Predictive learning rules generate a cortical-like replay of probabilistic sensory experiences

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Abstract

The brain is thought to construct an optimal internal model representing the probabilistic structure of the environment accurately. Evidence suggests that spontaneous brain activity gives such a model by cycling through activity patterns evoked by previous sensory experiences with the experienced probabilities. The brain's spontaneous activity emerges from internally-driven neural population dynamics. However, how cortical neural networks encode internal models into spontaneous activity is poorly understood. Recent computational and experimental studies suggest that a cortical neuron can implement complex computations, including predictive responses, through soma-dendrite interactions. Here, we show that a recurrent network of spiking neurons subject to the same predictive learning principle provides a novel mechanism to learn the spontaneous replay of probabilistic sensory experiences. In this network, the learning rules minimize probability mismatches between stimulus-evoked and internally driven activities in all excitatory and inhibitory neurons. This learning paradigm generates stimulus-specific cell assemblies that internally remember their activation probabilities using within-assembly recurrent connections. Our model contrasts previous models that encode the statistical structure of sensory experiences into Markovian transition patterns among cell assemblies. We demonstrate that the spontaneous activity of our model well replicates the behavioral biases of monkeys performing perceptual decision making. Our results suggest that interactions between intracellular processes and recurrent network dynamics are more crucial for learning cognitive behaviors than previously thought.

Introduction

The brain is believed to construct an internal statistical model of an uncertain environment from sensory information streams for predicting the external events that are likely to occur. Evidence suggests that spontaneous brain activity learns the representation of such a model through repeated experiences of sensory events. In the cat visual cortex, spontaneously emerging activity patterns cycle through cortical states that include neural response patterns to oriented bars (Kenet et al., 2003). In the ferret visual cortex, spontaneous activity gradually resembles a superposition of activity patterns evoked by natural scenes, eventually giving an optimal model of the visual experience (Berkes et al., 2011). As replay activities can provide prior information for hierarchical Bayesian computation by the brain (Ernst & Banks, 2002; Kording & Wolpert, 2004; Friston, 2010; Fiser et al., 2010; Bastos et al., 2012; Orban et al., 2016; Legaspi & Toyoizumi, 2019), clarifying how the brain learns the spontaneous replay of optimal internal models is crucial for understanding whole-brain computing. However, the neural mechanisms underlying this modeling process are only poorly understood.

Several mechanisms of the brain's probabilistic computation have been explored (Jimenez Rezende & Gerstner, 2014; Li et al., 2022). Models with reverberating activity are particularly interesting owing to their potential ability to generate spontaneous activity. For instance, spiking neuron networks with symmetric recurrent connections were proposed for Markov Chain Monte Carlo sampling of stochastic events (Buesing et al, 2011; Bill et al., 2015). Spike-timing-dependent plasticity was used to organize spontaneous sequential activity patterns, providing a predictive model of sequence input (Hartmann et al., 2015). However, previous models did not clarify how recurrent neural networks learn the spontaneous replay of the probabilistic structure of sensory experiences, for which these networks should learn the accurate probabilities of sensory stimuli and an appropriate excitation-inhibition balance simultaneously. Moreover, previous models assumed that each statistically salient stimulus in temporal input is already segregated and is delivered to a pre-assigned assembly of coding neurons, implying that the recurrent network, at least partly, knows the stochastic events to be modeled before learning. How the brain extracts salient events for statistical modeling has not been addressed.

Here, we present a learning principle to encode the experiences' probability structure into spontaneous network activity. To this end, we extensively use the synaptic plasticity rule proposed previously based on the hypothesis that the dendrites of a cortical neuron learn to predict its somatic responses (Urbanczik & Senn, 2014; Asabuki & Fukai, 2020). We generalize the hypothetical predictive learning to a learning principle at the entire network level. Namely, in a recurrent network driven by external input, we ask all synapses on the dendrites of each excitatory or inhibitory neuron to learn to predict its somatic responses (although the dendrites will not be explicitly modeled). This enables the network model to simultaneously learn the events' probabilistic structure and the excitation-inhibition balance required to replay this structure. Further, our network model requires no pre-assigned cell assemblies since the model neuron can automatically segment statistically salient events in temporal input (Asabuki & Fukai, 2020) - a cognitive process known as "chunking" (Fujii & Graybiel, 2003; Jin & Costa, 2010; Jin et al., 2014; Schapiro et al., 2013; Zacks et al., 2001). Intriguingly, the cell assemblies generated by our model store their replay probabilities primarily in the within-assembly network structure, and intrinsic dynamical properties of membership neurons also contribute to this coding. This is in striking contrast to other network models that encode probabilities into the Markovian transition dynamics among cell assemblies (Buesing et al., 2011; Hartmann et al., 2015; Asabuki & Clopath, 2024).

Our model trained on a perceptual decision-making task can replicate both unbiased and biased decision behaviors of monkeys without fine-tuning of parameters (Hanks et al., 2011). In addition, in a network model consisting of distinct excitatory and inhibitory neural populations, our learning rule predicts the emergence of two types of inhibitory connections with different computational roles. We show that the emergence of the two inhibitory connection types is crucial for robust learning of an optimal internal model.

Results
Replay of probabilistic sensory experiences - A toy example
We first explain the task our model solves with a toy example. Consider a task in which the animal should decide whether a given stimulus coincides with or resembles any of two previously learned stimuli. Whether the animal learned these

106 stimuli with a 50-50 chance or a 30-70 chance should affect the animal's antici-
107 pation of their occurrence and hence affect its decision.
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109 It has been suggested that spontaneous activity expresses an optimal internal
110 model of the sensory environment (Berkes et al., 2011). In our toy example, the
111 evoked activity patterns of the two stimuli should be spontaneously replayed with
112 the same probabilities as these stimuli were experienced during learning:

113
114 $$< P(\text{features}|\text{input}, \text{model}) >_{P(\text{input})} = P(\text{features}|\text{model}),$$
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where features = {stimulus 1, stimulus 2} and the right-hand side expresses the
probabilities of replayed activities. The angular brackets indicate averaging over
the stimuli. According to Hebb's hypothesis, two cell assemblies should be formed
to memorize the two stimuli in the toy example. Moreover, the spontaneous replay
of these cell assemblies should represent the probabilities given in the right-hand
side of the above equation. Below, we propose a mathematical principle of learn-
ing to achieve these requirements.
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Prediction-driven synaptic plasticity for encoding an internal model

We previously proposed a learning rule for a single two-compartment neuron
(Asabuki & Fukai, 2020). Briefly, our previous model learns statistically salient
features repeated in input sequences by minimizing the error between somatic
and dendritic response probabilities without external supervision to identify the
temporal locations of these features. In this study, we extend this plasticity rule to
recurrent networks by asking all neurons in a network to minimize the error in
response probabilities between the internally generated and stimulus-evoked ac-
tivities (Fig. 1). Our central interest is whether this learning principle generates
spontaneous activity representing the statistical model of previous experiences.
134
135 We first introduce our learning principle using a recurrent network model (nDL
136 model) that does not obey Dale's law for distinguishing between excitatory and

Figure 1. Unsupervised prior learning in a recurrent neural network. (a) A schematic of a network model is shown. The interconnected circles denote the model neurons, of which the activities are controlled by two types of inputs: feedforward (FF) and recurrent (REC) inputs. Colored circles indicate active neurons. Here, **W** denotes FF, and **M** and **G** denote REC connections. We considered two modes of activity (i.e., evoked and spontaneous activity). In the evoked mode, the membrane potential u of a network neuron was calculated as a linear combination of inputs across all different connections (v^W, v^M, and v^G). This evoked mode is considered during the learning phase, when all synapses attempt to predict the network activity, as we will explain in the main text. Once all synapses are sufficiently learned, all FF inputs are removed, and the network is driven spontaneously (spontaneous mode). Our interest lies in the statistical similarity of the network activity in these two modes. (b) The gain and threshold of output response function was controlled by a dynamic variable, h, which tracks the history of the membrane potential. (c) A schematic of the learning rule for a network neuron is shown (top). During learning, for each type of connection on a postsynaptic neuron, synaptic plasticity minimizes the error between output (gray diamond) and synaptic prediction (colored diamonds). Note that all types of synapses share the common plasticity rule, where weight updates are calculated as the multiplication of the error term and the presynaptic activities (bottom). Our hypothesis is that such plasticity rule allows a recurrent neural network to spontaneously replay the learned stochastic activity patterns without external input.

