When cheating turns into a stabilizing mechanism of mutualistic networks

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Codes are available here: https://github.com/f-duchenne/Cheating_in_mutualistic_networks

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FD designed the study and performed all analyses. EBa, MAM, TS, EG and CG designed the data collection and collected the data. FD, Eba,SA, TS and EBr curated the data. FD wrote the first draft and all authors contributed to final writing and editing.

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Abstract

Mutualistic interactions, such as plant-mycorrhizal or plant-pollinator interactions, are widespread in ecological communities and frequently exploited by cheaters, species that profit from interactions without providing benefits in return. Cheating usually negatively affects the fitness of the individuals that are cheated on, but the effects of cheating at the community level remains poorly understood. Here we describe two different kinds of cheating in mutualistic networks and use a generalized Lotka-Volterra model to show that they have very different consequences for the persistence of the community. Conservative cheating, where a species cheats on its mutualistic partners to escape the cost of mutualistic interactions, negatively affects community persistence. In contrast, innovative cheating occurs with species with whom legitimate interactions are not possible, because of a physiological or morphological barrier. Innovative cheating can enhance community persistence under some conditions: when cheaters have few mutualistic partners, cheat at low or intermediate frequency and the cost associated with mutualism is not too high. In this case, the negative effects of cheating on partner persistence are over-compensated at the community level by the positive feedback loops that arise in mutualistic networks. Using an empirical dataset of plant-bird interactions, we found that observed cheating patterns are highly consistent with theoretical cheating patterns found to increase community persistence. This result suggests that the cheating patterns observed in nature could contribute to promote species coexistence in mutualistic communities, instead of necessarily destabilizing them.

Main text

Introduction

Mutualism, an interaction that benefits all species involved, is widespread in the web of life (1,2). In natural systems involving mutualism, it is common to find cheaters, species reaping benefits from interactions without providing benefits to their partners (3,4). Cheating has been descried in mycorrhizal (5), plant-pollinator (6), cleaner fish-client (3) and seed-dispersal (7) interactions. Evolutionary theory has shown that a stable coexistence of mutualists and cheaters is possible (8–10), explaining their persistence in nature. Using pollination as a study model, it has been shown that illegitimate interactions between pollinators and plants (cheating, *i.e.* nectar robbing) affect the structure of the interaction networks (6,11), but the consequences of cheating for the ecological stability of these communities have been largely overlooked, but see (12).

From an evolutionary perspective, widely based on game theory, cheating is only viewed as a way to escape the cost associated with mutualism (8,13–15), for example, energy expenditure due to nectar production in plants or foraging in animals. In this case, while the species could interact legitimately (*i.e.* mutualistically), they cheat because the cost of cheating is lower than the cost of legitimate interactions. However, species can also cheat to profit from partners that are otherwise unavailable, when a legitimate interaction is not possible because of a physiological or morphological barrier (16,17). In the first case, cheating is directly detrimental for the mutualism because it replaces mutualistic interactions with antagonistic or commensalistic ones (Fig. 1a). We term this type of cheating, where the interaction niche of the species remains constant (Fig. 1b), conservative cheating. In the second case, cheaters use a partner that is otherwise unavailable, thus resulting in new interactions that would not exist in a purely mutualistic framework (Fig. 1a). We term this second type of cheating, where the interaction niche of the cheater expands (Fig. 1b), innovative cheating.

The consequences of cheating for the number of species being able to coexist (*i.e.* network or community persistence) are expected to be mediated by two main factors. First, increasing cheating frequency reduces mutualistic benefits, thus decreasing the persistence of the cheated species, which in turn decreases the overall network persistence. Second, intermediate cheating frequencies can help species to persist, which can feedback into more mutualistic partners for the other guild, thus increasing network persistence. The balance between these two opposite effects on network persistence is likely depends on whether cheating is conservative or innovative, as the type of cheating will re-organize the structure of interactions in different ways. When conservative cheating increases, we expect a decrease in network persistence, because a portion of interactions shift from mutualistic, which tend to increase persistence (18), to antagonistic or commensalistic, while species do not obtain any additional partners. For innovative cheating, the outcome on network persistence is uncertain. When innovative cheating increases mutualistic interactions are also replaced by antagonistic or commensalistic ones, but cheaters can rely on more partners that could increase their persistence, and thus the overall network persistence. Thus, when cheating is innovative, we expect different effects according to the role of the cheaters. If cheaters are generalist species (*i.e.* have many mutualistic partners), we expect that their persistence will be only slightly enhanced by innovative cheating, as they already have many partners. In this case, innovative cheating is more likely to decrease benefits for mutualistic partners with few positive counterparts, leading to a decrease in network persistence. If cheaters are specialists (*i.e.* with few partners), we expect that innovative cheating increases the overall network persistence, because it will increase persistence of specialists species. Specialists are often the most vulnerable species to extinction (18,19), thus increasing their persistence could increase the overall network persistence through positive feedback loops arising in mutualistic networks. In this case it is important to note that an additional mechanism could play a role: as specialist cheaters expand their interaction niche (Fig. 1b), this could promote competitive exclusion of other species from the same guild, making uncertain the positive effect of innovative cheating on persistence. Since these indirect facilitation and competition effects

arise mainly in large networks (20,21), the effects of cheating would be fully assessable only if considering
a realistic diversity, but not when considering a module of few species.

