Fast and flexible Bayesian Jolly Seber models and application to populations with

transients

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Abstract

1. Jolly Seber (JS) models are an appealing class of capture-recapture models for

modeling open populations because they allow for inferences about an array of

population parameters, including abundance, survival, and recruitment. Multiple

formulations of JS models have been developed and include both maximum

likelihood and Bayesian approaches. Bayesian approaches offer greater flexibility;

however, they are often extremely slow when applied to moderate to large

populations because the latent states of all observed individuals, as well as any

potential unobserved individuals (parameter-expanded data augmentation), must be

simulated at each time step.

2. JS model implementations can be sped up dramatically through marginalization,

whereby the conditional likelihoods of states are tracked for unique capture histories,

rather than the simulated states of all individuals. Here we describe a marginalized

implementation of a multistate JS model and compare its performance to that of an

implementation using simulated discrete states. We fit models to data generated under

two scenarios, one in which no data was missing and another in which 25% of data

was randomly removed. To illustrate how marginalization can accommodate more

complex models and datasets, we describe a modified version of the model for

application to populations with transients and fit the model to simulated data and to

data collected on Kentucky Warblers (*Geothlypis formosa*) as part of the Monitoring

Avian Productivity and Survivorship (MAPS) program.

3. Both the discrete latent state and marginalized JS model implementations performed

similarly with respect to bias and coverage; however, the marginalized

implementation was roughly 1,000 times faster when no data were missing and 100

times faster when 25% of data was missing. The marginalized model accommodating

transients also converged quickly and a more complex version of the model applied to

the larger multi-site Kentucky Warbler data set yielded useful estimates of most

parameters within a reasonable time frame (hours).

4. Gains in efficiency provided by marginalization shown here should stimulate

additional study and development of this useful class of models and provide new

opportunities for real-world applications to large complex data sets.

keywords: capture-recapture; discrete latent state, Hidden Markov model,

marginalization, Monitoring Avian Productivity and Survivorship, open population,

recruitment, residency, survival, transient model.

Introduction

Open-population capture-recapture models are important tools for estimating

demographic parameters of wildlife populations (Nichols 2005). These models include two

basic classes: (1) Cormack-Jolly-Seber (CJS) models, which condition on first capture and

provide estimates of apparent survival probability (Cormack 1964); and (2) Jolly-Seber (JS)

models (Jolly 1965, Seber 1965), which are informed by entire capture histories (i.e.,

including occasions both prior to and after first capture). JS models are appealing because

they make more complete use of available data and can provide inferences on an expanded

set of demographic parameters including abundance and recruitment-related parameters. JS

models assume that marked and unmarked animals have equal capture probability, which

may limit their applicability in some situations (e.g., mark-resight studies). However, this

assumption is likely reasonable for a broad array of studies that implement the same sampling

protocol for both captures and recaptures (e.g., Robinson et al. 2009).

A variety of formulations of both CJS and JS models have been developed and include

both maximum likelihood and Bayesian approaches (Pradel 1996, Schwarz and Arnason

1996, Link and Barker 2005, Dupuis and Schwarz 2007, Schofield and Barker 2008, Royle

and Dorazio 2012, Tenan et al. 2014, Hostetter et al. 2021). Bayesian implementations offer

several advantages over maximum likelihood methods, including ability to incorporate prior

information, flexibility for handling hierarchical random effects, and relative ease with which

derived quantities and their uncertainties can be calculated. A common Bayesian approach,

known as state-space modeling or discrete latent state modeling (Royle 2008, Yackulic et al.

2020), involves simulating the state of individuals (e.g., alive/dead) and the conditional

probability of their detection based on Bernoulli or categorical models applied to a set of

observed capture histories. For JS models, the data set must be augmented to include a set of

capture histories with no detections that represent individuals never observed to allow for

modeling of both the survival and entry processes (Kéry and Schaub 2011). A drawback of

this approach, however, is that computation times using Markov Chain Monte Carlo

(MCMC) techniques can be prohibitive for many applications, particularly when the

augmented data set includes many individuals or levels of stratification (e.g., sites or spatial

strata).

Bayesian open-population models with discrete latent states can be sped up dramatically

through marginalization (Yackulic et al. 2020). Rather than tracking the state of all

individuals at each time step, these marginalized models only require tracking likelihoods of

possible states given the demographic parameters for a reduced data set of unique capture

histories and their frequencies. Yackulic et al. (2020) provide a thorough introduction to the

marginalization in Bayesian population models, as well as code and examples for CJS

models. Here we extend this work in the context of JS models. We focus on the multistate

expression of the JS model described in Royle and Dorazio (2012), which is readily adaptable

to a variety of model extensions involving additional states (Kéry and Schaub 2011). We

apply the model to simulated complete data sets and data sets with random missing data, a

common scenario in multi-site multi-collaborator data sets (e.g., Saracco et al. 2010), and

compare parameter estimates and run times between the marginalized models and discrete

latent state implementations using the popular open-source software program JAGS

(Plummer 2003).

We also describe an extension of the basic marginalized multistate JS model to

accommodate situations where not all sampled individuals are part of the resident

populations. This model variant can both improve inferences about survival, recruitment, and

population size, as well as allow estimation of residency probability and proportions of

residents in populations (or, conversely, transience probability and proportions of transients),

which may also often be of ecological interest (Wilson et al. 2018, Genovart and Pradel 2019,

Oro and Doak 2020). Accounting for negative bias in survival estimates due to transiency,

and estimation of residency or transiency probabilities, has been treated within the context of

CJS models (Pradel et al. 1997, Nott and DeSante 2002, Hines et al. 2003, Royle and Dorazio

2008, Saracco et al. 2010). However, transiency or residency probability estimates from these

models only apply to newly marked individuals and so may not be representative of the larger

population because they depend, to some extent, on the proportions of previously marked

individuals still alive and available for capture (Hines et al. 2003). Estimation of parameters

related to the dynamics of resident and transient individuals within seasons has been

developed within an 'open robust design' framework (Ruiz-Gutierrez et al. 2016); however,

these models require additional data and model complication that may be unnecessary if

primary interest is on between season dynamics. Treatment of these parameters in the JS

context represents an important advance because it allows for disentangling of season-

specific observation (first capture) and state (residency) processes within a simpler multi-

season open population model.

We apply this 'transient JS' model to simulated data as well as to regional data from a

migratory bird species, Kentucky Warbler (*Geothlypis formosa*), from bird-banding stations

operated as part of the Monitoring Avian Productivity and Survivorship (MAPS) program

(DeSante et al. 2004) in the Central Hardwoods Bird Conservation Region of the United

States (Sauer et al. 2003).

Materials and Methods

Multistate Jolly Seber models: structure and data

Both the discrete latent state and multistate JS model assume a "superpopulation" (*sensu*

Schwarz and Arnason 1996), N_{super} , representing the number of individuals ever alive in the

population. Membership in N_{super} is determined as a function of parameters describing the

entry process and an augmented data set consisting of *M* individuals, including all those

observed during the study, as well as any unobserved individuals that could have been

members of the superpopulation. While the number of unobserved individuals to include in

the augmented data set is somewhat arbitrary, the choice is not innocuous, particularly when

using a discrete latent state implementation – too many and run times will be unnecessarily

increased, too few and parameter estimates may be biased.

Following Kéry and Schaub (2011) and Royle and Dorazio (2012), we model the entry

process in terms of a removal entry probability, γ, which represents the probability of entry

for a member of M conditional on not having previously entered (see Appendix S1 for an

alternative parameterization). Once entered, the probability of remaining alive and in the

population is determined by a survival parameter, ϕ. We can represent the latent state of the

$i = 1, ..., M$ individuals across $t = 0, ..., T$ time periods with a matrix, $\mathbf{S}$, with entries, $s_{i,t}$ that

can take values of: 1 = not yet entered into the population, 2 = alive and in the population,

and 3 = dead. The number of time periods, T, includes all observed sampling occasions as

well as a dummy occasion at $t = 0$ to allow modeling of initial entry into the population. All

$s_{i,0}$ are set equal to 1 to indicate that none have entered prior to the first observed time period

at $t = 1$. The hidden Markov process determining $s_{i,t}$ can be represented with an array, $\mathbf{\Omega}$,

with individual entries $\omega_{j,k,t}$ representing probabilities of transitioning from latent state j

(rows) in time t to latent state k (columns) in time $t + 1$:

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$$\omega_{j,k,t} = \begin{pmatrix} 1 - \gamma_t & \gamma_t & 0 \\ 0 & \phi_t & 1 - \phi_t \\ 0 & 0 & 1 \end{pmatrix}.$$

The data informing the latent states consist of a set of observed and unobserved (i.e.,

augmented) capture histories and, for the discrete latent state model, can be represented with

a $M \times T$ matrix, $\mathbf{Y}$, with entries $y_{i,t}$. For the marginalized model, the $y_{i,t}$ are summarized to a

more compact matrix, $\mathbf{YS}$, with entries $ys_{m,t}$ that represent $m = 1, ..., MS$ unique capture

histories over the T years. The data informing the marginalized model are then the $ys_{m,t}$ and

their observed frequencies. The entries of $\mathbf{Y}$ and $\mathbf{YS}$ can take values of 1 (captured) or 2s (not

captured). For computational purposes, we set all $y_{i,0} = 2$ and $ys_{m,0} = 2$ for the initial

dummy capture occasion. These capture histories are linked to latent states by a second array,

P, with entries $\rho_{j,o,t}$ indexed by latent state j (rows), observed state o (columns), and period

of observation t (not counting the dummy capture occasion), with time-specific capture

probabilities represented by p_t:

$$\rho_{j,o,t} = \begin{pmatrix} 0 & 1 \\ p_t & 1 - p_t \\ 0 & 1 \end{pmatrix}.$$

The principal difference between the discrete latent state and marginalized JS model

implementations is the definition of the likelihoods. In the discrete latent state model, the true

latent state is simulated for each individual and occasion for all $t > 0$ based on a categorical

model, $s_{i,t} \sim Cat\left(\omega_{z[i,t-1],1:3,t-1}\right)$. The likelihood is then determined based on a categorical

model of the observations conditional on the latent state, $y_{i,t} \sim Cat\left(\rho_{s[i,t],1:2,t}\right)$.

The likelihood for the marginalized JS model is defined in terms of an array, **Z**, which

tracks capture history likelihoods conditional on the demographic parameters. Its dimensions

are defined (in order) by unique capture histories, $t = 0, \dots, T$ sampling occasions (again,

including the dummy occasion at $t = 0$), and $s = 1:3$ states. Each entry, $\zeta_{m,t,s}$ is the

likelihood that an individual with capture history m was in state s at time t conditional on the

observed capture history through time t and values of the process and observation parameters.

As in the discrete latent state model, no individuals have entered the population at $t = 0$.

Thus, we set $\zeta_{m,0,1} = 1$ and $\zeta_{m,0,2:3} = 0$ so that all individuals are available prior to the study.

For each subsequent time step, $\zeta_{m,t,s}$ is determined by first taking the inner product of

$\zeta_{m,t-1,1:3}$ and the column vector taken from s^{th} column of the state transition matrix and then

multiplying this quantity by the probability of the observed state given the state s (i.e.,

$\zeta_{m,t,s} = \langle \zeta_{m,t-1,1:3}, \omega_{1:3,s,t-1} \rangle \times \rho_{s,o[m,t],t}$. For example, at the first true capture period ($t =$

1), the observation probability for capture histories with capture at that time period (i.e.,

$y_{m,1} = 1$) would be calculated as $\zeta_{m,1,1} = \zeta_{m,0,1}\omega_{1,1,0}\rho_{1,1,1} = 1 \times (1 - \gamma_0) \times 0 = 0$ for

individuals that did not enter (i.e., $s = 1$); $\zeta_{m,1,2} = \zeta_{m,0,1}\omega_{1,2,0}\rho_{2,1,1} = 1 \times \gamma_0 \times p_1 = \gamma_0 p_1$

for individuals that entered (i.e., $s = 2$); and $\zeta_{m,1,3} = \zeta_{m,0,1}\omega_{1,3,0}\rho_{2,1,1} = 1 \times 0 \times 0 = 0$ for

dead individuals (i.e., $s = 3$). Thus, the only possible transition for individuals captured at the

first true capture occasion is entry into the population.

The likelihood of each capture history is determined by summing the likelihoods of all

possible states, s, after the final capture occasion, $\sum_{s=1}^{3} \zeta_{m,T,s}$, weighted by the frequency of

the mth capture history. In BUGS language, as implemented in popular software programs

such as WinBUGS (Lunn et al. 2000), OpenBUGS (Lunn et al. 2009), JAGS (Plummer

2003), and NIMBLE (de Valpine et al. 2017), a modified version of the "ones trick" can be

used to update the posterior with these values. See Yackulic et al. (2020) and Appendix S1

for detail; Yackulic et al. (2020) also provide the appropriate approach to updating the

posterior using the program Stan (Carpenter et al. 2017).

For both the discrete latent state and marginalized models, unconditional time-specific

entry probabilities from the superpopulation to the population, b_t are derived as a function of

the entry probabilities conditional on not having previously entered, c_t, where $c_0 = \gamma_0$ and

$c_t = \gamma_t \prod_{j=0}^{t-1}(1 - \gamma_j)$ for $t \geq 1$, and the inclusion probability (i.e., probability of being a

member of the superpopulation), ψ (Kéry and Schaub 2011): $b_t = c_t/\psi$. In discrete latent

state models, secondary parameters (i.e., derived quantities) can be calculated directly from

the modeled latent states. For example, time-specific numbers of newly entered individuals

(i.e., newborns or immigrants), B_t, can be derived by counting the $z_{i,t} = 2|z_{i,t-1} = 1$, and

total time-specific abundance, N_t, can be calculated by counting the $z_{i,t} = 2$ for each sample

of the posterior distribution.

Alternatively, secondary parameters can be derived as functions of primary (i.e.,

modeled) parameters, other secondary parameters, and/or the input data; and this approach

can be applied to either model type. For example, numbers of new entrants can be estimated

as $B_t = c_t M$, and the superpopulation size, N_{super}, can then be derived as $\sum_{t=0}^{T-1} B_t$ (Schwarz

and Arnason 1996). Time-specific abundance can be estimated as $N_1 = B_0$ for the initial

sampling period and $N_t = B_{t-1} + \phi_t N_{t-1}$ for $t > 1$, or alternatively could be estimated with

the canonical estimator, $N_t = n_t/p_t$, where the n_t represents a count of the number of

individuals observed alive at time t (i.e., summing the frequencies of all $y_{i,t} = 1$ or $ys_{m,t} = $

1). Other quantities of interest that can be derived include population growth rate, $\lambda_t = $

N_{t+1}/N_t, and per capita entry rate, $f_t = B_t/N_t$ (or, alternatively, $f_t = \lambda_t - \phi_t$; Pradel 1996,

Link and Barker 2005). Additional methods for deriving secondary parameters from

marginalized models are also possible. For example, annual abundance can be derived by

simulating latent states from reconstituted individual capture histories (i.e., converting **YS**

back to **Y**) and summing them in a manner analogous to what is described above for the

discrete latent state models (see Appendix S2 for detail).

Marginalized multistate Jolly Seber model with transients

Capture-recapture studies often include individuals that are sampled but are not resident

in the local population. These transient individuals have been defined in the context of CJS

models as individuals having zero probability of being alive and available for capture

following initial capture (Pradel et al. 1997). In the JS context, however, transients can be

defined more generally as individuals appearing only once and never returning to the

sampling area. Thus, interpretation of transience and residency probabilities in the JS context

is more ecologically relevant because it refers to the larger population, not just the population

of newly marked individuals. We can accommodate transiency in the multistate JS model by

adding a state that allows for entry as either a resident or a transient, such that there are now

four possible states, including: 1 = not yet entered; 2 = alive resident; 3 = alive transient; and

4 = dead. Distinguishing between the two alive states requires an extra parameter π, denoting

the probability of being a resident. Thus, individual entries in the transition and capture

probability arrays become:

$$224 \qquad \omega_{j,k,t} = \begin{pmatrix} 1-\gamma_t & \gamma_t\pi & \gamma_t(1-\pi) & 0 \\ 0 & \phi_t & 0 & 1-\phi_t \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{pmatrix} \text{ and } \rho_{j,o,t} = \begin{pmatrix} 0 & 1 \\ p_t & 1-p_t \\ p_t & 1-p_t \\ 0 & 1 \end{pmatrix}.$$

The residency probability parameter, π, is estimated in the marginalized multistate

transient JS model based on $N_i^R \sim Bin(\pi, FR_i)$, where N_i^R is the number of residents

represented by unique capture history i. In some cases, the residency state can be partially

observed. For example, within a 'robust design' sampling framework (Pollock et al. 1990),

whereby multiple secondary sampling occasions are completed within each primary sampling

occasion, individuals observed on multiple secondary sampling occasions during the primary

sampling occasion in which they were marked can be used as an indicator of residency (Nott

and DeSante 2002, Hines et al. 2003). To accommodate this scenario, and following logic

developed for the discrete latent state version of a transient CJS model (Saracco et al. 2010),

we can define an observation model for residency as: $r_i \sim Bin(\kappa, N_i^R)$, where r_i is the

number of observed residents for capture history i, κ is the probability of observing

residency, and N_i^R is the true number of residents for capture history i. Note that in contrast to

the CJS scenario, where residency observation and state probabilities are specific to years of

first capture and allow for temporal modeling, here both κ and π are time-constant.

Nevertheless, we can derive numbers of transients and residents entering the population at

each time step as $B_t^{tr} = c_t * (1-\pi) * M$ and $B_t^{res} = c_t * \pi * M$, respectively. For transients,

the number of entries is equivalent to the number of transients in the population at any time

step; i.e., $B_t^{tr} = N_t^{tr}$. At $t = 1$, the total number of residents is also the same as the number

of resident entries, $N_1^R = B_1^R$; the number of residents can be derived as $N_t^R = B_t^R + \phi_t *$

N_{t-1}^R for subsequent time steps. The proportion of residents at any given time can then be

derived as $prop(res)_t = N_t^R / (N_t^R + N_t^{tr})$.

A critical assumption of this formulation of the transient JS model is that p_t, the

probability of capture at least once across the season, is the same for both transient and

resident individuals. This is plausible if most individuals enter the population early in the

season and we think of p_t as an initial capture probability, π as the probability of persisting

for multiple sampling periods, and κ as the probability of capturing an individual that persists

for multiple periods. Nevertheless, we acknowledge that in many cases residents and

transients will have differential exposure to capture, resulting in violations of the assumption

of equal p_t between these two groups. Accounting for these differences can be

accommodated with additional model development and data from secondary samples within

seasons (e.g., Ruiz-Gutierrez et al. 2016). For simplicity, we do not consider this additional

complication here.

Discrete v. marginalized multistate JS models: a simulation study

To compare the relative speed and efficacy of discrete latent state and marginalized JS

models, we simulated 100 capture-recapture data sets. As in Kéry and Schaub (2011), we

assumed a superpopulation size of $N_{super} = 400$ across $T - 1 = 7$ capture occasions, a

constant survival probability of $\phi = 0.70$, entry probabilities of $b_1 = 0.34$ and $b_{2...7} = 0.11$,

and a constant capture probability of $p = 0.50$. We assumed $U(0,1)$ prior distributions for

survival, ϕ, capture probability p, and entry probabilities b_t. Data sets were augmented with

500 all-ones capture histories to account for unobserved individuals for a total of M capture

histories (observed + unobserved). These individual capture histories made up the basic data

sets for the discrete latent state JS model, an $M \times T$ matrix, where T represents the number of

sampling occasions, including the dummy occasion. For the marginalized model, data sets

(including the augmented individuals) were aggregated to MS unique observed capture

histories and their frequencies.

