism for the host as the effects of the hyperparasite on parasite infectivity*

238 *(hypoinfectivity: $\eta < 1$; hyperinfectivity: $\eta > 1$) and virulence (λ) vary. Left column: hypovirulence ($\lambda < 1$); middle column:*

239 *no effect on virulence ($\lambda = 1$); right column: hypervirulence ($\lambda > 1$). All panels contain three sets of curves showing the*

240 *evolved outcome as the probability of hyperparasite co-transmission varies (shown in Fig. 1): $\rho = 0.1$ (blue), $\rho = 0.5$*

241 *(orange), $\rho = 0.9$ (green). The start and end of the hysteresis section are shown with empty and filled shapes. The black line*

242 *indicates the ancestral state prior to the introduction of the hyperparasite. (A-C) Average mortality rate of infected hosts*

243 *relative to before the introduction of the hyperparasite. (D-F) Host population size relative to before the introduction of the*

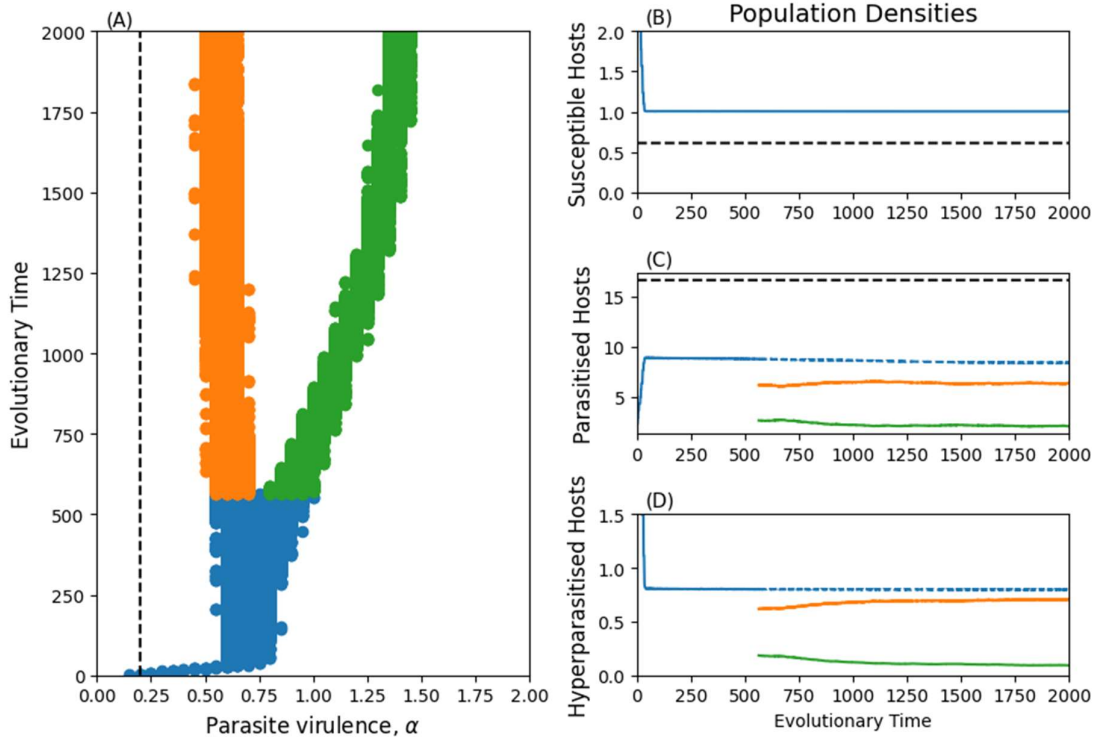
244 *hyperparasite.*

245 *HYPERPARASITE-INDUCED DIVERSIFICATION IN PARASITE VIRULENCE*

246 In the absence of the hyperparasite, parasite virulence evolves to a continuously stable strategy due
247 to the trade-off with transmission, which results in diminishing returns for the parasite. The
248 introduction of the hyperparasite either shifts the continuously stable strategy to a new value (as in
249 Fig. 1) or causes the parasite population to diversify through evolutionary branching into two strains,
250 one with relatively high virulence and the other with relatively low virulence (Fig. 4). In general,
251 branching is most likely to occur when the hyperparasite causes hypervirulence ($\lambda > 1$) and strong
252 hypoinfectivity ($\eta \ll 1$), and the probability of co-transmission is not too high ($\rho \ll 1$) (Fig. 5).
253 When hyperparasites increase virulence and reduce the infectivity of parasites, two contrasting
254 strategies can coexist. The first is a “short-lived”, more virulent strain which infects as many hosts as
255 possible before being itself infected by the hyperparasite (green branch, Fig. 4). The second is a
256 “long-lived”, less virulent strain which prioritises host infections whilst hyperparasitised (orange
257 branch, Fig. 4).