inhibitory neurons (Materials and Methods). A more realistic model with distinct excitatory and inhibitory neuron pools will be shown later. The nDL model consists of Poisson spiking neurons, each receiving Poisson spike trains from all input neurons via a modifiable all-to-all afferent feedforward (FF) connection matrix **W** (Fig. 1a). These input neurons may be grouped into multiple input neuron groups responding to different sensory features. Due to the all-to-all connectivity, the

afferent input has no specific predefined structure. Two types of all-to-all modifiable recurrent connections (REC), $\mathbf{M}$ and $\mathbf{G}$, exist among the neurons. Matrix $\mathbf{M}$ is a mixture of excitatory and inhibitory connections, and matrix $\mathbf{G}$ represents inhibitory-only connections. Due to a minus sign for v^G, all components of $\mathbf{G}$ are positive. The firing rate of neurons are defined as a modifiable sigmoidal function of the membrane potential (Fig.1b), which we will explain later in detail. All types of connections, both afferent and recurrent ones, are modifiable by unsupervised learning rules derived from a common principle: on each neuron, all synapses learn to predict the neuron's response optimally (Fig. 1c: see Materials and Methods). In reality, all synaptic inputs may be terminated on the dendrites, although they are not modeled explicitly.

Without a teaching signal, predictive learning may suffer a trivial solution problem in which all synapses vanish, and hence all neurons become silent (Asabuki & Fukai, 2020). To avoid it, we homeostatically regulate the dynamic range of each neuron (i.e., the slope and threshold of the response function) according to the history h of its subthreshold activity (see Eqs. 10-12). When the value of h is increased, the neuron's excitability is lowered (Fig.1b). The input-output curves of neurons are known to undergo homeostatic regulations through various mechanisms (Chance et al., 2002; Mitchell and Silver, 2003; Torres-Torrelo et al., 2014). Though no direct experimental evidence is available for our homeostatic process via h, it mathematically avoids saturating neuronal activity.

Note that the present homeostatic regulation of intrinsic excitability differs from the homeostatic synaptic scaling mechanism. The role of homeostatic synaptic scaling in generating irregular cell-assembly activity patterns was previously studied computationally (Hiratani and Fukai, 2014; Litwin-Kumar and Doiron, 2014; Zenke et al., 2015). However, unlike the present model, the previous models did not address whether and how synaptic scaling contributes to statistical modeling by recurrent neural networks. Furthermore, unlike our model, in which neurons in the recurrent layer and input neurons are initially connected in an all-to-all manner, most previous models assumed preconfigured receptive fields for recurrent-layer neurons, implying that these models had predefined stimulus-specific cell assemblies.

Cell assembly formation for learning statistically salient stimuli

We first explain how our network segments salient stimuli and forms stimulus-
specific cell assemblies via network-wide predictive learning rules. To this end,
we tested a simple case in which two non-overlapping input groups are intermit-
tently and repeatedly activated with equal probabilities. The two input patterns
were separated by irregular, low-frequency, unrepeated spike trains of all input
neurons (Materials and Methods). We will consider input patterns with unequal
occurrence probabilities later. After several presentations of individual input pat-
terns, each network neuron responded selectively to one of the repeated patterns
(Figure 2a). This result is consistent with our previous results (Asabuki & Fukai,
2020) that the plasticity of feedforward connections segments input patterns. In-
deed, feedforward synapses W on each neuron were strengthened or weakened
when they mediated its preferred or non-preferred stimulus, respectively (Fig. 2b,
left; Fig. 2c). Inhibitory connections G grew between neurons within the same
assembly but not between assemblies (Fig. 2b, right; Fig. 2c, bottom), enhancing
the decorrelation of within-assembly neural activities (Asabuki & Fukai, 2020).
Recurrent connections M were modified to form stimulus-specific cell assemblies,
as evidenced by the self-organization of excitatory (Fig. 2c, top) and inhibitory
(Fig. 2c, bottom) recurrent connections within and between cell assemblies, re-
spectively. The inhibitory components are necessary for suppressing the simulta-
neous replay of different cell assemblies, as shown later.

We then investigated whether and how spontaneous activity preserves and re-
plays these cell assemblies in the absence of afferent input. To demonstrate this
in a more complex task, we trained the network with afferent input involving five
repeated patterns and then removed the input and observed post-training spon-
taneous network activity (Fig. 2d). The termination of afferent input initially low-
ered the activities of neurons, but their dynamic ranges gradually recovered with
the excitability of the neural population (indicated by the population-averaged h
value), and the network eventually started spontaneously replaying the learned
cell assemblies. All plasticity rules were turned off during the recovery period
(about 20 seconds from the input termination), after which the network settled in
a stable spontaneous firing state (plasticity off), with firing rates lower than those
of the evoked activity (inset). Then, the plasticity rules could be turned on (plas-
ticity on) without drastically destroying the structure of spontaneous replay. Intri-
guingly, spontaneous neuronal activities were highly correlated within each cell
assembly but were uncorrelated between different cell assemblies (Fig. 2e). This

was because self-organized recurrent connections **M** were excitatory within
each cell assembly, whereas the between-assembly recurrent connections were
inhibitory, as in Fig. 2c.

Thus, the network model successfully segregates, remembers, and replays stim-
ulus-evoked activity patterns in temporal input. The loss of between-assembly
excitatory connections is interesting as it indicates that the present spontaneous
reactivation is not due to the sequential activation of cell assemblies. This can
also be seen from the relatively long intervals between consecutive cell-assembly
activations: spontaneous neural activity does not propagate directly from

Figure 2. Formation of stimulus-selective assemblies in a recurrent network. (a) Example
dynamics of neuronal output and synaptic predictions are shown before (left) and after (right)
learning. Colored bars at the top of the figures represent periods of stimulus presentations. (b)
Example dynamics of feedforward connection W and inhibitory connection G are shown. W-con-
nections onto neurons organizing to encode the same or different input patterns are shown in red
and blue, respectively. Similarly, the same colors are used to represent G connections within and
between assemblies. (c) Dynamics of the mean connection strengths are shown on neuron in cell
assembly 1. Shaded areas represent SDs. In the schematic, triangles indicate input neurons and
circles indicate network neurons. The color of each neuron indicates the stimulus preference of
each neuron. (d) Example dynamics of the averaged dynamical variable $\bar{h}$ (top) and the learned

network activity (bottom) are shown. The dynamical variables are averaged over the entire network. Neurons are sorted according to their preferred stimuli. During the spontaneous activity, afferent inputs to the network were removed. The inset shows the firing rate distribution of the evoked and the spontaneous activity. (e) Correlation coefficients of spontaneous activities of every pair of neurons are shown.

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one cell assembly to another (Fig. 2d). Indeed, within-assembly excitation is the major cause of spontaneous replay in this model, which we will study later in detail.

In summary, we have proposed the predictive learning rules as a novel plasticity mechanism for all types of synapses (i.e., feedforward and recurrent connections). We have shown that the plasticity rules in our model learn the segmentation of salient patterns in input sequences and form pattern-specific cell assemblies without preconfigured structures. We also showed that our model replays the learned assemblies even when external inputs were removed.

Replays of cell assemblies reflect a learned statistical model

We now turn to the central question of this study. We asked whether internally generated network dynamics through recurrent synapses (i.e., spontaneous replay of cell assemblies) can represent an optimal model of previous sensory experiences. Specifically, we examined whether the network spontaneously reactivates learned cell assemblies with relative frequencies proportional to the probabilities with which external stimuli activated these cell assemblies during learning. We addressed these questions in slightly more complex cases with increased numbers of external stimuli.

We first examined a case with five stimuli in which stimulus 1 was presented twice as often as the other four stimuli (Fig. 3a). Hereafter, the probability ratio refers to the relative number of times stimulus 1 is presented during learning. For instance, the case shown in Fig. 2d represents the probability ratio one. As in Fig. 2d, the network self-organized five cell assemblies to encode stimuli 1 to 5 and replayed all of them in subsequent spontaneous activity (Fig. 3b). We found that output neurons were activated more frequently and strongly in cell assembly 1 than in other cell assemblies. Therefore, we accessed quantitative differences in neuronal activity between different cell assemblies by varying the probability ratio.

