Genetic similarity between relatives provides evidence on the presence and history of assortative mating

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Abstract

Assortative mating – the non-random mating of individuals with similar traits – is known to increase trait-specific genetic variance and genetic similarity between relatives. However, empirical evidence is limited for many traits, and the implications hinge on whether assortative mating has started recently or many generations ago. Here we show theoretically and empirically that genetic similarity between relatives can provide evidence on the presence and history of assortative mating. First, we employed path analysis to understand how assortative mating affects genetic similarity between family members across generations, finding that similarity between distant relatives is more affected than close relatives. Next, we correlated polygenic indices of 47,135 co-parents from the Norwegian Mother, Father, and Child Cohort Study (MoBa) and found genetic evidence of assortative mating in eight out of fifteen examined traits. The same traits show elevated similarity between relatives, especially distant relatives. Five of the eight traits, including educational attainment, showed greater genetic variance among offspring, which is inconsistent with stable assortative mating over many generations. These results suggest an ongoing increase in familial similarity for these traits. The implications of this research extend to genetic methodology and the understanding of social and economic disparities.

Introduction

Assortative mating – the non-random pairing of individuals with similar traits – has long been a challenging topic of interest across various fields, including genetics[1-9], sociology[10-12], and economics[13,14]. Consequences of assortative mating are wide-ranging, affecting topics such as genetic research methods[15,16], relationship quality[10,17,18], and the perpetuation of social and economic inequalities[10,13,14]. Although partner similarity have been documented for numerous characteristics[15,16,19], it remains uncertain to what extent these similarities result from assortative mating or other processes, such as convergence over time[18,20]. Hence, the genetic consequences are unknown. Recent advances in data availability have enabled empirical investigation into the genetic consequences of assortative mating, wherein two are of key interest: First, partners should exhibit genetic similarity for assorted traits; and second, genetic similarity between relatives should increase for the assorted traits in subsequent generations[1-3]. In this paper, we aim to: 1) clarify the theoretical consequences of assortative mating on genetic similarity in extended families; 2) use polygenic indices to assess trait-specific genetic similarity between partners for a range of psychosocial, anthropometric, and health-related traits; 3) investigate whether these traits also exhibit increased genetic similarity among relatives; and 4) use the observed genetic similarity in mother-father-child trios to investigate the stability of assortative mating over many generations.

According to a recent meta-analysis, phenotypic correlations between partners exist for many traits[15]. The correlations are particularly high for cognitive and social traits like educational attainment (0.53) and political values (0.58), but moderate correlations exist for many diverse traits such as height (0.23), depression (0.14), and personality (0.08–0.21). Positive correlations between partners can arise from numerous processes, including convergence (partners becoming more alike over time due to mutual influence), common environments (partners originating from similar environments that affect their traits, but without influencing partner formation), and assortative mating (individuals tending to form partnerships with those having similar traits)[18]. If partner similarity arises because of assortative mating, then this will induce cross-partner correlations between the respective causes of the trait. If the trait is heritable – which most traits are[21,22] – then partners will tend to carry genetic variants with similar effects on the trait. Genetic similarity between partners has been documented for some traits, including height and educational attainment[6,19,23-25]. For example, Yengo, et al. [25] investigated genetic similarity in partners from the UK Biobank across 32 complex traits, but lack of statistical power left the question unresolved for most traits.

If assortative mating leads to genetic similarity between partners, then any resulting offspring are likely to inherit trait-specific genetic variants with similar effects from both parents. This has two important consequences: First, the trait-specific genetic variance in the population will increase because genetic variants with similar effects will tend to co-occur in the same individuals (i.e., variants will be in linkage disequilibrium)[3,8,26,27]. Second, trait-specific genetic similarity between relatives will increase because other family members are likely to inherit genetic variants with similar effects[1-4,8]. With no assortative mating, genotypic correlations between family members for a trait should correspond to the coefficient of relationship. For example, full siblings (not including monozygotic twins) and parent-offspring pairs are first-degree relatives, with a coefficient of 0.50; aunt/uncle-niece/nephew and grandparent-grandchild pairs are second-degree relatives, with a coefficient of 0.25; and first cousins are third-degree relatives, with a coefficient of 0.125. If assortative mating occurs, however, then the trait-