To explore potential effects of missing data, we randomly assigned 25% of the

individual × capture occasion data generated in the simulated data sets to be missing. For the

marginalized models, capture histories were then collapsed to unique capture history × effort

(missing or not). Missing data in the two model types are handled differently. For the discrete

latent state models, missing data values are imputed with the categorical models of the state

and observation process in the same way they are for the complete data situations, which

should result in relatively little increases in model run times. However, for the marginalized

models, where state and capture probabilities are tracked with deterministic nodes, missing

data can be accommodated by setting capture probabilities to zero for missed occasions. This

requires tracking capture probabilities and conditional state likelihoods across an additional

dimension allowing for different capture probabilities among individuals sampled at different

times, which may result in relatively greater loss in efficiency. An alternative approach,

which we do not explore here but that could also have implications for model run times,

would be to define a multistate model for p_t, whereby p_t can take 'available' or 'unavailable'

states depending on whether sampling occurred (e.g., Lovich et al. 2014).

For the discrete latent state models, we derived secondary parameters as functions of the

summed latent states as in Kéry and Schaub (2011). For the marginalized models, we derived

secondary parameters as analytical functions of the primary parameters and data or other

second-order states, as described above, as a simulation study based on the primary parameter

values used here showed better credible interval coverage, faster implementation time, and

less biased parameter estimates compared to alternative methods of deriving second-order

states and secondary parameters (Appendix S2).

To assess models and data sets, we compared the ability of models to recover data

generating values, 95% credible interval coverage, credible interval widths, and model run

times. We implemented all models in JAGS (Plummer 2003) with the jagsUI package

(Kellner 2015) in R (R Core Team 2021). R code for simulating data and implementing

models is provided in the data package (Saracco and Yackulic 2023), and a detailed

description of model code is provided in Appendix S1.

Transient marginalized multistate JS models

We applied a transient marginalized multistate JS model to 100 simulated data sets using

the same parameters as the marginalized JS model above, but with the added residency

parameters set to $\pi = 0.6$ and $\kappa = 0.4$. Simulation and model details are provided in the data

package.

We applied a version of this model to capture-recapture data from 2912 adult Kentucky

Warblers (*Geothlypis formosa*) banded between 1993 and 2015 in the Central Hardwoods

Bird Conservation Region in the United States (Sauer et al. 2003) as part of the Monitoring

Avian Productivity and Survivorship (MAPS) program. These data were collected at 51

MAPS stations, which on average operated ~ 10 yrs (sd = 6) of the 23-yr time span, resulting

in ~ 42% (28058 of 66976) of the individual × year data points missing. For the analysis,

these data were summarized to yield 876 unique capture histories. We used a $Beta\big(1/(T -$

$1), 2 - t/(T - 1)\big)$ prior distribution on γ_t due to the missing data and large number of

sampling periods (Dorazio 2020). Initial attempts using $U(0,1)$ priors for γ_t with MAPS data

resulted in marginal posterior distributions on N peaking at M, regardless of how many

unobserved individuals the data set was augmented with. To allow for spatial variation in

capture probability, we modeled $p_{sta[i]}$ with a logit-linear model with intercept and a random

station effect distributed as $Norm(0, \sigma^2)$. In addition, we included annual variation in

survival by modeling ϕ_t with a logit-linear model with intercept and a random year effect

distributed as $Norm(0, \sigma^2)$. We applied standard vague priors for intercepts ($Norm(0,0.01)$)

and variances of random effects ($Unif(0,10)$).

Results

Discrete v. marginalized multistate JS models

Median estimates of the data generating parameter values were successfully recovered

for both the discrete latent state and marginalized multistate JS model implementations (Fig.

1). Credible interval coverage was close to nominal at the 95% level for most parameters and

scenarios, although it was slightly lower for the N_{super} and p parameters (Table 1; Fig. 1).

Coverage for the N_{super} and p parameters for models with missing data was especially low

(~ 80-90%). The abundance estimates, N_t and N_{super}, tended to be biased high for all

models and data scenarios. Median bias of posterior medians for the abundance parameters

was lowest for the discrete latent state model with complete data (+ 3-7%), slightly higher for

the marginalized model with complete data (+ 5-8%), and greater still for the models with

missing data (+ 6-12% for the discrete latent state model and + 7-14% for the marginalized

model). Estimates of capture probability, p, tended to be biased low and was similar between

models (median – 5% bias in posterior p medians for both models with complete data and –

6% for models with missing data). Credible interval widths were essentially identical

between the discrete and marginalized models for the entry, survival, and capture probability

parameters; however, widths were ~ 10-20% greater for derived parameters, such as N_{super}

(Table 1). The marginalized models ran much faster than the discrete latent state models,

reaching 1000 effective samples for the least converged parameter ~ 100 × (missing data

model) to 1000 × faster than the discrete latent state versions (Fig. 2).

Transient model applied to simulated data

The model converged quickly, with a median time to achieve 1000 effective samples of

the least converged parameter of 0.5 minutes. Parameter estimates were very similar to the

data generating values, suggesting that the model can provide reliable inferences about

residency probability, numbers of residents in the population, survival and recapture

probabilities under the assumption of equal p_t between residents and transients. As for the

basic model version, however, estimates of capture probability tended to be biased low and

population size high (Fig. 3). Residency probability also tended to be biased high (Fig. 3a).

Coverage of 95% credible intervals was relatively low for capture probability and

superpopulation size of residents (between 80% and 85%, Fig. 3c).

Application to MAPS data

Based on a model run with 3 MCMC chains of 40000, burn-in of 10000, and thinning

rate of 3 (for a total of 30000 saved posterior samples), the model took approximately 24

hours to run, considerably longer than our simpler simulation examples. Most parameters

converged relatively quickly with the median time to achieve 1000 effective samples of 4

hours; however, a few parameters took longer with the least converged parameter taking 3.7

days to achieve 1000 effective samples. All parameters had $\hat{R} < 1.01$, suggesting satisfactory

convergence.

Model results suggested that survival probability was relatively consistent across the

study (ϕ=0.5 [0.46, 0.54]; σ=0.09 [0, 0.3]; Fig. 4a). The derived recruitment rate was much

more variable, particularly for the first and last time intervals (Fig. 4b). However, precision

of the recruitment estimates was also lower for those intervals and likely reflect the low

number of stations operated during the first and last years of the time series (8 and 3,

respectively). Annual population change and abundance matched patterns of recruitment

(Figs. 4c, d), suggesting the importance of this demographic rate in driving population

dynamics. Residency probability, π, was estimated to be ($\pi = 0.53$ [0.44, 0.64], and the

proportion of residents in the population was relatively consistent across years, again with the

exception of first and last years (Fig. 4e).

Discussion

Bayesian modeling with MCMC estimation provides a flexible framework for

implementing capture-recapture models with latent states and complex hierarchical model

structures. However, because common Bayesian implementations of these models require

simulating discrete latent states of each individual at each time step, they can be slow to

converge and require long run times for moderate to large data sets (Yackulic et al. 2020).

This is especially true for JS models, where observed capture histories must be augmented

with potentially large numbers of unobserved individuals to encompass the population of

interest. Here we show that through marginalization, whereby the individual capture histories

are aggregated to unique capture histories (or unique capture history × covariate) and their

frequencies, and state probabilities, rather than individual states, are tracked, parameter

estimates can be recovered in a fraction of the time. This gain in efficiency greatly expands

the potential applications for this useful class of capture-recapture model.

Because JS models do not condition on first capture, they require an assumption of equal

capture probability for captured and uncaptured individuals, which may limit their utility for

certain sampling scenarios (e.g., mark-resighting studies). However, whenever this

assumption is reasonable, these models provide an attractive alternative to CJS models,

because they enable inferences about an expanded suite of demographic parameters including

recruitment, population size, and population dynamics. As proposed in the original

formulations of Jolly (1965) and Seber (1965), population size can be estimated within a CJS

modeling context by simply dividing the number of individuals captured by the recapture

probability estimate (Dugger et al. 2004, McDonald et al. 2005 p. 241, see Yackulic et al.

2014, Appendix C for a complex application). However, this approach can lead to population

size estimates that suggest negative recruitment because entry parameters are not included in

the likelihood (Schwarz and Arnason 1996). By modeling both the recruitment and survival

processes, JS approaches provide a means of preventing such inconsistencies. Other options

that do condition on capture, yet are still able to provide inferences on recruitment through

modeling capture histories both forward and backward in time, offer an alternative approach

(Pradel 1996, Link and Barker 2005). These 'reverse-symmetry' models offer an advantage

over JS models in that the recruitment or population growth parameters can be included in the

likelihood and so modeled directly, rather than derived from the survival and population size

parameters (Tenan et al. 2014, Saracco et al. 2020). In addition, because they are based on

applying time-specific multinomial likelihoods to a compact set of sufficient statistics, they

too can be implemented quickly using Bayesian methods. Nevertheless, these reverse-

symmetry models do not allow the same level of flexibility as the multi-state JS models for

handling complexities such as transiency or demographic rates that depend on states that

change over time [e.g., age class or breeding status; Kendall et al. (2019), Hostetter et al.

(2021)]. Finally, while these models can provide inference about population dynamics

parameters, they are largely unable to inform population size (but see Tenan et al. 2019).

Median parameter estimates from our simulation study were very similar between the

discrete latent state and marginalized JS models for the set of parameter values we considered

in our simulations. However, both model implementations showed slight negative bias in

capture probability estimates and positive bias in population size estimates. These biases

were magnified for model runs with random missing data. We suggest that additional study is

needed to better understand the potential effects of missing data, including different amounts

and types of missing data (e.g., random v. consecutive missed years at particular sites), on

inferences across a range of combinations of parameter values. Understanding the

consequences of missing data is especially important for monitoring programs, such as

MAPS, where as much as half the sampling occasions can commonly be missed due to

stations entering and leaving the program over the years.

Credible intervals were wider for the marginalized v. discrete latent state models for the

population size and other parameters derived as deterministic functions of population size.

Nevertheless, these estimates exhibited better coverage compared to the discrete latent state

model or marginalized model with parameters derived from conditional estimates applied to

reconstituted capture histories (Appendix S2). Given the greater speed of implementation,

better coverage, and lack of bias in year-specific population size, recruitment, and population

change estimates, we suggest that this approach appears to be the most generally useful

among those considered here for implementing models and estimating derived parameters.

We described a variation of the basic marginalized multistate JS model to illustrate the

versatility of the basic modeling framework to address a common complication of many

capture-mark-recapture programs that involves the sampling of individuals that are not part

of the target population. This 'transient' version of the marginalized multistate JS model

assumes equal capture probability between residents and transients, which may be unrealistic

in many situations; however, because capture probability is informed here by between-year

recaptures, we suggest that it is unlikely to bias estimates of resident population size. Higher

resident than transient recapture probabilities would nonetheless be expected to result in

underestimates of transient populations and overestimates of the proportion of residents in

populations. Additional within-season data and model development (e.g., Ruiz Gutierrez et

al. 2016) will be required to provide a more complete understanding of resident and transient

components of populations.

The version of the transient JS model that we describe here successfully recovered

parameter values from our simulations, although the same biases in capture probability and

superpopulation estimates seen in the basic JS version were also evident in the transient

model, and there was some evidence in bias in the residency probability parameter as well.

We suggest that additional study is needed to assess how biases may change across different

combinations of parameter values.

While our application to the MAPS Kentucky Warbler data set was much slower than

the simple simulation scenarios we considered, this was not entirely unexpected given the

larger dimensions of the data set (~ 20 x the number of rows representing unique site x

capture histories and > 3 x the number of sampling occasions compared to the simulated

transient model data sets), random effects structure for the survival and capture probability

models, and large number of missed sampling occasions. Even with the longer run time,

reasonable inferences for most parameters were obtained within a few hours, demonstrating

the potential utility of this modeling framework for more complicated real-world examples.

Ideally, study design, objectives, and characteristics of the data set at hand should dictate

possible model applications without having to consider constraints of long implementation

times. We hope that the marginalized versions of the JS model described here will stimulate

additional study and development of this useful class of models and open new potential

applications to large complex data sets.

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Conflict of Interest Statement

The authors declare no conflict of interest.

Author Contributions

J. Saracco and C. Yackulic conceived the ideas and designed methodology; J. Saracco

prepared and analysed the data and led the writing of the manuscript. Both authors

contributed critically to the drafts and gave final approval for publication.

Data Availability

R code and data needed to reproduce results are archived in the Open Science

Framework https://doi.org/10.17605/OSF.IO/Q3458 (Saracco and Yackulic 2023).

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Table 1. 95% credible interval coverage and widths [mean with (SE) below] for the discrete latent state (D), marginalized (M), discrete latent

state with 25% missing data (D.NA), and marginalized with 25% missing data (M.NA) multistate Jolly Seber models applied to 100 simulated

data sets.

	% coverage					Width			
	D	M	D.NA	M.NA		D	M	D.NA	M.NA
N_{super}	90 (3.0)	92 (2.7)	83 (3.8)	87 (3.4)		82.1 (0.9)	99.3 (0.7)	116.4 (1.7)	129 (1.3)
ϕ	94 (2.4)	94 (2.4)	92 (2.7)	91 (2.9)		0.104 (0.000)	0.104 (0.001)	0.132 (0.001)	0.132 (0.001)
b_1	98 (1.4)	98 (1.4)	97 (1.7)	98 (1.4)		0.157 (0.001)	0.157 (0.001)	0.185 (0.001)	0.185 (0.001)
b_2	97 (1.7)	97 (1.7)	97 (1.7)	97 (1.7)		0.010 (0.010)	0.010 (0.010)	0.010 (0.010)	0.010 (0.010)
b_3	96 (2.0)	96 (2.0)	98 (1.4)	97 (1.7)		0.129 (0.001)	0.129 (0.001)	0.154 (0.002)	0.155 (0.002)
b_4	94 (2.4)	94 (2.4)	96 (2.0)	97 (1.7)		0.123 (0.001)	0.124 (0.001)	0.150 (0.002)	0.150 (0.002)
b_5	95 (2.2)	95 (2.2)	96 (2.0)	96 (2.0)		0.122 (0.001)	0.122 (0.001)	0.148 (0.002)	0.148 (0.002)
b_6	95 (2.2)	95 (2.2)	97 (1.7)	97 (1.7)		0.119 (0.001)	0.119 (0.001)	0.146 (0.002)	0.146 (0.002)
b_7	95 (2.2)	95 (2.2)	96 (2.0)	96 (2.0)		0.115 (0.001)	0.115 (0.001)	0.142 (0.002)	0.142 (0.002)
p	93 (2.6)	92 (2.7)	87 (3.4)	89 (3.1)		0.139 (0.001)	0.140 (0.001)	0.183 (0.002)	0.184 (0.002)

Figure 1. Boxplots of posterior medians for adult apparent survival probability, ɸ, entry

probability, b, capture probability, p (a); annual abundance, N_t, and superpopulation

abundance, N_{super}, (b) from discrete (D) and marginalized (M) multistate Jolly Seber models

applied to 100 complete simulated data sets and 100 data sets with 25% missing data. Data-

generating values are indicated with red lines.

Figure 2. Boxplot of the time required to reach 1000 effective samples of the least converged

parameter for discrete (D) and marginalized (M) multistate Jolly Seber models applied to 100

complete simulated data sets and to the same 100 data sets but with 25% of the data randomly

missing.

Figure 3. Boxplots of posterior medians for adult apparent survival probability, residency

probability, entry probability, capture probability (a), and superpopulation size of resident

individuals (b) from a marginalized multistate transient Jolly Seber model applied to 100

simulated data sets. Data-generating values are indicated with red lines. Mean 95% credible

interval coverage of model parameters is shown in (c).

Figure 4. Medians ± 95% credible intervals for annual demographic parameters estimated

for Kentucky warblers banded in the Central Hardwoods Bird Conservation Region as part of

the Monitoring Avian Productivity and Survivorship (MAPS) program.

 Supporting information for: Saracco, J. F. and C. B. Yackulic. Fast and

flexible Bayesian Jolly Seber models and application to populations with

transients

Appendix S1. BUGS/JAGS code for multistate Jolly Seber models.

In our simulation studies, we compared the discrete multistate JS model based on code in Kéry and Schaub (2011), Ch. 10, and compared results to a marginalized version of the same model. Here we provide model code in BUGS language, as implemented in popular software programs such as OpenBUGS (Lunn et al. 2009), JAGS (Plummer 2003), or NIMBLE (de Valpine et al. 2017) for these two model variations. Additional model detail is provided in the main manuscript.

First, priors for survival (ϕ), removal entry (γ), and capture probabilities (p) for both the discrete and marginalized models can be written as:

```
for (t in 1:(n.occasions-1)){
  phi[t] <- mean.phi
  gamma[t] ~ dunif(0, 1)
  p[t] <- mean.p
}

mean.phi ~ dunif(0, 1)
mean.p ~ dunif(0, 1)
```

Note that we follow Kéry and Schaub (2011) and Royle and Dorazio (2012) in parameterizing the recruitment process in terms of the removal entry probabilities, which can be related to the true entry probabilities, b_t, following:

$$b_1 = \gamma_1/\psi \text{ for } t = 1 \text{ and } b_t = \gamma_t \prod_{j=1}^{t-1} \left(1 - \gamma_j\right)/\psi \text{ for } t > 1,$$

where ψ represents the inclusion probability (i.e. probability that a member of the augmented data set is part of the superpopulation). In BUGS language, this can be written as:

```
for (t in 1:(n.occasions-1)){
    qgamma[t] <- 1-gamma[t]
```

```
647        b[t] <- c[t]/psi
648      }
649      for (t in 2:(n.occasions-1)){
650        c[t] <- gamma[t]*prod(qgamma[1:(t-1)])
651      }
652  psi <- sum(c[1:(n.occasions-1)])
653  c[1] <- gamma[1]
```

654   Alternatively, we could define a model for b_t and derive the removal entry probabilities.

655 The b_t could then be modeled as functions of covariates using a multinomial logit model

656 (e.g., see Kéry and Schaub (2012), p. 301) or simply with a Dirichlet prior distribution. For

657 example, as:

```
658    b[1:(n.occasions-1)] ~ ddirich(alpha[1:(n.occasions-1)])
659    psi ~ dunif (0, 1)
660    gamma[1]<-psi*b[1]
661   for (t in 2:n.occasions-1)){
662      gamma[t] <- psi*b[t]/(1-sum(b[1:(t-1)])
663      }
```

664   Second, state transition ($\mathbf{\Omega}$) and observation ($\mathbf{P}$) arrays for both model types can be

665 represented with:

```
666  #---------------------------
667  # States
668  # 1 = not yet entered
669  # 2 = alive
670  # 3 = dead
671
672  # Observations
673  # 1 = captured
674  # 2 = not captured
675  #---------------------------
676
677  # omega tracks probability of state at t+1 given state at t
678     for (t in 1:(n.occasions-1)){
679        omega[1,1,t] <- 1-gamma[t]
```

```
680        omega[1,2,t] <- gamma[t]
681        omega[1,3,t] <- 0
682        omega[2,1,t] <- 0
683        omega[2,2,t] <- phi[t]
684        omega[2,3,t] <- 1-phi[t]
685        omega[3,1,t] <- 0
686        omega[3,2,t] <- 0
687        omega[3,3,t] <- 1
688
689  # rho tracks capture probability at t given state at t
690        rho[1,1,t] <- 0
691        rho[1,2,t] <- 1
692        rho[2,1,t] <- p[t]
693        rho[2,2,t] <- 1 - p[t]
694        rho[3,1,t] <- 0
695        rho[3,2,t] <- 1
696      }
```

Note that Kéry and Schaub (2011) also tracked state and observation probabilities across

a fourth dimension of $\mathbf{\Omega}$ and $\mathbf{P}$ representing individuals. This is unnecessary here, as

parameters do not vary among individuals, and run time in JAGS (Plummer 2003) is

approximately halved by not indexing by individuals. For the discrete latent state model, we

then simulate the state ($s_{i,t}$) and conditional observations ($y_{i,t}$) from categorical distributions

for all $i = 1, \ldots, M$ individuals at each time step:

```
703    for (i in 1:M){
704      s[i,1] ~ dcat(1)
705      for (t in 2:n.occasions){
706        s[i,t] ~ dcat(omega[s[i,t-1],1:3,t-1])
707        y[i,t] ~ dcat(rho[s[i,t],1:2,t-1])
708      }
709    }
```

Note that the indexing for rho[,,t-1] here refers to capture probabilities at time t.

