Evolution of the Telencephalon Anterior-Posterior Patterning by Core Endogenous Network Bifurcation

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Abstract

How did the complex structure of telencephalon evolve? Existing explanations are based on

phenomena and lack the first principle. The Darwinian dynamics and the endogenous network

theory established a few years ago provide a mathematical and theoretical framework of a

dynamical structure, and a general constitutive structure for theory-experiment coupling,

respectively, for answering this question from the first principle perspective. By revisiting a

gene network that explains the anterior-posterior patterning of the vertebrate telencephalon,

we found that with the increase of the cooperative effect in this network, the fixed points

gradually evolve, accompanied by the occurrence of two bifurcations. The dynamic behavior

of this network consists with the knowledge obtained from experiments on telencephalon

evolution. Furtherly, our work drew an answer quantitatively of how the telencephalon

anterior-posterior patterning evolved from the pre-vertebrate chordate to the vertebrate and

gave a series of verifiable predictions in a first principle manner.

Keywords: telencephalon, evolution, gene regulatory network, endogenous network theory,
nonlinear process

31
32 **Figure Abstract**
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Introduction

As the material basis of cognitive abilities, the telencephalon results from hundreds of millions of years of evolution(Holland 2015; Briscoe and Ragsdale 2019; Chakraborty and Jarvis 2015). A series of events were discovered, like genome duplication and new genes emergence(Kaessmann 2010; Putnam et al. 2008), core gene network interconnectivity increasing(Gil-Gálvez et al. 2022), and neuropathway duplication(Chakraborty and Jarvis 2015), providing phenomenological explanations for how the complex structure of the telencephalon has evolved to this day. But like research on the celestial motion before the introduction of Newtonian mechanics, these phenomena-based explanations lack the fundamental core: the first principle.

Recently, some researchers also worried that researches in life science pay more attention on the experiment itself than the theory-experiment coupling(MacArthur 2023; Smaldino 2019; Nurse 2021); or even had a circling back sensation, at least in cancer research, after half a century of the journey(Weinberg 2014). Indeed, the phenomena of life are full of complexity, and the complexity science itself is still a newborn one. The discovery of a first principle in life is bound to be difficult. Nonetheless, there were fruits born in this "circle". Decades after the introduction of Boolean dynamics into the gene network(Kauffman 1969; Toulouse et al. 2005), the analysis of the dynamical structure of the hydrogen model in life science: the phage-λ gene switch(Zhu et al. 2004), provided an example of application of a general law alone with the mathematical framework for the evolution dynamics(Ping Ao 2005; Kwon, Ao, and Thouless 2005). Following this footpath, a theory provides the general constitutive structures of evolution dynamics on the gene network level, the endogenous network theory(Ping Ao et al. 2008) was established years after the postulation of the system biology(Hood 2003), unifies the gene network dynamics and the landscape concept raised by Wright and Waddington, allowing the qualitative and quantitative comparisons between theories and experiments(Ping Ao 2021; Prokop 2022). Under these theoretical sets, a series of efforts were made to address questions on cancer and development(Yuan et al. 2017). Now we may have enough mathematical and theoretical framework as well as the knowledge

obtained from experiments to address the question of how our brain evolved at the gene

network dynamics level in a first principle way.

In this work, the attempt was made by revisiting a pre-constructed model(Giacomantonio and

Goodhill 2010; 2014; Goodhill 2018) of telencephalon anterior-posterior patterning in

vertebrates containing 5 nodes and 10 edges, demonstrated that the dynamic behavior of such

a relatively small network is necessary to draw an answer under the mathematical and

theoretical framework mentioned above.

Results

A coarse-grained core endogenous network for telencephalon already exists

A Boolean 5-node network has been constructed, which sufficiently reproduced the

experimentally observed gradients of anterior-posterior patterning of early cortical

development in mammals(Giacomantonio and Goodhill 2010; Goodhill 2018). From the

perspective of data fitting, the existing experimental data were not sufficient to uniquely

specify interactions of a base network. And if such a base network exists, how the latent

factors regulate the base network is not clear(Giacomantonio and Goodhill 2010; 2014;

Goodhill 2018).