258

259 However, even though one of the parasite strains is less virulent than the other, both are more
260 virulent than the ancestral strain in the absence of the hyperparasite (Fig. 4a). The more virulent
261 strain is rarely infected by the hyperparasite (Fig. 4d), as the host either dies prior to encountering
262 the hyperparasite, or experiences hypervirulence and so dies shortly after being hyperparasitised.
263 Despite the parasite branching into two distinct strategies that are both more virulent than the
264 ancestral state, the overall impact on host and parasite population sizes is minimal (Fig. 4b-d).



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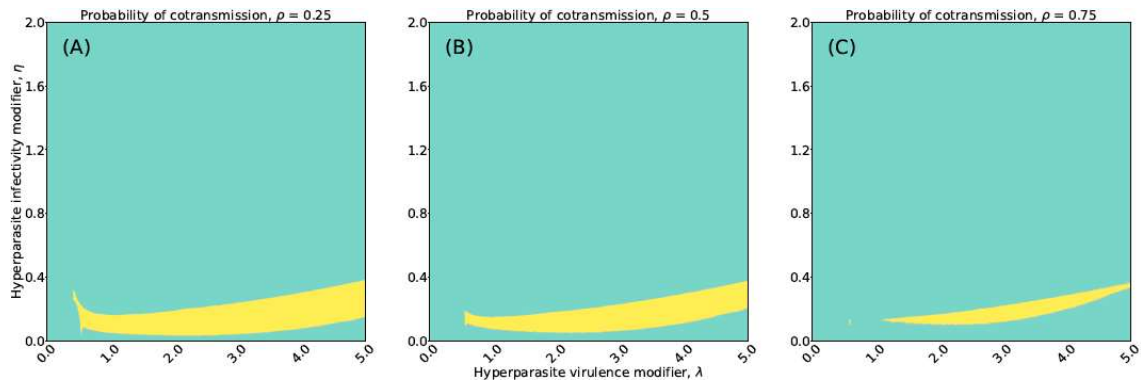
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Figure 4. Evolutionary branching in parasite virulence following the introduction of the hyperparasite. Parasite virulence in the absence of the hyperparasite is shown by the dashed line in (A). The parasite branches into relatively high (green) and low (orange) virulence strains. (B-D) Densities of the host, parasite and hyperparasite populations: total (blue), high-virulence strain (green), low-virulence strain (orange). The density of the host and parasite populations in the absence of the hyperparasite are plotted with a dashed black line. Parameters as in Table 1 except $d = 0.1, \sigma = 0.4, \rho = 0.5, \eta = 0.25, \lambda = 5.0, \gamma = 0.1$.

272



273

274 *Figure 5. Regions where evolutionary branching occurs (yellow) for the parasite following the introduction of the*

275 *hyperparasite, as the effects on transmission (η) and virulence (λ) vary. Parameters as in Table 1 except $d = 0.1, \sigma =$*

276 *0.4, $\gamma = 0.1$.*

277 DISCUSSION

278 Hyperparasites are abundant in nature and are promising sources of biological control in industry
279 (e.g. food production) and public health (e.g. phage therapy to combat antimicrobial resistance). Yet
280 the eco-evolutionary effects of hyperparasitism are poorly understood. In this study, we have
281 theoretically explored the impact of hyperparasites on the evolution of parasite virulence and the
282 consequences for the host population. We have shown that the introduction of hyperparasites can
283 lead to either higher or lower levels of evolved virulence depending on the ecological effects of the
284 hyperparasite on the parasite. Crucially, we have shown that relatively small changes in the
285 ecological effects of hyperparasites can cause large shifts in virulence, which can be difficult to
286 reverse due to hysteresis. Although a hyperparasite may cause selection for higher parasite
287 virulence, we have shown that this is not necessarily negative for the host population overall, as the
288 hyperparasite can suppress parasite prevalence and may mitigate virulence in infected hosts. Finally,
289 our model shows that the introduction of a hyperparasite can induce diversification in the parasite
290 population, with the potential for both strains to evolve to higher levels of virulence than in the
291 absence of the hyperparasite. Overall, our results suggest that the introduction of hyperparasites
292 can have a strong impact on the evolution of parasite virulence and that the nature of the outcome
293 depends crucially on how the hyperparasite affects parasite virulence and transmission.

