Gene-level alignment of single cell trajectories informs the progression of *in vitro* T cell differentiation

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Abstract:

Single cell data analysis can infer dynamic changes in cell populations, for example across
time, space or in response to perturbation. To compare these dynamics between two
conditions, trajectory alignment via dynamic programming (DP) optimization is frequently
used, but is limited by assumptions such as a definite existence of a match. Here we describe
Genes2Genes, a Bayesian information-theoretic DP framework for aligning single-cell
trajectories. **Genes2Genes** overcomes current limitations and is able to capture sequential
matches and mismatches between a reference and a query at single gene resolution,
highlighting distinct clusters of genes with varying patterns of gene expression dynamics.
Across both real life and simulated datasets, **Genes2Genes** accurately captured different
alignment patterns, and revealed that T cells differentiated *in vitro* matched to an immature *in*
vivo state while lacking the final TNFα signaling. This use case demonstrates that precise
trajectory alignment can pinpoint divergence from the *in vivo* system, thus providing an
opportunity to optimize *in vitro* culture conditions.

Introduction

Recent advances in single-cell genomics, the mainstay of which is single-cell RNA sequencing (scRNA-seq), have revolutionized our understanding of biology and opened up new avenues of research[1]. With their single-cell resolution and ability to observe thousands of genes simultaneously, these new technologies enable the identification of transition cell states and the study of dynamic cellular processes (e.g. cell differentiation/development; cellular response to perturbations). The computational task of deriving a 'timeline' for each dynamic process (e.g. based on transcriptomic similarity) is referred to as 'pseudotime trajectory inference'[2]. The next challenge is to then compare and align two (or more) trajectories, as when exploring similarities between *in vitro* cell differentiation and *in vivo* cell development, or the perturbation responses in control groups *versus* drug treatment groups (**Fig. 1a**). The benefit is obvious; for instance, identifying genes that differ between *in vitro* and *in vivo* systems can guide us to refine *in vitro* cell differentiation. Trajectory comparison poses a time series alignment problem which is dynamic programmable[3]. The goal is to find an optimal set of pairwise sequential correspondences between two trajectories.

Currently, dynamic time warping (DTW) is often used to align two single-cell trajectories. Several notable attempts[4–9], such as CellAlign[5], employ DTW to identify correspondences between two different profiles, allowing the detection of timing differences in biologically similar processes[10]. Current practice is to interpolate the gene expression time series prior to DTW, and then minimize the Euclidean distance of expression vectors between the matched time points to find an optimal alignment. While DTW is a powerful approach with numerous uses, we are motivated to overcome its main limitations, i.e., (1) requiring every time point in each trajectory to match with at least one time point in the other (capturing time-warps only); (2) disregarding missing data or substantial differences between two series, occurring in the form of insertions or deletions (indels); and (3) using a distance metric which relies only on the difference of mean expression, without considering their distributions. We specifically address these by developing a new DP framework that formally handles matches and mismatches in a principled way. It overcomes the need to impose any ad hoc thresholds[5] and/or post hoc processing of a DTW output[11] to capture differential regions in gene expression.

Warps and indels are fundamentally distinct (**Fig. 1b,c**). This is particularly highlighted in discussions about integrating DTW with the gap concept[12,13] (as in the area of biological sequence alignment[14,15]). Both matches and mismatches inform our understanding of temporal gene expression dynamics. A mismatch could either imply missing data or differential expression, which could be interesting to investigate further. For instance, a sudden rise or drop in expression of one system relative to the other might indicate that it is transitioning through a different cell state. A mismatch also occurs when a considerable fraction of cells in one system have a significantly different expression for some genes compared to that of the other, causing distributional differences. This is particularly clear when iPSC-derived organoid trajectories are compared to *in vivo* references, due to the upregulation of pluripotency markers in early stages of organoid development. On the other

hand, warps occur due to the differences in the relative speeds of cell maturation in diverse contexts. Matching and mismatching can also inform divergence and convergence patterns in expression (e.g. **Fig. 1d**), allowing their computational separation for further downstream analysis.

Here we present Genes2Genes (G2G; **Fig. 2**), a novel framework for aligning single-cell transcriptomic trajectories of a reference and query system at single-gene resolution. G2G utilizes a DP alignment algorithm that accounts for matches, warps and indels by combining the classical Gotoh's biological sequence alignment algorithm[15] and DTW[16]. It is inspired by the concepts discussed in the related literature[17–19], and employs a new Bayesian information-theoretic measure based on minimum message length inference[20–22] to quantify the distance between two gene expression distributions assumed to be Gaussian. G2G facilitates: (1) generating descriptive pairwise alignments at gene-level, (2) identifying gene clusters of similar alignment patterns, (3) identifying genes with differential dynamic expression profiles, (4) exploring associated biological pathways, and (5) deriving an aggregate alignment across all or a subset of genes.

We first validate G2G's ability to accurately align and capture different patterns using simulated datasets. We further demonstrate how G2G captures mismatches and offers gene-level alignment, through benchmarking against related methods on a published real dataset[23] and a simulated negative control[11]. We next show how G2G quantitatively assesses the progression of *in vitro* human T-cell differentiation in an in house cultured artificial thymic organoid (ATO) compared to an *in vivo* reference of human T cell development. We find that the TNFα signaling pathway in the final stage of *in vivo* T cell maturation is not recapitulated *in vitro*, and identify potential transcription factors for optimizing *in vitro* cell engineering.

Results

Genes2Genes (G2G) aligns single-cell trajectories with dynamic programming, employing a Bayesian information-theoretic measure

Dynamic programming (DP) remains central to many sequence alignment algorithms. G2G is a new DP framework to infer and analyze gene trajectory alignments between a single-cell reference and query. Given a reference sequence R (a time series with time points: $R_1, R_2, \ldots R_j, \ldots R_{|R|}$) and query sequence Q (a time series with time points: $Q_1, Q_2, \ldots Q_j, \ldots Q_{|Q|}$), a computational alignment between them can inform us of the one-to-one correspondences (matches), one-to-many/many-to-one correspondences (expansion/compression warps) and mismatches (insertions and deletions) between their time points in linear order (**Fig. 1b**). A general DP algorithm finds their optimal alignment by constructing a pairwise alignment cost matrix and generating the optimal path with the minimum cost (**Fig. 1c**). This relies on a scoring scheme to quantify correspondences between every pair of R and Q time points.

Unlike the current DP alignment approaches (i.e. DTW and DNA/protein alignment), G2G

implements a DP algorithm that handles both matches (including warps) and mismatches

jointly, and runs it between the reference and query for each gene. This algorithm extends

Gotoh's three-state sequence alignment algorithm[15] to five-states (**Fig. 1b**) for

accommodating warps. Our DP scoring scheme incorporates a Bayesian information-

theoretic cost function based on the minimum message length (MML) inference[20–22] (top left

of **Fig. 2, Supplementary Fig. 1**), and the state transition probabilities from a five-state

probabilistic finite state machine (**Extended Data Fig. 1**). The MML criterion allows us to

compute a cost for matching any reference time point R_j and query time point Q_i based on

their corresponding gene expression distributions. It evaluates their distributional differences

in terms of both mean and variance, acknowledging that one trajectory may be noisier than

the other. The five-state machine allows us to compute a cost of assigning an alignment state

for R_j and Q_i out of the five possible states of alignment.

Overview of the G2G framework

The G2G framework is composed of several components to support single-cell trajectory

comparison, which include input preprocessing, DP alignment algorithm, alignment

clustering and downstream analysis (**Fig. 2**). It takes the input as log1p normalized single-cell

gene expression matrices of a reference system and a query system, and their pseudotime

estimates. G2G then performs interpolation to smoothen each gene expression trajectory.

This first min-max normalizes the pseudotime axis over which we take a predefined number

of equispaced interpolation points, similar to CellAlign[5]. For each interpolation time point,

we estimate a Gaussian distribution of gene expression, taking into account all cells, kernel-

weighted[5] by their pseudotime distance to this interpolation time point. Compared to the

existing methods, our approach fits the entire distribution instead of only estimating the mean

expression level at each interpolation point. The interpolated gene trajectories of the

reference and query are then aligned using our DP algorithm. This generates optimal

trajectory alignments for all input genes, described by five-state alignment strings (**Fig. 1d**

and top right matrix of **Fig. 2**). These strings are then binary encoded to compute their

pairwise Hamming distances, and genes displaying similar alignment patterns are clustered

together using agglomerative hierarchical clustering. Alignments and their cluster

memberships together allow us to proceed with further downstream analysis such as gene set

overrepresentation analysis. (See Methods for details). The algorithmic novelties, definitions

and descriptive level of the generated alignments altogether fundamentally distinguishes G2G

from the current alignment approaches.

G2G accurately identifies different patterns of alignment with simulated data experiments

To benchmark how well G2G captures different alignment patterns, we performed two

simulated data experiments on: (1) an artificial dataset (**Fig. 3a,e, Extended Data Fig. 2,** and

Supplementary Table 2-3), and (2) a real biological dataset with artificial perturbations

(**Fig. 3f,g, Extended Data Fig. 3,** and **Supplementary Table 4-17**). See Methods for details.

Experiment 1
We simulated 3500 trajectory pairs under three main classes of pattern: (1) *Matching* (500
genes), (2) *Divergence* (1500 genes)*,* and (3) *Convergence* (1500 genes)*,* using Gaussian
Processes and suitable kernels[24,25], to test how well G2G aligns and captures them. Each
trajectory consists of 300 data points spread across the pseudotime range [0,1]. In the
Divergence and *Convergence* group, we have an equal number of pairs bifurcating at three
time points (approximately at bifurcation time point $t_b \in$ [0.25, 0.5, 0.75], indicating early,
mid, and late bifurcation, respectively). We first examined G2G performance on each of the
seven classes of pattern, in identifying matched and mismatched regions accurately (with 50
interpolated time points – shortest possible alignment length L_{min}= 50 and longest possible
alignment length L_{max}= 100), followed by clustering of all alignments.
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<u>Statistics for expected match and mismatch regions:</u> For *Matching* pairs (**Fig. 3b**), 86.4%
alignments give 100% alignment, while the rest show at least one false mismatch with an
average length of 4.74 (~9.4% L_{min}). The mean matching percentage (the percentage of total
matching, including one-to-one matches and warps, in the alignment string output, which we
term 'alignment similarity') is 98.8%. For *Divergence* (**Fig. 3c**), we expect to see a full match
at the beginning (start-match) followed by a full mismatch at the end (end-mismatch), where
the match/mismatch length depends on the approximate location of bifurcation. Thus we
report the distributions of start-match lengths (that follows a false mismatch if there is any),
end-mismatch lengths, and start-mismatch lengths (detecting false mismatches) in all
alignments across the three bifurcating locations. We observed no end matches,
demonstrating that G2G accurately mismatches the differentially expressed region. However,
33.13% of the divergent alignments give at least one false start-mismatch (30.4% for $t_b =$
0.25, 33.2% for $t_b =$ 0.5, and 35.8% for $t_b =$ 0.75). However, their median mismatch
length is 1 (with mean 2.29 = ~4.6% L_{min}). All distributions fall within their expected ranges
of length with a few outliers. As the bifurcation point moves towards the maximum
pseudotime, the number of matches increases while the number of mismatches decreases as
expected. In contrast, *Convergence* alignments (**Fig. 3d**) (where we expect start regions to
fully mismatch while end regions fully match) show only a 3.5% of all convergent
alignments with false end-mismatches (2.8% for $t_b =$ 0.25, 5.3% for $t_b =$ 0.5, and 2.4% for
$t_b =$ 0.75). Their median mismatch length is 4 (with mean 11.84 = ~23.7% L_{min} , mainly
due to just 4 outliers with complete mismatching alignments arising from t_b=0.75 case).
Again, the distributions of end-match lengths and start-mismatch lengths across all subgroups
fall within the expected ranges. We also see no false start matches. Only one 0.5
Convergence alignment (0.06%) showed a single mismatch within an expected match region.
In conclusion, for *Matching*, *Convergence* and *Divergence* patterns, G2G is able to generate
correct alignments with relatively high accuracy.
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<u>Clustering alignments:</u> **Fig. 3e** shows the pairwise alignment distance matrix, which
demonstrates a clear separation of the seven pattern classes. Hierarchical agglomerative
clustering of the alignments at 0.2 distance threshold results in 11 clusters, capturing all the
distinct patterns with only 0.34% mis-clustering rate. 21 alignments of early *Divergence* and

late *Convergence* appear in 4 pure subclusters due to warps, confirming G2G's ability to
distinguish between usual and outlying patterns. (Further results in **Extended Data Fig. 4**).
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207 Overall, G2G has a good detection accuracy of the expected matches and mismatches across
208 all the seven classes of trajectory alignment patterns we evaluated. Clustering results of their
209 five-state alignment strings also confirm the utility of such descriptive outputs.
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Experiment 2
To test the ability to detect matching patterns in real scRNA-seq data, we used a scRNA-seq
dataset of E15.5 murine pancreatic development[26] and considered gene expression profiles of
769 genes varying in expression during beta-cell differentiation. We randomly split cells into
query and reference, and simulated the presence of a mismatch in the form of a deleted
portion (perturbation scenario 1) or changed portion (perturbation scenario 2) of increasing
size (pseudotime was equally divided into 50 bins with an increasing number of bins being
perturbed) at the beginning of the trajectory (**Fig. 3f**). We then performed alignments with
G2G (under 50 interpolation time points) and calculated the percentage of match calling, i.e.,
alignment similarity (**Fig. 3g**). We found that on average, G2G recovered the matching region
accurately across genes, with 91% mean alignment similarity when no perturbation was
introduced, and 86% mean alignment similarity for mismatches smaller than 20% of
pseudotime bins (10/50 bins) across the two different perturbation scenarios. For perturbation
scenario 1, the alignment similarity decreases with increasing deletion sizes as expected
across smaller perturbation sizes. However, the detected mismatch length is shorter than
expected for deletions larger than 20%. This is due to the relative non-varying gene
expression trends between pseudotime bin 10 to 20 (**Extended Data Fig. 3a**) and hence it
causes warps instead of mismatches. For perturbation scenario 2, the alignment similarity has
an expected maximum and minimum. For example, if the perturbation size = 5 in the query,
the minimum mismatch segment to expect is: "IIIII", whereas the maximum mismatch
segment to expect is: "IIIIIDDDDD" (illustrated in **Extended Data Fig. 3b**). Accordingly,
the observed trend generally follows the expected trends, falling within the expected ranges
for larger perturbations sizes.
234
In general, we observe that the alignment accuracy drops when the underlying assumption of
a smooth trajectory breaks, and/or when there are significant inconsistencies in the cell
densities across the trajectories. As apparent from this experiment, we also note that it is
extremely challenging to simulate perturbations using real life datasets for trajectory
benchmarking, as they may introduce warps instead of expected mismatches as shown in
perturbation scenario 1. Consequently, it is difficult to guarantee a specific linear ordering of
matches and mismatches. Overall, the results support that G2G has a good accuracy rate of
match and mismatch detection.
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G2G captures mismatches and offers gene-level resolution alignment
To benchmark our method against the widely-known DTW-based method, CellAlign[5], we
performed G2G alignment on the same dataset[23] used by CellAlign (**Fig. 4a**), which includes