But in the other way, Giacomantonio and Goodhill have constructed a network with robust

dynamic behavior, which is exactly one of the most important features of the "backbone", or

say, the "core" structure of an endogenous network shaped by evolution that we argued in

2008, one of the others is being conserved among species during evolution(Ping Ao et al.

2008; Yuan et al. 2017). We found ortholog exists in amphioxus, one of the closest living

vertebrate relatives that diverged from the vertebrate lineage around 550 million years ago, of

all 5 genes(Putnam et al. 2008; Marlétaz et al. 2018; Takatori et al. 2008) in this network.

Nevertheless, Benito-Gutiérrez *et al.* discovered the resemblance of the expression pattern

between mature amphioxus cerebral vesicle and the developing vertebrate

telencephalon(Benito-Gutiérrez et al. 2021). These facts indicate that the network

Giacomantonio and Goodhill constructed is conserved in the pre-vertebrate chordate and the

vertebrate during evolution.

To further confirm the robustness of the model, we generated 128 Boolean function variations

based on the network (Figure 1. A) described by Goodhill in 2018(Goodhill 2018) by using

the combination of replacing "AND" with "OR". With the default operators, 2 point attractors

which correspond to the expression pattern of the posterior (boole_p1) or anterior (boole_p2)

telencephalon separately and 2 linear attractors (boole_li3 and boole_li14) were generated by

exhausting all initial vectors (Figure 1. B). For all Boolean variations, we obtained 26

attractors with 4 point ones and 22 linear ones (Figure 1. B). Among them, two attractors, the

posterior-like attractor boole_p1 and the anterior-like attractor boole_p2, were obtained in all

Boolean variations (Figure 1. C, E). The size of the attraction basins with each attractor in all

variations, in which the boole_p1 and the boole_p2 was equivalently the most common

attractor among all (Figure 1. D, E). These results further confirmed the robustness of the

Boolean dynamic behavior of this network.

Bifurcations observed with evolving Hill coefficient

Complex dynamic behavior, like transition states and bifurcation, cannot be obtained in

Boolean dynamics(Toulouse et al. 2005; P. Ao et al. 2010; Yuan et al. 2017). Thus, we turn

our attention to the ordinary differential equation (ODE) model. In this work, we used a

double-normalized Hill equation which has been described in detail previously(Toulouse et al.

2005; Yuan et al. 2017). The details of the direct interactions among genes in the current

network are still unclear, let alone their dynamic parameters. In order to extract insights from

such limited details, a set of dimensionless mesoscopic parameters, h and k, were used in this

work.

We chose h=3, k=10 as the first trial of the parameter set (the vanilla set) based on our

previous modelling experience(Yuan et al. 2017). Under this set, we obtained three fixed

points, with two stable ones (stable state) and an unstable one (transition state) (Figure 2. A,

B). The expression patterns of two stable states (Figure 2. A, B; vanilla_sta1, vanilla_sta2)

consist with the point attractors in Boolean Dynamics (Figure 2. A, B; Boole_p1, Boole_p2),

and the transition state also consists with the average of all the linear attractors in the Boolean

dynamics with the unaltered functions (Figure 2. A, B; Boole_li_allme: the average of

Boole_li_7 and Boole_li_18 in Figure 1. B).

In a nonlinear system, bifurcations may occur as parameters change. Oster and Alberch

argued that mathematical bifurcations could be an important mechanism behind development

and evolution 40 years ago(Oster and Alberch 1982; François 2012). We then tried to explore

the parameter space in order to find bifurcations.

133 Fitting an elephant with a wiggling trunk is not our purpose, therefore the number of arbitrary

134 parameters needs to be reduced at first. The number of the arbitrary parameters in this model

135 equals 20 (2n, n = edge number). Given that the details of these dynamical parameters are not

136 clear, and genes in the core network level should be considered equally important, as we

137 argued before(Ping Ao et al. 2008; Yuan et al. 2017), thus we took the same parameters for all

138 edges, therefore reducing the arbitrary parameters number from 20 to 2. Considering the

139 concentration/function of genes already normalized into [0, 1], in order to center the S shape

140 part of the sigmoid function, we let $k = 2^h$, therefore reducing the number of arbitrary

141 parameters to 1.

143 Increasing h (h=10, 25; $k=2^h$) results in two stable states and one transition state, which is

144 similar with the dynamic behavior under the vanilla parameter set (Figure 2. A, B). Since the

145 Hill equation is equivalent to its Boolean from h takes the limit, we expected the dynamic

146 behavior will not change significantly with further increased h.