294

295 Higher parasite virulence typically evolves under two conditions: either the hyperparasite
296 dramatically reduces the infectivity of the parasite population relative to the effect on parasite
297 virulence ($\eta < \lambda$ and $\eta < 1$), or the hyperparasite reduces the realised virulence when hosts are
298 infected ($\lambda < 1$). The former scenario selects for higher virulence because the transmission rate
299 from hyperparasitised hosts is reduced to a greater extent than realised virulence, which shifts the
300 balance in the transmission-virulence trade-off to greater transmission. In the second scenario ($\lambda <$
301 1), realised virulence is lower in hyperparasitised hosts and so the increased transmission comes at a

302 reduced cost. This can be trivially understood by considering a hyperparasite that completely
303 mitigates virulence ($\lambda = 0$), which greatly benefits the parasite. Conversely, when $\lambda > 1$ the
304 hyperparasite increases realised virulence and therefore selects for lower intrinsic virulence.

305

306 The hysteresis effect in our model suggests that not only might relatively small changes in
307 hyperparasite traits cause large evolutionary changes in the parasite, but that these might be
308 difficult to reverse. Hysteresis arises because for certain regions of parameter space the system is
309 bistable, meaning that the parasite can evolve to have relatively high or low virulence depending on
310 the current level of virulence. The hysteresis effect can be understood due to changes in the
311 prevalence of the hyperparasite. When the hyperparasite causes a significant reduction in
312 transmission ($\eta \ll 1$) it is very costly to the parasite and so selection favours higher transmission
313 and virulence to avoid being hyperparasitised (upper branch). The hyperparasite is therefore at
314 relatively low prevalence. As the effects of the hyperparasite on infectivity weaken (η increases), the
315 hyperparasite may become more common if it can co-transmit well with the parasite (high ρ),
316 resulting in a gradual increase in hyperparasite prevalence. Eventually a threshold is reached where
317 the risk of hyperparasitism is sufficiently high and the cost sufficiently low that selection favours a
318 large reduction in parasite virulence (lower branch), which feeds back to further increase
319 hyperparasite prevalence. This positive feedback, resulting in high hyperparasite prevalence, is
320 crucial to the hysteresis effect. If the hyperparasite once again reduces parasite infectivity more
321 strongly (η decreases), the system does not return to the high virulence state because hyperparasite
322 prevalence remains high (lower branch). As η continues to fall so too does hyperparasite prevalence,
323 until eventually the risk of hyperparasitism is sufficiently low and the cost sufficiently high that
324 selection favours a large increase in parasite virulence (upper branch).

325

326 The hysteresis effect has especially important implications for biocontrol, as a relatively small change
327 in the hyperparasite can have a large effect on the evolution of virulence and on the host
328 population. While hysteresis is well documented in the ecological literature (e.g. the spruce
329 budworm (Ludwig, Jones, and Holling 1978)), few examples exist in evolutionary models (Prado et al.
330 2009). As an exception, Prado *et al.* 2009 observed hysteresis when considering the evolution of host
331 sociality and pathogen virulence within contact networks. Prado *et al.* observed that the cycling
332 behaviour they see within their system, has hysteresis-like behaviour where selection for or against
333 host sociality does not occur until the parasite passes critical thresholds.

334

335 Our model reveals that the introduction of a hyperparasite can cause disruptive selection leading to
336 diversification into relatively high and low virulence parasite strains (although the “low” virulence
337 strain may still be more virulent than the ancestral strain, as in Fig. 4). Branching typically requires
338 the transmission-virulence trade-off to be close to linear as strongly diminishing returns have a
339 balancing effect on selection. Branching also typically requires the hyperparasite to reduce the
340 infectivity of the parasite far more than it decreases virulence ($\eta \ll \lambda$), which facilitates the
341 existence of high and low virulence phenotypes by creating distinct ecological niches. The high
342 virulence phenotype is rarely infected by the hyperparasite, favouring a “live fast, die young”
343 strategy, while the less virulent phenotype has a longer infectious period to mitigate the burden of
344 the hyperparasite.