time-course data of murine bone marrow-derived dendritic cells stimulated with PAM3CSK
(PAM) or lipopolysaccharide (LPS) to simulate responses to different pathogenic
components. The main difference between CellAlign and G2G is that, CellAlign only
considers matches and warps through DTW, while G2G's algorithm unifies matches and
mismatches through a single DP algorithm by imposing the notion of gaps on top of DTW via
a probabilistic framework and Gotoh's algorithm[15]. Further conceptual differences between
G2G and CellAlign are summarized in **Supplementary Table 1**. Of note, G2G outputs both
individual gene-level alignments and an aggregate (average) alignment path over all gene-
level alignments, unlike CellAlign which outputs only a single, high-dimensional alignment
across all genes. This is particularly useful when there is heterogeneity in alignment patterns
among different genes.
258
G2G's ability to capture mismatches is revealed in aligning genes from the "core antiviral
module" of the PAM/LPS dataset (**Supplementary Table 18-22**). CellAlign demonstrated a
'lag' in expression in PAM stimulation compared to LPS[5]. This is also captured by the G2G
aggregate alignment whereby later PAM pseudotime points were mapped to earlier LPS
pseudotime points (**Fig. 4b**). In addition, G2G identified mismatches in the early and late
pseudotime points.
265
In the early pseudotime points, the gene expression was consistently low in the PAM
condition, whereas some of the cells stimulated by LPS were already showing elevated
expression at early time points (**Fig. 4c**). These have also been noticed in the original paper
and were described as "precocious expressers"[23]. The mismatch in the late pseudotime points
of LPS stimulation was caused by the peaked expression, while the expression of the PAM-
stimulated cells was still on the rise and had not reached a peak yet (**Fig. 4c**).
272
In the case of aligning genes from the "peaked inflammatory module" (**Supplementary
Table 23-30**), **Fig. 4d** shows the main average path of alignment generated by G2G. In
addition, genes were clustered based on their alignment patterns (method illustrated in **Fig. 2**;
results in **Extended Data Fig. 5-6**), and the aggregate alignment path for each cluster was
different from the main average path (**Fig. 4d**). Representative genes from different clusters
are shown in **Fig. 4e**. Although they all had matches for some pseudotime points, there are
subtle differences in the length and position of the time points that are matched.
280
In addition, genes can be examined via the similarity between their expression profiles along
the query and reference pseudotime trajectories. This can be computed through their
percentage of alignment similarity. We identified genes with low alignment similarity and
high log fold change between query and reference data, such as *CCRL2* and *C5AR1*. *CCRL2*
expression started at a much higher level and peaked early in the LPS condition, whereas
following PAM stimulation it grew as a slow incline. This stark difference suggests that
CCRL2 is a more LPS-specific response gene, consistent with previous reports in murine
dendritic cells, macrophages, glial cells, astrocytes and microglia stimulated with LPS[27,28].
On the other hand, these data suggest that *C5AR1* is a PAM-specific response gene. In the
case of the *TNF* gene, although the differential expression log fold change is almost

negligible, the low alignment similarity revealed different expression dynamics. This
difference would not be picked up by differential gene expression, hence highlighting the
importance of such an alignment. For the genes that have high alignment similarity such as
CD44, the log fold change should be small due to consistent matching across the pseudotime.
295
The above results showcase the benefit of G2G alignments over DTW alignments, i.e., to
capture mismatched regions in gene expression trajectories. While the DP matrix of DTW
may reflect the time points of relative differences and similarities in gene expression between
two trajectories, we need extra effort subjected to thresholding to perform local DTW
alignment and extract mismatches. TrAGEDy[11], the most recent extension on CellAlign[5,11],
performs such ad hoc processing of DTW outputs (See feature comparison in
Supplementary Table 1). We next compared G2G with CellAlign and TrAGEDy on a
simulated dataset containing two trajectories with no shared process[11](referred to as a
negative control dataset). G2G successfully quantifies that they are very dissimilar, with a
low average of 34.5% alignment similarity across all the genes (**Supplementary Fig. 2a,**
Supplementary Table 52). G2G also generates an aggregate alignment solely with insertions
and deletions, which agrees with the expectation (**Supplementary Fig. 2b**). CellAlign is
unable to produce a meaningful output for this dataset due to its DTW assumption of no
mismatch. The alignment from TrAGEDy includes segments of one-to-one matches. This
could be caused by the assumption of a definite match in between, in TrAGEDy post hoc
thresholding. It is further validated by testing on three simulated genes with completely
mismatched trajectories (**Supplementary Fig. 2c**). While TrAGEDy falsely generates
matched subregions, G2G gives accurate outputs of 100% mismatch.
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315 Overall, the above results over a real biological dataset and a negative control validate that
316 G2G can accurately detect mismatches.
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In vivo, *in vitro* human T cell development comparison using G2G reveals differences in TNFα signaling

We next applied G2G to compare *in vitro* and *in vivo* human T cell development. Thymus is
the key site for T cell development in humans, where lymphoid progenitors differentiate
through stages of double negative (DN) and double positive (DP) T cells to acquire T cell
receptor (TCR) (illustrated in **Fig. 5a**). If the TCR recognizes self antigen presented on MHC
via the process of positive selection, the developing T cells further differentiate through
abT(entry) cells and finally mature into single positive (SP) T cells. There are different
subsets of SP T cells, including CD4+T, CD8+T and regulatory T (Treg) cells, as well as the
newly recognized unconventional type 1 and type 3 innate T cells and CD8AA[29,30]. To
investigate human T cell development in a model system, we differentiated induced
pluripotent stem cells (iPSCs) into mature T cells using the artificial thymic organoid (ATO)
system[31]. We previously harvested differentiated cells from week 3, 5, and 7 and reported
that the mature T cells in ATO were most similar to the *in vivo* type 1 innate T cells. To
explore this further, we performed scRNA-seq analysis of differentiated cells harvested at
regular intervals throughout the differentiation, i.e., including the early time points as well

(**Fig. 5b**). Cell types were annotated (low-level annotation in **Fig. 5c** with more refined
annotation in **Extended Data Fig. 7a**) using a combination of the logistic regression based
predictions with CellTypist[32] (**Extended Data Fig. 7b**) and marker gene analysis (**Extended**
Data Fig. 8). The ATO system captures the differentiation from stem cells, through
mesodermal progenitors, endothelium, to haematopoietic lineage, and then further down to T
cell lineage (**Fig. 5b**).
340
We then combined the *in vitro* ATO data with the relevant *in vivo* cell types from our
developing human immune atlas[30] (hereafter referred to as the pan fetal reference) and
integrated using scVI[33] onto a common latent embedding (**Fig. 5d,e**). For ATO data, the
pseudotime was estimated using a Gaussian Process Latent Variable Model (GPLVM)[34] with
sampling times as priors (**Fig. 5f**). GPLVM has previously been successfully applied in
single-cell trajectory inference to incorporate useful priors[35–39]. The pan fetal reference cells'
pseudotime was computed similarly by estimating their time priors from the nearby ATO
cells (see Methods).
349
Alignment between *in vitro* ATO data and *in vivo* pan fetal reference was performed with
G2G (under 15 equispaced time points in [0,1] pseudotime range) using all transcription
factor (TF) genes[40] (**Supplementary Table 31**), as many TFs function as 'master regulators'
of cell states and have been used to induce cell differentiation. The aggregate alignment result
for all TFs showed a mismatch at the beginning and a mismatch at the end (**Fig. 6a**). We
explored this further by performing gene set overrepresentation among the most mismatched
genes (alignment similarity < 40%, **Fig. 6b, Supplementary Table 32**), and found that
pluripotency and TNFα signaling pathways were the two most significant gene sets. Many of
the genes in the pluripotency signaling pathway, such as the well-known pluripotent genes
POU5F1, NANOG and *SOX2[41]*, were expressed at the beginning of ATO development but
missing from the reference (**Fig. 6c**). This is expected given that the *in vitro* differentiation
started from iPSCs, whereas the earliest cells from the *in vivo* reference were haematopoietic
stem cells (HSCs). On the other hand, *HHEX*, which is known to be expressed in HSC[42,43]
and early DN T cells[44] demonstrates another pattern: matching between *in vivo* and *in vitro*
HSC and DN T cells as expected although the maximum *HHEX* expression in *in vitro* cells
was lower than that of *in vivo* cells (**Fig. 6c**).
366
With regard to the TNFα signaling via NFκB pathway, many of the genes such as *FOSB,*
JUNB and *NR4A2* show an increasing trend at the last stage of *in vivo* T cell development,
and this increase is missing in the *in vitro* T cells (**Fig. 6d**). TNFα activation of NFκB
pathway has been implicated in the final functional maturation of murine T cells within the
thymus[45,46] and indicates that, while the ATO system captures the single positive T cell
development through positive selection, other *in vivo* signaling necessary for maturation,
such as TNFα pathway, might be missing. By systematically comparing the *in vivo* data to *in*
vitro data with G2G, it gives us potential targets for further *in vitro* optimization. There are
exceptions to this overall pattern, such as *KLF2*, whose expression is higher in *in vitro* T cells
than that in *in vivo* (**Fig. 6d**). This might be the result of each gene being regulated by more
than one signaling pathway. We remark that although it is possible to recover the difference

between TNFα signaling by doing direct differential gene expression between cell subsets,
e.g., end products of ATO vs *in vivo* T cells, a key advantage of using the trajectory
alignment is that we could pinpoint where along the differentiation did the mismatch occur.
This would in turn inform us when to introduce the TNFα in *in vitro* optimization.
382
Using G2G, genes are also clustered based on their alignment patterns (**Extended Data Fig.**
9, Supplementary Table 31,33-45). Cluster 4 captures the pluripotent genes, and the
majority show a complete mismatch alignment pattern. Cluster 10 genes are enriched in the
Hippo signaling pathway, and many of its genes show insertions at the beginning of the
pseudotime. Hippo signaling has been implicated in stem cell biology and pluripotency
regulation[47], and the observed mismatch might again be explained by the stem cell stage
present in the organoid but absent from the *in vivo* reference. Interestingly, cluster 0 genes
show mismatches in the middle time points. This might represent a missing cell state, e.g.,
BATF2 is expressed sparsely in endothelial cells which are present in the *in vitro* but not in
the *in vivo* system (**Extended Data Fig. 10**).
393
394 We further repeated the analysis restricting to T cell lineages, i.e., DN T cells onwards
395 (**Extended Data Fig. 11a-d, Supplementary Table 46-47**). TNFα signaling via NFκB
396 pathway remains the most significantly enriched gene set among the mismatched genes.
397
The above alignments were performed using *in vivo* type 1 innate T cells and the relevant
precursors, as we previously found that the *in vitro* mature T cells were most similar to the *in*
vivo type 1 innate T cells[30]. However, *in vitro* cell differentiation to conventional CD8+T
cells might also provide promising routes for cell therapies. We therefore performed another
G2G alignment using *in vivo* conventional CD8+T cells and the relevant T lineage precursors
(DN T cells onwards), with the results shown in **Extended Data Fig. 11e-h** (and
Supplementary Table 48-49). The most significantly enriched gene set among the
mismatched genes is also TNFα signaling pathway. To further explore the differences in the
two alignment results, we focused on genes that showed the most dissimilar alignment results
(genes that had alignment similarity differences > 0.5 or < -0.5) (**Fig. 6e**). Three of the genes,
SOX4, FOXP1 and *ARID5B* had large $\log_2$ fold change differences (absolute $\log_2$ fold change
> 1) between type 1 innate T cells and CD8+T cells. For these three genes, the expression
dynamics of *in vitro* T cell development are more similar to those of *in vivo* type 1 innate T
cells, whereas *in vivo* CD8+T cells had higher *SOX4, FOXP1* and lower *ARID5B* expression
in the last stages of development (**Fig. 6e**). While the role of *SOX4* in CD8+T cell
development is unclear, *FOXP1* has been shown to maintain a quiescent profile in naive
CD8+T cells[48,49] , and our results are in keeping with a more activated profile in type 1 innate
T cells. *ARID5B* has been reported to regulate metabolic programming and promote IFNγ
production in NK cells[50]. The higher expression in type 1 innate T cells might explain some
of their NK-like features[29,30]. On the other hand, for *BHLHE40*, which is downstream of
TNFα signaling and other pro-inflammatory cytokines[51], its expression dynamic in *in vitro* T
cell development is more similar to that in CD8+T cells, while the *in vivo* type 1 innate T
cells have increased expression at the end.
421

422 Overall, G2G alignment between *in vivo* and *in vitro* human T cell development revealed
423 potential targets for further optimization of *in vitro* T cell differentiation (illustrated in **Fig.**
424 **6f**).
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Discussion

Genes2Genes offers a structured alignment framework to compare single-cell pseudotime
trajectories at single-gene resolution. We validated G2G's accuracy in identifying
mismatches and different alignment patterns through extensive simulation studies. We have
also benchmarked against current state-of-art methods in trajectory alignment using a real-life
dataset and a simulated negative control dataset from the literature. In addition, we
demonstrated G2G's potential in identifying genes and pathways that can guide the
refinement of T cell differentiation in an organoid protocol.
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Given cell-by-gene matrices of reference and query systems along with their corresponding
pseudotime estimates, G2G generates a five-state alignment string for each gene of interest
by running a DP algorithm that handles both matches and mismatches. The gene sets to
compare can be all expressed genes against each other, or restricted to gene sets of interest
such as e.g. TFs, regulons, highly variable genes or genes associated with certain
biological/signaling pathways of interest. Compared to existing alignment approaches, G2G
outputs more descriptive and direct results highlighting both matched (including warps) and
mismatched regions of a gene over time. G2G provides a powerful addition to the current
repertoire of comparative analysis toolboxes for any pseudotime alignment task, e.g., *in*
vivo/*in vitro*, treatment/control, cross-species etc.
445

An important feature of G2G are the gene-specific alignments. Most existing methodologies
produce a single alignment for all genes by computing high-dimensional Euclidean distances
over their mean gene expression vectors. Such metrics suffer from 'the curse of
dimensionality' by losing accuracy as the number of genes increases[52]. Importantly, in many
contexts, an overall alignment across all genes masks gene heterogeneity along trajectories in
the reference and query systems. Alpert et al (2018)[5] discuss choosing the right alignment
resolution, recommending alignment of the largest gene set that shows significant differential
expression (DE genes) over time. This is to remove stably expressed genes which may add
noise and skew the alignment results. Our method goes further and fully resolves all gene
groups with distinct matching and mismatching patterns at different stages along trajectories
(**Fig. 4d**, **Extended Data Fig. 4-6**).
457

The gene-specific alignment of G2G also allows users to cluster genes based on their
matching patterns to form groups with broadly similar alignments. We show that pathway
overrepresentation analysis on each gene cluster can reveal specific biological signaling
pathways that are driving the differences in pseudotime trajectories at different stages. These
pathways and gene sets can be a starting point for protocol intervention strategies in the case
of *in vivo*/*in vitro* alignments, and for mechanistic molecular interpretation of differences
between trajectories in other cases.