Figure 1: Cheating can be conservative or innovative. (a) Above, mutualistic network built using only +/+ (legitimate)
interactions and below, mutualistic networks including one illegitimate interaction. Cheating is conservative if it
happens between partners that were already linked by a mutualistic interaction, or innovative if it happens between
partners that were not linked by a mutualistic interaction. (b) Cheating characterized in a niche concept. Symbols
represent the position of the legitimate (green) and illegitimate (yellow) partners of a given species of pollinator in their
trait space. Conservative cheating occurs within the mutualistic niche, which is the convex hull determined by trait
combination of legitimate partners. Innovative cheating occurs with plants that are outside of the mutualistic niche and
lead to an expansion of the interaction niche, defined as the convex hull determined by trait combination of legitimate
and illegitimate partners.

In empirical systems, cheating is often evidenced indirectly, for example using the presence of holes in
flowers (22,23). Such data do not allow evaluation of cheating at the interaction level, as the identity of the
cheaters is unknown. However, indirect evidence suggests that innovative cheating is common is pollination,
because pollinators often rob nectar in flowers with long corolla, in which nectar is difficult to access
(16,23,24). Thus, in addition to considering different kinds of cheating in theoretical models, we also need
to collect empirical data about the relative distribution of legitimate and illegitimate interactions in
mutualistic networks, to understand the consequences of cheating at the community level.

To test the hypotheses developed above, we used a theoretical ecological model, without evolutionary
dynamics, to assess the consequences of conservative and innovative cheating for the ecological stability of
bipartite mutualistic networks, measured as network persistence. We used a generalized Lotka-Volterra
model with two guilds with a moderate diversity, 20 plant and 20 pollinator species, embedded in an
obligatory mutualistic relationship. We incorporated three parameters to model cheating: the proportion of
pollinator species cheating ($\overline{\Delta}$), the cheating frequency of these cheaters (Ω), the proportion of innovative
cheating *vs* conservative cheating (Ψ); and a fourth parameter to model the cost associated with mutualism
(Λ), that is likely to mediate the effect of cheating. For simplicity we assumed that only pollinators cheat, so
only they were able to interact illegitimately with plants, *i.e.* piercing the flower corolla and robbing the
nectar without pollinating. In this model cheaters escape the cost associated with mutualism while robbed
plants do not benefit from these interactions and still pay the cost associated with mutualism (*i.e.* nectar
production). We also assumed no additional cost for plants due to cheating than the one associated with
mutualism, as cheaters often slightly damage flowers. To test how the degree of generalism of the cheaters
could affect community persistence we performed simulations for two scenarios: when the cheaters were the
most generalist species and when they were the most specialist species in the community (*cf.* Methods).

Using these results, we identified conditions in which cheating increases ecological persistence of
communities. In a second step, to see if these conditions are met or not in nature, we used an empirical dataset
including ~34,000 interactions between flowering plants and hummingbirds, collected in Costa-Rica and
Ecuador. Each interaction was classified as legitimate or illegitimate, allowing us to explore cheating patterns
in empirical mutualistic networks. Finally, to close the loop between theory and data, we used these empirical
data to parametrize our model and assess how observed patterns of cheating affect network persistence.

Results

Our simulations showed that the output of cheating on network persistence, measured as the percentage
of persisting species at equilibrium, could be negative or slightly positive (Fig. 2a & S1) and strongly
depended on its conservative *vs.* innovative character.

Figure 2: Innovative cheating can increase network persistence. Network persistence (percentage of persisting species
at equilibrium) as a function of cheating frequency (Ω), proportion of innovative cheating (Ψ), cost associated with
mutualism (Λ) and scenario (cheaters are generalist or specialist species) for (a) a case with 10% and (b) a case with
50% of animal species cheating. The colours represent the average effect of cheating on network persistence relative
to the corresponding case with no cheating (Ω = 0). Positive values (blue) indicate higher persistence with than without
cheating, while negative values (red) indicate the opposite, a negative effect of cheating on persistence. Results are
presented for initial values of connectance φ=0.4 and averaged over the 500 initial conditions. The black boxes
represent the space in which cheating has a positive effect on network persistence, which is represented in 3D for the
specialist scenario in (c) for Λ=0 (grey) and Λ=0.3 (dark blue). (d) represents the volume of this 3D space as a function
of the scenario and the cost associated with mutualism. Note that the full parameter space presented in (c) and (d) has

a volume of 1 and that a cost of Λ=0.15 or Λ=0.3 corresponds to 10% or 20% of benefits associated with mutualism,
respectively (Λ/α = 0.1 or 0.2).

As expected, when cheating was conservative it almost always negatively affected network persistence,
because cheating decreases benefits of plant-animal interactions for plants, thus decreasing their persistence.
In an obligatory mutualism, interacting guilds depend on each other, therefore a decrease in plant persistence
is likely to negatively affect overall network persistence. Regardless of its conservative/innovative character,
cheating had a more negative (or less positive) effect on persistence when there was a cost associated with
mutualism (Λ>0, Fig. 2a), *i.e.* when illegitimate interactions are antagonistic. Similarly, on average, cheating
had a less negative (or more positive) effect on network persistence when cheaters were specialist species
than when they were generalists (Fig. 2a). This difference is because cheating makes specialists better able
to persist and thus can buffer the negative effects of cheating on their partners through positive feedback
loops arising in mutualistic networks (Fig. S2). In contrast, cheating had few positive effects on persistence
of generalist species (Fig. S2), so when they cheat, cheating is likely to negatively affect network persistence.