specific genotypic correlations would be higher than the corresponding coefficients of relationship. Importantly, assortative mating only induces correlations between trait-associated loci and should not be confused with inbreeding, which induces correlations between all loci[28]. With successive generations of stable assortative mating, trait-specific genetic variance and genotypic correlations between relatives increase asymptotically towards an equilibrium, at which point they become constant across generations[3,8,26,27]. We describe this in more detail in the supplementary information.

Whereas earlier theoretical papers have primarily focused on the consequences for phenotypic correlations at equilibrium, our focus is on genotypic correlations and correlations between polygenic indices at both equilibrium and disequilibrium. Our first aim is therefore to derive the expected genotypic correlations and polygenic index correlations using path analysis. In doing so, we establish a general formula for finding such correlations between any two extended family members under assortative mating at equilibrium. Our results imply that genetic similarity between distant relatives should be more affected by assortative mating than similarity between close relatives, which mirrors earlier work[1,3,29]. Our second aim is to document polygenic index correlations for various traits among partners from the Norwegian Mother, Father, and Child Cohort Study (MoBa)[30,31]. We found genetic evidence of assortative mating for eight out of fifteen investigated traits. Our third aim is to investigate whether genetic similarity between relatives was increased as predicted for these traits. We found that polygenic index correlations among relatives were increased in a way that broadly corresponded to the theoretical expectations. Trait-specific genetic similarity between partners and elevated genetic similarity between relatives indicate that many of the previously observed phenotypic correlations are partly attributable to assortative mating. Our final aim was to use mother-father-child trios to test whether the observations were consistent with equilibrium. Although some traits did not significantly deviate from equilibrium expectations, psychosocial traits like education attainment did. This would imply that that the genetic variance and genetic similarity between relatives for these traits are still increasing across generations.

Results

Fig. 1 shows a theoretical model of similarity in extended families in the presence of assortative mating at intergenerational equilibrium. The model includes eight individuals (i) in three generations (g): two partners in the first generation, their two children in the second generation (who are each other's full sibling) along with their respective partners, and two children in the third generation (who are each other's first cousin). The phenotype that is assorted on is denoted with P_{ig}, whereas trait-associated additive genetic factors and unique environmental factors are denoted with A_{ig} and E_{ig}, respectively. The genotypic correlation between any two individuals is the sum of all valid chains of paths between their respective additive genetic factors and the value of a single chain is the product of its path coefficients[32,33]. Valid chains always begin by tracing backward ($\leftarrow$) in relation to the direction of arrows, incorporating exactly one double-headed arrow ($\leftrightarrow$), after which tracing continues in a forward direction ($\rightarrow$). Because the variables in Fig. 1 have unit variances, all valid chains connecting a variable to itself will sum to 1, allowing us to immediately trace in a forward direction (i.e., change direction at once). Copaths (—), which are arrowless paths representing associations arising from assortment[34], link together valid chains per the rules above, forming longer, valid chains. For a more detailed description of path tracing rules involving copaths, see Balbona, et al. [35] or Keller, et al. [36].