The neuronal firing rate of cell assembly 1 relative to other cell assemblies in-
creased approximately linearly with an increase in the probability ratio (Fig. 3c).
Similarly, the size of cell assembly 1 relative to other cell assemblies also in-
creased with the probability ratio (Fig. 3d). However, neither the relative firing rate
nor the relative assembly size faithfully reflects changes in the probability ratio:
scaling the probability ratio with a multiplicative factor does not scale these quan-
tities with this factor. Therefore, we further investigated whether the assembly
activity ratio, the ratio in the total firing rate of cell assembly 1 to other cell assem-
blies (Materials and Methods), scales faithfully with the probability ratio of cell
assembly 1. This was the case: the scaling was surprisingly accurate (Fig. 3e).

304
305 **Figure 3 Priors coded in spontaneous activity.** An nDL network was trained with five probabil-
306 istic inputs. (a) Stimulus 1 appeared twice as often as the other four stimuli during learning. The
307 example empirical probabilities of the stimuli used for learning are shown. (b) The spontaneous
308 activity of the trained network shows distinct assembly structures. (c) The mean ratio of the

To examine the ability of the nDL network further, we trained it with five stimuli
occurring with various probabilities (Fig. 3f and Supplementary Fig. 1a). After
learning, the spontaneous activity of the model replayed the learned cell assem-
blies at the desired ratios of population firing rates (Fig. 3g and Supplementary
Fig. 1b).

We then asked whether our model would learn a prior distribution for more stimuli.
To this end, we presented seven stimulus patterns to the same network with
graded probabilities (Supplementary Fig. 1c). The self-organized spontaneous
activity exhibited cell assemblies that well learned the graded probability distribu-
tion of these stimuli (Supplementary Fig. 1d). These results demonstrate that the
trained network remembers the probabilities of repetitively experienced stimuli by
the spontaneous firing rates of the encoding cell assemblies and that this dynam-
ical coding scheme has a certain degree of scalability.

So far, we have represented external stimuli with non-overlapping subgroups of
input neurons. However, in biologically realistic situations, input neuron groups
may share part of their membership neurons. We tested whether the proposed
model could learn the probability structure of overlapping input patterns in a case
where two input neuron groups shared half of their members. The two patterns
were presented with probabilities of 30% and 70%, respectively (Supplementary
Fig. 2a). After sufficient learning, the network model generated two assemblies
that encoded the two stimuli without sharing the coding neurons (Supplementary
Fig. 2b) and replayed these assemblies with frequencies proportional to the stim-
ulus presentation probabilities (Supplementary Fig. 2c). The results look reason-
able because each neuron in the network segments one of the stimulus patterns
and recurrent connections within each non-overlapping assembly can encode the
probability of its replay.

Altogether, these results suggest that our model spontaneously replays learned
cell assemblies with relative frequencies proportional to the probability that each

349 cell assembly was activated during the learning phase. We have shown that the
350 population activities of assemblies, rather than the firing rates of individual neu-
351 rons, encode the occurrence probabilities of stimulus patterns.

Within-assembly recurrent connections encode probabilistic sensory expe-riences

To understand the mechanism underlying the statistical similarity between the
evoked patterns and spontaneous activity, we then investigated whether and how
biases in probabilistic sensory experiences influence the strengths of recurrent
connections. To this end, we compared two cases in which two input patterns
(stim 1 and stim 2) occurred with equal (50% vs. 50%) and different (30% vs.
70%) probabilities during learning (Fig. 4a). From the results shown in Fig. 3, we
hypothesized that within-assembly learned connections should reflect the stimu-
lus occurrence probabilities and hence the activation probabilities of the corre-
sponding cell assemblies during spontaneous activity. Therefore, we calculated
the total strengths of incoming recurrent synapses on each neuron within the in-
dividual cell assemblies (Fig. 4b). While the distributions of incoming synaptic
strengths are similar between cell assemblies coding stimulus 1 and stimulus 2
in the 50-vs-50 case, they look different in the 30-vs-70 case (Fig. 4c).

Since incoming weights increased more significantly in the cell assembly acti-
vated by a more frequent stimulus (i.e., the assembly encoding stimulus 2 in the
30-vs-70 case), we expect that the degree of positive shifts in incoming weight
distributions will reflect stimulus probabilities. To examine whether this is indeed
the case, we computed the sum of total excitatory incoming weights (i.e., the sum
of positive elements of M) over neurons belonging to each assembly after training.
We then normalized these excitatory incoming weights over the two assemblies.

Figure 4. Probability encoding by learned within-assembly synapses. (a) Two input stimuli were presented in two protocols: uniform (50% vs. 50%) or biased (30% vs. 70%). (b) The total incoming synaptic strength on each neuron was calculated within each cell assembly. (c) *left,* The distributions of incoming synaptic strength are shown for the learned assemblies in the 50-vs-50 case. *right,* Same as in the left figure, but in the 30-vs-70 case. (d) *left,* The empirical probabilities of stimuli 1 and 2 and the normalized excitatory incoming weights within assemblies are compared in the 50-vs-50 case. *right,* Same as in the left figure, but in the 30-vs-70 case.

Interestingly, we found that the normalized excitatory incoming weights for the two assemblies well approximates the empirical probabilities of the two stimuli in both the 50-vs-50 and 30-vs-70 cases (Figure 4d). These analyses revealed that recurrent connections learned within assemblies encode biases in probabilistic sensory experiences. Indeed, the elimination of between-assembly excitatory connections did not significantly affect the replay probabilities, as the sampling is driven by strong within-assembly recurrent inputs after learning (Supplementary Fig. 3).

Roles of inhibitory plasticity for stabilizing cell assemblies

Experimental and computational results suggest that inhibitory synapses are more robust to spontaneous activity than excitatory synapses and are crucial for maintaining cortical circuit function (Mongillo et al., 2018). To see the crucial role of the inhibitory plasticity of G for cell assembly formation, we compared the spontaneously driven activities in the learned network between two cases, plastic inhibitory connection G versus fixed G, in the 30-vs-70 case. The results show that

399 only a single, highly active assembly self-organizes for fixed inhibitory synapses
400 (Supplementary Fig. 4a). In contrast, such unstable dynamics do not emerge from
401 plastic inhibitory synapses (Supplementary Fig. 4b), suggesting the crucial role
402 of inhibitory plasticity in stabilizing spontaneous activity.
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To further clarify the functional role of inhibitory plasticity in regulating spontane-
ous activity, we compared how the self-organized assembly structure of recurrent
connections $\mathbf{M}$ evolves in the two simulation settings shown in Supplementary
Fig. 5a. In the control model, we turned off the plasticity of $\mathbf{G}$ for a while after the
cessation of external stimuli but again switched it on, as was previously in Fig. 2.
The cell-assembly structure initially dissipated but eventually reached a well-de-
fined equilibrium structure (Supplementary Fig. 5b, magenta). Consistent with
this, the postsynaptic potentials mediated by connections $\mathbf{M}$ and $\mathbf{G}$ predicted
the normalized firing rate of a postsynaptic excitatory neuron in the control model
(Supplementary Fig. 5c). In striking contrast, the cell-assembly structure rapidly
dissipated in the truncated model in which the G-plasticity was kept turned off
after the cessation of external stimuli (Supplementary Fig. 5b, blue). Accordingly,
the postsynaptic potentials induced by $\mathbf{M}$ and $\mathbf{G}$, so was the normalized firing
rate, evolved into trivial solutions and almost vanished in the truncated model
(Supplementary Fig. 5d). Only the control model, but not the truncated model,
could maintain prediction errors small and nearly constant after the termination
of the stimuli (Supplementary Fig. 5e). These results indicate that maintaining the
learned representations requires the continuous tuning of within-assembly inhibi-
tion.
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The role of homeostatic regulation of neural activities
As indicated by the weak couplings between cell assemblies, the present mech-
anism of probability learning differs from the conventional sequence learning
mechanisms. Consistent with this, the network trained repetitively by a fixed se-
quence of patterned inputs does not exhibit stereotyped sequential transitions
among cell assemblies (due to the lack of strong inter-assembly excitatory con-
nections; Supplementary Fig. 6). Indeed, the probability-encoding spontaneous
activity emerges in the present model mainly from the within-assembly dynamics
driven by strong within-assembly reverberating synaptic input. However, homeo-
static variable h also plays a role in maintaining a stable spontaneous network
activity after learning (see Fig. 2d; activity pattern from 5 to 10 sec). This is

achieved by the time evolution of h, which maintains the firing rate of each neuron in a suitable range by adjusting the threshold and gain of the somatic sigmoidal response function (Fig. 1b).