The window of parameters in which cheating increases network persistence, relative to cases with no
cheating, mostly correspond to the cases when: cheaters were specialists, cheating was innovative with
intermediate frequencies and the cost associated with mutualism was low (Fig. 2 & S1). This parameter space
can be represented in 3 dimensions (Fig. 2c), using the three parameters controlling for cheating distribution,
the proportion species cheating ($\overline{\Delta}$), the cheating frequency of these cheaters (Ω) and the proportion of
innovative cheating (Ψ). The scenario of simulation, generalists *vs.* specialists, and the cost associated with
mutualism strongly affected the volume of the parameter window in which cheating had a positive effect on
persistence (Fig. 2c-d). Cheating increased network persistence by 4.7% maximum, suggesting that if
cheating could have a positive effect on persistence, it however remained a weak effect. This positive effect
on network persistence tended to disappear when cheaters were generalists and with the increasing cost
associated with mutualism (Fig. 2b) but remained even when the proportion of cheaters was high (Fig. 2d),
if the overall level of cheating, measured as $\overline{\Delta} \times \Omega$, was not too high (Fig. S3).

In extreme cases, when cheaters are specialists and when cheating frequency increased above a given
value, innovative cheating could have more negative effects on network persistence than conservative
cheating (Fig. 2a & S1). When the frequency of innovative cheating increases, specialists cheaters switch
from facilitators to competitors, because innovative cheating expands the interaction niche of specialists, thus
increasing competition with other species. When performing simulation without interference among
pollinators, this strong negative effects of innovative cheating at high frequency disappeared (Fig. 3a). This
suggests that the niche expansion of innovative cheaters that were initially specialists, can promote
competitive exclusion and thus decrease network persistence if cheating frequency is too high.

While these results were robust to change in connectance (Fig. S1 & S4), the positive effects of innovative
cheating on persistence tended to vanish when performing simulations on smaller communities, with 10
species per guild (Fig. 3b-c). This is consistent with our expectation, suggesting that a minimal number of
species is needed to see positive effects of cheating appearing, which likely propagate through long-path
feedback loops. Thus, these positive effects of cheating are likely to be missed in simpler model, that would
offer analytical solution but not model a realistic diversity of species.

Taken together, these results show that under some conditions, innovative cheating can enhance stable
coexistence of species in mutualistic communities, on average. The average results presented in Fig. 2a-b
explained ~57% of the variance in the effect of cheating on network persistence. A part of the remaining
variance was explained by the average growth rates of plants and animals and by network structure (Fig. S5).
Cheating was more likely to have a positive effect on persistence when plant and animals depend weakly on
each other than when this dependence is strong. On average, the effect of cheating was more positive (less
negative) when initial mutualistic interaction networks were more connected, more nested and more modular

 (Fig. S5), suggesting that the consequences of cheating were partially mediated by the structure of the
underlying mutualistic network.

Figure 3: Effect of cheating is mediated by interference among pollinators and diversity. *(a) Average effect of cheating*
on persistence, with or without competition among pollinators for partners (plants), when cheaters are specialists, for
an initial value of connectance φ=0.4. The case with competition is the same than in Fig. 2a. (b) Effect of cheating on
persistence in small communities, with 20 species (10 per guild) as a function effect of cheating on persistence in diverse
communities, with 40 species (20 per guild). For Λ=0.15 & φ=0.4. The bottom part is a zoom on the grey area of the
x-axis. The solid black line shows the first bisector while dashed black lines show the zero values (no effect of cheating
on persistence). (c) Volume of the 3D cheating parameter space in which cheating has a positive effect on network
persistence, as a function of of the scenario and the diversity, for Λ=0.15 & φ=0.4.

Considering the theoretical results developed above, empirical patterns of cheating should follow these
conditions to maximize community persistence: (i) cheaters should be mainly specialists species, (ii)
illegitimate interactions should mainly occur out of the mutualistic niche of cheaters (innovative cheating),
(iii) proportion of cheaters can be high but the overall level of cheating, measured as $\overline{\Delta} \times \Omega$, should stay low
(<0.5) and decrease with costs associated with mutualism, (iv) cost associated with mutualism should not be
too high.

To evaluate if these conditions are met in natural communities, we used a unique dataset of empirical interaction networks between flowering plants and pollinating birds, over 17 sites in two countries, Costa Rica and Ecuador. Analyzing empirical patterns using generalized linear models and type II ANOVA with Wald Chi-squared tests (cf. Methods), we found patterns consistent with the conditions in which cheating has a positive effect on persistence (Fig. 4). First, cheaters tended to be specialist species (Fig. 4b, $\chi^2 = 4,29$, p-value = 0.038), a result that was consistent across countries ($\chi^2 = 0.27$, p-value = 0.60 for the interaction). Second, birds tended to cheat mostly in an innovative way (Fig. 4c), *i.e.* outside of the niche defined by the morphological traits of their mutualistic partners (*cf.* Methods). Third, even if the proportion of cheaters was high in some cases (Fig. 4d), the overall level of cheating was low and strongly decreased with the elevation (Fig. 4e, $\chi^2 = 8.94$, p-value = 0.003), partially because the proportion of cheaters also decreased with elevation (Fig. 4d, $\chi^2 = 4.68$, p-value = 0.03). Elevation is likely a proxy of cost associated with mutualism because it increases physiological constraints on plants and birds (25,26), likely increasing the cost of nectar production for plants and flight for birds. These trends were not significantly different between countries (*cf.* Table S1). It was not possible to evaluate the fourth condition because cost associated with mutualism was not estimable from the data. Nonetheless, the three first conditions were highly consistent with the theoretical patterns of cheating that maximize network persistence.