For the marginalized model, we loop through the $i = 1, \ldots, MS$ unique capture histories

to track probabilities of state transitions and observations. Contributions of each unique

capture history likelihood to the overall likelihood were determined in the BUGS model

using the modified "ones trick" described by Yackulic et al. (2020), whereby capture history

frequencies are provided as data for both the frequency response variable fr and the number

of trials FR in binomial distributions with success probabilities defined by the likelihoods:

```
717   for (i in 1:MS){
718     zeta[i,1,1] <- 1  # all individuals unrecruited at first dummy
719 occasion
720     zeta[i,1,2] <- 0
721     zeta[i,1,3] <- 0
722
723     for (t in 2:n.occasions){
724       zeta[i,t,1] <- inprod(zeta[i,(t-1),1:3], omega[1:3,1,(t-1)] *
725 rho[1,ys[i,t],(t-1)])
726       zeta[i,t,2] <- inprod(zeta[i,(t-1),1:3], omega[1:3,2,(t-1)] *
727 rho[2,ys[i,t],(t-1)])
728       zeta[i,t,3] <- inprod(zeta[i,(t-1),1:3], omega[1:3,3,(t-1)] *
729 rho[3,ys[i,t],(t-1)])
730     }
731     lik[i] <- sum(zeta[i,n.occasions,1:3])
732     fr[i] ~ dbin(lik[i], FR[i])
733   }
```

734   For the discrete latent state model we can then derive secondary parameters from first-

735 order states following:

```
736 for (i in 1:M){
737   for (t in 2:n.occasions){
738     al[i,t-1] <- equals(s[i,t],2)
739     } # t
740   for (t in 1:(n.occasions-1)){
741     d[i,t] <- equals(s[i,t]-al[i,t],0)
742     } #t
743   alive[i] <- sum(al[i,])
744   } # i
745
```

```
for (t in 1:(n.occasions-1)){
  N[t] <- sum(al[,t])        # population size
  B[t] <- sum(d[,t])         # number of entries. Note that indexing in
paper
                             # goes from 0 (initial entry) to T
(n.occasions - 1)
  } # t
for (i in 1:M){
  w[i] <- 1-equals(alive[i],0) # w[i] = 1 if individual i ever entered
the
                                # population and 0 otherwise
  } # i
for(t in 1:(n.occasions-2)){
  lambda[t] <- N[t+1]/N[t] # population growth rate
  f[t] <- B[t+1]/N[t] # recruitment (per capita entry) rate. Could also be
                     # calculated as lambda[t] - phi[t]
} # t
Nsuper <- sum(w[]) # could also be calculated with sum(B[])
```

For the marginalized models, we can derive secondary parameters as functions of model parameters and first-order states:

```
for (t in 1:(n.occasions-1)){
  qgamma[t] <- 1-gamma[t]
} # t
c[1] <- gamma[1]
N[1] <- B[1]
for (t in 2:(n.occasions-1)){
  c[t] <- gamma[t] * prod(qgamma[1:(t-1)])
  N[t] <- B[t] + phi[t] * N[t-1]
} # t
psi <- sum(c[1:(n.occasions-1)])    # inclusion probability
for (t in 1:(n.occasions-1)){
  b[t] <- c[t] / psi      # entry probability
  B[t] <- c[t]*M          # number of entries
} # t
```

```
781    for(t in 1:(n.occasions-2)){
782    lambda[t] <- N[t+1]/N[t] # population growth rate
783    f[t] <- B[t+1]/N[t]      # recruitment (per capita entry) rate
784    } # t
785
786    Nsuper <- sum(B[1:(n.occasions-1)]) # superpopulation size
```

Missing data models

While the code for the discrete latent state model does not change with missing data (which are just entered as "NA" values), the marginalized models require the following modifications. First, for capture probability we add an index for unique capture history and multiply by an indicator variable, $op.ind_{i,t}$ denoting whether the individuals represented by that capture history were observable ($op.ind_{i,t} = 1$) or not ($op.ind_{i,t} = 0$) during that time period:

```
for (t in 1:(n.occasions-1)){
```

⋮

```
    for (i in 1:MS){
    p[i,t] <- mean.p*op.ind[i,t] # op.ind: 1 = effort, 0 = no effort
    }
```

⋮

```
}
```

Second, for **P** we need to add a fourth dimension for the capture probability array:

```
for (t in 1:(n.occasions-1)){
```

⋮

```
    for (i in 1:MS){
    rho[1,1,t,i] <- 0
    rho[1,2,t,i] <- 1
    rho[2,1,t,i] <- p[i,t]
    rho[2,2,t,i] <- 1 - p[i,t]
```

```
806        rho[3,1,t,i] <- 0
807        rho[3,2,t,i] <- 1
808        }
809     }
```

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Supporting information for: Saracco, J. and C. B. Yackulic. Efficient and
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Appendix S2. Variations of multistate Jolly Seber models and methods for estimating
derived quantities

We investigated four methods for estimating derived secondary parameters but
reported only the first two approaches in the manuscript. These methods include:

1) Estimating parameters using model "d", the discrete latent state model
presented in the manuscript. In this approach derived parameters are calculated
directly from the posteriors of first-order states.

2) Estimating parameters using model "m1", the marginalized model presented in
the manuscript. In this approach derived parameters are calculated as functions
of modeled parameters (see main manuscript and Appendix S1 for details).

3) Estimating parameters using model "m2", which was not presented in the
manuscript, but is identical to m1 except for in how derived parameters are
estimated. In this approach, N_{super} is calculated by estimating the number of
unobserved individuals by drawing from a binomial distribution using the
probability of inclusion and the number of augmented individuals and this
estimate of unobserved individuals is added to the known number of observed
individuals. Other derived parameters are calculated by determining the full
conditional estimates of different underlying dynamics based on the observed
capture history and simulating feasible true recruit and death timing based on
their relative likelihood based on an observed capture history.

4) Estimating parameters using model "m3," which was not presented in the
manuscript, but is identical to m1 except for in how derived parameters are
estimated. In this approach, N_{super} is calculated using the same approach as
"m2". N_t is derived by calculating forward-conditional probabilities for each
individual and time period and using a series of Bernoulli trials to determine the
expected number of alive individuals. B's are calculated as functions of modelled
parameters as in "m1".

We compared these four methods with respect to speed, coverage, and precision of
estimates of derived parameters based on 100 simulated data sets. Below we share
annotated code, as well as figures based on these simulations.

Credible interval coverage for the year-specific abundance estimates, N_t was relatively
low for the discrete latent state model and especially the marginalized model m2 (Table
S1). Credible interval coverage was highest and generally above the nominal 95% level
for model m1, although this likely reflects the broader credible intervals for that model.
For model m2, N_t estimates were biased high for time periods 3-7 (Fig. S1). Model m1
was fastest, but all of the marginalized models were relatively fast compared to model d
(Fig. S2).

Table S1. *95% credible interval coverage and widths [mean (sd)] for discrete (d) and marginalized (m1, m2, and m3) JS models applied to 100 simulated data sets that differed with respect to how abundance (N), population change, and recruitment are estimated.*

	d		m1		m2		m3	
	% coverage	Width	% coverage	Width	% coverage	Width	% coverage	Width
N_{super}	90.0	80.4	93.0	97.0	89.0	80.7	90.0	77.2
	(30.2)	(11.4)	(25.6)	(8.5)	(31.4)	(10.6)	(30.2)	(9.7)
N_1	65.0	68.4	72.0	81.5	85.0	55.1	63.0	74.6
	(47.9)	(9.1)	(45.1)	(8.6)	(35.9)	(6.4)	(48.5)	(11.4)
N_2	72.0	54.7	85.0	67.3	60.0	50.7	77.0	57.5
	(45.1)	(7.4)	(35.9)	(6.8)	(49.2)	(5.8)	(42.3)	(9.0)
N_3	79.0	51.2	90.0	63.7	54.0	51.5	85.0	57.1
	(40.9)	(7.0)	(30.2)	(6.5)	(50.1)	(5.6)	(35.9)	(8.2)
N_4	85.0	50.0	93.0	63.6	48.0	53.6	88.0	57.7
	(35.9)	(6.6)	(25.6)	(6.1)	(50.2)	(5.7)	(32.7)	(7.8)
N_5	85.0	50.2	95.0	64.0	52.0	55.3	88.0	57.7
	(35.9)	(7.2)	(21.9)	(6.5)	(50.2)	(6.6)	(32.7)	(9.1)
N_6	91.0	52.0	98.0	65.4	65.0	57.2	91.0	57.7
	(28.8)	(7.1)	(14.1)	(6.6)	(47.9)	(7.0)	(28.8)	(8.6)
N_7	90.0	56.1	93.0	67.2	86.0	64.4	89.0	56.6
	(30.2)	(7.9)	(25.6)	(7.6)	(34.9)	(9.6)	(31.4)	(8.3)
λ_1	84.0	0.403	89.0	0.451	87.0	0.406	79.0	0.429

	d		m1		m2		m3	
	% coverage	Width	% coverage	Width	% coverage	Width	% coverage	Width
	(36.8)	(0.078)	(31.4)	(0.098)	(33.8)	(0.072)	(40.9)	(0.087)
λ_2	90.0	0.367	92.0	0.410	88.0	0.314	84.0	0.412
	(30.2)	(0.057)	(27.3)	(0.071)	(32.7)	(0.042)	(36.8)	(0.063)
λ_3	93.0	0.353	95.0	0.392	90.0	0.281	93.0	0.401
	(25.6)	(0.043)	(21.9)	(0.051)	(30.2)	(0.029)	(25.6)	(0.047)
λ_4	87.0	0.339	91.0	0.374	87.0	0.260	90.0	0.386
	(33.8)	(0.050)	(28.8)	(0.060)	(33.8)	(0.029)	(30.2)	(0.055)
λ_5	88.0	0.343	90.0	0.376	80.0	0.253	88.0	0.390
	(32.7)	(0.051)	(30.2)	(0.062)	(40.2)	(0.026)	(32.7)	(0.058)
λ_6	89.0	0.354	92.0	0.385	85.0	0.268	87.0	0.390
	(31.4)	(0.048)	(27.3)	(0.061)	(35.9)	(0.025)	(33.8)	(0.052)
f_1	85.0	0.416	91.0	0.458	90.0	0.445	78.0	0.445
	(35.9)	(0.086)	(28.8)	(0.103)	(30.2)	(0.080)	(41.6)	(0.137)
f_2	90.0	0.369	93.0	0.414	89.0	0.342	88.0	0.433
	(30.2)	(0.059)	(25.6)	(0.074)	(31.4)	(0.045)	(32.7)	(0.083)

	d		m1		m2		m3	
	% coverage	Width	% coverage	Width	% coverage	Width	% coverage	Width
f_3	93.0	0.349	97.0	0.397	89.0	0.307	92.0	0.418
	(25.6)	(0.044)	(17.1)	(0.053)	(31.4)	(0.032)	(27.3)	(0.058)
f_4	88.0	0.332	92.0	0.379	85.0	0.290	89.0	0.393
	(32.7)	(0.052)	(27.3)	(0.065)	(35.9)	(0.036)	(31.4)	(0.074)
f_5	87.0	0.333	92.0	0.383	85.0	0.302	88.0	0.393
	(33.8)	(0.053)	(27.3)	(0.066)	(35.9)	(0.038)	(32.7)	(0.073)
f_6	90.0	0.342	92.0	0.393	86.0	0.326	89.0	0.392
	(30.2)	(0.051)	(27.3)	(0.064)	(34.9)	(0.034)	(31.4)	(0.063)

Figure S1. *Boxplots of posterior medians of derived parameters from discrete (d) and marginalized (m1, m2, m3) multistate Jolly Seber models applied to 100 simulated data sets. Abundance estimates are shown in (a; note right y-axis shows scale for N_{super}); population change in (b) and recruitment in (c). Data-generating values are indicated with red lines.*

879 ***Figure S2***. *Boxplot of the time required to reach 1000 effective samples of the least*
880 *converged parameter for discrete (d) and marginalized (m1, m2, and m3) multistate Jolly*
881 *Seber models applied to 100 complete simulated data sets.*