Therefore, we explored the role of the homeostatic variable in learning an accurate internal model of the sensory environment. In each neuron, the variable h is updated whenever the membrane potential undergoes an abrupt increase (Eq. 10). Therefore, the time evolution of h monitors the activity of each neuron over the timescale of seconds, which in turn regulates the neural activity by controlling the activation function (Supplementary Fig. 7a; Eqs.8-9). When the instantaneous value of h is high, the neuron's excitability is lowered (namely, the gain and threshold of the response function are decreased or increased, respectively: see Eqs. 10-12). This activity regulation is crucial to avoid the trivial solution of the plasticity rules (Asabuki and Fukai, 2020) but not critical for sampling with appropriate probabilities. Actually, a model with a fixed value of h still showed spontaneous replay, although the true probability distribution was estimated less accurately (Supplementary Fig. 7b: cf. Fig. 3f).

Learning conditioned prior distributions

The predictive coding hypothesizes that top-down input from higher cortical areas provides prior knowledge about computations in lower cortical areas. This implies in the brain's hierarchical computation that the top-down input conditions the prior distributions in local cortical areas to those relevant to the given context. The proposed learning rules can account for how a conditioned input from other cortical areas conditions the prior distribution in a local cortical circuit.

The neural network consists of two mutually interacting non-overlapping subnetworks of equal sizes, where the subnetworks may represent different cortical areas (Supplementary Fig. 8a). Subnetwork A was randomly exposed to stimuli 1 and 2 (S1 and S2) with equal probabilities 1/2, whereas subnetwork B was to stimuli 3 and 4 (S3 and S4) with the conditional probabilities 1/3 and 2/3 if S1 was presented to subnetwork A and the conditional probabilities 2/3 and 1/3 if S2 was presented to subnetwork A. After learning, the network model self-organized four cell assemblies each of which responded preferentially to one of the four stimuli (Supplementary Fig. 8b). Consistent with this, the self-organized connection matrix represented strong within-assembly connections within each cell assembly

and weak between-assembly connections (Supplementary Fig. 8c). Note that be-
tween-assembly connections were inhibitory between assemblies encoding mu-
tually exclusive stimuli, i.e., S1 and S2 and S3 and S4, as they should be. Now,
we turned off S3 and S4 to subnetwork B and only applied S1 or S2 to subnetwork
A each at one time. Applying the same stimulus (i.e., S1 or S2) to subnetwork A
activated either S3- or S4-coding cell assembly in subnetwork B in a probabilistic
manner (Supplementary Fig. 8d). The cell assemblies evoked in subnetwork B
by S1 or S2 to subnetwork A varied the total firing rates approximately in propor-
tion to the conditional probabilities (e.g., $P(S3|S1) = 1/3$ vs. $P(S4|S1) = 2/3$) used
during learning (Supplementary Fig. 8e). Note that S3- and S4-coding cell as-
semblies could become simultaneously active to represent the desired activation
probabilities (e.g., a vertical arrow in Supplementary Fig. 8d). Together, these re-
sults indicate that our network can learn prior distributions conditioned by addi-
tional inputs through different pathways.

Replication of biased perceptual decision making in monkeys
Prior knowledge about the environment often biases our percept of the external
world. For instance, if we know that two possible stimuli exist and that stimulus A
appears more often than stimulus B, we tend to feel that a given stimulus is more
likely to be stimulus A than stimulus B. Previously, a similar bias was quantita-
tively studied in monkeys performing a perceptual decision making task (Hanks
et al., 2011). In the experiment, monkeys had to judge the direction (right or left)
of the coherent motion of moving dots on a display. When both directions of co-
herent motion appeared randomly during learning, the monkey showed unbiased
choice behaviors. However, if the frequencies of the two motion directions were
different, the monkey's choice was biased toward the direction of a more frequent
motion stimulus.

We constructed a network model shown in Fig. 5a to examine whether the pre-
sent mechanism of spontaneous replay could account for the behavioral bias.
The model comprises a recurrent network similar to that used in Fig. 2 and two
input neuron groups, L and R, encoding leftward or rightward coherent dot move-
ments, respectively. We modulated the firing rates of these input neurons in pro-
portion to the coherence of moving dots (Materials and Methods). During learning,
we trained this model with external stimuli having input coherence Coh of either
-0.5 or +0.5 (Materials and Methods), where all dots move leftward in the former
or rightward in the latter. In so doing, we mimicked the two protocols used in the

behavioral experiment of monkeys: in the 50:50 protocol, two stimuli with Coh =
±0.5 were presented randomly with equal probabilities, while in the 80:20 protocol,
stimuli with Coh = +0.5 and -0.5 were delivered with probabilities of 80% and 20%,
respectively. In the 80:20 protocol, stimuli were highly biased toward a coherent
rightward motion.
509
510　The network model could explain the biased choices of monkeys surprisingly
511　well. In either training protocol, the recurrent network self-organized two cell
512　assemblies responding selectively to one of the R and L input neuron groups.
513　Then, we examined whether the responses of the self-organized network are
514　consistent with experimental observations by stimulating it with external inputs

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Figure 5. Simulations of biased perception of visual motion coherence. (a) The network
model simulated perceptual decision-making of coherence in random dot motion patterns. In the
network shown here, network neurons have already learned two assemblies encoding leftward or
rightward movements from input neuron groups L and R. The firing rates of input neuron groups
were modulated according to the coherence level Coh of random dot motion patterns (Materials
and Methods). (b) The choice probabilities of monkeys (circles) and the network model (solid
lines) are plotted against the motion coherence in two learning protocols with different prior prob-
abilities. The experimental data were taken from Hanks et al. (2011). In the 50:50 protocol, moving
dots in the "R" (Coh = 0.5) and "L" (Coh = -0.5) directions were presented randomly with equal
probabilities, while in the 80:20 protocol, the "R" and "L" directions were trained with 80% and
20% probabilities, respectively. Shaded areas represent SDs over 20 independent simulations.
The computational and experimental results show surprising coincidence without curve fitting.
(c) Spontaneous and evoked activities of the trained networks are shown for the 50:50 (left) and
80:20 (right) protocols. Evoked responses were calculated for three levels of coherence: Coh = -
50%, 0%, and 50%. In both protocols, the activity ratio in spontaneous activity matches the prior

probability and gives the baseline for evoked responses. In the 80:20 protocol, the biased priors of "R" and "L" motion stimuli shift the activity ratio in spontaneous activity to an "R"-dominant regime.

having various degrees of input coherence. The resultant psychometric curves almost perfectly coincide with those obtained in the experiment (Fig. 5b). We note that the psychometric curves of the model do not significantly depend on the specific choices of parameter values as far as the network learned stable spontaneous activity. We did not perform any curve fitting to experimental data, implying that the psychometric curves are free from parameter finetuning.

Biases in the psychometric curves emerged from biased firing rates of spontaneous activity of the self-organized cell assemblies. To show this, we investigated how the activities of the two self-organized cell assemblies change before and after the onset of test stimuli in three relatively simple cases, i.e., Coh = -0.5, 0, and +0.5. Figure 5c shows the activity ratio AR between the R-encoding cell assembly and the entire network (Materials and Methods) in pre-stimulus spontaneous and post-stimulus evoked activity. When the network was trained in a non-biased fashion (i.e., in the 50:50 protocol), the activity ratio was close to 0.5 in spontaneous activity, implying that the two cell assemblies had similar activity levels. In contrast, when the network was trained in a biased fashion (i.e., in the 80:20 protocol), the activity ratio in spontaneous activity was close to 0.8, implying that the total spontaneous firing rate of R-encoding cell assembly was four times higher than that of L-encoding cell assembly.   Our results show that the spontaneous activity generated by the proposed mechanism can account for the precise relationship between motion coherence and perceptual biases in decision making by monkeys.

Crucial roles of distinct inhibitory pathways
The model presented so far lacked biological plausibility in several key aspects. Specifically, we assumed that the recurrent connections M could change its sign through plasticity and be either excitatory or inhibitory, while the inhibitory connection G was restricted to being inhibitory only. This setting does not reflect the biological constraint that synapses maintain a consistent excitatory or inhibitory type. Furthermore, due to this unconstrained recurrent connectivity M, the original model had two types of inhibitory connections (i.e., the negative part of M and the inhibitory connection G) without providing a clear computational role for each type of inhibition.