Figure 4: Empirical cheating patterns in plant-bird interaction networks fit theoretical conditions to maximize network persistence. (a) An empirical network of interactions between plants (green) and birds (blue) from Ecuador for a given site. Thickness of the lines is proportional to interaction frequency, while colour of the lines represents cheating frequency, grey (only legitimate) and from pink (low cheating frequency) to bright red (only illegitimate). (b) Frequency of cheating as a function of mutualistic partner diversity, for each combination of bird species and site, for datasets from Costa Rica (beige) and Ecuador (dark blue). The size of the point represents the total number of interactions of the species in the given site. The solid lines show predictions of a generalized linear mixed-effects model with associated 95% confidence interval. (c) Proportions of innovative cheating, where each point is a bird species who cheated at least once. The size of the point represents the total number of interactions of the species summed over sites. (d) Proportion of cheaters and (e) overall level of cheating, for each site, as a function of elevation (in meters above sea level). The solid lines show predictions of generalized linear models with associated 95% confidence intervals.

To close the loop between theory and data, we also used these empirical networks to parametrize our dynamic model and perform simulations over a gradient of model parameters that were not estimable from data (*cf.* Methods, Fig. 5). We confirmed that observed cheating patterns increased network persistence of empirical network, when the cost associated with mutualism was low, regardless the competition strength (Fig. 5). Effects of cheating on network persistence in empirical networks became negative when considering high levels of per-interaction benefits and cost associated with mutualism. However, few empirical studies have shown that costs associated with mutualism are probably low, because they don't find negative effects of robbing on seed sets (27,28) while the only study we know that quantified per-interaction benefits (α) in pollination system found very low values (29). Thus, natural systems are probably more situated on the left of the Fig. 5, substantiating positive effects of cheating on network persistence.

Figure 5: Parametrizing theoretical models with empirical data reveal that cheating can increase network persistence, when cost associated with mutualism is low. *Effect of cheating on network persistence when parametrizing the model with empirical patterns of cheating, as a function of per-interaction benefit (α), strength of competition for mutualistic partners (c) and cost associated with mutualism (Λ). Points represent the average effects over the 100 simulations performed over different growth rate vectors, while error bars represent the standard deviation. Black cross represents the overall average (over sites) and associated 95% confidence interval (vertical error bars, often hidden because too small). Note that the x-axis is not linear, there is a jump between Λ = 0.15 and Λ = 0.3.*

Discussion

We described two different kinds of cheating in mutualistic systems: conservative cheating arising when a species profits from a mutualistic partner, and innovative cheating, when a species profits from a species that is not a mutualistic partner. Highlighting these nuances in cheating allowed us to unify in a common theoretical framework two different conceptions of cheating: a concept inherited from game theory in which species cheat to escape cost (conservative cheating, see *ref.* 9 & 14) and empirical observations showing that species cheat to access new resources (innovative cheating, see *ref.* 18). Here we show that these nuances in cheating are important because they have different consequences for network persistence. While conservative cheating almost always negatively affects network persistence, innovative cheating, the most prevalent kind of cheating in our empirical dataset, can have a positive effect on network persistence. In our empirical study case of plant-bird interactions, simulations and data analyses consistently show that cheating can increase the number of species able to coexist at ecological equilibrium. Evolutionary theory has proposed answers to the paradox of the persistence of mutualism in presence of cheaters (9,30). Here we show that these cheaters are not rare in nature, and that they can enhance species coexistence in mutualistic communities instead of destabilizing them. Since cheating has been reported in many kinds of mutualisms, such as mycorrhizal (5), cleaner fish-client (31), or seed-dispersal (7) interactions, it could be a common mechanism driving ecological stability of natural communities.

Most empirical studies focusing on cheating in mutualistic networks have used indirect proxies of cheating, such as marks on flower corollas left by nectar robbers (22,23) or heterotrophic status of plants in plant-mycorrhizal networks (5). Although these proxies are valuable, they do not allow to characterize

cheating as conservative or innovative, because cheating is defined at the species level. Here, by using camera
traps we were able to characterize each interaction as legitimate or illegitimate, and thus define cheating at
the interaction level, allowing us to estimate the relative importance of conservative and innovative cheating.
Our analyses of this unique empirical dataset show a continuum gradient between cheating and mutualism:
cheaters are common (up to 60% of the bird species, Fig. 4d) but they often cheat at a low frequency. Using
theoretical simulations, we show that such low cheating frequency can dramatically affect network
persistence, negatively or positively depending on the context (innovative *vs* conservative, cost and identity
of cheaters). Previous work has shown that this continuum from mutualistic to antagonistic interactions,
embedded in mutualistic networks, is important for community stability (7,32). We extend these results by
showing the distribution of the antagonistic links *vs.* mutualistic ones has important consequences for
stability. When considering overlapping commensalistic/antagonistic and mutualistic links (*i.e.* conservative
cheating) network persistence is lower than when commensalistic/antagonistic and mutualistic links occur
between different species pairs (*i.e.* innovative cheating).

Our theoretical results highlight four conditions that can turn cheating into a factor increasing network
persistence: (i) cheaters should be mainly specialists species; (ii) illegitimate interactions should mainly occur
out of the mutualistic niche of cheaters (innovative cheating); (iii) the proportion of cheaters can be high but
the overall level of cheating, measured as $\overline{\Delta} \times \Omega$, should be low (<0.5) and decrease with costs associated
with mutualism; and (iv) costs associated with mutualism should not be too high. Parametrizing our model
according to these rules led to ecological equilibriums that were on average more diverse than other parameter
combinations. However, since our model did not include evolution, the question remains whether these
ecological equilibriums are also evolutionary stable, that is can we expect to find them in nature.