Expected genotypic correlations in the nuclear family

There is only one valid chain between partners' respective additive genetic factors (e.g., A_{11} and A_{21}): $h \times \mu \times h$. The genotypic correlation between partners (denoted ρ_g) is thus the phenotypic correlation attributable to assortative mating, μ, weighted by the trait's heritability, h^2:

$$\rho_g = \mu h^2 \tag{1}$$

Similarly, we can trace all valid chains between the additive genetic factors of a parent and their offspring (e.g., A_{11} and A_{22}). There are two valid chains: one directly from parental genetic factors to offspring genetic factors, $\frac{1}{2}$, and one through the other parent via the assorted phenotype: $h \times \mu \times h \times \frac{1}{2}$. The genotypic correlation between parent and offspring is therefore $\frac{1}{2} + \frac{h\mu h}{2}$. With no assortative mating ($\mu = 0$), this reduces to $\frac{1}{2}$. For siblings (A_{22} and A_{23}), there are four valid chains: $\frac{1}{4} + \frac{1}{4} + \frac{h\mu h}{4} + \frac{h\mu h}{4}$, which can be rearranged so that it equals the genotypic parent-offspring correlation. Because they are equal, we can define a common denotation (r_{g_1}) for first-degree relatives. We can also substitute $h \times \mu \times h$ with ρ_g giving us:

$$r_{g_1} = \frac{1 + \rho_g}{2} \tag{2}$$

In other words, the genotypic correlation between first-degree relatives, r_{g_1}, is increased by half the genotypic correlation between partners at equilibrium. Note that the phenotypic correlation will not be the same for siblings and parent-offspring despite the same genotypic correlation[3]. An advantage of using path analysis is how easy path diagrams are to expand. In the supplementary information, we detail how including polygenic indices (section 1, 4 and 5) and relaxing the assumption of equilibrium (section 2, 4, and 5) changes the correlations. During

Fig. 1. Path diagram for a model of genetic similarity in extended families under phenotypic assortative mating at intergenerational equilibrium (i.e., equal variance across generations). The partner correlation attributable to assortment is denoted by μ, the recombination variance is denoted by V_K, and h and e denote the effect of additive genetic (A_{ig}) and environmental factors (E_{ig}), respectively, on the phenotype (P_{ig}) of individual i in generation g. All variables have unit variance, meaning $e = \sqrt{1 - h^2}$ and $V_K = \frac{1-\mu h^2}{2}$. See the supplementary information for path diagrams representing disequilibrium and including polygenic indices.

disequilibrium, the true correlation will be less than what equation 2 suggests. For polygenic index correlations, one must include a term representing the imperfect correlation between the polygenic index and the true genetic propensity (Supplementary Fig. 1). The polygenic index correlation between partners should therefore be:

$$\rho_{pgi} = \mu h^2 s^2 \tag{3}$$

where s^2 is the shared variance between the polygenic index and the true additive genetic factor (i.e., the genetic signal). If the genetic signal is low, the polygenic index correlation between partners will be biased towards zero compared to the true genotypic correlation[19]. For first-degree relatives, the equation becomes similarly altered, but because the error terms in the polygenic indices are correlated between relatives, the polygenic index correlation will be biased towards the coefficient of relatedness rather than zero:

$$r_{pgi_1} = \frac{1 + \rho_{pgi}}{2} \tag{4}$$

Expected genotypic correlations in the extended family

The model in Fig. 1 has two properties that allow a general algorithm to find the expected genotypic correlation between any two members in extended families. First, all the chains that connect the genotypes of first-degree relatives can readily be continued without breaking path tracing rules. Second, all chains between the genotypes

Fig. 2. Assortative mating's effect on genotypic correlations between various relatives. **Top**: The expected genotypic correlation (r_g) at equilibrium between (**A**) full siblings (i.e., first-degree relatives) and (**B**) first cousins (i.e., third-degree relatives) under different combinations of assortment strengths (μ) and heritabilities (h^2). **Bottom**: The relative (**C**) and absolute (**D**) increase in genotypic correlation at equilibrium for various relatives and genotypic correlations between partners (p_g). The reproducible code for this figure is available at https://osf.io/dgw4r/.

