

1 **Attention rhythmically shapes sensory tuning**

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16 **Conflict of interest**

17 The authors declare no competing financial interests.

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24 **Summary**

25 The rhythmic sampling theory of attention, stating that attention periodically samples
26 information at low frequencies (<20Hz), has become an important topic of research¹⁻⁴, with a
27 surge of studies finding rhythmic fluctuations of behavioral performance (reaction time, d-
28 prime, accuracy) in various sensory modalities (vision⁵⁻⁹, audition^{10,11}, somatosensation¹²) and
29 types of behavioral response (finger, hand, arm, eye movements¹³⁻¹⁵). Yet, the existence, and
30 thus, functional significance of such rhythmic behavior remains largely debated, due to a
31 combination of complex and controversial methodological procedures, as well as the lack of
32 understanding of the functional (sensory) mechanism underlying such rhythms. Here, we
33 specifically assess the link between behavioral rhythms and sensory representations. In a ~22-
34 hour behavioral experiment, participants (n=15) performed a dual task in which covert, spatial
35 (sustained and exploratory) attention was manipulated, and then probed at various delays
36 during the task. Our results show that sustained attention samples information periodically at
37 ~12Hz (alpha), while exploratory attention reorients from one stimulus to another at ~6Hz
38 (theta). Critically, reverse correlation analyses¹⁶⁻²⁰ show that the alpha sustained-attention
39 rhythm reflects both increased suppression of distracting features and increased gain to task-
40 relevant stimulus feature (orientation). Together these two processes keep the influence of
41 relevant stimulus information constant over time while improving performance (periodically) via
42 noise reduction. The theta exploratory-attention rhythm, however, is only associated with
43 changes in the gain around the task-relevant stimulus feature. Our study goes beyond rhythms
44 quantification and demonstrates how attention rhythmically shapes sensory representations.

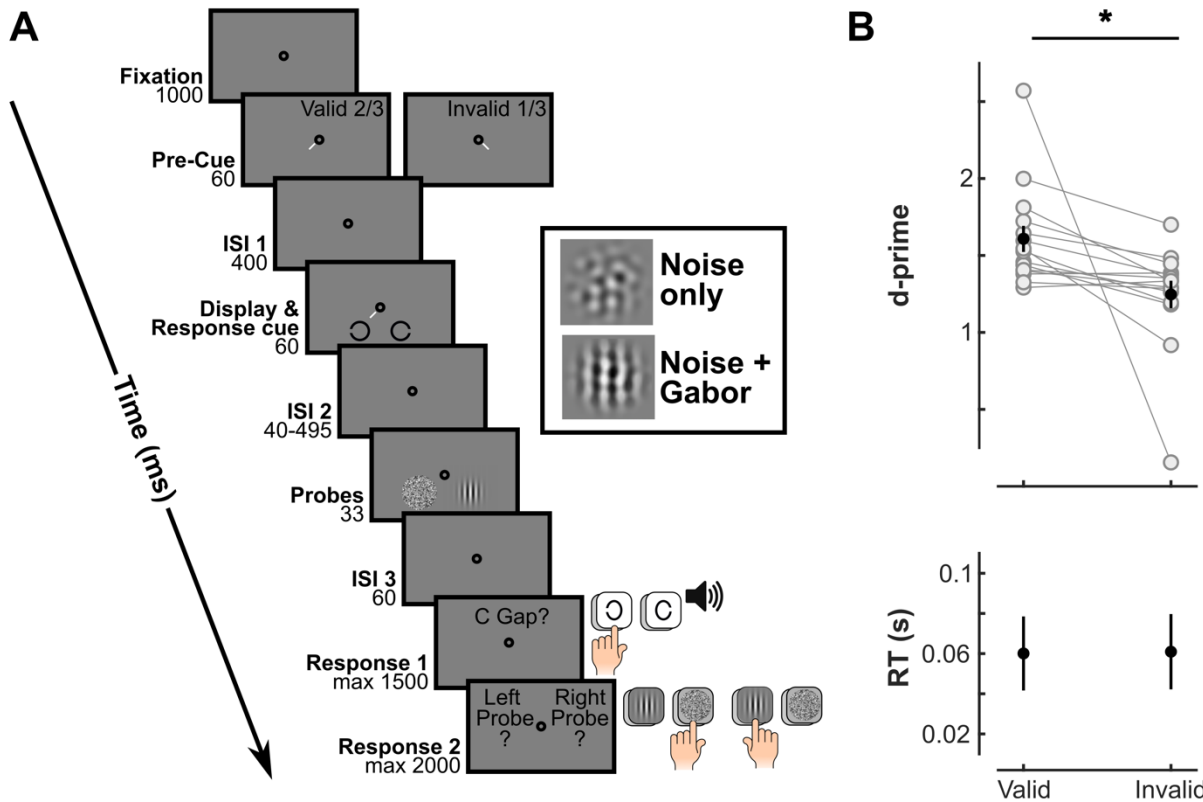
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46 **Keywords**