Our analyses of empirical data suggest that patterns of cheating following the four conditions described
above can be found in nature. Empirical communities appeared to be in the parameter window in which
cheating tends to optimize ecological stability. Strong cheaters were specialist species, cheaters mainly
cheated in an innovative way and the overall level of cheating was relatively low and decreased when costs
associated with mutualism are likely to be greater (*i.e.* higher elevations). However, the cost associated with
mutualism is a key parameter that determines the outcome of cheating on community stability, but we were
not able to assess it from empirical data. Assessing this cost would require complex physiological
measurement on birds and plants, that currently have been only rarely done (33,34), and never on both guilds
simultaneously. Although these missing measures of cost associated with mutualism add a layer of
uncertainty on the effect of cheating on community stability, our theoretical results show that even with a
cost reaching 20% of the mutualism benefits, innovative cheating can still have a stabilizing effect, in a very
narrow parameter combination (Fig. 2b & S1).

The empirical patterns observed are the result of an interplay between community assembly processes
and evolutionary dynamics (35), suggesting that, against what we could have expected, eco-evolutionary
dynamics have shaped cheating patterns in a way that it increases community stability. The selection for
innovative cheating in specialist species could be explained by the ability of species to select partners, that
could lead to a competitive disadvantage for cheaters, strong enough to prevent generalists to become
conservative cheaters, but still allowing specialists species to evolve as innovative cheaters. It has been shown
recently that the coexistence of cheaters and mutualists can be evolutionary stabilized because of the ability
of species to select the partners to which they give benefits (10). This ability to choose can be itself
evolutionary stabilized by the presence or emergence of cheaters at each generation (36), thus leading to a
loop of eco-evolutionary feedbacks that could explain the empirical patterns observed here. However, it is
hard to substantiate this idea because studies focusing on cheating and evolution of mutualism have only
considered conservative cheating (8–10,30,36). Innovative cheating could also emerge because of divergent
optimal trait matching between plant and pollinators (37), leading to an arm race between them, than is likely
to evolve towards antagonistic interactions (38), and thus innovative cheating in this context. Given the
importance of innovative cheating for community stability, our results stress the need to revisit eco-
evolutionary theory of cheating in a network context (11,39). This future direction would provide new

insights on the astonishing faculty of evolutionary processes to sometimes create structures that promote
ecological stability at the community level (40).

Finally, since our theoretical model went through a necessary step of oversimplifying natural systems, we
likely neglected subtilities in the way species cheat that could affect the consequences of cheating for
community stability, for example behavioural changes of pollinators due to robbers (41). It has been shown
that many opportunistic pollinators use already existing holes in flower corolla (17,42). In this case, there is
likely a difference of cost for plants between the primary cheating event, degrading the floral parts that
involve an additional cost for plants, and secondary cheating events that only involve the cost associated with
mutualism (*i.e.* nectar production). In addition, consequences of such flower degradation likely depends to
when it occurs, after of before pollination, suggesting that the sequential order of these
mutualistic/antagonistic interactions is likely to drive the overall effect of cheating on lifetime fitness, as
suggested in plant-ant interactions (43). However, our results offer a new perspective on cheating in a
mutualism context, extending the classic view inherited from the game theory, to describe a kind of cheating,
innovative cheating, that was previously neglected in theoretical works. We derived a set of simple conditions
turning cheating in a mechanism enhancing species coexistence, showing that antagonistic interactions
embedded in mutualistic networks can play a key role in community stability. While previous studies on
evolution have shown that mutualism and cheaters can coexist in the same communities, here we show that
this mixture can increase the number of species coexisting in nature.

Materials and Methods

Theoretical model

We used a generalized Lotka-Volterra model with two guilds, plant (P_i) and pollinator (A_j), modelling
temporal variations of abundance for each species. We incorporated four parameters ($\overline{\Delta}$, Ω, Ψ, Λ) that control
respectively for the proportion of species cheating, proportion of links affected by cheating for each cheater
(cheating frequency), the proportion of innovative cheating (*vs* conservative cheating) and the cost associated
with mutualism. Since we expect that effect of cheating can be partially mediated by competition for partners,
we chose to use a complex functional response, accounting for interference among species from the same
guild (cf. equations (1) and (2)).

We generated a gaussian morphological trait for each species, to define an initial binary interaction matrix
(I_M) with a given connectance (*cf.* Supplementary Methods). $I_{M_{ij}}$ was the pairwise interaction strength
between plant i and pollinator j, and equaled either zero (no interaction) or one (mutualistic interaction). $I_{M.j}$
defined the mutualistic niche of pollinator j, *i.e.* all partners with which pollinator j interacted mutualistically.
The mutualistic niche of plant i was given by I_{M_i}.

Each species of pollinator was defined by a binary state, cheaters (1) *vs* non cheater (0), stored in the
vector Δ. The number of cheaters was defined as $round(\overline{\Delta}n_A)$, $\overline{\Delta}$ being the proportion of species cheating.
To define cheaters, we used two different scenarios, one in each of those cheaters are the most specialist
species and one in which they are the most generalist species (*cf.* Supplementary Methods). Each cheater
cheated with a frequency Ω of their initial legitimate interactions. This amount of cheating was divided in
conservative cheating $(1 - \Psi)\Omega$ and innovative cheating $\Psi\Omega$. The cost associated with mutualism was set
by parameter Λ, which could vary between 0 and α, the per-interaction benefit of mutualistic interactions, to
be in a mutualism case.