465
The reliability of a trajectory alignment depends on how trustworthy the given pseudotime
estimates are[2]. Different pseudotime estimates can produce different alignment distributions.
While our initial G2G framework provides proof-of-concept by demonstrating the power of
gene-level DP alignment to discover differential genes along pseudotime trajectories, future
work is needed to develop suitable methods to calibrate its input (i.e. pseudotime estimates
and interpolation), and better parameter optimization strategies to ensure more reliable
alignment distributions. For instance, an adaptive window size for the Gaussian kernel-based
interpolation may optimize the method's sensitivity to the variance of expression in the
nearby cells. Furthermore, the current G2G version can only compare two linear trajectories
without considering branching processes. We are aware of other efforts in aligning branched
processes with DTW based tree alignment[8]. The output from such alignments, i.e., identified
pairs of correspondences, could be further inputted into G2G for a comprehensive pairwise
lineage alignment to capture mismatches.
479
In summary, G2G provides a formal trajectory alignment for single-cell transcriptomic data
and is able to capture matches and mismatches at single-gene level. It enables a deeper
understanding of the diversity of gene-level trajectory alignments across single-cell datasets.
The G2G package is easy-to-use and freely available online at
https://github.com/Teichlab/Genes2Genes with a tutorial. We have demonstrated that
regenerative medicine can specifically benefit from such trajectory comparisons by extracting
cues to guide refinement of *in vitro* cell engineering to recapitulate *in vivo* development. We
envision that the software will be useful to the community for exploring other biological
scenarios such as cell activation/stimulation responses in control and disease, generating new
insights to advance our understanding of cell development and function in health and disease.

Main Figures

Fig. 1 | Computational alignment of single-cell transcriptomic trajectories. a, Trajectory
alignment is important for comparing different single-cell reference and query systems that
dynamically change. This could be between *in vivo* cell development and *in vitro* cell
differentiation, or between control and drug-treated cells in response to the same perturbation,
or between the responses to vaccination or pathogen challenge in healthy *versus* diseased
individuals. A complete alignment between them can capture matches and mismatches for
further downstream analysis. **b,** Schematic illustration of the different states of alignment and
their theoretical origins. Left: dynamic time warping and biological sequence alignment are
complementary to each other[14–16], where both address matches yet capture either warps or
indels respectively. Right: between discrete time points in R (reference trajectory) and Q
(query trajectory), there may exist 5 different states of alignment: matches (1-1
correspondences), warps (1-to-many expansion or many-to-1 compression correspondences)
and mismatches (insertions/deletions denoting a significant difference in one system
compared to the other). **c,** Example alignment path across a pairwise time point matrix
between R and Q trajectories. Diagonal lines (green) refer to matches (M); vertical lines refer
to either insertions (I) (red) or expansion warps (V) (green); horizontal lines refer to deletions
(D) (red) or compression warps (W) (green). Any matrix cell (i, j) denotes the pairing of a
reference time point R_j and query time point Q_i. **d,** Example gene alignment plot (left) and the
corresponding five-state alignment string generated by G2G (right). Plots display interpolated
log1p normalized expression (*y*-axis) between a reference (green) and query (blue) against

their pseudotime (*x*-axis) for the gene *SERTAD2* in the PAM/LPS dataset from Shalek et al
(2014)[23]. The bold lines represent mean expression trends, while the faded data points are 50
random samples from the estimated expression distribution at each time point. The black
dashed lines visualize matches and warps between time points. The boxed alignment string
describes matches and mismatches for the gene (stars represent time points, and ^ represent a
repeated time point from the left due to a warp).

518
Fig. 2 | Overview of the Genes2Genes (G2G) alignment framework for comparing
single-cell transcriptomic trajectories. Schematic illustration of G2G workflow. Given
log1p normalized cell by gene expression matrices of a reference (R) and query (Q) system
and their pseudotime estimates, G2G infers individual alignments for a list of genes of
interest. It first interpolates data by extending mean based interpolation in Alpert et al (2018)[5]
to distributional interpolation, and then runs Gotoh's dynamic programming (DP) algorithm[15]
adapted for a five-state alignment machine (**Extended Data Fig. 1a**) defining a match (M),
compression warp (W), expansion warp (V), insertion (I) and deletion (D). All reported
alignments are then clustered and used to deliver statistics on the overall degree of alignment
between R and Q, supporting further downstream analyses. Top left, the DP recurrence
relations utilize a match cost function defined under minimum message length (MML)[21]
statistical inductive inference. Given a hypothesis (a distribution model) and data, MML can
define the total message length of encoding them for lossless compression along an
imaginary message transmission. G2G defines two hypotheses: (1) Φ: R_j and Q_i time points
mismatch, and (2) A: R_j and Q_i time points match. Under Φ, the message length is the sum of
independent encoding lengths of their corresponding interpolated expression data and
distributions. Under A, the message length is their joint encoding length of the corresponding
interpolated expression data with a single Gaussian distribution (either of R_j or Q_i). The
match cost is taken as the difference of A and Φ per datum encoding lengths. Bottom left,
G2G encodes the five-state alignment strings using a binary scheme and computes a pairwise
Hamming distance matrix to cluster all gene-level alignments. Top right: example output of

five-state alignment strings for each gene. Bottom right, example clustermap showcasing the

clustering result of alignment strings. The color represents the pairwise Hamming distance,

and the clustering is performed using Agglomerative hierarchical clustering.

543
Fig. 3 | G2G accurately identifies different patterns of alignment with simulated data
experiments. a, Experiment 1 uses a Gaussian Process based simulator to generate 3500
simulated pairs of reference and query gene trajectories to test G2G on. These include three
main classes of alignment pattern: (1) *Matching*, (2) *Divergence* and (3) *Convergence*. The
Divergence and *Convergence* groups further sub-categorised based on their approximate

location of bifurcation (0.25, 0.5, and 0.75 within [0,1] pseudotime range), resulting in seven
pattern classes (each with 500 alignments). **b,** Alignment frequency histogram of mismatch
percentages observed in the 500 alignments for the simulated *Matching* class. **c,** Distributions
of start match lengths (following a false mismatch if there is any), end mismatch lengths
(prior to a false match if there is any), and start mismatch lengths (number of mismatches
starting from time point 0) in the 1500 *Divergence* alignments across the three bifurcation
subgroups. 50 equispaced time points on pseudotime [0,1] were used for distribution
interpolation and alignment. In the case of early divergence, i.e., bifurcation at 0.25, there are
2 cases showing complete mismatch, i.e., mismatch length of 100. **d,** Distributions of end
match lengths (prior to a false mismatch if there is any), start mismatch lengths (following a
false match if there is any), and end mismatch lengths (number of mismatches before time
point 1) in the 1500 *Convergence* alignments across the three bifurcation subgroups. 50
equispaced time points on pseudotime [0,1] were used for distribution interpolation and
alignment. In the case of late convergence, i.e., bifurcation at 0.75, there are 4 cases showing
complete mismatch, i.e., mismatch length of 100. **e,** The clustergram of the pairwise
Hamming distance matrix across all alignments, which clearly shows the separate classes of
pattern. **f,** Experiment 2 uses the mouse pancreas development dataset (Beta lineage) scRNA-
seq dataset [26] to generate perturbed pairs of alignment from the expected *Matching*
alignments. Perturbation scenario 1 deletes the start region from the reference trajectory,
whereas perturbation scenario 2 changes the start region from the reference trajectory. **g,** The
alignment similarity distributions for varying sizes (percentage of 50 pseudotime bins) of
perturbation under perturbation scenario 1 (left) and perturbation scenario 2 (right). Each
point represents a gene (total number of genes n = 769). In each plot, the observed average
alignment similarity across different perturbation sizes is shown by the green line. For
perturbation scenario 1 (left), the blue line shows the expected alignment similarity across
different perturbation sizes. For perturbation scenario 2 (right), there are two expected lines:
maximum (in blue) and minimum (in red). The maximum mismatch length is expected when
both reference and query time points form insertions and deletions, making the maximum
expected length *size**2. The minimum mismatch length is expected when only the changed
reference time points are mismatched as insertions, while the corresponding query time
points are matched to the non-perturbed reference time points (illustrated in **Extended Data
Fig. 3b)**.

Fig. 4 | G2G captures mismatches and offers gene-level resolution alignment. a, G2G
alignment was performed on a time-course data[23] of murine bone marrow-derived dendritic
cells stimulated with PAM or LPS. Both the gene expression data and the inferred
pseudotime were taken from Alpert et al. 2018[5]. **b,** Top: schematic illustration of the
aggregate alignment result for all the genes in the "core antiviral module". The stacked bar
plots represent the cell compositions at each time point (50 equispaced time points on
pseudotime [0,1]), colored by the time of sampling post stimulation. Boxed segments
represent mismatched time points. The black dashed lines represent matches and warps
between time points. Bottom: pairwise time point matrix between PAM and LPS pseudotime.
The color represents the number of genes showing match or warp for the given pair of a PAM
time point and an LPS time point. The white line represents the main average alignment path.
c, Gene expression plots for three representative genes (*IRF7*, *STAT2* and *IFIT1*) from the
"core antiviral module" in LPS-stimulated (blue) and PAM-stimulated (green) data along
their pseudotime. Left column: the interpolated log1p normalized expression (*y*-axis) against
pseudotime (*x*-axis). The bold lines represent mean expression trends, while the faded data
points are 50 random samples from the estimated expression distribution at each time point.
The black dashed lines represent matches and warps between time points. Right two columns:
the actual log1p normalized expression (*y*-axis) against pseudotime (*x*-axis). Each point
represents a cell. The five-state alignment string for each gene is shown below the expression
plots. Red circles highlight the cells with high expression values at early time points, which
are referred to as 'precocious expressers'. **d,** The same plots as in **b** for genes in the "peaked
inflammatory module". In the pairwise time point matrix, the white line represents the main
average alignment path. The genes are also clustered based on their alignment results
(**Extended Data Fig. 5**), and dashed lines with different colors represent examples of cluster-
specific alignment paths. **e,** The same plots as in **c** for a representative gene from each cluster
shown in **d**. **f,** Plot of alignment similarity (*y*-axis) against $\log_2$ fold change of mean
expression (*x*-axis) for all genes in the "peaked inflammatory module" (middle). The color
also represents the alignment similarity. The surrounding plots show the interpolated log1p
normalized expression (*y*-axis) against pseudotime (*x*-axis) on the left, and the violin plot of
total gene expression on the right for four selected genes (*CD44*, *CCRL2*, *TNF*, *C5AR1*).

Fig. 5 | *in vivo*, *in vitro* human T cell development data integration and pseudotime inference. a, Schematic illustration of T cell development in the human thymus. **b,** Top: schematic showing the experimental set-up of T cell differentiation from iPSCs in ATOs. Bottom: barplot of cell type composition in ATO at different time points during differentiation. **c,** UMAP visualization of different cell types in the ATO dataset (low-level

annotation, number of cells n = 31,483), with more refined annotation in **Extended Data Fig.**
7a. **d,** Workflow of integrating *in vitro* (i.e. ATO) and *in vivo* (i.e. pan fetal reference from
Suo et al. 2022[30]) human T cell development data and pseudotime inference using GPLVM.
e, Main: UMAP visualization of integrated *in vivo* and *in vitro* human T cell development
data, colored by the cell types. Right insert: the same UMAP visualization colored by the data
source. **f,** Stripplot of the inferred pseudotime (*x*-axis) against different cell types (*y*-axis),
colored by the cell types, of *in vivo* pan fetal reference data (top) and *in vitro* organoid data
(bottom).

Fig. 6 | *in vivo*, *in vitro* human T cell development alignment with G2G. a, Aggregate
alignment result for all TFs between *in vitro* organoid (i.e. ATO) and *in vivo* reference (i.e.
pan fetal reference from Suo et al. 2022[30]) human T cell development data shown in the
pairwise time point matrix between organoid and reference pseudotime. The color represents
the number of genes showing match or warp for the given pair of an organoid time point and
a reference time point. The white line represents the main average alignment path. The
stacked bar plots represent the cell compositions at each time point (15 equispaced time
points on pseudotime [0,1]), colored by the cell types, for reference (top) and organoid (left)
separately. **b,** Gene set overrepresentation results of the most mismatched genes from
alignment in **a**, with the gene set names in *y*-axis, and -$\log_{10}$(adjusted P-value) in *x*-axis. The
size of the point represents the percentage of genes from that gene set being within the list of
most mismatched genes. The color represents the -$\log_{10}$(adjusted P-value). Two most
significant gene sets were boxed in red. **c,** Alignment results for all genes in the pluripotency
signaling pathway. Top left: pairwise time point matrix between organoid and reference
pseudotime. The color represents the number of genes showing match or warp for the given
pair of an organoid time point and a reference time point. The white line represents the main
average alignment path. Top right: schematic illustration of the aggregate alignment result.
The stacked bar plots represent the cell compositions at each time point, colored by the cell
types. The black dashed lines represent matches and warps between time points. Boxed
segment represents the mismatched pluripotency stage in the organoid. Bottom left: the
interpolated log1p normalized expression (*y*-axis) against pseudotime (*x*-axis) for selected
genes. Bottom right: heatmap of the smoothened (interpolated) and z-normalized mean gene
expression along the pseudotime. **d,** The same plots as in **c** for all genes in the TNFα
signaling via NFκB pathway. The boxed segment in the right top plot represents the
mismatched last stage *in vivo* T cell maturation. **e,** Plots showing the alignment differences
between *in vivo* conventional CD8+T lineage *versus in vitro* organoid, and *in vivo* type 1
innate T cell lineage *versus in vitro* organoid. Middle: plot of alignment similarity difference
(*y*-axis) against $\log_2$ fold change of mean expression between CD8+T and type 1 innate T
cells (*x*-axis). The color reflects the absolute value of alignment similarity difference.
Surrounding plots: the interpolated log1p normalized expression (*y*-axis) against pseudotime
(*x*-axis) showing the alignment between *in vivo* type 1 innate T cell lineage (green) and *in*
vitro organoid (blue) (top), and the alignment between *in vivo* CD8+T lineage (orange) and *in*
vitro organoid (blue) (bottom), for four selected genes. **f,** Schematic illustration of potential
targets for further optimization of *in vitro* T cell differentiation towards either type 1 innate T
cells or conventional CD8+T cells.

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Methods

Genes2Genes (G2G): A new alignment framework for single-cell trajectories

As described in the main text, Genes2Genes performs dynamic programming (DP) alignment independently for all genes of interest, between a reference trajectory R and a query trajectory Q. In other words, each gene-level (i.e. gene-specific) trajectory alignment is an independent DP task of pairwise time series alignment. The aim is to generate an optimal sequence of matched time point pairs and mismatched time point pairs between R and Q for each gene. As illustrated in **Fig. 1b**, there are five different alignment states which denote these matches and mismatches between two time points. For each time point in any gene trajectory, there is a respective expression distribution, as explained by an observed dataset of single-cell (scRNA-seq) measurements. G2G evaluates the similarities of these reference and query expression distributions over time, to determine a match or mismatch between their time points.

The following sections introduce the problem of pairwise time series alignment, and describe the main components of our G2G framework (**Fig. 2**) which operate together to produce optimal gene-specific alignments.