47 Alpha, Attention, Behavioral rhythms, Gain, Noise suppression, Sensory representations,
48 Theta

49 **Results**

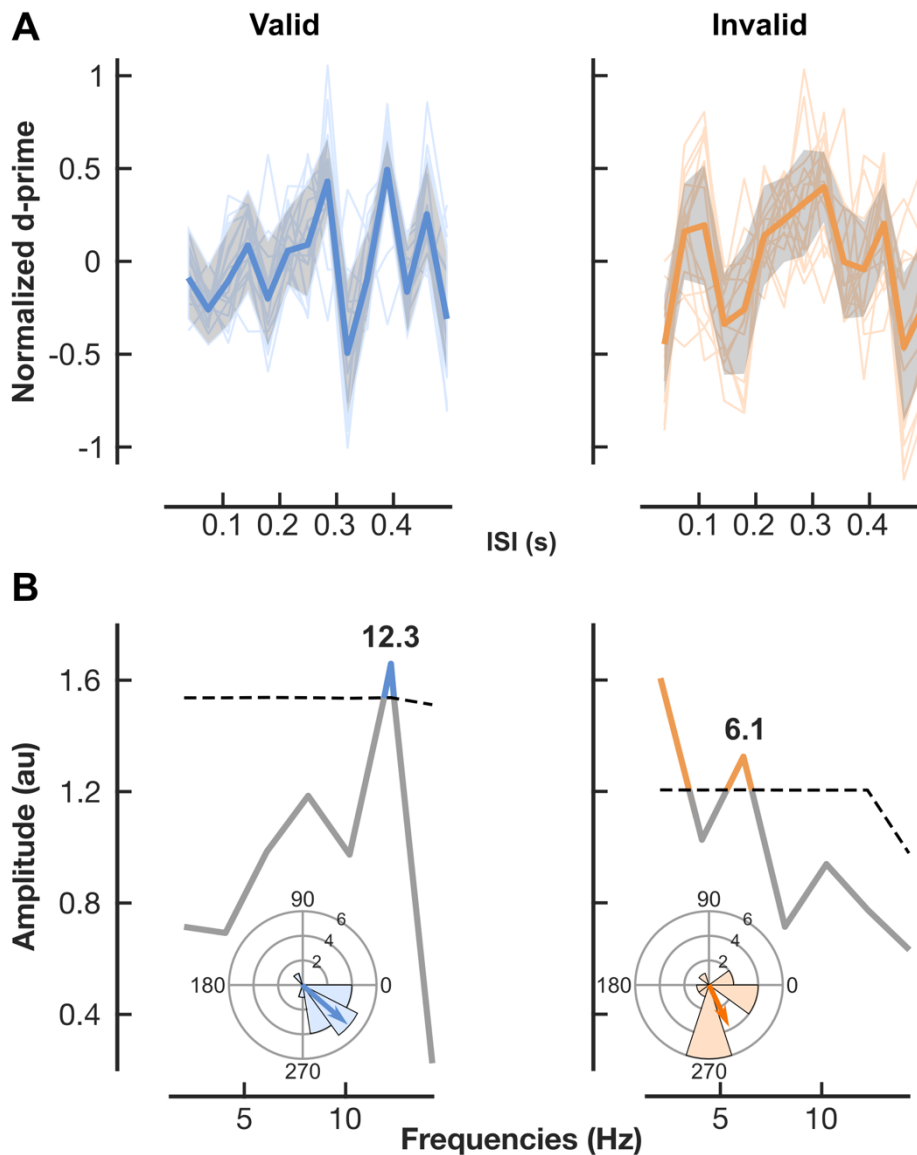
50 Attention allows selective facilitation of sensory information processing, efficiently allocating
51 resources based on task demands^{21–23}. When voluntarily deployed, (endogenous) attention's
52 influence on perception and behavior can be sustained at will, benefiting performance for long
53 periods of time. Although this classic understanding of sustained attention is well established,
54 a growing body of evidence converges toward a more complex dynamic: attention periodically
55 samples information, across both time and spatial locations^{1–4}. Specifically, rhythmic
56 fluctuations in performance due to attention suggest that sensory information processing
57 alternates between periods of greater (when in the attention spotlight) and lesser (when
58 outside) facilitation. This view has been recently challenged^{3,4,24–27} notably based on
59 considerations regarding protocols (e.g., low number of trials²⁷, low sampling frequency
60 resolution³ and analysis procedures²⁶; but see^{25,28,29}). Additionally, there remains a lack of
61 evidence for the specific sensory mechanism underlying variations in behavioral performance.
62 Here we address these issues by designing a protocol for measuring periodic fluctuations of
63 attentional performance in individual participants (with a large number of trials), and using an
64 analysis procedure well-suited to assess potential fluctuations in sensory representations.