Thus, a plant i interacted in a legitimate way with pollinator j with a strength $M_{ij} = I_{M_{ij}}\left(1 - \Delta_j\Omega\right)$. The
same pair of species interacted illegitimately (with benefits only for the pollinator) with a strength $C_{ij} =$
$\Delta_j\Omega\left((1 - \Psi)I_{M_{ij}} + \Psi(1 - I_{M_{ij}})\right)$, where $\Delta_j\Omega(1 - \Psi)I_{M_{ij}}$ was the conservative cheating and $\Delta_j\Omega\Psi(1 -$
$I_{M_{ij}})$ the innovative cheating.

The model was described by the following system of differential equations for the plants and the
pollinators, respectively:

$$\frac{dP_i}{dt} = P_i\left(r_{P_i} + \frac{(\alpha - \Lambda)\sum_{j=1}^{n_A} M_{ij}A_j}{1 + \beta\sum_{j=1}^{n_A} M_{ij}A_j + c\sum_{k=1}^{n_P} \Pi_{ik} \times P_k} - \frac{\Lambda\sum_{j=1}^{n_A} C_{ij}A_j}{1 + \beta\sum_{j=1}^{n_A} C_{ij}A_j + c\sum_{k=1}^{n_P} Y_{ik} \times P_k} - \sum_{k=1}^{n_P} c_{P_{ik}} \times P_k\right) \quad (1)$$

$$\frac{dA_j}{dt} = A_j\left(r_{A_j} + \frac{\sum_{i=1}^{n_P}[\alpha(M_{ij} + C_{ij}) - \Lambda M_{ij}]P_i}{1 + \beta\sum_{i=1}^{n_P}(M_{ij} + C_{ij})P_i + c\sum_{k=1}^{n_A} \Theta_{jk} \times A_k} - \sum_{k=1}^{n_A} c_{A_{jk}} \times A_k\right) \quad (2)$$

The between parentheses part of equation (1) can be divided in four parts.

First, r_{P_i} was the basal growth rate of the focal species. Growth rates were scaled between -0.5 and -
0.001, and drawn randomly from a beta distribution, to sample a wide variety of possible vectors of growth
rates (*cf.* Supplementary Methods).

The second part modeled the balance between benefits and cost associated with mutualistic interactions.
For plants, per-interaction benefit (α) is the link between visits and the number of successful pollination
events, while the cost associated with mutualism (Λ) is the cost of nectar production on survival. To have
mutualistic interaction the benefits in terms of reproduction should be higher than the cost in term of survival
, so we fixed $\alpha > \Lambda$ (Table 1). Thus, overall benefits increased with the product of legitimate interaction
strength (M_{ij}) and abundance of the interaction partners by a rate $\alpha - \Lambda$. But since successful pollination can
not increase infitenly with the number of visits because of physiological limits, benefits saturated with a rate
β, which can be represented by the time a pollinator need to visit and access a flower of the focal species
(handling time, Table 1). Benefits also saturated because of competition among plants for shared pollinators,
by a rate c, Π_{ik} being a vector of interaction similarity between P_i and P_k (*cf.* Supplementary Methods).

The third part modeled the cost of cheating interactions only, regardless of their kind, innovative or
conservative. For the costs of illegitimate interactions for plants, we used a similar functional response than
for mutualistic interactions. Similarly, costs of illegitimate interactions increased and saturated with the
product of the amount of cheating in interactions C_{ij} and abundance of the interaction partners by a rate Λ
and β respectively. Costs also saturated because of dilution of cheaters among plants sharing cheaters (Y_{ik},
cf. Supplementary Methods), by a rate c.

Finally, the fourth part modeled the competition among plants, independent from mutualistic partners, for
example competition for space. For simplicity, here we considered only intraspecific competition setting
inter-specific competition strength for space at zero (Table 1).

Equation (2) can be divided in analogous parts, except that the third part described in equation (1) is
absent, as the cost-benefit balance associated with mutualism and cheating could be grouped in one functional
response, because all interactions with plants, regardless of their legitimate or illegitimate status, participated
to competition among pollinators. Since changing β or α roughly leads to the same result, for simplicity we
fixed $\beta=1$ for all species. Then we set the value of α in a way that species can theoretically persist when there
is no cheating, but not too high to be able to observe variation in persistence. Thus, we set $\alpha = 1.5$ for all
species (*cf.* Supplementary Methods).

Numerical simulations

We created 500 different set of species, with different traits and growth rates, while fixing
$n_A = n_P = 20$. For each of these initial conditions we solved the model numerically, for the 3630 chosen
possible combinations of cheating parameters (Δ, Ω, Ψ, Λ, Table 1). For each of these combinations and
initial conditions we applied two scenarios, one in which cheaters were the generalist pollinator species,
another one in which they were the most specialist species (*cf.* Supplementary Methods). We also performed
all these simulations with three different values of initial connectance (cf. Table 1). That led to 500×3630

× 2 × 3 = 10,890,000 simulations. We stopped a simulation when the variance of species abundance over the
last 10 time steps was lower than 10^{-14} or when the number of iteration reached 8,000. In >99,98% of the
simulations this was enough to reach a stable steady equilibrium (all eigen values of the Jacobian matrix have
negative real parts).

We also performed additional simulations to explore side mechanisms, using a given value of connectance
($\varphi=0.4$) and cost associated with mutualism ($\Lambda=0.15$). To test if cheating can still have a positive effect in
smaller communities, we performed simulations with $n_A = n_P = 10$. To investigate the role of competitive
exclusion in the fact that innovative cheating strongly affects persistence in a negative way when cheating
frequency is close to one, we performed simulations without competition (*i.e.* interference) among pollinators
for shared partners.