Pairwise time series alignment for trajectory comparison

A trajectory is a continuous path of change through some feature space, along some axis of progression (such as time)[53]. In single-cell transcriptomics, this feature space is usually defined by genes, and a trajectory through a high-dimensional gene space can describe the transcriptomic state of a cell as a function of time. A temporal (e.g. pseudotime) ordering of a set of single cells represents a discretization of the respective cell state trajectory, and their entire gene expression dataset forms a multivariate time series. On the other hand, their expression of a single gene forms a univariate time series. In this work, we consider a pairwise alignment of univariate time series, which allows us to perform gene-specific trajectory alignment.

Given two time series (sequences), reference R and query Q of length (i.e. a finite number of time points) $|R|$ and $|Q|$, their pairwise alignment describes sequential correspondences between their time points. As an optimization problem, computational alignment has two key properties: (1) an optimal substructure, and (2) overlapping set of subproblems, which make it dynamic programmable (DP)[3]. Property (1) means, the optimal alignment of any two prefixes $R_{1..j}$ and $Q_{1..i}$ depends on the optimality of three sub-alignments: (i) $R_{1..j-1}$ and $Q_{1..i-1}$, (ii) $R_{1..j-1}$ and $Q_{1..i}$, and (iii) $R_{1..j}$ and $Q_{1..i-1}$. Property (2) means, there exists subproblems (prefix alignments) that are overlapping. DP begins optimizing the alignment of prefixes, starting from null (Φ) sequences until it completes an alignment of the entire two sequences. During this process, it computes overlapping subproblems only once and reuses them through a memoization (history) matrix H. In the standard DP alignment algorithm, any cell (i, j) in H stores the optimal alignment cost of the two prefix sequences: $R_{1:j}$ and $Q_{1:i}$, by optimizing an objective function which quantifies the alignment through a set of recurrence relations. Once all H matrix cells are computed, the optimal alignment can be retrieved by

857   backtracking, starting from the right-most bottom cell ($|Q| + 1, |R| + 1$) until reaching the
858   matrix cell (0,0). The time complexity of this algorithm depends on how its alignment
859   scoring scheme is designed. (The standard scheme has a quadratic complexity to find the best
860   alignment out of the factorially growing all possible number of alignments).
861

Preprocessing a trajectory time series by distributional interpolation
Interpolation is a necessary preprocessing step that a time series has to undergo prior to
taking part in an alignment. This is to ensure smoothly changing and uniformly distributed
data that are in phase (i.e. having the same rate of sampling) at least approximately; otherwise
a reliable alignment cannot be guaranteed[5,12]. Here we chose to extend the mean gene
expression based interpolation method used by CellAlign[5] to a distributional interpolation, for
preprocessing a reference and query time series of gene expression before their alignment.
869

Given a pseudotime series t of (log1p normalized) expression in some gene g_j of a single-
cell dataset, our distributional interpolation method first min-max-normalizes the pseudotime
of t as to be in the range of [0,1]. Then, m equally spaced artificial (interpolated) time points
are determined within [0,1], where for each artificial time point t', we estimate a Gaussian
distribution (of mean $g_j(t')_{mean}$ and standard deviation $g_j(t')_{std}$) by using the Gaussian
kernel-based weighted approach. For each cell i annotated with pseudotime t_i , an associated
weight is computed w.r.t each artificial time point t' as:

877
$$w_i = exp(-\frac{(t_i - t')^2}{window\_size^2})$$

878   , where default $window\_size = 0.1$. The below equations are then used to compute the
879   Gaussian distribution parameters $g_j(t')_{mean}$ and $g_j(t')_{std}$:

880
$$g_j(t')_{mean} = \frac{1}{\Sigma w_i} \sum_{i=1}^{n} w_i \, g_j(t_i)$$

881
$$g_j(t')_{std} = c_{t'} \sqrt{n \frac{\sum_{i=1}^{n} w_i \, [g_{j\_mean} - g_j(t_i)]^2}{(n-1)\Sigma w_i}}$$

882
$$\text{where } g_{j\_mean} = \frac{\sum_{i=1}^{n} g_j(t_i)}{n},$$

884   , n is the total number of cells, and $c_{t'}$ is the weighted cell density (abundance of cells) at the
885   interpolated time point t'. The weighted cell density computed as:

886
$$c_{t'} = \frac{\sum_{i=1}^{n} w_i}{n},$$

is the expected weight of a cell at t'. A higher expected weight is indicative of a higher cell
density. This way, we account for cell abundance when deciding the variance for the
interpolated point (otherwise with a very low number of cells, we may get a very high
variance). Next, we generate $k = 50$ random data points from the Gaussian distribution
$N(g_j(t')_{mean} , g_j(t')_{std})$ for each interpolated time t', representing the interpolated
distribution of single-cell gene expression. Note: In this work, we use a fixed number of
interpolated time points m for both reference and query. As m controls the resolution of the

alignment, it should suffice to represent the entire trajectory. This interpolation also adds an
$O(nm)$ time complexity due to taking a weighted contribution from all cells at each t'. To
overcome this, a general solution is to subsample datasets before the analysis and/or to reduce
the number of contributing cells by considering only the nearest neighborhood.
898
899 The reference pseudotime series and query pseudotime series of each gene is preprocessed
900 using the above described distributional interpolation method. The interpolated time series
901 are then input to our G2G dynamic programming algorithm as detailed in the next section.
902

A new dynamic programming algorithm for time series alignment of a single
gene

Here we describe a new dynamic programming (DP) algorithm to generate an alignment
between a reference time series R and query time series Q of log-normalized expression of a
specified gene. This algorithm jointly adapts Gotoh's sequence alignment[15] with classical
dynamic time warping (DTW)[16] to accommodate five states of alignment (**Fig. 1b**), i.e., one-
to-one match (m), many-to-one warp (w_d), one-to-many warp (w_i), insertion (i), and deletion
(d) between time points in the two time series. We denote the five-state space as $\Omega = [m, w_d,$
$w_i, d, i]$. Our approach unifies matches and mismatches within a single DP algorithm unlike
DTW which only handles matches (including warps).
913
The DTW algorithm originated from the speech recognition domain[16] under the family of
dynamic programming algorithms for optimization[3]. It has been extensively used to align
time series with shifts (warps). Sankoff and Kruskal (1983)[12] had previously discussed how
to capture warps and indels both from a single alignment algorithm. They provided a DP
recurrence relation involving evaluations of the five alignment states to decide the optimal
state for each pair of R and Q time points when aligning two time series. Extending this idea
further, we implemented the Gotoh's $O(|R||Q|)$ DP algorithm to generate an optimal five-
state alignment hypothesis for R and Q time series by:
● Defining a Bayesian information-theoretic measure of distance between two gene
expression distributions using the minimum message length statistical inductive
inference framework[12,21].
● Defining a five-state machine that models state transitions in the alignment hypothesis
across the five different matching and mismatching states, defining one-to-one
matches, warps (i.e. many-to-one compression matches and one-to-many expansion
matches), and insertions-deletions (indels).
929
The scoring scheme of the DP algorithm evaluates every pair of reference time point j and
query time point i to generate an optimal alignment across all time points. This involves
computing two types of cost: (1) the cost of matching the two time points, j and i (denoted by
$Cost_{match}(i,j)$) based on their respective (interpolated) gene expression distributions, and
(2) the cost of assigning an alignment state $x \in \Omega$ for the two time points j and i. The
following sections first detail on how we compute these costs, and then describe how our DP
optimization works using this scoring scheme.

Note: The reference time point j and query time point i are also denoted by R_j and Q_i in the

main text.

The DP scoring scheme

The cost of match between the reference time point j and query time point i

We expect a match between the reference time point j and query time point i if they have

similar distributions of gene expression. Thus, to score the likelihood of a match, we define a

distance measure between the two gene expression distributions corresponding to the j and i

time points, respectively. To compute this distance, we first take the interpolated single-cell

expression datasets at time point j of R (denoted by $R(j)$) and time point i of Q (denoted by

$Q(i)$). We already know the mean (μ) and standard deviation (σ) statistics for $R(j)$ and $Q(i)$

separately, as they were estimated during the time series interpolation step. Thus we define

the Gaussian distribution $N(\mu_{R(j)}, \sigma_{R(j)})$ for $R(j)$, and the Gaussian distribution

$N(\mu_{Q(i)}, \sigma_{Q(i)})$ for $Q(i)$ using their respective μ and σ statistics. Accordingly, if $D_{R(j)} =$

$[d_1, d_2, \ldots, d_{|R(j)|}]$ and $D_{Q(i)} = [d_1, d_2, \ldots, d_{|Q(i)|}]$ are the expression data vectors of the $R(j)$

and $Q(i)$ datasets, respectively, then:

955
$$d_k \sim N(\mu_{R(j)}, \sigma_{R(j)}) \ \forall \ d_k \ \in D_{R(j)}$$

956
$$d_k \sim N(\mu_{Q(i)}, \sigma_{Q(i)}) \ \forall \ d_k \ \in D_{Q(i)}$$

To be brief, we denote $N(\mu_{R(j)}, \sigma_{R(j)})$ distribution by $N_{R(j)}$, and $N(\mu_{Q(i)}, \sigma_{Q(i)})$ by $N_{Q(i)}$.

Next, we implement the cost function, $Cost_{match}(i, j)$, to consider both:

1. **Data:** $D_{R(j)}$ and $D_{Q(i)}$ expression vectors of the $R(j)$ and $Q(i)$ datasets, respectively,

2. **Models:** Gaussian distributions, $N_{R(j)}$ and $N_{Q(i)}$,

when computing the distance between $R(j)$ and $Q(i)$. To do so, we use the minimum

message length (MML) criterion[21,22] and define a Bayesian information-theoretic distance

measure. **Fig. 2** (top left) illustrates an abstract overview of our MML framework and its

place in the overall G2G alignment framework. **Supplementary Fig. 1a** further expands this

illustration to explain how the $Cost_{match}(i, j)$ computation works for a pair of reference time

point j and query time point i, as detailed by the following sections.

Primer on minimum message length inference (MML)

MML[20-22] is an inductive inference paradigm for model comparison and selection, grounded

on Bayesian statistics, information and coding theory. It facilitates designing hypothesis test

schemes specific to a problem domain. Given a hypothesis (model) H and some data D, it

lays an imaginary message transmission from a sender who jointly encodes H and D, aiming

for their lossless decoding at a recipients' side. Bayes theorem defines their joint probability

as:

976
$$Pr(H, D) = Pr(H) \cdot Pr(D|H) = Pr(D) \cdot Pr(H|D).$$

977   Separately, Shannon information defines the optimal length of a message that encodes some

978   event E with a probability $Pr(E)$ as:

979
$$I(E) = -log_e(Pr(E))$$
980 measured in nits, where I denotes information. By applying the Shannon information[54] to
981 Bayes theorem, we can map the respective probability elements in $Pr(H, D) = Pr(H) \cdot$
982 $Pr(D|H)$ onto the information space, describing the amount of Shannon information needed
983 to encode H and D jointly as:
984
$$I(H, D) = I(H) + I(D|H) \quad \text{– Equation (1)}$$
985 This gives a two-part total message length of encoding H and D jointly. The first part $I(H)$
986 refers to the message length of encoding the hypothesis H itself, whereas the second part
987 $I(D|H)$ refers to the message length of encoding the data points in D using H.
988
989 When there are two hypotheses, H_1 and H_2, that describe the same data D, MML enables us
990 to select the best hypothesis that gives a model-complexity vs. model-fit tradeoff, by
991 evaluating a compression statistic $\Delta = I(H_1, D) - I(H_2, D)$. Here, Δ is also the log odds
992 posterior ratio between the two hypotheses.
993
$$\Delta = log\left(\frac{Pr(H_2,D)}{Pr(H_1,D)}\right) = log\left(\frac{Pr(D)Pr(H_2|D)}{Pr(D)Pr(H_1|D)}\right) = log\left(\frac{Pr(H_2|D)}{Pr(H_1|D)}\right) \text{ – Equation (2)}$$
994 If $\Delta>0$, this implies that the hypothesis H_2 is e^Δ times more likely than H_1, and vice versa.
995

Casting the cost of matching between reference time point j and query time point i under MML

996
997
Given the expression data D (containing both $D_{R(j)}$ and $D_{Q(i)}$) and their estimated Gaussian
distributions ($N(\mu_{R(j)}, \sigma_{R(j)})$ and $N(\mu_{Q(i)}, \sigma_{Q(i)})$ denoted by $N_{R(j)}$ and $N_{Q(i)}$, respectively),
we formulate two different hypotheses:
1. **Hypothesis A:** assumes that the two time points match, and thus explains data D with
a single, representative Gaussian distribution $N(\mu_*, \sigma_*)$ denoted by N_* (which is either
$N_{R(j)}$ or $N_{Q(i)}$).
2. **Hypothesis Φ:** assumes that the two time points mismatch, and thus explains data
$D_{R(j)}$ with $N_{R(j)}$, and data $D_{Q(i)}$ with $N_{Q(i)}$, independently.
We then compute the two message lengths: $I(A, D)$ and $I(\Phi, D)$ according to **Equation 1** in
the above described MML formulation:
1008
$$I(A, D) = I(A) + I(D|A) \text{ – Equation (3)}$$
1009
$$I(\Phi, D) = I(\Phi) + I(D|\Phi) \text{ – Equation (4)}$$
1010 where, $A = [N_*]$ and $\Phi = [N_{R(j)}, N_{Q(i)}]$. $I(A, D)$ is the total message length of encoding A
1011 and D jointly, where $I(A)$ refers to the encoding length of the parameters μ_*, σ_* of
1012 N_* distribution. $I(D|A)$ refers to the encoding length of all data points in D based on their
1013 likelihood under $N(\mu_*, \sigma_*)$. Accordingly, we can re-write and expand **Equation 3** to:
1014
$$I(A, D) = I(N_*) + I(D|N_*)$$
1015
$$= I(\mu_*, \sigma_*) + I(D|\mu_*, \sigma_*)$$
On the other hand, $I(\Phi, D)$ is the total message length of encoding Φ and D jointly, where
$I(\Phi)$ refers to the sum of the independent encoding lengths of parameters $\mu_{R(j)}, \sigma_{R(j)}$ of $N_{R(j)}$
and $\mu_{Q(i)}, \sigma_{Q(i)}$ of $N_{Q(i)}$. $I(D|\Phi)$ refers to the sum of the independent encoding lengths of

all data points in $D_{R(j)}$ and all data points in $D_{Q(i)}$ based on their likelihood under their

respective Gaussian distributions: $N(\mu_{R(j)}, \sigma_{R(j)})$ and $N(\mu_{Q(i)}, \sigma_{Q(i)})$. Accordingly, we can

re-write and expand **Equation 4** to:

1022
$$I(\Phi, D) = I(N_{R(j)}) + I(N_{Q(i)}) + I(D|N_{R(j)}, N_{Q(i)})$$

1023
$$= I(\mu_{R(j)}, \sigma_{R(j)}) + I(\mu_{Q(i)}, \sigma_{Q(i)}) + I(D_{R(j)}|\mu_{R(j)}, \sigma_{R(j)}) + I(D_{Q(i)}|\mu_{Q(i)}, \sigma_{Q(i)})$$

1024   Note: See the next section for the equations used to compute each term in **Equation 3** and

1025   **Equation 4.**

1026

1027   Next, we normalize each total message length to compute a per datum message length (i.e.

1028   entropy), by dividing them by the total number of datapoints (single-cells) in D.