65
 66 **Figure 1. Attentional manipulation. (A) Trial Sequence.** Trials began with a central fixation
 67 period of 1000ms. An endogenous pre-cue appeared for 60ms. After 400ms, Landolt-Cs were
 68 displayed for 60ms together with a response cue indicating which Landolt-C was the target
 69 (2/3 of Valid trials, i.e., target at pre-cued location). Each Landolt-C could be oriented to the
 70 right or to the left randomly. After a variable delay from 40ms to 495ms (35ms step; only the
 71 fixation circle remained on the screen), two patches were presented for 33ms at the same
 72 location as the Landolt-C. Each patch could either show noise only (1/2 of trials) or noise +
 73 Gabor (1/2). After a third ISI of 60ms, participants were instructed to report: (1) the orientation
 74 of the target Landolt-C (right/left; discrimination task), and (2) the presence or absence of a
 75 Gabor in each of the two patches. **(B) Behavioral results of the discrimination task.** Individual
 76 (gray) and averaged (black) d-primes and median reaction times (RT) in the valid and invalid
 77 conditions. Error bars: standard error of the mean. *: significant difference between valid and
 78 invalid trials ($p=0.034$).

79 We used a well-established psychophysics protocol (**Figure 1A**) tailored to identifying rhythms
 80 in attentional tasks^{8,30,31} (for review³). Covert, voluntary attention was manipulated using a pre-
 81 cue (2/3 validity). Participants ($n=15$) were instructed to first perform a discrimination task (by
 82 indicating the side of the gap, left or right, of a target Landolt-C) allowing us to confirm that
 83 attention was successfully manipulated and deployed to the cued location (**Figure 1B**). D-
 84 prime was significantly higher for valid (target at the cued location) than invalid (target at the
 85 uncued location) trials (paired-sample two-tailed t-test: $t(14) = 2.34$, $p\text{-value} = 0.034$, Cohen's
 86 $d = -1.07$). Reaction times were similar for valid and invalid trials ($t(14) = -0.83$, $p\text{-value} = 0.418$,
 87 Cohen's $d = 0.02$), indicating no speed-accuracy trade-off.

88 In the same trial, after a variable delay, participants were presented with a second target, on
89 which they were asked to perform a detection task reporting the presence or absence of a
90 vertical Gabor embedded in band-passed noise. The noise had random orientation content,
91 drawn from a uniform distribution across all orientations -90 to +90 degrees (polar angle) and
92 a spatial frequency of 3 cycles per degree (cpd). On half of the trials, a Gabor (3 cpd sinusoidal
93 grating in an envelope subtending 2°; oriented vertically) was embedded in the noise patch.
94 This second task was used to probe attention at each of the two stimulus locations and at
95 various times during attentional orienting (valid trials; sustained attention) and reorienting
96 (invalid; exploratory attention), assessing potential rhythms in attentional sampling.
97 We computed d-primes for this detection task independently for the valid and invalid conditions
98 and for each ISI between the discrimination and probes onset. Across ISIs, d-prime exhibited
99 multiple peaks and troughs, and individual data makes clear this was highly consistent across
100 participants (**Figure 2A**). We then performed fast-fourier transforms (FFT) of the averaged d-
101 primes for the valid and invalid conditions separately. Peak frequencies were identified: 12.3Hz
102 in valid and 6.1Hz in invalid (permutations tests: 100,000 surrogates, $p = 0.05$; **Figure 2B**).
103 Note that in the invalid condition, an additional significant peak frequency was observed at
104 2.04Hz reflecting the inverted U-shape trend (no detrending was performed here, see^{7,31}; we
105 did not analyze it further). We also showed that the 12.3Hz (for the valid condition) and 6.1Hz
106 (for the invalid) individual periodic modulations were in phase across participants (Rayleigh
107 tests for circular data showed significant non-uniform distributions for both valid: $Z = 9.75$, $p =$
108 9.04×10^{-6} ; and invalid: $Z = 4.22$, $p = 0.012$).



109

110 **Figure 2. Behavioral rhythms.** (A) Individual (light traces) and averaged (dark traces) d-prime
111 time-courses ($n=15$) for valid (blue) and invalid (orange) conditions separately. Shaded area:
112 95% confidence interval. (B) Amplitude spectra obtained from FFT of d-primes time course
113 averaged across participants. Dotted line: $p=0.05$ (permutation test). Polar histogram of
114 individual phases (light bins) and weighted phase averages (arrows) at 12.3Hz in the valid
115 condition and 6.1Hz in the invalid condition.

116 For valid and invalid conditions separately, we split the ISI into low- and high-performance ISIs.

117 ISIs corresponding to d-prime local maxima (and which were above the averaged d-prime time-

118 courses) were categorized as *high-performance* and ISIs corresponding to d-prime local

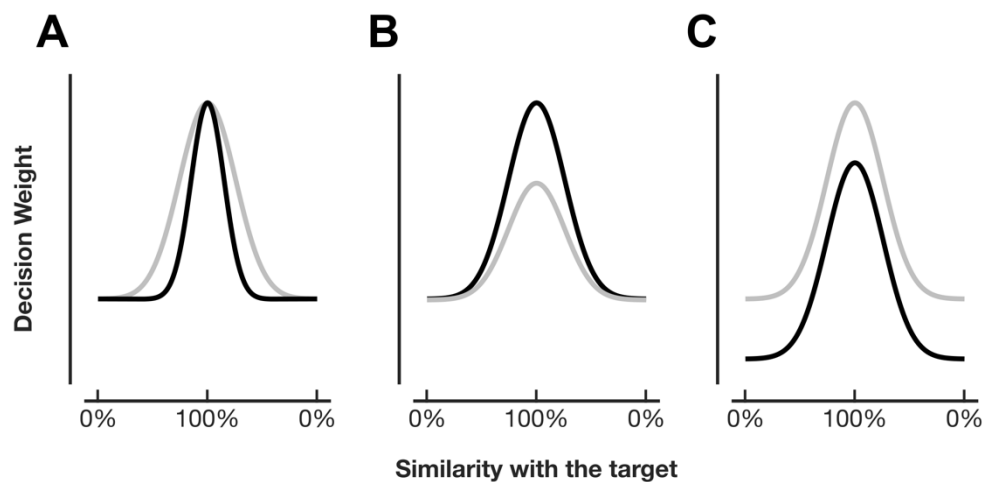
119 minima (and which were below the average) were categorized as *low-performance*. We then