of any two related individuals are mediated sequentially through the genotypes of first-degree relatives. The genotypic correlation between k^{th}-degree relatives, denoted r_{g_k}, can thus be attained by raising the genotypic correlation between first-degree relatives to the degree of relatedness:

$$r_{g_k} = r_{g_1}^k = \left(\frac{1 + \rho_g}{2} \right)^k \tag{5}$$

For example, the expected genotypic correlation between third-degree relatives like first cousins is $r_{g_1}^3$. This can be verified by manually tracing all valid chains between A_{13} and A_{23} in Fig. 1. The genotypic correlation between non-blood relatives like in-laws, which will be non-zero under assortative mating, can be attained by linking together chains of r_{g_k} and ρ_g (for example, $Corr(A_{12}, A_{42}) = r_{g_1}\rho_g^2$). As for polygenic index correlations, they can be attained by replacing ρ_g with ρ_{pgi} in equation 5 (see supplementary information, section 1).

Fig. 2 shows how assortative mating changes genotypic correlations between relatives at equilibrium. In Panels A and B, it is evident that assortative mating has a much larger effect on first cousins than full siblings. For example,

for a trait where $\mu = .50$ and $h^2 = 50\%$ (meaning $\rho_g = .25$), siblings (Panel A) will have a correlation of $r_{g_1} = .625$ whereas cousins (Panel B) will have a correlation of $r_{g_3} = .244$, reflecting increases of 25% and 95%, respectively, compared to random mating. Panel C shows how this pattern extends to more distant relatives, with the genotypic correlation between second cousins 3.5 times higher than normal if $\rho_g = .25$ ($r_{g_5} = .095$ *vs.* $.031$). The larger relative increase is not merely because the correlations are smaller to begin with: Panel D shows that the largest absolute increase typically occurs in second-degree relatives like uncles/aunts and nephews/nieces.

The relatively greater increase in correlation between cousins is because third-degree relatives are affected by three assortment processes: Mother-father, uncle-aunt, and grandfather-grandmother partnerships are all correlated under assortative mating and contribute to the increased correlation (Fig. 1). For each additional degree of relatedness, there is an additional assortment process opening pathways for relatives to correlate. This pattern extends to unrelated individuals like siblings-in-laws, who would have a genotypic correlation of $\rho_g r_{g_1} = .157$ if $\rho_g = .25$. It is evident that assortative mating has a relatively larger impact on the genotypic correlation between distant relatives compared to close relatives, and that heritable traits subject to strong assortment can produce significant genotypic correlations between family members who would otherwise be virtually uncorrelated.

Empirical polygenic index correlations between partners and relatives

Fig. 3 shows polygenic index correlations between family members for a range of traits. Eight out of fifteen traits were significantly correlated between partners (Panel A), including height (.07), body mass index (.05), intelligence (.04), and educational attainment (.14). When educational attainment was split into cognitive and non-cognitive factors (GWAS-by-subtraction[37]), we find roughly equal partner correlations for both components. Psychiatric traits like ADHD, depression, cross-psychiatric disorder, and bipolar disorder exhibited no significant correlations between partners. Keep in mind that the correlations will be biased downwards to the extent the genetic signal is poor (ref. equation 3).

Panels B, C, and D show polygenic index correlations between full siblings, parents and offspring, and first cousins, respectively (see Supplementary Fig. 9 for other relatives). The vertical dashed lines are the expected correlations under random mating and the black crosses are the expected correlations at equilibrium given the partner correlation. All traits with significant correlations between partners had significantly higher parent-offspring correlations than would be expected under random mating, and we observed similar patterns for higher-degree relatives. For example, the correlation between polygenic indices for educational attainment was 0.56 (instead of 0.50) between full siblings and 0.20 (instead of 0.125) between first cousins.