To address these limitations and to understand the role of the two types of inhibition, we considered a novel architecture in which all recurrent connections are constrained to be either exclusively excitatory or inhibitory, maintaining their sign throughout the learning process. The refined model includes two different types of inhibitory connections (i.e., M_{inh} and G), each serving a specific computational purpose: minimizing prediction error and maintaining the excitatory-inhibitory balance. In combination with the excitatory connection M_{exc}, the M_{inh} connections are trained to minimize the prediction error between somatic and dendritic activity, as considered in the original M connection in Figure 1. We found that the trained M_{inh} connections introduce competition among cell assembly activities by forming strong connections between assemblies (Fig. 6b), allowing the network to effectively sample and replay the activities of individual assemblies. In contrast, inhibitory connections G were trained to balance network dynamics, as in the original setting. We found that the inhibitory G connections form strong intra-assembly inhibition (Fig. 6c), which balances the strong excitatory connections that arise within cell assemblies through plasticity (Fig. 6a).

In summary, the dual inhibitory mechanism allows the network to perform the reactivation of different cell assemblies while regulating their internal dynamics. The prediction-error-minimizing inhibitory connections M_{inh} facilitate selecting and activating specific assemblies through competition such that the learned probabilities are replayed. In contrast, the network-balancing inhibitory connections G prevent runaway excitation within active assemblies.

Figure 6. A network model with distinct excitatory and inhibitory connections. (a) Strong excitatory connections were formed within assemblies. (b) The first type of recurrent inhibitory connections, M_{inh}, became stronger between assemblies, enhancing assembly competition. (c) The second type of inhibitory connections G were strengthened within assemblies to

600   balance the strong excitatory inputs.

An elaborate network model with distinct excitatory and inhibitory neuron pools

The predictive learning rule performed well in training the nDL model to learn the probabilistic structure of the stimulus-evoked activity patterns. However, whether the same learning rule works in a more realistic neural network is yet to be investigated. To examine this, we constructed an elaborate network model (DL model) consisting of distinct excitatory and inhibitory neuron pools, obeying Dale's law (Fig. 7a). The nDL model suggested the essential roles of inhibitory plasticity in maintaining excitation-inhibition balance and generating an appropriate number of cell assemblies. To achieve these functions, inhibitory neurons in the DL model project to excitatory and other inhibitory neurons via two synaptic paths (Fig. 7b), motivated by the results shown in Figure 6. In path1, inhibitory connections alone predict the postsynaptic activity, whereas inhibitory and excitatory connections jointly predict the activity of the postsynaptic neuron in path2 (Materials and Methods). All synapses in the DL model are subject to the predictive learning rule. We trained the DL model with three input neuron groups while varying their activation probabilities. As in the nDL model, the DL model self-organized three cell assemblies activated selectively by the three input neuron groups (Supplementary Fig.9a). Furthermore, in the absence of external stimuli, the DL model spontaneously replayed these assemblies with the assembly activity ratios in proportion to the occurrence probabilities of the corresponding stimuli during learning (Fig. 7c).

The two inhibitory paths divided their labors consistent with the results shown in Figure 6. To see this, we investigated the connectivity structures learned by these paths. In path 1, inhibitory connections were primarily found on excitatory neurons in the same assemblies (Fig. 7d, top). In contrast, in path 2, inhibitory connections were stronger on excitatory neurons in different assemblies than those in the same assemblies (Fig. 7d, bottom). On both excitatory and inhibitory neurons, the total inhibition (i.e., path 1 + path 2) was balanced with excitation (Fig. 7e). Figure 7f summarizes the connectivity structure of the DL model. Excitatory neurons in a cell assembly project to inhibitory neurons in the same assembly. Then, these inhibitory neurons project back to excitatory neurons in the same or different assemblies via paths 1 and 2. Interestingly, lateral inhibition through path 1 is more potent between excitatory neurons within each cell assembly than between different assemblies (Fig. 7g). In contrast, path 2 mediates equally strong

637 within-assembly and between-assembly inhibition.
638
639 We can understand the necessity of the two inhibitory paths based on the dynam-
640 ical properties of competitive neural networks. Figure 7h displays the effective
641 competitive network of excitatory cell assemblies suggested by the above results.
642 Both paths 1 and 2 contribute to within-assembly inhibition

643
Figure 7. The DL model of excitatory and inhibitory cell assemblies. (a) This model consists
of distinct excitatory and inhibitory neuron pools, obeying Dale's law. (b) Each inhibitory neuron
projects to another neuron X through two inhibitory paths, path 1 and path 2, where the index X
refers to an excitatory or an inhibitory postsynaptic neuron. Hexagons represent minimal units for
prediction and learning in the neuron model and may correspond to dendrites, which were not
modeled explicitly. (c) The probability ratios estimated by numerical simulations are plotted for the
assembly activity ratios (purple), firing rate ratios (cyan), and assembly size ratios (green) as
functions of the true probability ratio of external stimuli. Error bars indicate SEs calculated over
five simulation trials with different initial states of neurons and synaptic weights in each parameter
setting. (d) Inhibitory connection matrices are shown for path 1 and path 2. (e) The mean weights
of self-organized synapses on excitatory and inhibitory postsynaptic neurons are shown. (f)
Within-assembly and between-assembly connectivity patterns of excitatory and inhibitory neurons
are shown. Colors indicate three cell assemblies self-organized. (g) The strengths of lateral inhi-
bitions within- (W/N) and between-assemblies (B/N) are shown for paths 1 and 2. Horizontal
bars show the medians and quartiles. (h) The resultant connectivity pattern suggests an effective

competitive network between excitatory assemblies with self- (within-assembly) and lateral (between-assembly) inhibition.

among excitatory neurons, whereas between-assembly inhibition (i.e., lateral inhibition) mainly comes from path 2. In a competitive network, the lateral inhibition to self-inhibition strength ratio determines the number of winners having non-vanishing activities: the higher the ratio is, the smaller the number of winners is (Fukai & Tanaka, 1997). Therefore, self-organizing the same number of excitatory cell assemblies as that of external stimuli requires tuning the balance between the within-assembly and between-assembly inhibitions. This tuning during learning is likely easier when the network has two independently learnable inhibitory circuits. Indeed, a network model with only one inhibitory path rarely succeeded in encoding and replaying all stimuli used in learning (Supplementary Fig. 9b, c).

In summary, we have shown the roles of distinct recurrent inhibitory connections. Using a network consisting of excitatory and inhibitory populations, we have shown that distinct inhibitory circuits are necessary to generate within- and between-assembly competition crucial to maintain the stability of learned multiple assemblies.

Discussion

Having proper generative models is crucial for accurately predicting statistical events. The brain is thought to improve the prediction accuracy of inference by learning internal generative models of the environment. These models are presumably generated through multiple mechanisms. For instance, the predictive coding hypothesizes that top-down cortical inputs provide lower sensory areas with prior information about sensory experiences (Friston, 2010; Bastos et al., 2012; Keller & Mrsic-Flogel, 2018). However, experimental evidence also suggests that spontaneous activity represents an optimal model of the environment in sensory cortices. This study proposed a biologically plausible mechanism to learn such a model, or priors for experiences, with the brain's internal dynamics.

Our model adopted a single predictive learning principle for the plasticity of excitatory and inhibitory synapses to learn the replay of probabilistic experiences. On each neuron, excitatory and inhibitory synaptic weights undergo plastic changes to improve their independent predictions on the cell's firing. This was done by

minimizing the mismatch between the output firing rate and the network predictions(Eqs. 13 and 17). This simple learning rule showed excellent performance in a simplified network model and in a more realistic model obeying Dale's law. The latter model predicts a division of labor between two inhibitory paths. Intriguingly, the inhibitory path 2 of this model resembles interpyramidal inhibitory connections driven directly by nearby pyramidal cells (Ren et al., 2007). In both models, inhibitory synaptic plasticity plays a crucial role in learning an accurate internal model by maintaining excitation-inhibition balance and decorrelating cell-assembly activities (Vogels et al., 2013; Sprekeler, 2017). It should be noted that while several network models that perform error-based computations like ours exploit only inhibitory recurrent plasticity (Mikulasch et al., 2021; Mackwood et al., 2021; Hertäg and Clopath., 2022; Mikulasch et al., 2023), our model learns to reproduce appropriate statistics by modifying both excitatory and inhibitory recurrent connections.