120 combined all high-performance trials (coming from 4 different ISIs in valid: 145, 285, 390 and

121 460ms; 3 ISIs in invalid: 110, 320 and 425ms) and low-performance trials (5 ISIs in valid: 75,

122 180, 320, 425 and 495ms; 4 ISIs in invalid: 40, 145, 390 and 460ms) for the next analysis.

123 Subsampling (100 repetitions) was performed to equalize the number of trials between valid
124 and invalid, and high- and low-performance conditions. This trial separation was then used to
125 assess modulations in sensory representations using reverse correlation analysis.
126 Fluctuations in sensitivity (d-prime) suggest a modification of sensory representations over
127 time, such that high performance should be associated with more optimal sensory tuning
128 compared to low performance. Here we assess which characteristics of sensory
129 representations varied. If sensory tuning is modeled as a Gaussian distribution across
130 orientations (**Figure 3**), tuning can vary via differences in: **(A)** tuning sharpness or variance:
131 for high-performance trials, the perception would present a sharper tuning to the relevant
132 elements for the task; **(B)** gain or amplitude: for high-performance trials, there would be a
133 higher gain for the relevant information for the task; and **(C)** suppression or baseline shift: for
134 high-performance trials, there would be a decrease in the baseline, i.e., suppression of
135 irrelevant information for the task.

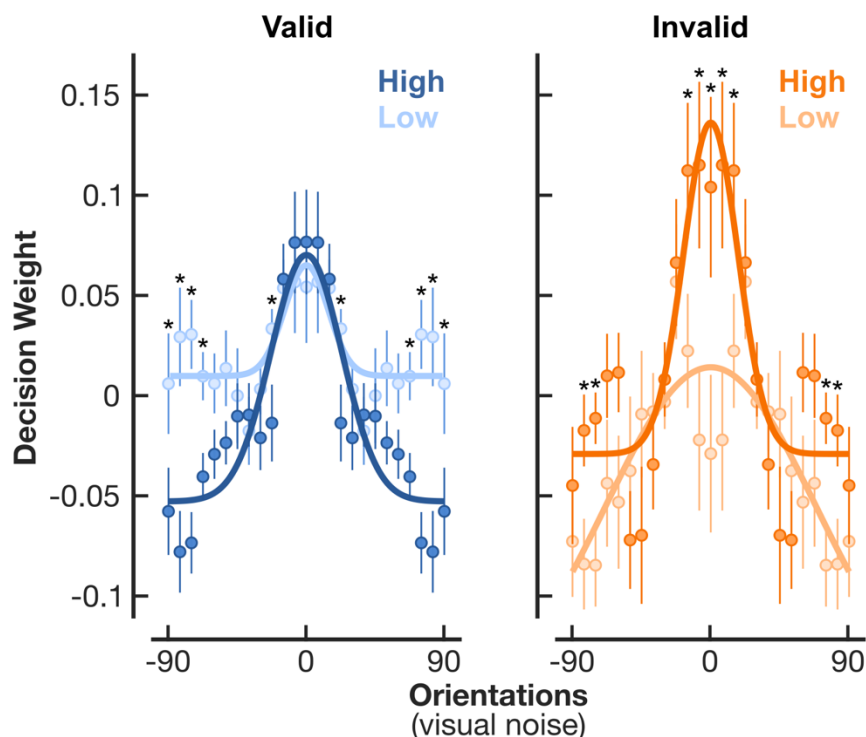


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137 **Figure 3. Sensory tuning hypotheses.** Gaussian model of participant's sensory tuning.
138 Sensory representations are different during phases of high (black traces) versus phases of
139 low (gray traces) performance. Modifications in the **(A)** tuning sharpness, **(B)** tuning amplitude
140 **(gain)**, **(C)** tuning baseline.