1029
$$I(A, D)_{entropy} = \frac{I(A, D)}{|D_{R(j)}| + |D_{Q(i)}|}$$

1030
$$I(\Phi, D)_{entropy} = \frac{I(\Phi, D)}{|D_{R(j)}| + |D_{Q(i)}|}$$

1031   Note: to make the $I(A, D)_{entropy}$ measure symmetric, we take the average:

1032
$$I(A, D)_{entropy} = \frac{I(N_{R(j)}, D)_{entropy} + I(N_{Q(i)}, D)_{entropy}}{2} \text{ nits per datum}$$

1033

1034   Afterwards, we compute a compression statistic Δ, which is taken as our $Cost_{match}(i, j)$:

1035
$$\Delta = I(A, D)_{entropy} - I(\Phi, D)_{entropy}$$

1036
$$Cost_{match}(i, j) = \Delta$$

1037   As in **Equation 2,** this reflects the log odds posterior ratio:

1038
$$I(A, D) - I(\Phi, D) = log\left[\frac{Pr(D) \cdot Pr(\Phi|D)}{Pr(D) \cdot Pr(A|D)}\right] = log\left[\frac{Pr(\Phi|D)}{Pr(A|D)}\right]$$

1039   When $R(j)$ and $Q(i)$ are very dissimilar, the total encoding length under hypothesis A (i.e.

1040   the time points match) results in a larger value compared to that of hypothesis Φ (i.e. the time

1041   points mismatch). Thus, $Cost_{match}(i, j)$ increases as the distributions deviate from each other

1042   (**Extended Data Fig. 1b, Supplementary Fig. 1b,c**).

1043

Computing the total encoding message length for any Gaussian model N_* and data D of

size N

The above described $Cost_{match}(i, j)$ distance measure is computed using the standard MML

Wallace Freeman approximation[21,54] defined for a Gaussian distribution[22,55,56]. As defined by

Equation 1, for any dataset D and a hypothesis H that describes $D = [x_1, x_2, \ldots, x_N]$ under a

Gaussian distribution $N(\mu, \sigma)$ with parameters $\vec{\theta} = (\mu, \sigma)$, the total message length of

encoding H and D jointly is given by:

1051
$$I(H, D) = I(\vec{\theta}, D) = I(\vec{\theta}) + I(D|\vec{\theta})$$

1052   MML Wallace Freeman approximation expands this to:

1053
$$I(\vec{\theta}, D) = \frac{d}{2} log(\kappa_d) - log[h(\vec{\theta})] + \frac{1}{2} log(det[Fisher(\vec{\theta})]) + L(\vec{\theta}) + \frac{d}{2}$$

1054   , where d is the number of free parameters ($d = 2$ for a Gaussian), and κ_d is the Conway

1055   lattice constant[57] (κ_d is $\frac{5}{36\sqrt{3}}$ for $d = 2$). Here: $h(\vec{\theta})$ is the prior over the parameters. μ is

1056   defined with a uniform prior over a predefined range of length R_μ. $log(\sigma)$ is defined with a

1057   uniform prior over a predefined range of length R_σ. Accordingly,

1058
$$h(\vec{\theta}) = h(\mu) \cdot h(\sigma) = (\frac{1}{R_\mu})(\frac{1}{\sigma R_\sigma})$$

1059
$$\Rightarrow I[h(\vec{\theta})] = -log[h(\vec{\theta})] = log(\sigma) + log(R_\mu R_\sigma)$$

1060   We use R_μ=15.0 and R_σ= 3.0 as reasonable for log normalized gene expression data.

1061 $L(\vec{\theta})$ is the negative log likelihood:

1062
$$L(\vec{\theta}) = N\,log(\sigma) + \frac{N}{2}log(2\pi) + \frac{1}{2\sigma^2}\sum_{i=1}^{N}(x_i - \mu)^2 - \sum_{i=1}^{N}log(\epsilon)$$

1063   where, ϵ is the precision of measurement for each data point (taken as ϵ=0.001).

1064 $det[Fisher(\vec{\theta})]$ is the determinant of the expected Fisher matrix (i.e. the matrix of the

1065   expected second derivatives of the negative log likelihood function). This determinant has the

1066   closed form: $\frac{2N^2}{\sigma^4}$.

1067

The cost of alignment state assignment for the reference time point j and query time

point i

The DP scoring scheme also involves computing a cost of assigning a certain alignment state

$x \in \Omega$ =[m, w_d, w_i, d, i] for the two time points j and i. This state assignment cost is

computed as the amount of Shannon information[54] required to encode state x given the

assigned state y for the preceding time points. As previously said, in information theory,

Shannon information defines the optimal length of a message that encodes some event E with

a probability $Pr(E)$ as: $I(E) = -log_e(Pr(E))$ measured in nits, where I denotes

information. Accordingly, the cost of assigning state x given a previous state y is: $I(x|y) =$

$-log_e(Pr(x|y))$. We define a five-state machine (**Extended Data Fig. 1a**) to explain these

conditional probabilities of state assignments (a.k.a state transitions).

1079

This finite state machine extends the general three-state alignment machine[17,18] which has a

match (m) state, delete (d) state, and insert (i) state, by adding two new states: compression

warp (w_d) state and expansion warp (w_i) state (**Fig. 1b**). The warp states are equivalent to the

match state but are extensions to accommodate one-to-many and many-to-one matches

between the two series, respectively. As in the three-state alignment machine[19], we enforce

symmetry, while prohibiting an invalid transition from an indel state to a warp state. That is,

we do not allow i→w_d and d→w_i, as they can be covered by a single m state in the first

place. On the other hand, we have the choice of allowing d→w_d and i→w_i, as there can be

a legitimate case of a warp match after an insertion or deletion. Note: all the outgoing

transitions of each state in this finite state machine add up to a probability of 1. It also treats

<i and d> and <w_i and w_d> equivalently. Consequently, there are 23 total number of state

transitions in this machine, yet there are only three free transition probability

parameters: $[Pr(m|m), Pr(i|i), Pr(m|i)]$, due to the symmetry and characteristics of the

machine. These probabilities control the expected lengths of a match and a mismatch. In this

work, we have chosen reasonable values $[Pr(m|m)$=0.99, $Pr(i|i)$=0.25, $Pr(m|i)$=0.4] based

on manual tuning. However, we note that these parameters can be automatically inferred
using an added layer of optimization and time complexity on top of the main DP
optimization, which will be an interesting future direction to follow.

1098

1099   Altogether, our G2G DP scoring scheme utilizes the $Cost_{match}(i,j)$ function, and the above
1100   described state assignment costs (i.e. all possible state transition costs evaluated as $I(x|y)$ for
1101   all possible $y \to x$ state transitions under the five-state machine), are then used to define the
1102   recurrence relations of our DP algorithm.

1103

Dynamic programming recurrence relations We formulate the DP problem using five
history matrices $[Hist_m, Hist_{w_d}, Hist_{w_i}, Hist_d, Hist_i]$, where each matrix corresponds to
each alignment state in Ω, respectively. Any history matrix, $Hist_x$ for state $x \in \Omega$, has the
dimensions $(|Q| + 1 \times |R| + 1)$. In other words, the columns correspond to the time points in
the reference series R, while the rows correspond to the time points in the query series Q.
Each cell $Hist_x(i,j)$ stores the optimal cost of aligning the prefix time series $R[1..j]$ and
$Q[1..i]$ ending in state x. The DP recurrence relations to compute each matrix cell (i,j) of
each history matrix for $i > 0, j > 0$ are:

$$
\text{Hist}_{\mathtt{m}}(i,j) = \min \begin{cases}
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{m}}(i-1,j-1) + I(\mathtt{m}|\mathtt{m}) \\
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{w_d}}(i-1,j-1) + I(\mathtt{m}|\mathtt{w_d}) \\
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{w_i}}(i-1,j-1) + I(\mathtt{m}|\mathtt{w_i}) \\
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{d}}(i-1,j-1) + I(\mathtt{m}|\mathtt{d}) \\
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{i}}(i-1,j-1) + I(\mathtt{m}|\mathtt{i})
\end{cases}
$$

$$
\text{Hist}_{\mathtt{w_d}}(i,j) = \min \begin{cases}
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{m}}(i,j-1) + I(\mathtt{w_d}|\mathtt{m}) \\
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{w_d}}(i,j-1) + I(\mathtt{w_d}|\mathtt{w_d}) \\
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{w_i}}(i,j-1) + I(\mathtt{w_d}|\mathtt{w_i}) \\
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{d}}(i,j-1) + I(\mathtt{w_d}|\mathtt{d})
\end{cases}
$$

$$
\text{Hist}_{\mathtt{w_i}}(i,j) = \min \begin{cases}
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{m}}(i-1,j) + I(\mathtt{w_i}|\mathtt{m}) \\
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{w_d}}(i-1,j) + I(\mathtt{w_i}|\mathtt{w_d}) \\
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{w_i}}(i-1,j) + I(\mathtt{w_i}|\mathtt{w_i}) \\
\text{Cost}_{match}(i,j) + \text{Hist}_{\mathtt{i}}(i-1,j) + I(\mathtt{w_i}|\mathtt{i})
\end{cases}
$$

$$
\text{Hist}_{\mathtt{d}}(i,j) = \min \begin{cases}
\text{Hist}_{\mathtt{m}}(i,j-1) + I(\mathtt{d}|\mathtt{m}) \\
\text{Hist}_{\mathtt{w_d}}(i,j-1) + I(\mathtt{d}|\mathtt{w_d}) \\
\text{Hist}_{\mathtt{w_i}}(i,j-1) + I(\mathtt{d}|\mathtt{w_i}) \\
\text{Hist}_{\mathtt{d}}(i,j-1) + I(\mathtt{d}|\mathtt{d}) \\
\text{Hist}_{\mathtt{i}}(i,j-1) + I(\mathtt{d}|\mathtt{i})
\end{cases}
$$

$$
\text{Hist}_{\mathtt{i}}(i,j) = \min \begin{cases}
\text{Hist}_{\mathtt{m}}(i-1,j) + I(\mathtt{i}|\mathtt{m}) \\
\text{Hist}_{\mathtt{w_d}}(i-1,j) + I(\mathtt{i}|\mathtt{w_d}) \\
\text{Hist}_{\mathtt{w_i}}(i-1,j) + I(\mathtt{i}|\mathtt{w_i}) \\
\text{Hist}_{\mathtt{d}}(i-1,j) + I(\mathtt{i}|\mathtt{d}) \\
\text{Hist}_{\mathtt{i}}(i-1,j) + I(\mathtt{i}|\mathtt{i})
\end{cases}
$$

1112
1113
As previously described, $Cost_{match}(i,j)$ measures the distance between the two interpolated
gene expression distributions corresponding to the reference time point j and query time point
i. The cost term $I(x|y) \; \forall \; x, y \in \Omega$ refers to the Shannon information of a state transition $y \to$
x (e.g. $I(i|m)$ is the cost of $m \to i$, computed as $-log_e[Pr(i|m)]$), based on the five-state

alignment machine as explained before. Prior to computing the above relations, the history
matrices are initialized as:

$$\text{Hist}_x(i,j)_{x \in \{m, w_d, w_i\}} = \begin{cases} 0 & \text{for } i > 0, j > 0 \\ \infty & \text{otherwise} \end{cases}$$

$$\text{Hist}_i(i,j) = \text{Hist}_i(i-1,0) + I(i|i)$$
$$\text{Hist}_d(i,j) = \text{Hist}_d(0,j-1) + I(d|d)$$

1120
1121 Note: For the cases of $<i = 1$ and $j = 1>$ (i.e. before the first state transition), we assign a
1122 uniform transition cost: $I(m) = I(i) = I(d) = -log_e(1/3)$. All the five history matrices are
1123 computed by running the aforementioned DP algorithm. We then generate the optimal
1124 alignment Y^* as a five-state string by backtracking, starting from the cell:

$$\min \begin{cases} \text{Hist}_m(|Q|, |R|) \\ \text{Hist}_{w_d}(|Q|, |R|) \\ \text{Hist}_{w_i}(|Q|, |R|) \\ \text{Hist}_d(|Q|, |R|) \\ \text{Hist}_i(|Q|, |R|) \end{cases}$$

1125
1126 Note: The optimal alignment cost landscape matrix L can be visualized by constructing:
1127 $$L(i,j) = min_{\forall x \in \Omega}\{Hist_x(i,j)\}$$
1128
Y^* is the optimal alignment between R and Q time series that minimizes the total DP
alignment cost under our DP scoring scheme and recurrence relations. In other words,
Y^* describes the optimal set of reference time point and query time point pairs that are
matched, as well as the optimal set of reference time points and query time points that are
mismatched. The kth character in Y^*, i.e., $Y^*[k]$, gives the alignment state for the
corresponding reference and query time points ($Y^*[k] \in \Omega = $[m, w$_d$, w$_i$, i, d]). Let the set of
matched time point pairs (i, j) in Y^* be denoted by $T_{matched}$. Then, the total alignment cost of
Y^* is the sum of the total match cost (C_{match}) and the total state assignment cost (C_{state}),
where:

$$1138 \quad C_{match}(Y^*) = \sum_{\forall(i,j) \in T_{matched}} Cost_{match}(i,j)$$

$$1139 \quad C_{state}(Y^*) = \sum_{k=1}^{|Y^*|} I(Y^*[k]|Y^*[k-1])$$

1140 under our scoring scheme.
1141 Overall, the optimal alignment Y^* is generated by optimizing the following objective
1142 function:
1143 $$Y^* = argmin \, \forall Y \in \mathbf{Y} \, \{C_{match}(Y) + C_{state}(Y)\}$$
1144 where $\mathbf{Y}$ is the space of all possible five-state alignment hypotheses.
1145
Note on using a custom $Cost_{match}(i,j)$ function: Our MML-based $Cost_{match}(i,j)$ function
defines a distribution-based distance measure to compute the cost of matching the reference
time point j and query time point i based on their gene expression distributions (as explained