147 Then we explored the parameter space with smaller h, and discovered two bifurcations

148 (2<h<2.01; 2.325<h<2.35; $k=2^h$). When h<2, there is only one stable state, which has a

149 pattern similar with the transition state with the vanilla parameter set. The pattern gradually

150 evolves from the vanilla transition state-like pattern to a vanilla stable state 2-like pattern with

151 increasing h. Passing over the first bifurcation (2<h<2.01), a transition state emerges, which

152 then evolves to a vanilla stable state 1-like pattern (2.01<h<2.325). The second bifurcation

153 (2.325<h<2.35) gives birth to the second stable state (Figure 2. C).

155 **Evolution of the telencephalon anterior-posterior patterning by bifurcations of**
156 **the network dynamic behavior**

158 Surprisingly, the dynamic behavior of this network is highly consistent with the facts we

159 know about the evolution of telencephalon.

160 A telencephalon-like structure has been identified recently in amphioxus with a low level of

161 Pax4/6 and a high level of EmxA and EmxB(Benito-Gutiérrez et al. 2021). Only one stable

162 state exists when weak or negative cooperativity among this network (0<h<2.01) with a low

163 level of Pax6 and intermediate-high level of Emx2, which consists with the expression pattern

of the telencephalon-like structure identified in amphioxus. The expression pattern of this

solitary stable state gradually evolves to a posterior telencephalon-like pattern with the

increasing h.

With a further increased h ($2.01 \leq h \leq 2.325$), the first bifurcation occurs, giving birth to a stable

state and a transition state. The expression pattern of the stable state consists with the

posterior part of the telencephalon, and the expression pattern of the popping-out transition

state is similar with the anterior part of the telencephalon. We don't know which organism

would eventually end in development at this stage. Still, in the development of the vertebrate

embryonic central nervous system, the telencephalon first appears near the anterior end of

prosencephalon(Briscoe and Ragsdale 2019).

This model results in two stable states consisting with telencephalon anterior-posterior

patterning in vertebrates after the second bifurcation ($h \geq 2.35$); and one transition state which

shares the similarity in expression pattern with the telencephalon-like structure in amphioxus

as well as the sable state when weak or negative cooperativity among this network, reminds

us of the biogenetic law(Levit et al. 2022).

We did not observe any significant variation in the dynamic behavior of this network after the

second bifurcation ($h \geq 2.35$). On the biological side, no matter how complex the brain evolves,

the binary patterning of pallium/subpallium or olfactory bulb/olfactory cortex can always be

observed in the vertebrate telencephalon(Briscoe and Ragsdale 2019).

Predictions
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Based on the results above, we can make the following predictions:

1. The topological structure of the core endogenous network that determines the
telencephalon anterior-posterior patterning has already evolved in the ancestral chordate
550 million years ago;

2. The expression pattern of the telencephalon-like structure in such ancestral chordate 550
million years ago and in the Amphioxus today consists with the stable states we obtained
before the first bifurcation ($0 < h \leq 2$）；

3. An ancestral organism with primitive telencephalon structure would undergo an
expression pattern consistent with the anterior part of the vertebrate telencephalon and the
transition state we obtained under the parameter range of $2.01 \leq h \leq 2.325$ during
development, then would mature in the expression pattern consistent with the posterior
part of the vertebrate telencephalon and the stable state we obtained under this parameter
range of $2.01 \leq h \leq 2.325$.

4. Experiments that reduce the cooperative effect in the network described above in
vertebrates, series of events: the vanishing of the anterior-posterior patterning of the
telencephalon; a structure with the expression pattern consists with the posterior part of
the telencephalon; a structure with the expression pattern consists with the Amphioxus
telencephalon-like structure would be observed.
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Conclusion

The current results display such a picture:

The ancestral chordate 550 million years ago evolved a 5-node core endogenous network described in this work with weak or even negative cooperative effect, which determines a telencephalon-like structure with a similar expression pattern with the developing telencephalon during early embryonic stage in the vertebrate, but without the anterior-posterior patterning;

Between 550 million to 500 million years ago, new genes emerged from the genome duplication and mutations. As a result, the cooperative effect in the 5-node core endogenous network increased so that a primitive telencephalon structure gradually evolved to the expression pattern of the posterior part of the vertebrate telencephalon, and during development, it would undergo an expression pattern similar to the anterior part of the vertebrate telencephalon;

With the further increase of the cooperative effect during evolution, a telencephalon with the anterior-posterior patterning emerged, which like the biogenetic law concluded, would undergo a development stage with an expression pattern similar to that of the ancestral telencephalon-like structure.