141 Reverse correlation of behavioral performance (see **STAR Methods**) allowed testing of these
142 three hypotheses, separately for each attention condition – sustained (valid) and exploratory
143 (invalid). To infer the underlying sensory representation from the behavioral responses, we
144 regressed the stimulus energy (i.e., visual resemblance of the noise to a range of orientation
145 values) across trials –separately for high- and low-performance trials– with each participant's

146 responses using a binomial regression. This provided a sensitivity kernel for each orientation,
147 i.e., β (or decision) weight, representing the level of correlation between the proportion of trials
148 reporting “Target Present” and the energy of that particular orientation in the noise of the
149 stimulus (**Figure 4**; Note that decision weights were averaged for positive and negative
150 orientations). A high decision weight indicates a high correlation, suggesting that more energy
151 for the orientation value in question within the noise positively influenced the likelihood of
152 “Target Present” responses. The results first show that the highest decision weights were
153 observed for orientation corresponding to the target grating orientation (0° ; peak of the
154 Gaussian). For each orientation, a paired t-test on the difference between high- and low-
155 performance trials’ decision weights was then computed and Bonferroni corrected for 13
156 comparisons (p-threshold Bonferroni corrected = 0.0038; positive and negative orientation
157 results were averaged). We observed significant differences for the values far from the target
158 orientation mainly in the valid condition, and for near-target values in the invalid condition.



159

160 **Figure 4: Decision weight from reverse correlation for valid and invalid trials.** Dark
161 traces: high-performance trials. Light traces: low-performance trials. Circles: average weight
162 across participants of the correlation between energy at each orientation (averaged across
163 positive and negative orientations) and participant’s response using a GLM. Error bars: 95%
164 confidence interval. Solid lines: Gaussian fit. *: significant difference between high- and low-
165 performance (p-threshold Bonferroni corrected = 0.0038).

166 We then fitted a single gaussian curve –the tuning curve– to the 25 decisions weights (1 per
167 orientation; see **STAR methods**). To identify the changes in tuning that accompany periodicity
168 in d-prime, we compared, across participants, the three following free parameters in the tuning
169 fits: standard deviation (SD), amplitude and baseline, between high-performance and low-
170 performance trials, separately for the valid and invalid conditions. There was no significant
171 difference between high- and low-performance trials in both valid and invalid conditions for the
172 SD (valid: $t(14) = 1.14$, $p = 0.274$ estimate = 9.27 ± 8.14 , standard error; invalid: $t(14) = -0.12$,
173 $p = 0.903$, estimate = -1.07 ± 8.71). Amplitude was significantly higher in high- compared to
174 low-performance trials in both valid and invalid conditions (valid: $t(14) = -3.76$, $p = 0.002$,
175 estimate = -0.08 ± 0.02 ; invalid: $t(14) = -4.23$, $p = 0.001$, estimate = -0.11 ± 0.03). Baseline
176 was significantly lower in high- compared to low-performance trials for the valid condition only
177 (valid: $t(14) = 6.96$, $p = 0$, estimate = 0.07 ± 0.01 ; invalid: $t(14) = -1.51$, $p = 0.153$, estimate = -
178 0.03 ± 0.02). These results suggest that, in the valid condition, when the attention was
179 sustained at one location, the performance fluctuation at alpha frequency is mediated by
180 rhythmic enhancement (gain) of relevant features and suppression of distracting features
181 (baseline) (**Figure 3**, hypotheses B and C); whereas, in the invalid condition, when attention
182 had to explore the space, we observed fluctuation at theta frequency mediated exclusively by
183 a rhythmic change in enhancement (gain) of relevant features (**Figure 3**, hypothesis B).

184

185 **Discussion**

186 The rhythmic sampling theory of attention has become an important topic of research, yet
187 remains largely debated due to methodological considerations, as well as a lack of clear
188 understanding regarding the sensory mechanism underlying performance fluctuations. Here
189 we addressed this critical gap using a psychophysics paradigm with a large amount of data
190 collected for each participant, and applying reverse correlation analysis correlating stimulus
191 energy of irrelevant noise with behavioral detection performance. We assessed the fluctuations
192 in sensory representations for two voluntary attention modes, i.e., sustained and exploratory.

193 First, we showed that performance fluctuated periodically at the alpha frequency (12.3Hz) for
194 sustained attention and theta frequency (6.1Hz) for exploratory attention, replicating previous
195 reports^{8,9,32,33}. Such effects were further observed for each individual participant. Second,
196 reverse correlation analysis revealed differences in feature tuning across time between the two
197 attention modes. Sustained attention displayed rhythmic suppression of distracting features
198 (while keeping the gain constant). Exploratory attention exclusively showed enhancement
199 (gain) of relevant features. Together, these results confirm attention-specific rhythms of
200 behavioral performance, and go beyond by demonstrating specific underlying sensory
201 mechanisms.

202 Previous decades of attention research have concentrated on the general effects of attention
203 on perceptual performance and showed a wealth of evidence for both signal enhancement of
204 task-relevant stimulus features and external noise reduction. Authors have notably
205 demonstrated that attention can enhance signals through contrast gain (e.g.,³⁴⁻³⁷), response
206 gain (e.g.,^{36,37}), orientation sensitivity gain (e.g.,^{35,38}), spatial resolution gain (e.g.,³⁹⁻⁴²) or
207 information processing speed gain (e.g.,⁴³). Such enhancement could occur for targets
208 presented below, above or at threshold. Similarly, active suppression of irrelevant information,
209 also called external noise reduction, would occur both for targets presented suprathreshold
210 and near-threshold⁴⁴⁻⁵¹. Given the accumulated evidence for both attentional mechanisms
211 (enhancement and suppression), they are almost certainly not mutually exclusive. Doshier and
212 Lu⁵² indeed showed that either mechanism can arise in the same task under different levels of
213 task difficulty: with fewer distractor locations or low external noise, there is a stronger signal
214 enhancement effect; and with more distractor locations or higher external noise, there is a
215 stronger external noise reduction effect. Others have also argued that which of the two
216 mechanisms is engaged depends on the type of attention deployed. For instance, while
217 endogenous (voluntary) attention is more often linked to external noise reduction, exogenous
218 (involuntary) attention is linked to both external noise reduction and signal enhancement⁵³.