Testing intergenerational equilibrium

We fitted structural equation models using mother-father-child to see if a model constrained to equal variance across generations (i.e., equilibrium) resulted in significantly worse fit (see supplementary information, section 6). Five out of eight traits were significantly different from equilibrium. We also investigated two consequences of disequilibrium, namely greater variance in the offspring generation (Fig 4A) and smaller-than-expected parent-offspring correlations (Fig. 4B). During disequilibrium, the ratio of offspring polygenic index variance to parental polygenic index variance should be positive: $Q_{pgi} = \frac{Offspring\ Variance}{Parental\ Variance}$ (see supplementary information, section 2 and 4). However, this ratio is quite sensitive to the genetic signal of the polygenic index, and therefore provides

Fig. 3: Polygenic index correlations for various traits between various family members: (**A**) partners, (**B**) full siblings, (**C**) parent-offspring, and (**D**) first cousins. The vertical dashed lines are the expected correlation under random mating (i.e., the coefficient of relatedness), and the black crosses are the expected correlation at equilibrium given equation 5. Abbreviations: EA = educational attainment; BMI = body mass index; IQ = intelligence; ADHD = attention-deficit hyperactivity disorder. Error bars are 95% confidence intervals. The summary statistics and reproducible code for this figure is available at https://osf.io/dgw4r/.

limited information about the history of assortative mating beyond demonstrating disequilibrium. An alternative measure that is less sensitive to the genetic signal is the observed increase in polygenic index correlation as a percentage of the expected increase[19]: $U_{pgi} = \frac{Observed\ Increase}{Expected\ Increase}$ (see supplementary information, section 3 and 5). This provides a measure of how close the trait is to equilibrium. By comparing U_{pgi} to reference values under various heritabilities and assortment strengths, it is possible to infer the equivalent number of generations of stable assortative mating. If the parental generation was the first generation to mate assortatively, we would expect a $U_{pgi} \approx 70\%$, while we would expect $U_{pgi} = 100\%$ if the trait was in equilibrium.

Height and body mass index did not deviate from equilibrium: There was no significant difference between the parental and offspring variance nor between the observed and expected correlations. Psychosocial traits, on the other hand, deviated from equilibrium: For example, the polygenic index variance for educational attainment was 2.4% greater in the offspring generation compared to the parental generation. The true genetic variance ratio is likely much larger: For example, if the polygenic index captures one third of the true genetic factor ($s^2 = 1/3$),

Fig. 4: (**A**) Ratio of offspring polygenic index variance to parental polygenic index variance (Q_{pgi}, see supplementary information, section 2 and 4). A value above 1 would indicate that the variance is greater in the offspring generation compared to the parental generation, as expected during disequilibrium. (**B**) Observed increase in parent-offspring correlation compared to expected increase at equilibrium (U_{pgi}, see supplementary information, section 3 and 5). A value of about 70% would indicate that the parent generation was the first generation to assort on this trait, whereas 100% would indicate that the trait is in intergenerational equilibrium. Only traits with significant correlations between partners are shown. Abbreviations: EA = educational attainment; BMI = body mass index; IQ = intelligence. Error bars are 95% confidence intervals. The summary statistics and reproducible code for this figure is available at https://osf.io/dgw4r/.

then the true variance ratio would be approximately 7.2% (see supplementary information, section 4). The parent-offspring polygenic index correlation was also slightly but significantly lower than expected at equilibrium (U_{pgi} = 90%, 95% CIs: 87–93%), with similar results for the other psychosocial traits. When we compared this to calculations of what the observed increase would have been after successive generations of stable assortment, we found that U_{pgi} = 90% is equivalent to approximately three generations of stable assortative mating (see supplementary information, section 3 and 5).

Discussion

In this study, our goal was to clarify the theoretical consequences of assortative mating on genetic similarity in extended families and assess empirical measures of genetic similarity to provide insights into the presence and history of assortative mating. We first employed path analysis to deduce the expected polygenic index correlations between relatives under assortative mating. We then presented empirical evidence that assortative mating is present for many traits, leading to significantly increased genetic similarity among relatives for those traits. Finally, we showed that – while assortative mating does not appear to be a recent phenomenon for most traits – genetic similarity is still increasing across generations for psychosocial traits. Here, we discuss the implications of our findings.