883 R and JAGS code for writing model files, simulating data, running models, and extracting
884 results, are as follows:

```
885 #------------------------------------------------------------------------
886 ---# Write models to files

887 # 1. Discrete latent state model (d)
888 {
889 sink("js-ms-d.txt")
890 cat("
891 model {

892
893 #-------------------------------------
894 # phi: survival probability
895 # gamma: removal entry probability
896 # p: capture probability
897 #-------------------------------------

898
899 # Priors and constraints
900 for (t in 1:(n.occasions-1)){
901    phi[t] <- mean.phi      # Constant survival
902    gamma[t] ~ dunif(0,1)  # Time-dependent entry
903    p[t] <- mean.p          # Constant capture probability
904    }

905
906 mean.phi ~ dunif(0,1)    # Prior for mean survival
907 mean.p ~ dunif(0,1)      # Prior for mean capture
```

```
908
909    #-------------------------------------
910    # States (S):
911    # 1 not yet entered
912    # 2 alive
913    # 3 dead
914    #-------------------------------------
915
916    # Probabilities of state S(t+1) given S(t)
917       for (t in 1:(n.occasions-1)){
918          omega[1,1,t] <- 1-gamma[t]
919          omega[1,2,t] <- gamma[t]
920          omega[1,3,t] <- 0
921          omega[2,1,t] <- 0
922          omega[2,2,t] <- phi[t]
923          omega[2,3,t] <- 1-phi[t]
924          omega[3,1,t] <- 0
925          omega[3,2,t] <- 0
926          omega[3,3,t] <- 1
927
928    #-------------------------------------
929    # Observations (O):
930    # 1 captured
931    # 2 not captured
932    #-------------------------------------
933
934    # Probabilities of O(t) given S(t)
935          rho[1,1,t] <- 0
936          rho[1,2,t] <- 1
937          rho[2,1,t] <- p[t]
938          rho[2,2,t] <- 1-p[t]
939          rho[3,1,t] <- 0
940          rho[3,2,t] <- 1
941          } #t
942
943    # Likelihood
944    for (i in 1:M){
945       # Define latent state at first occasion
946       s[i,1] ~ dcat(1)    # Make sure that all M individuals are in state 1 at
947    t=1
948       for (t in 2:n.occasions){
949          # State process: draw S(t) given S(t-1)
950          s[i,t] ~ dcat(omega[s[i,t-1],,t-1])
951          # Observation process: draw O(t) given S(t)
952          y[i,t] ~ dcat(rho[s[i,t],,t-1])
953          } #t
954       } #i
955
956    # Derived population parameters
957    for (t in 1:(n.occasions-1)){
958       qgamma[t] <- 1-gamma[t]
959       }
960    c[1] <- gamma[1]
```

```r
961   for (t in 2:(n.occasions-1)){
962      c[t] <- gamma[t] * prod(qgamma[1:(t-1)])
963      } # t
964   psi <- sum(c[1:(n.occasions-1)])          # inclusion probability
965   for (t in 1:(n.occasions-1)){
966      b[t] <- c[t] / psi      # entry probability
967      } # t
968
969   for (i in 1:M){
970      for (t in 2:n.occasions){
971         al[i,t-1] <- equals(s[i,t],2)
972         } # t
973      for (t in 1:(n.occasions-1)){
974         d[i,t] <- equals(s[i,t]-al[i,t],0)
975         } #t
976      alive[i] <- sum(al[i,])
977      } # i
978
979   for (t in 1:(n.occasions-1)){
980      N[t] <- sum(al[,t])        # population size
981      B[t] <- sum(d[,t])         # number of entries
982      } # t
983   for (i in 1:M){
984      w[i] <- 1-equals(alive[i],0)
985      } # i
986   for(t in 1:(n.occasions-2)){
987     lambda[t] <- N[t+1]/N[t] # population growth rate
988     f1[t] <- B[t+1]/N[t] # recruitment rate
989     f2[t] <- lambda[t] - phi[t]
990   } # t
991   Nsuper <- sum(w[])            # superpopulation size
992   }
993   ",fill = TRUE)
994   sink()
995
996
997   # 2. Marginalized multistate Jolly Seber model - derived parameters (m1)
998
999   sink("js-ms-m1.txt")
1000  cat("
1001
1002  model{
1003
1004    # Priors and constraints
1005    for (t in 1:(n.occasions-1)){
1006      phi[t] <- mean.phi     # Constant survival
1007      gamma[t] ~ dunif(0,1)  # Time-dependent entry probabilities
1008      p[t] <- mean.p         # Constant capture probability
1009    }
1010
1011    mean.phi ~ dunif(0,1)    # Prior for mean survival
1012    mean.p ~ dunif(0,1)      # Prior for mean capture
1013
```

```
1014      for (t in 1:(n.occasions-1)){
1015
1016        #---------------------------------------------------------
1017        # states (S)
1018        # 1 = not yet entered
1019        # 2 = alive
1020        # 3 = dead
1021        #---------------------------------------------------------
1022
1023        # Probabilities of state S(t+1) given S(t)
1024          omega[1,1,t] <- 1-gamma[t]
1025          omega[1,2,t] <- gamma[t]
1026          omega[1,3,t] <- 0
1027          omega[2,1,t] <- 0
1028          omega[2,2,t] <- phi[t]
1029          omega[2,3,t] <- 1-phi[t]
1030          omega[3,1,t] <- 0
1031          omega[3,2,t] <- 0
1032          omega[3,3,t] <- 1
1033
1034        #---------------------------------------------------------
1035        # observations (O)
1036        # 1 = captured
1037        # 2 = not captured
1038        #---------------------------------------------------------
1039
1040        # Probabilities of O(t) given S(t)
1041          rho[1,1,t] <- 0
1042          rho[1,2,t] <- 1
1043          rho[2,1,t] <- p[t]
1044          rho[2,2,t] <- 1 - p[t]
1045          rho[3,1,t] <- 0
1046          rho[3,2,t] <- 1
1047
1048      } # t
1049
1050      # Likelihood
1051      for (i in 1:MS){
1052        # Define latent state at first occasion
1053        zeta[i,1,1] <- 1   # Set all individuals to state 1 (not yet entered)
1054  at t=1
1055        zeta[i,1,2] <- 0
1056        zeta[i,1,3] <- 0
1057
1058        for (t in 2:(n.occasions)){
1059          # State process: draw S(t+1) given S(t)
1060          zeta[i,t,1] <- inprod(zeta[i,(t-1),1:3], omega[1:3,1,(t-1)] *
1061          rho[1,ys[i,t],(t-1)])
1062          zeta[i,t,2] <- inprod(zeta[i,(t-1),1:3], omega[1:3,2,(t-1)] *
1063          rho[2,ys[i,t],(t-1)])
1064          zeta[i,t,3] <- inprod(zeta[i,(t-1),1:3], omega[1:3,3,(t-1)] *
1065          rho[3,ys[i,t],(t-1)])
1066        } # t
```

```
1067        lik[i] <- sum(zeta[i,(n.occasions),1:3])
1068        fr[i] ~ dbin(lik[i], FR[i])
1069      } # i
1070
1071      # Calculate derived population parameters
1072      for (t in 1:(n.occasions-1)){
1073        qgamma[t] <- 1-gamma[t]
1074      } # t
1075      c[1] <- gamma[1]
1076      N[1] <- B[1]
1077      for (t in 2:(n.occasions-1)){
1078        c[t] <- gamma[t] * prod(qgamma[1:(t-1)])
1079        N[t] <- B[t] + phi[t] * N[t-1]
1080      } # t
1081      psi <- sum(c[1:(n.occasions-1)])    # inclusion probability
1082      for (t in 1:(n.occasions-1)){
1083        b[t] <- c[t] / psi      # entry probability
1084        B[t] <- c[t]*M        # number of entries
1085      } # t
1086
1087      for(t in 1:(n.occasions-2)){
1088      lambda[t] <- N[t+1]/N[t] # population growth rate
1089      f1[t] <- B[t+1]/N[t] # recruitment rate
1090      f2[t] <- lambda[t] - phi[t]
1091      } # t
1092
1093      Nsuper <- sum(B[1:(n.occasions-1)]) # superpopulation size
1094    }
1095
1096    ",fill=TRUE)
1097    sink()
1098
1099    # 3. Marginalized multistate Jolly Seber model - simulated N and B (m2)
1100
1101    sink("js-ms-m2.txt")
1102    cat("
1103    model{
1104
1105      # Priors and constraints
1106      for (t in 1:(n.occasions-1)){
1107        phi[t] <- mean.phi     # Constant survival
1108        gamma[t] ~ dunif(0,1)  # Time-dependent entry probabilities
1109        p[t] <- mean.p         # Constant capture probability
1110      }
1111
1112      mean.phi ~ dunif(0,1)    # Prior for mean survival
1113      mean.p ~ dunif(0,1)      # Prior for mean capture
1114
1115      for (t in 1:(n.occasions-1)){
1116
1117      #---------------------------------------------------------
1118      # states (S)
1119      # 1 = not yet entered
```

```
1120      # 2 = alive
1121      # 3 = dead
1122      #------------------------------------------------------------
1123
1124      # Probabilities of state S(t+1) given S(t)
1125        omega[1,1,t] <- 1-gamma[t]
1126        omega[1,2,t] <- gamma[t]
1127        omega[1,3,t] <- 0
1128        omega[2,1,t] <- 0
1129        omega[2,2,t] <- phi[t]
1130        omega[2,3,t] <- 1-phi[t]
1131        omega[3,1,t] <- 0
1132        omega[3,2,t] <- 0
1133        omega[3,3,t] <- 1
1134
1135      #------------------------------------------------------------
1136      # observations (O)
1137      # 1 = captured
1138      # 2 = not captured
1139      #------------------------------------------------------------
1140
1141      # Probabilities of O(t) given S(t)
1142        rho[1,1,t] <- 0
1143        rho[1,2,t] <- 1
1144        rho[2,1,t] <- p[t]
1145        rho[2,2,t] <- 1 - p[t]
1146        rho[3,1,t] <- 0
1147        rho[3,2,t] <- 1
1148
1149      } # t
1150
1151      # Likelihood
1152      for (i in 1:MS){
1153        # Define latent state at first occasion
1154        zeta[i,1,1] <- 1   # Set all individuals to state 1 (not yet entered)
1155   at t=1
1156        zeta[i,1,2] <- 0
1157        zeta[i,1,3] <- 0
1158
1159        for (t in 2:(n.occasions)){
1160          # State process: draw S(t+1) given S(t)
1161          zeta[i,t,1] <- inprod(zeta[i,(t-1),1:3], omega[1:3,1,(t-1)] *
1162          rho[1,ys[i,t],(t-1)])
1163          zeta[i,t,2] <- inprod(zeta[i,(t-1),1:3], omega[1:3,2,(t-1)] *
1164          rho[2,ys[i,t],(t-1)])
1165          zeta[i,t,3] <- inprod(zeta[i,(t-1),1:3], omega[1:3,3,(t-1)] *
1166          rho[3,ys[i,t],(t-1)])
1167        } # t
1168        lik[i] <- sum(zeta[i,(n.occasions),1:3])
1169        fr[i] ~ dbin(lik[i], FR[i])
1170      } # i
1171
1172      # Calculate derived population parameters
```

```
1173      for (t in 1:(n.occasions-1)){
1174        qgamma[t] <- 1-gamma[t]
1175      } # t
1176      c[1] <- gamma[1]
1177      for (t in 2:(n.occasions-1)){
1178        c[t] <- gamma[t] * prod(qgamma[1:(t-1)])
1179      } # t
1180      psi <- sum(c[1:(n.occasions-1)])     # inclusion probability
1181      for (t in 1:(n.occasions-1)){
1182        b[t] <- c[t] / psi                 # entry probability
1183      } # t
1184
1185      p0_inc<-sum(zeta[MS,n.occasions,2:3])/sum(zeta[MS,n.occasions,1:3])
1186      U ~ dbin(p0_inc,FR[MS]) #assumes empty CH is always the last one
1187      Nsuper <- sum(FR[1:(MS-1)])+U # superpopulation size
1188
1189   # This loop calculates the likelihood that an individual recruits during
1190   time
1191   # step poss[i,1], dies during time step poss[i,2] and is never seen while
1192   alive
1193
1194   for (i in 1:nposs){
1195       lik0[i]<-omega[1,2,poss[i,1]]*((1-equals(poss[i,2],(n.occasions-1)))*
1196
1197   (prod(rho[2,2,poss[i,1]:poss[i,2]])*prod(omega[2,2,poss[i,1]:(n.occasions-
1198   1)]))*
1199       (omega[2,3,poss[i,2]])/prod(omega[2,2,(poss[i,2]):(n.occasions-1)]))+
1200           (equals(poss[i,2],(n.occasions-
1201   1)))*(prod(rho[2,2,poss[i,1]:poss[i,2]])
1202           *prod(omega[2,2,poss[i,1]:(n.occasions-
1203   1)])/prod(omega[2,2,poss[i,2]:(n.occasions-1)])))
1204   }
1205
1206   # The next set of loops determines for each individual (linked to
1207   summarized
1208   # capture history by lookup) determine if an underlying set of underlying
1209   dynamics
1210   # (i.e., recruit and death period) is possible given their capture history
1211
1212   for (i in 1:Nobs_ind){
1213       for (j in 1:(n.occasions-1)){
1214           for (k in 1:nposs){
1215               inc_a[i,j,k]<-
1216   equals(poss[k,1],j)*equals(poss_obs[k,lookup[i]],1)
1217               inc_l[i,j,k]<-
1218   equals(poss[k,2],j)*equals(poss_obs[k,lookup[i]],1)
1219               }
1220           p_a[i,j]<-inprod(inc_a[i,j,1:nposs],lik0[1:nposs])
1221           p_l[i,j]<-inprod(inc_l[i,j,1:nposs],lik0[1:nposs])
1222           }
1223       ar[i]~dcat(p_a[i,])
1224       li[i]~dcat(p_l[i,])
1225       A[i]<-ar[i]
```

```
1226        L[i]<-li[i]
1227        for (j in 1:(n.occasions-1)){
1228            S[i,j]<-step(j-A[i])*step(L[i]-j)
1229            }
1230    }
1231
1232    # The next set of loops determines the likelihood of an underlying set of
1233    # underlying dynamics (i.e., recruit and death period) given an individual
1234    # was never seen.
1235
1236    for (j in 1:(n.occasions-1)){
1237        for (k in 1:nposs){
1238            inc_a_no[j,k]<-equals(poss[k,1],j)
1239            inc_l_no[j,k]<-equals(poss[k,2],j)
1240            }
1241        p_a_no[j]<-inprod(inc_a_no[j,1:nposs],lik0[1:nposs])
1242        p_l_no[j]<-inprod(inc_l_no[j,1:nposs],lik0[1:nposs])
1243        }
1244
1245    for (i in (Nobs_ind+1):(Npos_ind)){
1246        ar[i]~dcat(p_a_no)
1247        li[i]~dcat(p_l_no)
1248        A[i]<-ar[i]*step(Nobs_ind+U-i)
1249        L[i]<-li[i]*step(Nobs_ind+U-i)
1250        for (j in 1:(n.occasions-1)){
1251            S[i,j]<-step(j-A[i])*step(L[i]-j)
1252            }
1253        }
1254
1255    for (t in 1:(n.occasions-1)){
1256      B[t] <- sum(equals(A[1:(Npos_ind)],t)) # number of entries
1257      N[t] <- sum(S[1:(Npos_ind),t])
1258      } # t
1259      for(t in 1:(n.occasions-2)){
1260      lambda[t] <- N[t+1]/N[t] # population growth rate
1261      f1[t] <- B[t+1]/N[t]# recruitment rate
1262      f2[t] <- lambda[t] - phi[t]
1263      } # t
1264     }
1265        ", fill =TRUE)
1266    sink()
1267
1268    # 3. Marginalized multistate Jolly Seber model - simulated N, not B (m3)
1269
1270    sink("js-ms-m3.txt")
1271    cat("
1272    model{
1273
1274      # Priors and constraints
1275      for (t in 1:(n.occasions-1)){
1276        phi[t] <- mean.phi      # Constant survival
1277        gamma[t] ~ dbeta(1/(n.occasions-1), 2-t/(n.occasions-1)) # Time-
1278    dependent entry probabilities
```

```
1279        p[t] <- mean.p          # Constant capture probability
1280      }
1281
1282    mean.phi ~ dunif(0,1)     # Prior for mean survival
1283    mean.p ~ dunif(0,1)       # Prior for mean capture
1284
1285    for (t in 1:(n.occasions-1)){
1286
1287      #---------------------------------------------------------
1288      # states (S)
1289      # 1 = not yet entered
1290      # 2 = alive
1291      # 3 = dead
1292      #---------------------------------------------------------
1293
1294      # Probabilities of state S(t+1) given S(t)
1295        omega[1,1,t] <- 1-gamma[t]
1296        omega[1,2,t] <- gamma[t]
1297        omega[1,3,t] <- 0
1298        omega[2,1,t] <- 0
1299        omega[2,2,t] <- phi[t]
1300        omega[2,3,t] <- 1-phi[t]
1301        omega[3,1,t] <- 0
1302        omega[3,2,t] <- 0
1303        omega[3,3,t] <- 1
1304
1305      #---------------------------------------------------------
1306      # observations (O)
1307      # 1 = captured
1308      # 2 = not captured
1309      #---------------------------------------------------------
1310
1311      # Probabilities of O(t) given S(t)
1312        rho[1,1,t] <- 0
1313        rho[1,2,t] <- 1
1314        rho[2,1,t] <- p[t]
1315        rho[2,2,t] <- 1 - p[t]
1316        rho[3,1,t] <- 0
1317        rho[3,2,t] <- 1
1318
1319    } # t
1320
1321    # Likelihood
1322    for (i in 1:MS){
1323      # Define latent state at first occasion
1324      zeta[i,1,1] <- 1   # Set all individuals to state 1 (not yet entered)
1325 at t=1
1326      zeta[i,1,2] <- 0
1327      zeta[i,1,3] <- 0
1328
1329      for (t in 2:(n.occasions)){
1330        zeta[i,t,1] <- inprod(zeta[i,(t-1),1:3], omega[1:3,1,(t-1)] *
1331        rho[1,ys[i,t],(t-1)])
```

```
1332        zeta[i,t,2] <- inprod(zeta[i,(t-1),1:3], omega[1:3,2,(t-1)] *
1333          rho[2,ys[i,t],(t-1)])
1334        zeta[i,t,3] <- inprod(zeta[i,(t-1),1:3], omega[1:3,3,(t-1)] *
1335          rho[3,ys[i,t],(t-1)])
1336      } # t
1337      lik[i] <- sum(zeta[i,(n.occasions),1:3])
1338      fr[i] ~ dbin(lik[i], FR[i])
1339    } # i
1340
1341    # Calculate derived population parameters
1342    for (t in 1:(n.occasions-1)){
1343      qgamma[t] <- 1-gamma[t]
1344    } # t
1345    c[1] <- gamma[1]
1346    for (t in 2:(n.occasions-1)){
1347      c[t] <- gamma[t] * prod(qgamma[1:(t-1)])
1348    } # t
1349    psi <- sum(c[1:(n.occasions-1)])    # inclusion probability
1350    for (t in 1:(n.occasions-1)){
1351      b[t] <- c[t] / psi              # entry probability
1352      B[t] <- c[t]*M
1353    } # t
1354
1355    p0_inc<-sum(zeta[MS,n.occasions,2:3])/sum(zeta[MS,n.occasions,1:3])
1356    U ~ dbin(p0_inc,FR[MS]) #assumes empty CH is always the last one
1357    Nsuper <- sum(FR[1:(MS-1)])+U # superpopulation size
1358
1359    for (i in 1:M){
1360    # Simulations need to be done for individuals even though zeta can be
1361  calculated
1362    # for summarized capture histories. lookup refers each individual in M,
1363  to the
1364    # appropriate summarized capture history.
1365    for (t in 2:(n.occasions)){
1366    al[i,t-1] ~ dbern(zeta[lookup[i],t,2]/sum(zeta[lookup[i],t,1:3]))
1367    } # t
1368    } # i
1369
1370    for (t in 1:(n.occasions-1)){
1371    N[t] <- sum(al[1:M,t]) # population size
1372    } # t
1373
1374    for(t in 1:(n.occasions-2)){
1375    lambda[t] <- N[t+1]/N[t] # population growth rate
1376
1377    f1[t] <- B[t+1]/N[t]# recruitment rate
1378    f2[t] <- lambda[t] - phi[t] # recruitment rate
1379    } # t
1380  }
1381      ", fill =TRUE)
1382  sink()
1383  }
```

```r
# some functions ----------------------------------------------------
---

# Simulate capture histories (from Kery and Schaub 2011)

simul.js <- function(PHI, P, b, Nsuper){