219 Here we used reverse correlation of behavioral performance to assess feature tuning across
220 time and attention modes, which d-prime measures alone are not directly capable of. While

221 signal enhancement was observed for both sustained and exploratory attention modes, the
222 suppression of irrelevant features, analogous to external noise reduction, was only observed
223 for sustained attention. Specifically, when attention was directed to the target location –valid
224 condition– attention suppressed irrelevant features far from the target orientation (baseline
225 shift), and then compensated with an increase in gain (amplitude). This resulted in equal
226 decision weights at and near the target feature for both high- and low-performance phases of
227 d-prime sensitivity, but lower decision weights far from the target orientation. In other words,
228 when attention is oriented and sustained at a target location, alpha rhythms in performance
229 are primarily due to fluctuations in the suppression of irrelevant stimulus features –
230 advantageous suppression at peaks and poorer suppression at troughs– while a gain
231 mechanism keeps the influence of relevant stimulus information constant over time. When
232 attention is instead reoriented from an irrelevant location to a relevant one –invalid condition–
233 theta rhythms in behavioral sensitivity are associated only with changes in the amplitude of the
234 tuning function, most strongly influencing sensitivity around the target feature, such that high-
235 performance phases have higher decision weights at orientations close to target feature
236 compared to low-performance phases.

237 Notably, we found external noise reduction and signal enhancement in separate modes of
238 voluntary spatial attention –sustained and exploratory, respectively–, while difficulty remained
239 constant, as both attention conditions shared the same number of targets, locations, and
240 distractors, as well as the same level of stimulus noise. We speculate that the pattern of our
241 findings is related to the distinct functional roles of the sustained and exploratory modes of
242 attention. In other words, because attention efficiently allocates resources based on task
243 demands^{21–23}, finding distinct behavioral tradeoffs during different modes of attention suggests
244 the two modes have distinct roles in aiding perception and performance. On the one hand,
245 when attention shifts from one location to another, i.e., attention is exploring space, signal
246 enhancement of the most relevant features may aid in locating the target, which is necessary
247 before it can be examined and discriminated. On the other hand, when attention is sustained
248 on a single location, i.e., the target location has already been identified, perception is enhanced

249 via external noise reduction, as it is no longer necessary to find the target via signal
250 enhancement.

251 Further, the particular frequency of either sensory tuning modulation may be related to their
252 corresponding attention modes' respective functional roles (see reviews^{3,33}). Alternatively,
253 sensory mechanism may operate necessarily at a particular frequency due to metabolic or
254 neural processing constraints. The link between attention mode, the respective frequencies of
255 performance modulation, and the underlying sensory tuning mechanisms is a topic in need of
256 further investigation.

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404 **Methods**

405 **Participants**

406 Nineteen participants were recruited for this experiment (11 female, age $M \pm SD = 23.26 \pm$
407 3.80 years; range 18-31). Two participants were excluded from the analyses because they did
408 not complete the full experiment and two because they did not manage to perform the task. All
409 participants had normal or corrected-to-normal vision and reported no history of psychiatric or
410 neurological disorders, gave their written informed consent and were compensated for their
411 participation. All procedures were approved by the French ethics committee Ouest IV - Nantes
412 (IRB #20.04.16.71057) and followed the Code of Ethics of the World Medical Association
413 (Declaration of Helsinki).

414 **Apparatus and stimuli**

415 Participants sat in a dark room at 57cm from a calibrated and linearized CRT monitor (800*600
416 pixels, width = 37.8cm, height = 28.4cm, refresh rate 120Hz). Their heads were positioned on
417 a chin rest to maintain the distance between the monitor and the eyes. Stimuli were generated
418 using PsychToolbox 3 in Matlab R2018b (MathWorks). Background was gray (127.5, 127.5,
419 127.5 RGB). A black central fixation annulus with inner eccentricity of 0.2° (degree of visual
420 angle) and thickness of 0.16° was presented throughout the experiment. The cue and
421 response cue were white rectangles (255, 255, 255 RGB, 0.5° long, 0.16° large) adjacent to
422 the fixation (0.65° eccentricity from the center) and pointing down with a 45° angle toward the
423 bottom left or bottom right. Stimuli were two conventional Landolt-C optotypes (2° high, 2°
424 wide, 5.5° from the center at 45° angle toward the left or the right), and randomly generated
425 noise patches at the same locations (2° high, 2° wide; circular window) with or without
426 embedded Gabors (3 cycles per degree; circular window).