Aim 1: Theoretical expectations

Our first aim was to clarify the theoretical consequences of assortative mating. Our key finding is the stronger impact of assortative mating on genotypic correlations between more distant relatives. Although not a novel discovery – even Fisher mentioned it offhandedly in his seminal paper[1] – this effect has been largely overlooked in the literature (cf. [29]). This is despite important implications. A Swedish economics paper reported that nearly one-third of persistence in inequality across generations – traditionally attributable to parent-offspring relationships – is attributable to the extended family[38]. Assortative mating's effects on similarity in extended families may be key to understanding these issues. Similar logic may also apply to environmentally mediated sources of similarity[39].

Aim 2: Genetic similarity between partners

The second aim of this study was to investigate which traits show genetic evidence of assortative mating. One key challenge when evaluating the pervasiveness of assortative mating is that phenotypic partner similarity can come about from multiple processes. Genotypic similarity, on the other hand, can more confidently be attributed to assortative mating. Most anthropometric traits and psychosocial traits had significant polygenic index correlations between partners. The largest correlation was for educational attainment (.14), which adds to the growing list of evidence that variants associated with educational attainment is undergoing assortative mating[6,19,23,25,40].

Somewhat surprisingly, psychiatric traits did not show evidence of assortative mating despite pervasive phenotypic partner correlations[15,16]. The findings are in line with a recent study that found no genetic partner similarity on general risk for psychopathology (i.e., the "p-factor")[41]. This could indicate that phenotypic partner similarity are caused by processes other than assortative mating, such as convergence[20]. On the other hand, they could also be false negatives resulting from inadequate polygenic indices. As highlighted in equation 3, the polygenic index correlation between partners should be the product of the phenotypic correlation attributable to assortative mating (μ), the heritability (h^2), and the genetic signal (s^2). If the polygenic index fail to adequately measure the relevant genetic factors (meaning $s^2 \approx 0$), for example due to lack of statistical power or other measurement issues[42] in the underlying genome-wide associations study (GWAS), then the polygenic index correlation will be biased towards zero. The highest observed correlations were for educational attainment and height, which are among the traits with the largest sample sizes in the underlying GWAS. A corollary is that the correlations reported here do not quantify the exact degree of assortative mating because it is confounded by the quality of the polygenic index.

Aim 3: Genetic similarity between relatives

Our third aim was to investigate whether relatives were more genetically similar for traits that exhibit evidence of assortative mating. Our findings broadly correspond to theoretical expectations: Traits with significant polygenic index correlations between partners showed increased similarity between relatives, whereas traits with no correlations between partners broadly exhibit patterns as expected under random mating. These empirical patterns demonstrate the theoretical expectations derived earlier, meaning we should expect distant relatives to be highly correlated for traits under strong assortment. The correlations reported here are underestimated by the quality of the polygenic index, meaning the true genotypic correlations between relatives are likely much larger. Our findings have at least two implications. First, genetic variants associated with traits undergoing assortment, such as educational attainment, cluster in extended families, thus increasing or maintaining societal stratification by families[38] (i.e. between-family variation); and second, genetic studies that unknowingly involve numerous distantly related individuals may be biased if the genotypic correlations between them are not negligible.

Aim 4: Intergenerational equilibrium

Our fourth aim was to investigate the history of assortative mating. Our findings differed across traits: Height and body mass index did not deviate from equilibrium expectations, whereas psychosocial traits such as educational attainment did. This was evident in both lower-than-expected parent-offspring polygenic index correlations and greater variance in the offspring generation. Whether or not a trait is in intergenerational equilibrium has important implications for the consequences of assortative mating because it decides whether differences are increasing across generations or merely maintained. We found that polygenic index variance was stable across generations for height and body mass index (as well as for traits not undergoing assortative mating). However, psychosocial traits have greater variance in the offspring generation, implying that the traits are in disequilibrium and that assortative mating is currently leading to *increased* genetic differences in these traits. Although the non-genetic consequences may differ, assortative mating may therefore play a key role in explaining recent increases in inequality[10,13].