in the previous sections). Considering expression distributions rather than just the mean
expression values allows us to make technical/batch variations implicit. However, we note
that this can be any cost function (e.g. KL-divergence) which can measure the distance
between two Gaussian distributions. However, our MML-based compression statistic Δ
enables us to define a complete description of each hypothesis, which considers both model-
complexity and data-fit. On the other hand, KL-divergence is equivalent to the expected log-
likelihood ratio, which does not take the complexity of model parameters into account.
1156
1157 **Reporting alignment statistics over gene-level alignments**
1158
1159 G2G generates individual alignments for all genes of interest by running the DP alignment
1160 algorithm (detailed in the previous section) independently for each gene between the
1161 reference and query. Each optimal alignment output is a five-state alignment string describing
1162 the matches and mismatches. These gene-level alignments are further analyzed to generate
1163 useful statistics and insights as below.
1164
Distribution of Alignment similarities The percentage of total matching (i.e. one-to-one
matches and warps) (termed as 'alignment similarity' percentage) in each five-state gene-
alignment string, as well as its average across all genes, provide quantitative measures of the
degree of concordance between the reference and query. We also generate a single aggregate
alignment across all genes using each of their optimal alignment landscapes. Recall that any
matrix cell (i, j) in the optimal alignment landscape (i.e. $L(i, j) = min_{\forall x \in \Omega}\{Hist_x(i, j)\}$)
refers to the optimal ending alignment state of the prefix time series $R_{1..j}$ and $Q_{1..i}$. Thus,
across such matrices of all genes, there is a five-state frequency distribution for each (i, j). To
generate an average alignment, we start a traversal from the right-most bottom cell $(|Q| +$
$1, |R| + 1)$, and choose the most probable alignment state $x \in \Omega$ for $R_{|R|}$ and $Q_{|Q|}$ time points
as the most frequent state across all genes. According to this state, we traverse to the next
matrix cell (i.e. if it is m, we go to $(i - 1, j - 1)$; if it is d, we go to $(i, j - 1)$ and so on). By
the time we reach the cell $(0,0)$, we have a representative five-state alignment string.
1178
Clustering five-state alignment strings Given a set of five-state alignment strings (i.e. gene-
specific alignments), we employ a string clustering approach to identify groups of genes that
show similar temporal matching and mismatching patterns. This requires the definition of a
distance measure between two alignment paths. While the polygonal area based distance
measure[58] is ideal for three-state alignment strings, it is unable to distinguish between warps
and indels. Thus, we use a binary encoding scheme that transforms each five-state alignment
string into a binary vector of size $|R| + |Q|$. This is done by traversing through the alignment
path, recording for each trajectory, the match/mismatch state of their respective pseudotime
points (i.e a match state $x \in [m, w_d, w_i]$ is encoded by 1; a mismatch state $x \in [i, d]$ is
encoded by 0). The resultant binary strings of R and Q are then concatenated to numerically
represent their alignment path. Next, the binary representation of each gene-specific
alignment is used to compute a pairwise Hamming distance matrix between all pairs of
alignments, which is then input to standard agglomerative hierarchical clustering (under the

average linkage method; using the Python *sklearn.cluster* package). The threshold parameter
for linkage distance controls the level at which the cluster merge stops, allowing inspection of
the clusters at different levels of a clustering hierarchy.

1195

Pathway overrepresentation analysis The alignment similarity percentage of each gene-
specific alignment allows us to rank all the genes, from which we select the top k
mismatching genes to analyze their pathway overrepresentation. The identified clusters of
genes are also analyzed. We use the GSEApy Enrichr[58–60] wrapper against the
MSigDB_Hallmark_2020[61] and *KEGG_2021_Human* pathway genesets[61,62]. For all analyses,
a 0.05 significance threshold of the adjusted P-value (with the default FDR correction method
used by GSEApy) was applied.

1203

1204 **<u>Datasets</u>**

1205

1206 **Datasets for simulated experiments**

1207

Simulating pairwise datasets with different alignment patterns using Gaussian
Processes
We modeled log-normalized expression of a gene x as a function f of time t using a
Gaussian Process (GP), a stochastic process where any finite instantiation of it follows a
multivariate Gaussian distribution. In other words, it is a distribution of functions, from
which we can sample an $f(t)$:

$$f(t) \sim GP(\vec{\mu}(t), K(t, t'))$$

1215

where, μ is the mean vector, and $K(t, t')$ is a kernel function which evaluates a covariance
matrix covering every pair of finite time points where the $f(\text{t})$ is evaluated. The
characteristics of this function are controlled by the class of the kernel being used (e.g. a
Radial Basis Function (RBF) kernel for generating smooth, non branching functions; a
change point kernel for generating branching functions). Therefore, a GP with an appropriate
kernel is ideal to simulate different trajectory patterns in single-cell gene expression across
pseudotime. Following the standard textbook and kernels discussed in literature[24,25], we
implemented a simulator for three different types of pairwise trajectory patterns: (1)
Matching, (2) *Divergence*, and (3) *Convergence*, across a pseudotime range [0,1] with 300
total number of simulated cells for each trajectory.

1226

Generating a *Matching* pair of reference and query gene trajectories We used a GP with
a constant c mean vector $\vec{\mu_c}$ ($c \in [0.5, 9.0]$ uniform random sampled) and RBF kernel K to
first sample a function $\mu(t)$ that describes an average expression value for each time point.
Next, we sampled two gene expression trajectories: $GEX_{ref}(t)$ and $GEX_{query}(t)$, from a GP
where the mean is $\mu(t)$ and the covariance matrix is $\sigma^2 I$ ($\sigma \in [0.05, 1.0]$ uniform random
sampled, and I= identity matrix).

$$\mu(t) \sim N(\vec{\mu_c}, K)$$
$$GEX_{ref}(t) \sim N(\mu(t), \sigma^2 I)$$

$$GEX_{query}(t) \sim N(\mu(t), \sigma^2 I)$$

Generating a *Divergence* pair of reference and query gene trajectories Here we use a Change Point (CP) kernel which imposes a bifurcation in the trajectory as it reaches an approximate time point t_{CP} (a.k.a. change point). The idea is to activate one covariance function before t_{CP} and another covariance function after t_{CP}. We used the below CP kernel[24,25] K_{CP}:

$$K_{CP}(t, t') = aK_1(t, t') + a'K_2(t, t')$$

where,

$$a = \sigma(t)\sigma(t')$$
$$a' = [1 - \sigma(t)][1 - \sigma(t')]$$
$$\sigma(x) = \frac{1}{1 + exp(-s(x - t_{CP}))} \text{ (sigmoid function)}$$

with s acting as a steepness parameter, deciding how steep the change point is. Penfold et al (2018)[24] defines a branching process by enforcing a zero kernel (K_1) imposed before t_{CP} and another suitable kernel (K_2) afterwards. We used an RBF for K_2. Following is the generative process starting with a base mean function $\mu(t)$ sampled from a separate GP with a constant c mean vector $\overrightarrow{\mu_c}$ ($c \in [0.5, 9.0]$ uniform randomly sampled), and an RBF kernel K.

$$\mu(t) \sim N(\overrightarrow{\mu_c}, K)$$
$$f_1(t) \sim N(\mu(t), K_{CP})$$
$$f_2(t) \sim N(\mu(t), K_{CP})$$
$$GEX_{ref}(t) \sim N(f_1(t), \sigma^2 I)$$
$$GEX_{query}(t) \sim N(f_2(t), \sigma^2 I)$$

Next, two functions were sampled from a GP with base $\mu(t)$ and CP(t,t'), which were then used as mean vectors to generate $GEX_{ref}(t)$ and $GEX_{query}(t)$ with covariance matrix $\sigma^2 I$ (σ=0.3). This was run for [t_{CP}=0.25, t_{CP}=0.5, t_{CP}= 0.75] to obtain 3 different groups of *Divergence* with varying bifurcation points. We use a constant σ which is not too low and not too high, and also apply a filtering criteria to ensure that the final dataset includes pairs of simple and clear divergence (a stable ground truth with no complex patterns). Pairs are filtered through basic heuristics such as the difference between mean expression before divergence and at the end terminals of reference and query.

Extended Data Fig. 2 shows that the branching effect may start approximately before the change point. Therefore, we expect the early non-divergent segment to continue at least until time point $i < t_{CP}$ where we begin to see > 0.01 covariance in the change point kernel. Accordingly, given our approx_bifurcation_start_point $= i$, we expect the range of match lengths to fall between a lower limit $= n\_total\_pseudotime\_points \times i$ and upper limit $= n\_total\_pseudotime\_points \times change\_point$. Equivalently, we expect mismatch lengths to fall between $n\_total\_pseudotime\_points \times (1 - i)$ and upper limit $= n\_total\_pseudotime\_points \times (1 - change\_point)$.

1277 **Generating a *Convergence* pair of reference and query gene trajectories** For
1278 *Convergence,* we simply inverted the above generated divergent trajectory pairs, as the
1279 *Convergence* and *Divergence* patterns are complementary to each other.
1280

Simulating mismatches on real scRNA-seq data
We downloaded the mouse pancreas development dataset[26] from the CellRank python
package[63]. We subset the dataset to include only cells in the beta-cell lineage, using the
annotations from the original authors (selecting cells labeled as "Ngn3 low EP", "Ngn3 high
EP", "Fev+", "Beta"), retaining 1845 cells. To select genes varying along beta-cell
differentiation, we ran the CellRank pipeline (v1.5.1) to compute lineage drivers, following
the package tutorials
(https://cellrank.readthedocs.io/en/stable/auto_examples/estimators/compute_lineage_drivers.html) and selected genes
significantly associated with differentiation potential to beta-cells (at 1% FDR we selected
769/2000 highly variable genes). For the pseudotime axis, we used the diffusion pseudotime
estimated by the CellRank authors. To simulate trajectories for alignment, we divided the
diffusion pseudotime (between 0 and 1) equally into 50 bins, assigned cells to the bins based
on their estimated pseudotime and randomly split cells into query and reference datasets in
each bin. To simulate deletions of n bins, we excluded query cells from the first n pseudotime
bins (i.e. cells where the pseudotime value was less or equal to the upper margin of the nth
bin). To simulate mismatches of n bins, we found the pseudotime bin with highest mean
expression for the gene of interest in the query cells, and calculated mean (*max_mean*) and
standard deviation (*max_std*) of expression of query cells for this bin; then, for each of the
first n pseudotime bins, we substitute expression values of the query cells with a sample from
a normal distribution with mean = *max_mean* + *max_std* and standard deviation = *max_std* .
Pseudotime values for the query cells were min-max normalized to [0,1] after perturbation.
We then ran the G2G alignment on each tested gene and calculated their alignment similarity
(match calling) percentages.
1304

1305 **Datasets for benchmarking G2G**
1306

Dendritic cell stimulation dataset
The normalized single-cell expression datasets of PAM/LPS stimulation and their pseudotime
estimates were downloaded from the CellAlign[5] github repository and converted into
Anndata objects. These contain two gene sets: 'core antiviral module' (99 genes) and 'peaked
inflammatory module' (89 genes), pre-selected from the original publication[23] and referred to
as global and local modules, respectively by Alpert et al (2018)[5]. The datasets include 179
PAM-stimulated cells and 290 LPS-stimulated cells for which the pseudotime has been
estimated by CellAlign authors using Diffusion-maps.
1315

Simulated dataset containing trajectories with no shared process
This is a simulated, negative control dataset which was generated using the published script
by Laidlaw et al (2023) (in the TrAGEDy[11] Git repository). Their script uses DynGen[64], a
single-cell data simulator for dynamic processes. The resulting negative dataset contains two

trajectories simulated under two different gene regulatory networks and TF activity, ensuring
that there is no shared process between them. The reference and query trajectories have 619
genes across 2000 and 1940 cells, respectively.

1323

We reproduced the high-dimensional alignments from CellAlign and TrAGEDy over the 619
genes in this dataset by re-running the scripts provided by Laidlaw et al (2023). Here,
CellAlign uses Euclidean distance, whereas TrAGEDy uses Spearman correlation. Note: For
gene-level alignment, TrAGEDy was run using the Euclidean distance as in CellAlign; this is
because Spearman correlation is mathematically undefined for a single gene dimension. We
input log normalized, scaled gene expression data to CellAlign, following its documentation.

1330

1331   **Dataset preparation for *in vivo in vitro* T cell development comparison**

1332

Cell cultures for artificial thymic organoid (ATO) and single-cell RNA sequencing
experiment
MS5 line transduced with human DLL4 was obtained from G. Crooks (UCLA) as a gift. The
MS5-hDLL4 cells were cultured in DMEM (Gibco) with 10% FBS. Two iPSC lines were
used in this study. Cell lines HPSI0114i-kolf_2 (Kolf) and HPSI0514i-fiaj_1 (Fiaj) were
obtained from the Human Induced Pluripotent Stem Cell initiative (HipSci: www.hipsci.org)
collection. All iPSC lines were cultured on vitronectin (diluted 1:25 in PBS; Gibco) coated
plates, in TeSR-E8 media (Stemcell Technologies).

1341

We followed the PSC-ATO protocol as previously described[31]. iPSC cells were harvested as
a single-cell suspension and seeded (3×10^6 cells per well) in GFR reduced Matrigel (Corning)
- coated 6-well plates in X-VIVO 15 media (Lonza), supplemented with rhActivin A,
rhBMP4, rhVEGF, rhFGF (all from R&D Systems), and ROCK inhibitor (Y27632; LKT
Labs) on day −17, and only rhBMP4, rhVEGF and rhFGF on days −16 and −15. Cells were
harvested 3.5 days later (day−14) , and isolated by FACS for CD326⁻CD56⁺ (PE anti-human
CD326 antibody, Biolegend, 324205; APC anti-human CD56 antibody, Biolegend, 318309)
human embryonic mesodermal progenitors (hEMPs).

1350

Isolated hEMPs were combined with MS5-hDLL4 at a ratio of 1:50. Two or three cell-dense
droplets (5×10^5 cells in 6 μl hematopoietic induction medium) were deposited on top of an
insert in each well of a six-well plate. Hematopoietic induction medium composed of EGM2
(Lonza) supplemented with ROCK inhibitor and SB blocker (TGF-β receptor kinase inhibitor
SB- 431542; Abcam) was added into the wells outside the inserts so that the cells sat at the
air-liquid interface. The organoids were then cultured in EGM2 with SB blocker for 7 days
(days −14 to −7), before the addition of cytokines rhSCF, rhFLT3L, rhTPO (all from
Peprotech) between days −6 to 0. These 2 weeks formed the hematopoietic induction phase.
On day 1, media was changed again to RB27 (RPMI supplemented with B27 (Gibco),
ascorbic acid (Sigma-Aldrich), penicillin/streptomycin (Sigma-Aldrich) and glutamax
(Thermo Fisher Scientific)) with rhSCF, rhFLT3L and rhIL7. The organoids can be
maintained in culture for 7 more weeks in this medium.

1363

For dissociation of organoids on day −7, they were removed from culture insert and
incubated in digestion buffer, which consisted of collagenase type IV solution (StemCell
Technologies) supplemented with 0.88mg/ml collagenase/dispase (Roche) and 50U DNase I
(Sigma), for 20 minutes at 37°C. Vigorous pipetting was performed in the middle of the
incubation and at the end. After complete disaggregation, single cell suspension was prepared
by passing through a 50-μm strainer.

1370

1371 For dissociation of organoids from day 0 onwards, a cell scraper was used to detach ATOs
1372 from cell culture insert membranes and detached ATOs were then submerged in cold flow
1373 buffer (PBS (Gibco) containing 2% (v/v) fetal bovine serum (FBS; Gibco) and 2 mM EDTA
1374 (Invitrogen)). Culture inserts were washed and detached ATOs were pipetted up and down to
1375 form single-cell suspension before passing through a 50-μm strainer.