Table 1: Parameter values and initial values for variables for simulations. SM = Supplementary Methods

Parameter or Variable	Meaning	Value	Vary with parameter combination	Vary among initial conditions
$P_{i_{t=0}}$	Initial abundance of plant species i	1	No	No
$A_{j_{t=0}}$	Initial abundance of pollinator species j	1	No	No
α	Per-mutualistic interaction benefit	1.5	No	No
β	Per-interaction handling time	1	No	No
c	Per-capita interference for partners, within guild	1 (or 0 for pollinators in SM)	No	No
r_{P_i}	Plant basal growth rates for species i	ϵ [-0.5, -0.001], *cf.* SM	No	Yes
r_{A_j}	Pollinator basal growth rates for species j	ϵ [-0.5, -0.001], *cf.* SM	No	Yes
$c_{P_{ik_{k\neq i}}}$ $c_{A_{jk_{k\neq j}}}$	Strength of inter-specific competition strength for space, within guilds	0	No	No
$c_{P_{ik_{k=i}}}$ $c_{A_{jk_{k=j}}}$	Strength of intra-specific competition for space	1	No	No
n_P	Number of plant species	20 (or 10 in SM)	No	No
n_A	Number of pollinator species	20 (or 10 in SM)	No	No
$I_{M_{ij}}$	Per-capita interaction strength between plant i and pollinator j	0/1, *cf.* SM	No	Yes
$\bar{\Delta}$	Proportion of species cheating in pollinators	0.1 -> 1 per 0.1	Yes	No
Ω	Frequency of cheating for cheaters	0 -> 1 per 0.1	Yes	No
Ψ	Proportion of innovative cheating	0 -> 1 per 0.1	Yes	No
Λ	Per-interaction cost associated with mutualism	0/0.15/0.3	Yes	No

φ	Initial connectance of I_M	0.2/0.3/0.4	No	No

Networks metrics

To understand how the initial structure of the network affects persistence we measured the nestedness and
the modularity of the initial binary interaction matrix (I_M), using NODF index (44) and Newman's modularity
measure (45), respectively. The Newman's modularity measure is the likelihood-equivalent of the final
proposed module structure after optimization, which was done using the algorithm proposed by Beckett
(2016) as implemented in R package *bipartite* (47).

We evaluated network stability at equilibrium, as network persistence. Network persistence was measured
as the percentage of persisting species at equilibrium, with an abundance greater than 10^{-5} at the equilibrium,
other species being considered as extinct, for each community and simulation.

Analyses of theoretical results

We presented theoretical results either as the absolute values of network persistence over parameters and
scenario values (Fig. S1 for example), or as the difference between the case without cheating and the focal
simulation for similar initial conditions (Fig. 2). The later one directly represents the effect of cheating on
network persistence. These absolute or difference measures were averaged over the 500 initial conditions.

To determine the proportion of variance explained in cheating effect on persistence by our parameter and
scenario combinations (group), we calculated the overall variance of network persistence over all simulations
(V), and the variance within group (V_g), corresponding to the variance of centered persistence values for each
group (minus the average persistence of that group). These centered values represent the residual effects of
cheating on persistence, once we have accounted for parameter and scenario combinations. Then we
estimated the proportion of variance explained in cheating effect on persistence by our parameter and
scenario combinations as 1- V_g /V.

To understand what drives the residual cheating effect on persistence, we used a linear model to explain
the residual effect of cheating by: average growth rates of animals and plants and connectance, modularity
and nestedness of initial mutualistic interaction matrix. To break the correlation between connectance and
nestedness and between connectance and modularity, we centered values of nestedness and modularity by
the average nestedness and modularity, respectively, for each of the connectance values.

Empirical dataset

To assess the conservative/innovative character of cheating in empirical communities we used data of
interactions among flowering plants and birds, hummingbirds (Trochilidae) in Costa Rica and hummingbirds
and flowerpiercers (*Diglossa sp.*) in Ecuador. Sampled sites were located over an elevation gradient in the
tropical forests of Costa Rica and Ecuador (Table S2), in which interaction were recorded along transects
using camera traps, as described in Graham & Weinstein (2018, *ref.* 35). With each recorded interaction, the
information of the interaction status, legitimate (bird bill entering the corolla opening) *vs* illegitimate (bird
piercing the corolla), was recorded. Thus, here we assumed that illegitimate interactions do not bring any
benefits to the plants and that when a bird bill enters the corolla the interaction is legitimate. Previous results
have shown that even interaction that seem illegitimate can participate to pollination and thus be mutualistic
(49). However, because piercing is often done at the base of the corolla, robbing interaction described here
are likely to be non-efficient in terms of pollination, so as cheaters, although a strict classification would
require fitness estimate (30).

Data from Costa Rica includes 18,199 interactions from 12 different sites, sampled monthly between June
2019 and May 2021. Data from Ecuador includes 15,459 interactions from 5 different sites, sampled monthly

between February 2017 and December 2019. To obtain interaction frequency independent from the sampling
pressure, each interaction count was divided by the number of hours of sampling on the corresponding plant,
then multiplied per 24 to get interaction frequencies in interaction.day^{-1}, for legitimate and illegitimate
interactions. Then, in both datasets, we aggregated interactions over time to get one interaction network per
site (Fig. S6 & S7). Since on the transect plant abundance have been recorded independently, we were able
to compare the diversity of flowering plants we sample relative to the observed diversity on the transect. On
average we sampled 74% of the flowering plants present on each site, with values going from 57% to 93%.
Most of non-sampled plants were either non-tubular, so unlikely to be visited by hummingbirds, or species
of low abundance (Fig. S8).