Various models have been proposed to account for neural mechanisms of Bayesian computation by the brain (Tully et al., 2014; Kappel et al., 2015; Hiratani & Fukai, 2018; Hiratani & Latham, 2020; Aitchison et al., 2021; Ma et al., 2006; Deneve, 2008; Nessler et al., 2013; Hiratani & Fukai, 2016; Huang & Rao, 2016; Isomura et al., 2022; Friston, 2010; Bastos et al., 2012; Keller & Mrsic-Flogel, 2018). Typically, these models embed prior knowledge on sensory experiences into the wiring patterns of afferent (and sometimes also recurrent) synaptic inputs such that these inputs can evoke the learned activity patterns associated with the prior knowledge. The present model differs from the previous models in several aspects: i) First, the model segments repeated stimuli to be remembered in an unsupervised fashion; ii) Then it generates cell assemblies encoding the segmented stimuli; (iii) Finally, it replays these cell assemblies spontaneously with learned probabilities. Note that the same learning rules enable the network to perform all necessary computations for (i) to (iii). To our knowledge, our model is the first to perform all these steps for encoding an optimal model of the environment into spontaneous network activity.

The present mechanism of memory formation differs from the previous ones that self-organize cell assemblies through Hebbian learning rules (Vogels et al., 2011; Hiratani and Fukai, 2014; Litwin-Kumar and Doiron, 2014; Zenke et al., 2015; Triplett et al., 2018; Montangie 2020). Firstly, these mechanisms did not aim for

explicit statistical modeling of the environment. Secondly, the previous studies suggested that the orchestration of multiple plasticity rules, including inhibitory plasticity and homeostatic synaptic scaling, enables the maintenance of cell assemblies (however, see Manz et al., 2023). For instance, in spike-timing-dependent plasticity (STDP), slight changes in the relative times of pre and postsynaptic spikes can change the polarity of synaptic modifications, implying that STDP requires a mechanism to keep synaptic weights finite (Kempter et al., 1999; Song et al., 2000; Masquelier et al., 2008). In contrast, our learning rule, which induces either long-term potentiation or depression according to the sign of the prediction error calculated independently within each postsynaptic neuron, does not suffer such instability.

Our model predicts a novel intracellular process that regulates the neuron's dynamic range according to the history of its subthreshold dynamics. This process plays two important roles in the statistical modeling of our model. First, it avoids the trivial solution (i.e., the zero-weight solution) of our unsupervised predictive learning by homeostatically regulating neurons' intrinsic excitability. Second, the intracellular process cooperates with reverberating synaptic inputs within each cell assembly to generate spontaneous replay activity. We have shown that the intracellular homeostasis enhances the sampling from learned distribution without relying on the recurrences among assemblies. This mechanism contrasts with the previous sampling-based models that rely on the transition dynamics between cell assemblies (Buesing et al., 2011; Bill et al., 2015). How neural systems implement the proposed homeostasis is an open question.

Previous computational models have demonstrated that recurrent networks with Hebbian-like plasticity can learn appropriate Markovian statistics (Kappel et al., 2014; Asabuki and Clopath, 2024). However, our model differs conceptually from these previous models. Kappel et al. showed that STDP in winner-take-all circuits can approximate online learning of hidden Markov models (HMMs). A key difference with our model is that their neural representations acquire sequences using Markovian sampling dynamics, whereas our model does not depend on such ordered sampling. Specifically, in their model, sequential sampling arises from the off-diagonal elements learned in the recurrent connections (i.e., between-assembly connections). In contrast, our network learns to generate a stochastic reactivation of cell assemblies solely by within-assembly connections. A similar

argument can be made for Asabuki and Clopath paper as well. Further, while our
model introduced plasticity   at all types of synaptic connections,   the previous
model assumed plasticity only at recurrent synapses projecting onto the excita-
tory neurons. In addition, unlike our model, the cell assembly memberships need
to be preconfigured in the previous model.

The proposed mechanism can account for the behavioral biases observed in per-
ceptual decision making (Hanks et al., 2011). This behavioral experiment quanti-
tatively clarified how the difference in the probability between sensory experi-
ences during learning biases the alternative choice behavior of monkeys. In our
model, two cell assemblies encoding the different stimuli are replayed at the total
firing rates proportional to the corresponding occurrence probabilities. Our results
suggest that the difference in spontaneous firing rates of cell assemblies is suffi-
cient to explain the behavioral biases of monkeys. However, other mechanisms,
such as biased top-down input, cannot be excluded.

What could be the advantages of coding prior distributions into spontaneous ac-
tivity over other ways of probability coding? First, spontaneous replay activities in
lower cortical areas may provide training data for modeling by higher cortical ar-
eas, promoting hierarchical statistical modeling in predictive coding. This is anal-
ogous to the situation where hippocampal engram cells are replayed to reinforce
the activity patterns of cortical engrams for memory consolidation during sleep
(Tonegawa et al., 2018; Ghandour et al., 2019; Klinzing et al., 2019; Takehara-
Nishiuchi, 2021). Memory reinforcement by activity replay has also been studied
in machine intelligence (Dayan et al., 1995; Goodfellow et al., 2014; Luczak et al.,
2022). Second, spontaneous replay of internal models may support knowledge
generalization during sleep. It was recently reported that a transitive inference
task requires post-learning sleep (Kareem et al., 2021). In this task, mice had to
infer a correct reward delivery rule in a novel behavioral situation from the out-
comes of past experiences. The mice failed to generalize the learned rules if the
activity of the anterior cingulate cortex was suppressed during post-learning sleep,
suggesting that dynamic interactions among rule-coding cortical neurons in spon-
taneous activity are crucial for rule generalization. Clarifying how spontaneous
brain activity generalizes the learned internal models is an intriguing open ques-
tion.

Methods

The source codes used in this study are available at:

https://github.com/TAsabuki/PriorNet_codes

Neural network model

Below, we first describe the model architecture and learning rule for the nDL model (i.e., single population violating the Dale's law). Details of simulation of distinct excitatory and inhibitory populations will be explained later. Unless otherwise stated, recurrent neural networks used in this study consist of $N(=500)$ Poisson neurons, which generate spikes according to a non-stationary Poisson process with rate $\hat{\varphi}(u)$, where $\hat{\varphi}(\cdot)$ is a dynamics sigmoidal function, which we will explain later. The membrane potential u of neuron i at time t is given as follows:

$$u_i(t) = \sum_{k=1}^{K} W_{ik} x_k(t) + \sum_{k=1}^{N} (M_{ik} - G_{ik}) y_k(t), \tag{5}$$

where K is the number of input neurons. In some simulations, the network model had more than one input neuron group although the number of input neuron groups is not explicitly shown in Eq. 5. Three matrices $\mathbf{W} \in \mathbb{R}^{N \times K}$, $\mathbf{M} \in \mathbb{R}^{N \times N}$, and $\mathbf{G} \in \mathbb{R}^{N \times N}$ represent the weights of afferent synaptic connections, recurrent synaptic connections and inhibitory-only connections, respectively, on neurons in the recurrent network. These synaptic connections are all-to-all. In terms of the kernel function

$$\varepsilon(s) = \exp(-s/\tau) \cdot \Theta(s), \tag{6}$$

recurrent input and afferent input to neuron i are calculated as

$$x_i(t) = \sum_{t' \in t_{\mathrm{aff}}^{\mathrm{f}}} \varepsilon(t - t'), \tag{7a}$$

$$y_i(t) = \sum_{t' \in t_{\mathrm{rec}}^{\mathrm{f}}} \varepsilon(t - t'), \tag{7b}$$

where τ stands for the membrane time constant, $t_{\mathrm{aff}}^{\mathrm{f}}$ and $t_{\mathrm{rec}}^{\mathrm{f}}$ for the time sets of afferent and recurrent presynaptic spikes, and $\Theta(\cdot)$ for the Heaviside function.