In a way, we have drawn an answer to how did the telencephalon anterior-posterior patterning evolve quantitively in a first principle manner.

Discussion

For the evolution of the telencephalon anterior-posterior patterning, we found that such a 5-node network alone is sufficient to draw an answer, but it is not enough for the evolution of the whole central nervous system, let alone the entire vertebrate body plan. The network described in this work can be taken as a subnetwork(Wang et al. 2018), which has the potential to expand into the global decision-making network for the evolution and development of the central nervous system or even the entire vertebrate body plan shaped by evolution.

Preliminary evidence suggest the hypothesis that the network described in this work is conserved during evolution from pre-vertebrate chordate to vertebrate is acceptable, the results obtained by Giacomantonio and Goodhill(Giacomantonio and Goodhill 2010; 2014) and the results described in this work combined further validated this hypothesis at the computational level. Nonetheless, the efforts on the experiments' side to validate the hypothesis are still indispensable.

As the knowledge of the real dynamics parameters is little, if not none, we used a set of dimensionless mesoscopic parameters and made the parameter sets equal at the core network level based on a set of working hypotheses postulated before(Ping Ao et al. 2008; Yuan et al. 2017). This work showed that useful predictions can still be drawn even with such little knowledge. But exploring the range of these parameters in real biological systems is still a non-negligible task.

In response to the growing emphasis on theory-experiment coupling in life science recently(MacArthur 2023; Nurse 2021; Smaldino 2019; Prokop 2022; Ping Ao 2021), our work showed that the combination of existing experimental facts as well as the aforementioned mathematical and theoretical framework, although not perfect yet, has been able to give birth to new knowledge and verifiable predictions.

Methods

Boolean dynamics

For the unaltered function set, we used "AND" to represent the interaction of activation,

"NOT" to represent the interaction of inhibition:

A=Fgf8 A (t+1) = D (t)

B=Emx2 B (t+1) = NOT A (t)

C=Pax6 C (t+1) = A (t) AND (NOT B (t)) AND (NOT E (t))

D=Sp8 D (t+1) = (NOT B (t)) AND (NOT E (t))

E=Coup-tfi E (t+1) = (NOT A (t)) AND (NOT C(t)) AND (NOT D (t))

For the Boolean variations, an agent affected by 1, 2, 3 agents will respectively result in 1, 2,

8 equations in this work. Thus, we generated 1*1*8*2*8=128 sets of functions. All variants

are presented in the supplemental table.

We iterated the function set with exhausted all initial vectors until stable, then collected and

counted attractors, attractor types, and basin of each attractor size. These data are presented in

the supplemental table in detail.

ODE

The ODE functions we used are as follows:

x(1)=Fgf8; $\frac{dx(1)}{dt} = -x(1) + \frac{k*x(5)^h}{1+k*x(5)^h}$

x(2)=Pax6; $\frac{dx(2)}{dt} = -x(2) + \frac{k*x(1)^h}{1+k*x(1)^h} * \frac{1}{1+k*(x(3)^h+x(4)^h)}$

x(3)=Emx2; $\frac{dx(3)}{dt} = -x(3) + \frac{1}{1+k*x(1)^h}$

x(4)=Coup-tfi; $\frac{dx(4)}{dt} = -x(4) + \frac{1}{1+k*(x(1)^h+x(2)^h+x(5)^h)}$

x(5)=Sp8; $\frac{dx(5)}{dt} = -x(5) + \frac{1}{1+k*(x(3)^h+x(4)^h)}$

We used Newton's iteration to obtain fixed points; determined the stability of the fixed point

by the real part of the eigenvalue of its Jacobian matrix; used Euler's method to verify the

stable fixed points parallelly.