427 **Eye-tracking**

428 The dominant eye of each participant was monitored using an infrared video camera (EyeLink
429 1000 plus, SR Research, Ottawa, Canada). Participants were instructed to maintain fixation.
430 Trial started when they were fixating, and they had to maintain fixation until after the probe
431 presentation. If a fixation break occurred, i.e., if participants' gaze deviated by $>1.5^\circ$ or if they
432 blinked, the trial was stopped and removed from the analysis. Supernumerary trials were
433 added at the end of each block to compensate for rejected trials ($M \pm SD = 2257.73 \pm 1320.76$
434 fixation breaks total on average across participants).

435 **Procedure**

436 Participants performed a total of 22 sessions. First, in a 1h-training session they were
437 familiarized with the trial sequence at slower delays. They then performed two staircase blocks
438 (see below) in an additional 1h-session. They finally performed 20 1h-long sessions (over
439 several days) of the main task.

440 *Main task.* Each session was composed of 4 blocks of 126 trials each as well as
441 supernumerary trials in case of fixation break (see **Eye-tracking** section). Central fixation
442 remained on the screen during the entire block. After a 1000ms-stable fixation a pre-cue
443 appeared for 60ms followed by a 400ms-inter-stimulus interval (ISI). The two Landolt-Cs were
444 displayed for 60ms (one in each lower quadrant) along with a response cue indicating which
445 of the two was the target. Participants were instructed to discriminate the position of the C gap
446 (left/right) of the target Landolt-C (their response was collected at the end of the trial
447 sequence). When the target appeared at the cued location (2/3 of the trials), the trial was valid;
448 otherwise (1/3 of the trials) the trial was invalid. Then a second, variable ISI (randomly chosen
449 among 14 different possibilities equally distributed between 40ms and 495ms) preceded the
450 presentation of two new stimuli, i.e., two patches of noise or noise+Gabor for 33ms, at the
451 same location as the previous Landolt-Cs, followed by a 60ms delay. Participants were

452 instructed to detect the presence/absence of the Gabor inside each patch of noise (50%).
453 These patches presented at multiples delays after the previous Landolt-Cs were used to probe
454 the state of attention across time. At the end of the trial, participants were first asked to report
455 the position of the gap in the target Landolt-C (press C key for a gap on the left with the left
456 hand, and press B key for a gap on the right with the right hand; maximum response time of
457 1500ms), and then to report the presence or the absence of the Gabor inside each patch (for
458 left patch, press C key for Gabor present and D key for Gabor absent with left hand; for right
459 patch, press B key for Gabor present and H key for Gabor absent with right hand; maximum
460 response time 2000ms).

461 *Staircases*. Two independent staircases were implemented via a Best PEST procedure⁵⁴ using
462 the Palamedes toolbox⁵⁵ in Matlab, to adapt first the size of the Landolt-C gap in the
463 discrimination task, and second the SNR (signal- (Gabor) to-noise ratio) for the detection task.
464 In the first staircase (208 trials), only the discrimination task sequence was presented and the
465 size of the Landolt-Cs gap ($1.4 \pm 0.4^\circ$ on average across participants) was adjusted according
466 to a running-fit estimation (Best PEST) of the alpha parameter of a Weibull distribution,
467 corresponding to the gap-size threshold reaching between 70% and 80% performance
468 accuracy ($76 \pm 2.5\%$ across participants). Here the trial sequence consisted of a neutral pre-
469 cue (both the left and right cue) for 60ms, a 400ms-ISI and the Landolt-Cs together with the
470 response cue for 60ms. Participants had 1.5s to report the location of the gap. In the second
471 staircase (200 trials), the procedure was the same. Only the detection task sequence was
472 presented and the ratio between noise and Gabor was adapted to reach around 50%
473 performance ($28 \pm 6.9\%$ across participants; note that this staircase was not successful at
474 reaching 50% but there is no reason to presume this impacts the analysis). One trial consisted
475 of neutral pre-cue for 60ms, a 400ms-ISI and the 2 probe patches (50% noise only and 50%
476 noise+Gabor, at each location) with a response cue for 33ms. Participants had 2s to report the
477 presence or the absence of the Gabor in each of the two patches.

478 **Analysis**

479 *Behavioral rhythms.* All analyses were performed on subsampled trials (100 repetitions) to
480 equalize the number of valid trials to the number of invalid ones. For the discrimination task,
481 performance was evaluated as per d-prime in each cueing condition. We also checked reaction
482 times from Response 1 screen onset (**Figure 1**) to control for speed-accuracy trade-off. Paired
483 samples t-tests were performed to assess statistical differences between cueing conditions.

484 For the detection task, normalized d-primes were examined for each cueing (valid and invalid)
485 and ISI (delay between the Landolt-C and the probe patches) condition. Responses to both
486 patches were combined. In total, there were 720 trials per ISI and participant. Fast Fourier
487 Transform decompositions (FFT) were further performed on averaged d-primes to assess
488 possible periodicity. Phase angles were extracted from FFTs performed on each participants
489 data for 12.3Hz in valid and 6.1Hz in invalid. We selected high- and low-performance trials by
490 taking local maxima (above d-prime average) and minima (below d-prime average) for each of
491 the d-prime time courses (ISI Valid high: 145, 285, 390 and 460ms; low: 75, 180, 320, 425 and
492 495ms; ISI invalid high: 110, 320 and 425ms; low: 40, 145, 390 and 460ms). Two local maxima
493 were removed, one in each condition, because they were below the averaged d-primes. All
494 analyses described below were done separately for the high- and low-performance trials.