  B <- rmultinom(1, Nsuper, b) # Generate no. of entering ind. per
occasion
  n.occasions <- dim(PHI)[2] + 1
  CH.sur <- CH.p <- matrix(0, ncol = n.occasions, nrow = Nsuper)
  # Define a vector with the occasion of entering the population
  ent.occ <- numeric()
  for (t in 1:n.occasions){
    ent.occ <- c(ent.occ, rep(t, B[t]))
  }
  # Simulating survival
  for (i in 1:Nsuper){
    CH.sur[i, ent.occ[i]] <- 1   # Write 1 when ind. enters the pop.
    if (ent.occ[i] == n.occasions) next
    for (t in (ent.occ[i]+1):n.occasions){
      # Bernoulli trial: has individual survived occasion?
      sur <- rbinom(1, 1, PHI[i,t-1])
      ifelse (sur==1, CH.sur[i,t] <- 1, break)
    } #t
  } #i
  # Simulating capture
  for (i in 1:Nsuper){
    CH.p[i,] <- rbinom(n.occasions, 1, P[i,])
  } #i
  # Full capture-recapture matrix
  CH <- CH.sur * CH.p

  # Remove individuals never captured
  cap.sum <- rowSums(CH)
  never <- which(cap.sum == 0)
  CH <- CH[-never,]
  Nt <- colSums(CH.sur)    # Actual population size
  return(list(CH=CH, B=B, Nsuper=Nt))
}

# Collapse capture histories (from Yackulic et al. 2020)
collapse.ch <- function(ch){
  ch.char = apply(ch, 1, function(x) paste(x, collapse = ","))

  ch.sum.out = t(sapply(strsplit(names(table(ch.char)), split = ","),
                        as.numeric))
  fr.out = as.numeric(as.vector(table(ch.char)))

  return(list(ch.sum.out, fr.out))
}
```

```
1437  #--------------------------------------------------------------------
1438  ---
1439
1440  library(jagsUI)
1441  library(dplyr)
1442  ##
1443  ## Attaching package: 'dplyr'
1444  ## The following objects are masked from 'package:stats':
1445  ##
1446  ##      filter, lag
1447  ## The following objects are masked from 'package:base':
1448  ##
1449  ##      intersect, setdiff, setequal, union
1450  library(data.table)
1451  ##
1452  ## Attaching package: 'data.table'
1453  ## The following objects are masked from 'package:dplyr':
1454  ##
1455  ##      between, first, last
1456  # some functions -------------------------------------------------------
1457  ------
1458
1459  # Simulate capture histories (from Kery and Schaub 2011)
1460
1461  simul.js <- function(PHI, P, b, Nsuper){
1462    B <- rmultinom(1, Nsuper, b) # Generate no. of entering ind. per
1463  occasion
1464    n.occasions <- dim(PHI)[2] + 1
1465    CH.sur <- CH.p <- matrix(0, ncol = n.occasions, nrow = Nsuper)
1466    # Define a vector with the occasion of entering the population
1467    ent.occ <- numeric()
1468    for (t in 1:n.occasions){
1469      ent.occ <- c(ent.occ, rep(t, B[t]))
1470    }
1471    # Simulating survival
1472    for (i in 1:Nsuper){
1473      CH.sur[i, ent.occ[i]] <- 1   # Write 1 when ind. enters the pop.
1474      if (ent.occ[i] == n.occasions) next
1475      for (t in (ent.occ[i]+1):n.occasions){
1476        # Bernoulli trial: has individual survived occasion?
1477        sur <- rbinom(1, 1, PHI[i,t-1])
1478        ifelse (sur==1, CH.sur[i,t] <- 1, break)
1479      } #t
1480    } #i
1481    # Simulating capture
1482    for (i in 1:Nsuper){
1483      CH.p[i,] <- rbinom(n.occasions, 1, P[i,])
1484    } #i
```

```
1485    # Full capture-recapture matrix
1486    CH <- CH.sur * CH.p
1487
1488    # Remove individuals never captured
1489    cap.sum <- rowSums(CH)
1490    never <- which(cap.sum == 0)
1491    CH <- CH[-never,]
1492    Nt <- colSums(CH.sur)    # Actual population size
1493    return(list(CH=CH, B=B, Nsuper=Nt))
1494  }
1495
1496
1497  # Fill in initial values for s. Set to 1 (not entered) for all occasions
1498  prior to
1499  # first capture, 2 for occasions from first to last capture, and 3 for
1500  occasions
1501  # after last capture (from Kery and Schaub 2011).
1502
1503  js.multistate.init <- function(ch, ns){
1504    ch[ch==2] <- NA
1505    state <- ch
1506    for (i in 1:nrow(ch)){
1507      n1 <- min(which(ch[i,]==1))
1508      n2 <- max(which(ch[i,]==1))
1509      state[i,n1:n2] <- 2
1510    }
1511    state[state==0] <- NA
1512    get.first <- function(x) min(which(!is.na(x)))
1513    get.last <- function(x) max(which(!is.na(x)))
1514    f <- apply(state, 1, get.first)
1515    l <- apply(state, 1, get.last)
1516    for (i in 1:nrow(ch)){
1517      state[i,1:f[i]] <- 1
1518      if(l[i]!=ncol(ch)) state[i, (l[i]+1):ncol(ch)] <- 3
1519      state[i, f[i]] <- 2
1520    }
1521    state <- rbind(state, matrix(1, ncol = ncol(ch), nrow = ns))
1522    return(state)
1523  }
1524
1525  # Collapse capture histories (from Yackulic et al. 2020)
1526
1527  collapse.ch <- function(ch){
1528    options(warn=-1)
1529    ch.char = apply(ch, 1, function(x) paste(x, collapse = ","))
1530    ch.sum.out = t(sapply(strsplit(names(table(ch.char)), split = ","),
1531  as.numeric))
1532    fr.out = as.numeric(as.vector(table(ch.char)))
1533    return(list(ch.sum.out, fr.out))
1534  }
1535
1536  nrep <- 100
1537  # Define parameter values
```

```r
n.occasions <- 7                            # Number of capture occasions
Nsuper <- 400                               # Superpopulation size
phi <- rep(0.7, n.occasions-1)              # Survival probabilities
b <- c(0.40, rep(0.11, n.occasions-1))      # Entry probabilities
p <- rep(0.5, n.occasions)                  # Capture probabilities

PHI <- matrix(rep(phi, (n.occasions-1)*Nsuper), ncol = n.occasions-1, nrow =
                   Nsuper, byrow = TRUE)
P <- matrix(rep(p, n.occasions*Nsuper), ncol = n.occasions, nrow = Nsuper,
               byrow = TRUE)

# Create data frames to store results
js.med.df <- data.frame(model=character(), Nsuper=numeric(), phi=numeric(),
                          b1=numeric(), b2=numeric(), b3=numeric(), b4=numeric(),
                          b5=numeric(), b6=numeric(), b7=numeric(), p=numeric(),
                          f1=numeric(), f2=numeric(), f3=numeric(), f4=numeric(),
                          f5=numeric(), f6=numeric(), N1=numeric(), N2=numeric(),
                          N3=numeric(), N4=numeric(), N5=numeric(), N6=numeric(),
                          N7=numeric(), lambda1=numeric(), lambda2=numeric(),
lambda3=numeric(),lambda4=numeric(),lambda5=numeric(),
                          lambda6=numeric())

js.sd.df <- data.frame(model=character(), Nsuper=numeric(), phi=numeric(),
                          b1=numeric(), b2=numeric(), b3=numeric(), b4=numeric(),
                          b5=numeric(), b6=numeric(), b7=numeric(), p=numeric(),
                          f1=numeric(), f2=numeric(), f3=numeric(), f4=numeric(),
                          f5=numeric(), f6=numeric(), N1=numeric(), N2=numeric(),
                          N3=numeric(), N4=numeric(), N5=numeric(), N6=numeric(),
                          N7=numeric(), lambda1=numeric(), lambda2=numeric(),
lambda3=numeric(),lambda4=numeric(),lambda5=numeric(),
                          lambda6=numeric())

js.025.df <- data.frame(model=character(), Nsuper=numeric(), phi=numeric(),
                          b1=numeric(), b2=numeric(), b3=numeric(), b4=numeric(),
                          b5=numeric(), b6=numeric(), b7=numeric(), p=numeric(),
```

```r
                                  f1=numeric(), f2=numeric(), f3=numeric(),
f4=numeric(),
                                  f5=numeric(), f6=numeric(), N1=numeric(),
N2=numeric(),
                                  N3=numeric(), N4=numeric(), N5=numeric(),
N6=numeric(),
                                  N7=numeric(), lambda1=numeric(),
lambda2=numeric(),

lambda3=numeric(),lambda4=numeric(),lambda5=numeric(),
                                  lambda6=numeric())

js.975.df <- data.frame(model=character(), Nsuper=numeric(),
phi=numeric(),
                                  b1=numeric(), b2=numeric(), b3=numeric(),
b4=numeric(),
                                  b5=numeric(), b6=numeric(), b7=numeric(),
p=numeric(),
                                  f1=numeric(), f2=numeric(), f3=numeric(),
f4=numeric(),
                                  f5=numeric(), f6=numeric(), N1=numeric(),
N2=numeric(),
                                  N3=numeric(), N4=numeric(), N5=numeric(),
N6=numeric(),
                                  N7=numeric(), lambda1=numeric(),
lambda2=numeric(),

lambda3=numeric(),lambda4=numeric(),lambda5=numeric(),
                                  lambda6=numeric())

js.mcmc.df <- data.frame(model=character(), rt=numeric(),
min.ess=numeric(),
                                   max.ess=numeric(), med.ess=numeric(),
max.Rhat=numeric())

# Simulate data and run models

# define number of iterations
nrep <- 100

js <- function(nrep){

  for (i in 1:nrep){

    # Simulate capture histories
    sim <- simul.js(PHI, P, b, Nsuper)
    CH <- sim$CH
    # Add dummy occasion
    CH.du <- cbind(rep(0, dim(CH)[1]), CH)
    # Augment data
    ns <- 500
    CH.ms <- rbind(CH.du, matrix(0, ncol = dim(CH.du)[2], nrow = ns))
    # Recode CH matrix: 2 = Not captured , 1 = captured
```

```
1644        CH.ms[CH.ms==0] <- 2
1645        # collapse to unique capture histories and frequencies
1646        chsum <- collapse.ch(CH.ms)
1647        ys <- chsum[[1]]
1648        FR <- chsum[[2]]
1649        M <- sum(FR)
1650
1651        # MCMC settings
1652        ni <- 20000
1653        nt <- 3
1654        nb <- 5000
1655        nc <- 3
1656
1657        # Parameters to monitor
1658        parameters <- c("Nsuper", "mean.phi", "b", "mean.p", "N", "lambda",
1659                        "f1", "f2")
1660
1661        # model d ------------------------------------------------------------
1662
1663        # Data for discrete multistate JS model
1664        jags.data <- list(y = CH.ms, n.occasions = dim(CH.ms)[2], M =
1665    dim(CH.ms)[1])
1666        # initial values for s
1667        sst <- js.multistate.init(CH.du, ns)
1668        # set initial values
1669        inits <- function(){list(mean.phi = runif(1, .6, .8),
1670                                 mean.p = runif(1, .4, .6), s = sst)}
1671
1672        # run model
1673        js.ms.d <- jags(jags.data, inits, parameters, "js-ms-d.txt", n.chains
1674    = nc,
1675                        n.thin = nt, n.iter = ni, n.burnin = nb,
1676    parallel=TRUE)
1677
1678        # extract results
1679
1680        js.med.df <- rbind(js.med.df, data.frame(model = "d",
1681                    Nsuper = median(js.ms.d$sims.list$Nsuper),
1682                    phi = median(js.ms.d$sims.list$mean.phi),
1683                    b1 = median(js.ms.d$sims.list$b[,1]),
1684                    b2 = median(js.ms.d$sims.list$b[,2]),
1685                    b3 = median(js.ms.d$sims.list$b[,3]),
1686                    b4 = median(js.ms.d$sims.list$b[,4]),
1687                    b5 = median(js.ms.d$sims.list$b[,5]),
1688                    b6 = median(js.ms.d$sims.list$b[,6]),
1689                    b7 = median(js.ms.d$sims.list$b[,7]),
1690                    p = median(js.ms.d$sims.list$mean.p),
1691                    f1 = median(js.ms.d$sims.list$f1[,1]),
1692                    f2 = median(js.ms.d$sims.list$f1[,2]),
1693                    f3 = median(js.ms.d$sims.list$f1[,3]),
1694                    f4 = median(js.ms.d$sims.list$f1[,4]),
1695                    f5 = median(js.ms.d$sims.list$f1[,5]),
1696                    f6 = median(js.ms.d$sims.list$f1[,6]),
```

```
1697                    N1 = median(js.ms.d$sims.list$N[,1]),
1698                    N2 = median(js.ms.d$sims.list$N[,2]),
1699                    N3 = median(js.ms.d$sims.list$N[,3]),
1700                    N4 = median(js.ms.d$sims.list$N[,4]),
1701                    N5 = median(js.ms.d$sims.list$N[,5]),
1702                    N6 = median(js.ms.d$sims.list$N[,6]),
1703                    N7 = median(js.ms.d$sims.list$N[,7]),
1704                  lambda1 = median(js.ms.d$sims.list$lambda[,1]),
1705                  lambda2 = median(js.ms.d$sims.list$lambda[,2]),
1706                  lambda3 = median(js.ms.d$sims.list$lambda[,3]),
1707                  lambda4 = median(js.ms.d$sims.list$lambda[,4]),
1708                  lambda5 = median(js.ms.d$sims.list$lambda[,5]),
1709                  lambda6 = median(js.ms.d$sims.list$lambda[,6])))
1710
1711      js.sd.df <- rbind(js.sd.df, data.frame(model = "d",
1712                  Nsuper = sd(js.ms.d$sims.list$Nsuper),
1713                  phi = sd(js.ms.d$sims.list$mean.phi),
1714                  b1 = sd(js.ms.d$sims.list$b[,1]),
1715                  b2 = sd(js.ms.d$sims.list$b[,2]),
1716                  b3 = sd(js.ms.d$sims.list$b[,3]),
1717                  b4 = sd(js.ms.d$sims.list$b[,4]),
1718                  b5 = sd(js.ms.d$sims.list$b[,5]),
1719                  b6 = sd(js.ms.d$sims.list$b[,6]),
1720                  b7 = sd(js.ms.d$sims.list$b[,7]),
1721                  p = sd(js.ms.d$sims.list$mean.p),
1722                  f1 = sd(js.ms.d$sims.list$f1[,1]),
1723                  f2 = sd(js.ms.d$sims.list$f1[,2]),
1724                  f3 = sd(js.ms.d$sims.list$f1[,3]),
1725                  f4 = sd(js.ms.d$sims.list$f1[,4]),
1726                  f5 = sd(js.ms.d$sims.list$f1[,5]),
1727                  f6 = sd(js.ms.d$sims.list$f1[,6]),
1728                  N1 = sd(js.ms.d$sims.list$N[,1]),
1729                  N2 = sd(js.ms.d$sims.list$N[,2]),
1730                  N3 = sd(js.ms.d$sims.list$N[,3]),
1731                  N4 = sd(js.ms.d$sims.list$N[,4]),
1732                  N5 = sd(js.ms.d$sims.list$N[,5]),
1733                  N6 = sd(js.ms.d$sims.list$N[,6]),
1734                  N7 = sd(js.ms.d$sims.list$N[,7]),
1735                  lambda1 = sd(js.ms.d$sims.list$lambda[,1]),
1736                  lambda2 = sd(js.ms.d$sims.list$lambda[,2]),
1737                  lambda3 = sd(js.ms.d$sims.list$lambda[,3]),
1738                  lambda4 = sd(js.ms.d$sims.list$lambda[,4]),
1739                  lambda5 = sd(js.ms.d$sims.list$lambda[,5]),
1740                  lambda6 = sd(js.ms.d$sims.list$lambda[,6])))
1741
1742      js.025.df <- rbind(js.025.df, data.frame(model = "d",
1743                  Nsuper = quantile(js.ms.d$sims.list$Nsuper, probs =
1744 0.025),
1745                  phi = quantile(js.ms.d$sims.list$mean.phi, probs = 0.025),
1746                  b1 = quantile(js.ms.d$sims.list$b[,1], probs = 0.025),
1747                  b2 = quantile(js.ms.d$sims.list$b[,2], probs = 0.025),
1748                  b3 = quantile(js.ms.d$sims.list$b[,3], probs = 0.025),
1749                  b4 = quantile(js.ms.d$sims.list$b[,4], probs = 0.025),
1750                  b5 = quantile(js.ms.d$sims.list$b[,5], probs = 0.025),
```

```
1751                    b6 = quantile(js.ms.d$sims.list$b[,6], probs = 0.025),
1752                    b7 = quantile(js.ms.d$sims.list$b[,7], probs = 0.025),
1753                    p = quantile(js.ms.d$sims.list$mean.p, probs = 0.025),
1754                    f1 = quantile(js.ms.d$sims.list$f1[,1], probs = 0.025),
1755                    f2 = quantile(js.ms.d$sims.list$f1[,2], probs = 0.025),
1756                    f3 = quantile(js.ms.d$sims.list$f1[,3], probs = 0.025),
1757                    f4 = quantile(js.ms.d$sims.list$f1[,4], probs = 0.025),
1758                    f5 = quantile(js.ms.d$sims.list$f1[,5], probs = 0.025),
1759                    f6 = quantile(js.ms.d$sims.list$f1[,6], probs = 0.025),
1760                    N1 = quantile(js.ms.d$sims.list$N[,1], probs = 0.025),
1761                    N2 = quantile(js.ms.d$sims.list$N[,2], probs = 0.025),
1762                    N3 = quantile(js.ms.d$sims.list$N[,3], probs = 0.025),
1763                    N4 = quantile(js.ms.d$sims.list$N[,4], probs = 0.025),
1764                    N5 = quantile(js.ms.d$sims.list$N[,5], probs = 0.025),
1765                    N6 = quantile(js.ms.d$sims.list$N[,6], probs = 0.025),
1766                    N7 = quantile(js.ms.d$sims.list$N[,7], probs = 0.025),
1767                    lambda1 = quantile(js.ms.d$sims.list$lambda[,1], probs =
1768  0.025),
1769                    lambda2 = quantile(js.ms.d$sims.list$lambda[,2], probs =
1770  0.025),
1771                    lambda3 = quantile(js.ms.d$sims.list$lambda[,3], probs =
1772  0.025),
1773                    lambda4 = quantile(js.ms.d$sims.list$lambda[,4], probs =
1774  0.025),
1775                    lambda5 = quantile(js.ms.d$sims.list$lambda[,5], probs =
1776  0.025),
1777                    lambda6 = quantile(js.ms.d$sims.list$lambda[,6], probs =
1778  0.025)))

1780     js.975.df <- rbind(js.975.df, data.frame(model = "d",
1781                    Nsuper = quantile(js.ms.d$sims.list$Nsuper, probs =
1782  0.975),
1783                    phi = quantile(js.ms.d$sims.list$mean.phi, probs = 0.975),
1784                    b1 = quantile(js.ms.d$sims.list$b[,1], probs = 0.975),
1785                    b2 = quantile(js.ms.d$sims.list$b[,2], probs = 0.975),
1786                    b3 = quantile(js.ms.d$sims.list$b[,3], probs = 0.975),
1787                    b4 = quantile(js.ms.d$sims.list$b[,4], probs = 0.975),
1788                    b5 = quantile(js.ms.d$sims.list$b[,5], probs = 0.975),
1789                    b6 = quantile(js.ms.d$sims.list$b[,6], probs = 0.975),
1790                    b7 = quantile(js.ms.d$sims.list$b[,7], probs = 0.975),
1791                    p = quantile(js.ms.d$sims.list$mean.p, probs = 0.975),
1792                    f1 = quantile(js.ms.d$sims.list$f1[,1], probs = 0.975),
1793                    f2 = quantile(js.ms.d$sims.list$f1[,2], probs = 0.975),