1376

Cells were then stained with designed panels of antibodies and analyzed by flow cytometry.
FACS was performed at the same time and live human DAPI⁻anti-mouse CD29⁻ (APC/Cy7
anti-mouse CD29 antibody, Biolegend, 102225) cells were sorted for day −7, day 0 and week
3 samples, and live (DAPI−) cells were sorted for week 5 and week 7 samples before loading
onto each channel of the Chromium chip from Chromium single cell V(D)J kit (10X
Genomics). The metadata for all the ATO samples can be found in **Supplementary Table
50.** For the day −14 sample, some sorted (both hEMP and the rest of DAPI⁻ fraction) and
unsorted cells were stained with hashtag antibodies (TotoalSeq-C antibodies from Biolegend,
see **Supplementary Table 51**, following 10X cell surface protein labeling protocol) before
being mixed together with some mouse stromal cells (MS5-hDLL4) for 10X loading. For
week 1 sample, hashtag antibodies were added in at the same time as the FACS antibodies
i.e., before sorting.

1389

Single-cell cDNA synthesis, amplification and gene expression (GEX) and cell surface
protein (CITE-seq) libraries were generated following the manufacturer's instructions.
Sequencing was performed on the Illumina Novaseq 6000 system. The gene expression
libraries were sequenced at a target depth of 50,000 reads per cell using the following
parameters: Read1: 26 cycles, i7: 8 cycles, i5: 0 cycles; Read2: 91 cycles to generate 75-bp
paired-end reads.

1396

ATO data preprocessing and annotation
Raw scRNA-seq reads were mapped with cellranger 3.0.2 with combined human reference of
GRCh38.93 and mouse reference of mm10-3.1.0. Low quality cells were filtered out
(minimum number of reads = 2000, minimum number of genes = 500, maximum number of
genes = 7000, Scrublet[65] (v0.2.3) doublet detection score < 0.15, mitochondrial reads fraction
< 0.2). Cells where the percentage of counts from human genes was < 90% were considered
as mouse cells and excluded from downstream analysis. Cells were assigned to different cell
lines (Kolf, Fiaj) using genotype prediction with Souporcell (v2.4.0)[66]. The mapping outputs
of the eight samples were merged, with the sample ID prepended to the barcode IDs in both
the BAM and barcodes.tsv to prevent erroneous cross-sample barcode overlap. Souporcell

was run with `--skip_remap True --K 2` and the common variants file based on common
(>= 2% population allele frequency) SNPs from 1000 genomes data, as distributed in the
tool's repository. We selected 2 clusters due to the already known 2 cell lines. Next the data
went through the standard pipeline of filtering out genes (cell cycle[67] genes, genes detected in
less than 3 cells), and normalizing the per cell total count to 10,000 followed by log1p
transformation and scaling to zero mean and unit variance (with max_value = 10 to clip after
scaling), using SCANPY[68]. The final dataset had 31,483 ATO cells with 23,526 genes which
were input to CellTypist[6] (for prediction using pre-trained logistic regression classifier –
Pan_Fetal_Human model under majority voting). We then obtained a Uniform Manifold
Approximation and Projection (UMAP) embedding for this dataset based on its scVI[33] batch
corrected embedding (v0.14.5 with 10 latent dimensions (default), 2 hidden layers, 128 nodes
per hidden layer (default), and 0.2 dropout rate for the neural network), and subsetted cells to
non-hematopoietic lineage, T/ILC/NK lineage, and other hematopoietic lineage cells
(**Extended data Fig. 8**) using their Leiden clustering. By default, scVI models gene counts
with zero-inflated negative binomial distribution, defines a normal latent distribution, and
handles batch effects. For each lineage, scVI latent dimensions and UMAP embedding were
re-computed and cell types were annotated by inspecting both the CellTypist results and
marker gene expression.
1425
Joint Embedding of reference and organoid in preparation for pseudotime estimation
We downloaded the annotated human fetal atlas dataset from
https://developmental.cellatlas.io/fetal-immune and extracted the cell types (79,535 cells in
total) representing the T cell developmental trajectory starting from progenitor cells towards
Type 1 Innate T cells (T1 dataset), including Cycling MPP, HSC_MPP, LMPP_MLP,
DN(early) T, DN(P) T, DN(Q) T, DP(P) T, DP(Q) T, ABT(entry) and Type 1 innate T cells.
We then compiled a reduced representation (20,384 cells) that preserve their underlying cell
type composition. This was done by random subsampling from each cell type (with minimum
sample size = 500 cells, aiming ~20,000 total number of cells) based on their originally
published annotations. Such stratified-sampling approach is practical for dealing with
massive single-cell datasets to reduce computational resource requirements. Separately, we
extracted the cell types from the ATO dataset (19,013 cells) representing the trajectory
starting from iPSCs towards SP T cells, including iPSC, primitive streak, mesodermal
progenitor, endothelium, HSC_MPP, HSC_MPP/LMPP_MLP/DC2, DN(early) T, DN T,
DP(P) T, DP(Q) T, ABT(entry), SP T cells.
1441
Then the T1 and ATO datasets were merged and preprocessed together by filtering out cells
with more than 8% total mitochondrial UMI, cell cycle genes[67] and genes expressed in less
than 3 cells (`min_cells = 3`). Next, the highly variable genes were selected after per cell
count normalization to 10,000 reads per cell and log1p normalization. The T1 pan fetal
reference had 33 batches (due to different 10X chemistry 3' *versus* 5' and different donors),
while the ATO had only 2 batches (due to 2 cell lines, Kolf and Fiaj). This merged dataset
was then input to constructing a joint latent embedding using the scVI (v0.14.5) variational
autoencoder implementation[33] (with 10 latent dimensions (default), 2 hidden layers, 128
nodes per hidden layer (default) and 0.2 dropout rate for the neural network). The joint

embedding was then taken to build the cell neighborhood graph and UMAP embedding using
SCANPY[68]. The final T1 and ATO datasets comprise 20,327 cells and 17,176 cells
respectively. 18,436 cells of T1 and 10,089 cells of ATO belong to T cell lineage, i.e., DN T
onwards.
1455
We followed a similar preprocessing for the pan fetal reference representing the trajectory
towards CD8+T (CD8 dataset) (including Cycling MPP, HSC_MPP, LMPP_MLP, DN(early)
T, DN(P) T, DN(Q) T, DP(P) T, DP(Q) T, ABT(entry) and CD8+T cells). The initially
extracted CD8 subset (83,177 cells) was reduced to 20,412 cells, which was then merged
with the 19,013 ATO cells and subjected to the same filtering and normalization as for the
T1+ATO merge prior to scVI integration. The final CD8 dataset comprises 20,324 cells of
which, 18,490 cells are DN T onwards.
1463
Pseudotime estimation using the Gaussian Process Latent Variable Model
The differentiation pseudotime was estimated separately for T1 reference, CD8 reference and
ATO by employing the Gaussian Process Latent Variable Model (GPLVM)[34,37]. GPLVM is a
probabilistic non-linear dimensionality reduction method which models observed gene
expression as a function $f(X)$ of a set of latent covariates X. It enables us to incorporate
Gaussian time priors when estimating pseudotime as a latent dimension. We used the Pyro[69]
GPLVM implementation (Pyro v1.8.0) with Sparse Gaussian Process inference (32 inducing
points) and Radial Basis Function kernel to obtain a 2D latent embedding, where the first
latent dimension corresponds to pseudotime and the second latent dimension corresponds to a
second level of latent effects (e.g. batch). The first dimension was assigned a Gaussian prior
with cell capture times as the mean. The second latent dimension was zero initialized to allow
for a second level of latent effects (e.g. batch). The model used Adam optimizer to infer the
optimal latent embedding with 2000 iterations (where the loss curve reasonably converged).
1477
For the ATO, the GPLVM was initialized with cell capture days as the prior. Since there was
no temporal data present in the pan fetal reference, we first approximated time prior for each
reference cell as the weighted average of their k-nearest organoid neighborhood (kNN)
capture time. A k=3 organoid neighborhood for a reference cell was obtained using the
cKDTree based search method implemented in BBKNN[70] on their scVI based UMAP
embedding. Contribution of each organoid neighbor was weighted according to its distance.
(kNN distance vector was softmax transformed, and the normalized reciprocal of each
distance was taken as the associated weight, enforcing less contribution from distant
neighbors towards the weighted average). This approximation may introduce outliers due to
the spatial arrangement of different cell types in the UMAP. Thus, we leveraged the known
cell-type annotations to refine the approximation by assigning each reference cell with the
average approximated capture time of its cell type. These approximated capture times were
scaled to be in [0,1] range and input as the mean prior to the previously described GPLVM.
For T1 and CD8 GPLVMs, the input gene space was 2608 genes and 2616 genes respectively
(same as at scVI integration). To ensure no outliers, the GPLVM estimated pseudotime was
further refined by correcting outliers of each cell type using the cell-type specific average of
estimated pseudotime. Outliers were selected based on the Interquartile Range (IQR) rule (i.e.

1.5 times IQR below the first quartile and above the third quartile of the cell-type specific
pseudotime distribution).
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Genes2Genes alignment
For the complete T1 vs ATO comparison using G2G, the total common gene space of 20,240
genes was considered upon filtering genes with less than 3 cells expressed, 10,000 total count
per cell normalization, and log1p normalization. For the DN T onwards comparison, there
were 17,718 genes for T1 vs. ATO, and 20,183 genes for CD8 vs. ATO. All pseudotime
estimates were min-max normalized to ensure [0,1] range. These total gene spaces were
subsetted to include only the transcription factors[40] (1371 TFs) and relevant signaling
pathways focused in this work. G2G alignment was performed using 15 equispaced
pseudotime points.
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1508 **Software packages used in the work**
1509 Genes2Genes framework and all analysis related code (including plot generation) were
1510 implemented using the standard Python libraries (Numpy, Pandas, Seaborn, scikit-learn),
1511 GPyTorch, GSEApy. Illustrations were made using Adobe Illustrator 2023 and BioRender.

Code and data availability

Genes2Genes is implemented as an open-source package in Python 3 (v3.8) with tutorial
available at: https://github.com/Teichlab/Genes2Genes. Code and data used to generate
figures and perform analyses in the manuscript are available at:
https://github.com/Teichlab/G2G_notebooks and
https://drive.google.com/drive/folders/15LKmo3yRB-
cR8Aq3aE59Taq2r0KtJSdX?usp=sharing. Raw sequencing data for newly generated
sequencing libraries have been deposited in ArrayExpress (accession number E-MTAB-
12720).

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Author contributions

D.S., C.S. and S.A.T. conceived the initial project. D.S. and C.S. set up and directed the study. D.S., C.S., E.D. and K.P. performed bioinformatic analyses. D.S. designed and developed the software. C.S. A.S.S. and J.P. performed cell culture experiments. D.M., E.D., B.D. and S.A.T. provided intellectual input. S.A.T. acquired funding. D.S. and C.S. wrote the manuscript. All authors read and/or edited the manuscript.

Competing interests

In the past three years, S.A.T. has received remuneration for Scientific Advisory Board Membership from Sanofi, GlaxoSmithKline, Foresite Labs and Qiagen. S.A.T. is a co-founder and holds equity in Transition Bio.

1554 **Extended Data Figures**

a

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Extended Data Fig. 1 | The dynamic programming algorithm in G2G relies on a five-
state machine and a Bayesian information-theoretic match cost function. a, This is a
(five-state) finite state machine which can generate a string over the alphabet, $\Omega = [m, w_d, w_i,$
$d, i]$ that describes all the 5 possible states of alignment (**Fig. 1b**) between two time points.
Each arrow represents a state transition. Arrows with the same color tag implies equal
probability of state transition. **b,** Behavior of the minimum message length (MML) inference
based match cost function used by G2G. It plots the MML distance (i.e. match cost) between
the standard Gaussian distribution $N(0,1)$ and $N(\mu, 1)$ Gaussian distribution for $\mu \in [0,9]$ at
50 equispaced points. 5000 data points have been randomly sampled from each $N(\mu, 1)$
distribution to represent itself. More illustrative examples are shown in **Supplementary Fig.**
1b,c.

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Extended Data Fig. 2 | Simulating the bifurcation of reference and query trajectories

using change point kernels. a, Change point kernel heatmaps for each approximate

bifurcation point (change point) $\in [0.25, 0.5, 0.75]$. **b,** The same change point kernels

binarized based on the 0.01 covariance threshold (top), **c,** The average covariance plotted for

each $i \times i$ sub square matrix from $i = 0$ to $i =$ change point, showing that the branching

effect can approximately start before the specified change point. **d,** Expected bifurcation

region is taken from the point where we begin to see > 0.01 covariance in the change point

kernel, until the particular change point.

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Extended Data Fig. 3 | Simulation Experiment 2: simulating perturbations across 769
genes in the scRNA-seq dataset of E15.5 murine pancreatic development[26]**. a,** Overall
smoothened (interpolated) and z-normalized mean gene expression along the pseudotime
(equally divided into 50 bins) for all genes in the dataset. **b,** Example illustrations of the two
types of trajectory alignment that gives the minimum expected mismatch length and the
maximum expected mismatch under the perturbation scenario 2 **(Fig. 3f,g),** where a start
portion of a particular size in the query trajectory (in blue) is changed with respect to the
reference trajectory (in green).

Extended Data Fig. 4 | Simulation Experiment 1: G2G alignments for different classes
of pattern give expected results. a, Example simulated divergent pairs of reference (green)
and query (blue) trajectories for approximate bifurcation point ∈ [0.25,0.5,0.75] (left) and

their alignment cost landscapes with the optimal alignment path highlighted by the black

dashed line (right). **b,** Example simulated convergent pairs for approximate bifurcation point

$\in [0.25, 0.5, 0.75]$ (left) and their alignment cost landscapes with the optimal alignment path

highlighted by the black dashed line. (right). **c,** Example simulated matching pair (left) and its

alignment cost landscape with the optimal alignment path highlighted by the black dashed

line. **d,** Mean percentage of alignment similarity observed in the 7 classes of alignment

pattern. **e,** On the pairwise total time-point match count matrix between reference and query

trajectories, the main average alignment path across all the 1500 alignments (left), and the

individual, cluster-specific average alignment paths for the 7 representative clusters that

accurately capture the 7 classes of pattern (right). Note: the color codes for the paths follow

the same in d. **f,** The five-state alignment strings of the 7 cluster-specific average alignments

with their alignment similarity percentages.

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Extended Data Fig. 5 | The PAM vs. LPS 'peaked inflammatory module' alignment
clustering outputs. a, The clustermap of the pairwise Hamming distance matrix of all 89
gene alignments. **b,** Density plot of the alignment similarity distribution (i.e. distribution of
the percentage of matches/warps across all the alignment outputs). **c,** Seven gene alignment
clusters were identified from hierarchical agglomerative clustering at a 0.3 distant threshold.
Each plot titled by "Cluster-x | n" is the pairwise matrix of reference and query time points,
visualizing alignment paths for all the genes (one alignment per gene and a total of n genes in
the cluster) in cluster x. *C5AR1* (Cluster-3) and *RCAN1* (Cluster-5) stand out as single-gene
clusters.