495 *Reverse Correlation analysis.* To perform this analysis, we subsampled (100 repetitions) the
496 number of high- (or low-) performance trials (separately for valid and invalid conditions) to
497 equalize to the number of low- (or high-) performance trials. To address behavioral feature
498 tuning, we first transformed the noise from luminance intensity into the energy of different
499 orientation components. We converted the noise image of each trial from pixel space
500 (luminance intensity of each pixel) to a 1D space defined by the noise energy of components
501 responding to different orientations (varied across all of orientation space, -90° to 90° , in steps
502 of 7.5° , for 25 points on a linear scale). To compute the energy of each component, we took

503 the noise image S of each trial, and convolved it with two grating filters ($g_{\theta, sin}$ in sine phase
504 and $g_{\theta, cos}$ in cosine phase) with the corresponding orientation. The energy was computed as:

$$(Eq1) \quad E_{\theta} = \sqrt{(S * g_{\theta, sin})^2 + (S * g_{\theta, cos})^2}$$

505 in which $*$ represents the cross-correlation operator. We took the energy centered at the test
506 stimulus (vertical orientation) for analysis. For each component with preferred orientation θ ,
507 we estimated the correlation between the energy of that component and behavioral responses
508 using a GLM to predict the binomial dependent variable:

$$(Eq2) \quad p(yes) = \psi(\beta_{\theta} E_{\theta}^* + b_{\theta})$$

509 in which $p(yes)$ was the percentage of yes responses in the detection task and ψ was a
510 cumulative normal distribution. Two free parameters β_{θ} and b_{θ} were fitted. β_{θ} represented the
511 correlation between the energy and the behavioral response. A zero β_{θ} indicated that the
512 energy of that component did not influence participants' responses. b_{θ} represented a baseline
513 tendency of the participants to respond "present" (i.e., false alarm rate), which was not related
514 to the stimuli. E_{θ}^* represented the centered and normalized energy of each component. Before
515 applying the GLM, the energy of each component was first sorted into two groups based on
516 whether the target signal was present or absent in each trial, and the mean of the energy was
517 removed for each group. Therefore, we only used the energy fluctuation of the noise relative
518 to the mean, and the energy used for analysis was centered at zero for both target-present
519 and target-absent trials. To let the estimated β_{θ} be comparable across components, we further
520 normalized the energy across all the trials in each component to have a standard deviation of
521 1. The estimated sensitivity kernel was a 1D matrix K in which $K(\theta) = \beta_{\theta}$. Before Gaussian
522 fitting, positive and negative orientations' energy were averaged.

$$(Eq3) \quad x[1] * \left(\exp\left(-\frac{(\text{ori} - x[2])^2}{2 * x[3]^2}\right) \right)^{x[4]} + x[5]$$

523 A Gaussian tuning curve was fit to the data (Eq3) for each condition, where ori represented all
524 noise orientation channels (25 orientations). As we were agnostic as to the precise shape of
525 the tuning function, in addition to the single fit (Eq3)—a simple, standard model of feature tuning

526 –a double Gaussian fit –a “Mexican hat” (Eq4) shape that sometimes arises due to attention⁵⁶–
527 was computed.

$$(Eq4) \quad x[1] * \left(\exp \left(-\frac{(ori - x[2])^2}{2 * x[3]^2} \right) \right)^{x[4]} + x[5] + x[6] * \left(\exp \left(-\frac{(ori - x[2])^2}{2 * x[7]^2} \right) \right)^{x[8]} + x[9]$$

528 AIC corrected (AICc) for small data samples were performed using Python (3.8.1)
529 independently for each condition to compare single and double Gaussian fits. AICc criterion
530 was computed as shown in (Eq5) where k was the number of parameters, L the maximized
531 value of the likelihood function and n the number of participants.

$$(Eq5) \quad 2k - 2 \ln(L) + \frac{2k(k + 1)}{n - k - 1}$$

532 For each condition, the single fit better explained the results (valid high-performance AICc
533 difference (single fit – double fit) = -18.9; valid low-performance AICc difference = -37.4; invalid
534 high-performance AICc difference = -37.3; invalid low performance AICc difference = -37.4).
535 All further analyses were thus performed with the tuning curve from the single fits.

536 We assessed the statistical differences between high- and low-performance trials’ tuning
537 curves using linear mixed model with R (4.2.2), and specifically, differences in the standard
538 deviation, amplitude and baseline of the tuning curves. Linear models were fitted by
539 maximizing the restricted log likelihood and using a normal distribution function. Performance
540 was used as predictor with 2 levels (high and low) and participants as random effect.

541 **Code Accessibility**

542 All data and analysis code are available on the OSF repository
543 (<https://doi.org/10.17605/OSF.IO/CXKBU>).