836   Throughout this study, τ = 15 ms.

838   The instantaneous firing rate $f_i(t)$ of each neuron is given as

840
$$f_i(t) = \hat{\varphi}(u_i(t); h_i), \tag{8}$$

842   in terms of a dynamical sigmoidal response function $\hat{\varphi}$:

844
$$\hat{\varphi}(u_i; h_i) = \varphi_0\left[1 + \exp[g\beta(h_i)(-u_i + g\theta(h_i))]\right]^{-1}, \tag{9}$$

846   with a constant value of $g = 3$ and we have dropped the explicit time depend-
847   ence in our notation for the sake of simplicity. Here, the dynamical variable h is
848   determined by the history of the membrane potential:

850
$$\begin{aligned} \dot{h}_i &= -\tau_h{}^{-1}h_i, && \text{if } h_i > u_i, \\ h_i &\leftarrow u_i, && \text{otherwise.} \end{aligned} \tag{10}$$

852   The maximum instantaneous firing rate φ_0 is 50 Hz and $\tau_h = 10$ s. Through Eq.
853   10, h_i tracks the maximum value of the membrane potential u_i in a time window
854   of approximately the length τ_h in the immediate past. The value of h is utilized
855   to regulate the gain β and threshold θ of the sigmoidal response function as
856   follows:

858
$$\beta(h_i) = h_i{}^{-1}\beta_0 , \tag{11}$$

860
$$\theta(h_i) = h_i\theta_0 , \tag{12}$$

where the values of constant parameters are $\beta_0 = 5$, and $\theta_0 = 1$. Neuron i gen-
erates a Poisson spike train at the instantaneous firing rate of $f_i(t)$. While a small
value of h leads to a steep slope of our activation function (Eq. 11), we have
shown numerically that this does not lead to a problem in neural dynamics. Fur-
ther, the saturation part of the sigmoidal function is crucial for stable formation of
assemblies.

Learning rules

We first explain the plasticity rule for feedforward connections. Synaptic connec-
tions were modified to minimize the Kullback–Leibler divergence (KL-divergence)
between two Poisson distributions associated with the neuron's output and the
feedforward activity over a sufficiently long period T:

874
$$\mathcal{L}_W = \int_0^T dt \sum_{i=1}^N D_{KL}\big[f_i(t)||\varphi(\mathrm{v}_i^W(t))\big], \qquad (13)$$

875 where v_i^W is a feedforward prediction of a firing rate, defined as:
876
$$\mathrm{v}_i^W = \sum_{j=1}^K W_{ij} \cdot x_j, \qquad (14)$$

877 and f_i is the firing rate of i-th neuron. The function φ is a static sigmoidal func-
878 tion, defined as:

879
$$\varphi(\mathrm{v}_i) = \varphi_0\big[1 + \exp[g\beta_0(-\mathrm{v}_i + g\theta_0)]\big]^{-1}. \,(15)$$

880 The above cost function evaluates to what extent the feedforward potential pre-
881 dicts the activity of postsynaptic neurons (Asabuki and Fukai, 2020). We have
882 previously shown that taking the gradient of the cost function in Eq.13 derives the
883 online plasticity rule for the feedforward connections as:

887
$$\Delta W_{ij} = \eta\varphi_0^{-1}\left(1 - \frac{\varphi(\mathrm{v}_i^W)}{\varphi_0}\right)\big[f_i - \varphi(\mathrm{v}_i^W)\big], \quad (16)$$

884 where ϵ is a learning rateand was set to $\epsilon = 10^{-4}$, unless otherwise specified.
885 Here, we have dropped the explicit time dependence in our notation for the sake
886 of simplicity.
888
889 Similarly, the recurrent connections were modified to minimize the following cost
890 function:

891
$$\mathcal{L}_M = \int_0^T dt \sum_{i=1}^N D_{KL}\big[f_i(t)||\varphi(\mathrm{v}_i^M(t))\big], \,(17)$$

892 where $\mathrm{v}_i^M = \sum_{j=1}^N M_{ij} \cdot y_j$ is a recurrent prediction. Similar to the feedforward
893 plasticity, the gradient descent of the above cost function leads to the following
894 plasticity rule:

895
$$\Delta M_{ij} = \eta\varphi_0^{-1}\left(1 - \frac{\varphi(\mathrm{v}_i^M)}{\varphi_0}\right)\big[f_i - \varphi(\mathrm{v}_i^M)\big]. \,(18)$$

896 The derived recurrent plasticity rule suggests that the recurrent prediction learns
897 the statistical model of the evoked activity, which in turn allows the network to
898 replay the learned internal model.
899

900 In addition to the above plasticity rules, we defined the cost function for the inhib-
901 itory plasticity as:

$$\mathcal{L}_G = \sum_{i=1}^{N}\bigl[f_i(t) - \varphi(v_i^G(t))\bigr]^2, \qquad (19)$$

903 where v_i^G is the inhibitory input onto postsynaptic neuron via inhibitory connec-
904 tion G:

$$v_i^G = \sum_{j=1}^{N} G_{ij} \cdot y_j. \qquad (20)$$

906 Again, by taking the gradient of $\mathcal{L}_G$ with respect to G_{ij} derive the following in-
907 hibitory plasticity rule to keep the network dynamics balanced:

$$\Delta G_{ij} \propto -\frac{\partial \mathcal{L}_G}{\partial G_{ij}}$$

$$\propto \bigl[f_i - \varphi(v_i^G)\bigr] \times \frac{\partial \varphi(v_i^G)}{\partial G_{ij}}$$

$$\propto \varphi(v_i^G)\left(1 - \frac{\varphi(v_i^G)}{\varphi_0}\right) \cdot \bigl[f_i - \varphi(v_i^G)\bigr] \cdot y_j. \quad (21)$$

911 While the resultant rule is not the same as feedforward and recurrent plasticity
912 rules, all of these rules are similar in a sense that the weight updates are propor-
913 tional to the prediction error and the presynaptic activity. We therefore assumed
914 the following rule for the inhibitory plasticity, which has the same structure with
915 the rest of the plasticity rules that we have already explained:

$$\Delta G_{ij} = \eta \varphi_0^{-1}\left(1 - \frac{\varphi(v_i^G)}{\varphi_0}\right)\bigl[f_i - \varphi(v_i^G)\bigr]. \quad (22)$$

We have shown by numerical simulation that the rule keeps the network dynam-
ics balanced.

Initial values of $\mathbf{W}$ and $\mathbf{M}$ are sampled from gaussian distributions with the
mean 0 and variances $0.1/\sqrt{K}$ and $0.1/\sqrt{N}$, respectively. During learning, the el-
ements of $\mathbf{W}$ and $\mathbf{M}$ can take both positive and negative values. After sufficient
learning, the postsynaptic potentials v_i^W and v_i^M on neuron on neuron i con-
verge to a common value of v_i^*. Therefore, $\varphi(v_i^W) \approx \varphi(v_i^M) \approx \varphi(v_i^*) \approx f_i$, imply-
ing that the postsynaptic potentials of afferent and recurrent synaptic inputs to
neuron i can both predict its output f_i after learning. The initial values of $\mathbf{G}$ are
uniformly set to $1/\sqrt{N}$, and its elements are truncated to non-negative values
during learning. This implies that v_i^G does not become negative. After learning,
$\varphi(v_i^G) \approx f_i$ is satisfied. Although some elements of $\mathbf{M}$ may give recurrent inhibi-
tory connections, modifiable connections in $\mathbf{G}$ are necessary to encode all

external inputs into specific cell assemblies.

Stimulation protocols

Feedforward input to the recurrent network consisted of K Poisson spike trains
with a background firing rate of 2Hz. The input randomly presented n non-over-
lapping patterns of 100 spike trains (the duration 100 ms and the mean frequency
50 Hz), one at a time, with pattern-to-pattern intervals of 100 ms. Therefore, the
number of input neurons and patterns satisfy the relationship of $K = 100 \times n$. For
simplicity, we simulated the constant-interval case, but using irregular intervals
does not change the essential results. The value of n varies from task to task,
and the values for each figure are as follows: $n = 5$ (Fig. 2c-e, Fig. 3, Fig. 6);
$n = 2$ (Fig. 2a-b, Figs. 4-5); $n = 3$ (Fig. 7). The typical time length required for
the convergence of learning is 1,000 s.