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Extended Data Fig. 6 | The PAM vs. LPS 'core antiviral module' alignment clustering
outputs. a, The clustermap of the pairwise Hamming distance matrix of all 99 gene
alignments. **b,** Density plot of the alignment similarity distribution (i.e. distribution of the
percentage of matches/warps across all the alignment outputs). **c,** Four gene alignment
clusters were identified from hierarchical agglomerative clustering at a 0.25 distant threshold.
Each plot titled by "Cluster-x | n" is the pairwise matrix of reference and query time points,
visualizing alignment paths for all the genes (one alignment per gene and a total of n genes in
the cluster) in a cluster x. *CXCL10* (Cluster-2) and *IFITM3* (Cluster-3) stand out as single-
gene clusters.

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Extended Data Fig. 7 | Analysis of artificial thymic organoid scRNA-seq data. a, UMAP
visualization of different cell types in the ATO (refined annotation). iPSC: induced
pluripotent stem cell, HSC_MPP: hematopoietic stem cell, and multipotent progenitor,
LMPP_MLP: lymphoid-primed multipotent progenitor and multi lymphoid progenitor, DC:
dendritic cell, CMP: common myeloid progenitor, GMP: granulocyte and monocyte
progenitor, MK: megakaryocyte, MEP: megakaryocyte erythroid progenitor, YS_ERY: yolk
sac-like erythrocyte, EARLY_ERY: early erythrocyte, MID_ERY: mid-stage erythrocyte,

DN(EARLY) T: early double negative T cell, DN T: double negative T cell, DP(P) T:

proliferating double positive T cell, DP(Q) T: quiescent double positive T cell, SP T: single

positive T cell, NK: natural killer cell, ILC: innate lymphoid cell. **b,** Predicted annotations

from logistic regression model with CellTypist using the developing human immune atlas[30]

as the training dataset, overlaid on the same UMAP plot as in **a**.

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Extended Data Fig. 8 | Annotation of artificial thymic organoid scRNA-seq data. For
each subset lineage embedding generated through scVI, we show UMAP embeddings of cells
colored by annotated cell populations and dot plots of mean expression (log-normalized
counts, dot color) and fraction of expressing cells (dot size) of marker genes (columns) used
for cell population annotation (rows). **a,** Annotation of non-hematopoietic cells. **b,**
Annotation of T/ILC/NK lineage cells. **c,** Annotation of other hematopoietic cells that are not
in **b**.

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Extended Data Fig. 9 | Pan fetal reference vs artificial thymic organoid alignment
clustering outputs. a, The clustermap of the pairwise Hamming distance matrix of all 1371
transcription factor alignments. **b,** Density plot of the alignment similarity distribution (i.e.
distribution of the percentage of matches/warps across all the alignment outputs). **c,** Fifteen
gene alignment clusters were identified from hierarchical agglomerative clustering at a 0.3
distant threshold. Each plot titled by "Cluster-x | n" is the pairwise matrix of reference and
query time points, visualizing alignment paths for all the genes (one alignment per gene and a
total of n genes in the cluster) in a cluster x.

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Extended Data Fig. 10 | ***BATF2*** **expression in** ***in vitro*** **ATO and** ***in vivo*** **pan fetal**

reference. a, Left panel: the interpolated log1p normalized expression (*y*-axis) against

pseudotime (*x*-axis) for *BATF2*. Right two panels: the actual log1p normalized expression (*y*-

axis) against pseudotime (*x*-axis). Each point represents a cell. **b,** The same UMAP

visualization as in **Fig. 5e**, subsetted to *in vitro* cells from ATO, colored by the *BATF2* gene

expression value (left) or the cell types (right).

Type1 Innate T Reference vs. ATO for DN onwards

CD8 Reference vs. ATO for DN onwards

Extended Data Fig. 11 | Analysis of the pan fetal reference vs artificial thymic organoid (ATO) alignment from DN T cells onwards. a, Aggregate alignment between Type 1 Innate T cell reference and ATO across 1220 human transcription factors. **b,** Gene set overrepresentation results of the most mismatched genes from alignment in **a**. **c,** Twelve gene alignment clusters were identified for **a** from hierarchical agglomerative clustering at a 0.3 distant threshold. Each plot titled by "Cluster-x | n" is the pairwise matrix of reference and query time points, visualizing alignment paths for all the genes (one alignment per gene and a total of n genes in the cluster) in a cluster x. **d,** The clustermap of the pairwise Hamming

distance matrix of all TF alignments in **a**. **e,** Aggregate alignment between CD8+ Reference
and ATO across 1219 human transcription factors. **f,** Gene set overrepresentation results of
the most mismatched genes from alignment in **e**. **g,** Fourteen gene alignment clusters were
identified for **e** from hierarchical agglomerative clustering at a 0.3 distant threshold. Each
plot titled by "Cluster-x | n" is the pairwise matrix of reference and query time points,
visualizing alignment paths for all the genes (one alignment per gene and a total of n genes in
the cluster) in a cluster x. **h,** The clustermap of the pairwise Hamming distance matrix of all
TF alignments in **e**.

 Supplementary Figures

Supplementary Fig. 1 | Minimum message length (MML) inference based distance
function to compute the cost $Cost_{match}(i,j)$ of matching a reference time point j and
query time point i. a, The top right plot gives the interpolated log-normalized expression (y-
axis) of a particular gene X in the observed single-cell data of a reference R and query Q,
against their pseudotime estimates (x-axis). The bold lines represent mean expression trends.
The faded data points represent the interpolated data (i.e. 50 random samples from the
estimated Gaussian distribution at each time point). As detailed in the Methods of the main
text, the scoring scheme of the G2G DP algorithm computes the cost of matching every pair
of time points between R and Q based on their corresponding interpolated expression
distributions. Here we consider an example reference time point j and query time point i, and
their respective single-cell expression datasets, $R(j)$ and $Q(i)$, as circled in the plot. Their
interpolated expression distributions are $N(\mu_{R(j)}, \sigma_{R(j)})$ and $N(\mu_{Q(i)}, \sigma_{Q(i)})$, denoted by $N_{R(j)}$
and $N_{Q(i)}$, respectively. Their interpolated expression data vectors are $D_{R(j)}$ and $D_{Q(i)}$. The
top left is the schematic illustration of our MML framework, extending the overview
schematic **Fig. 2** (top left) in the main text. Under the MML framework, we define two
hypotheses: Hypothesis **A:** the (i,j) time points match, and Hypothesis Φ: the (i,j) time
points mismatch. Next we compute: (1) the total (per datum) message length of encoding **A**
and D jointly, and (2) the total (per-datum) message length of encoding Φ and D jointly.
Then we define $Cost_{match}(i,j)$ to be the difference between those two message lengths,
measured in nits (a unit of information). **b,** Example cases of distributional differences
(caused by the difference in means, the difference in variance, the difference in both mean
and variance) between $R(j)$ and $Q(i)$, and their $Cost_{match}(i,j)$ values measured in nits.
When the mean and variance is the same, $Cost_{match}(i,j) \sim 0$. **c,** Behavior of $Cost_{match}(i,j)$
as the difference between the distributions increases. Left plot: $Cost_{match}(i,j)$ between the
standard Gaussian distribution $N(0,1)$ and $N(\mu,1)$ Gaussian distribution for $\mu \in [0,9]$ at 50
equispaced points. 5000 data points have been randomly sampled from each $N(\mu,1)$
distribution to represent itself. Right plot: $Cost_{match}(i,j)$ between the standard Gaussian
distribution $N(0,1)$ and $N(0,\sigma)$ Gaussian distribution for $\sigma \in [0.1,3]$ at 50 equispaced
points. 5000 data points have been randomly sampled from each $N(0,\sigma)$ distribution to
represent itself.

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Supplementary Fig. 2 | Benchmarking G2G against the DTW based approach:

CellAlign[5] and its most recent extension, TrAGEDy[11], over a simulated negative control

dataset from literature[11]. a, Density plot of the G2G alignment similarity distribution (i.e.

distribution of the percentage of matches/warps across all the G2G gene-level alignment

outputs inferred for the 619 genes in the negative control dataset). **b,** The single alignments

produced by CellAlign, TrAGEDy and G2G for all the 619 simulated genes. CellAlign and

TrAGEDy generate a high dimensional alignment, whereas G2G generates an average

alignment across all the gene-specific alignments. The alignment paths are drawn (in black)

on the pairwise time point matrix between the reference and query trajectories. The color of
the CellAlign and TrAGEDy matrices represent their cost of aligning the corresponding pair
of reference and query time points. In the G2G matrix, the color represents the number of
genes showing match or warp for the corresponding pair of time points. In CellAlign and
TrAGEDy alignment plots, the vertical and horizontal lines represent warps, whereas
diagonal lines represent one-to-one matches. In the G2G alignment plots here, the full
vertical line joined by the full horizontal line denotes an alignment path with all insertions
followed by all deletions. **c,** CellAlign, TrAGEDy, and G2G outputs for three simulated
genes (with IDs: *HK118*, *HK110*, *HK45*) that have completely mismatched trajectories. Each
row gives the gene-specific alignment paths (highlighted in black) on the pairwise time point
matrices produced by each method for the corresponding gene. The matrix color represents
each methods' cost of aligning the corresponding pair of reference and query time points. For
G2G, this is the $\log_{10}$ normalized nits compression (i.e. the difference between the match cost
and the mismatch cost as described in the Methods and **Supplementary Fig. 1**). The right-
most column ("Gene trajectories") shows the reference and query trajectories of the
corresponding gene in each row. For each gene row, the top panel shows the interpolated
log1p normalized expression (*y*-axis) against pseudotime (*x*-axis). The bold lines represent
mean expression trends, while the faded data points are 50 random samples from the
estimated expression distribution at each time point. The bottom panels show the actual log1p
normalized expression (*y*-axis) against pseudotime (*x*-axis) for reference (right) and query
(left). Each point represents a cell.

 Supplementary Tables

Framework component	CellAlign[5]	TrAGEDy[11]	Genes2Genes
Input	(1) Log-normalized single-cell gene expression data (2) Pseudotime estimates of the cells inferred using any available method of choice		
Algorithm	Uses Dynamic Time Warping (DTW) algorithm.	Builds on top of CellAlign, and performs post-hoc changes to the DTW alignment to capture mismatches.	Combines DTW and Gotoh's biological sequence alignment[15] through a new dynamic programming algorithm.
Alignment states	Handles matches and warps only, subjected to a weight scheme with constant weight for warp open/extension	Identifies optimal start and end time points of the trajectories for DTW alignment to exclude regions of mismatch at the beginning and end. It further filters the DTW aligned regions based on alignment cost thresholding to identify mismatches.	Handles matches, warps and mismatches jointly, subjected to a five-state machine with state transition probabilities, handling gap/warp open/extension.
Trajectory Interpolation	Interpolates data using a Gaussian kernel-based weighted mean expression.	Extends CellAlign interpolation to use a cell density weighted window size.	Extends CellAlign interpolation to distributional interpolation using weighted variance.
Distance measure between a pair of reference and query time points	Uses min-max normalized, mean gene expression based Euclidean distance measure, to identify similar trends of expression dynamics across two conditions.	Uses Spearman correlation, which does not require gene expression scaling as done in CellAlign, but does not support gene-level alignment.	Uses a minimum message length inference based distributional distance measure, aiming to compare the gene expression distributions between two conditions.
Alignment output	Outputs only a single, high-dimensional alignment (across a given gene list). A single, gene-level alignment can be obtained by giving a single gene input.	Modified, high-dimensional DTW alignment after pruning the matches.	Outputs gene-specific alignments with an explicit alignment state description via a five-state alignment string for all the given genes. Can output an aggregate alignment for any given set of genes.
Alignment clustering	Can cluster genes only based on the pseudotime shifts in their	Does not explicitly discuss clustering.	Can cluster genes based on their five-state alignment strings,

	alignments.		covering both matches and mismatches.
Differential expression capture	Requires additional downstream tasks to extract differential genes and regions (e.g. local DTW alignment with user-defined similarity threshold).	Sliding window soft clustering approach to extract DE using t-test/Mann-Whitney U test.	A gene-specific alignment output itself is a direct description of the differential expression status along the time axis. Provides a ranked list of genes based on their alignment similarity percentage.

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Supplementary Table 1 | List of features included in trajectory alignment frameworks.
A table outlining and comparing the features of CellAlign[5], TrAGEDy[11] and G2G.

Supplementary Table 2
Gaussian Process based simulated gene alignments
GP_based_simulations_gene_alignments.csv

Supplementary Table 3
Gaussian Process based simulated gene alignment cluster statistics
GP_based_simulations_cluster_statistics.csv

Supplementary Table 4-17
Real data based simulations alignment statistics
pancreas_simulations_<perturbation_type>_size<perturbation_size>gene_alignments.csv

Supplementary Table 18
PAM vs. LPS 'core antiviral module' alignments
PAM_LPS_global_gene_alignments.csv

Supplementary Table 19-22
Overrepresentation analysis results of PAM vs. LPS 'core antiviral module' alignment clusters
PAM_LPS_global_cluster_<CLUSTER_ID>_pathways.csv

Supplementary Table 23
PAM vs. LPS 'peaked inflammatory module' alignments
PAM_LPS_local_gene_alignments.csv

Supplementary Table 24-30
Overrepresentation analysis results of PAM vs. LPS 'peaked inflammatory module' alignment clusters
PAM_LPS_locall_cluster_<CLUSTER_ID>_pathways.csv

Supplementary Table 31
T1 vs. ATO all alignments
SPT_all_gene_alignments.csv

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1784 **Supplementary Table 32**

1785 Overrepresentation analysis results of T1 vs. ATO top 165 genes (under <40% alignment similarity

1786 threshold)

1787 *SPT_all_overrep_results_top_k_DE_threshold_0.4sim_165genes.csv*

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1789 **Supplementary Table 33-45**

1790 Overrepresentation analysis results of T1 vs. ATO alignment clusters

1791 *SPT_all_cluster_<CLUSTER_ID>_pathways.csv*

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1793 **Supplementary Table 46**

1794 T1 vs. ATO DN onwards all alignments

1795 *SPT_DN_gene_alignments.csv*

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1797 **Supplementary Table 47**

1798 Overrepresentation analysis results of T1 vs. ATO DN onwards top 130 genes (under <40% alignment

1799 similarity threshold)

1800 *SPT_dn_overrep_results_top_k_DE_threshold_0.4sim_130genes.csv*

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1802 **Supplementary Table 48**

1803 CD8+T vs. ATO DN onwards all alignments

1804 *CD8_DN_gene_alignments.csv*

1805

1806 **Supplementary Table 49**

1807 Overrepresentation analysis results of CD8+T vs. ATO DN onwards top 120 genes (under <40%

1808 alignment similarity threshold)

1809 *CD8_dn_overrep_results_top_k_DE_threshold_0.4sim_120genes.csv*

1810

1811 **Supplementary Table 50**

1812 ATO metadata

1813 *ATO_WT_manifest.csv*

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1815 **Supplementary Table 51**

1816 ATO CITE-seq metadata

1817 *ATO_hashtagging.csv*

1818

1819 **Supplementary Table 52**

1820 Negative control alignments

1821 *negative_control_gene_alignments.csv*