For the vanilla parameter set (n=3, k=10), we first used 1000 random initial vectors, followed

by 100000 random initial vectors to verify the integrity of the results. The results showed that

1000 random initial vectors were sufficient to obtain complete results, so 1000 random initial

vectors were used to explore the parameter space.

The connection between transition states and stable states was obtained by perturbation on the

transition state with a small random vector; in this work, the number of such small random

vectors is 100.

Figure 1. Boolean dynamics of the core endogenous network for telencephalon
anterior-posterior patterning. A, The network we used in this work. B, Results of Boolean
dynamics, linear attractors were averaged. C, The occurrence of attractors among all Boolean
equation variations. D, Total size of each attractor in all attractors combined. E, An overview
of the attractors for all Boolean variations. The color of the circle represents the attractor type
(red: linear attractor; blue: point attractor). Aera of the circle represents the attractor size.
Each attractor of each Boolean variant shows the same transparency, thus the less
transparency represents the higher occurrence. _p: point attractor; _l: linear attractor.
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Figure 2. Bifurcations occur when exploring the parameter space. A, A Numeric way of
showing the bifurcation. All fixed points under all parameter h we have been tried were
displayed in this picture, the first column on the left is under vanilla parameter set (h=3,
k=10), the rightest column is the results of the unaltered Boolean functions (h→+∞), and
others are arranged from small to large for h. B, Heatmap of all ODE fixed points
demonstrated after hierarchical clustering. C, Bifurcations occur with the growth of h. Arrows
point to the stable states from the transition state. sta: stable state; tra: transition state
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Contribution

Design: Ao, Yao;

Execution: Sun, Yao, Xiong, Su;

Drafting: Yao, Sun, Zhu;

Figure: Yao, Sun, Xiong;

Revising: Sun, Yao, Xiong, Su, Zhu, Ao.

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	vanilla_sta1		h_1.5_sta1	h_2_sta1	h_2.01_sta1	h_2.325_sta1	h_2.35_sta1	h_2.5_sta1	h_2.75_sta1	h_3_sta1	h_10_sta1	h_25_sta1	Boole_p1
Fgf8	0.00		0.27	0.05	0.05	0.02	0.02	0.01	0.00	0.00	0.00	0.00	0.00
Pax6	0.00		0.08	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
Emx2	1.00		0.71	0.99	0.99	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
Coup-tfi	1.00		0.54	0.94	0.94	0.98	0.98	0.99	1.00	1.00	1.00	1.00	1.00
Sp8	0.05		0.26	0.12	0.12	0.09	0.09	0.08	0.07	0.06	0.00	0.00	0.00

	vanilla_tra1	h_0.1_sta1	h_0.5_sta1	h_1_sta1	h_1.1_sta1		h_2.35_tra1	h_2.5_tra1	h_2.75_tra1	h_3_tra1	h_10_tra1	h_25_tra1	Boole_li_allme
Fgf8	0.50	0.49	0.46	0.42	0.41		0.64	0.58	0.55	0.53	0.50	0.50	0.50
Pax6	0.25	0.17	0.18	0.16	0.16		0.41	0.34	0.30	0.29	0.25	0.25	0.17
Emx2	0.45	0.50	0.51	0.54	0.56		0.36	0.41	0.44	0.45	0.50	0.50	0.50
Coup-tfi	0.30	0.26	0.29	0.35	0.36		0.19	0.24	0.27	0.28	0.33	0.33	0.17
Sp8	0.46	0.34	0.36	0.36	0.35		0.64	0.57	0.54	0.52	0.50	0.50	0.50

	vanilla_sta2		h_2.01_tra1	h_2.325_tra1	h_2.35_sta2	h_2.5_sta2	h_2.75_sta2	h_3_sta2	h_10_sta2	h_25_sta2	Boole_p2
Fgf8	0.90		0.62	0.67	0.70	0.79	0.85	0.88	1.00	1.00	1.00
Pax6	0.87		0.33	0.45	0.50	0.64	0.75	0.82	1.00	1.00	1.00
Emx2	0.12		0.36	0.34	0.31	0.24	0.19	0.16	0.00	0.00	0.00
Coup-tfi	0.04		0.18	0.17	0.15	0.10	0.07	0.06	0.00	0.00	0.00
Sp8	0.98		0.57	0.67	0.72	0.84	0.93	0.97	1.00	1.00	1.00

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