Measures for cell assembly activities

946 Here, we explain the measures used in Fig. 3. We calculated the firing rate ratio
947 of cell assembly 1 in Fig. 3c as follows:

948
$$\text{Firing rate ratio} = \frac{r_i^{(1)}}{\left(\Sigma_{j=2}^{5}\frac{1}{N_j}\Sigma_{i=1}^{N_j} r_i^{(j)}\right)/4} \ , \tag{23}$$

949 using the average firing rate $r_i^{(j)}$ of the i-th neuron in cell assembly j and the
950 number N_j of neurons belonging to the cell assembly. Similarly, we defined the
951 assembly size ratio of cell assembly 1 as

952
$$\text{Assembly size ratio} = \frac{N_1}{\left(\Sigma_{j=2}^{5} N_j\right)/4} \ . \tag{24}$$

953 in Fig.3d and assembly activity ratio of cell assembly 1 as

954
$$\text{Assembly activity ratio} = \frac{r_{\text{pop}}^{(1)}}{\left(\Sigma_{i=2}^{5} r_{\text{pop}}^{(i)}\right)/4} \ , \tag{25}$$

955 in Fig. 3e. Here, $r_{\text{pop}}^{(i)}$ represents the population neural activity of cell assembly

956 i:

957
$$r_{\text{pop}}^{(j)} \equiv \Sigma_{i=1}^{N_j} r_i^{(j)}. \tag{26}$$

Simulations of perceptual decision making

In each learning trial, we trained the network with either leftward or rightward dot

movement represented by the corresponding input neurons firing at $r_{\max} = 50$
Hz. In test trials, we defined input coherence as $\text{Coh} = \rho_R - 0.5$ according to
Hanks et al. (2011), where ρ_R is the ratio of R input neurons to the sum of R and
L input neurons in firing rate. The value of Coh ranges between -0.5 (all dots
moving leftward) and +0.5 (all dots moving rightward). Then, in test trials for input
coherence Coh, we generated Poisson spike trains of R and L input neurons at
the rates $(\text{Coh} + 0.5)r_{\max}$ and $(-\text{Coh} + 0.5)r_{\max}$, respectively.

In Fig. 5c, we calculated the activity ratio (AR) as

$$\text{AR} = \frac{r_R^{\text{pop}}}{r_R^{\text{pop}} + r_L^{\text{pop}}}, \tag{27}$$

971 where r_R^{pop} and r_L^{pop} represent the average population firing rates of R-encod-
972 ing and L-encoding cell assemblies, respectively. In Fig. 5b, we defined "choices
973 to right" as

$$\text{Choices to right} = \text{AR} \times 100 \ (\%). \tag{28}$$

976 **A network model with distinct excitatory and inhibitory synapses**
977 Here, we explain the network model and the plasticity rules used in Figu. 6. The
978 network consists of 500 neurons and the membrane potential of a neuron i at
979 time t is given as follows:

$$u_i^{\square}(t) = \underbrace{\sum_{k=1}^{K} W_{ik}^{\square} x_k(t)}_{=:v_i^W} + \underbrace{\left[\sum_{n=1}^{N} M_{in}^{\text{exc}} y_n^{\square}(t)\right]}_{=:v_i^{M(\text{exc})}} - \underbrace{\left[\sum_{n=1}^{N} M_{in}^{\text{inh}} y_n^{\square}(t)\right]}_{=:v_i^{M(\text{inh})}}$$

$$- \underbrace{\sum_{n=1}^{N} G_{in}^{\square} y_n^{\square}(t)}_{=:v_i^G}, \tag{29}$$

where $\{W_{ik}^{\square}\}$ is afferent synaptic weights, which are a mixture of excitatory and
inhibitory connections as in the nDL model. The weights of recurrent excitatory
synapses are $\{M_{in}^{\text{exc}}\}$. Here, we considered two types of recurrent inhibitory con-
nections, denoted by $M_{\square}^{\text{inh}}$ and G, respectively. Here, we assumed that half of
the recurrent connections were assumed to be excitatory and the remaining con-
nections were all inhibitory, half of which were $M_{\square}^{\text{inh}}$ and the other half were G.
We modified these weights according to the following equations:

$$\Delta W_{ij}^{\square} = \eta \mathcal{E}(f_i, v_i^W) x_j, \tag{30a}$$

$$\Delta M_{ij}^{\text{exc}} = \eta \mathcal{E}\left(f_i, v_i^{M(\text{exc})} - v_i^{M(\text{inh})}\right) y_j^{\square}, \tag{30b}$$

992
$$\Delta \mathrm{M}_{ij}^{\mathrm{exc}} = -\eta \mathcal{E}\left(f_i, \mathrm{v}_i^{\mathrm{M(exc)}} - \mathrm{v}_i^{\mathrm{M(inh)}}\right) y_j^{\square}, \qquad (30c)$$

993
$$\Delta \mathrm{G}_{ij}^{\square} = \eta \mathcal{E}(f_i, \mathrm{v}_i^{\mathrm{G}}) y_j^{\square}, \qquad (30d)$$

994 where $\mathcal{E}(f_i, \mathrm{v}_i^{\square})$ is the error term defined as:

995
$$\mathcal{E}(f_i, \mathrm{v}_i^{\square}) = \varphi_0^{-1}\left(1 - \frac{\varphi(\mathrm{v}_i^{\square})}{\varphi_0}\right)[f_i - \varphi(\mathrm{v}_i^{\square})]. \qquad (31)$$

At each time step during learning, we truncated all weights of recurrent connec-
tions to non-negative values during learning.

A network model with distinct excitatory and inhibitory neuron populations
Here, we explain the architecture of the model used in Fig. 7. The network con-
sists of $N_E (= 500)$ excitatory and $N_I (= 500)$ inhibitory neurons. The membrane
potential of a neuron i of a population X (= E or I) at time t is given as follows:

1003

1004
$$u_i^{\mathrm{X}}(t) = \underbrace{\sum_{k=1}^{K} \mathrm{W}_{ik}^{\mathrm{X}} x_k(t)}_{=:\mathrm{v}_i^{\mathrm{W}}} + \underbrace{\left[\sum_{l=1}^{N_E} \mathrm{M}_{il}^{\mathrm{XE}} y_l^E(t) - \sum_{m=1}^{N_I} \mathrm{G}_{im}^{\mathrm{XI\,(path2)}} y_m^I(t)\right]}_{=:\mathrm{v}_i^{\mathrm{M(2)}}}$$

1005
$$\underbrace{- \sum_{m=1}^{N_I} \mathrm{G}_{im}^{\mathrm{XI\,(path1)}} y_m^I(t)}_{=:\mathrm{v}_i^{\mathrm{M(1)}}}, \qquad (32)$$

1006

where $\{\mathrm{W}_{ik}^{\mathrm{X}}\}$ is afferent synaptic weights, which are a mixture of excitatory and
inhibitory connections as in the nDL model. The weights of recurrent excitatory
synapses are $\{\mathrm{M}_{il}^{\mathrm{XE}}\}$. Here, we considered two types of recurrent inhibitory con-
nections (i.e., path 1 and path 2), denoted by $\mathrm{G}_{im}^{\mathrm{XI\,(path1)}}$ and $\mathrm{G}_{im}^{\mathrm{XI\,(path2)}}$, respec-
tively. Using the same definitions of the error term as in Eq. 31, we modified these
weights according to the following equations:

1013
$$\Delta \mathrm{W}_{ij}^{\mathrm{X}} = \eta \mathcal{E}(f_i, \mathrm{v}_i^{\mathrm{W}}) x_j, \qquad (33a)$$

1014
$$\Delta \mathrm{M}_{ij}^{\mathrm{XE}} = \eta \mathcal{E}\left(f_i, \mathrm{v}_i^{\mathrm{M(2)}}\right) y_j^E, \qquad (33b)$$

1015
$$\Delta \mathrm{G}_{ij}^{\mathrm{XI\,(path2)}} = -\eta \mathcal{E}\left(f_i, \mathrm{v}_i^{\mathrm{M(2)}}\right) y_j^I, \qquad (33c)$$

1016
$$\Delta \mathrm{G}_{ij}^{\mathrm{XI\,(path1)}} = \eta \mathcal{E}\left(f_i, \mathrm{v}_i^{\mathrm{M(1)}}\right) y_j^I. \qquad (33d)$$

1017 To satisfy the Dale's law, we truncated all weights of recurrent connections to non-

1018 negative values during learning.

1019

1020 In Fig. 7g, we measured the lateral inhibition between excitatory neurons via path

1021 1 by calculating:

$$\left[W_{i,j}^{\text{LI}}\right] = \sum_{k=1}^{N_E} G_{ik}^{\text{EI (path1)}} M_{kj}^{\text{IE}}. \qquad (34)$$

1023 Lateral inhibition via path 2 was calculated in a similar fashion.

1024

Simulation details

1026 All simulations were performed in customized Python3 code written by TA with

1027 numpy 1.17.3 and scipy 0.18. Differential equations were numerically integrated

1028 using a Euler method with integration time steps of 1 ms.

1029

Author Contributions: T.A. and T.F. conceived the study and wrote the paper.

1031 T.A. performed the simulations and data analyses.

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