Despite being in disequilibrium, the evidence does not suggest that the parental generation was the first to assort on educational attainment. Instead, it appears that the trait is quite near equilibrium. This would also explain the discrepancy between our conclusion and that in Torvik, et al. [19], who found no significant deviation from equilibrium using an earlier version of data from the same cohort. We attribute the change in result from an increase in statistical power, stemming from more genotyped individuals available in the current sample. In this paper, we estimate that the evidence for educational attainment corresponds to approximately three generations of stable assortative mating, but the exact history of assortment may be longer if the strength of assortment has varied over time or if the heritability increased for other reasons[43].

Methodological implications

Many genetic research methods assume random mating, but our findings suggest that such assumptions are unwarranted for many traits. Accounting for assortative mating poses its own challenges, as the genetic consequences and corresponding methods needed depend on whether assortative mating started recently or has reached intergenerational equilibrium. Studies on the genetics of educational attainment especially – or the many traits that correlate with educational attainment[44] – may therefore be biased unless this is properly accounted for.

Twin and family studies that account for assortative mating typically assume equilibrium[36]. For example, Clark [45] uses equations that assume equilibrium when he claims that familial correlations in social class in the United Kingdom can be explained by genetic similarity alone. Conversely, Kong, et al. [46], who investigated genetic nurture effects of educational attainment in an Icelandic sample, assumed no assortment prior to their parental generation. Our findings imply that, for some traits, neither of these assumptions are valid. Although the patterns and history of assortment may be different across populations, future research should investigate how the conclusions from Kong, et al. [46] and related papers depend on these assumptions[47,48].

Newer genetic methods that can account for disequilibrium are being developed[35]. When these methods are impractical, the potential biases induced by different assumptions must be considered on a case-by-case and method-by-method basis. Different methods will be biased in different ways. For example, assortative mating leads to underestimated heritability in classical twin designs[36,49] and overestimated heritability in molecular designs[50], with the corollary that the missing heritability problem may be larger than previously assumed[51,52]. Overall, researchers must carefully consider what impacts the presence and history of assortative mating would have on their results.

Limitations and future directions

Despite our large sample size, our results are limited by low-quality polygenic indices, which results in lower partner correlations and consequently less power to detect assortative mating. This is amplified for the tests of equilibrium, where smaller polygenic index correlations between partners result in less statistical power to detect deviations from equilibrium. Our tests for equilibrium are therefore less conclusive for traits with small polygenic index correlations, such as smoking.

Another concern is that our results may be confounded by population stratification[53], where (1) the trait in question happens to be more common within certain strata (e.g., subcultures or geographical areas), (2) some genetic variants are randomly present at higher frequencies in these strata, and (3) individuals are more likely to mate within these strata. The combination of the first two phenomena would result in a spurious correlation between those genetic variants and the trait, and when coupled with the third phenomenon, similar spurious correlations could emerge between partners. While we controlled for 20 principal components in our analysis, which is the standard method for addressing stratification[54], this approach may not fully account for this phenomenon[55]. However, the evidence we present aligns well with predictions given assortative mating. It is also not obvious how population stratification could explain increased variance in the offspring generation. Consequently, our results should be considered indicative of assortative mating until a more compelling alternative explanation is offered. Future theoretical work should investigate how the consequences of assortative mating and population stratification differ so that they can better be distinguished in future research.

There are several interesting research avenues that could follow from this work. First, we did not consider shared environmental effects or gene-environment correlations in our models, which may affect the genetic consequences of assortative mating. Second, there may be some selection bias in the cohort study our results are based on. Future work using population-wide phenotypic data might provide insights into how much this matters. Third, patterns of assortative mating are likely to vary between populations[56,57], meaning that our empirical findings may not be universally generalizable. Replicating these results in other populations will therefore be beneficial. Fourth, future

research may want to investigate which phenotypes mediate the polygenic index correlations between partners, as it may not always be attributable to the phenotype that the polygenic index supposedly measures.