1794                    f3 = quantile(js.ms.d$sims.list$f1[,3], probs = 0.975),
1795                    f4 = quantile(js.ms.d$sims.list$f1[,4], probs = 0.975),
1796                    f5 = quantile(js.ms.d$sims.list$f1[,5], probs = 0.975),
1797                    f6 = quantile(js.ms.d$sims.list$f1[,6], probs = 0.975),
1798                    N1 = quantile(js.ms.d$sims.list$N[,1], probs = 0.975),
1799                    N2 = quantile(js.ms.d$sims.list$N[,2], probs = 0.975),
1800                    N3 = quantile(js.ms.d$sims.list$N[,3], probs = 0.975),
1801                    N4 = quantile(js.ms.d$sims.list$N[,4], probs = 0.975),
1802                    N5 = quantile(js.ms.d$sims.list$N[,5], probs = 0.975),
1803                    N6 = quantile(js.ms.d$sims.list$N[,6], probs = 0.975),
1804                    N7 = quantile(js.ms.d$sims.list$N[,7], probs = 0.975),
```

```r
1805                  lambda1 = quantile(js.ms.d$sims.list$lambda[,1], probs =
1806  0.975),
1807                  lambda2 = quantile(js.ms.d$sims.list$lambda[,2], probs =
1808  0.975),
1809                  lambda3 = quantile(js.ms.d$sims.list$lambda[,3], probs =
1810  0.975),
1811                  lambda4 = quantile(js.ms.d$sims.list$lambda[,4], probs =
1812  0.975),
1813                  lambda5 = quantile(js.ms.d$sims.list$lambda[,5], probs =
1814  0.975),
1815                  lambda6 = quantile(js.ms.d$sims.list$lambda[,6], probs =
1816  0.975)))
1817
1818      js.mcmc.df <- rbind(js.mcmc.df, data.frame(model="d",
1819                  rt=js.ms.d$mcmc.info$elapsed.mins,
1820                  min.ess=min(unlist(js.ms.d$n.eff)),
1821                  max.ess=max(unlist(js.ms.d$n.eff)),
1822                  med.ess=median(unlist(js.ms.d$n.eff)),
1823                  max.Rhat=max(unlist(js.ms.d$Rhat))))
1824
1825      # model m1 -------------------------------------------------------
1826
1827      # data for marginalized JS model
1828      jags.data<- list(FR=FR, fr=FR, ys = ys, n.occasions=dim(ys)[2],
1829  MS=dim(ys)[1],
1830                       M = M)
1831      # set initial values
1832      inits <- function(){ list(mean.phi = .45, mean.p = runif(1, .4, .6))}
1833      # run model
1834      js.ms.m1 <- jags(jags.data, inits, parameters, "js-ms-m1.txt",
1835  n.chains = nc,
1836                  n.thin =nt, n.iter = ni, n.burnin = nb, parallel=TRUE)
1837
1838      # extract results
1839      js.med.df <- rbind(js.med.df, data.frame(model = "m1",
1840                  Nsuper = median(js.ms.m1$sims.list$Nsuper),
1841                  phi = median(js.ms.m1$sims.list$mean.phi),
1842                  b1 = median(js.ms.m1$sims.list$b[,1]),
1843                  b2 = median(js.ms.m1$sims.list$b[,2]),
1844                  b3 = median(js.ms.m1$sims.list$b[,3]),
1845                  b4 = median(js.ms.m1$sims.list$b[,4]),
1846                  b5 = median(js.ms.m1$sims.list$b[,5]),
1847                  b6 = median(js.ms.m1$sims.list$b[,6]),
1848                  b7 = median(js.ms.m1$sims.list$b[,7]),
1849                  p = median(js.ms.m1$sims.list$mean.p),
1850                  f1 = median(js.ms.m1$sims.list$f1[,1]),
1851                  f2 = median(js.ms.m1$sims.list$f1[,2]),
1852                  f3 = median(js.ms.m1$sims.list$f1[,3]),
1853                  f4 = median(js.ms.m1$sims.list$f1[,4]),
1854                  f5 = median(js.ms.m1$sims.list$f1[,5]),
1855                  f6 = median(js.ms.m1$sims.list$f1[,6]),
1856                  N1 = median(js.ms.m1$sims.list$N[,1]),
1857                  N2 = median(js.ms.m1$sims.list$N[,2]),
```

```r
                          N3 = median(js.ms.m1$sims.list$N[,3]),
                          N4 = median(js.ms.m1$sims.list$N[,4]),
                          N5 = median(js.ms.m1$sims.list$N[,5]),
                          N6 = median(js.ms.m1$sims.list$N[,6]),
                          N7 = median(js.ms.m1$sims.list$N[,7]),
                       lambda1 = median(js.ms.m1$sims.list$lambda[,1]),
                       lambda2 = median(js.ms.m1$sims.list$lambda[,2]),
                       lambda3 = median(js.ms.m1$sims.list$lambda[,3]),
                       lambda4 = median(js.ms.m1$sims.list$lambda[,4]),
                       lambda5 = median(js.ms.m1$sims.list$lambda[,5]),
                       lambda6 = median(js.ms.m1$sims.list$lambda[,6])))

       js.sd.df <- rbind(js.sd.df, data.frame(model = "m1",
                       Nsuper = sd(js.ms.m1$sims.list$Nsuper),
                       phi = sd(js.ms.m1$sims.list$mean.phi),
                       b1 = sd(js.ms.m1$sims.list$b[,1]),
                       b2 = sd(js.ms.m1$sims.list$b[,2]),
                       b3 = sd(js.ms.m1$sims.list$b[,3]),
                       b4 = sd(js.ms.m1$sims.list$b[,4]),
                       b5 = sd(js.ms.m1$sims.list$b[,5]),
                       b6 = sd(js.ms.m1$sims.list$b[,6]),
                       b7 = sd(js.ms.m1$sims.list$b[,7]),
                       p = sd(js.ms.m1$sims.list$mean.p),
                       f1 = sd(js.ms.m1$sims.list$f1[,1]),
                       f2 = sd(js.ms.m1$sims.list$f1[,2]),
                       f3 = sd(js.ms.m1$sims.list$f1[,3]),
                       f4 = sd(js.ms.m1$sims.list$f1[,4]),
                       f5 = sd(js.ms.m1$sims.list$f1[,5]),
                       f6 = sd(js.ms.m1$sims.list$f1[,6]),
                       N1 = sd(js.ms.m1$sims.list$N[,1]),
                       N2 = sd(js.ms.m1$sims.list$N[,2]),
                       N3 = sd(js.ms.m1$sims.list$N[,3]),
                       N4 = sd(js.ms.m1$sims.list$N[,4]),
                       N5 = sd(js.ms.m1$sims.list$N[,5]),
                       N6 = sd(js.ms.m1$sims.list$N[,6]),
                       N7 = sd(js.ms.m1$sims.list$N[,7]),
                       lambda1 = sd(js.ms.m1$sims.list$lambda[,1]),
                       lambda2 = sd(js.ms.m1$sims.list$lambda[,2]),
                       lambda3 = sd(js.ms.m1$sims.list$lambda[,3]),
                       lambda4 = sd(js.ms.m1$sims.list$lambda[,4]),
                       lambda5 = sd(js.ms.m1$sims.list$lambda[,5]),
                       lambda6 = sd(js.ms.m1$sims.list$lambda[,6])))

     js.025.df <- rbind(js.025.df, data.frame(model = "m1",
                       Nsuper = quantile(js.ms.m1$sims.list$Nsuper, probs =
0.025),
                       phi = quantile(js.ms.m1$sims.list$mean.phi, probs =
0.025),
                       b1 = quantile(js.ms.m1$sims.list$b[,1], probs = 0.025),
                       b2 = quantile(js.ms.m1$sims.list$b[,2], probs = 0.025),
                       b3 = quantile(js.ms.m1$sims.list$b[,3], probs = 0.025),
                       b4 = quantile(js.ms.m1$sims.list$b[,4], probs = 0.025),
                       b5 = quantile(js.ms.m1$sims.list$b[,5], probs = 0.025),
                       b6 = quantile(js.ms.m1$sims.list$b[,6], probs = 0.025),
```

```
1912                           b7 = quantile(js.ms.m1$sims.list$b[,7], probs = 0.025),
1913                           p = quantile(js.ms.m1$sims.list$mean.p, probs = 0.025),
1914                           f1 = quantile(js.ms.m1$sims.list$f1[,1], probs = 0.025),
1915                           f2 = quantile(js.ms.m1$sims.list$f1[,2], probs = 0.025),
1916                           f3 = quantile(js.ms.m1$sims.list$f1[,3], probs = 0.025),
1917                           f4 = quantile(js.ms.m1$sims.list$f1[,4],probs = 0.025),
1918                           f5 = quantile(js.ms.m1$sims.list$f1[,5], probs = 0.025),
1919                           f6 = quantile(js.ms.m1$sims.list$f1[,6], probs = 0.025),
1920                           N1 = quantile(js.ms.m1$sims.list$N[,1], probs = 0.025),
1921                           N2 = quantile(js.ms.m1$sims.list$N[,2], probs = 0.025),
1922                           N3 = quantile(js.ms.m1$sims.list$N[,3], probs = 0.025),
1923                           N4 = quantile(js.ms.m1$sims.list$N[,4], probs = 0.025),
1924                           N5 = quantile(js.ms.m1$sims.list$N[,5], probs = 0.025),
1925                           N6 = quantile(js.ms.m1$sims.list$N[,6], probs = 0.025),
1926                           N7 = quantile(js.ms.m1$sims.list$N[,7], probs = 0.025),
1927                           lambda1 = quantile(js.ms.m1$sims.list$lambda[,1], probs =
1928         0.025),
1929                           lambda2 = quantile(js.ms.m1$sims.list$lambda[,2], probs =
1930         0.025),
1931                           lambda3 = quantile(js.ms.m1$sims.list$lambda[,3], probs =
1932         0.025),
1933                           lambda4 = quantile(js.ms.m1$sims.list$lambda[,4], probs =
1934         0.025),
1935                           lambda5 = quantile(js.ms.m1$sims.list$lambda[,5], probs =
1936         0.025),
1937                           lambda6 = quantile(js.ms.m1$sims.list$lambda[,6], probs =
1938         0.025)))

1939
1940     js.975.df <- rbind(js.975.df, data.frame(model = "m1",
1941                       Nsuper = quantile(js.ms.m1$sims.list$Nsuper, probs =
1942         0.975),
1943                       phi = quantile(js.ms.m1$sims.list$mean.phi, probs =
1944         0.975),
1945                           b1 = quantile(js.ms.m1$sims.list$b[,1], probs = 0.975),
1946                           b2 = quantile(js.ms.m1$sims.list$b[,2], probs = 0.975),
1947                           b3 = quantile(js.ms.m1$sims.list$b[,3], probs = 0.975),
1948                           b4 = quantile(js.ms.m1$sims.list$b[,4], probs = 0.975),
1949                           b5 = quantile(js.ms.m1$sims.list$b[,5], probs = 0.975),
1950                           b6 = quantile(js.ms.m1$sims.list$b[,6], probs = 0.975),
1951                           b7 = quantile(js.ms.m1$sims.list$b[,7], probs = 0.975),
1952                           p = quantile(js.ms.m1$sims.list$mean.p, probs = 0.975),
1953                           f1 = quantile(js.ms.m1$sims.list$f1[,1], probs = 0.975),
1954                           f2 = quantile(js.ms.m1$sims.list$f1[,2], probs = 0.975),
1955                           f3 = quantile(js.ms.m1$sims.list$f1[,3], probs = 0.975),
1956                           f4 = quantile(js.ms.m1$sims.list$f1[,4],probs = 0.975),
1957                           f5 = quantile(js.ms.m1$sims.list$f1[,5], probs = 0.975),
1958                           f6 = quantile(js.ms.m1$sims.list$f1[,6], probs = 0.975),
1959                           N1 = quantile(js.ms.m1$sims.list$N[,1], probs = 0.975),
1960                           N2 = quantile(js.ms.m1$sims.list$N[,2], probs = 0.975),
1961                           N3 = quantile(js.ms.m1$sims.list$N[,3], probs = 0.975),
1962                           N4 = quantile(js.ms.m1$sims.list$N[,4], probs = 0.975),
1963                           N5 = quantile(js.ms.m1$sims.list$N[,5], probs = 0.975),
1964                           N6 = quantile(js.ms.m1$sims.list$N[,6], probs = 0.975),
1965                           N7 = quantile(js.ms.m1$sims.list$N[,7], probs = 0.975),
```

```
                    lambda1 = quantile(js.ms.m1$sims.list$lambda[,1], probs =
0.975),
                    lambda2 = quantile(js.ms.m1$sims.list$lambda[,2], probs =
0.975),
                    lambda3 = quantile(js.ms.m1$sims.list$lambda[,3], probs =
0.975),
                    lambda4 = quantile(js.ms.m1$sims.list$lambda[,4], probs =
0.975),
                    lambda5 = quantile(js.ms.m1$sims.list$lambda[,5], probs =
0.975),
                    lambda6 = quantile(js.ms.m1$sims.list$lambda[,6], probs =
0.975)))

    js.mcmc.df <- rbind(js.mcmc.df, data.frame(model="m1",
                   rt=js.ms.m1$mcmc.info$elapsed.mins,
                   min.ess=min(unlist(js.ms.m1$n.eff)),
                   max.ess=max(unlist(js.ms.m1$n.eff)),
                   med.ess=median(unlist(js.ms.m1$n.eff)),
                   max.Rhat=max(unlist(js.ms.m1$Rhat))))

    # model m2 --------------------------------------------------------

    all_add<-function(NO_OCC=7){
      # calculates different combinations of arrival and departure timing
      arr<-numeric()
      dep<-numeric()
      t<-1
      for (i in 1:NO_OCC){
        for (j in i:NO_OCC){
          arr[t]<-i
          dep[t]<-j
          t<-t+1
        }}
      return(cbind(arr,dep))}

    MS=dim(ys)[1]

    poss<-all_add()

    first<-function(x){
      #determine timing of first observation
      which(x==1)[1]}

    last<-function(x){
      #determine timing of last observation
      tx<-which(x==1)
      lx<-length(tx)
      tx[lx]
    }

    fd<-apply(ys[-MS,-1],1,first)
```

```
2019     ld<-apply(ys[-MS,-1],1,last)

2020

2021     nposs=length(poss[,1])

2022

2023     poss_obs<-matrix(NA,nrow=nposs,ncol=(MS-1))

2024

2025     for (i in 1:(MS-1)){
2026        #for each summarized capture history this loop determines if the
2027     possible
2028        # underlying dynamics implied by poss are possible
2029        poss_obs[,i]<-ifelse(poss[,1]<=fd[i]&poss[,2]>=ld[i],1,0)
2030     }

2031

2032     Nobs_ind <- sum(FR[-MS])

2033

2034     lookup <- rep(seq(1,length(FR[-MS]), 1), FR[-MS])

2035

2036     jags.data<- list(FR=FR, fr=FR, ys = ys, n.occasions=dim(ys)[2],
2037     MS=dim(ys)[1],
2038                      Nobs_ind = Nobs_ind,Npos_ind = sum(FR) ,
2039     lookup=lookup,
2040                      nposs=nposs, poss=poss, poss_obs=poss_obs)

2041

2042     inits <- function(){list(mean.phi = runif(1, .6, .8),
2043                              mean.p = runif(1, .4, .6),
2044     A=rep(c(fd,NA),FR),
2045                              L=rep(c(ld,NA),FR), ar=rep(c(fd,1), FR),
2046                              li=rep(c(ld,(dim(ys)[2]-1)),FR), U=FR[MS])}

2047

2048     js.ms.m2 <- jags(jags.data, inits, parameters, "js-ms-m2.txt",
2049     n.chains = nc,
2050                      n.thin =nt, n.iter = ni, n.burnin = nb,
2051     parallel=TRUE)

2052

2053     # extract results
2054     js.med.df <- rbind(js.med.df, data.frame(model = "m2",
2055                     Nsuper = median(js.ms.m2$sims.list$Nsuper),
2056                     phi = median(js.ms.m2$sims.list$mean.phi),
2057                     b1 = median(js.ms.m2$sims.list$b[,1]),
2058                     b2 = median(js.ms.m2$sims.list$b[,2]),
2059                     b3 = median(js.ms.m2$sims.list$b[,3]),
2060                     b4 = median(js.ms.m2$sims.list$b[,4]),
2061                     b5 = median(js.ms.m2$sims.list$b[,5]),
2062                     b6 = median(js.ms.m2$sims.list$b[,6]),
2063                     b7 = median(js.ms.m2$sims.list$b[,7]),
2064                     p = median(js.ms.m2$sims.list$mean.p),
2065                     f1 = median(js.ms.m2$sims.list$f1[,1]),
2066                     f2 = median(js.ms.m2$sims.list$f1[,2]),
2067                     f3 = median(js.ms.m2$sims.list$f1[,3]),
2068                     f4 = median(js.ms.m2$sims.list$f1[,4]),
2069                     f5 = median(js.ms.m2$sims.list$f1[,5]),
2070                     f6 = median(js.ms.m2$sims.list$f1[,6]),
2071                     N1 = median(js.ms.m2$sims.list$N[,1]),
```

```
2072                    N2 = median(js.ms.m2$sims.list$N[,2]),
2073                    N3 = median(js.ms.m2$sims.list$N[,3]),
2074                    N4 = median(js.ms.m2$sims.list$N[,4]),
2075                    N5 = median(js.ms.m2$sims.list$N[,5]),
2076                    N6 = median(js.ms.m2$sims.list$N[,6]),
2077                    N7 = median(js.ms.m2$sims.list$N[,7]),
2078                  lambda1 = median(js.ms.m2$sims.list$lambda[,1]),
2079                  lambda2 = median(js.ms.m2$sims.list$lambda[,2]),
2080                  lambda3 = median(js.ms.m2$sims.list$lambda[,3]),
2081                  lambda4 = median(js.ms.m2$sims.list$lambda[,4]),
2082                  lambda5 = median(js.ms.m2$sims.list$lambda[,5]),
2083                  lambda6 = median(js.ms.m2$sims.list$lambda[,6])))
2084
2085      js.sd.df <- rbind(js.sd.df, data.frame(model = "m2",
2086                  Nsuper = sd(js.ms.m2$sims.list$Nsuper),
2087                  phi = sd(js.ms.m2$sims.list$mean.phi),
2088                  b1 = sd(js.ms.m2$sims.list$b[,1]),
2089                  b2 = sd(js.ms.m2$sims.list$b[,2]),
2090                  b3 = sd(js.ms.m2$sims.list$b[,3]),
2091                  b4 = sd(js.ms.m2$sims.list$b[,4]),
2092                  b5 = sd(js.ms.m2$sims.list$b[,5]),
2093                  b6 = sd(js.ms.m2$sims.list$b[,6]),
2094                  b7 = sd(js.ms.m2$sims.list$b[,7]),
2095                  p = sd(js.ms.m2$sims.list$mean.p),
2096                  f1 = sd(js.ms.m2$sims.list$f1[,1]),
2097                  f2 = sd(js.ms.m2$sims.list$f1[,2]),
2098                  f3 = sd(js.ms.m2$sims.list$f1[,3]),
2099                  f4 = sd(js.ms.m2$sims.list$f1[,4]),
2100                  f5 = sd(js.ms.m2$sims.list$f1[,5]),
2101                  f6 = sd(js.ms.m2$sims.list$f1[,6]),
2102                  N1 = sd(js.ms.m2$sims.list$N[,1]),
2103                  N2 = sd(js.ms.m2$sims.list$N[,2]),
2104                  N3 = sd(js.ms.m2$sims.list$N[,3]),
2105                  N4 = sd(js.ms.m2$sims.list$N[,4]),
2106                  N5 = sd(js.ms.m2$sims.list$N[,5]),
2107                  N6 = sd(js.ms.m2$sims.list$N[,6]),
2108                  N7 = sd(js.ms.m2$sims.list$N[,7]),
2109                  lambda1 = sd(js.ms.m2$sims.list$lambda[,1]),
2110                  lambda2 = sd(js.ms.m2$sims.list$lambda[,2]),