345

346 Our study is closely related to previous theoretical explorations of evolution in host-parasite-
347 hyperparasite systems (Sandhu et al. 2021; Northrup et al. 2021). Sandhu et al (2021) also explored
348 the evolution of parasite virulence, but in contrast to our study found that the introduction of a
349 hyperparasite generally selects for increased virulence and reduces the average mortality rate of the
350 host. Furthermore, Sandhu et al (2021) did not observe a hysteresis effect, nor did they find

351 diversification in their model of virulence evolution. The differences in our results are likely due to
352 crucial differences in our assumptions. In particular, we assumed that hosts could recover from
353 infection and that the hyperparasite is co-transmitted with a certain probability (ρ) rather than
354 always occurring, as in Sandhu et al. In reality, one would not expect the hyperparasite to always co-
355 transmit with the parasite, and our model reveals that this parameter has critical effects on the
356 evolution of virulence. Although models of hyperparasitism are relatively rare, especially in an
357 evolutionary context, some of our key findings are mirrored in models of other tripartite systems.
358 For example, multiple studies have found that introducing an additional species to a host-parasite
359 system can lead to evolutionary branching in the host (Best 2018) or the parasite (Kisdi, Geritz, and
360 Boldin 2013; Best 2018; Smith and Ashby 2022) populations. In a related study that also has
361 relevance to biocontrol, Smith and Ashby (2022) explore how the introduction of a tolerance-
362 conferring defensive symbiont affects the evolution of parasite virulence. They show that even if the
363 defensive symbiont is initially beneficial to the host population, in the long-term it is costly because
364 it always selects for higher parasite virulence. Our results similarly emphasise the complex eco-
365 evolutionary outcomes that can arise following the introduction of a hyperparasite, with potentially
366 disastrous consequences for the host population.

367

368 In established host-parasite-hyperparasite systems, it is difficult to separate the ecological and
369 evolutionary consequences of the hyperparasite. Few empirical studies have therefore explored the
370 effects of hyperparasitism on parasite evolution (Parratt and Laine 2016), and those that do often
371 focus on consequences for antimicrobial resistance (Chan et al. 2016; Burmeister et al. 2020), the
372 acquisition of virulence factors from hyperparasites (Miao and Miller 1999), or pleiotropic effects on
373 virulence due to selection for resistance against hyperparasitism (Castledine et al. 2022). For
374 example, (Evans et al. 2010) showed that strains of the bacteria *Erwinia carotovora ssp. atroseptica*
375 (*Eca*) resistant to the hyperparasite ϕ AT1 were less likely to produce rot in potato tubers; Castledine

376 et al. showed that evolution of phage resistance in *Pseudomonas aeruginosa* coincided with the loss
377 of virulence in vitro and in vivo; and (Scanlan and Buckling 2012) showed that coevolution between
378 the bacteria *P. fluorescens* and a lytic phage ($\phi 2$) selects for a mucoid phenotype, which is a
379 virulence factor in both lung infections of cystic fibrosis patients and in plant infections. Clearly, the
380 available empirical evidence suggests that hyperparasites can indeed have significant evolutionary
381 effects on parasite virulence, although the precise effects may depend on pleiotropy between
382 resistance and virulence. Our model did not consider resistance to hyperparasitism but
383 understanding how pleiotropy with resistance affects virulence evolution is a critical direction for
384 future theoretical work (Sandhu et al. 2021).

385

386 We focused our investigation on the evolution of virulence, but the evolutionary dynamics of the
387 hyperparasite are also likely to be important (Sandhu et al. 2021; Northrup et al. 2021). However, in
388 certain cases the hyperparasite might behave as if it is evolutionarily static (e.g. the repeated
389 application of a particular biocontrol to an agricultural crop), in which case the model analysed here
390 will be especially applicable. Still, future theoretical work should consider how our findings are
391 affected by hyperparasite evolution, and whether the hysteresis in our model could lead to
392 fluctuating selection as in Prado et al. (2009). Additionally, the joint dynamics of resistance and
393 virulence evolution deserve further scrutiny, which could be explored using a resource-allocation
394 model where the parasite can either allocate resources to transmission or defence, with the overall
395 resource “budget” depending on the level of virulence.

396

397 Overall, we have shown that the introduction of hyperparasites can have dramatic effects on the
398 evolutionary dynamics of parasite virulence, leading to selection for higher or lower virulence, or to
399 branching, with the outcome critically dependent on the effects of the hyperparasite on infectivity
400 and realised virulence, and on the probability of co-transmission. We have also shown how relatively

401 small changes in hyperparasite traits can have dramatic consequences for virulence evolution, which
402 has important implications for the use of hyperparasites as agents of biocontrol.

403

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411

412 CONFLICTS OF INTEREST

413 The authors declare they have no conflicts of interest

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