Methods

Sample

We used data from the Norwegian Mother, Father and Child Cohort Study (MoBa)[30]. MoBa is a population-based pregnancy cohort study conducted by the Norwegian Institute of Public Health. Participants were recruited from all over Norway from 1999-2008. The women consented to participation in 41% of the pregnancies. Blood samples were obtained from both parents during pregnancy and from mothers and children (umbilical cord) at birth[58]. The cohort includes approximately 114,500 children, 95,200 mothers and 75,200 fathers. The current study is based on version 12 of the quality-assured data files released for research in January 2019. The establishment of MoBa and initial data collection was based on a license from the Norwegian Data Protection Agency and approval from The Regional Committees for Medical and Health Research Ethics. The MoBa cohort is currently regulated by the Norwegian Health Registry Act. The current study was approved by The Regional Committees for Medical and Health Research Ethics (2017/2205).

For the correlations, the sample included 47,135 unique mother-father dyads (i.e., partners) where both had been genotyped and passed quality control [31]. As described in Corfield, et al. [31], relatedness relationships in MoBa were inferred from genetic data by applying KING programs[59] to a subset of single nucleotide polymorphisms (SNPs) with call rate < 98% and minor allele frequency (MAF) < 5%. KING accurately infers monozygotic twin or duplicate pairs (kinship coefficient > 0.3540), first-degree (parent-offspring, full siblings, dizygotic twin pairs; kinship coefficient range 0.1770 - 0.3540), second-degree (half siblings, grandparent-offspring, avuncular relationships; kinship coefficient range 0.0884 – 0.1770), and third-degree (first cousins; kinship coefficient range 0.0442 – 0.0884) relationships. This method identified 117,041 parent-offspring dyads, 22,575 full sibling dyads, 35,923 second-degree dyads (e.g., uncle-nephew), 28,330 third-degree dyads (e.g., first cousins), 9,392 fourth-degree dyads, and 235,209 dyads of unrelated family members (e.g., in-laws, nephews–uncles' spouses, partners, etc.,) where both members of the dyads had been genotyped and passed quality control.

To test equilibrium, we used mother-father-child trios from MoBa. After randomly selecting one offspring from each nuclear family, we were able to construct a sample of 81,145 genotyped mothers, 54,550 genotyped fathers, and 71,544 genotyped offspring, resulting in a total of 93,767 families. Of these, 36,764 were complete trios, whereas 10,371 included only partners, 24,659 included only mother-offspring dyads, and 4,914 included only father-offspring dyads.

Measures

We used beta weights from large, publicly available up-to-date genome-wide association studies listed the supplementary information, section 8. Polygenic indices were calculated using LDPred[60], a Bayesian approach that uses a prior on the expected polygenicity of a trait (assumed fraction of non-zero effect markers) and adjusts for linkage disequilibrium (LD) based on a reference panel to compute SNPs weights. Genotypes were coordinated with the summary statistics, with the number of overlapping SNPs reported in supplementary information, section 8. LD adjustment was performed using the European subsample of the 1000 Genomes genotype data as LD reference panel[61]. The weights were estimated based on the heritability explained by the markers in the GWAS summary statistics and the assumed fraction of markers with non-zero effects. For each GWAS trait we created

LDpred PGI with the –score command in plink2[62]. Prior to calculating correlations between partners and relatives, we residualised the polygenic indices by regressing out the first 20 principal components of genetic ancestry, as well as chip, imputation, and batch number.

Statistics

The polygenic index correlations were attained by correlating the residualised polygenic indices between partners and relatives using *cor.test* in R. 4.0.3[63]. We tested whether the observed correlations were consistent with equilibrium by fitting structural equation models to mother-father-child trio covariance matrices, and testing whether a model constrained to equilibrium via equal variance across generations resulted in significantly worse fit. We describe this procedure in more detail in the supplementary information, section 6.

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