Estimation of empirical cheating parameters

To compare empirical patterns with our theoretical results, we estimated the 3 parameters related to
cheating in our model: the proportion of pollinator species cheating ($\overline{\Delta}$), cheating frequency of these cheaters
(Ω), the proportion of innovative cheating *vs* conservative cheating (Ψ). The estimation of these 3 parameters
is detailed below.

To estimate the proportion of cheaters in each site, we calculated the proportion of species with at least
one illegitimate interaction.

To estimate the cheating frequency for each bird species in each site, we calculated the proportion of
illegitimate interactions for each species for each site, as the frequency of illegitimate interaction divided per
the total frequency of interaction, both summed over all the partners of the focal bird species in the given
site.

To estimate the proportion of innovative cheating, we first built a 2-dimensional mutualistic niche for
each bird species. To do so, we used 2 plant traits measured on flowers (*cf.* Supplementary methods), the
length of the corolla and its curvature. We had to exclude 17 plant species over 246 because of missing trait
values. For each bird species we then calculated a 2D kernel density distribution of mutualistic partners, over
corolla length and curvature, weighting each plant by the legitimate interaction frequency with the focal bird
species. This 2D density distribution models the mutualistic niche of the bird. We then did the same
manipulation, but weighting the density by the illegitimate interaction frequencies, to obtain the space in
which bird are cheating. Each density distribution summed to one. The overlap between the density function,
measured as the area under the minimum of both functions, corresponds to the proportion of conservative
cheating. It equals to one when bird cheat only within their mutualistic niche, and zero when bird cheat only
outside of their mutualistic niche. To obtain the proportion of innovative cheating we simply took one minus
this overlap, because the proportion of innovative cheating equals one minus the proportion of conservative
cheating.

Finally, to estimate the overall level of cheating in each site ($\overline{\Delta} \times \Omega$), we calculated the average proportion
of illegitimate interactions across all species of the focal site, as the frequency of illegitimate interactions
divided by the total frequency of interactions, both summed over all pairs of plant and bird species in the
given site.

Statistical analyses of empirical patterns

Since elevation negatively affects net primary production of plants (25), it is expected to be positively
correlated with the cost of nectar production, especially because of temperature-mediated effects on
photosynthetic activity (50). Elevation is also known to increase flight cost for birds, especially
hummingbirds(26,34). These elements make elevation a good proxy of costs associated with mutualism. To
assess how the proportion of cheaters and overall level of cheating varied over elevation, for each of these
response variables we used a generalized linear model with a quasibinomial error distribution and a logit link
function, where we included elevation as predictor and its interaction with country.

To assess how cheating frequency varies with the level of generalization/specialization of birds, we used
a generalized linear mixed-effects model with a binomial error distribution and a logit link function. This
model explains cheating frequency of each bird species in each site per the logarithm of their diversity of
mutualistic partners, in interaction with the country. We used the logarithm to implement a saturation to
generalism, all species with many partners being similarly generalists, while considering an important
difference in term of generalism between a species having one partner and a species having three partners
We also included random site and bird effects on the intercept. Diversity of mutualistic partners was
calculated as the number of plants with which at least one legitimate interaction was recorded, for each bird
species and site.

Numerical simulations with empirical networks

To test if the observed patterns of cheating were likely to increase network persistence, we parametrized
our dynamic model with empirical patterns of cheating. First, we converted empirical interaction networks
presented in Fig. S6 & S7, into binary interaction matrix I, in which I_{ij} is a binary state describe if bird j and
plant i interacted at least once mutualistically (1) or never (0). We used a binary interaction matrix as a
mutualistic backbone rather than a quantitative interaction matrix because we assume that it reflects the
ability of species to interact in a mutualistic way, while interaction frequencies depend much more on
abundance. Second, we estimated the proportion of cheating among those species (C_{ij}) by dividing the
frequency of illegitimate interactions per the total number of interactions. Then we estimated the ability of
this species pair to interact in a legitimate way using $M_{ij} = I_{ij}(1 - C_{ij})$, In our model abundances were
modelled a part of the interaction matrix, thus this interaction matrix should reflect only the ability to interact,
and not interaction frequencies.

Parameters from the functional response could not be inferred from the data: the per-interaction benefit
(α), sometimes called mutualistic strength (51,52), the cost associated with mutualism (Λ), the handling time
(β) and the strength of competition for mutualistic partners (c). To overcome this limitation, we performed
simulations over a gradient of possible values, even if it is hard to give an empirical meaning to those
parameters. We thus perform simulations from low ($\alpha = 1$) to high per-interaction benefits ($\alpha = 2$) by steps
of 0.2, for 3 different values of cost associated with mutualism ($\Lambda \in [0, 0.05, 0.1, 0.15, 0.3]$) and two different
values of competition, intermediate ($c = 0.5$) and high competition strength ($c = 1$). Since changing the value
of β has roughly the same consequences as changing α, we decided to keep β constant. For each of these per-
interaction benefit and cost combinations we generated 100 different combinations of growth rate vectors,
using equation (S1, *cf.* Supplementary Methods). For each of the 17 site, 100 initial conditions and 60
parameter combinations, we performed simulations with all empirical interactions, or without cheating
interactions (setting $C_{ij} = 0$, for all i and j).

This part led to 204,000 new simulations. To analyze these simulations, we measured persistence at
equilibrium, as explained above, and we subtracted the value of the simulation set without cheating to the
value of the corresponding simulation with all interactions. This allowed us to obtain the effect of cheating
on network persistence, presented in Fig. 5.

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Supporting information files

S1. Supplementary Methods

S2. Supplementary Figures and Tables.

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