2111                  lambda3 = sd(js.ms.m2$sims.list$lambda[,3]),
2112                  lambda4 = sd(js.ms.m2$sims.list$lambda[,4]),
2113                  lambda5 = sd(js.ms.m2$sims.list$lambda[,5]),
2114                  lambda6 = sd(js.ms.m2$sims.list$lambda[,6])))
2115
2116      js.025.df <- rbind(js.025.df, data.frame(model = "m2",
2117                  Nsuper = quantile(js.ms.m2$sims.list$Nsuper, probs =
2118  0.025),
2119                  phi = quantile(js.ms.m2$sims.list$mean.phi, probs =
2120  0.025),
2121                  b1 = quantile(js.ms.m2$sims.list$b[,1], probs = 0.025),
2122                  b2 = quantile(js.ms.m2$sims.list$b[,2], probs = 0.025),
2123                  b3 = quantile(js.ms.m2$sims.list$b[,3], probs = 0.025),
2124                  b4 = quantile(js.ms.m2$sims.list$b[,4], probs = 0.025),
2125                  b5 = quantile(js.ms.m2$sims.list$b[,5], probs = 0.025),
```

```
2126                           b6 = quantile(js.ms.m2$sims.list$b[,6], probs = 0.025),
2127                           b7 = quantile(js.ms.m2$sims.list$b[,7], probs = 0.025),
2128                           p = quantile(js.ms.m2$sims.list$mean.p, probs = 0.025),
2129                           f1 = quantile(js.ms.m2$sims.list$f1[,1], probs = 0.025),
2130                           f2 = quantile(js.ms.m2$sims.list$f1[,2], probs = 0.025),
2131                           f3 = quantile(js.ms.m2$sims.list$f1[,3], probs = 0.025),
2132                           f4 = quantile(js.ms.m2$sims.list$f1[,4], probs = 0.025),
2133                           f5 = quantile(js.ms.m2$sims.list$f1[,5], probs = 0.025),
2134                           f6 = quantile(js.ms.m2$sims.list$f1[,6], probs = 0.025),
2135                           N1 = quantile(js.ms.m2$sims.list$N[,1], probs = 0.025),
2136                           N2 = quantile(js.ms.m2$sims.list$N[,2], probs = 0.025),
2137                           N3 = quantile(js.ms.m2$sims.list$N[,3], probs = 0.025),
2138                           N4 = quantile(js.ms.m2$sims.list$N[,4], probs = 0.025),
2139                           N5 = quantile(js.ms.m2$sims.list$N[,5], probs = 0.025),
2140                           N6 = quantile(js.ms.m2$sims.list$N[,6], probs = 0.025),
2141                           N7 = quantile(js.ms.m2$sims.list$N[,7], probs = 0.025),
2142                           lambda1 = quantile(js.ms.m2$sims.list$lambda[,1], probs =
2143    0.025),
2144                           lambda2 = quantile(js.ms.m2$sims.list$lambda[,2], probs =
2145    0.025),
2146                           lambda3 = quantile(js.ms.m2$sims.list$lambda[,3], probs =
2147    0.025),
2148                           lambda4 = quantile(js.ms.m2$sims.list$lambda[,4], probs =
2149    0.025),
2150                           lambda5 = quantile(js.ms.m2$sims.list$lambda[,5], probs =
2151    0.025),
2152                           lambda6 = quantile(js.ms.m2$sims.list$lambda[,6], probs =
2153    0.025)))
2154
2155        js.975.df <- rbind(js.975.df, data.frame(model = "m2",
2156                           Nsuper = quantile(js.ms.m2$sims.list$Nsuper, probs =
2157    0.975),
2158                           phi = quantile(js.ms.m2$sims.list$mean.phi, probs =
2159    0.975),
2160                           b1 = quantile(js.ms.m2$sims.list$b[,1], probs = 0.975),
2161                           b2 = quantile(js.ms.m2$sims.list$b[,2], probs = 0.975),
2162                           b3 = quantile(js.ms.m2$sims.list$b[,3], probs = 0.975),
2163                           b4 = quantile(js.ms.m2$sims.list$b[,4], probs = 0.975),
2164                           b5 = quantile(js.ms.m2$sims.list$b[,5], probs = 0.975),
2165                           b6 = quantile(js.ms.m2$sims.list$b[,6], probs = 0.975),
2166                           b7 = quantile(js.ms.m2$sims.list$b[,7], probs = 0.975),
2167                           p = quantile(js.ms.m2$sims.list$mean.p, probs = 0.975),
2168                           f1 = quantile(js.ms.m2$sims.list$f1[,1], probs = 0.975),
2169                           f2 = quantile(js.ms.m2$sims.list$f1[,2], probs = 0.975),
2170                           f3 = quantile(js.ms.m2$sims.list$f1[,3], probs = 0.975),
2171                           f4 = quantile(js.ms.m2$sims.list$f1[,4], probs = 0.975),
2172                           f5 = quantile(js.ms.m2$sims.list$f1[,5], probs = 0.975),
2173                           f6 = quantile(js.ms.m2$sims.list$f1[,6], probs = 0.975),
2174                           N1 = quantile(js.ms.m2$sims.list$N[,1], probs = 0.975),
2175                           N2 = quantile(js.ms.m2$sims.list$N[,2], probs = 0.975),
2176                           N3 = quantile(js.ms.m2$sims.list$N[,3], probs = 0.975),
2177                           N4 = quantile(js.ms.m2$sims.list$N[,4], probs = 0.975),
2178                           N5 = quantile(js.ms.m2$sims.list$N[,5], probs = 0.975),
2179                           N6 = quantile(js.ms.m2$sims.list$N[,6], probs = 0.975),
```

```
2180                    N7 = quantile(js.ms.m2$sims.list$N[,7], probs = 0.975),
2181                    lambda1 = quantile(js.ms.m2$sims.list$lambda[,1], probs =
2182    0.975),
2183                    lambda2 = quantile(js.ms.m2$sims.list$lambda[,2], probs =
2184    0.975),
2185                    lambda3 = quantile(js.ms.m2$sims.list$lambda[,3], probs =
2186    0.975),
2187                    lambda4 = quantile(js.ms.m2$sims.list$lambda[,4], probs =
2188    0.975),
2189                    lambda5 = quantile(js.ms.m2$sims.list$lambda[,5], probs =
2190    0.975),
2191                    lambda6 = quantile(js.ms.m2$sims.list$lambda[,6], probs =
2192    0.975)))
2193
2194        js.mcmc.df <- rbind(js.mcmc.df, data.frame(model="m2",
2195                        rt=js.ms.m2$mcmc.info$elapsed.mins,
2196                        min.ess=min(unlist(js.ms.m2$n.eff)),
2197                        max.ess=max(unlist(js.ms.m2$n.eff)),
2198                        med.ess=median(unlist(js.ms.m2$n.eff)),
2199                        max.Rhat=max(unlist(js.ms.m2$Rhat))))
2200
2201
2202        # model m3 ----------------------------------------------------------
2203
2204        # create index to recover discrete latent states for derived
2205    parameters
2206        lookup <- rep(seq(1,length(FR), 1), FR)
2207        jags.data<- list(FR=FR, fr=FR, ys = ys, n.occasions=dim(ys)[2],
2208    MS=dim(ys)[1], M=M,
2209                        lookup=lookup)
2210        inits <- function(){list(mean.phi = runif(1, .6, .8), mean.p =
2211    runif(1, .4, .6),
2212                            U=FR[MS])}
2213        js.ms.m3 <- jags(jags.data, inits, parameters, "js-ms-m3.txt",
2214    n.chains = nc,
2215                        n.thin =nt, n.iter = ni, n.burnin = nb,
2216    parallel=TRUE)
2217
2218        # extract results
2219        js.med.df <- rbind(js.med.df, data.frame(model = "m3",
2220                        Nsuper = median(js.ms.m3$sims.list$Nsuper),
2221                        phi = median(js.ms.m3$sims.list$mean.phi),
2222                        b1 = median(js.ms.m3$sims.list$b[,1]),
2223                        b2 = median(js.ms.m3$sims.list$b[,2]),
2224                        b3 = median(js.ms.m3$sims.list$b[,3]),
2225                        b4 = median(js.ms.m3$sims.list$b[,4]),
2226                        b5 = median(js.ms.m3$sims.list$b[,5]),
2227                        b6 = median(js.ms.m3$sims.list$b[,6]),
2228                        b7 = median(js.ms.m3$sims.list$b[,7]),
2229                        p = median(js.ms.m3$sims.list$mean.p),
2230                        f1 = median(js.ms.m3$sims.list$f1[,1]),
2231                        f2 = median(js.ms.m3$sims.list$f1[,2]),
2232                        f3 = median(js.ms.m3$sims.list$f1[,3]),
```

```
2233                          f4 = median(js.ms.m3$sims.list$f1[,4]),
2234                          f5 = median(js.ms.m3$sims.list$f1[,5]),
2235                          f6 = median(js.ms.m3$sims.list$f1[,6]),
2236                          N1 = median(js.ms.m3$sims.list$N[,1]),
2237                          N2 = median(js.ms.m3$sims.list$N[,2]),
2238                          N3 = median(js.ms.m3$sims.list$N[,3]),
2239                          N4 = median(js.ms.m3$sims.list$N[,4]),
2240                          N5 = median(js.ms.m3$sims.list$N[,5]),
2241                          N6 = median(js.ms.m3$sims.list$N[,6]),
2242                          N7 = median(js.ms.m3$sims.list$N[,7]),
2243                          lambda1 = median(js.ms.m3$sims.list$lambda[,1]),
2244                          lambda2 = median(js.ms.m3$sims.list$lambda[,2]),
2245                          lambda3 = median(js.ms.m3$sims.list$lambda[,3]),
2246                          lambda4 = median(js.ms.m3$sims.list$lambda[,4]),
2247                          lambda5 = median(js.ms.m3$sims.list$lambda[,5]),
2248                          lambda6 = median(js.ms.m3$sims.list$lambda[,6])))
2249
2250      js.sd.df <- rbind(js.sd.df, data.frame(model = "m3",
2251                      Nsuper = sd(js.ms.m3$sims.list$Nsuper),
2252                      phi = sd(js.ms.m3$sims.list$mean.phi),
2253                      b1 = sd(js.ms.m3$sims.list$b[,1]),
2254                      b2 = sd(js.ms.m3$sims.list$b[,2]),
2255                      b3 = sd(js.ms.m3$sims.list$b[,3]),
2256                      b4 = sd(js.ms.m3$sims.list$b[,4]),
2257                      b5 = sd(js.ms.m3$sims.list$b[,5]),
2258                      b6 = sd(js.ms.m3$sims.list$b[,6]),
2259                      b7 = sd(js.ms.m3$sims.list$b[,7]),
2260                      p = sd(js.ms.m3$sims.list$mean.p),
2261                      f1 = sd(js.ms.m3$sims.list$f1[,1]),
2262                      f2 = sd(js.ms.m3$sims.list$f1[,2]),
2263                      f3 = sd(js.ms.m3$sims.list$f1[,3]),
2264                      f4 = sd(js.ms.m3$sims.list$f1[,4]),
2265                      f5 = sd(js.ms.m3$sims.list$f1[,5]),
2266                      f6 = sd(js.ms.m3$sims.list$f1[,6]),
2267                      N1 = sd(js.ms.m3$sims.list$N[,1]),
2268                      N2 = sd(js.ms.m3$sims.list$N[,2]),
2269                      N3 = sd(js.ms.m3$sims.list$N[,3]),
2270                      N4 = sd(js.ms.m3$sims.list$N[,4]),
2271                      N5 = sd(js.ms.m3$sims.list$N[,5]),
2272                      N6 = sd(js.ms.m3$sims.list$N[,6]),
2273                      N7 = sd(js.ms.m3$sims.list$N[,7]),
2274                      lambda1 = sd(js.ms.m3$sims.list$lambda[,1]),
2275                      lambda2 = sd(js.ms.m3$sims.list$lambda[,2]),
2276                      lambda3 = sd(js.ms.m3$sims.list$lambda[,3]),
2277                      lambda4 = sd(js.ms.m3$sims.list$lambda[,4]),
2278                      lambda5 = sd(js.ms.m3$sims.list$lambda[,5]),
2279                      lambda6 = sd(js.ms.m3$sims.list$lambda[,6])))
2280
2281      js.025.df <- rbind(js.025.df, data.frame(model = "m3",
2282                      Nsuper = quantile(js.ms.m3$sims.list$Nsuper, probs =
2283 0.025),
2284                      phi = quantile(js.ms.m3$sims.list$mean.phi, probs =
2285 0.025),
2286                      b1 = quantile(js.ms.m3$sims.list$b[,1], probs = 0.025),
```

```
2287                          b2 = quantile(js.ms.m3$sims.list$b[,2], probs = 0.025),
2288                          b3 = quantile(js.ms.m3$sims.list$b[,3], probs = 0.025),
2289                          b4 = quantile(js.ms.m3$sims.list$b[,4], probs = 0.025),
2290                          b5 = quantile(js.ms.m3$sims.list$b[,5], probs = 0.025),
2291                          b6 = quantile(js.ms.m3$sims.list$b[,6], probs = 0.025),
2292                          b7 = quantile(js.ms.m3$sims.list$b[,7], probs = 0.025),
2293                          p = quantile(js.ms.m3$sims.list$mean.p, probs = 0.025),
2294                          f1 = quantile(js.ms.m3$sims.list$f1[,1], probs = 0.025),
2295                          f2 = quantile(js.ms.m3$sims.list$f1[,2], probs = 0.025),
2296                          f3 = quantile(js.ms.m3$sims.list$f1[,3], probs = 0.025),
2297                          f4 = quantile(js.ms.m3$sims.list$f1[,4], probs = 0.025),
2298                          f5 = quantile(js.ms.m3$sims.list$f1[,5], probs = 0.025),
2299                          f6 = quantile(js.ms.m3$sims.list$f1[,6], probs = 0.025),
2300                          N1 = quantile(js.ms.m3$sims.list$N[,1], probs = 0.025),
2301                          N2 = quantile(js.ms.m3$sims.list$N[,2], probs = 0.025),
2302                          N3 = quantile(js.ms.m3$sims.list$N[,3], probs = 0.025),
2303                          N4 = quantile(js.ms.m3$sims.list$N[,4], probs = 0.025),
2304                          N5 = quantile(js.ms.m3$sims.list$N[,5], probs = 0.025),
2305                          N6 = quantile(js.ms.m3$sims.list$N[,6], probs = 0.025),
2306                          N7 = quantile(js.ms.m3$sims.list$N[,7], probs = 0.025),
2307                          lambda1 = quantile(js.ms.m3$sims.list$lambda[,1], probs =
2308    0.025),
2309                          lambda2 = quantile(js.ms.m3$sims.list$lambda[,2], probs =
2310    0.025),
2311                          lambda3 = quantile(js.ms.m3$sims.list$lambda[,3], probs =
2312    0.025),
2313                          lambda4 = quantile(js.ms.m3$sims.list$lambda[,4], probs =
2314    0.025),
2315                          lambda5 = quantile(js.ms.m3$sims.list$lambda[,5], probs =
2316    0.025),
2317                          lambda6 = quantile(js.ms.m3$sims.list$lambda[,6], probs =
2318    0.025)))
2319
2320       js.975.df <- rbind(js.975.df, data.frame(model = "m3",
2321                          Nsuper = quantile(js.ms.m3$sims.list$Nsuper, probs =
2322    0.975),
2323                          phi = quantile(js.ms.m3$sims.list$mean.phi, probs =
2324    0.975),
2325                          b1 = quantile(js.ms.m3$sims.list$b[,1], probs = 0.975),
2326                          b2 = quantile(js.ms.m3$sims.list$b[,2], probs = 0.975),
2327                          b3 = quantile(js.ms.m3$sims.list$b[,3], probs = 0.975),
2328                          b4 = quantile(js.ms.m3$sims.list$b[,4], probs = 0.975),
2329                          b5 = quantile(js.ms.m3$sims.list$b[,5], probs = 0.975),
2330                          b6 = quantile(js.ms.m3$sims.list$b[,6], probs = 0.975),
2331                          b7 = quantile(js.ms.m3$sims.list$b[,7], probs = 0.975),
2332                          p = quantile(js.ms.m3$sims.list$mean.p, probs = 0.975),
2333                          f1 = quantile(js.ms.m3$sims.list$f1[,1], probs = 0.975),
2334                          f2 = quantile(js.ms.m3$sims.list$f1[,2], probs = 0.975),
2335                          f3 = quantile(js.ms.m3$sims.list$f1[,3], probs = 0.975),
2336                          f4 = quantile(js.ms.m3$sims.list$f1[,4], probs = 0.975),
2337                          f5 = quantile(js.ms.m3$sims.list$f1[,5], probs = 0.975),
2338                          f6 = quantile(js.ms.m3$sims.list$f1[,6], probs = 0.975),
2339                          N1 = quantile(js.ms.m3$sims.list$N[,1], probs = 0.975),
2340                          N2 = quantile(js.ms.m3$sims.list$N[,2], probs = 0.975),
```

```r
                           N3 = quantile(js.ms.m3$sims.list$N[,3], probs = 0.975),
                           N4 = quantile(js.ms.m3$sims.list$N[,4], probs = 0.975),
                           N5 = quantile(js.ms.m3$sims.list$N[,5], probs = 0.975),
                           N6 = quantile(js.ms.m3$sims.list$N[,6], probs = 0.975),
                           N7 = quantile(js.ms.m3$sims.list$N[,7], probs = 0.975),
                           lambda1 = quantile(js.ms.m3$sims.list$lambda[,1], probs =
0.975),
                           lambda2 = quantile(js.ms.m3$sims.list$lambda[,2], probs =
0.975),
                           lambda3 = quantile(js.ms.m3$sims.list$lambda[,3], probs =
0.975),
                           lambda4 = quantile(js.ms.m3$sims.list$lambda[,4], probs =
0.975),
                           lambda5 = quantile(js.ms.m3$sims.list$lambda[,5], probs =
0.975),
                           lambda6 = quantile(js.ms.m3$sims.list$lambda[,6], probs =
0.975)))

      js.mcmc.df <- rbind(js.mcmc.df, data.frame(model="m3",
                       rt=js.ms.m3$mcmc.info$elapsed.mins,
                       min.ess=min(unlist(js.ms.m3$n.eff)),
                       max.ess=max(unlist(js.ms.m3$n.eff)),
                       med.ess=median(unlist(js.ms.m3$n.eff)),
                       max.Rhat=max(unlist(js.ms.m3$Rhat))))
  }
  return(list(js.med.df, js.sd.df, js.025.df, js.975.df, js.mcmc.df))
}

if (file.exists("js_out_marg.rds")) {
  js.out.marg <- readRDS("js_out_marg.rds")
} else {
  js.out.marg <- js(nrep)  # a time-consuming function
  saveRDS(js.out.marg, "js_out_marg.rds")
}

## extract posterior medians
d.meds <- js.out.marg[[1]][js.out.marg[[1]]$model%in%"d",]
m1.meds <- js.out.marg[[1]][js.out.marg[[1]]$model%in%"m1",]
m2.meds <- js.out.marg[[1]][js.out.marg[[1]]$model%in%"m2",]
m3.meds <- js.out.marg[[1]][js.out.marg[[1]]$model%in%"m3",]

save(d.meds, m1.meds, m2.meds, m3.meds, file = "modelcomparefigS1.RData")

library(kableExtra)
options(knitr.kable.NA = '')

js.out.marg[[5]]$mps100 <-
js.out.marg[[5]]$rt/js.out.marg[[5]]$min.ess*100
js.out.marg[[5]]$mps1000 <-
js.out.marg[[5]]$rt/js.out.marg[[5]]$min.ess*1000

# expected values
```

```r
2393   E_N <- c(136, 139, 141, 143, 144, 145, 145)
2394   E_lam <- E_N[2:7]/E_N[1:6]
2395   E_f <- E_lam - .7
2396
2397   # summarize simulations
2398   simsum <- data.frame(model = js.out.marg[[3]]$model,
2399                        Nsuper.cov = ifelse(js.out.marg[[3]]$Nsuper <= 400 &
2400                                              js.out.marg[[4]]$Nsuper >= 400,
2401   1, 0),
2402                        Nsuper.w = js.out.marg[[4]]$Nsuper -
2403   js.out.marg[[3]]$Nsuper,
2404                        N1.cov = ifelse(js.out.marg[[3]]$N1 <= E_N[1] &
2405                                          js.out.marg[[4]]$N1 >= E_N[1], 1,
2406   0),
2407                        N1.w = js.out.marg[[4]]$N1 - js.out.marg[[3]]$N1,
2408                        N2.cov = ifelse(js.out.marg[[3]]$N2 <= E_N[2] &
2409                                          js.out.marg[[4]]$N2 >= E_N[2], 1,
2410   0),
2411                        N2.w = js.out.marg[[4]]$N2 - js.out.marg[[3]]$N2,
2412                        N3.cov = ifelse(js.out.marg[[3]]$N3 <= E_N[3] &
2413                                          js.out.marg[[4]]$N3 >= E_N[3], 1,
2414   0),
2415                        N3.w = js.out.marg[[4]]$N3 - js.out.marg[[3]]$N3,
2416                        N4.cov = ifelse(js.out.marg[[3]]$N4 <= E_N[4] &
2417                                          js.out.marg[[4]]$N4 >= E_N[4], 1,
2418   0),
2419                        N4.w = js.out.marg[[4]]$N4 - js.out.marg[[3]]$N4,
2420                        N5.cov = ifelse(js.out.marg[[3]]$N5 <= E_N[5] &
2421                                          js.out.marg[[4]]$N5 >= E_N[5], 1,
2422   0),
2423                        N5.w = js.out.marg[[4]]$N5 - js.out.marg[[3]]$N5,
2424                        N6.cov = ifelse(js.out.marg[[3]]$N6 <= E_N[6] &
2425                                          js.out.marg[[4]]$N6 >= E_N[6], 1,
2426   0),
2427                        N6.w = js.out.marg[[4]]$N6 - js.out.marg[[3]]$N6,
2428                        N7.cov = ifelse(js.out.marg[[3]]$N7 <= E_N[7] &
2429                                          js.out.marg[[4]]$N7 >= E_N[7], 1,
2430   0),
2431                        N7.w = js.out.marg[[4]]$N7 - js.out.marg[[3]]$N7,
2432                        lam1.cov = ifelse(js.out.marg[[3]]$lambda1 <=
2433   E_lam[1] &
2434                                            js.out.marg[[4]]$lambda1 >=
2435   E_lam[1], 1, 0),
2436                        lam1.w = js.out.marg[[4]]$lambda1 -
2437   js.out.marg[[3]]$lambda1,
2438                        lam2.cov = ifelse(js.out.marg[[3]]$lambda2 <=
2439   E_lam[2] &
2440                                            js.out.marg[[4]]$lambda2 >=
2441   E_lam[2], 1, 0),
2442                        lam2.w = js.out.marg[[4]]$lambda2 -
2443   js.out.marg[[3]]$lambda2,
2444                        lam3.cov = ifelse(js.out.marg[[3]]$lambda3 <=
2445   E_lam[3] &
2446                                            js.out.marg[[4]]$lambda3 >=
```

```r
2447    E_lam[3], 1, 0),
2448                            lam3.w = js.out.marg[[4]]$lambda3 -
2449    js.out.marg[[3]]$lambda3,
2450                            lam4.cov = ifelse(js.out.marg[[3]]$lambda4 <=
2451    E_lam[4] &
2452                                            js.out.marg[[4]]$lambda4 >=
2453    E_lam[4], 1, 0),
2454                            lam4.w = js.out.marg[[4]]$lambda4 -
2455    js.out.marg[[3]]$lambda4,
2456                            lam5.cov = ifelse(js.out.marg[[3]]$lambda5 <=
2457    E_lam[5] &
2458                                            js.out.marg[[4]]$lambda5 >=
2459    E_lam[5], 1, 0),
2460                            lam5.w = js.out.marg[[4]]$lambda5 -
2461    js.out.marg[[3]]$lambda5,
2462                            lam6.cov = ifelse(js.out.marg[[3]]$lambda6 <=
2463    E_lam[6] &
2464                                            js.out.marg[[4]]$lambda6 >=
2465    E_lam[6], 1, 0),
2466                            lam6.w = js.out.marg[[4]]$lambda6 -
2467    js.out.marg[[3]]$lambda6,
2468                            f1.cov = ifelse(js.out.marg[[3]]$f1 <= E_f[1] &
2469                                            js.out.marg[[4]]$f1 >= E_f[1], 1,
2470    0),
2471                            f1.w = js.out.marg[[4]]$f1 - js.out.marg[[3]]$f1,
2472                            f2.cov = ifelse(js.out.marg[[3]]$f2 <= E_f[2] &
2473                                            js.out.marg[[4]]$f2 >= E_f[2], 1,
2474    0),
2475                            f2.w = js.out.marg[[4]]$f2 - js.out.marg[[3]]$f2,
2476                            f3.cov = ifelse(js.out.marg[[3]]$f3 <= E_f[3] &
2477                                            js.out.marg[[4]]$f3 >= E_f[3], 1,
2478    0),
2479                            f3.w = js.out.marg[[4]]$f3 - js.out.marg[[3]]$f3,
2480                            f4.cov = ifelse(js.out.marg[[3]]$f4 <= E_f[4] &
2481                                            js.out.marg[[4]]$f4 >= E_f[4], 1,
2482    0),
2483                            f4.w = js.out.marg[[4]]$f4 - js.out.marg[[3]]$f4,
2484                            f5.cov = ifelse(js.out.marg[[3]]$f5 <= E_f[5] &
2485                                            js.out.marg[[4]]$f5 >= E_f[5], 1,
2486    0),
2487                            f5.w = js.out.marg[[4]]$f5 - js.out.marg[[3]]$f5,
2488                            f6.cov = ifelse(js.out.marg[[3]]$f6 <= E_f[6] &
2489                                            js.out.marg[[4]]$f6 >= E_f[6], 1,
2490    0),
2491                            f6.w = js.out.marg[[4]]$f6 - js.out.marg[[3]]$f6)
2492
2493    library(tidyverse)
2494    library(data.table)
2495
2496    x <- simsum %>% group_by(model) %>% summarise(across(.cols=everything(),
2497                            list(mean = mean, sd = sd), .names =
2498    "{.col}.{.fn}"))
2499
```

```r
2500  xt <- data.table::transpose(x, make.names="model")
2501  xt$parm <- unlist(strsplit(names(x)[2:ncol(x)], "\\.", ""))[seq(1,
2502  length(unlist(strsplit(names(x)[2:ncol(x)], "\\.", ""))), 3)]
2503  xt$var <- rep(c("cov", "cov", "w", "w"), 20)
2504  xt$stat <- rep(c("mean", "sd"), 40)
2505  xt <- xt %>% pivot_wider(id_cols = c(parm, stat), names_from = var,
2506  values_from = c(d, m1, m2, m3))
2507  xt <- data.frame(xt)
2508
2509  xt$d_cov <- sprintf("%.1f", round(xt$d_cov*100, 1))
2510  xt$d_w[xt$parm %in% c("Nsuper", "N1", "N2", "N3", "N4", "N5", "N6", "N7")]
2511  <-
2512    sprintf("%.1f", round(xt$d_w[xt$parm %in% c("Nsuper", "N1", "N2", "N3",
2513  "N4",
2514                                               "N5", "N6", "N7")], 1))
2515  xt$d_w[!(xt$parm %in% c("Nsuper", "N1", "N2", "N3", "N4", "N5", "N6",
2516  "N7"))] <-
2517    sprintf("%.3f", round(as.numeric(xt$d_w[!(xt$parm %in% c("Nsuper", "N1",
2518                                      "N2", "N3", "N4", "N5", "N6",
2519  "N7"))]), 3))
2520
2521  xt$m1_cov <- sprintf("%.1f", round(xt$m1_cov*100, 1))
2522  xt$m1_w[xt$parm %in% c("Nsuper", "N1", "N2", "N3", "N4", "N5", "N6",
2523  "N7")] <-
2524    sprintf("%.1f", round(xt$m1_w[xt$parm %in% c("Nsuper", "N1", "N2", "N3",
2525  "N4",
2526                                               "N5", "N6", "N7")], 1))
2527  xt$m1_w[!(xt$parm %in% c("Nsuper", "N1", "N2", "N3", "N4", "N5", "N6",
2528  "N7"))] <-
2529    sprintf("%.3f", round(as.numeric(xt$m1_w[!(xt$parm %in% c("Nsuper",
2530  "N1", "N2",
2531                                               "N3", "N4", "N5", "N6",
2532  "N7"))]), 3))
2533
2534  xt$m2_cov <- sprintf("%.1f", round(xt$m2_cov*100, 1))
2535  xt$m2_w[xt$parm %in% c("Nsuper", "N1", "N2", "N3", "N4", "N5", "N6",
2536  "N7")] <-
2537    sprintf("%.1f", round(xt$m2_w[xt$parm %in% c("Nsuper", "N1", "N2", "N3",
2538  "N4",
2539                                               "N5", "N6", "N7")], 1))
2540  xt$m2_w[!(xt$parm %in% c("Nsuper", "N1", "N2", "N3", "N4", "N5", "N6",
2541  "N7"))] <-
2542    sprintf("%.3f", round(as.numeric(xt$m2_w[!(xt$parm %in% c("Nsuper",
2543  "N1", "N2",
2544                                               "N3", "N4", "N5", "N6",
2545  "N7"))]), 3))
2546
2547  xt$m3_cov <- sprintf("%.1f", round(xt$m3_cov*100, 1))
2548  xt$m3_w[xt$parm %in% c("Nsuper", "N1", "N2", "N3", "N4", "N5", "N6",
2549  "N7")] <-
2550    sprintf("%.1f", round(xt$m3_w[xt$parm %in% c("Nsuper", "N1", "N2", "N3",
2551  "N4",
2552                                               "N5", "N6", "N7")], 1))
```

```r
2553   xt$m3_w[!(xt$parm %in% c("Nsuper", "N1", "N2", "N3", "N4", "N5", "N6",
2554   "N7"))] <-
2555     sprintf("%.3f", round(as.numeric(xt$m3_w[!(xt$parm %in% c("Nsuper",
2556   "N1", "N2",
2557                                                   "N3", "N4", "N5", "N6",
2558   "N7"))]), 3))
2559
2560   xt$parm[seq(2,40,2)] <- NA
2561
2562   xt$d_cov[seq(2,40,2)] <- paste0("(", xt$d_cov[seq(2,40,2)], ")")
2563   xt$d_w[seq(2,40,2)] <- paste0("(", xt$d_w[seq(2,40,2)], ")")
2564   xt$m1_cov[seq(2,40,2)] <- paste0("(", xt$m1_cov[seq(2,40,2)], ")")
2565   xt$m1_w[seq(2,40,2)] <- paste0("(", xt$m1_w[seq(2,40,2)], ")")
2566   xt$m2_cov[seq(2,40,2)] <- paste0("(", xt$m2_cov[seq(2,40,2)], ")")
2567   xt$m2_w[seq(2,40,2)] <- paste0("(", xt$m2_w[seq(2,40,2)], ")")
2568   xt$m3_cov[seq(2,40,2)] <- paste0("(", xt$m3_cov[seq(2,40,2)], ")")
2569   xt$m3_w[seq(2,40,2)] <- paste0("(", xt$m3_w[seq(2,40,2)], ")")
2570
2571   tabS1 <- data.frame(xt[,c(1,3:10)])
2572   tabS1$parm[1] <- "$N_{super}$"
2573   tabS1$parm[3] <- "$N_{1}$"
2574   tabS1$parm[5] <- "$N_{2}$"
2575   tabS1$parm[7] <- "$N_{3}$"
2576   tabS1$parm[9] <- "$N_{4}$"
2577   tabS1$parm[11] <- "$N_{5}$"
2578   tabS1$parm[13] <- "$N_{6}$"
2579   tabS1$parm[15] <- "$N_{7}$"
2580   tabS1$parm[17] <- "$\\lambda_1$"
2581   tabS1$parm[19] <- "$\\lambda_2$"
2582   tabS1$parm[21] <- "$\\lambda_3$"
2583   tabS1$parm[23] <- "$\\lambda_4$"
2584   tabS1$parm[25] <- "$\\lambda_5$"
2585   tabS1$parm[27] <- "$\\lambda_6$"
2586   tabS1$parm[29] <- "$f_1$"
2587   tabS1$parm[31] <- "$f_2$"
2588   tabS1$parm[33] <- "$f_3$"
2589   tabS1$parm[35] <- "$f_4$"
2590   tabS1$parm[37] <- "$f_5$"
2591   tabS1$parm[39] <- "$f_6$"
2592
2593   #----------------------------------------------------------------------------------------------------------------
2594   ----
2595   # Create Table S1
2596   kbl(tabS1, format = "pipe", booktabs = TRUE, caption = "Table S1. 95\\%
2597   credible interval coverage and widths [mean (sd)] for discrete (d) and
2598   marginalized (m1, m2, and m3) JS models applied to 100 simulated data sets
2599   that differed with respect to how abundance (N), population change, and
2600   recruitment are estimated.", col.names = c("", "\\% coverage", "Width",
2601   "\\% coverage", "Width", "\\% coverage", "Width", "\\% coverage",
2602   "Width"), align = "c") %>%
2603     add_header_above(header = c(" ", "d" = 2, "m1" = 2, "m2" = 2, "m3" = 2))
```

```
2604    # note that "add_header_above() not working when knitting document to Word.

2605    #--------------------------------------------------------------------------
2606    ---

2607    # Create Figure S1

2608    library(fields)
2609    library(wesanderson)
2610
2611    par(family = "serif", mfrow=c(3,1), mar = c(4,5,0,3))
2612    # in response to review, ad hoc y-axis split, Nsuper shown on right
2613    d.meds$Nsuper <- d.meds$Nsuper - 100
2614    m1.meds$Nsuper <- m1.meds$Nsuper - 100
2615    m2.meds$Nsuper <- m2.meds$Nsuper - 100
2616    m3.meds$Nsuper <- m3.meds$Nsuper - 100
2617
2618    bplot(d.meds[,c(18:24,2)], use.cols = TRUE, outline = FALSE, staplewex=0,
2619    col= wes_palette("Royal1")[1],
2620          boxwex=.15, lty=1, pos = seq(from=.5, by=2, length=8), xaxt="n",
2621    yaxt="n", ylab = "Abundance (N)",
2622          xlim=c(0,16), ylim=c(50, 400), las=1, cex.lab=1.25, cex.axis=1)
2623    axis(2, at = c(100, 150, 200), las=1, cex.axis=1.25)
2624    axis(4, at = c(300, 350, 400), labels = c(400, 450, 500), las=1,
2625    cex.axis=1.25)
2626    abline(h=225, lty=2, col="gray")
2627    bplot(m1.meds[,c(18:24,2)], use.cols = TRUE, outline = FALSE, staplewex=0,
2628    col= wes_palette("Royal1")[2],
2629          boxwex=.15, lty=1, pos = seq(from=.83, by=2, length=8), las=1,
2630    xaxt="n", yaxt="n", add=TRUE)
2631    bplot(m2.meds[,c(18:24,2)], use.cols = TRUE, outline = FALSE, staplewex=0,
2632    col= wes_palette("Royal1")[3],
2633          boxwex=.15, lty=1, pos = seq(from=1.17, by=2, length=8), las=1,
2634    xaxt="n", yaxt="n", add=TRUE)
2635    bplot(m3.meds[,c(18:24,2)], use.cols = TRUE, outline = FALSE, staplewex=0,
2636    col= wes_palette("Royal1")[4],
2637          boxwex=.15, lty=1, pos = seq(from=1.5, by=2, length=8), las=1,
2638    xaxt="n", yaxt="n", add=TRUE)
2639    bplot(data.frame(136, 139, 141, 143, 144, 145, 145, 300), xaxt="n",
2640    yaxt="n",
2641          use.cols = TRUE, boxwex=.8, border= "red", las=1, pos = seq(from=1,
2642    by=2, length=8),
2643          add=TRUE)
2644    axis(1, at = c(1,3,5,7,9,11,13,15), labels = c(expression(N[1]),
2645    expression(N[2]), expression(N[3]), expression(N[4]), expression(N[5]),
2646    expression(N[6]), expression(N[7]), "Nsuper"), cex.axis=1)
2647    legend("top", legend = c("d", "m1", "m2", "m3" ), fill =
2648    wes_palette("Royal1"),
2649          bty="n")
2650    title(main = "a", line=-1, adj=0.01, cex.main=1.5)
2651
2652    bplot(d.meds[,25:30], use.cols = TRUE, outline = FALSE, staplewex=0, col=
2653    wes_palette("Royal1")[1],
2654          boxwex=.15, lty=1, pos = seq(from=.5, by=2, length=6), xaxt="n",
```

```r
2655         ylab = expression(paste("Population change (", lambda, ")"),
2656 sep=""),
2657         xlim=c(0,12), ylim = c(0.2, 1.7), las=1, cex.lab=1.25, cex.axis=1)
2658 bplot(m1.meds[,25:30], use.cols = TRUE, outline = FALSE, staplewex=0, col=
2659 wes_palette("Royal1")[2],
2660         boxwex=.15, lty=1, pos = seq(from=.83, by=2, length=6), las=1,
2661 xaxt="n", add=TRUE)
2662 bplot(m2.meds[,25:30], use.cols = TRUE, outline = FALSE, staplewex=0, col=
2663 wes_palette("Royal1")[3],
2664         boxwex=.15, lty=1, pos = seq(from=1.17, by=2, length=6), las=1,
2665 xaxt="n", add=TRUE)
2666 bplot(m3.meds[,25:30], use.cols = TRUE, outline = FALSE, staplewex=0, col=
2667 wes_palette("Royal1")[4],
2668         boxwex=.15, lty=1, pos = seq(from=1.5, by=2, length=6), las=1,
2669 xaxt="n", add=TRUE)
2670 bplot(data.frame(E_lam[1], E_lam[2], E_lam[3], E_lam[4], E_lam[5],
2671 E_lam[6]), xaxt="n",
2672         use.cols = TRUE, boxwex=.8, border= "red", las=1, pos = seq(from=1,
2673 by=2, length=6),
2674         add=TRUE)
2675 axis(1, at = c(1,3,5,7,9,11), labels = c(expression(italic(lambda[1])),
2676
2677 expression(italic(lambda[2])),
2678
2679 expression(italic(lambda[3])),
2680
2681 expression(italic(lambda[4])),
2682
2683 expression(italic(lambda[5])),
2684
2685 expression(italic(lambda[6]))), cex.axis=1)
2686 title(main="b", line=-1, adj=0.01, cex.main=1.5)
2687
2688
2689 bplot(d.meds[,12:17], use.cols = TRUE, outline = FALSE, staplewex=0, col=
2690 wes_palette("Royal1")[1],
2691         boxwex=.15, lty=1, pos = seq(from=.5, by=2, length=6), xaxt="n",
2692         ylab = "Recruitment (f)",
2693         xlim=c(0,12), ylim = c(0, 1), las=1, cex.lab=1.25, cex.axis=1)
2694 bplot(m1.meds[,12:17], use.cols = TRUE, outline = FALSE, staplewex=0, col=
2695 wes_palette("Royal1")[2],
2696         boxwex=.15, lty=1, pos = seq(from=.83, by=2, length=6), las=1,
2697 xaxt="n", add=TRUE)
2698 bplot(m2.meds[,12:17], use.cols = TRUE, outline = FALSE, staplewex=0, col=
2699 wes_palette("Royal1")[3],
2700         boxwex=.15, lty=1, pos = seq(from=1.17, by=2, length=6), las=1,
2701 xaxt="n", add=TRUE)
2702 bplot(m3.meds[,12:17], use.cols = TRUE, outline = FALSE, staplewex=0, col=
2703 wes_palette("Royal1")[4],
2704         boxwex=.15, lty=1, pos = seq(from=1.5, by=2, length=6), las=1,
2705 xaxt="n", add=TRUE)
2706 bplot(data.frame(E_f[1], E_f[2], E_f[3], E_f[4], E_f[5], E_f[6]),
2707 xaxt="n",
2708         use.cols = TRUE, boxwex=.8, border= "red", las=1, pos = seq(from=1,
```

```r
2709    by=2, length=6),
2710            add=TRUE)
2711    axis(1, at = c(1,3,5,7,9,11), labels = c(expression(italic(f[1])),
2712                                              expression(italic(f[2])),
2713                                              expression(italic(f[3])),
2714                                              expression(italic(f[4])),
2715                                              expression(italic(f[5])),
2716                                              expression(italic(f[6]))),
2717    cex.axis=1)
2718    title(main="c", line=-1, adj=0.01, cex.main=1.5)

2719    #-------------------------------------------------------------------------
2720    ---

2721    # Create Figure S2

2722
2723    js.out.marg[[5]]$mps100 <-
2724    js.out.marg[[5]]$rt/js.out.marg[[5]]$min.ess*100
2725    js.out.marg[[5]]$mps1000 <-
2726    js.out.marg[[5]]$rt/js.out.marg[[5]]$min.ess*1000

2727
2728    par(family = "serif", mfrow=c(1,1), mar = c(4,5,0,0)) # family = "CM
2729    Roman",
2730    boxplot(js.out.marg[[5]]$mps1000 ~ js.out.marg[[5]]$model, log = 'y',
2731    xlab= "Model",
2732            ylab = "Time to 1000 effective samples (min)",
2733            xaxt= "n", yaxt="n", outline=FALSE, lty=1, staplewex=0)
2734    axis(2, at = c(0, 0.1, 1, 10, 100), las = 1)
2735    axis(1, at = c(1, 2, 3, 4), labels = c("d", "m1", "m2", "m3"), las = 1)

2736
```